LSTM

November 18, 2023

```
[1]: from sklearn.metrics import mean_squared_error
     from torch.autograd import Variable
     from sklearn.preprocessing import MinMaxScaler
     import numpy as np
     import pandas as pd
     import pandas_datareader as pdr
     import torch
     import torch.nn as nn
     import time
     import seaborn as sns
     import math, time
     import plotly.express as px
     import plotly.graph_objects as go
     import matplotlib
     import matplotlib.pyplot as plt
     import gc
     import plotly.io as pio
     %matplotlib inline
     matplotlib.rcParams['figure.facecolor'] = '#ffffff'
     pio.renderers.default = "notebook_connected"
     pd.options.mode.chained_assignment = None
```

0.1 Download Dataset

C:\Users\ROG\AppData\Roaming\Python\Python310\sitepackages\pandas_datareader\tiingo.py:234: FutureWarning:

In a future version of pandas all arguments of concat except for the argument 'objs' will be keyword-only.

```
dataset_df = pd.read_csv('AAPL.csv')
[4]:
     dataset_df
[4]:
                                                                               open
           symbol
                                           date
                                                   close
                                                            high
                                                                      low
                                                                                    \
     0
              AAPL
                    1980-12-12 00:00:00+00:00
                                                   28.75
                                                           28.87
                                                                    28.75
                                                                             28.750
     1
             AAPL
                    1980-12-15 00:00:00+00:00
                                                   27.25
                                                           27.38
                                                                    27.25
                                                                             27.380
     2
              AAPL
                    1980-12-16 00:00:00+00:00
                                                   25.25
                                                           25.37
                                                                    25.25
                                                                             25.370
     3
              AAPL
                    1980-12-17 00:00:00+00:00
                                                   25.87
                                                           26.00
                                                                    25.87
                                                                             25.870
     4
              AAPL
                    1980-12-18 00:00:00+00:00
                                                   26.63
                                                           26.75
                                                                    26.63
                                                                             26.630
                                                     •••
              AAPL
     10818
                    2023-11-13 00:00:00+00:00
                                                 184.80
                                                          186.03
                                                                   184.21
                                                                           185.820
     10819
              AAPL
                    2023-11-14 00:00:00+00:00
                                                 187.44
                                                          188.11
                                                                   186.30
                                                                           187.700
     10820
              AAPL
                    2023-11-15 00:00:00+00:00
                                                 188.01
                                                          189.50
                                                                   187.78
                                                                           187.845
              AAPL
                    2023-11-16 00:00:00+00:00
                                                 189.71
     10821
                                                          190.96
                                                                   188.65
                                                                            189.570
     10822
              AAPL
                    2023-11-17 00:00:00+00:00
                                                                            190.250
                                                 189.69
                                                          190.38
                                                                   188.57
               volume
                          adjClose
                                        adjHigh
                                                      adjLow
                                                                  adj0pen
                                                                           adjVolume
     0
              2093900
                          0.099568
                                      0.099984
                                                    0.099568
                                                                0.099568
                                                                           469034069
     1
               785200
                          0.094373
                                      0.094823
                                                    0.094373
                                                                0.094823
                                                                           175884975
     2
               472000
                         0.087447
                                      0.087862
                                                    0.087447
                                                                0.087862
                                                                           105728105
     3
               385900
                          0.089594
                                      0.090044
                                                    0.089594
                                                                0.089594
                                                                             86441686
     4
               327900
                          0.092226
                                      0.092642
                                                    0.092226
                                                                0.092226
                                                                             73449673
            43627519
                       184.800000
     10818
                                    186.030000
                                                 184.210000
                                                              185.820000
                                                                             43627519
     10819
             60108378
                       187.440000
                                    188.110000
                                                 186.300000
                                                              187.700000
                                                                             60108378
     10820
             53790499
                       188.010000
                                    189.500000
                                                 187.780000
                                                              187.845000
                                                                             53790499
     10821
             54412915
                       189.710000
                                    190.960000
                                                 188.650000
                                                              189.570000
                                                                             54412915
     10822
            50002825
                       189.690000
                                    190.380000
                                                 188.570000
                                                              190.250000
                                                                             50002825
            divCash
                      splitFactor
     0
                 0.0
                               1.0
     1
                               1.0
                 0.0
     2
                 0.0
                               1.0
     3
                               1.0
                 0.0
     4
                 0.0
                               1.0
                 0.0
                               1.0
     10818
                               1.0
                 0.0
     10819
     10820
                 0.0
                               1.0
     10821
                 0.0
                               1.0
     10822
                 0.0
                               1.0
     [10823 rows x 14 columns]
```

<class 'pandas.core.frame.DataFrame'>

[5]: dataset_df.info()

RangeIndex: 10823 entries, 0 to 10822 Data columns (total 14 columns):

#	Column	Non-Null Count	Dtype	
0	symbol	10823 non-null	object	
1	date	10823 non-null	object	
2	close	10823 non-null	float64	
3	high	10823 non-null	float64	
4	low	10823 non-null	float64	
5	open	10823 non-null	float64	
6	volume	10823 non-null	int64	
7	adjClose	10823 non-null	float64	
8	adjHigh	10823 non-null	float64	
9	adjLow	10823 non-null	float64	
10	adj0pen	10823 non-null	float64	
11	adjVolume	10823 non-null	int64	
12	divCash	10823 non-null	float64	
13	${\tt splitFactor}$	10823 non-null	float64	
<pre>dtypes: float64(10), int64(2), object(2)</pre>				
memory usage: 1.2+ MB				

0.2 Cleaning Dataset

```
[6]: #removing the timestap
dataset_df['date'] = dataset_df['date'].str.split(' ').str[0]
dataset_df.head()
```

```
[6]:
      symbol
                                                             adjClose
                                                                        adjHigh \
                    date close
                                 high
                                         low
                                               open
                                                      volume
              1980-12-12 28.75
                                       28.75
                                              28.75
        AAPL
                                28.87
                                                     2093900
                                                             0.099568
                                                                       0.099984
    1
        AAPL
              1980-12-15 27.25
                                27.38
                                       27.25
                                              27.38
                                                      785200
                                                             0.094373
                                                                       0.094823
    2
        AAPL
              1980-12-16 25.25
                                25.37
                                       25.25
                                              25.37
                                                      472000
                                                             0.087447
                                                                       0.087862
    3
        AAPL
              1980-12-17 25.87
                                26.00
                                       25.87
                                              25.87
                                                      385900
                                                             0.089594
                                                                       0.090044
        AAPL
             1980-12-18 26.63 26.75 26.63
                                              26.63
                                                      327900 0.092226
                                                                       0.092642
                                     divCash
         adjLow
                  adjOpen adjVolume
                                              splitFactor
    0 0.099568 0.099568 469034069
                                         0.0
                                                      1.0
    1 0.094373 0.094823 175884975
                                         0.0
                                                      1.0
    2 0.087447
                 0.087862 105728105
                                         0.0
                                                      1.0
    3 0.089594 0.089594
                           86441686
                                         0.0
                                                      1.0
    4 0.092226 0.092226
                           73449673
                                         0.0
                                                      1.0
```

```
[7]: #resetting index and changing variable type
dataset_df = dataset_df.reset_index()[['date', 'adjClose']]
df_dates = dataset_df.iloc[:,0]
dataset_df['date'] = pd.to_datetime(dataset_df['date'])
dataset_df = dataset_df.set_index('date')
```

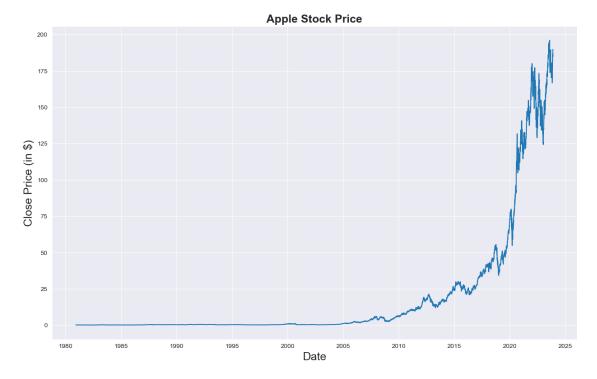
```
dataset_df.head()
```

adjClose

[7]:

```
date
    1980-12-12    0.099568
    1980-12-15    0.094373
    1980-12-16    0.087447
    1980-12-17    0.089594
    1980-12-18    0.092226

[8]: sns.set_style("darkgrid")
    plt.figure(figsize = (15, 9))
    plt.plot(dataset_df[['adjClose']])
    plt.title("Apple Stock Price", fontsize=18, fontweight='bold')
    plt.xlabel('Date', fontsize=18)
    plt.ylabel('Close Price (in $)', fontsize=18)
    plt.show()
```



```
[9]: #array of original prices data
dataset_df_prices = dataset_df['adjClose'].values.reshape(-1,1)
print(dataset_df_prices)
```

[[9.95681294e-02] [9.43732705e-02]

```
[8.74467919e-02]
      [1.88010000e+02]
      [1.89710000e+02]
      [1.89690000e+02]]
[10]: def get_default_device():
          if torch.cuda.is_available():
              return torch.device('cuda')
          else.
              return torch.device('cpu')
      def to device(data, device):
          if isinstance(data, (list,tuple)):
              return [to_device(x, device) for x in data]
          return data.to(device, non_blocking=True)
      def torch_data(data, device):
          return to_device(torch.from_numpy(data).type(torch.Tensor), device)
      device = get_default_device()
      device
[10]: device(type='cpu')
     0.3 Preprocessing Dataset
[11]: def create_sequence(dataset, time_step):
          dataX, dataY = [], []
          for i in range(len(dataset) - time_step -1):
              a = dataset.iloc[i:(i + time_step)]
              dataX.append(a)
              dataY.append(dataset.iloc[i + time step])
          return np.array(dataX), np.array(dataY)
[12]: def curate_dataset(dataset, time_step):
          train size = round(len(dataset) * 0.80)
          remaining_size = len(dataset) - train_size
          val_size = round(0.50 * remaining_size)
          train_data, val_data, test_data = dataset.iloc[0:train_size, :], dataset.
       oiloc[train_size:(train_size + val_size), :], dataset.iloc[(train_size + u
       ⇔val_size):len(dataset), :]
          scaler = MinMaxScaler(feature_range = (0, 1))
          train_data['adjClose'] = scaler.fit_transform(np.

¬array(train_data['adjClose']).reshape(-1, 1))
```

```
val_data['adjClose'] = scaler.transform(np.array(val_data['adjClose']).
Greshape(-1, 1))

test_data['adjClose'] = scaler.transform(np.array(test_data['adjClose']).
Greshape(-1, 1))

X_train, y_train = create_sequence(train_data, time_step)
X_val, y_val = create_sequence(val_data, time_step)
X_test, y_test = create_sequence(test_data, time_step)

X_train = X_train.reshape(X_train.shape[0], X_train.shape[1], 1)
X_val = X_val.reshape(X_val.shape[0], X_val.shape[1], 1)
X_test = X_test.reshape(X_test.shape[0], X_test.shape[1], 1)

y_train = y_train.reshape(y_train.shape[0], 1)
y_val = y_val.reshape(y_val.shape[0], 1)
y_test = y_test.reshape(y_test.shape[0], 1)
return X_train, X_val, X_test, y_train, y_val, y_test, scaler
```

```
[13]: def curate_dataset_test(dataset, time_step):
          train_size = round(len(dataset) * 0.90)
          train_data, test_data = dataset.iloc[0:train_size, :], dataset.
       →iloc[train_size:, :]
          scaler = MinMaxScaler(feature range = (0, 1))
          train_data['adjClose'] = scaler.fit_transform(np.

¬array(train_data['adjClose']).reshape(-1, 1))

          test_data['adjClose'] = scaler.transform(np.array(test_data['adjClose']).
       \negreshape(-1, 1))
          X_train, y_train = create_sequence(train_data, time_step)
          X_test, y_test = create_sequence(test_data, time_step)
          X_train = X_train.reshape(X_train.shape[0], X_train.shape[1], 1)
          X_test = X_test.reshape(X_test.shape[0], X_test.shape[1], 1)
          y_train = y_train.reshape(y_train.shape[0], 1)
          y_test = y_test.reshape(y_test.shape[0], 1)
          return X_train, X_test, y_train, y_test, scaler
```

0.4 Model Architecture (Vanilla RNN)

```
[14]: class RNN_base(nn.Module):
    def __init__(self, input_dim, hidden_dim, layer_dim, output_dim):
        super(RNN_base, self).__init__()
```

```
self.hidden_dim = hidden_dim
              self.layer_dim = layer_dim
              self.rnn = nn.RNN(input_dim, hidden_dim, layer_dim, batch_first = True,_
       →nonlinearity = 'tanh')
              self.fc = nn.Linear(hidden dim, output dim)
          def forward(self, x):
              h0 = Variable(torch.zeros(self.layer_dim, x.size(0), self.hidden_dim,_

device=device))
              out, hn = self.rnn(x, h0)
              out = self.fc(out[:, -1, :])
              return out
[15]: def fit(num_epochs, lr, model, loss_type, opt_func, X_train, y_train):
          optimiser = opt_func(model.parameters(), lr)
          hist = np.zeros(num_epochs)
          start_time = time.time()
          for t in range(num_epochs):
              y_train_pred = model(X_train)
              loss = loss_type(y_train_pred, y_train)
              print("Epoch ", t, "MSE: ", loss.item())
              hist[t] = loss.item()
              optimiser.zero_grad()
              loss.backward()
              optimiser.step()
          training_time = time.time()-start_time
          print("T-time: {}\n".format(training_time))
          return hist, y_train_pred
[16]: def plot_loss(history):
          sns.set_style("darkgrid")
          fig = plt.figure(figsize=(8, 5))
          fig.subplots_adjust(hspace=0.2, wspace=0.2)
          ax = sns.lineplot(data = history, color='royalblue')
          ax.set xlabel("Epoch", size = 14)
          ax.set_ylabel("Loss", size = 14)
          ax.set_title("Training Loss", size = 14, fontweight='bold')
```

```
[17]: def plotly_predictions(results):
          fig = go.Figure()
          fig.add_trace(go.Scatter(go.Scatter(x=results['date'], y=results[0],
                              mode='lines',
                              name='Train prediction',
                              line = dict(color='#ff7f0e'))))
          fig.add_trace(go.Scatter(x=results['date'], y=results[1],
                              mode='lines',
                              name='Test prediction',
                              line = dict(color='#d62728')))
          fig.add_trace(go.Scatter(go.Scatter(x=results['date'], y=results[2],
                              opacity=0.6,
                              mode='lines',
                              name='Actual Value',
                              line = dict(color='#1f77b4'))))
          fig.update_layout(
              xaxis=dict(
                  title_text='Dates',
                  titlefont=dict(
                      family='Rockwell',
                      size=12,
                      color='black',
                  ),
                  showline=True,
                  showgrid=True,
                  showticklabels=True,
                  linecolor='black',
                  linewidth=2,
                  ticks='outside',
                  tickfont=dict(
                      family='Rockwell',
                      size=12,
                      color='black',
                  ),
              ),
              yaxis=dict(
                  title_text='Close (USD)',
                  titlefont=dict(
                      family='Rockwell',
                      size=12,
                      color='black',
                  ),
                  showline=True,
                  showgrid=True,
                  showticklabels=True,
                  linecolor='black',
                  linewidth=2,
```

```
ticks='outside',
        tickfont=dict(
            family='Rockwell',
            size=12,
            color='black',
        ),
    ),
    showlegend=True,
    template = 'plotly_white'
)
annotations = \Pi
annotations.append(dict(xref='paper', yref='paper', x=0.0, y=1.05,
                             xanchor='left', yanchor='bottom',
                             text='Results',
                             font=dict(family='Rockwell',
                                         size=26,
                                         color='black'),
                             showarrow=False))
fig.update_layout(annotations=annotations)
fig.show()
```

```
[18]: def evaluate_model_experiments(model, num_epochs, lr, loss_type, optimiser,
       →time step):
          X_train, X_val, X_test, y_train, y_val, y_test, scaler =_

¬curate_dataset(dataset_df, time_step)
          X_train = torch_data(X_train, device)
          X_val = torch_data(X_val, device)
          X_test = torch_data(X_test, device)
          y_train = torch_data(y_train, device)
          y_val = torch_data(y_val, device)
          y_test = torch_data(y_test, device)
          history, y_train_pred = fit(num_epochs, lr, model, loss_type, optimiser,_
       →X_train, y_train)
          gc.collect()
          torch.cuda.empty_cache()
          y_val_pred = model(X_val)
          y train pred = scaler.inverse transform(y train_pred.cpu().detach().numpy())
          y_train = scaler.inverse_transform(y_train.cpu().detach().numpy())
          y_val_pred = scaler.inverse_transform(y_val_pred.cpu().detach().numpy())
          y_val = scaler.inverse_transform(y_val.cpu().detach().numpy())
```

```
print("======="")
         print('Train Score: %.2f RMSE' % (trainScore))
         print("======="")
         valScore = math.sqrt(mean_squared_error(y_val, y_val_pred))
         print('Validation Score: %.2f RMSE' % (valScore))
         print("======="")
         end_of_time = len(y_train_pred) + len(y_val_pred) + (time_step * 2) + 1
         trainPredictPlot = np.empty_like(dataset_df_prices[0 : end_of_time])
         trainPredictPlot[:, :] = np.nan
         trainPredictPlot[time_step : len(y_train_pred) + time_step, :] =__

    y_train_pred

         valPredictPlot = np.empty_like(dataset_df_prices[0 : end_of_time])
         valPredictPlot[:, :] = np.nan
         valPredictPlot[len(y_train_pred) + (time_step * 2) + 1 : end_of_time, :] =_u

y_val_pred

         original = dataset_df[0 : end_of_time]
         predictions = np.append(trainPredictPlot, valPredictPlot, axis=1)
         predictions = np.append(predictions, original, axis=1)
         result = pd.DataFrame(predictions)
         result = pd.concat([result, df_dates.iloc[0 : end_of_time]], axis = 1)
         metadata = [[time_step, model.layer_dim, model.hidden_dim, trainScore,_
      ⇔valScore]]
         metadata = pd.DataFrame(metadata, columns=['time_step', 'num_layers',_
      return metadata
[19]: def evaluate_single_model(model, num_epochs, lr, loss_type, optimiser,
      →time_step):
         X_train, X_val, X_test, y_train, y_val, y_test, scaler =
      Grate_dataset(dataset_df, time_step)
         X train = torch data(X train, device)
         X_val = torch_data(X_val, device)
         X_test = torch_data(X_test, device)
         y_train = torch_data(y_train, device)
         y_val = torch_data(y_val, device)
         y_test = torch_data(y_test, device)
         history, y_train_pred = fit(num_epochs, lr, model, loss_type, optimiser, u

¬X_train, y_train)
```

trainScore = math.sqrt(mean_squared_error(y_train, y_train_pred))

```
gc.collect()
         torch.cuda.empty_cache()
         y_val_pred = model(X_val)
         y_train_pred = scaler.inverse_transform(y_train_pred.cpu().detach().numpy())
         y_train = scaler.inverse_transform(y_train.cpu().detach().numpy())
         y_val_pred = scaler.inverse_transform(y_val_pred.cpu().detach().numpy())
         y_val = scaler.inverse_transform(y_val.cpu().detach().numpy())
         trainScore = math.sqrt(mean_squared_error(y_train, y_train_pred))
         print("========"")
         print('Train Score: %.2f RMSE' % (trainScore))
         print("=======")
         valScore = math.sqrt(mean_squared_error(y_val, y_val_pred))
         print('Validation Score: %.2f RMSE' % (valScore))
         print("======="")
         end_of_time = len(y_train_pred) + len(y_val_pred) + (time_step * 2) + 1
         trainPredictPlot = np.empty_like(dataset_df_prices[0 : end_of_time])
         trainPredictPlot[:, :] = np.nan
         trainPredictPlot[time_step : len(y_train_pred) + time_step, :] =__

y_train_pred

         valPredictPlot = np.empty_like(dataset_df_prices[0 : end_of_time])
         valPredictPlot[:, :] = np.nan
         valPredictPlot[len(y_train_pred) + (time_step * 2) + 1 : end_of_time, :] =__
       →y_val_pred
         original = dataset_df[0 : end_of_time]
         predictions = np.append(trainPredictPlot, valPredictPlot, axis=1)
         predictions = np.append(predictions, original, axis=1)
         result = pd.DataFrame(predictions)
         result = pd.concat([result, df_dates.iloc[0 : end_of_time]], axis = 1)
         plot_loss(history)
         plotly_predictions(result)
         return None
[20]: def test_final_model(model, num_epochs, lr, loss_type, optimiser, time_step):
         X_train, X_test, y_train, y_test, scaler = curate_dataset_test(dataset_df,__
       →time step)
```

X_train = torch_data(X_train, device)
X_test = torch_data(X_test, device)
y_train = torch_data(y_train, device)
y_test = torch_data(y_test, device)

```
history, y_train_pred = fit(num_epochs, lr, model, loss_type, optimiser,__
→X_train, y_train)
  gc.collect()
  torch.cuda.empty cache()
  y_test_pred = model(X_test)
  y_train_pred = scaler.inverse_transform(y_train_pred.cpu().detach().numpy())
  y_train = scaler.inverse_transform(y_train.cpu().detach().numpy())
  y_test_pred = scaler.inverse_transform(y_test_pred.cpu().detach().numpy())
  y_test = scaler.inverse_transform(y_test.cpu().detach().numpy())
  trainScore = math.sqrt(mean_squared_error(y_train, y_train_pred))
  print("======"")
  print('Train Score: %.2f RMSE' % (trainScore))
  print("======="")
  testScore = math.sqrt(mean_squared_error(y_test, y_test_pred))
  print('Test Score: %.2f RMSE' % (testScore))
  print("======"")
  end_of_time = len(y_train_pred) + len(y_test_pred) + (time_step * 2) + 1
  trainPredictPlot = np.empty_like(dataset_df_prices[0 : end_of_time])
  trainPredictPlot[:, :] = np.nan
  trainPredictPlot[time_step : len(y_train_pred) + time_step, :] =__

y_train_pred

  testPredictPlot = np.empty_like(dataset_df_prices[0 : end_of_time])
  testPredictPlot[:, :] = np.nan
  testPredictPlot[len(y_train_pred) + (time_step * 2) + 1 : end_of_time, :]__

y_test_pred

  original = dataset_df[0 : end_of_time]
  predictions = np.append(trainPredictPlot, testPredictPlot, axis=1)
  predictions = np.append(predictions, original, axis=1)
  result = pd.DataFrame(predictions)
  result = pd.concat([result, df_dates.iloc[0 : end_of_time]], axis = 1)
  plot loss(history)
  plotly_predictions(result)
  return None
```

0.5 Vanilla RNN

0.6 Model Architecture (Vanilla RNN with ReLU)

0.7 Vanilla RNN with ReLU

```
[23]: input_dim = 1
hidden_dim = 1
num_layers = 1
output_dim = 1
```

```
num_epochs = 100
lr = 0.01
loss_type = torch.nn.MSELoss(reduction='mean')
optimiser = torch.optim.Adam
time_step = 20
torch.manual_seed(42)
relu_rnn = RNN_relu(input_dim = input_dim, hidden_dim = hidden_dim, output_dim_
 →= output_dim, layer_dim = num_layers)
relu_rnn = to_device(relu_rnn, device)
evaluate_single_model(relu_rnn, num_epochs, lr, loss_type, optimiser, time_step)
Epoch 0 MSE: 0.8626009821891785
Epoch 1 MSE: 0.6538116931915283
Epoch 2 MSE: 0.4951014816761017
Epoch 3 MSE: 0.3755500018596649
Epoch 4 MSE: 0.2861906588077545
Epoch 5 MSE: 0.21986396610736847
Epoch 6 MSE: 0.17097650468349457
Epoch 7 MSE: 0.13522690534591675
Epoch 8 MSE: 0.1093410849571228
Epoch 9 MSE: 0.09084150195121765
Epoch 10 MSE: 0.07785815000534058
Epoch 11 MSE: 0.06897977739572525
Epoch 12 MSE: 0.0631399005651474
Epoch 13 MSE: 0.05953085795044899
Epoch 14 MSE: 0.057539667934179306
Epoch 15 MSE:
               0.056700270622968674
Epoch 16 MSE: 0.05665802210569382
Epoch 17 MSE: 0.05714334174990654
Epoch 18 MSE: 0.057951975613832474
Epoch 19 MSE: 0.05893015116453171
Epoch 20 MSE: 0.05996333435177803
Epoch 21 MSE:
               0.06096770614385605
Epoch 22 MSE:
               0.06188347190618515
Epoch 23 MSE:
               0.06266980618238449
Epoch 24 MSE:
               0.06330068409442902
Epoch 25 MSE:
               0.06376182287931442
Epoch 26 MSE:
               0.06404796987771988
Epoch 27 MSE: 0.06416090577840805
Epoch 28 MSE:
               0.0641077533364296
Epoch 29 MSE:
               0.06389957666397095
Epoch 30 MSE:
               0.06355028599500656
Epoch 31 MSE:
               0.06307563930749893
Epoch 32 MSE:
               0.06249261647462845
Epoch 33 MSE: 0.06181862950325012
```

Epoch 34 MSE: 0.061071161180734634

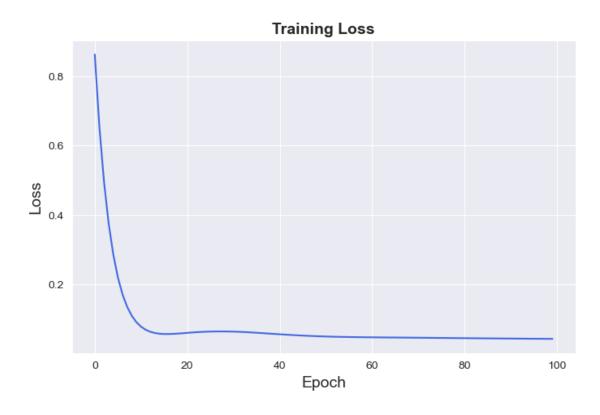
```
35 MSE:
Epoch
                0.060267239809036255
Epoch
       36 MSE:
                0.059423189610242844
Epoch
       37 MSE:
                0.05855433642864227
       38 MSE:
Epoch
                0.057674769312143326
Epoch
       39 MSE:
                0.056797269731760025
Epoch
       40 MSE:
                0.0559331439435482
Epoch
       41 MSE:
                0.0550922155380249
Epoch
       42 MSE:
                0.054282769560813904
Epoch 43 MSE:
                0.05351156368851662
Epoch
       44 MSE:
                0.052783891558647156
       45 MSE:
Epoch
                0.05210358649492264
Epoch
      46 MSE:
                0.05147317051887512
Epoch
      47 MSE:
                0.050893913954496384
Epoch
       48 MSE:
                0.05036596208810806
Epoch
      49 MSE:
                0.04988844320178032
Epoch 50 MSE:
                0.04945962876081467
Epoch
      51 MSE:
                0.04907705634832382
       52 MSE:
Epoch
                0.04873766377568245
Epoch
       53 MSE:
                0.04843795672059059
Epoch
       54 MSE:
                0.04817410930991173
Epoch
       55 MSE:
                0.047942087054252625
Epoch 56 MSE:
                0.047737814486026764
Epoch 57 MSE:
                0.04755723476409912
Epoch 58 MSE:
                0.04739641770720482
Epoch
       59 MSE:
                0.047251634299755096
Epoch
       60 MSE:
                0.04711943492293358
       61 MSE:
Epoch
                0.04699669033288956
Epoch
       62 MSE:
                0.04688062518835068
       63 MSE:
Epoch
                0.04676882550120354
Epoch
       64 MSE:
                0.046659283339977264
       65 MSE:
Epoch
                0.046550359576940536
Epoch
       66 MSE:
                0.04644076153635979
       67 MSE:
                0.0463295616209507
Epoch
       68 MSE:
Epoch
                0.046216126531362534
Epoch
       69 MSE:
                0.04610009491443634
Epoch
       70 MSE:
                0.04598134011030197
Epoch
      71 MSE:
                0.045859940350055695
Epoch
      72 MSE:
                0.04573613777756691
Epoch 73 MSE:
                0.04561026766896248
Epoch
      74 MSE:
                0.04548276960849762
Epoch 75 MSE:
                0.045354120433330536
Epoch
      76 MSE:
                0.045224837958812714
Epoch
       77 MSE:
                0.04509541392326355
Epoch
      78 MSE:
                0.044966332614421844
Epoch
       79 MSE:
                0.044838037341833115
Epoch
       80 MSE:
                0.0447109192609787
Epoch
       81 MSE:
                0.04458531364798546
       82 MSE:
Epoch
                0.04446149617433548
```

Epoch 83 MSE: 0.04433968663215637 Epoch 84 MSE: 0.04422002285718918Epoch 85 MSE: 0.044102609157562256 Epoch 86 MSE: 0.04398748651146889 Epoch 87 MSE: 0.043874647468328476 Epoch 88 MSE: 0.04376406595110893 Epoch 89 MSE: 0.04365566000342369 Epoch 90 MSE: 0.043549321591854095 Epoch 91 MSE: 0.04344496130943298 Epoch 92 MSE: 0.04334244132041931 Epoch 93 MSE: 0.04324163869023323 Epoch 94 MSE: 0.04314242675900459 Epoch 95 MSE: 0.04304467514157295 Epoch 96 MSE: 0.04294827952980995 Epoch 97 MSE: 0.042853135615587234 Epoch 98 MSE: 0.042759139090776443 Epoch 99 MSE: 0.04266621917486191

T-time: 0.8902041912078857

Train Score: 6.16 RMSE

-----Validation Score: 35.55 RMSE



0.8 Hyperparameters Tuning

```
[24]: input_dim = 1
     output_dim = 1
     num_epochs = 100
     lr = 0.01
     loss_type = torch.nn.MSELoss(reduction = 'mean')
     optimiser = torch.optim.Adam
     num_layers = [1, 2]
     sliding_windows = [20, 30, 50, 100]
     hidden_dims = [2, 4, 8, 16, 32]
     tanh_results = []
     relu_results = []
     for time_step in sliding_windows:
         for hidden dim in hidden dims:
             for layers in num_layers:
                 print("======="")
                print("Time Step =", time_step, "| Hidden States =", hidden_dim, "|
      →Num Layers =", layers)
                 print("========"")
                print()
                torch.manual seed(42)
                 tanh_rnn = RNN_base(input_dim = input_dim, hidden_dim = hidden_dim,_
      output_dim = output_dim, layer_dim = layers)
                 tanh_rnn = to_device(tanh_rnn, device)
                 tanh_res = evaluate_model_experiments(tanh_rnn, num_epochs, lr,_
      ⇔loss_type, optimiser, time_step)
                tanh results += [tanh res.iloc[0]]
                print()
                torch.manual_seed(42)
                 relu_rnn_exp = RNN_relu(input_dim = input_dim, hidden_dim =_
       hidden_dim, output_dim = output_dim, layer_dim = layers)
                 relu rnn exp = to device(relu rnn exp, device)
                 relu_res = evaluate_model_experiments(relu_rnn_exp, num_epochs, lr,_
      ⇔loss_type, optimiser, time_step)
                 relu_results += [relu_res.iloc[0]]
                print()
```

Time Step = 20 | Hidden States = 2 | Num Layers = 1

Epoch	O MSE:	0.3117377460002899
Epoch	1 MSE:	0.2746148705482483
Epoch	2 MSE:	0.24029582738876343
Epoch	3 MSE:	0.2088046669960022
Epoch	4 MSE:	0.18011356890201569
Epoch	5 MSE:	0.15414702892303467
Epoch	6 MSE:	0.13079072535037994
Epoch	7 MSE:	0.10990475863218307
Epoch	8 MSE:	0.09133993089199066
Epoch	9 MSE:	0.07495430111885071
Epoch	10 MSE:	0.06062619760632515
Epoch	11 MSE:	0.0482601523399353
Epoch	12 MSE:	0.03778504580259323
Epoch	13 MSE:	0.029145292937755585
Epoch	14 MSE:	0.022287432104349136
Epoch	15 MSE:	0.017145032063126564
Epoch	16 MSE:	0.013624034821987152
Epoch	17 MSE:	0.011590245179831982
Epoch	18 MSE:	0.010860525071620941
Epoch	19 MSE:	0.011199633590877056
Epoch	20 MSE:	0.012325135990977287
Epoch	21 MSE:	0.013922504149377346
Epoch	22 MSE:	0.01567043736577034
Epoch	23 MSE:	0.017272917553782463
Epoch	24 MSE:	0.018491139635443687
Epoch	25 MSE:	0.019167141988873482
Epoch	26 MSE:	0.019233496859669685
Epoch	27 MSE:	0.018707819283008575
Epoch	28 MSE:	0.017675455659627914
Epoch	29 MSE:	0.016265716403722763
Epoch	30 MSE:	0.014627196826040745
Epoch	31 MSE:	0.012906101532280445
Epoch	32 MSE:	0.0112299844622612
Epoch	33 MSE:	0.00969753973186016
Epoch	34 MSE:	0.008374340832233429
Epoch	35 MSE:	0.007293331902474165
Epoch	36 MSE:	0.006458870600908995
Epoch	37 MSE:	0.005852764938026667
Epoch	38 MSE:	0.005441170185804367
Epoch	39 MSE:	0.0051812585443258286
Epoch	40 MSE:	0.005027052015066147
Epoch	41 MSE:	0.004934088326990604
Epoch	42 MSE:	0.004862802103161812
Epoch	43 MSE:	0.004780729301273823
Epoch	44 MSE:	0.0046636853367090225
Epoch	45 MSE:	0.004496104083955288

```
Epoch
       46 MSE:
                0.004270744509994984
Epoch
       47 MSE:
                0.003987906035035849
Epoch
       48 MSE:
                0.00365428626537323
       49 MSE:
Epoch
                0.0032815926242619753
Epoch
       50 MSE:
                0.0028849891386926174
Epoch
       51 MSE:
                0.0024814587086439133
Epoch
       52 MSE:
                0.002088163746520877
Epoch
       53 MSE:
                0.0017209150828421116
Epoch 54 MSE:
                0.0013928103726357222
Epoch
       55 MSE:
                0.001113177859224379
       56 MSE:
                0.0008869089651852846
Epoch
Epoch
       57 MSE:
                0.0007142574759200215
Epoch
       58 MSE:
                0.0005911331390962005
Epoch
       59 MSE:
                0.0005098793189972639
Epoch
       60 MSE:
                0.00046043048496358097
Epoch
      61 MSE:
                0.00043171283323317766
Epoch
       62 MSE:
                0.00041307733044959605
       63 MSE:
Epoch
                0.0003955672145821154
Epoch
       64 MSE:
                0.0003728352312464267
Epoch
       65 MSE:
                0.00034157687332481146
Epoch
       66 MSE:
                0.00030148058431223035
Epoch
       67 MSE:
                0.0002547134936321527
       68 MSE:
Epoch
                0.00020510681497398764
       69 MSE:
Epoch
                0.00015719386283308268
       70 MSE:
                0.00011528654431458563
Epoch
Epoch
      71 MSE:
                8.273294224636629e-05
       72 MSE:
Epoch
                6.144928920548409e-05
Epoch
      73 MSE:
                5.1759907364612445e-05
      74 MSE:
Epoch
                5.251675975159742e-05
Epoch 75 MSE:
                6.143575592432171e-05
Epoch 76 MSE:
                7.555991760455072e-05
Epoch
      77 MSE:
                9.175587183563039e-05
Epoch
      78 MSE:
                0.00010716305405367166
       79 MSE:
                0.00011953746434301138
Epoch
Epoch
       80 MSE:
                0.0001274529640795663
Epoch
       81 MSE:
                0.00013035847223363817
Epoch
       82 MSE:
                0.0001285011530853808
Epoch
       83 MSE:
                0.0001227488974109292
       84 MSE:
Epoch
                0.00011435322812758386
Epoch
       85 MSE:
                0.00010469750850461423
       86 MSE:
Epoch
                9.506429341854528e-05
       87 MSE:
Epoch
                8.646068454254419e-05
Epoch
       88 MSE:
                7.951490260893479e-05
Epoch
       89 MSE:
                7.444860966643319e-05
Epoch
       90 MSE:
                7.112261664588004e-05
Epoch
       91 MSE:
                6.913165270816535e-05
Epoch
       92 MSE:
                6.792864587623626e-05
       93 MSE:
Epoch
                6.695143383694813e-05
```

Epoch 94 MSE: 6.572956044692546e-05 Epoch 95 MSE: 6.395686068572104e-05 Epoch 96 MSE: 6.15210083196871e-05 Epoch 97 MSE: 5.8493082178756595e-05 Epoch 98 MSE: 5.5085391068132594e-05 Epoch 99 MSE: 5.159010834177025e-05

T-time: 1.8453047275543213

Train Score: 0.21 RMSE

-----Validation Score: 7.19 RMSE

Epoch 0 MSE: 0.3827359974384308 Epoch 1 MSE: 0.3520311713218689 Epoch 2 MSE: 0.32390904426574707 Epoch 3 MSE: 0.2981649339199066 Epoch 4 MSE: 0.27455583214759827 Epoch 5 MSE: 0.25288188457489014 Epoch 6 MSE: 0.23295852541923523 Epoch 7 MSE: 0.21464243531227112 Epoch 8 MSE: 0.1978011131286621 Epoch 9 MSE: 0.18231302499771118 Epoch 10 MSE: 0.16807158291339874 Epoch 11 MSE: 0.1549799144268036 Epoch 12 MSE: 0.14294840395450592 Epoch 13 MSE: 0.13189317286014557 Epoch 14 MSE: 0.12173602730035782 Epoch 15 MSE: 0.11251281201839447 Epoch 16 MSE: 0.10683837532997131 Epoch 17 MSE: 0.10185562819242477 Epoch 18 MSE: 0.0972844660282135 Epoch 19 MSE: 0.09301668405532837 Epoch 20 MSE: 0.08900274336338043 Epoch 21 MSE: 0.08521147072315216 Epoch 22 MSE: 0.08161132037639618 Epoch 23 MSE: 0.07817497104406357 Epoch 24 MSE: 0.074886754155159 Epoch 25 MSE: 0.07173069566488266 Epoch 26 MSE: 0.06869389116764069 Epoch 27 MSE: 0.06576559692621231 Epoch 28 MSE: 0.06293129175901413 Epoch 29 MSE: 0.06017298251390457 Epoch 30 MSE: 0.05747758224606514 Epoch 31 MSE: 0.05482881888747215 Epoch 32 MSE: 0.052210211753845215 Epoch 33 MSE: 0.04961252957582474

```
Epoch
       34 MSE:
                0.047029681503772736
Epoch
       35 MSE:
                0.044454678893089294
       36 MSE:
Epoch
                0.041884973645210266
       37 MSE:
Epoch
                0.0393255241215229
Epoch
       38 MSE:
                0.03678921237587929
Epoch
       39 MSE:
                0.034300755709409714
Epoch
       40 MSE:
                0.03191641718149185
Epoch
      41 MSE:
                0.02969357557594776
Epoch 42 MSE:
                0.028323451057076454
Epoch
       43 MSE:
                0.027018167078495026
Epoch
       44 MSE:
                0.025080803781747818
Epoch 45 MSE:
                0.02265768125653267
Epoch
      46 MSE:
                0.020739207044243813
Epoch
       47 MSE:
                0.019182784482836723
Epoch
      48 MSE:
                0.017726972699165344
Epoch 49 MSE:
                0.016350198537111282
Epoch
      50 MSE:
                0.015056292526423931
       51 MSE:
Epoch
                0.01385438907891512
Epoch
       52 MSE:
                0.012753626331686974
Epoch
       53 MSE:
                0.01176621112972498
Epoch
       54 MSE:
                0.01089926902204752
Epoch 55 MSE:
                0.010146772488951683
Epoch 56 MSE:
                0.009485400281846523
Epoch 57 MSE:
                0.008878180757164955
Epoch
       58 MSE:
                0.008289242163300514
Epoch
       59 MSE:
                0.007702012080699205
       60 MSE:
Epoch
                0.007124858442693949
Epoch
       61 MSE:
                0.006580339279025793
       62 MSE:
Epoch
                0.006089876871556044
Epoch
      63 MSE:
                0.005661685485392809
Epoch
       64 MSE:
                0.0052896165288984776
Epoch
       65 MSE:
                0.004957614466547966
Epoch
       66 MSE:
                0.004647092893719673
       67 MSE:
                0.004343724809587002
Epoch
Epoch
       68 MSE:
                0.004041047766804695
Epoch
       69 MSE:
                0.0037405428010970354
Epoch
      70 MSE:
                0.003448688890784979
Epoch
      71 MSE:
                0.00317455199547112
      72 MSE:
Epoch
                0.002923700027167797
Epoch
      73 MSE:
                0.0026991108898073435
Epoch 74 MSE:
                0.0024961994495242834
Epoch
      75 MSE:
                0.002305493922904134
Epoch
       76 MSE:
                0.0021182100754231215
      77 MSE:
Epoch
                0.0019312226213514805
Epoch
       78 MSE:
                0.0017489787423983216
Epoch
       79 MSE:
                0.0015777562512084842
Epoch
       80 MSE:
                0.0014215982519090176
       81 MSE:
                0.001281876233406365
Epoch
```

```
Epoch 82 MSE: 0.0011569602647796273
Epoch 83 MSE: 0.0010438221506774426
Epoch 84 MSE:
               0.0009400132694281638
Epoch 85 MSE:
               0.0008441716199740767
Epoch 86 MSE:
               0.0007566206040792167
Epoch 87 MSE:
               0.000679206452332437
Epoch 88 MSE:
               0.0006130092078819871
Epoch 89 MSE:
               0.0005631667445413768
Epoch 90 MSE:
               0.0005560519639402628
Epoch 91 MSE:
               0.0005452704499475658
Epoch 92 MSE:
               0.0005018326919525862
Epoch 93 MSE:
               0.0004423184727784246
Epoch 94 MSE:
               0.0003954576386604458
Epoch 95 MSE:
               0.0003737170191016048
Epoch 96 MSE:
               0.00035890069557353854
Epoch 97 MSE:
               0.0003344895667396486
Epoch 98 MSE:
               0.0003006292972713709
Epoch 99 MSE:
               0.0002652383700478822
```

T-time: 1.5774409770965576

Train Score: 0.49 RMSE

Validation Score: 1.16 RMSE

Time Step = 20 | Hidden States = 2 | Num Layers = 2

Epoch 0 MSE: 0.3221622407436371 Epoch 1 MSE: 0.27891892194747925 Epoch 2 MSE: 0.24024921655654907 Epoch 3 MSE: 0.20576758682727814 Epoch 4 MSE: 0.17484527826309204 Epoch 5 MSE: 0.14685076475143433 Epoch 6 MSE: 0.12144927680492401 Epoch 7 MSE: 0.09863541275262833 Epoch 8 MSE: 0.07859832048416138 Epoch 9 MSE: 0.061599843204021454 Epoch 10 MSE: 0.04789050295948982 Epoch 11 MSE: 0.037643350660800934 Epoch 12 MSE: 0.03089490532875061 Epoch 13 MSE: 0.027493031695485115 Epoch 14 MSE: 0.027059728279709816 Epoch 15 MSE: 0.028982290998101234 Epoch 16 MSE: 0.03245070204138756 Epoch 17 MSE: 0.036555781960487366

```
Epoch
       18 MSE:
                0.04043719545006752
Epoch
       19 MSE:
                0.0434299036860466
Epoch
      20 MSE:
                0.04514726623892784
      21 MSE:
Epoch
                0.04548101872205734
Epoch
      22 MSE:
                0.04454479366540909
Epoch
      23 MSE:
                0.04259803518652916
Epoch
      24 MSE:
                0.039973512291908264
Epoch
      25 MSE:
                0.037017956376075745
Epoch 26 MSE:
                0.034047406166791916
Epoch
      27 MSE:
                0.03131736069917679
      28 MSE:
Epoch
                0.029006430879235268
      29 MSE:
Epoch
                0.027212565764784813
Epoch
       30 MSE:
                0.025959370657801628
       31 MSE:
Epoch
                0.02520977519452572
Epoch
      32 MSE:
                0.02488354966044426
Epoch 33 MSE:
                0.024875450879335403
Epoch
       34 MSE:
                0.02507156692445278
      35 MSE:
Epoch
                0.025362376123666763
Epoch
       36 MSE:
                0.025652095675468445
Epoch
       37 MSE:
                0.02586441859602928
Epoch
       38 MSE:
                0.025945212692022324
       39 MSE:
Epoch
                0.025862837210297585
Epoch 40 MSE:
                0.025606654584407806
Epoch 41 MSE:
                0.025184307247400284
Epoch
      42 MSE:
                0.024618078023195267
Epoch
      43 MSE:
                0.02394074946641922
Epoch 44 MSE:
                0.023191148415207863
Epoch
       45 MSE:
                0.022409707307815552
      46 MSE:
Epoch
                0.021634234115481377
Epoch 47 MSE:
                0.020896179601550102
Epoch 48 MSE:
                0.020217759534716606
Epoch
       49 MSE:
                0.019610103219747543
      50 MSE:
Epoch
                0.019072722643613815
      51 MSE:
                0.018594397231936455
Epoch
Epoch
       52 MSE:
                0.018155382946133614
Epoch
      53 MSE:
                0.01773076131939888
Epoch
       54 MSE:
                0.017294446006417274
Epoch 55 MSE:
                0.016823288053274155
      56 MSE:
Epoch
                0.016300613060593605
Epoch 57 MSE:
                0.01571863703429699
Epoch 58 MSE:
                0.015079392120242119
       59 MSE:
Epoch
                0.014393958263099194
Epoch
       60 MSE:
                0.013680252246558666
       61 MSE:
Epoch
                0.012959697283804417
Epoch
      62 MSE:
                0.012253446504473686
Epoch
       63 MSE:
                0.011578774079680443
Epoch
       64 MSE:
                0.010946273803710938
       65 MSE:
Epoch
                0.010358346626162529
```

```
Epoch 66 MSE:
               0.009809304028749466
Epoch 67 MSE:
               0.009287075139582157
Epoch 68 MSE:
               0.008776305243372917
Epoch 69 MSE:
               0.008262296207249165
Epoch 70 MSE:
               0.007734960410743952
Epoch 71 MSE:
               0.007191913202404976
Epoch 72 MSE:
               0.006639763247221708
Epoch 73 MSE:
               0.006093134637922049
Epoch 74 MSE:
               0.005571344867348671
Epoch 75 MSE:
               0.005093524232506752
Epoch 76 MSE:
               0.004673514980822802
Epoch 77 MSE:
               0.004316309001296759
Epoch 78 MSE:
               0.004017437808215618
Epoch 79 MSE:
               0.0037658566143363714
Epoch 80 MSE:
               0.0035493304021656513
Epoch 81 MSE:
               0.0033600018359720707
Epoch 82 MSE:
               0.0031973563600331545
               0.003066812874749303
Epoch 83 MSE:
Epoch 84 MSE:
               0.0029744331259280443
Epoch 85 MSE:
               0.0029206627514213324
Epoch
      86 MSE:
               0.00289706839248538
Epoch 87 MSE:
               0.002888555871322751
Epoch 88 MSE:
               0.0028800389263778925
Epoch 89 MSE:
               0.0028632411267608404
Epoch 90 MSE:
               0.0028389468789100647
Epoch 91 MSE:
               0.0028133755549788475
Epoch 92 MSE:
               0.0027916315011680126
Epoch 93 MSE:
               0.0027730974834412336
Epoch 94 MSE:
               0.002751774387434125
Epoch 95 MSE:
               0.002720651915296912
Epoch 96 MSE:
               0.002676458563655615
Epoch 97 MSE:
               0.0026214260142296553
Epoch 98 MSE:
               0.0025613214820623398
Epoch 99 MSE:
               0.0025016984436661005
T-time: 3.0339999198913574
```

Train Score: 1.49 RMSE

-----Validation Score: 18.72 RMSE

Epoch 0 MSE: 0.297961562871933 Epoch 1 MSE: 0.2620787024497986 Epoch 2 MSE: 0.22657398879528046 Epoch 3 MSE: 0.19166314601898193 Epoch 4 MSE: 0.15771439671516418 Epoch 5 MSE: 0.12510862946510315

```
Epoch
       6 MSE:
               0.0942835658788681
Epoch
       7 MSE:
               0.0647982805967331
       8 MSE:
Epoch
               0.03800031915307045
Epoch
       9 MSE:
               0.0169442817568779
Epoch
       10 MSE:
                0.003862029640004039
Epoch
       11 MSE:
                0.00140914146322757
Epoch
       12 MSE:
                0.010696016252040863
Epoch
       13 MSE:
                0.02509397268295288
Epoch 14 MSE:
                0.03394744545221329
Epoch
       15 MSE:
                0.03447912260890007
       16 MSE:
Epoch
                0.029230255633592606
       17 MSE:
Epoch
                0.02174612693488598
Epoch
       18 MSE:
                0.01459302008152008
Epoch
       19 MSE:
                0.009079720824956894
Epoch
       20 MSE:
                0.005616957787424326
Epoch
       21 MSE:
                0.004040262196213007
Epoch
       22 MSE:
                0.003921796102076769
       23 MSE:
                0.004766523838043213
Epoch
Epoch
       24 MSE:
                0.006102390121668577
Epoch
       25 MSE:
                0.0075308093801140785
Epoch
       26 MSE:
                0.00871251430362463
       27 MSE:
Epoch
                0.009517575614154339
Epoch
       28 MSE:
                0.009908189065754414
       29 MSE:
Epoch
                0.009894216433167458
Epoch
       30 MSE:
                0.009522398002445698
Epoch
       31 MSE:
                0.00886671245098114
       32 MSE:
Epoch
                0.008017515763640404
Epoch
       33 MSE:
                0.007071839179843664
       34 MSE:
Epoch
                0.006123715080320835
Epoch
       35 MSE:
                0.005255219992250204
Epoch
       36 MSE:
                0.004528507124632597
Epoch
       37 MSE:
                0.0039809513837099075
Epoch
       38 MSE:
                0.003621883923187852
Epoch
       39 MSE:
                0.0034342228900641203
Epoch
       40 MSE:
                0.0033777186181396246
Epoch
       41 MSE:
                0.0033957213163375854
Epoch
       42 MSE:
                0.0034263411071151495
Epoch
       43 MSE:
                0.0034233403857797384
       44 MSE:
Epoch
                0.0033719725906848907
Epoch
       45 MSE:
                0.0032204221934080124
      46 MSE:
                0.0029349145479500294
Epoch
Epoch
       47 MSE:
                0.0025379061698913574
Epoch
       48 MSE:
                0.0020859644282609224
       49 MSE:
Epoch
                0.00164602801669389
Epoch
       50 MSE:
                0.0012731541646644473
Epoch
       51 MSE:
                0.0009978474117815495
Epoch
       52 MSE:
                0.0008176950505003333
       53 MSE:
                0.000711524102371186
Epoch
```

```
Epoch 54 MSE:
                0.0006545609212480485
Epoch 55 MSE:
                0.0006212094449438155
Epoch 56 MSE:
                0.0005891569890081882
Epoch
      57 MSE:
                0.000542834575753659
Epoch
      58 MSE:
                0.0004755063564516604
Epoch
      59 MSE:
                0.00038917287020012736
Epoch
       60 MSE:
                0.0002922018466051668
Epoch 61 MSE:
                0.00019854499259963632
Epoch 62 MSE:
                0.00012452858209144324
Epoch
      63 MSE:
                8.281521149910986e-05
      64 MSE:
Epoch
                7.827435183571652e-05
Epoch 65 MSE:
                0.00010480501805432141
Epoch
      66 MSE:
                0.00014817748160567135
       67 MSE:
Epoch
                0.00019119908392895013
Epoch
      68 MSE:
                0.00021953794930595905
Epoch 69 MSE:
                0.00022618952789343894
Epoch 70 MSE:
                0.00021272036246955395
Epoch 71 MSE:
                0.00018725702830124646
Epoch 72 MSE:
                0.00016031693667173386
Epoch 73 MSE:
                0.00014050719619262964
Epoch 74 MSE:
                0.00013172220496926457
Epoch 75 MSE:
                0.00013273197691887617
Epoch 76 MSE:
                0.00013864894572179765
Epoch 77 MSE:
                0.00014345742238219827
Epoch 78 MSE:
                0.00014244996418710798
Epoch 79 MSE:
                0.00013372718240134418
Epoch 80 MSE:
                0.00011846952111227438
Epoch
      81 MSE:
                0.00010008439858211204
Epoch 82 MSE:
                8.271920523839071e-05
Epoch 83 MSE:
                6.974201096454635e-05
Epoch 84 MSE:
                6.271102029131725e-05
Epoch
      85 MSE:
                6.11253926763311e-05
Epoch
      86 MSE:
                6.293384649325162e-05
Epoch
      87 MSE:
                6.551459955517203e-05
Epoch
       88 MSE:
                6.670141738140956e-05
Epoch
      89 MSE:
                6.547017983393744e-05
Epoch
      90 MSE:
                6.208451668499038e-05
Epoch 91 MSE:
                5.7731547713046893e-05
      92 MSE:
Epoch
                5.386580596677959e-05
Epoch 93 MSE:
                5.158617932465859e-05
Epoch 94 MSE:
                5.126586984260939e-05
Epoch 95 MSE:
                5.25112591276411e-05
Epoch
      96 MSE:
                5.44309732504189e-05
Epoch
      97 MSE:
                5.60344269615598e-05
Epoch
      98 MSE:
                5.6607848819112405e-05
      99 MSE:
Epoch
                5.5922719184309244e-05
T-time: 2.954310894012451
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Train Score: 0.22 RMSE

Validation Score: 1.16 RMSE

Time Step = 20 | Hidden States = 4 | Num Layers = 1

Epoch 0 MSE: 0.13150110840797424 Epoch 1 MSE: 0.09961990267038345 Epoch 2 MSE: 0.07914496958255768 Epoch 3 MSE: 0.06759276241064072 Epoch 4 MSE: 0.062282297760248184 Epoch 5 MSE: 0.06058744341135025 Epoch 6 MSE: 0.06027151271700859 Epoch 7 MSE: 0.05979962646961212 Epoch 8 MSE: 0.05843152850866318 Epoch 9 MSE: 0.05606463924050331 Epoch 10 MSE: 0.05297219008207321 Epoch 11 MSE: 0.04957352951169014 Epoch 12 MSE: 0.04628126695752144 Epoch 13 MSE: 0.04341447725892067 Epoch 14 MSE: 0.0411575585603714 Epoch 15 MSE: 0.039550963789224625 Epoch 16 MSE: 0.03850703686475754 Epoch 17 MSE: 0.03784612938761711 Epoch 18 MSE: 0.03734634816646576 Epoch 19 MSE: 0.03679636865854263 Epoch 20 MSE: 0.03603914752602577 0.03499677777290344 Epoch 21 MSE: Epoch 22 MSE: 0.0336734801530838 Epoch 23 MSE: 0.03214031085371971 Epoch 24 MSE: 0.03050883300602436 Epoch 25 MSE: 0.028900932520627975 Epoch 26 MSE: 0.027420081198215485 Epoch 27 MSE: 0.026128524914383888 Epoch 28 MSE: 0.02503422647714615 Epoch 29 MSE: 0.02409137226641178 Epoch 30 MSE: 0.023216255009174347 Epoch 31 MSE: 0.022315163165330887 Epoch 32 MSE: 0.02131510339677334 Epoch 33 MSE: 0.020185701549053192 Epoch 34 MSE: 0.018944963812828064 Epoch 35 MSE: 0.017648566514253616 Epoch 36 MSE: 0.01636810041964054 Epoch 37 MSE: 0.015165803954005241

```
Epoch
       38 MSE:
                0.014073267579078674
Epoch
       39 MSE:
                0.013080640695989132
Epoch
       40 MSE:
                0.01214095763862133
       41 MSE:
Epoch
                0.011190218850970268
Epoch
       42 MSE:
                0.010176819749176502
Epoch
       43 MSE:
                0.009087163023650646
Epoch
       44 MSE:
                0.007953930646181107
Epoch
       45 MSE:
                0.00684200506657362
Epoch 46 MSE:
                0.005818046163767576
Epoch
       47 MSE:
                0.004917980637401342
       48 MSE:
                0.004130267072468996
Epoch
       49 MSE:
Epoch
                0.003408480668440461
Epoch
       50 MSE:
                0.002709138672798872
Epoch
       51 MSE:
                0.0020287816878408194
Epoch
       52 MSE:
                0.0014117861865088344
Epoch
      53 MSE:
                0.0009215478203259408
Epoch
       54 MSE:
                0.0005933180218562484
       55 MSE:
Epoch
                0.00040389696368947625
Epoch
       56 MSE:
                0.0002904135035350919
Epoch
       57 MSE:
                0.00020905885321553797
       58 MSE:
Epoch
                0.00017268426017835736
       59 MSE:
Epoch
                0.00022182182874530554
Epoch
       60 MSE:
                0.00036012069904245436
       61 MSE:
Epoch
                0.0005299026961438358
       62 MSE:
                0.0006615917081944644
Epoch
Epoch
       63 MSE:
                0.0007374346605502069
       64 MSE:
Epoch
                0.0007895224262028933
Epoch
       65 MSE:
                0.0008408876601606607
       66 MSE:
Epoch
                0.0008701222250238061
Epoch
       67 MSE:
                0.0008433462353423238
Epoch
       68 MSE:
                0.0007626520819030702
Epoch
       69 MSE:
                0.000663854880258441
       70 MSE:
Epoch
                0.0005753102013841271
       71 MSE:
                0.0004952741437591612
Epoch
Epoch
       72 MSE:
                0.0004096037591807544
Epoch
       73 MSE:
                0.00031875577406026423
Epoch
      74 MSE:
                0.00023959427198860794
Epoch
       75 MSE:
                0.0001859543554019183
      76 MSE:
Epoch
                0.00015541244647465646
      77 MSE:
Epoch
                0.00013586373825091869
       78 MSE:
                0.00012011553917545825
Epoch
Epoch
       79 MSE:
                0.00011077721137553453
Epoch
       80 MSE:
                0.00011282829655101523
       81 MSE:
Epoch
                0.00012514514673966914
Epoch
       82 MSE:
                0.0001405237417202443
Epoch
       83 MSE:
                0.00015245267422869802
       84 MSE:
Epoch
                0.00016006853547878563
       85 MSE:
                0.00016645969299133867
Epoch
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Epoch 86 MSE: 0.00017348944675177336 Epoch 87 MSE: 0.00017930654576048255 Epoch 88 MSE: 0.00018067187920678407 Epoch 89 MSE: 0.0001766977657098323 Epoch 90 MSE: 0.00016963751113507897 Epoch 91 MSE: 0.00016228746972046793 Epoch 92 MSE: 0.0001553410111228004 Epoch 93 MSE: 0.00014758484030608088 Epoch 94 MSE: 0.00013823194603901356 Epoch 95 MSE: 0.00012837871327064931 Epoch 96 MSE: 0.00011999591515632346 Epoch 97 MSE: 0.00011394401371944696 Epoch 98 MSE: 0.00010946145630441606 Epoch 99 MSE: 0.00010552418098086491

T-time: 1.8887569904327393

Epoch 0 MSE: 0.11875616759061813 Epoch 1 MSE: 0.10860424488782883 Epoch 2 MSE: 0.09938566386699677 Epoch 3 MSE: 0.09090611338615417 Epoch 4 MSE: 0.08317798376083374 Epoch 5 MSE: 0.07624413818120956 Epoch 6 MSE: 0.0701715275645256 Epoch 7 MSE: 0.06496895849704742 Epoch 8 MSE: 0.06069688871502876 Epoch 9 MSE: 0.0573975034058094 Epoch 10 MSE: 0.055055081844329834 Epoch 11 MSE: 0.05353667959570885 Epoch 12 MSE: 0.05258754640817642

Epoch 15 MSE: 0.05089385807514191 Epoch 16 MSE: 0.050290822982788086 Epoch 17 MSE: 0.04958265647292137 Epoch 18 MSE: 0.04877021908760071 Epoch 19 MSE: 0.047875795513391495

0.05194589123129845

0.05142199248075485

Epoch 13 MSE:

Epoch 14 MSE:

Epoch 19 MSE: 0.047875795513391495 Epoch 20 MSE: 0.04693381488323212 Epoch 21 MSE: 0.04598284140229225 Epoch 22 MSE: 0.04505929350852966 Epoch 23 MSE: 0.0441933274269104

Epoch 24 MSE: 0.043406516313552856 Epoch 25 MSE: 0.04271119832992554

```
Epoch
      26 MSE:
                0.04211100935935974
Epoch
      27 MSE:
                0.041602250188589096
Epoch
      28 MSE:
                0.04117562249302864
      29 MSE:
Epoch
                0.040818218141794205
Epoch
      30 MSE:
                0.040515314787626266
Epoch
      31 MSE:
                0.04025202617049217
Epoch
       32 MSE:
                0.04001453146338463
Epoch
      33 MSE:
                0.039791032671928406
Epoch 34 MSE:
                0.03957226499915123
Epoch
      35 MSE:
                0.03935173898935318
      36 MSE:
                0.03912566974759102
Epoch
      37 MSE:
Epoch
                0.038892712444067
Epoch
      38 MSE:
                0.038653548806905746
Epoch
       39 MSE:
                0.038410358130931854
Epoch 40 MSE:
                0.03816628456115723
Epoch 41 MSE:
                0.037924908101558685
Epoch 42 MSE:
                0.03768973797559738
      43 MSE:
Epoch
                0.03746384009718895
Epoch
       44 MSE:
                0.03724951669573784
Epoch
      45 MSE:
                0.03704812750220299
Epoch
       46 MSE:
                0.036860015243291855
Epoch 47 MSE:
                0.036684565246105194
Epoch 48 MSE:
                0.0365203358232975
Epoch 49 MSE:
                0.036365289241075516
Epoch
      50 MSE:
                0.036217037588357925
Epoch 51 MSE:
                0.03607311472296715
Epoch 52 MSE:
                0.03593124821782112
Epoch
       53 MSE:
                0.03578951582312584
Epoch 54 MSE:
                0.03564648702740669
Epoch 55 MSE:
                0.035501305013895035
Epoch 56 MSE:
                0.03535360470414162
Epoch 57 MSE:
                0.03520349785685539
Epoch 58 MSE:
                0.03505135700106621
      59 MSE:
Epoch
                0.03489777073264122
Epoch
       60 MSE:
                0.03474331274628639
Epoch
      61 MSE:
                0.03458847478032112
Epoch
      62 MSE:
                0.03443354368209839
Epoch
       63 MSE:
                0.03427858650684357
       64 MSE:
Epoch
                0.03412340581417084
Epoch
      65 MSE:
                0.033967580646276474
      66 MSE:
Epoch
                0.033810507506132126
       67 MSE:
Epoch
                0.033651478588581085
Epoch
       68 MSE:
                0.03348973020911217
       69 MSE:
Epoch
                0.033324502408504486
Epoch
      70 MSE:
                0.033155109733343124
Epoch
      71 MSE:
                0.032980963587760925
Epoch
      72 MSE:
                0.032801553606987
      73 MSE:
Epoch
                0.03261649236083031
```

```
Epoch 74 MSE: 0.032425474375486374
Epoch 75 MSE: 0.03222823515534401
Epoch 76 MSE: 0.03202454000711441
Epoch 77 MSE:
               0.03181414678692818
Epoch 78 MSE:
               0.03159676119685173
Epoch 79 MSE:
               0.031372036784887314
Epoch 80 MSE:
               0.03113955445587635
Epoch 81 MSE:
               0.0308988094329834
Epoch 82 MSE:
               0.030649244785308838
Epoch 83 MSE:
               0.030390236526727676
Epoch 84 MSE:
               0.03012111410498619
Epoch 85 MSE:
               0.02984119951725006
Epoch 86 MSE:
               0.02954978123307228
Epoch 87 MSE:
               0.029246171936392784
Epoch 88 MSE:
               0.02892967313528061
Epoch 89 MSE:
               0.028599591925740242
Epoch 90 MSE:
               0.028255239129066467
Epoch 91 MSE:
               0.027895910665392876
Epoch 92 MSE:
               0.02752087265253067
Epoch 93 MSE:
               0.027129368856549263
Epoch 94 MSE:
               0.02672058343887329
Epoch 95 MSE:
               0.026293663308024406
Epoch 96 MSE: 0.02584848739206791
Epoch 97 MSE: 0.025391479954123497
Epoch 98 MSE:
               0.024937951937317848
Epoch 99 MSE:
               0.02447507716715336
```

T-time: 1.9537885189056396

Train Score: 4.67 RMSE

_____ Validation Score: 29.53 RMSE _____

Time Step = 20 | Hidden States = 4 | Num Layers = 2

Epoch 0 MSE: 0.14334483444690704 Epoch 1 MSE: 0.0771237388253212 Epoch 2 MSE: 0.03169119730591774 Epoch 3 MSE: 0.011012035422027111 Epoch 4 MSE: 0.013505011796951294 Epoch 5 MSE: 0.027539493516087532 Epoch 6 MSE: 0.037603095173835754 Epoch 7 MSE: 0.038004592061042786 Epoch 8 MSE: 0.031059544533491135 Epoch 9 MSE: 0.021251199766993523

```
Epoch
       10 MSE:
                0.012524732388556004
Epoch
       11 MSE:
                0.0072272527031600475
Epoch 12 MSE:
                0.0058388542383909225
       13 MSE:
Epoch
                0.0073640430346131325
Epoch
       14 MSE:
                0.010120854713022709
Epoch
       15 MSE:
                0.01250118762254715
Epoch
       16 MSE:
                0.013444487936794758
Epoch
      17 MSE:
                0.012596268206834793
Epoch 18 MSE:
                0.010237338952720165
Epoch
       19 MSE:
                0.007083946373313665
      20 MSE:
Epoch
                0.004026561509817839
      21 MSE:
Epoch
                0.0018495575059205294
Epoch
      22 MSE:
                0.0009819628903642297
Epoch
      23 MSE:
                0.001357759116217494
Epoch 24 MSE:
                0.002463115146383643
                0.00357668474316597
Epoch 25 MSE:
Epoch
      26 MSE:
                0.004095400217920542
      27 MSE:
                0.0037783407606184483
Epoch
Epoch
      28 MSE:
                0.002797173336148262
Epoch
       29 MSE:
                0.0015996524598449469
Epoch
       30 MSE:
                0.0006763892015442252
      31 MSE:
Epoch
                0.0003400748537387699
Epoch 32 MSE:
                0.0006061470485292375
      33 MSE:
Epoch
                0.0012197202304378152
Epoch
      34 MSE:
                0.0018074300605803728
Epoch
      35 MSE:
                0.002068799454718828
      36 MSE:
Epoch
                0.0019051248673349619
Epoch
       37 MSE:
                0.0014304250944405794
      38 MSE:
Epoch
                0.0008804212557151914
Epoch 39 MSE:
                0.0004819741006940603
Epoch 40 MSE:
                0.0003506467037368566
Epoch
       41 MSE:
                0.00045837441575713456
Epoch
      42 MSE:
                0.0006739501841366291
      43 MSE:
                0.0008444260456599295
Epoch
Epoch
       44 MSE:
                0.0008712830021977425
Epoch
      45 MSE:
                0.0007461814093403518
Epoch 46 MSE:
                0.0005373554886318743
Epoch 47 MSE:
                0.00034283226705156267
       48 MSE:
Epoch
                0.00023875865736044943
Epoch
      49 MSE:
                0.0002476582885719836
Epoch 50 MSE:
                0.00033742657979018986
       51 MSE:
Epoch
                0.00044567236909642816
Epoch
      52 MSE:
                0.0005134740495122969
      53 MSE:
Epoch
                0.0005114704254083335
Epoch
      54 MSE:
                0.00044796260772272944
Epoch
       55 MSE:
                0.00035851928987540305
Epoch
       56 MSE:
                0.00028476741863414645
      57 MSE:
                0.0002536349056754261
Epoch
```

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Epoch 58 MSE:
                0.0002666363143362105
Epoch 59 MSE:
                0.0003030527732335031
Epoch 60 MSE:
                0.00033376243663951755
Epoch 61 MSE:
                0.00033748289570212364
Epoch 62 MSE:
                0.00031076473533175886
Epoch
      63 MSE:
                0.00026729280943982303
Epoch
      64 MSE:
                0.00022819824516773224
Epoch 65 MSE:
                0.0002097164688166231
Epoch 66 MSE:
                0.0002151568332919851
Epoch 67 MSE:
                0.00023497662914451212
      68 MSE:
                0.00025383796310052276
Epoch
Epoch 69 MSE:
                0.0002598176070023328
Epoch 70 MSE:
                0.00025037722662091255
Epoch 71 MSE:
                0.00023219938157126307
Epoch 72 MSE:
                0.0002158486604457721
Epoch 73 MSE:
                0.0002090392808895558
Epoch 74 MSE:
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Epoch 75 MSE:
                0.00022101817012298852
Epoch 76 MSE:
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Epoch 77 MSE:
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Epoch 78 MSE:
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Epoch 79 MSE:
                0.000206250449991785
Epoch 80 MSE:
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Epoch 82 MSE:
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Epoch 83 MSE:
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Epoch 84 MSE:
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Epoch 85 MSE:
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Epoch 86 MSE:
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Epoch 87 MSE:
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Epoch 88 MSE:
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Epoch
      89 MSE:
                0.00019086652901023626
Epoch 90 MSE:
                0.00019233618513680995
Epoch 91 MSE:
                0.00019303012231830508
Epoch
      92 MSE:
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Epoch 93 MSE:
                0.00018916981935035437
Epoch 94 MSE:
                0.00018615872249938548
Epoch 95 MSE:
                0.00018408367759548128
Epoch 96 MSE:
                0.00018336866924073547
Epoch 97 MSE:
                0.0001834852882893756
Epoch 98 MSE:
                0.00018347089644521475
      99 MSE:
                0.00018265207472722977
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T-time: 3.0723373889923096

Train Score: 0.40 RMSE

Validation Score: 10.11 RMSE

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Epoch 0 MSE: 0.2550846040248871
Epoch
       1 MSE:
               0.20965315401554108
Epoch 2 MSE:
               0.1708953082561493
Epoch 3 MSE:
               0.13941694796085358
Epoch 4 MSE:
               0.11258117109537125
Epoch 5 MSE:
               0.0899198055267334
Epoch 6 MSE:
               0.0709933191537857
Epoch 7 MSE:
               0.05540340766310692
Epoch 8 MSE:
               0.04275799170136452
Epoch 9 MSE:
               0.03267022967338562
Epoch 10 MSE:
                0.024770090356469154
Epoch 11 MSE:
                0.018663005903363228
Epoch 12 MSE:
                0.013972103595733643
Epoch 13 MSE:
                0.010352651588618755
Epoch 14 MSE:
                0.007528757676482201
Epoch 15 MSE:
                0.005551889538764954
Epoch
       16 MSE:
                0.0035988017916679382
Epoch
       17 MSE:
                0.0018786754226312041
Epoch
       18 MSE:
                0.0009374682558700442
Epoch 19 MSE:
                0.0009088294464163482
Epoch 20 MSE:
                0.0012743272818624973
Epoch 21 MSE:
                0.0013502002693712711
Epoch
      22 MSE:
                0.001258679199963808
Epoch 23 MSE:
                0.0013215410290285945
Epoch 24 MSE:
                0.0016296820249408484
Epoch 25 MSE:
                0.0020280107855796814
Epoch 26 MSE:
                0.0022279920522123575
Epoch 27 MSE:
                0.0020855567418038845
Epoch 28 MSE:
                0.0016608773730695248
Epoch
      29 MSE:
                0.0011401731753721833
Epoch
      30 MSE:
                0.000715788803063333
      31 MSE:
                0.0004797110450454056
Epoch
Epoch
       32 MSE:
                0.00042223281343467534
Epoch
      33 MSE:
                0.00042258520261384547
Epoch 34 MSE:
                0.0003453076060395688
Epoch
      35 MSE:
                0.00022173549223225564
      36 MSE:
Epoch
                0.00016730211791582406
Epoch 37 MSE:
                0.00023457326460629702
Epoch 38 MSE:
                0.00037376198451966047
       39 MSE:
Epoch
                0.000489494763314724
Epoch
      40 MSE:
                0.0005190781666897237
Epoch 41 MSE:
                0.0004699661221820861
Epoch 42 MSE:
                0.0003984368813689798
Epoch
       43 MSE:
                0.0003570067638065666
Epoch
       44 MSE:
                0.00035637334804050624
      45 MSE:
                0.00035483899409882724
Epoch
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Epoch
       46 MSE:
                0.00029466807609423995
Epoch
       47 MSE:
                0.00019539987260941416
Epoch
       48 MSE:
                0.00012499500007834285
       49 MSE:
Epoch
                0.00011202224413864315
Epoch
       50 MSE:
                0.00012422727013472468
Epoch
       51 MSE:
                0.00012027863704133779
Epoch
       52 MSE:
                9.361421689391136e-05
Epoch
      53 MSE:
                7.342580647673458e-05
Epoch 54 MSE:
                8.703218190930784e-05
Epoch
      55 MSE:
                0.00011941004049731418
       56 MSE:
Epoch
                0.00013054058945272118
Epoch
       57 MSE:
                0.00011153476953040808
Epoch
       58 MSE:
                9.133484854828566e-05
Epoch
       59 MSE:
                8.865477138897404e-05
Epoch
       60 MSE:
                9.01499661267735e-05
Epoch 61 MSE:
                7.617472147103399e-05
Epoch
       62 MSE:
                5.0264254241483286e-05
       63 MSE:
Epoch
                3.3158863516291603e-05
Epoch
       64 MSE:
                3.388381446711719e-05
Epoch
       65 MSE:
                3.8454287278000265e-05
Epoch
       66 MSE:
                3.333490531076677e-05
Epoch
       67 MSE:
                2.6499337764107622e-05
Epoch
       68 MSE:
                3.0048042390262708e-05
       69 MSE:
Epoch
                3.893994289683178e-05
Epoch
      70 MSE:
                4.0904589695855975e-05
Epoch
     71 MSE:
                3.507962537696585e-05
      72 MSE:
Epoch
                3.0845447327010334e-05
Epoch
     73 MSE:
                3.185156310792081e-05
Epoch 74 MSE:
                3.122929410892539e-05
Epoch 75 MSE:
                2.507691169739701e-05
Epoch 76 MSE:
                1.9223547496949323e-05
Epoch 77 MSE:
                1.8424787413096055e-05
Epoch
      78 MSE:
                1.9737934053409845e-05
      79 MSE:
Epoch
                1.8953121980302967e-05
Epoch
       80 MSE:
                1.720967520668637e-05
Epoch
       81 MSE:
                1.7950973415281624e-05
Epoch
       82 MSE:
                2.057048368442338e-05
Epoch
       83 MSE:
                2.1521154849324375e-05
Epoch
       84 MSE:
                2.0223060346324928e-05
Epoch
       85 MSE:
                1.9296550817671232e-05
      86 MSE:
Epoch
                1.9637114746728912e-05
Epoch
       87 MSE:
                1.9388275177334435e-05
Epoch
       88 MSE:
                1.7702337572700344e-05
Epoch
       89 MSE:
                1.625109689484816e-05
Epoch
       90 MSE:
                1.6244019207078964e-05
Epoch
       91 MSE:
                1.662002432567533e-05
Epoch
       92 MSE:
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Epoch
       93 MSE:
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Epoch 94 MSE: 1.643188443267718e-05

Epoch 95 MSE: 1.708767013042234e-05

Epoch 96 MSE: 1.6994628822430968e-05

Epoch 97 MSE: 1.6547352061024867e-05

Epoch 98 MSE: 1.6487458196934313e-05

Epoch 99 MSE: 1.6537869669264182e-05
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T-time: 3.044351577758789

Train Score: 0.12 RMSE

-----Validation Score: 5.85 RMSE

Time Step = 20 | Hidden States = 8 | Num Layers = 1

0.0019425706705078483

0.0007563027902506292

0.0007302159792743623

0.0008453840855509043

0.0005777942133136094

0.0002932864590547979

Epoch 0 MSE: 0.0527842678129673 Epoch 1 MSE: 0.033607058227062225 Epoch 2 MSE: 0.02729419432580471 Epoch 3 MSE: 0.031045515090227127 Epoch 4 MSE: 0.03097517229616642 Epoch 5 MSE: 0.0260578952729702 Epoch 6 MSE: 0.02095322497189045 Epoch 7 MSE: 0.01810598000884056 Epoch 8 MSE: 0.017289673909544945 Epoch 9 MSE: 0.01700352504849434 Epoch 10 MSE: 0.015787092968821526 Epoch 11 MSE: 0.01306844037026167 Epoch 12 MSE: 0.009403295814990997 Epoch 13 MSE: 0.006175782065838575 Epoch 14 MSE: 0.004754423629492521 Epoch 15 MSE: 0.004778053145855665 Epoch 16 MSE: 0.0037487701047211885 Epoch 17 MSE: 0.0012004730524495244 Epoch 18 MSE: 0.0003792186616919935 Epoch 19 MSE: 0.002634403295814991 Epoch 20 MSE: 0.0034192318562418222 Epoch 21 MSE: 0.002201696392148733 Epoch 22 MSE: 0.002727847546339035Epoch 23 MSE: 0.0033487596083432436

Epoch 24 MSE:

Epoch 25 MSE:

Epoch 26 MSE:

Epoch 27 MSE:

Epoch 28 MSE:

Epoch 29 MSE:

```
30 MSE:
Epoch
                0.00037036306457594037
Epoch
      31 MSE:
                0.0007205598521977663
      32 MSE:
Epoch
                0.0009847291512414813
Epoch
      33 MSE:
                0.000966812192928046
Epoch
       34 MSE:
                0.0007821757462807
Epoch
      35 MSE:
                0.0006495261914096773
Epoch
       36 MSE:
                0.000642504368443042
Epoch
      37 MSE:
                0.0006533821579068899
Epoch 38 MSE:
                0.0005504863802343607
Epoch
      39 MSE:
                0.0003380657872185111
      40 MSE:
                0.00015514952247031033
Epoch
Epoch 41 MSE:
                0.00011827681737486273
Epoch 42 MSE:
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Epoch
      43 MSE:
                0.00021129670494701713
Epoch 44 MSE:
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Epoch 45 MSE:
                0.00014163253945298493
Epoch 46 MSE:
                0.00020845689869020134
      47 MSE:
Epoch
                0.0002831336169037968
Epoch
       48 MSE:
                0.00026966514997184277
Epoch
      49 MSE:
                0.0001951527374330908
Epoch
       50 MSE:
                0.00015049483045004308
Epoch 51 MSE:
                0.0001524468680145219
Epoch 52 MSE:
                0.00014250243839342147
Epoch 53 MSE:
                9.658630006015301e-05
Epoch 54 MSE:
                5.795023389509879e-05
Epoch 55 MSE:
                6.263986142585054e-05
Epoch 56 MSE:
                9.076762944459915e-05
Epoch
       57 MSE:
                0.00010361338354414329
      58 MSE:
Epoch
                9.526342182653025e-05
Epoch 59 MSE:
                8.93671385711059e-05
Epoch 60 MSE:
                9.86564700724557e-05
Epoch
       61 MSE:
                0.00010784040932776406
Epoch
      62 MSE:
                9.89845793810673e-05
      63 MSE:
Epoch
                7.800159801263362e-05
Epoch
       64 MSE:
                6.446017505368218e-05
Epoch
       65 MSE:
                6.379968544933945e-05
Epoch
       66 MSE:
                6.37236880720593e-05
Epoch
       67 MSE:
                5.624253390124068e-05
Epoch
       68 MSE:
                4.9524711357662454e-05
Epoch
      69 MSE:
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Epoch 70 MSE:
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Epoch 71 MSE:
                6.373723590513691e-05
Epoch
      72 MSE:
                5.956153472652659e-05
Epoch
     73 MSE:
                5.735424201702699e-05
Epoch 74 MSE:
                5.8805693697649986e-05
Epoch
      75 MSE:
                5.765194873674773e-05
Epoch
      76 MSE:
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      77 MSE:
Epoch
                4.686461397795938e-05
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Epoch 78 MSE: 4.661463026423007e-05 Epoch 79 MSE: 4.7889156121527776e-05 Epoch 80 MSE: 4.702334990724921e-05 Epoch 81 MSE: 4.5588662032969296e-05 Epoch 82 MSE: 4.6451546950265765e-05 Epoch 83 MSE: 4.843365968554281e-05 Epoch 84 MSE: 4.849215110880323e-05 4.665035521611571e-05 Epoch 85 MSE: Epoch 86 MSE: 4.535672997008078e-05 Epoch 87 MSE: 4.522270683082752e-05 Epoch 88 MSE: 4.458209878066555e-05 Epoch 89 MSE: 4.292494850233197e-05 Epoch 90 MSE: 4.181574331596494e-05 Epoch 91 MSE: 4.206608355161734e-05 Epoch 92 MSE: 4.249731864547357e-05 Epoch 93 MSE: 4.216980960336514e-05 Epoch 94 MSE: 4.177328446530737e-05 Epoch 95 MSE: 4.197633097646758e-05 Epoch 96 MSE: 4.2125117033720016e-05 Epoch 97 MSE: 4.1543560655554757e-05 Epoch 98 MSE: 4.074180105817504e-05 Epoch 99 MSE: 4.0397113480139524e-05 T-time: 2.368370294570923

Train Score: 0.19 RMSE

Validation Score: 6.41 RMSE

Epoch 0 MSE: 0.051062941551208496 Epoch 1 MSE: 0.03999146819114685 Epoch 2 MSE: 0.03518593683838844 Epoch 3 MSE: 0.03586225584149361 Epoch 4 MSE: 0.03642748296260834 Epoch 5 MSE: 0.03458893299102783 Epoch 6 MSE: 0.031704436987638474 Epoch 7 MSE: 0.029234107583761215 Epoch 8 MSE: 0.02769237756729126 Epoch 9 MSE: 0.02682698890566826 Epoch 10 MSE: 0.02605593577027321 Epoch 11 MSE: 0.02491629868745804 Epoch 12 MSE: 0.023238487541675568 Epoch 13 MSE: 0.021097302436828613 Epoch 14 MSE: 0.01872711069881916 Epoch 15 MSE: 0.016384322196245193 Epoch 16 MSE: 0.014461628161370754 Epoch 17 MSE: 0.01327712181955576

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Epoch
       18 MSE:
                0.012049922719597816
Epoch
       19 MSE:
                0.010776203125715256
Epoch
      20 MSE:
                0.00947749987244606
      21 MSE:
Epoch
                0.008200135082006454
Epoch
      22 MSE:
                0.006950742565095425
Epoch
      23 MSE:
                0.0057051037438213825
Epoch
      24 MSE:
                0.004444983322173357
Epoch
      25 MSE:
                0.003240748541429639
Epoch 26 MSE:
                0.0022044300567358732
Epoch
      27 MSE:
                0.0013892556307837367
      28 MSE:
                0.0007624808931723237
Epoch
      29 MSE:
Epoch
                0.0003879956784658134
Epoch
       30 MSE:
                0.0004044284869451076
Epoch
       31 MSE:
                0.0006753685884177685
Epoch
      32 MSE:
                0.0011379948118701577
Epoch 33 MSE:
                0.0016910627018660307
Epoch
       34 MSE:
                0.001988198608160019
      35 MSE:
                0.0020920296665281057
Epoch
Epoch
       36 MSE:
                0.001882838667370379
Epoch
       37 MSE:
                0.001544222584925592
       38 MSE:
Epoch
                0.0011667313519865274
       39 MSE:
Epoch
                0.0008001386886462569
Epoch 40 MSE:
                0.0005566774634644389
Epoch 41 MSE:
                0.00039411982288584113
      42 MSE:
                0.00031961954664438963
Epoch
Epoch
      43 MSE:
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Epoch 44 MSE:
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Epoch
       45 MSE:
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      46 MSE:
Epoch
                0.000495244690682739
Epoch 47 MSE:
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Epoch 48 MSE:
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Epoch
       49 MSE:
                0.0005939549882896245
      50 MSE:
                0.0005760466447100043
Epoch
      51 MSE:
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Epoch
Epoch
       52 MSE:
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Epoch
      53 MSE:
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Epoch
       54 MSE:
                0.00028124250820837915
Epoch
      55 MSE:
                0.00017754669534042478
      56 MSE:
Epoch
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Epoch 57 MSE:
                7.857759192120284e-05
Epoch 58 MSE:
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       59 MSE:
Epoch
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Epoch
       60 MSE:
                0.0002061078994302079
Epoch
       61 MSE:
                0.00013960177602712065
Epoch
      62 MSE:
                7.278155680978671e-05
Epoch
       63 MSE:
                5.1074726798105985e-05
       64 MSE:
Epoch
                6.325664435280487e-05
       65 MSE:
                7.791019743308425e-05
Epoch
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Epoch 66 MSE:
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Epoch 67 MSE: 0.00010406207729829475
Epoch 68 MSE:
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Epoch 69 MSE:
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Epoch 70 MSE:
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Epoch 71 MSE:
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Epoch 72 MSE:
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Epoch 73 MSE:
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Epoch 74 MSE:
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Epoch 75 MSE:
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Epoch 76 MSE:
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Epoch 77 MSE:
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Epoch 78 MSE:
               4.4109383452450857e-05
Epoch 79 MSE:
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Epoch 80 MSE:
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Epoch 81 MSE:
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Epoch 82 MSE:
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Epoch 85 MSE:
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Epoch 86 MSE:
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Epoch 87 MSE:
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Epoch 95 MSE:
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Epoch 96 MSE:
               2.2150612494442612e-05
Epoch 97 MSE:
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Epoch 98 MSE:
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Epoch 99 MSE:
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T-time: 2.4798943996429443

Train Score: 0.14 RMSE

-----Validation Score: 2.07 RMSE

Time Step = 20 | Hidden States = 8 | Num Layers = 2

Epoch 0 MSE: 0.04952426254749298 Epoch 1 MSE: 0.036013469099998474

```
Epoch 2 MSE:
               0.04220707714557648
Epoch
       3 MSE:
               0.03397147357463837
Epoch
       4 MSE:
               0.026170630007982254
Epoch
       5 MSE:
               0.025158515200018883
Epoch
       6 MSE:
               0.02567467838525772
Epoch 7 MSE:
               0.021704761311411858
Epoch
       8 MSE:
               0.014898579567670822
Epoch
      9 MSE:
               0.010468153282999992
Epoch 10 MSE:
                0.010068998672068119
Epoch
       11 MSE:
                0.007948752492666245
Epoch
       12 MSE:
                0.002451049629598856
Epoch
       13 MSE:
                0.0010973798343911767
Epoch
       14 MSE:
                0.0047994074411690235
Epoch
       15 MSE:
                0.0036800107918679714
Epoch
       16 MSE:
                0.0045299772173166275
Epoch 17 MSE:
                0.006031800527125597
Epoch
       18 MSE:
                0.003006525104865432
       19 MSE:
Epoch
                0.0017825885443016887
Epoch
       20 MSE:
                0.0019478130852803588
Epoch
       21 MSE:
                0.0011439495719969273
Epoch
       22 MSE:
                0.0004836340667679906
       23 MSE:
Epoch
                0.0009379183175042272
Epoch
       24 MSE:
                0.0017570145428180695
       25 MSE:
Epoch
                0.001990336924791336
Epoch
       26 MSE:
                0.0017038615187630057
Epoch
       27 MSE:
                0.0015051978407427669
       28 MSE:
Epoch
                0.0015903894091024995
Epoch
       29 MSE:
                0.001586827216669917
       30 MSE:
Epoch
                0.001188503229059279
Epoch
       31 MSE:
                0.000637293909676373
       32 MSE:
Epoch
                0.0003994397702626884
Epoch
       33 MSE:
                0.0005010399036109447
Epoch
       34 MSE:
                0.0005360940122045577
Epoch
       35 MSE:
                0.00039184652268886566
Epoch
       36 MSE:
                0.00041271603549830616
Epoch
       37 MSE:
                0.0006690514856018126
Epoch
       38 MSE:
                0.0007672138162888587
Epoch
       39 MSE:
                0.0005895008216612041
       40 MSE:
Epoch
                0.0004510378639679402
Epoch
       41 MSE:
                0.00045150594087317586
       42 MSE:
                0.0003836370597127825
Epoch
Epoch
       43 MSE:
                0.00022831578098703176
Epoch
       44 MSE:
                0.00017601094441488385
       45 MSE:
Epoch
                0.00025537132751196623
Epoch
       46 MSE:
                0.00031429051887243986
Epoch
       47 MSE:
                0.00029484438709914684
Epoch
       48 MSE:
                0.0002834045444615185
       49 MSE:
                0.0003173686272930354
Epoch
```

```
Epoch 50 MSE:
                0.0003213116724509746
Epoch
      51 MSE:
                0.0002560626599006355
      52 MSE:
                0.00019137182971462607
Epoch
Epoch
      53 MSE:
                0.00018109513621311635
Epoch
      54 MSE:
                0.00018226038082502782
Epoch
      55 MSE:
                0.000157597751240246
Epoch
       56 MSE:
                0.00014848430873826146
Epoch 57 MSE:
                0.00017917758668772876
Epoch 58 MSE:
                0.000199176836758852
Epoch 59 MSE:
                0.00018203664512839168
Epoch
       60 MSE:
                0.00016696045349817723
Epoch
      61 MSE:
                0.00016738651902414858
Epoch
       62 MSE:
                0.00015301025996450335
Epoch
       63 MSE:
                0.00012692069867625833
Epoch
      64 MSE:
                0.00012079757289029658
Epoch 65 MSE:
                0.00013021094491705298
Epoch
       66 MSE:
                0.00013026606757193804
       67 MSE:
                0.00012582792260218412
Epoch
Epoch
       68 MSE:
                0.000131158041767776
Epoch
       69 MSE:
                0.00013500383647624403
Epoch
      70 MSE:
                0.0001255514071090147
Epoch 71 MSE:
                0.0001149943855125457
Epoch 72 MSE:
                0.00011284036736469716
Epoch 73 MSE:
                0.00010969607683364302
Epoch 74 MSE:
                0.0001028960250550881
Epoch 75 MSE:
                0.00010250233754049987
Epoch 76 MSE:
                0.0001069468489731662
Epoch 77 MSE:
                0.00010627409938024357
Epoch 78 MSE:
                0.00010303071030648425
Epoch 79 MSE:
                0.00010282260336680338
Epoch 80 MSE:
                0.00010084781388286501
Epoch
      81 MSE:
                9.531758405501023e-05
Epoch
      82 MSE:
                9.25324420677498e-05
      83 MSE:
Epoch
                9.271293674828485e-05
Epoch
       84 MSE:
                9.132778359344229e-05
Epoch
      85 MSE:
                9.001295256894082e-05
Epoch
       86 MSE:
                9.088174556382e-05
Epoch
      87 MSE:
                9.055033297045156e-05
      88 MSE:
Epoch
                8.80849183886312e-05
Epoch
      89 MSE:
                8.653698023408651e-05
Epoch 90 MSE:
                8.554450323572382e-05
Epoch
       91 MSE:
                8.344200614374131e-05
Epoch
      92 MSE:
                8.205576887121424e-05
Epoch
      93 MSE:
                8.210788655560464e-05
Epoch
      94 MSE:
                8.15613311715424e-05
Epoch
       95 MSE:
                8.055901707848534e-05
Epoch
      96 MSE:
                8.021085523068905e-05
      97 MSE:
Epoch
                7.93965591583401e-05
```

Epoch 98 MSE: 7.785463822074234e-05 Epoch 99 MSE: 7.690577331231907e-05

T-time: 4.258131265640259

Train Score: 0.26 RMSE

Validation Score: 8.88 RMSE

Epoch 0 MSE: 0.03801354393362999 Epoch 1 MSE: 0.03231310099363327 Epoch 2 MSE: 0.033228594809770584 Epoch 3 MSE: 0.032042235136032104 Epoch 4 MSE: 0.029601454734802246 Epoch 5 MSE: 0.027956893667578697 Epoch 6 MSE: 0.026787491515278816 Epoch 7 MSE: 0.025032859295606613 Epoch 8 MSE: 0.0223383866250515 Epoch 9 MSE: 0.019487174227833748 Epoch 10 MSE: 0.017636461183428764 Epoch 11 MSE: 0.016014425083994865 Epoch 12 MSE: 0.013053761795163155 Epoch 13 MSE: 0.010477731004357338 Epoch 14 MSE: 0.009034672752022743 Epoch 15 MSE: 0.006561379414051771 Epoch 16 MSE: 0.004736900795251131 Epoch 17 MSE: 0.0036861577536910772 Epoch 18 MSE: 0.002670750953257084 Epoch 19 MSE: 0.0021849730983376503 Epoch 20 MSE: 0.002764027798548341 Epoch 21 MSE: 0.0027873211074620485 Epoch 22 MSE: 0.003007430350407958 Epoch 23 MSE: 0.0025733583606779575 Epoch 24 MSE: 0.001731877215206623 Epoch 25 MSE: 0.0013842781772837043 Epoch 26 MSE: 0.0011069471947848797 Epoch 27 MSE: 0.0016163198743015528 Epoch 28 MSE: 0.0019093886949121952 Epoch 29 MSE: 0.002002923283725977 Epoch 30 MSE: 0.0018666837131604552 Epoch 31 MSE: 0.0013787414645776153 Epoch 32 MSE: 0.0011336376192048192 Epoch 33 MSE: 0.0008749669650569558 Epoch 34 MSE: 0.0009343042620457709 Epoch 35 MSE: 0.001081822789274156 Epoch 36 MSE: 0.0011318182805553079 Epoch 37 MSE: 0.0011208379874005914

```
Epoch
       38 MSE:
                0.0008837123750708997
Epoch
       39 MSE:
                0.0007532959571108222
Epoch
       40 MSE:
                0.000580416526645422
       41 MSE:
Epoch
                0.0005826298147439957
Epoch
       42 MSE:
                0.0005965761956758797
Epoch
       43 MSE:
                0.0006343557615764439
Epoch
       44 MSE:
                0.0006594851147383451
Epoch
       45 MSE:
                0.000599266029894352
Epoch 46 MSE:
                0.0005632781540043652
Epoch
       47 MSE:
                0.0004670620255637914
       48 MSE:
                0.00043364136945456266
Epoch
       49 MSE:
Epoch
                0.0003994687576778233
Epoch
       50 MSE:
                0.00040858419379219413
Epoch
       51 MSE:
                0.0004248431941960007
Epoch 52 MSE:
                0.00042902270797640085
Epoch 53 MSE:
                0.0004299055435694754
Epoch
       54 MSE:
                0.00039704187656752765
       55 MSE:
Epoch
                0.0003763578424695879
Epoch
       56 MSE:
                0.0003375741944182664
Epoch
       57 MSE:
                0.0003291362663730979
Epoch
       58 MSE:
                0.0003112988779321313
       59 MSE:
Epoch
                0.0003188509726896882
Epoch
       60 MSE:
                0.00031100568594411016
       61 MSE:
Epoch
                0.0003130347467958927
       62 MSE:
                0.0002966133179143071
Epoch
Epoch
       63 MSE:
                0.0002853843616321683
       64 MSE:
Epoch
                0.00026392846484668553
Epoch
       65 MSE:
                0.00025279331021010876
       66 MSE:
Epoch
                0.000239689921727404
Epoch
       67 MSE:
                0.00023789520491845906
Epoch
       68 MSE:
                0.00023220710863824934
Epoch
       69 MSE:
                0.00023212176165543497
      70 MSE:
Epoch
                0.00022347288904711604
       71 MSE:
                0.00021822396956849843
Epoch
Epoch
       72 MSE:
                0.0002064451400656253
Epoch
      73 MSE:
                0.00020025167032144964
Epoch
     74 MSE:
                0.00019113333837594837
Epoch
      75 MSE:
                0.000187761164852418
Epoch 76 MSE:
                0.0001833838177844882
Epoch 77 MSE:
                0.00018073311366606504
Epoch 78 MSE:
                0.0001765077031450346
Epoch
       79 MSE:
                0.00017051132454071194
Epoch
       80 MSE:
                0.0001652275532251224
Epoch
       81 MSE:
                0.0001581187971169129
Epoch
       82 MSE:
                0.00015415434609167278
Epoch
       83 MSE:
                0.0001492084702476859
Epoch
       84 MSE:
                0.0001465760578867048
       85 MSE:
                0.00014335197920445353
Epoch
```

```
Epoch 86 MSE: 0.00013957232295069844
Epoch 87 MSE: 0.000136233662487939
Epoch 88 MSE: 0.00013138644862920046
Epoch 89 MSE:
               0.00012777336814906448
Epoch 90 MSE:
               0.00012383268040139228
Epoch 91 MSE:
               0.00012020765279885381
Epoch 92 MSE:
               0.00011741727212211117
Epoch 93 MSE:
               0.00011391357838874683
Epoch 94 MSE:
               0.00011083604476880282
Epoch 95 MSE:
               0.0001073898165486753
Epoch 96 MSE:
               0.00010363355977460742
Epoch 97 MSE: 0.00010044804366771132
Epoch 98 MSE: 9.71735134953633e-05
Epoch 99 MSE: 9.426844189874828e-05
```

T-time: 4.197821617126465

Train Score: 0.29 RMSE

Validation Score: 6.89 RMSE

Time Step = 20 | Hidden States = 16 | Num Layers = 1

Epoch 0 MSE: 0.11688412725925446 Epoch 1 MSE: 0.057557009160518646 Epoch 2 MSE: 0.030678261071443558 Epoch 3 MSE: 0.03053380735218525 Epoch 4 MSE: 0.040378447622060776 Epoch 5 MSE: 0.040537480264902115 Epoch 6 MSE: 0.03283340856432915 Epoch 7 MSE: 0.024670369923114777 Epoch 8 MSE: 0.01996000111103058 Epoch 9 MSE: 0.019083641469478607 Epoch 10 MSE: 0.02034519426524639 Epoch 11 MSE: 0.021152909845113754 Epoch 12 MSE: 0.019715365022420883 Epoch 13 MSE: 0.016081158071756363 Epoch 14 MSE: 0.011634751223027706 Epoch 15 MSE: 0.008115794509649277 Epoch 16 MSE: 0.006653478369116783 Epoch 17 MSE: 0.006825649179518223 Epoch 18 MSE: 0.006530591752380133 Epoch 19 MSE: 0.0041007231920957565 Epoch 20 MSE: 0.00092784856678918 Epoch 21 MSE: 0.0005236984579823911

```
Epoch 22 MSE:
                0.0034884933847934008
Epoch
      23 MSE:
                0.004348206799477339
      24 MSE:
Epoch
                0.0021173551212996244
      25 MSE:
Epoch
                0.0013048086548224092
Epoch
      26 MSE:
                0.002359129022806883
Epoch
      27 MSE:
                0.0024402879644185305
Epoch
      28 MSE:
                0.001183599466457963
Epoch
      29 MSE:
                0.00018964995979331434
Epoch 30 MSE:
                0.00024302772362716496
Epoch
      31 MSE:
                0.0008588089840486646
Epoch
      32 MSE:
                0.001253483584150672
Epoch
      33 MSE:
                0.0011290162801742554
Epoch
      34 MSE:
                0.0007311491062864661
Epoch
       35 MSE:
                0.00046422804007306695
Epoch
      36 MSE:
                0.0005161102744750679
                0.000749591737985611
Epoch 37 MSE:
Epoch
      38 MSE:
                0.000876557023730129
      39 MSE:
                0.0007357922731898725
Epoch
Epoch
       40 MSE:
                0.0004249964258633554
Epoch
      41 MSE:
                0.0001836870942497626
Epoch
       42 MSE:
                0.00016016323934309185
Epoch 43 MSE:
                0.00028601186932064593
Epoch 44 MSE:
                0.000367838452802971
Epoch 45 MSE:
                0.000297011632937938
Epoch 46 MSE:
                0.00015473418170586228
Epoch
      47 MSE:
                0.00010143363761017099
Epoch 48 MSE:
                0.00018500033183954656
Epoch
       49 MSE:
                0.0002930896880570799
Epoch 50 MSE:
                0.0002975177194457501
Epoch 51 MSE:
                0.00020208142814226449
Epoch 52 MSE:
                0.00011580643331399187
Epoch 53 MSE:
                0.00011124824231956154
Epoch 54 MSE:
                0.00015372459893114865
Epoch 55 MSE:
                0.00016567388956900686
Epoch
       56 MSE:
                0.00012320377572905272
Epoch
      57 MSE:
                7.126051787054166e-05
Epoch
      58 MSE:
                6.0531550843734294e-05
Epoch
      59 MSE:
                9.14981501409784e-05
       60 MSE:
Epoch
                0.00012279899965506047
Epoch
      61 MSE:
                0.00012169247929705307
Epoch 62 MSE:
                9.562201739754528e-05
       63 MSE:
Epoch
                7.57636662456207e-05
Epoch
       64 MSE:
                7.908885891083628e-05
Epoch
       65 MSE:
                9.280514495912939e-05
Epoch
      66 MSE:
                9.375505760544911e-05
Epoch
       67 MSE:
                7.628395542269573e-05
Epoch
       68 MSE:
                5.672995757777244e-05
       69 MSE:
Epoch
                5.243369014351629e-05
```

```
Epoch 70 MSE:
               6.205546378623694e-05
Epoch 71 MSE:
               6.978850433370098e-05
Epoch 72 MSE:
               6.582881906069815e-05
Epoch 73 MSE:
               5.670761311193928e-05
Epoch 74 MSE:
               5.429984230431728e-05
Epoch 75 MSE:
               6.001130532240495e-05
Epoch 76 MSE:
               6.446158658945933e-05
Epoch 77 MSE:
               6.0751444834750146e-05
Epoch 78 MSE:
               5.26848052686546e-05
Epoch 79 MSE:
               4.850115146837197e-05
Epoch 80 MSE:
               5.025079371989705e-05
Epoch 81 MSE:
               5.265421714284457e-05
Epoch 82 MSE:
               5.11282923980616e-05
Epoch 83 MSE:
               4.7349745727842674e-05
Epoch 84 MSE:
               4.5909429900348186e-05
Epoch 85 MSE:
               4.7882327635306865e-05
Epoch 86 MSE:
               4.9921971367439255e-05
Epoch 87 MSE:
               4.907139373244718e-05
Epoch 88 MSE:
               4.63221367681399e-05
Epoch 89 MSE:
               4.4675707613350824e-05
Epoch 90 MSE:
               4.5045784645481035e-05
Epoch 91 MSE:
               4.553761027636938e-05
Epoch 92 MSE:
               4.4475709728430957e-05
Epoch 93 MSE:
               4.2642328480724245e-05
Epoch 94 MSE:
               4.18883646489121e-05
Epoch 95 MSE:
               4.249874473316595e-05
Epoch 96 MSE:
               4.302180605009198e-05
Epoch 97 MSE:
               4.243283183313906e-05
Epoch 98 MSE:
               4.137313226237893e-05
Epoch 99 MSE: 4.094876567251049e-05
T-time: 3.5270230770111084
```

Train Score: 0.19 RMSE

-----Validation Score: 4.91 RMSE

Epoch 0 MSE: 0.11828106641769409
Epoch 1 MSE: 0.0916253924369812
Epoch 2 MSE: 0.06765365600585938
Epoch 3 MSE: 0.046796780079603195
Epoch 4 MSE: 0.030002595856785774
Epoch 5 MSE: 0.01999811641871929
Epoch 6 MSE: 0.02015121653676033
Epoch 7 MSE: 0.027303054928779602
Epoch 8 MSE: 0.030426036566495895
Epoch 9 MSE: 0.026394810527563095

```
Epoch
       10 MSE:
                0.0193175021559
Epoch
       11 MSE:
                0.012706698849797249
Epoch
       12 MSE:
                0.008814768865704536
       13 MSE:
Epoch
                0.006721417885273695
Epoch
       14 MSE:
                0.005563763901591301
Epoch
       15 MSE:
                0.004392965696752071
Epoch
       16 MSE:
                0.0032462840899825096
Epoch
       17 MSE:
                0.0020330650731921196
Epoch 18 MSE:
                0.0013393317349255085
Epoch
       19 MSE:
                0.0017322334460914135
       20 MSE:
                0.002439511474221945
Epoch
       21 MSE:
Epoch
                0.002229397650808096
Epoch
       22 MSE:
                0.0017954868962988257
Epoch
       23 MSE:
                0.0019241080153733492
Epoch
       24 MSE:
                0.002347873989492655
Epoch
      25 MSE:
                0.002531682373955846
Epoch
       26 MSE:
                0.002297573257237673
       27 MSE:
                0.0017996254609897733
Epoch
Epoch
       28 MSE:
                0.001335890032351017
Epoch
       29 MSE:
                0.00110893533565104
Epoch
       30 MSE:
                0.001126451650634408
       31 MSE:
Epoch
                0.0011685533681884408
       32 MSE:
Epoch
                0.0010594812920317054
       33 MSE:
Epoch
                0.0008542860159650445
Epoch
       34 MSE:
                0.0007030539563857019
Epoch
       35 MSE:
                0.0006685214466415346
       36 MSE:
Epoch
                0.0007043943624012172
Epoch
       37 MSE:
                0.000726349011529237
       38 MSE:
Epoch
                0.0006799536058679223
Epoch
       39 MSE:
                0.0005813458119519055
      40 MSE:
Epoch
                0.00047747211647219956
Epoch
       41 MSE:
                0.00038989874883554876
Epoch
       42 MSE:
                0.00033066325704567134
       43 MSE:
                0.00028203282272443175
Epoch
Epoch
       44 MSE:
                0.00022508030815515667
Epoch
       45 MSE:
                0.00016640983812976629
Epoch
       46 MSE:
                0.00013151705206837505
Epoch
       47 MSE:
                0.00013320134894456714
       48 MSE:
Epoch
                0.00015364638238679618
Epoch
       49 MSE:
                0.00015730068844277412
Epoch 50 MSE:
                0.00013224984286352992
       51 MSE:
Epoch
                0.0001031487772706896
Epoch
       52 MSE:
                9.530584793537855e-05
       53 MSE:
Epoch
                0.0001009341431199573
Epoch
       54 MSE:
                9.892565867630765e-05
Epoch
       55 MSE:
                8.688696107128635e-05
Epoch
       56 MSE:
                8.031647303141654e-05
       57 MSE:
Epoch
                8.6749299953226e-05
```

```
Epoch 58 MSE:
                9.577249875292182e-05
Epoch 59 MSE:
                9.456167026655748e-05
Epoch 60 MSE:
                8.390942093683407e-05
Epoch
      61 MSE:
                7.490302959922701e-05
Epoch
      62 MSE:
                7.348763756453991e-05
Epoch
      63 MSE:
                7.406801159959286e-05
Epoch
       64 MSE:
                6.996640149736777e-05
Epoch
      65 MSE:
                6.385231245076284e-05
Epoch 66 MSE:
                6.261254020500928e-05
Epoch 67 MSE:
                6.623404624406248e-05
Epoch
      68 MSE:
                6.819441478000954e-05
Epoch 69 MSE:
                6.521305476780981e-05
Epoch 70 MSE:
                6.0970065533183515e-05
Epoch 71 MSE:
                5.949979095021263e-05
Epoch 72 MSE:
                5.943355427007191e-05
Epoch 73 MSE:
                5.743222573073581e-05
Epoch 74 MSE:
                5.408327342593111e-05
Epoch 75 MSE:
                5.2602463256334886e-05
Epoch 76 MSE:
                5.3496543841902167e-05
Epoch 77 MSE:
                5.409671211964451e-05
Epoch
     78 MSE:
                5.2818468248005956e-05
Epoch 79 MSE:
                5.104243609821424e-05
Epoch 80 MSE:
                5.0336959247943014e-05
Epoch 81 MSE:
                5.001245153835043e-05
Epoch 82 MSE:
                4.870578777627088e-05
Epoch 83 MSE:
                4.685321982833557e-05
Epoch 84 MSE:
                4.589787567965686e-05
Epoch
      85 MSE:
                4.591439210344106e-05
Epoch 86 MSE:
                4.569891098071821e-05
Epoch 87 MSE:
                4.4794302084483206e-05
Epoch 88 MSE:
                4.3957388697890565e-05
Epoch
      89 MSE:
                4.3610274587990716e-05
Epoch 90 MSE:
                4.315172918722965e-05
Epoch 91 MSE:
                4.2159605072811246e-05
Epoch
      92 MSE:
                4.1146900912281126e-05
Epoch
      93 MSE:
                4.063700544065796e-05
Epoch 94 MSE:
                4.035217716591433e-05
Epoch 95 MSE:
                3.983163696830161e-05
Epoch
      96 MSE:
                3.919571463484317e-05
Epoch 97 MSE:
                3.8778947782702744e-05
Epoch 98 MSE:
                3.847017069347203e-05
      99 MSE:
                3.794682561419904e-05
T-time: 3.5649304389953613
```

Train Score: 0.18 RMSE

Validation Score: 1.42 RMSE

Time Step = 20 | Hidden States = 16 | Num Layers = 2

Epoch 0 MSE: 0.10661523789167404 Epoch 1 MSE: 0.04174577817320824 Epoch 2 MSE: 0.06355692446231842 Epoch 3 MSE: 0.051207415759563446 Epoch 4 MSE: 0.03490522503852844 Epoch 5 MSE: 0.03413781151175499 Epoch 6 MSE: 0.03849876672029495 Epoch 7 MSE: 0.03632911294698715 Epoch 8 MSE: 0.029340552166104317 Epoch 9 MSE: 0.024690713733434677 Epoch 10 MSE: 0.025840649381279945 Epoch 11 MSE: 0.025886939838528633 Epoch 12 MSE: 0.019996896386146545 Epoch 13 MSE: 0.014509729109704494 Epoch 14 MSE: 0.014459039084613323 Epoch 15 MSE: 0.014145593158900738 Epoch 16 MSE: 0.007502408232539892 Epoch 17 MSE: 0.0034690683241933584 Epoch 18 MSE: 0.0063647739589214325 Epoch 19 MSE: 0.0019006341462954879 Epoch 20 MSE: 0.006527863442897797 Epoch 21 MSE: 0.004894745536148548 Epoch 22 MSE: 0.0037168313283473253 Epoch 23 MSE: 0.005056479014456272 Epoch 24 MSE: 0.0013296068646013737 Epoch 25 MSE: 0.0013590173330157995 Epoch 26 MSE: 0.0026201687287539244 Epoch 27 MSE: 0.0018329037120565772 Epoch 28 MSE: 0.001132253441028297 Epoch 29 MSE: 0.0018402277491986752 Epoch 30 MSE: 0.0025750889908522367 Epoch 31 MSE: 0.0021618884056806564 Epoch 32 MSE: 0.0013628628803417087 Epoch 33 MSE: 0.001228366862051189 Epoch 34 MSE: 0.0014407708076760173 Epoch 35 MSE: 0.0011126479366794229 Epoch 36 MSE: 0.00046822914737276733 Epoch 37 MSE: 0.00046759223914705217 Epoch 38 MSE: 0.0009264703840017319 Epoch 39 MSE: 0.0008842720999382436 Epoch 40 MSE: 0.0006437855190597475 Epoch 41 MSE: 0.0008400605875067413

```
Epoch
       42 MSE:
                0.0009121146867983043
Epoch
       43 MSE:
                0.0005509936599992216
Epoch
       44 MSE:
                0.00035329931415617466
       45 MSE:
Epoch
                0.00046231536543928087
Epoch
       46 MSE:
                0.00046889655641280115
Epoch
       47 MSE:
                0.00035410383134149015
Epoch
       48 MSE:
                0.0003863151650875807
Epoch
       49 MSE:
                0.0005184028996154666
       50 MSE:
Epoch
                0.0005157889681868255
Epoch
       51 MSE:
                0.0003937056171707809
       52 MSE:
                0.00034183089155703783
Epoch
Epoch
       53 MSE:
                0.00036351734888739884
Epoch
       54 MSE:
                0.00031675983336754143
Epoch
       55 MSE:
                0.00023337073798757046
Epoch
       56 MSE:
                0.0002506514429114759
Epoch
      57 MSE:
                0.00031485315412282944
Epoch
       58 MSE:
                0.00030002035782672465
       59 MSE:
                0.00026378605980426073
Epoch
Epoch
       60 MSE:
                0.0002821263624355197
Epoch
       61 MSE:
                0.0002789911814033985
Epoch
       62 MSE:
                0.00022337798145599663
Epoch
       63 MSE:
                0.00020033807959407568
Epoch
       64 MSE:
                0.00022109370911493897
       65 MSE:
Epoch
                0.00022023373458068818
       66 MSE:
                0.00020265780040062964
Epoch
Epoch
       67 MSE:
                0.00021145553910173476
       68 MSE:
Epoch
                0.00022449909010902047
Epoch
       69 MSE:
                0.00020683534967247397
       70 MSE:
Epoch
                0.0001851048436947167
Epoch
      71 MSE:
                0.00018543635087553412
      72 MSE:
Epoch
                0.00018371152691543102
Epoch
       73 MSE:
                0.0001696461986284703
                0.00016879275790415704
Epoch
       74 MSE:
       75 MSE:
                0.000178822097950615
Epoch
Epoch
       76 MSE:
                0.00017477790242992342
Epoch
       77 MSE:
                0.0001649100158829242
Epoch
       78 MSE:
                0.00016467231034766883
Epoch
       79 MSE:
                0.0001615305955056101
       80 MSE:
Epoch
                0.00015122946933843195
Epoch
       81 MSE:
                0.00014862215903121978
       82 MSE:
                0.00015189674741122872
Epoch
Epoch
       83 MSE:
                0.00014921993715688586
Epoch
       84 MSE:
                0.00014545302838087082
       85 MSE:
Epoch
                0.00014611586811952293
Epoch
       86 MSE:
                0.0001436998718418181
Epoch
       87 MSE:
                0.0001373736304230988
Epoch
       88 MSE:
                0.00013497019244823605
       89 MSE:
                0.00013471097918227315
Epoch
```

Epoch 90 MSE: 0.00013174832565709949 Epoch 91 MSE: 0.0001299875002587214 Epoch 92 MSE: 0.00013042658974882215 Epoch 93 MSE: 0.00012822555436287075 Epoch 94 MSE: 0.00012479684664867818 Epoch 95 MSE: 0.0001234616938745603 Epoch 96 MSE: 0.00012173905997769907 Epoch 97 MSE: 0.00011908904707524925 Epoch 98 MSE: 0.00011818335769930854 Epoch 99 MSE: 0.00011765429371735081

T-time: 6.383364677429199

Train Score: 0.32 RMSE

Validation Score: 8.19 RMSE

Epoch 0 MSE: 0.050460334867239 Epoch 1 MSE: 0.034989189356565475 Epoch 2 MSE: 0.03429438918828964 Epoch 3 MSE: 0.036887023597955704 Epoch 4 MSE: 0.031412530690431595 Epoch 5 MSE: 0.02801433764398098 Epoch 6 MSE: 0.027321910485625267 Epoch 7 MSE: 0.02666962891817093 Epoch 8 MSE: 0.02450587972998619 Epoch 9 MSE: 0.021284103393554688 Epoch 10 MSE: 0.018562329933047295 Epoch 11 MSE: 0.01683441549539566 Epoch 12 MSE: 0.01416365709155798 Epoch 13 MSE: 0.009257834404706955 0.004895031917840242 Epoch 14 MSE: Epoch 15 MSE: 0.0029262336902320385 Epoch 16 MSE: 0.0010456073796376586 Epoch 17 MSE: 0.0009483190951868892 Epoch 18 MSE: 0.003917243797332048 Epoch 19 MSE: 0.004556581843644381 Epoch 20 MSE: 0.0035910664591938257 Epoch 21 MSE: 0.0035663496237248182 Epoch 22 MSE: 0.0034997796174138784 Epoch 23 MSE: 0.0024122430477291346 Epoch 24 MSE: 0.0011986178578808904 Epoch 25 MSE: 0.001135561615228653 Epoch 26 MSE: 0.0019516005413606763 Epoch 27 MSE: 0.002214355394244194 Epoch 28 MSE: 0.0018354705534875393 Epoch 29 MSE: 0.0017153358785435557

```
30 MSE:
Epoch
                0.001696425606496632
Epoch
       31 MSE:
                0.0014146118192002177
       32 MSE:
Epoch
                0.0008848285069689155
       33 MSE:
Epoch
                0.00043343991274014115
Epoch
       34 MSE:
                0.00038442673394456506
Epoch
       35 MSE:
                0.0005921105039305985
Epoch
       36 MSE:
                0.000621135113760829
Epoch
       37 MSE:
                0.0005092602223157883
      38 MSE:
Epoch
                0.0005341938813216984
Epoch
       39 MSE:
                0.0006227849517017603
       40 MSE:
                0.0005495246150530875
Epoch
      41 MSE:
Epoch
                0.0003231549635529518
Epoch
      42 MSE:
                0.00025645323330536485
Epoch
       43 MSE:
                0.0004494673339650035
Epoch
      44 MSE:
                0.0003939242160413414
Epoch 45 MSE:
                0.0002906789886765182
Epoch
       46 MSE:
                0.0003943337651435286
       47 MSE:
Epoch
                0.0004366450593806803
Epoch
       48 MSE:
                0.00028882711194455624
Epoch
       49 MSE:
                0.0002082519931718707
Epoch
       50 MSE:
                0.0002672694390639663
Epoch 51 MSE:
                0.00022971096041146666
      52 MSE:
Epoch
                0.00015256273036357015
      53 MSE:
Epoch
                0.00020900399249512702
Epoch
       54 MSE:
                0.00024668010883033276
Epoch
       55 MSE:
                0.00017789358389563859
       56 MSE:
Epoch
                0.0001605092838872224
Epoch
       57 MSE:
                0.000188265839824453
       58 MSE:
Epoch
                0.00014340148482006043
Epoch 59 MSE:
                0.0001142652181442827
       60 MSE:
Epoch
                0.00014968926552683115
Epoch
       61 MSE:
                0.00015214669110719115
       62 MSE:
Epoch
                0.00012469736975617707
       63 MSE:
                0.0001360001479042694
Epoch
Epoch
       64 MSE:
                0.00014313826977740973
Epoch
       65 MSE:
                0.00011233491386519745
Epoch
       66 MSE:
                0.0001047121622832492
Epoch
       67 MSE:
                0.00011744906078092754
       68 MSE:
Epoch
                0.0001057047993526794
Epoch
       69 MSE:
                9.938331641023979e-05
      70 MSE:
                0.00011348073167027906
Epoch
      71 MSE:
Epoch
                0.000107124142232351
Epoch
       72 MSE:
                9.44488201639615e-05
Epoch
      73 MSE:
                9.92643617792055e-05
Epoch
      74 MSE:
                9.552595292916521e-05
Epoch
       75 MSE:
                8.591597725171596e-05
Epoch
       76 MSE:
                9.111232793657109e-05
       77 MSE:
                9.317320655100048e-05
Epoch
```

```
Epoch 78 MSE: 8.627490751678124e-05
Epoch 79 MSE: 8.732575224712491e-05
Epoch 80 MSE: 8.750258712098002e-05
Epoch 81 MSE:
               8.019447705009952e-05
Epoch 82 MSE: 7.918904884718359e-05
Epoch 83 MSE:
               8.059088577283546e-05
Epoch 84 MSE:
               7.640779949724674e-05
Epoch 85 MSE:
               7.597217336297035e-05
Epoch 86 MSE: 7.682231080252677e-05
Epoch 87 MSE:
               7.258504047058523e-05
Epoch 88 MSE:
               7.064503006404266e-05
Epoch 89 MSE:
               7.031787390587851e-05
Epoch 90 MSE:
               6.693327304674312e-05
Epoch 91 MSE:
               6.578551256097853e-05
Epoch 92 MSE:
               6.586966628674418e-05
Epoch 93 MSE: 6.328550080070272e-05
Epoch 94 MSE: 6.195896276040003e-05
Epoch 95 MSE: 6.118913734098896e-05
Epoch 96 MSE: 5.850343222846277e-05
Epoch 97 MSE: 5.7181550801033154e-05
Epoch 98 MSE:
               5.637286085402593e-05
Epoch 99 MSE: 5.433464684756473e-05
```

T-time: 6.971682548522949

Train Score: 0.22 RMSE

Validation Score: 2.29 RMSE

Epoch 0 MSE: 0.04924992099404335
Epoch 1 MSE: 0.03935188427567482
Epoch 2 MSE: 0.040303975343704224
Epoch 3 MSE: 0.02297935076057911
Epoch 4 MSE: 0.0220342930406332
Epoch 5 MSE: 0.01913538947701454
Epoch 6 MSE: 0.008324443362653255
Epoch 7 MSE: 0.013593225739896297
Epoch 8 MSE: 0.003648148151114583
Epoch 9 MSE: 0.005610182415693998
Epoch 10 MSE: 0.00474493857473135
Epoch 11 MSE: 0.0020236377604305744
Epoch 12 MSE: 0.005057177972048521
Epoch 13 MSE: 0.0004919097991660237

```
Epoch
       14 MSE:
                0.001032938715070486
Epoch
       15 MSE:
                0.002619341015815735
       16 MSE:
Epoch
                0.0018473200034350157
       17 MSE:
Epoch
                0.0008685515495017171
Epoch
       18 MSE:
                0.0012045282637700438
Epoch
       19 MSE:
                0.0018448535120114684
Epoch
      20 MSE:
                0.0014675254933536053
Epoch
      21 MSE:
                0.0004653270880226046
Epoch
      22 MSE:
                0.00016472175775561482
Epoch
      23 MSE:
                0.000709800748154521
Epoch
      24 MSE:
                0.0008908883901312947
Epoch
      25 MSE:
                0.00039707613177597523
Epoch
      26 MSE:
                0.0002698904136195779
Epoch
      27 MSE:
                0.0006667573470622301
Epoch
      28 MSE:
                0.0006764447316527367
Epoch 29 MSE:
                0.0002343765809200704
Epoch
      30 MSE:
                4.825955693377182e-05
      31 MSE:
Epoch
                0.00025158311473205686
Epoch
       32 MSE:
                0.0003951620892621577
Epoch
       33 MSE:
                0.00028188308351673186
Epoch
       34 MSE:
                0.0001508542336523533
Epoch
      35 MSE:
                0.0001981045788852498
Epoch
      36 MSE:
                0.0003015433612745255
      37 MSE:
Epoch
                0.00025916521553881466
Epoch
      38 MSE:
                0.00010487875260878354
Epoch
      39 MSE:
                4.048720438731834e-05
      40 MSE:
Epoch
                0.00011774903396144509
Epoch
       41 MSE:
                0.00017496838700026274
      42 MSE:
Epoch
                0.00012146389781264588
Epoch 43 MSE:
                7.166325667640194e-05
Epoch 44 MSE:
                0.00010918559564743191
Epoch
       45 MSE:
                0.00014233472757041454
Epoch
      46 MSE:
                9.408405458088964e-05
      47 MSE:
Epoch
                3.635873144958168e-05
Epoch
       48 MSE:
                4.732000161311589e-05
Epoch
       49 MSE:
                8.677388541400433e-05
Epoch
       50 MSE:
                8.54036770761013e-05
Epoch
      51 MSE:
                5.6753891840344295e-05
Epoch
      52 MSE:
                5.340957795851864e-05
Epoch
      53 MSE:
                7.24944329704158e-05
Epoch 54 MSE:
                7.024288788670674e-05
       55 MSE:
Epoch
                4.296838233130984e-05
Epoch
       56 MSE:
                3.101639958913438e-05
Epoch
       57 MSE:
                4.664146763388999e-05
Epoch
      58 MSE:
                5.6818938901415095e-05
Epoch
       59 MSE:
                4.585751594277099e-05
Epoch
       60 MSE:
                3.8029407733120024e-05
       61 MSE:
                4.550362064037472e-05
Epoch
```

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Epoch 62 MSE:
               4.811938924831338e-05
Epoch 63 MSE:
               3.680462759803049e-05
Epoch 64 MSE:
                2.9802171411574818e-05
Epoch 65 MSE:
                3.624373857746832e-05
Epoch 66 MSE:
                4.168432133155875e-05
Epoch 67 MSE:
                3.727557123056613e-05
Epoch 68 MSE:
                3.3145439374493435e-05
Epoch 69 MSE:
                3.590529377106577e-05
Epoch 70 MSE:
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                3.241445301682688e-05
Epoch 71 MSE:
Epoch 72 MSE:
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Epoch 73 MSE:
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Epoch 74 MSE:
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Epoch 75 MSE:
                3.221450970158912e-05
Epoch 76 MSE:
                3.057930007344112e-05
Epoch 77 MSE:
                3.207412373740226e-05
Epoch 78 MSE:
                3.204312815796584e-05
Epoch 79 MSE:
                2.9541310141212307e-05
Epoch 80 MSE:
                2.896751175285317e-05
Epoch 81 MSE:
                3.072859180974774e-05
Epoch
      82 MSE:
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Epoch 83 MSE:
                2.9598399123642594e-05
Epoch 84 MSE:
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Epoch 85 MSE:
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Epoch 86 MSE:
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Epoch 87 MSE:
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Epoch 88 MSE:
                2.8746499083354138e-05
Epoch 89 MSE:
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Epoch 90 MSE:
                2.8964299417566508e-05
Epoch 91 MSE:
                2.842502908606548e-05
Epoch 92 MSE:
                2.8664655474130996e-05
Epoch 93 MSE:
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Epoch 94 MSE:
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Epoch 95 MSE:
                2.7970267183263786e-05
Epoch 96 MSE:
                2.8341697543510236e-05
Epoch 97 MSE:
                2.8267773814150132e-05
Epoch 98 MSE:
                2.7898326152353548e-05
Epoch 99 MSE:
                2.7893829610547982e-05
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T-time: 6.775812149047852

Train Score: 0.16 RMSE

----Validation Score: 3.24 RMSE

Epoch 0 MSE: 0.04200812801718712 Epoch 1 MSE: 0.041303642094135284

```
Epoch 2 MSE:
               0.032244350761175156
Epoch
       3 MSE:
               0.03061683289706707
Epoch
      4 MSE:
               0.029338615015149117
       5 MSE:
Epoch
               0.024828260764479637
Epoch
       6 MSE:
               0.022728214040398598
Epoch 7 MSE:
               0.02093980461359024
Epoch
       8 MSE:
               0.01639198698103428
Epoch
      9 MSE:
               0.012856408953666687
Epoch 10 MSE:
                0.01098731067031622
Epoch
       11 MSE:
                0.00614006444811821
Epoch
       12 MSE:
                0.0027352492325007915
Epoch
       13 MSE:
                0.0012241005897521973
Epoch
       14 MSE:
                0.0013187754666432738
Epoch
       15 MSE:
                0.004542363807559013
Epoch
       16 MSE:
                0.004638268146663904
Epoch 17 MSE:
                0.002477741800248623
Epoch
       18 MSE:
                0.00070976372808218
       19 MSE:
Epoch
                0.0005057586822658777
Epoch
       20 MSE:
                0.0009146146476268768
Epoch
       21 MSE:
                0.0015810279874131083
Epoch
       22 MSE:
                0.002143273362889886
Epoch
       23 MSE:
                0.002165901707485318
Epoch
       24 MSE:
                0.0017459222581237555
       25 MSE:
Epoch
                0.0011546985479071736
Epoch
       26 MSE:
                0.000647310575004667
Epoch
       27 MSE:
                0.0003062535251956433
       28 MSE:
Epoch
                0.00023943002452142537
Epoch
       29 MSE:
                0.0005018288502469659
       30 MSE:
Epoch
                0.0008268079254776239
Epoch
       31 MSE:
                0.0009180511115118861
       32 MSE:
Epoch
                0.0007044993690215051
Epoch
       33 MSE:
                0.0004274067177902907
Epoch
       34 MSE:
                0.0002833798062056303
       35 MSE:
                0.00017133541405200958
Epoch
Epoch
       36 MSE:
                0.00022647541482001543
Epoch
       37 MSE:
                0.0003847816842608154
Epoch
       38 MSE:
                0.00044236532994545996
Epoch
       39 MSE:
                0.00041256501572206616
       40 MSE:
Epoch
                0.0003714552440214902
Epoch
       41 MSE:
                0.0002732824650593102
       42 MSE:
                0.00014390099386218935
Epoch
       43 MSE:
Epoch
                0.00010680349805625156
Epoch
       44 MSE:
                0.0001355912972940132
Epoch
       45 MSE:
                0.00016271173080895096
Epoch
       46 MSE:
                0.0002129539498127997
Epoch
       47 MSE:
                0.00021494909015018493
       48 MSE:
Epoch
                0.00014768137771170586
       49 MSE:
                0.00010209988977294415
Epoch
```

```
Epoch 50 MSE:
                7.439241016982123e-05
Epoch
      51 MSE:
                6.566826050402597e-05
                9.892202069750056e-05
Epoch
      52 MSE:
Epoch
      53 MSE:
                0.0001225466694450006
Epoch
      54 MSE:
                0.00011759264452848583
Epoch
      55 MSE:
                0.00010707147885113955
Epoch
       56 MSE:
                7.957035268191248e-05
Epoch
      57 MSE:
                5.19972454640083e-05
Epoch 58 MSE:
                5.325765232555568e-05
Epoch
      59 MSE:
                6.144004873931408e-05
Epoch
       60 MSE:
                7.186339644249529e-05
Epoch
      61 MSE:
                8.068101305980235e-05
Epoch
      62 MSE:
                6.738259980920702e-05
Epoch
       63 MSE:
                5.317795876180753e-05
Epoch
      64 MSE:
                4.486439866013825e-05
Epoch 65 MSE:
                4.06379513151478e-05
Epoch
      66 MSE:
                4.912765507469885e-05
      67 MSE:
Epoch
                5.444547423394397e-05
Epoch
       68 MSE:
                5.312324356054887e-05
Epoch
       69 MSE:
                4.961947342962958e-05
Epoch
      70 MSE:
                4.0186936530517414e-05
Epoch
      71 MSE:
                3.578089672373608e-05
Epoch 72 MSE:
                3.6929264751961455e-05
Epoch 73 MSE:
                3.872512388625182e-05
Epoch 74 MSE:
                4.241391798132099e-05
Epoch 75 MSE:
                4.025400266982615e-05
Epoch 76 MSE:
                3.61915044777561e-05
Epoch
     77 MSE:
                3.3015909139066935e-05
Epoch 78 MSE:
                3.085485514020547e-05
Epoch 79 MSE:
                3.2885076507227495e-05
Epoch 80 MSE:
                3.387661854503676e-05
Epoch
      81 MSE:
                3.395384919713251e-05
Epoch
      82 MSE:
                3.2461048249388114e-05
      83 MSE:
Epoch
                2.951495480374433e-05
Epoch
       84 MSE:
                2.8619238946703263e-05
Epoch
      85 MSE:
                2.8258085876586847e-05
Epoch
      86 MSE:
                2.9207138140918687e-05
Epoch
      87 MSE:
                2.9435073884087615e-05
Epoch
      88 MSE:
                2.834838960552588e-05
Epoch
      89 MSE:
                2.7178419259143993e-05
Epoch 90 MSE:
                2.578320163593162e-05
Epoch
      91 MSE:
                2.5805304176174104e-05
Epoch
      92 MSE:
                2.589634823380038e-05
Epoch
      93 MSE:
                2.601892083475832e-05
Epoch
      94 MSE:
                2.5525980163365602e-05
Epoch
       95 MSE:
                2.452164153510239e-05
Epoch
      96 MSE:
                2.3915854399092495e-05
      97 MSE:
                2.347132067370694e-05
Epoch
```

Epoch 98 MSE: 2.3647633497603238e-05 Epoch 99 MSE: 2.3491549654863775e-05

T-time: 7.229863882064819

Train Score: 0.14 RMSE

Validation Score: 1.80 RMSE

Time Step = 20 | Hidden States = 32 | Num Layers = 2

```
Epoch 0 MSE: 0.056970253586769104
Epoch 1 MSE: 0.1911926120519638
Epoch 2 MSE: 0.03376320004463196
Epoch 3 MSE: 0.05331186205148697
Epoch 4 MSE: 0.05366164818406105
Epoch 5 MSE: 0.03524738550186157
Epoch 6 MSE: 0.026686394587159157
Epoch 7 MSE: 0.036526598036289215
Epoch 8 MSE: 0.03493746370077133
Epoch 9 MSE: 0.023316720500588417
Epoch 10 MSE: 0.019105277955532074
Epoch 11 MSE: 0.02097022905945778
Epoch 12 MSE: 0.0199042409658432
Epoch 13 MSE:
               0.012191840447485447
Epoch 14 MSE:
               0.0045249005779623985
Epoch 15 MSE:
               0.00877147726714611
Epoch 16 MSE:
               0.00432552769780159
Epoch 17 MSE:
               0.004425468388944864
Epoch 18 MSE:
               0.008806100115180016
Epoch 19 MSE:
               0.002310869749635458
Epoch 20 MSE:
               0.0013006668305024505
Epoch 21 MSE:
               0.0030225254595279694
Epoch 22 MSE:
               0.0021974050905555487
Epoch 23 MSE:
               0.0013384524499997497
Epoch 24 MSE:
               0.0019242720445618033
Epoch 25 MSE:
               0.0027942671440541744
Epoch 26 MSE:
               0.002754766959697008
Epoch 27 MSE:
               0.0018096350831910968
Epoch 28 MSE:
               0.0008815072942525148
Epoch 29 MSE:
               0.0007469786214642227
Epoch 30 MSE:
               0.0010597031796351075
Epoch 31 MSE:
               0.000892339798156172
Epoch 32 MSE:
               0.00039781330269761384
Epoch 33 MSE: 0.00048282466013915837
```

```
Epoch
       34 MSE:
                0.001029693754389882
Epoch
       35 MSE:
                0.0011278789024800062
      36 MSE:
Epoch
                0.0006542145856656134
      37 MSE:
Epoch
                0.00031448554364033043
Epoch
       38 MSE:
                0.00039737633778713644
Epoch
      39 MSE:
                0.0004858626634813845
Epoch
       40 MSE:
                0.00034067235537804663
Epoch
      41 MSE:
                0.00022168623399920762
Epoch 42 MSE:
                0.00032317914883606136
Epoch
      43 MSE:
                0.0004888514522463083
      44 MSE:
                0.0004947244888171554
Epoch
Epoch 45 MSE:
                0.00034220388624817133
Epoch 46 MSE:
                0.00021591942640952766
Epoch
      47 MSE:
                0.00022111267026048154
Epoch
      48 MSE:
                0.00025528506375849247
Epoch 49 MSE:
                0.00020205069449730217
Epoch 50 MSE:
                0.0001330822124145925
      51 MSE:
Epoch
                0.0001653981307754293
Epoch
      52 MSE:
                0.00024675531312823296
Epoch
      53 MSE:
                0.00024908603518269956
Epoch
       54 MSE:
                0.00017622682207729667
Epoch 55 MSE:
                0.00013453704013954848
Epoch 56 MSE:
                0.00015027205517981201
Epoch 57 MSE:
                0.00015270814765244722
Epoch
      58 MSE:
                0.0001196306839119643
Epoch
      59 MSE:
                0.00010620835382724181
      60 MSE:
Epoch
                0.0001340700255241245
Epoch
       61 MSE:
                0.00015705334953963757
      62 MSE:
Epoch
                0.00014121457934379578
Epoch 63 MSE:
                0.000112436871859245
      64 MSE:
Epoch
                0.00010648910392774269
Epoch
       65 MSE:
                0.0001131597236962989
Epoch
       66 MSE:
                0.00010456813470227644
      67 MSE:
Epoch
                8.9433575340081e-05
Epoch
       68 MSE:
                9.313509508501738e-05
Epoch
       69 MSE:
                0.0001078492496162653
Epoch
     70 MSE:
                0.0001076403641491197
Epoch 71 MSE:
                9.39735837164335e-05
Epoch 72 MSE:
                8.782622899161652e-05
Epoch
      73 MSE:
                9.061737364390865e-05
Epoch 74 MSE:
                8.773257286520675e-05
Epoch
     75 MSE:
                8.004865958355367e-05
Epoch
      76 MSE:
                8.0097459431272e-05
      77 MSE:
Epoch
                8.632185199530795e-05
Epoch
      78 MSE:
                8.673310367157683e-05
Epoch
      79 MSE:
                8.063855057116598e-05
       80 MSE:
Epoch
                7.733948586974293e-05
       81 MSE:
Epoch
                7.81349663157016e-05
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Epoch 82 MSE: 7.639620889676735e-05 Epoch 83 MSE: 7.239690603455529e-05 Epoch 84 MSE: 7.219724648166448e-05 Epoch 85 MSE: 7.47850863263011e-05 Epoch 86 MSE: 7.426457887049764e-05 Epoch 87 MSE: 7.111026934580877e-05 Epoch 88 MSE: 6.985195796005428e-05 Epoch 89 MSE: 6.990742986090481e-05 Epoch 90 MSE: 6.824899173807353e-05 Epoch 91 MSE: 6.633659359067678e-05 Epoch 92 MSE: 6.662202213192359e-05 Epoch 93 MSE: 6.730416498612612e-05 Epoch 94 MSE: 6.616158498218283e-05 Epoch 95 MSE: 6.461789598688483e-05 Epoch 96 MSE: 6.420546560548246e-05 Epoch 97 MSE: 6.368995673255995e-05 Epoch 98 MSE: 6.23539017396979e-05 Epoch 99 MSE: 6.16145262029022e-05

T-time: 15.115833759307861

Train Score: 0.23 RMSE

Validation Score: 6.11 RMSE

Epoch 0 MSE: 0.08024495095014572 Epoch 1 MSE: 0.03558538109064102 Epoch 2 MSE: 0.0503331758081913 Epoch 3 MSE: 0.04169435054063797 Epoch 4 MSE: 0.03350633382797241 Epoch 5 MSE: 0.031117025762796402 Epoch 6 MSE: 0.031270455569028854 Epoch 7 MSE: 0.03104744292795658 Epoch 8 MSE: 0.029027357697486877 Epoch 9 MSE: 0.02533632703125477 Epoch 10 MSE: 0.021798761561512947 Epoch 11 MSE: 0.02015637420117855 Epoch 12 MSE: 0.0201789028942585 Epoch 13 MSE: 0.014230762608349323 Epoch 14 MSE: 0.008676717057824135 Epoch 15 MSE: 0.006079191341996193 Epoch 16 MSE: 0.003683346090838313 Epoch 17 MSE: 0.0006208492559380829 Epoch 18 MSE: 0.004154627211391926 Epoch 19 MSE: 0.004882219713181257 Epoch 20 MSE: 0.002827702322974801 Epoch 21 MSE: 0.003504342632368207

```
Epoch 22 MSE:
                0.0034184579271823168
Epoch
      23 MSE:
                0.0017453309847041965
      24 MSE:
Epoch
                0.0005337395123206079
      25 MSE:
Epoch
                0.0013181816320866346
Epoch
      26 MSE:
                0.002431813394650817
Epoch
      27 MSE:
                0.002032879274338484
Epoch
      28 MSE:
                0.0012406788300722837
Epoch
      29 MSE:
                0.001183325075544417
Epoch 30 MSE:
                0.0014736357843503356
Epoch
      31 MSE:
                0.0013759627472609282
Epoch
      32 MSE:
                0.0007443660870194435
Epoch
      33 MSE:
                0.00014996422396507114
Epoch
      34 MSE:
                0.00028573846793733537
Epoch
      35 MSE:
                0.0007765700574964285
Epoch
      36 MSE:
                0.000618414138443768
Epoch 37 MSE:
                0.00021101327729411423
Epoch
      38 MSE:
                0.0002916563826147467
      39 MSE:
                0.0005375298205763102
Epoch
Epoch
       40 MSE:
                0.0004483023367356509
Epoch
      41 MSE:
                0.00012213132868055254
Epoch
       42 MSE:
                0.0001581912365509197
Epoch 43 MSE:
                0.00046684592962265015
Epoch 44 MSE:
                0.00022419630840886384
Epoch 45 MSE:
                8.901473484002054e-05
Epoch 46 MSE:
                0.00025506390375085175
Epoch 47 MSE:
                0.0002659439924173057
Epoch 48 MSE:
                0.00010108391870744526
Epoch
       49 MSE:
                5.79161242058035e-05
Epoch 50 MSE:
                0.00018963411275763065
Epoch 51 MSE:
                0.0001914934255182743
Epoch 52 MSE:
                6.727626896463335e-05
Epoch 53 MSE:
                6.736813520547003e-05
Epoch 54 MSE:
                0.0001427126699127257
Epoch 55 MSE:
                0.0001256572868442163
Epoch
       56 MSE:
                4.880207052337937e-05
Epoch
      57 MSE:
                5.5134787544375286e-05
Epoch
      58 MSE:
                0.00011268393427599221
Epoch
      59 MSE:
                9.053738176589832e-05
Epoch
       60 MSE:
                4.051646828884259e-05
Epoch
      61 MSE:
                5.857679934706539e-05
Epoch 62 MSE:
                8.658769365865737e-05
       63 MSE:
Epoch
                6.191692227730528e-05
Epoch
       64 MSE:
                3.3862317650346085e-05
Epoch
      65 MSE:
                5.3126677812542766e-05
Epoch
      66 MSE:
                6.932936230441555e-05
Epoch
       67 MSE:
                4.5448698074324057e-05
Epoch
       68 MSE:
                3.396104875719175e-05
       69 MSE:
Epoch
                5.025982318329625e-05
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Epoch 70 MSE: 5.2327803132357076e-05
Epoch 71 MSE: 3.4172127925558016e-05
               3.1567116820951924e-05
Epoch 72 MSE:
Epoch 73 MSE:
               4.456937676877715e-05
Epoch 74 MSE:
               3.967718657804653e-05
Epoch 75 MSE:
               2.7792331820819527e-05
Epoch 76 MSE:
               3.262158497818746e-05
Epoch 77 MSE:
               3.765518340514973e-05
Epoch 78 MSE:
               2.936461714853067e-05
Epoch 79 MSE:
               2.48701217060443e-05
Epoch 80 MSE:
               3.105514406342991e-05
Epoch 81 MSE:
               3.0276685720309615e-05
Epoch 82 MSE:
               2.3680069716647267e-05
Epoch 83 MSE:
               2.5393228497705422e-05
Epoch 84 MSE:
               2.8241129257366993e-05
Epoch 85 MSE:
               2.3966947992448695e-05
Epoch 86 MSE:
               2.1963602193864062e-05
Epoch 87 MSE:
               2.5264771466027014e-05
Epoch 88 MSE:
               2.4164741262211464e-05
Epoch 89 MSE:
               2.1144418496987782e-05
Epoch 90 MSE:
               2.2795939003117383e-05
Epoch 91 MSE:
               2.3507613150286488e-05
Epoch 92 MSE:
               2.094406409014482e-05
Epoch 93 MSE:
               2.10711732506752e-05
Epoch 94 MSE:
               2.2501160856336355e-05
Epoch 95 MSE:
               2.1023724912083708e-05
Epoch 96 MSE:
               2.0319546820246615e-05
Epoch 97 MSE:
               2.1516820197575726e-05
Epoch 98 MSE:
               2.0886549464194104e-05
Epoch 99 MSE: 1.986884126381483e-05
T-time: 15.113189697265625
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Train Score: 0.13 RMSE Validation Score: 0.83 RMSE _____

_____ Time Step = 30 | Hidden States = 2 | Num Layers = 1 ______

Epoch 0 MSE: 0.31168508529663086 Epoch 1 MSE: 0.27456560730934143 Epoch 2 MSE: 0.24024991691112518 Epoch 3 MSE: 0.20876213908195496 Epoch 4 MSE: 0.18007436394691467 Epoch 5 MSE: 0.15411125123500824

```
6 MSE: 0.13075850903987885
Epoch
Epoch
       7 MSE:
               0.10987623780965805
      8 MSE:
Epoch
               0.09131525456905365
Epoch
       9 MSE:
               0.07493362575769424
Epoch
       10 MSE:
                0.06060963496565819
Epoch
       11 MSE:
                0.04824777692556381
Epoch
       12 MSE:
                0.03777685761451721
Epoch
       13 MSE:
                0.029141167178750038
Epoch 14 MSE:
                0.02228713035583496
Epoch
       15 MSE:
                0.01714821718633175
       16 MSE:
                0.013630237430334091
Epoch
       17 MSE:
Epoch
                0.011598894372582436
Epoch
       18 MSE:
                0.010870971716940403
Epoch
       19 MSE:
                0.011211185716092587
Epoch
       20 MSE:
                0.01233710814267397
Epoch
      21 MSE:
                0.013934272341430187
Epoch
       22 MSE:
                0.015681486576795578
       23 MSE:
Epoch
                0.017282895743846893
Epoch
       24 MSE:
                0.018499862402677536
Epoch
       25 MSE:
                0.019174590706825256
Epoch
       26 MSE:
                0.019239777699112892
      27 MSE:
Epoch
                0.018713122233748436
Epoch
      28 MSE:
                0.017680007964372635
       29 MSE:
Epoch
                0.0162697434425354
Epoch
       30 MSE:
                0.014630894176661968
Epoch
       31 MSE:
                0.012909626588225365
       32 MSE:
Epoch
                0.011233431287109852
Epoch
       33 MSE:
                0.00970096793025732
       34 MSE:
Epoch
                0.008377757854759693
Epoch
      35 MSE:
                0.007296719588339329
       36 MSE:
Epoch
                0.006462176330387592
Epoch
       37 MSE:
                0.005855931434780359
Epoch
       38 MSE:
                0.005444129463285208
       39 MSE:
Epoch
                0.0051839472725987434
Epoch
       40 MSE:
                0.005029417108744383
Epoch
       41 MSE:
                0.004936083219945431
Epoch
       42 MSE:
                0.004864392336457968
Epoch
       43 MSE:
                0.004781894385814667
       44 MSE:
Epoch
                0.004664415493607521
Epoch
       45 MSE:
                0.004496401641517878
Epoch 46 MSE:
                0.00427062576636672
       47 MSE:
Epoch
                0.003987395204603672
Epoch
       48 MSE:
                0.0036534196697175503
       49 MSE:
Epoch
                0.0032804158981889486
Epoch
       50 MSE:
                0.002883554669097066
Epoch
       51 MSE:
                0.002479822840541601
Epoch
       52 MSE:
                0.0020863921381533146
       53 MSE:
                0.001719071064144373
Epoch
```

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Epoch 54 MSE:
                0.0013909544795751572
Epoch 55 MSE:
                0.0011113676009699702
Epoch 56 MSE:
                0.0008851917809806764
Epoch 57 MSE:
                0.0007126688142307103
Epoch 58 MSE:
                0.0005896961665712297
Epoch 59 MSE:
                0.0005086007295176387
Epoch
      60 MSE:
                0.00045930681517347693
Epoch 61 MSE:
                0.000430730520747602
Epoch 62 MSE:
                0.0004122164682485163
Epoch 63 MSE:
                0.00039480888517573476
Epoch 64 MSE:
                0.00037216063356027007
Epoch 65 MSE:
                0.00034097599564120173
Epoch
      66 MSE:
                0.0003009497304446995
Epoch
      67 MSE:
                0.0002542562724556774
Epoch 68 MSE:
                0.00020473428594414145
Epoch 69 MSE:
                0.0001569174783071503
Epoch 70 MSE:
                0.00011511743650771677
Epoch 71 MSE:
                8.267835801234469e-05
Epoch 72 MSE:
                6.151025445433334e-05
Epoch 73 MSE:
                5.192918251850642e-05
Epoch 74 MSE:
                5.2779818361159414e-05
Epoch 75 MSE:
                6.177167233545333e-05
Epoch 76 MSE:
               7.594375347252935e-05
Epoch 77 MSE:
                9.216120088240132e-05
Epoch 78 MSE:
                0.00010756459960248321
Epoch 79 MSE:
                0.00011991443170700222
Epoch 80 MSE:
                0.0001277897390536964
Epoch 81 MSE:
                0.00013064574159216136
Epoch 82 MSE:
                0.00012873536616098136
Epoch 83 MSE:
                0.0001229317713296041
Epoch 84 MSE:
                0.00011449122393969446
Epoch 85 MSE:
                0.00010479826596565545
Epoch 86 MSE:
                9.51367401285097e-05
Epoch 87 MSE:
                8.65132751641795e-05
Epoch
      88 MSE:
                7.955395267345011e-05
Epoch
      89 MSE:
                7.447881944244727e-05
Epoch 90 MSE:
                7.114611798897386e-05
Epoch 91 MSE:
                6.914885307196528e-05
Epoch 92 MSE:
                6.793917418690398e-05
Epoch 93 MSE:
                6.695430784020573e-05
Epoch 94 MSE:
                6.572438724106178e-05
Epoch 95 MSE:
                6.394410593202338e-05
Epoch
      96 MSE:
                6.150191620690748e-05
Epoch
      97 MSE:
                5.8470290241530165e-05
Epoch
      98 MSE:
                5.5061984312487766e-05
Epoch
      99 MSE:
                5.1569331844802946e-05
T-time: 3.420062780380249
```

Train Score: 0.21 RMSE

Validation Score: 7.22 RMSE

Epoch 0 MSE: 0.38266265392303467 Epoch 1 MSE: 0.35195863246917725 Epoch 2 MSE: 0.32383808493614197 Epoch 3 MSE: 0.2980961501598358 Epoch 4 MSE: 0.27448973059654236 Epoch 5 MSE: 0.2528187036514282 Epoch 6 MSE: 0.23289845883846283 Epoch 7 MSE: 0.214585542678833 Epoch 8 MSE: 0.19774752855300903 Epoch 9 MSE: 0.18226271867752075 Epoch 10 MSE: 0.16802451014518738 Epoch 11 MSE: 0.15493610501289368 Epoch 12 MSE: 0.14290781319141388 Epoch 13 MSE: 0.13185574114322662 Epoch 14 MSE: 0.12170173972845078 Epoch 15 MSE: 0.11248093098402023 Epoch 16 MSE: 0.10680723935365677 Epoch 17 MSE: 0.10182614624500275 Epoch 18 MSE: 0.0972568616271019 Epoch 19 MSE: 0.09299106150865555 Epoch 20 MSE: 0.08897912502288818 Epoch 21 MSE: 0.08518989384174347 Epoch 22 MSE: 0.08159173280000687 Epoch 23 MSE: 0.07815733551979065 0.07487098127603531 Epoch 24 MSE: Epoch 25 MSE: 0.07171671837568283 0.06868162751197815 Epoch 26 MSE: Epoch 27 MSE: 0.06575493514537811 Epoch 28 MSE: 0.06292213499546051 Epoch 29 MSE: 0.06016519293189049 Epoch 30 MSE: 0.057471033185720444 Epoch 31 MSE: 0.0548233799636364 Epoch 32 MSE: 0.05220571905374527 Epoch 33 MSE: 0.049608826637268066 Epoch 34 MSE: 0.0470266155898571 Epoch 35 MSE: 0.044452082365751266 Epoch 36 MSE: 0.0418827086687088 Epoch 37 MSE: 0.03932345286011696 Epoch 38 MSE: 0.036787234246730804 Epoch 39 MSE: 0.03429880738258362 Epoch 40 MSE: 0.031914498656988144 Epoch 41 MSE: 0.02969176694750786

```
Epoch
       42 MSE:
                0.028321411460638046
Epoch
       43 MSE:
                0.02701745741069317
Epoch
       44 MSE:
                0.025081971660256386
       45 MSE:
Epoch
                0.022660011425614357
Epoch
       46 MSE:
                0.02073844149708748
Epoch
       47 MSE:
                0.019181950017809868
Epoch
       48 MSE:
                0.017726240679621696
Epoch
       49 MSE:
                0.016349611803889275
Epoch 50 MSE:
                0.015055852942168713
Epoch
      51 MSE:
                0.013854077085852623
       52 MSE:
Epoch
                0.012753374874591827
Epoch
       53 MSE:
                0.011765990406274796
Epoch
       54 MSE:
                0.010899057611823082
Epoch
       55 MSE:
                0.010146597400307655
Epoch
       56 MSE:
                0.009485355578362942
Epoch 57 MSE:
                0.008878380991518497
Epoch
       58 MSE:
                0.008289773017168045
       59 MSE:
Epoch
                0.0077028656378388405
Epoch
       60 MSE:
                0.007125951815396547
Epoch
       61 MSE:
                0.006581561174243689
Epoch
       62 MSE:
                0.0060911462642252445
Epoch
       63 MSE:
                0.005662973970174789
Epoch
       64 MSE:
                0.005290942266583443
       65 MSE:
Epoch
                0.004959005396813154
Epoch
       66 MSE:
                0.004648585803806782
Epoch
       67 MSE:
                0.004345317836850882
       68 MSE:
Epoch
                0.004042737185955048
Epoch
       69 MSE:
                0.003742291359230876
       70 MSE:
Epoch
                0.0034504481591284275
Epoch
      71 MSE:
                0.003176299622282386
      72 MSE:
Epoch
                0.0029254057444632053
Epoch
      73 MSE:
                0.002700744429603219
Epoch
      74 MSE:
                0.002497768262401223
       75 MSE:
Epoch
                0.002307020127773285
Epoch
       76 MSE:
                0.00211971253156662
Epoch
       77 MSE:
                0.001932691317051649
Epoch
      78 MSE:
                0.001750380964949727
Epoch
       79 MSE:
                0.0015790832694619894
       80 MSE:
Epoch
                0.001422844361513853
Epoch
       81 MSE:
                0.0012830429477617145
       82 MSE:
Epoch
                0.0011580577120184898
       83 MSE:
Epoch
                0.0010448535904288292
Epoch
       84 MSE:
                0.0009409801568835974
Epoch
       85 MSE:
                0.0008450758177787066
Epoch
       86 MSE:
                0.0007574601913802326
Epoch
       87 MSE:
                0.0006799767725169659
Epoch
       88 MSE:
                0.0006137228338047862
       89 MSE:
                0.0005636896821670234
Epoch
```

```
Epoch 90 MSE: 0.0005563280428759754
Epoch 91 MSE: 0.0005457653314806521
Epoch 92 MSE:
               0.0005026151775382459
Epoch 93 MSE:
               0.0004431274428498
Epoch 94 MSE:
               0.00039602129254490137
Epoch 95 MSE:
               0.00037403954775072634
Epoch 96 MSE:
               0.000359276426024735
Epoch 97 MSE:
               0.00033499120036140084
Epoch 98 MSE:
               0.00030119094299152493
Epoch 99 MSE:
               0.0002657509467098862
```

T-time: 3.6822509765625

Train Score: 0.49 RMSE

_____ Validation Score: 1.16 RMSE _____

______ Time Step = 30 | Hidden States = 2 | Num Layers = 2 _____

```
Epoch 0 MSE: 0.3222784698009491
Epoch 1 MSE: 0.27903011441230774
Epoch 2 MSE: 0.2403552383184433
Epoch 3 MSE: 0.20586763322353363
Epoch 4 MSE: 0.17493769526481628
Epoch 5 MSE: 0.14693357050418854
Epoch 6 MSE: 0.12152116000652313
Epoch 7 MSE: 0.0986960232257843
Epoch 8 MSE: 0.07864818722009659
Epoch 9 MSE: 0.06164006143808365
Epoch 10 MSE: 0.047922611236572266
Epoch 11 MSE: 0.03766923397779465
Epoch 12 MSE:
               0.03091660514473915
Epoch 13 MSE:
               0.027512596920132637
Epoch 14 MSE:
               0.027078993618488312
Epoch 15 MSE:
               0.029002685099840164
Epoch 16 MSE:
               0.032473087310791016
Epoch 17 MSE:
               0.036580394953489304
Epoch 18 MSE:
               0.04046371951699257
Epoch 19 MSE:
               0.043457671999931335
Epoch 20 MSE:
               0.045175403356552124
Epoch 21 MSE:
               0.045508697628974915
Epoch 22 MSE:
               0.04457128420472145
Epoch 23 MSE:
               0.042622800916433334
Epoch 24 MSE:
               0.03999623656272888
Epoch 25 MSE: 0.03703851252794266
```

```
Epoch
       26 MSE:
                0.03406589478254318
Epoch
       27 MSE:
                0.03133401274681091
Epoch
       28 MSE:
                0.02902158722281456
       29 MSE:
Epoch
                0.027226630598306656
Epoch
       30 MSE:
                0.02597273513674736
Epoch
       31 MSE:
                0.02522278018295765
Epoch
       32 MSE:
                0.02489646151661873
Epoch
       33 MSE:
                0.024888429790735245
Epoch 34 MSE:
                0.025084668770432472
Epoch
       35 MSE:
                0.025375591591000557
       36 MSE:
                0.025665320456027985
Epoch
       37 MSE:
Epoch
                0.02587750181555748
Epoch
       38 MSE:
                0.025957979261875153
       39 MSE:
Epoch
                0.02587508223950863
Epoch
       40 MSE:
                0.025618206709623337
Epoch 41 MSE:
                0.02519499510526657
Epoch
       42 MSE:
                0.02462778426706791
       43 MSE:
                0.02394939959049225
Epoch
Epoch
       44 MSE:
                0.023198718205094337
Epoch
       45 MSE:
                0.02241622842848301
Epoch
       46 MSE:
                0.021639754995703697
Epoch
      47 MSE:
                0.020900791510939598
Epoch 48 MSE:
                0.02022155374288559
      49 MSE:
Epoch
                0.01961315982043743
Epoch
       50 MSE:
                0.019075099378824234
Epoch
       51 MSE:
                0.018596109002828598
       52 MSE:
Epoch
                0.018156398087739944
Epoch
       53 MSE:
                0.01773100718855858
       54 MSE:
Epoch
                0.017293816432356834
Epoch 55 MSE:
                0.016821658238768578
                0.01629786379635334
Epoch 56 MSE:
Epoch
       57 MSE:
                0.01571468450129032
      58 MSE:
Epoch
                0.015074198134243488
       59 MSE:
                0.014387557283043861
Epoch
Epoch
       60 MSE:
                0.013672742061316967
Epoch
       61 MSE:
                0.012951231561601162
Epoch
       62 MSE:
                0.012244228273630142
Epoch
       63 MSE:
                0.011569015681743622
       64 MSE:
Epoch
                0.010936169885098934
Epoch
       65 MSE:
                0.010348048061132431
       66 MSE:
Epoch
                0.00979889277368784
       67 MSE:
Epoch
                0.009276563301682472
Epoch
       68 MSE:
                0.00876565370708704
       69 MSE:
Epoch
                0.008251437917351723
Epoch
      70 MSE:
                0.007723853457719088
Epoch
       71 MSE:
                0.007180573884397745
Epoch
       72 MSE:
                0.006628320552408695
       73 MSE:
                0.006081819999963045
Epoch
```

```
Epoch 74 MSE:
                0.005560470279306173
Epoch 75 MSE:
                0.005083424970507622
Epoch 76 MSE:
                0.004664478357881308
Epoch 77 MSE:
                0.00430850638076663
Epoch 78 MSE:
                0.004010898061096668
Epoch 79 MSE:
                0.0037604928947985172
Epoch 80 MSE:
                0.0035450102295726538
Epoch 81 MSE:
                0.0033566260244697332
Epoch 82 MSE:
                0.0031949032563716173
Epoch 83 MSE:
                0.0030653178691864014
Epoch 84 MSE:
                0.002973916009068489
Epoch 85 MSE:
                0.002921041799709201
Epoch 86 MSE:
                0.0028981263749301434
Epoch 87 MSE:
                0.002889992669224739
Epoch 88 MSE:
                0.0028815821278840303
Epoch 89 MSE:
                0.002864730777218938
Epoch 90 MSE:
                0.0028403496835380793
Epoch 91 MSE:
                0.0028147203847765923
Epoch 92 MSE:
                0.0027929143980145454
Epoch 93 MSE:
                0.002774246269837022
Epoch 94 MSE:
                0.002752674510702491
Epoch 95 MSE:
                0.002721215831115842
Epoch 96 MSE:
                0.0026766755618155003
Epoch 97 MSE:
                0.002621361520141363
Epoch 98 MSE:
                0.002561075845733285
Epoch 99 MSE:
                0.0025013568811118603
```

T-time: 5.778496265411377

Train Score: 1.49 RMSE

-----Validation Score: 18.77 RMSE

Epoch 0 MSE: 0.29807865619659424 Epoch 1 MSE: 0.2621855139732361 Epoch 2 MSE: 0.22666998207569122 Epoch 3 MSE: 0.1917477548122406 Epoch 4 MSE: 0.15778708457946777 Epoch 5 MSE: 0.12516888976097107 Epoch 6 MSE: 0.09433102607727051 Epoch 7 MSE: 0.06483282148838043 Epoch 8 MSE: 0.038022931665182114 Epoch 9 MSE: 0.01695605181157589 Epoch 10 MSE: 0.0038654657546430826 Epoch 11 MSE: 0.0014090311015024781 Epoch 12 MSE: 0.010699622333049774 13 MSE: 0.02510492503643036 Epoch

```
Epoch
       14 MSE:
                0.03396249935030937
Epoch
       15 MSE:
                0.03449345752596855
       16 MSE:
Epoch
                0.02924114465713501
       17 MSE:
Epoch
                0.02175324410200119
Epoch
       18 MSE:
                0.014597320929169655
Epoch
       19 MSE:
                0.009082449600100517
Epoch
       20 MSE:
                0.005619177594780922
Epoch
       21 MSE:
                0.004042669665068388
Epoch
       22 MSE:
                0.003924746997654438
Epoch
       23 MSE:
                0.004770132713019848
Epoch
       24 MSE:
                0.006106595043092966
Epoch
       25 MSE:
                0.0075356061570346355
Epoch
       26 MSE:
                0.008718141354620457
Epoch
       27 MSE:
                0.009523543529212475
Epoch
       28 MSE:
                0.00991413090378046
Epoch
      29 MSE:
                0.009899788536131382
Epoch
       30 MSE:
                0.009527312591671944
       31 MSE:
                0.00887078233063221
Epoch
Epoch
       32 MSE:
                0.008020643144845963
Epoch
       33 MSE:
                0.007074045483022928
Epoch
       34 MSE:
                0.006125086452811956
Epoch
       35 MSE:
                0.005255918949842453
Epoch
       36 MSE:
                0.004528750199824572
       37 MSE:
Epoch
                0.0039809877052903175
Epoch
       38 MSE:
                0.0036219561006873846
Epoch
       39 MSE:
                0.003434533253312111
       40 MSE:
Epoch
                0.0033784417901188135
Epoch
       41 MSE:
                0.003396890824660659
       42 MSE:
Epoch
                0.003428007010370493
Epoch
      43 MSE:
                0.0034260039683431387
Epoch
      44 MSE:
                0.0033759367652237415
Epoch
       45 MSE:
                0.003223852952942252
Epoch
       46 MSE:
                0.0029371106065809727
       47 MSE:
Epoch
                0.00253877486102283
Epoch
       48 MSE:
                0.0020860289223492146
Epoch
       49 MSE:
                0.0016460136976093054
Epoch
       50 MSE:
                0.0012737471843138337
Epoch
       51 MSE:
                0.0009994221618399024
Epoch
       52 MSE:
                0.0008198163122870028
Epoch
       53 MSE:
                0.0007138070068322122
      54 MSE:
Epoch
                0.0006567599484696984
       55 MSE:
Epoch
                0.0006231250590644777
Epoch
       56 MSE:
                0.0005906839505769312
Epoch
       57 MSE:
                0.0005439228261820972
Epoch
       58 MSE:
                0.0004761815071105957
Epoch
       59 MSE:
                0.00038952138856984675
Epoch
       60 MSE:
                0.0002923642750829458
       61 MSE:
Epoch
                0.00019859152962453663
```

```
Epoch 62 MSE: 0.00012451084330677986
Epoch 63 MSE: 8.275578875327483e-05
Epoch 64 MSE:
               7.819325401214883e-05
Epoch 65 MSE:
               0.00010471040150150657
Epoch 66 MSE:
               0.00014806599938310683
Epoch 67 MSE:
               0.00019106242689304054
Epoch 68 MSE:
               0.0002193786931456998
Epoch 69 MSE:
               0.00022601902310270816
Epoch 70 MSE:
               0.00021255889441818
Epoch 71 MSE:
               0.00018712293240241706
Epoch 72 MSE:
               0.00016022348427213728
Epoch 73 MSE:
               0.0001404605427524075
Epoch 74 MSE:
               0.0001317220157943666
Epoch 75 MSE:
               0.00013277714606374502
Epoch 76 MSE:
               0.0001387267402606085
Epoch 77 MSE:
               0.00014355946041177958
Epoch 78 MSE:
               0.0001425677037332207
Epoch 79 MSE:
               0.00013385291094891727
Epoch 80 MSE:
               0.00011859599908348173
Epoch 81 MSE:
               0.00010020648187492043
Epoch 82 MSE:
               8.283080387627706e-05
Epoch 83 MSE:
               6.983943603700027e-05
Epoch 84 MSE:
               6.279120862018317e-05
Epoch 85 MSE:
               6.118803139543161e-05
Epoch 86 MSE:
               6.297955405898392e-05
Epoch 87 MSE:
               6.554340507136658e-05
Epoch 88 MSE:
               6.671592564089224e-05
Epoch 89 MSE:
               6.547228986164555e-05
Epoch 90 MSE:
               6.207778642419726e-05
Epoch 91 MSE:
               5.771922951680608e-05
Epoch 92 MSE:
               5.3848372772336006e-05
Epoch 93 MSE:
               5.156659972271882e-05
Epoch 94 MSE:
               5.124495510244742e-05
Epoch 95 MSE:
               5.249131208984181e-05
Epoch 96 MSE:
               5.441350003820844e-05
Epoch 97 MSE:
               5.602049714070745e-05
Epoch 98 MSE:
               5.659730959450826e-05
Epoch 99 MSE:
               5.591701847151853e-05
T-time: 4.957951784133911
```

1 01mc. 1.30/301/01100311

Train Score: 0.22 RMSE

-----Validation Score: 1.17 RMSE

Time Chan - 20 | Hidden Chahar - 4 | Nom Laurer - 1

Time Step = 30 | Hidden States = 4 | Num Layers = 1

Epoch	O MSE:	0.13149809837341309
Epoch	1 MSE:	0.09963641315698624
Epoch	2 MSE:	0.07917803525924683
Epoch	3 MSE:	0.06763906031847
Epoch	4 MSE:	0.06233752518892288
Epoch	5 MSE:	0.060646362602710724
Epoch	6 MSE:	0.06032881140708923
Epoch	7 MSE:	0.05985136330127716
Epoch	8 MSE:	0.05847601220011711
Epoch	9 MSE:	0.05610226094722748
Epoch	10 MSE:	0.05300470441579819
Epoch	11 MSE:	0.04960326850414276
Epoch	12 MSE:	0.046310488134622574
Epoch	13 MSE:	0.04344494640827179
Epoch	14 MSE:	0.041190262883901596
Epoch	15 MSE:	0.03958602249622345
Epoch	16 MSE:	0.03854375705122948
Epoch	17 MSE:	0.03788324072957039
Epoch	18 MSE:	0.03738231584429741
Epoch	19 MSE:	0.03682979568839073
Epoch	20 MSE:	0.03606904670596123
Epoch	21 MSE:	0.03502277657389641
Epoch	22 MSE:	0.033695802092552185
Epoch	23 MSE:	0.032159674912691116
Epoch	24 MSE:	0.03052624501287937
Epoch	25 MSE:	0.028917407616972923
Epoch	26 MSE:	0.02743644267320633
Epoch	27 MSE:	0.026145176962018013
Epoch	28 MSE:	0.0250510573387146
Epoch	29 MSE:	0.024107785895466805
Epoch	30 MSE:	0.02323133498430252
Epoch	31 MSE:	0.022327976301312447
Epoch	32 MSE:	0.021324992179870605
Epoch	33 MSE:	0.02019250951707363
Epoch	34 MSE:	0.01894904486835003
Epoch	35 MSE:	0.017650648951530457
Epoch	36 MSE:	0.016369014978408813
Epoch	37 MSE:	0.015166203491389751
Epoch	38 MSE:	0.014073378406465054
Epoch	39 MSE:	0.013080161064863205
Epoch	40 MSE:	0.01213916763663292
Epoch	41 MSE:	0.011186265386641026
Epoch	42 MSE:	0.010170145891606808
Epoch	43 MSE:	0.009077813476324081
Epoch	44 MSE:	0.007942619733512402
Epoch	45 MSE:	0.006829829886555672

```
Epoch
       46 MSE:
                0.005806009750813246
Epoch
       47 MSE:
                0.004906513728201389
Epoch
       48 MSE:
                0.0041190627962350845
       49 MSE:
Epoch
                0.00339686032384634
Epoch
       50 MSE:
                0.0026967518497258425
Epoch
       51 MSE:
                0.0020161443389952183
Epoch
       52 MSE:
                0.0014002036768943071
Epoch
       53 MSE:
                0.0009124029893428087
Epoch 54 MSE:
                0.0005871688481420279
Epoch
       55 MSE:
                0.00040012667886912823
       56 MSE:
                0.00028797617414966226
Epoch
       57 MSE:
Epoch
                0.00020772349671460688
Epoch
       58 MSE:
                0.00017331948038190603
Epoch
       59 MSE:
                0.0002252475533168763
Epoch
       60 MSE:
                0.0003657652996480465
Epoch
       61 MSE:
                0.0005359567585401237
Epoch
       62 MSE:
                0.0006666507106274366
       63 MSE:
Epoch
                0.000741573516279459
Epoch
       64 MSE:
                0.0007934779278002679
Epoch
       65 MSE:
                0.0008445589919574559
Epoch
       66 MSE:
                0.0008724444778636098
Epoch
       67 MSE:
                0.0008436392527073622
Epoch
       68 MSE:
                0.0007614509086124599
       69 MSE:
Epoch
                0.0006621888023801148
Epoch
       70 MSE:
                0.0005736087332479656
Epoch
      71 MSE:
                0.0004932694137096405
       72 MSE:
Epoch
                0.0004070967552252114
Epoch
      73 MSE:
                0.0003161117492709309
      74 MSE:
Epoch
                0.00023742156918160617
Epoch
     75 MSE:
                0.00018452087533660233
Epoch 76 MSE:
                0.00015452044317498803
Epoch
      77 MSE:
                0.0001352223043795675
Epoch
      78 MSE:
                0.00011968657054239884
       79 MSE:
                0.0001107272255467251
Epoch
Epoch
       80 MSE:
                0.0001132416509790346
Epoch
       81 MSE:
                0.000125873411889188
Epoch
       82 MSE:
                0.00014131008356343955
Epoch
       83 MSE:
                0.0001531489979242906
       84 MSE:
Epoch
                0.00016069984121713787
Epoch
       85 MSE:
                0.00016710047202650458
       86 MSE:
                0.00017412242596037686
Epoch
       87 MSE:
Epoch
                0.00017981835117097944
Epoch
       88 MSE:
                0.0001809683453757316
       89 MSE:
Epoch
                0.000176792309503071
Epoch
       90 MSE:
                0.0001696201943559572
Epoch
       91 MSE:
                0.00016222351405303925
Epoch
       92 MSE:
                0.00015522027388215065
       93 MSE:
                0.00014736891898792237
Epoch
```

```
Epoch 94 MSE:
               0.00013793096877634525
Epoch 95 MSE:
               0.00012806215090677142
Epoch 96 MSE:
               0.0001197316450998187
Epoch 97 MSE:
               0.00011374369205441326
Epoch 98 MSE:
               0.00010929525888059288
Epoch 99 MSE:
               0.00010537834896240383
```

T-time: 3.1757357120513916

Train Score: 0.31 RMSE ______ Validation Score: 10.04 RMSE _____

Epoch 0 MSE: 0.11873690038919449 Epoch 1 MSE: 0.10858886688947678 Epoch 2 MSE: 0.09937623888254166 Epoch 3 MSE: 0.09090328961610794 Epoch 4 MSE: 0.0831817016005516 Epoch 5 MSE: 0.07625410705804825 Epoch 6 MSE: 0.07018733769655228 Epoch 7 MSE: 0.06499002128839493 Epoch 8 MSE: 0.06072250381112099 Epoch 9 MSE: 0.05742676928639412 Epoch 10 MSE: 0.055086709558963776 Epoch 11 MSE: 0.05356884002685547 Epoch 12 MSE: 0.052618417888879776 Epoch 13 MSE: 0.05197449028491974 Epoch 14 MSE: 0.05144820734858513 Epoch 15 MSE: 0.050918083637952805 Epoch 16 MSE: 0.05031367763876915 Epoch 17 MSE: 0.04960484802722931 Epoch 18 MSE: 0.048792384564876556 Epoch 19 MSE: 0.047898441553115845 Epoch 20 MSE: 0.04695729538798332 Epoch 21 MSE: 0.04600735381245613 Epoch 22 MSE: 0.0450848750770092 Epoch 23 MSE: 0.04421991854906082 Epoch 24 MSE: 0.04343396797776222 Epoch 25 MSE: 0.04273933917284012 Epoch 26 MSE: 0.04213965684175491 Epoch 27 MSE: 0.041631218045949936 Epoch 28 MSE: 0.0412047803401947 Epoch 29 MSE: 0.04084744676947594 Epoch 30 MSE: 0.04054456576704979 Epoch 31 MSE: 0.0402812622487545 Epoch 32 MSE: 0.04004376381635666 33 MSE: 0.03982028365135193

Epoch

```
Epoch
      34 MSE:
                0.039601586759090424
Epoch
       35 MSE:
                0.039381176233291626
Epoch
      36 MSE:
                0.03915528208017349
      37 MSE:
Epoch
                0.038922544568777084
Epoch
      38 MSE:
                0.03868364915251732
Epoch
      39 MSE:
                0.0384407564997673
Epoch
      40 MSE:
                0.03819701448082924
Epoch 41 MSE:
                0.03795596957206726
Epoch 42 MSE:
                0.03772113099694252
                0.037495557218790054
Epoch 43 MSE:
      44 MSE:
Epoch
                0.037281546741724014
Epoch 45 MSE:
                0.037080444395542145
Epoch 46 MSE:
                0.0368926003575325
Epoch
      47 MSE:
                0.03671739250421524
Epoch 48 MSE:
                0.03655340149998665
Epoch 49 MSE:
                0.036398570984601974
Epoch 50 MSE:
                0.036250531673431396
      51 MSE:
Epoch
                0.03610682114958763
Epoch
      52 MSE:
                0.035965170711278915
Epoch 53 MSE:
                0.03582365810871124
Epoch
       54 MSE:
                0.0356808602809906
Epoch 55 MSE:
                0.035535916686058044
Epoch 56 MSE:
                0.03538847714662552
Epoch 57 MSE:
                0.03523862361907959
Epoch 58 MSE:
                0.035086750984191895
Epoch
      59 MSE:
                0.034933432936668396
      60 MSE:
Epoch
                0.034779250621795654
Epoch
       61 MSE:
                0.034624673426151276
      62 MSE:
Epoch
                0.03447001799941063
Epoch 63 MSE:
                0.034315325319767
Epoch 64 MSE:
                0.03416040539741516
Epoch
       65 MSE:
                0.034004829823970795
      66 MSE:
Epoch
                0.03384801372885704
Epoch
      67 MSE:
                0.033689238131046295
Epoch
       68 MSE:
                0.033527739346027374
Epoch
       69 MSE:
                0.03336276859045029
Epoch 70 MSE:
                0.03319362923502922
Epoch 71 MSE:
                0.03301972895860672
Epoch 72 MSE:
                0.03284057602286339
Epoch 73 MSE:
                0.03265577182173729
Epoch 74 MSE:
                0.03246500343084335
Epoch
     75 MSE:
                0.03226802125573158
Epoch
      76 MSE:
                0.03206457942724228
      77 MSE:
Epoch
                0.03185443952679634
Epoch
      78 MSE:
                0.031637296080589294
Epoch
      79 MSE:
                0.031412817537784576
Epoch
       80 MSE:
                0.031180566176772118
       81 MSE:
                0.030940059572458267
Epoch
```

Epoch 82 MSE: 0.030690722167491913 Epoch 83 MSE: 0.030431929975748062 Epoch 84 MSE: 0.03016301989555359 Epoch 85 MSE: 0.029883306473493576 Epoch 86 MSE: 0.029592081904411316 Epoch 87 MSE: 0.02928866073489189 Epoch 88 MSE: 0.028972331434488297 Epoch 89 MSE: 0.02864241600036621 Epoch 90 MSE: 0.028298210352659225 Epoch 91 MSE: 0.02793900854885578 Epoch 92 MSE: 0.02756408601999283 Epoch 93 MSE: 0.027172671630978584 Epoch 94 MSE: 0.026763955131173134 Epoch 95 MSE: 0.02633707970380783 Epoch 96 MSE: 0.0258918646723032 Epoch 97 MSE: 0.02543424256145954 Epoch 98 MSE: 0.024980008602142334 Epoch 99 MSE: 0.02451673522591591

T-time: 5.6565210819244385

Train Score: 4.67 RMSE

_____ Validation Score: 29.59 RMSE

Time Step = 30 | Hidden States = 4 | Num Layers = 2 _____

Epoch 0 MSE: 0.1433069258928299 Epoch 1 MSE: 0.07710074633359909 Epoch 2 MSE: 0.03168284147977829 Epoch 3 MSE: 0.011016794480383396 Epoch 4 MSE: 0.013518337160348892 Epoch 5 MSE: 0.027552442625164986 Epoch 6 MSE: 0.03760810196399689 Epoch 7 MSE: 0.03800003603100777 Epoch 8 MSE: 0.031048117205500603 Epoch 9 MSE: 0.021237678825855255 Epoch 10 MSE: 0.012513917870819569 Epoch 11 MSE: 0.007222149055451155 Epoch 12 MSE: 0.005839816760271788 Epoch 13 MSE: 0.007369123864918947 Epoch 14 MSE: 0.010126856155693531 Epoch 15 MSE: 0.012504811398684978 Epoch 16 MSE: 0.01344325952231884 Epoch 17 MSE: 0.01258918922394514

```
Epoch
       18 MSE:
                0.010225184261798859
Epoch
       19 MSE:
                0.007069110870361328
Epoch
      20 MSE:
                0.004012463614344597
      21 MSE:
Epoch
                0.0018395651131868362
Epoch
      22 MSE:
                0.0009781125700101256
Epoch
      23 MSE:
                0.0013598032528534532
Epoch
      24 MSE:
                0.0024685324169695377
Epoch
      25 MSE:
                0.0035818249452859163
Epoch 26 MSE:
                0.00409723212942481
Epoch
      27 MSE:
                0.003775843186303973
Epoch
      28 MSE:
                0.002791648032143712
      29 MSE:
Epoch
                0.0015939167933538556
Epoch
       30 MSE:
                0.0006733298650942743
Epoch
       31 MSE:
                0.0003412370278965682
Epoch
      32 MSE:
                0.0006110130925662816
                0.0012260433286428452
Epoch 33 MSE:
Epoch
       34 MSE:
                0.0018124519847333431
      35 MSE:
Epoch
                0.0020706462673842907
Epoch
       36 MSE:
                0.0019035818986594677
Epoch
       37 MSE:
                0.001426788279786706
       38 MSE:
Epoch
                0.0008766322862356901
       39 MSE:
Epoch
                0.0004796137218363583
Epoch 40 MSE:
                0.00035028046113438904
Epoch 41 MSE:
                0.0004595018399413675
Epoch
      42 MSE:
                0.0006754745845682919
Epoch
      43 MSE:
                0.0008453124319203198
Epoch 44 MSE:
                0.0008710527908988297
Epoch
       45 MSE:
                0.0007450501434504986
      46 MSE:
Epoch
                0.000535993545781821
Epoch 47 MSE:
                0.00034196823253296316
Epoch 48 MSE:
                0.0002388173743383959
Epoch
       49 MSE:
                0.00024860765552148223
      50 MSE:
Epoch
                0.0003388607583474368
      51 MSE:
Epoch
                0.00044704886386170983
Epoch
       52 MSE:
                0.000514366605784744
Epoch
      53 MSE:
                0.0005117342225275934
Epoch
       54 MSE:
                0.00044774371781386435
Epoch
      55 MSE:
                0.00035813706927001476
      56 MSE:
Epoch
                0.00028453851700760424
Epoch 57 MSE:
                0.0002537255350034684
Epoch 58 MSE:
                0.0002670037210918963
Epoch
       59 MSE:
                0.0003034995752386749
Epoch
       60 MSE:
                0.000334063806803897
Epoch
       61 MSE:
                0.0003375121741555631
Epoch
      62 MSE:
                0.00031056065927259624
Epoch
       63 MSE:
                0.000267021416220814
       64 MSE:
Epoch
                0.00022805813932791352
       65 MSE:
                0.0002098264085361734
Epoch
```

```
Epoch 66 MSE:
               0.00021550175733864307
Epoch 67 MSE:
               0.00023543024144601077
Epoch 68 MSE:
               0.00025424352497793734
Epoch 69 MSE:
               0.0002600757288746536
Epoch 70 MSE:
               0.00025048962561413646
Epoch 71 MSE:
               0.00023224885808303952
Epoch 72 MSE:
               0.00021593795099761337
Epoch 73 MSE:
               0.00020922330440953374
Epoch 74 MSE:
               0.0002128445339621976
Epoch 75 MSE:
               0.00022128272394184023
Epoch 76 MSE:
               0.00022703740978613496
Epoch 77 MSE:
               0.000225432391744107
Epoch 78 MSE:
               0.00021698637283407152
Epoch 79 MSE:
               0.00020628444326575845
Epoch 80 MSE:
               0.00019857953884638846
Epoch 81 MSE:
               0.0001965377014130354
Epoch 82 MSE:
               0.00019908057583961636
Epoch 83 MSE:
               0.00020268662774469703
Epoch 84 MSE:
               0.00020395225146785378
Epoch 85 MSE:
               0.00020163961744401604
Epoch
      86 MSE:
               0.00019704220176208764
Epoch 87 MSE:
               0.00019271770725026727
Epoch 88 MSE:
               0.0001906429388327524
Epoch 89 MSE:
               0.00019104013335891068
Epoch 90 MSE:
               0.00019250874174758792
Epoch 91 MSE:
               0.00019318082195241004
Epoch 92 MSE:
               0.0001919993810588494
Epoch 93 MSE:
               0.00018927373457700014
Epoch 94 MSE:
               0.00018626217206474394
Epoch 95 MSE:
               0.0001842003402998671
Epoch 96 MSE:
               0.0001834999566199258
Epoch 97 MSE:
               0.00018362217815592885
Epoch 98 MSE:
               0.00018360187823418528
Epoch 99 MSE:
               0.0001827716187108308
```

T-time: 5.70621919631958

Train Score: 0.40 RMSE

-----Validation Score: 10.15 RMSE

Epoch 0 MSE: 0.2550153434276581 Epoch 1 MSE: 0.2095935195684433 Epoch 2 MSE: 0.170844167470932 Epoch 3 MSE: 0.1393737643957138 Epoch 4 MSE: 0.11254601925611496 Epoch 5 MSE: 0.0898924171924591

```
6 MSE:
               0.07097331434488297
Epoch
Epoch
      7 MSE:
               0.05539015308022499
Epoch 8 MSE:
               0.04275066405534744
Epoch
      9 MSE:
               0.03266792371869087
Epoch
       10 MSE:
                0.02477172389626503
Epoch
       11 MSE:
                0.018667301163077354
Epoch
       12 MSE:
                0.013977711088955402
Epoch
       13 MSE:
                0.010358172468841076
Epoch 14 MSE:
                0.007532702758908272
Epoch
       15 MSE:
                0.005553756840527058
       16 MSE:
                0.0035986308939754963
Epoch
       17 MSE:
Epoch
                0.0018780081300064921
Epoch
       18 MSE:
                0.000937403179705143
Epoch
       19 MSE:
                0.0009102059993892908
Epoch
      20 MSE:
                0.0012762368423864245
Epoch
      21 MSE:
                0.0013515419559553266
Epoch
       22 MSE:
                0.0012593321735039353
      23 MSE:
                0.0013216034276410937
Epoch
Epoch
       24 MSE:
                0.00163002940826118
Epoch
       25 MSE:
                0.002029021503403783
Epoch
       26 MSE:
                0.00222956296056509
      27 MSE:
Epoch
                0.002087288536131382
Epoch
      28 MSE:
                0.001662412192672491
      29 MSE:
Epoch
                0.0011413426836952567
Epoch
      30 MSE:
                0.0007166664581745863
Epoch
      31 MSE:
                0.0004806744691450149
      32 MSE:
Epoch
                0.000422908051405102
Epoch
       33 MSE:
                0.00042321704677306116
       34 MSE:
Epoch
                0.0003457537095528096
Epoch 35 MSE:
                0.00022183200053405017
      36 MSE:
Epoch
                0.00016717638936825097
Epoch
       37 MSE:
                0.00023439853976015002
Epoch
      38 MSE:
                0.0003736783692147583
      39 MSE:
                0.0004896096070297062
Epoch
Epoch
       40 MSE:
                0.0005194160039536655
Epoch
      41 MSE:
                0.00047045497922226787
Epoch
      42 MSE:
                0.00039894875953905284
Epoch
       43 MSE:
                0.0003574597940314561
       44 MSE:
Epoch
                0.00035678298445418477
Epoch
      45 MSE:
                0.000355272350134328
Epoch 46 MSE:
                0.00029513085610233247
       47 MSE:
Epoch
                0.0001957939239218831
Epoch
       48 MSE:
                0.0001252049405593425
      49 MSE:
Epoch
                0.00011203618487343192
Epoch
      50 MSE:
                0.00012416235404089093
Epoch
       51 MSE:
                0.00012031127698719501
Epoch
       52 MSE:
                9.378666436532512e-05
       53 MSE:
                7.35119974706322e-05
Epoch
```

```
Epoch 54 MSE:
                8.690168033353984e-05
Epoch 55 MSE:
                0.00011929378524655476
Epoch 56 MSE:
                0.0001306927006226033
Epoch 57 MSE:
                0.00011186304618604481
Epoch 58 MSE:
                9.151174162980169e-05
Epoch
      59 MSE:
                8.86170964804478e-05
Epoch
      60 MSE:
                9.012355440063402e-05
Epoch 61 MSE:
                7.634704525116831e-05
Epoch 62 MSE:
                5.048369348514825e-05
Epoch 63 MSE:
                3.3187105145771056e-05
Epoch 64 MSE:
                3.369911064510234e-05
Epoch 65 MSE:
                3.836713221971877e-05
Epoch
      66 MSE:
                3.345196819282137e-05
Epoch
      67 MSE:
                2.6569994588498957e-05
Epoch 68 MSE:
                2.993333873746451e-05
Epoch 69 MSE:
                3.881896554958075e-05
Epoch 70 MSE:
                4.098139106645249e-05
Epoch 71 MSE:
                3.5258035495644435e-05
Epoch 72 MSE:
                3.088611993007362e-05
Epoch 73 MSE:
                3.1783034501131624e-05
Epoch 74 MSE:
                3.1303174182539806e-05
Epoch 75 MSE:
                2.528998811612837e-05
Epoch 76 MSE:
                1.933266503328923e-05
Epoch 77 MSE:
                1.8383265341981314e-05
Epoch 78 MSE:
                1.9732107830350287e-05
Epoch 79 MSE:
                1.9055913071497343e-05
Epoch 80 MSE:
                1.7288009985350072e-05
Epoch 81 MSE:
                1.7916228898684494e-05
Epoch 82 MSE:
                2.0527491869870573e-05
Epoch 83 MSE:
                2.157505150535144e-05
Epoch 84 MSE:
                2.0308820239733905e-05
Epoch 85 MSE:
                1.931704355229158e-05
Epoch 86 MSE:
                1.962594069482293e-05
Epoch 87 MSE:
                1.9425924620009027e-05
Epoch
      88 MSE:
                1.7771411876310594e-05
Epoch
      89 MSE:
                1.627782876312267e-05
Epoch 90 MSE:
                1.6229510947596282e-05
Epoch 91 MSE:
                1.662608156038914e-05
Epoch 92 MSE:
                1.631325540074613e-05
Epoch 93 MSE:
                1.595057619852014e-05
Epoch 94 MSE:
                1.6422534827142954e-05
Epoch 95 MSE:
                1.7093665519496426e-05
Epoch 96 MSE:
                1.7026130080921575e-05
Epoch 97 MSE:
                1.657261782384012e-05
Epoch
      98 MSE:
                1.6495509044034407e-05
Epoch
      99 MSE:
                1.6553076420677826e-05
T-time: 5.240422248840332
```

Train Score: 0.12 RMSE

Validation Score: 5.88 RMSE

Time Step = 30 | Hidden States = 8 | Num Layers = 1

Epoch 0 MSE: 0.05278213694691658 Epoch 1 MSE: 0.03361978754401207 Epoch 2 MSE: 0.02731967158615589 Epoch 3 MSE: 0.031066661700606346 Epoch 4 MSE: 0.030981848016381264 Epoch 5 MSE: 0.026058509945869446 Epoch 6 MSE: 0.02095559425652027Epoch 7 MSE: 0.018112970516085625 Epoch 8 MSE: 0.017298994585871696 Epoch 9 MSE: 0.017008569091558456 Epoch 10 MSE: 0.01577960141003132 Epoch 11 MSE: 0.013044299557805061 Epoch 12 MSE: 0.009370028041303158 Epoch 13 MSE: 0.006152652204036713 Epoch 14 MSE: 0.0047519453801214695 Epoch 15 MSE: 0.004772848449647427 Epoch 16 MSE: 0.0037172678858041763 Epoch 17 MSE: 0.0011691413819789886 Epoch 18 MSE: 0.000393932219594717 Epoch 19 MSE: 0.0026690575759857893 Epoch 20 MSE: 0.003409460885450244 Epoch 21 MSE: 0.0021971629466861486 Epoch 22 MSE: 0.00276157446205616 Epoch 23 MSE: 0.003334128763526678 Epoch 24 MSE: 0.0019008215749636292 Epoch 25 MSE: 0.0007423684583045542 Epoch 26 MSE: 0.0007273777737282217 Epoch 27 MSE: 0.000835050770547241 Epoch 28 MSE: 0.0005690010730177164 Epoch 29 MSE: 0.00029128804453648627 Epoch 30 MSE: 0.000369840330677107 Epoch 31 MSE: 0.0007153096958063543 Epoch 32 MSE: 0.0009738623048178852 Epoch 33 MSE: 0.0009548494126647711 Epoch 34 MSE: 0.0007753787795081735 Epoch 35 MSE: 0.0006506607169285417 Epoch 36 MSE: 0.0006474862457253039 Epoch 37 MSE: 0.0006541337352246046

```
Epoch
       38 MSE:
                0.000543351867236197
Epoch
       39 MSE:
                0.00032901408849284053
       40 MSE:
Epoch
                0.00015351128240581602
       41 MSE:
Epoch
                0.00012415357923600823
Epoch
       42 MSE:
                0.0001862193166743964
Epoch
       43 MSE:
                0.00020434979523997754
Epoch
       44 MSE:
                0.00015486370830330998
Epoch
       45 MSE:
                0.00014183342864271253
Epoch 46 MSE:
                0.00021460371499415487
Epoch
       47 MSE:
                0.0002848793810699135
       48 MSE:
                0.0002654272539075464
Epoch
       49 MSE:
Epoch
                0.00019356803386472166
Epoch
       50 MSE:
                0.00015622872160747647
Epoch
       51 MSE:
                0.00015905538748484105
Epoch
       52 MSE:
                0.00014278202434070408
Epoch 53 MSE:
                9.306035644840449e-05
Epoch
       54 MSE:
                5.772589793195948e-05
       55 MSE:
Epoch
                6.662660598522052e-05
Epoch
       56 MSE:
                9.344331192551181e-05
Epoch
       57 MSE:
                0.000101790064945817
Epoch
       58 MSE:
                9.250688162865117e-05
Epoch
       59 MSE:
                9.052677341969684e-05
Epoch
       60 MSE:
                0.00010294208186678588
       61 MSE:
Epoch
                0.0001103850154322572
                9.82069832389243e-05
       62 MSE:
Epoch
Epoch
       63 MSE:
                7.755197293590754e-05
       64 MSE:
Epoch
                6.719017255818471e-05
Epoch
       65 MSE:
                6.743230187566951e-05
       66 MSE:
Epoch
                6.467309867730364e-05
Epoch
       67 MSE:
                5.52221063117031e-05
       68 MSE:
Epoch
                5.014980342821218e-05
Epoch
       69 MSE:
                5.589789725490846e-05
       70 MSE:
Epoch
                6.359057442750782e-05
       71 MSE:
Epoch
                6.365303124766797e-05
Epoch
       72 MSE:
                5.974005762254819e-05
Epoch
       73 MSE:
                5.959281770628877e-05
Epoch
      74 MSE:
                6.135851435828954e-05
Epoch
      75 MSE:
                5.851071546203457e-05
      76 MSE:
Epoch
                5.1992614316986874e-05
Epoch
      77 MSE:
                4.830924444831908e-05
      78 MSE:
Epoch
                4.8854813940124586e-05
       79 MSE:
Epoch
                4.914290548185818e-05
Epoch
       80 MSE:
                4.7348767111543566e-05
Epoch
       81 MSE:
                4.656691089621745e-05
Epoch
       82 MSE:
                4.838252061745152e-05
Epoch
       83 MSE:
                5.002191392122768e-05
Epoch
       84 MSE:
                4.919691491522826e-05
       85 MSE:
                4.746708873426542e-05
Epoch
```

Epoch 86 MSE: 4.693479058914818e-05 Epoch 87 MSE: 4.679728590417653e-05 Epoch 88 MSE: 4.544924740912393e-05 Epoch 89 MSE: 4.364998312667012e-05 Epoch 90 MSE: 4.310723306844011e-05 Epoch 91 MSE: 4.353961776359938e-05 Epoch 92 MSE: 4.3499658204382285e-05 Epoch 93 MSE: 4.296464248909615e-05 Epoch 94 MSE: 4.2948224290739745e-05 Epoch 95 MSE: 4.334181357990019e-05 Epoch 96 MSE: 4.314526086091064e-05 Epoch 97 MSE: 4.233754953020252e-05 Epoch 98 MSE: 4.177206210442819e-05 Epoch 99 MSE: 4.1587743908166885e-05 T-time: 7.5070459842681885

Train Score: 0.19 RMSE

Validation Score: 6.44 RMSE

Epoch 0 MSE: 0.05106747895479202 Epoch 1 MSE: 0.04000783711671829 Epoch 2 MSE: 0.035214584320783615 Epoch 3 MSE: 0.03589357063174248 Epoch 4 MSE: 0.03644981235265732 Epoch 5 MSE: 0.03460550308227539 Epoch 6 MSE: 0.0317227803170681 Epoch 7 MSE: 0.029256943613290787 Epoch 8 MSE: 0.02771889604628086 Epoch 9 MSE: 0.0268555860966444 Epoch 10 MSE: 0.026085566729307175 Epoch 11 MSE: 0.024944549426436424 Epoch 12 MSE: 0.02326631173491478 Epoch 13 MSE: 0.02112613059580326 Epoch 14 MSE: 0.018757790327072144 Epoch 15 MSE: 0.016418617218732834 Epoch 16 MSE: 0.014477932825684547 Epoch 17 MSE: 0.013293270952999592 Epoch 18 MSE: 0.012063956819474697 Epoch 19 MSE: 0.010787257924675941 Epoch 20 MSE: 0.009486738592386246 Epoch 21 MSE: 0.008209380321204662 Epoch 22 MSE: 0.006960908882319927 Epoch 23 MSE: 0.005715483333915472 Epoch 24 MSE: 0.0044549135491251945 Epoch 25 MSE: 0.003249770263209939

```
Epoch
       26 MSE:
                0.0022121246438473463
Epoch
       27 MSE:
                0.001395604689605534
Epoch
       28 MSE:
                0.0007670857012271881
       29 MSE:
Epoch
                0.0003895141708198935
Epoch
       30 MSE:
                0.0004035530728287995
Epoch
       31 MSE:
                0.0006746084545738995
Epoch
       32 MSE:
                0.0011361748911440372
Epoch
       33 MSE:
                0.0016898877220228314
       34 MSE:
Epoch
                0.0019877550657838583
Epoch
       35 MSE:
                0.0020919612143188715
       36 MSE:
                0.0018833709182217717
Epoch
       37 MSE:
Epoch
                0.0015440450515598059
Epoch
       38 MSE:
                0.0011663420591503382
Epoch
       39 MSE:
                0.0007990178419277072
Epoch
       40 MSE:
                0.0005547424079850316
Epoch 41 MSE:
                0.00039213517447933555
Epoch
       42 MSE:
                0.00031762433354742825
       43 MSE:
                0.0003269977169111371
Epoch
Epoch
       44 MSE:
                0.00036295183235779405
Epoch
       45 MSE:
                0.0004217087116558105
Epoch
       46 MSE:
                0.0004930587019771338
Epoch
       47 MSE:
                0.0005438716034404933
Epoch
      48 MSE:
                0.0005761570064350963
       49 MSE:
Epoch
                0.0005912467604503036
       50 MSE:
                0.0005732380086556077
Epoch
Epoch
       51 MSE:
                0.0005289987311698496
       52 MSE:
Epoch
                0.0004668090841732919
Epoch
       53 MSE:
                0.000378903845557943
       54 MSE:
Epoch
                0.00027368892915546894
Epoch 55 MSE:
                0.00016877090092748404
                8.711807458894327e-05
Epoch 56 MSE:
Epoch
       57 MSE:
                8.212379907490686e-05
Epoch
       58 MSE:
                0.0001637105888221413
       59 MSE:
                0.0002212417166447267
Epoch
Epoch
       60 MSE:
                0.0001988554431591183
Epoch
       61 MSE:
                0.00012974548735655844
Epoch
       62 MSE:
                6.685456173727289e-05
Epoch
       63 MSE:
                5.038969175075181e-05
       64 MSE:
Epoch
                6.524207128677517e-05
Epoch
       65 MSE:
                8.008144504856318e-05
       66 MSE:
Epoch
                9.334533388027921e-05
       67 MSE:
Epoch
                0.00010369331721449271
Epoch
       68 MSE:
                9.841927385423332e-05
Epoch
       69 MSE:
                8.543949661543593e-05
Epoch
      70 MSE:
                7.501655636588112e-05
Epoch
       71 MSE:
                6.141121411928907e-05
Epoch
       72 MSE:
                4.689349589170888e-05
       73 MSE:
                4.006346716778353e-05
Epoch
```

```
Epoch 74 MSE: 3.725471833604388e-05
Epoch 75 MSE: 3.783651482081041e-05
Epoch 76 MSE: 4.4220414565643296e-05
Epoch 77 MSE:
               4.5573400711873546e-05
Epoch 78 MSE:
               4.3364787416066974e-05
Epoch 79 MSE:
               3.624219971243292e-05
Epoch 80 MSE:
               2.691508416319266e-05
Epoch 81 MSE:
               2.292606768605765e-05
Epoch 82 MSE:
               2.1535959604079835e-05
Epoch 83 MSE:
               2.3935424906085245e-05
Epoch 84 MSE:
               2.7583984774537385e-05
Epoch 85 MSE:
               2.920997212640941e-05
Epoch 86 MSE:
               3.022539385710843e-05
Epoch 87 MSE:
               2.8443455448723398e-05
Epoch 88 MSE:
               2.5892655685311183e-05
Epoch 89 MSE:
               2.394677903794218e-05
Epoch 90 MSE:
               2.2640451788902283e-05
Epoch 91 MSE:
               2.366723128943704e-05
Epoch 92 MSE:
               2.4835046133375727e-05
Epoch 93 MSE:
               2.562371446401812e-05
Epoch 94 MSE:
               2.523822695366107e-05
Epoch 95 MSE:
               2.3375660020974465e-05
Epoch 96 MSE: 2.19309949898161e-05
Epoch 97 MSE: 2.072254937957041e-05
Epoch 98 MSE:
               2.0591982320183888e-05
Epoch 99 MSE:
               2.1014366211602464e-05
```

T-time: 3.923851251602173

Train Score: 0.14 RMSE

-----Validation Score: 2.01 RMSE

Epoch 0 MSE: 0.049527596682310104
Epoch 1 MSE: 0.03605470061302185
Epoch 2 MSE: 0.042219243943691254
Epoch 3 MSE: 0.0339699424803257
Epoch 4 MSE: 0.026178669184446335
Epoch 5 MSE: 0.025176018476486206
Epoch 6 MSE: 0.025676369667053223
Epoch 7 MSE: 0.02168041467666626
Epoch 8 MSE: 0.014866574667394161
Epoch 9 MSE: 0.010453994385898113

```
Epoch
       10 MSE:
                0.010063659399747849
Epoch
       11 MSE:
                0.007909794338047504
       12 MSE:
Epoch
                0.002407744061201811
       13 MSE:
Epoch
                0.0011232304386794567
Epoch
       14 MSE:
                0.004829954821616411
Epoch
       15 MSE:
                0.003660020884126425
Epoch
       16 MSE:
                0.004582020454108715
Epoch
       17 MSE:
                0.005983611568808556
Epoch 18 MSE:
                0.002934611402451992
Epoch
       19 MSE:
                0.0017652814276516438
       20 MSE:
                0.0019233215134590864
Epoch
Epoch
      21 MSE:
                0.0011201351881027222
Epoch
      22 MSE:
                0.0004837086598854512
Epoch
      23 MSE:
                0.0009504971094429493
Epoch
      24 MSE:
                0.0017617633566260338
Epoch 25 MSE:
                0.0019835468847304583
Epoch
      26 MSE:
                0.0016940936911851168
      27 MSE:
                0.001497879740782082
Epoch
Epoch
      28 MSE:
                0.0015820709522813559
Epoch
       29 MSE:
                0.0015721811214461923
Epoch
       30 MSE:
                0.0011696434812620282
Epoch
      31 MSE:
                0.0006228992715477943
Epoch
      32 MSE:
                0.00039383122930303216
       33 MSE:
Epoch
                0.0004983940161764622
Epoch
      34 MSE:
                0.0005307348328642547
Epoch
       35 MSE:
                0.00038809425313957036
       36 MSE:
Epoch
                0.00041482914821244776
Epoch
       37 MSE:
                0.0006704626721329987
       38 MSE:
Epoch
                0.0007617941009812057
Epoch
      39 MSE:
                0.0005821087979711592
                0.0004467391408979893
Epoch 40 MSE:
Epoch
       41 MSE:
                0.00044751103268936276
Epoch
      42 MSE:
                0.000377791584469378
      43 MSE:
                0.00022386199270840734
Epoch
Epoch
       44 MSE:
                0.00017497186490800232
Epoch
      45 MSE:
                0.0002552059886511415
Epoch
      46 MSE:
                0.0003125865769106895
Epoch
      47 MSE:
                0.00029254183755256236
       48 MSE:
Epoch
                0.00028199763619340956
Epoch
      49 MSE:
                0.00031598805799148977
Epoch 50 MSE:
                0.0003185309760738164
       51 MSE:
Epoch
                0.00025270445621572435
Epoch
       52 MSE:
                0.00018918384739663452
Epoch
       53 MSE:
                0.00017986312741413713
Epoch
      54 MSE:
                0.0001806614745873958
Epoch
       55 MSE:
                0.0001559048832859844
Epoch
       56 MSE:
                0.00014775843010284007
       57 MSE:
Epoch
                0.00017878417565952986
```

```
Epoch 58 MSE:
                0.00019791844533756375
Epoch 59 MSE:
                0.00018043819000013173
      60 MSE:
Epoch
                0.0001659086556173861
      61 MSE:
Epoch
                0.00016636497457511723
Epoch
      62 MSE:
                0.0001515565818408504
Epoch
      63 MSE:
                0.00012573276762850583
Epoch
       64 MSE:
                0.00012022441660519689
Epoch
      65 MSE:
                0.00012960191816091537
Epoch 66 MSE:
                0.00012937095016241074
Epoch 67 MSE:
                0.00012512411922216415
Epoch
      68 MSE:
                0.00013066337851341814
      69 MSE:
Epoch
                0.00013425563520286232
Epoch 70 MSE:
                0.00012463299208320677
Epoch 71 MSE:
                0.0001143340123235248
Epoch 72 MSE:
                0.00011232681572437286
Epoch 73 MSE:
                0.0001090371297323145
Epoch 74 MSE:
                0.00010229462350253016
Epoch 75 MSE:
                0.00010213439963990822
Epoch 76 MSE:
                0.00010653513891156763
Epoch 77 MSE:
                0.00010571795428404585
Epoch
     78 MSE:
                0.00010257239773636684
Epoch 79 MSE:
                0.00010244380246149376
Epoch 80 MSE:
                0.00010036485764430836
Epoch 81 MSE:
                9.484994370723143e-05
Epoch 82 MSE:
                9.220679203281179e-05
Epoch 83 MSE:
                9.238265920430422e-05
Epoch 84 MSE:
                9.094436973100528e-05
Epoch
      85 MSE:
                8.970429917098954e-05
Epoch 86 MSE:
                9.061129094334319e-05
Epoch 87 MSE:
                9.021440928336233e-05
Epoch 88 MSE:
                8.776136382948607e-05
Epoch
      89 MSE:
                8.628127397969365e-05
Epoch
      90 MSE:
                8.527203317498788e-05
Epoch 91 MSE:
                8.315730519825593e-05
Epoch
      92 MSE:
                8.183064346667379e-05
Epoch
      93 MSE:
                8.189453365048394e-05
Epoch 94 MSE:
                8.13181177363731e-05
Epoch 95 MSE:
                8.034346683416516e-05
Epoch
      96 MSE:
                8.001896640053019e-05
Epoch 97 MSE:
                7.918218761915341e-05
Epoch 98 MSE:
                7.765303598716855e-05
      99 MSE:
                7.67369128880091e-05
T-time: 7.340830326080322
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Train Score: 0.26 RMSE

Validation Score: 8.91 RMSE

Epoch	O MSE:	0.03802943229675293
Epoch	1 MSE:	0.032343484461307526
Epoch	2 MSE:	0.03325287625193596
Epoch	3 MSE:	0.03205745294690132
Epoch	4 MSE:	0.029616938903927803
Epoch	5 MSE:	0.027972757816314697
Epoch	6 MSE:	0.0267972219735384
Epoch	7 MSE:	0.02503165416419506
Epoch	8 MSE:	0.022328585386276245
Epoch	9 MSE:	0.019478648900985718
Epoch	10 MSE:	0.01762983202934265
Epoch	11 MSE:	0.01599186845123768
Epoch	12 MSE:	0.013019567355513573
Epoch	13 MSE:	0.010455413721501827
Epoch	14 MSE:	0.008998037315905094
Epoch	15 MSE:	0.006527467630803585
Epoch	16 MSE:	0.004716497380286455
Epoch	17 MSE:	0.0036773746833205223
Epoch	18 MSE:	0.002660722006112337
Epoch	19 MSE:	0.0022078712936490774
Epoch	20 MSE:	0.002793322317302227
Epoch	21 MSE:	0.002801052061840892
Epoch	22 MSE:	0.0030199741013348103
Epoch	23 MSE:	0.002545987954363227
Epoch	24 MSE:	0.0017130895284935832
Epoch	25 MSE:	0.001369559089653194
Epoch	26 MSE:	0.001118310377933085
Epoch	27 MSE:	0.0016328484052792192
Epoch	28 MSE:	0.0019065128872171044
Epoch	29 MSE:	0.001991968834772706
Epoch	30 MSE:	0.0018296599155291915
Epoch	31 MSE:	0.0013502661604434252
Epoch	32 MSE:	0.0011078735115006566
Epoch	33 MSE:	0.0008505926234647632
Epoch	34 MSE:	0.0009283379768021405
Epoch	35 MSE:	0.0010610708268359303
Epoch	36 MSE:	0.0011206634808331728
Epoch	37 MSE:	0.0011200001000001720
Epoch	38 MSE:	0.0010310023107003390
_	39 MSE:	0.0007309984066523612
Epoch	40 MSE:	0.0007309984060323612
Epoch		
Epoch	41 MSE:	0.0005737202591262758
Epoch	42 MSE:	0.0005830045556649566
Epoch	43 MSE:	0.000628706649877131
Epoch	44 MSE:	0.0006435530376620591
Epoch	45 MSE:	0.0005891544278711081

```
Epoch
       46 MSE:
                0.0005501447012647986
Epoch
       47 MSE:
                0.00045637256698682904
Epoch
       48 MSE:
                0.0004274841630831361
       49 MSE:
Epoch
                0.000391364679671824
Epoch
       50 MSE:
                0.000406360428314656
       51 MSE:
Epoch
                0.00041643797885626554
Epoch
       52 MSE:
                0.00042619684245437384
Epoch
       53 MSE:
                0.00042159692384302616
       54 MSE:
Epoch
                0.00039380346424877644
Epoch
       55 MSE:
                0.00036967970663681626
       56 MSE:
                0.0003349975449964404
Epoch
       57 MSE:
Epoch
                0.0003234276664443314
Epoch
       58 MSE:
                0.00030757029890082777
       59 MSE:
Epoch
                0.00031400989973917603
Epoch
       60 MSE:
                0.0003069073718506843
Epoch
       61 MSE:
                0.00030932368827052414
Epoch
       62 MSE:
                0.00029274364351294935
       63 MSE:
                0.0002824223483912647
Epoch
Epoch
       64 MSE:
                0.00026045076083391905
Epoch
       65 MSE:
                0.00025035024737007916
       66 MSE:
Epoch
                0.00023673434043303132
       67 MSE:
Epoch
                0.00023574849183205515
Epoch
       68 MSE:
                0.00022989802528172731
       69 MSE:
Epoch
                0.00023032247554510832
       70 MSE:
                0.00022213546617422253
Epoch
Epoch
       71 MSE:
                0.0002167396160075441
       72 MSE:
Epoch
                0.00020556342497002333
Epoch
       73 MSE:
                0.00019801416783593595
       74 MSE:
Epoch
                0.00018984726921189576
Epoch
      75 MSE:
                0.00018551875837147236
      76 MSE:
Epoch
                0.00018264864047523588
Epoch
       77 MSE:
                0.0001789262460079044
Epoch
       78 MSE:
                0.00017557853425387293
       79 MSE:
                0.00016898548346944153
Epoch
       80 MSE:
Epoch
                0.00016407427028752863
Epoch
       81 MSE:
                0.00015704809629824013
Epoch
       82 MSE:
                0.00015293812612071633
Epoch
       83 MSE:
                0.00014869548613205552
       84 MSE:
Epoch
                0.00014566448226105422
Epoch
       85 MSE:
                0.00014315111911855638
       86 MSE:
                0.00013915020099375397
Epoch
       87 MSE:
Epoch
                0.00013593440235126764
Epoch
       88 MSE:
                0.00013125354598741978
       89 MSE:
Epoch
                0.00012722346582449973
Epoch
       90 MSE:
                0.00012352765770629048
Epoch
       91 MSE:
                0.00011984807497356087
Epoch
       92 MSE:
                0.00011720684415195137
       93 MSE:
                0.0001139999003498815
Epoch
```

```
Epoch 94 MSE: 0.00011084928701166064
Epoch 95 MSE: 0.00010766084596980363
Epoch 96 MSE: 0.00010392320837127045
Epoch 97 MSE: 0.00010082822700496763
Epoch 98 MSE: 9.788572060642764e-05
Epoch 99 MSE: 9.510454401606694e-05
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T-time: 7.341888904571533

Train Score: 0.29 RMSE

-----Validation Score: 6.94 RMSE

Time Step = 30 | Hidden States = 16 | Num Layers = 1

Epoch 0 MSE: 0.11697173863649368 Epoch 1 MSE: 0.05761765316128731 Epoch 2 MSE: 0.030711645260453224 Epoch 3 MSE: 0.030545208603143692 Epoch 4 MSE: 0.04039274901151657 Epoch 5 MSE: 0.040561381727457047 Epoch 6 MSE: 0.03285698592662811 Epoch 7 MSE: 0.02468780055642128 Epoch 8 MSE: 0.019972635433077812 Epoch 9 MSE: 0.019096899777650833 Epoch 10 MSE: 0.020361468195915222 Epoch 11 MSE: 0.021166985854506493 Epoch 12 MSE: 0.019719256088137627 Epoch 13 MSE: 0.016071006655693054 Epoch 14 MSE: 0.011613896116614342 Epoch 15 MSE: 0.008093533106148243 Epoch 16 MSE: 0.006639287807047367 Epoch 17 MSE: 0.006818080320954323 Epoch 18 MSE: 0.00651130685582757 Epoch 19 MSE: 0.004058878868818283 Epoch 20 MSE: 0.000894286553375423 Epoch 21 MSE: 0.0005521047278307378 Epoch 22 MSE: 0.003548421198502183 Epoch 23 MSE: 0.004341201391071081 Epoch 24 MSE: 0.0020897607319056988 Epoch 25 MSE: 0.0013162357499822974 Epoch 26 MSE: 0.0023737563751637936 Epoch 27 MSE: 0.0024238601326942444 Epoch 28 MSE: 0.0011583393206819892 Epoch 29 MSE: 0.00018140760948881507

```
30 MSE:
Epoch
                0.0002516580279916525
Epoch
       31 MSE:
                0.0008704348583705723
       32 MSE:
Epoch
                0.0012585902586579323
       33 MSE:
Epoch
                0.001127780182287097
Epoch
       34 MSE:
                0.0007288441411219537
Epoch
       35 MSE:
                0.00046513095730915666
Epoch
       36 MSE:
                0.0005203788750804961
Epoch
       37 MSE:
                0.0007538172067143023
      38 MSE:
Epoch
                0.000876997655723244
Epoch
       39 MSE:
                0.0007317897980101407
       40 MSE:
                0.00041958430665545166
Epoch
Epoch
      41 MSE:
                0.00018076006381306797
Epoch
       42 MSE:
                0.00016089098062366247
Epoch
       43 MSE:
                0.00028803449822589755
Epoch
      44 MSE:
                0.000368100794730708
Epoch 45 MSE:
                0.00029516243375837803
Epoch
       46 MSE:
                0.0001532428286736831
       47 MSE:
Epoch
                0.00010244784789392725
Epoch
       48 MSE:
                0.00018774504133034497
Epoch
       49 MSE:
                0.00029485695995390415
Epoch
       50 MSE:
                0.00029690691735595465
Epoch 51 MSE:
                0.00020036209025420249
      52 MSE:
Epoch
                0.00011498801177367568
      53 MSE:
Epoch
                0.00011172807717230171
       54 MSE:
                0.00015431526117026806
Epoch
Epoch
       55 MSE:
                0.00016538389900233597
       56 MSE:
Epoch
                0.00012232120207045227
Epoch
       57 MSE:
                7.075844041537493e-05
       58 MSE:
Epoch
                6.0886693972861394e-05
Epoch
      59 MSE:
                9.227888949681073e-05
       60 MSE:
Epoch
                0.00012325840361882
Epoch
       61 MSE:
                0.000121568918984849
Epoch
       62 MSE:
                9.530015086056665e-05
       63 MSE:
                7.573464245069772e-05
Epoch
Epoch
       64 MSE:
                7.939319038996473e-05
Epoch
       65 MSE:
                9.305828280048445e-05
Epoch
       66 MSE:
                9.364834113512188e-05
Epoch
       67 MSE:
                7.594106864416972e-05
       68 MSE:
Epoch
                5.653306288877502e-05
Epoch
       69 MSE:
                5.257003431324847e-05
      70 MSE:
Epoch
                6.233104795683175e-05
      71 MSE:
Epoch
                6.990422116359696e-05
Epoch
       72 MSE:
                6.574757571797818e-05
Epoch
      73 MSE:
                5.66548878850881e-05
Epoch
      74 MSE:
                5.443838017527014e-05
Epoch
       75 MSE:
                6.0237889556447044e-05
Epoch
       76 MSE:
                6.456921983044595e-05
       77 MSE:
                6.0701611801050603e-05
Epoch
```

Epoch 78 MSE: 5.2631487051257864e-05 Epoch 79 MSE: 4.857435851590708e-05 Epoch 80 MSE: 5.0404745707055554e-05 Epoch 81 MSE: 5.275727380649187e-05 Epoch 82 MSE: 5.114371015224606e-05 Epoch 83 MSE: 4.736760092782788e-05 Epoch 84 MSE: 4.601200998877175e-05 Epoch 85 MSE: 4.803898264071904e-05 Epoch 86 MSE: 5.0042282964568585e-05 Epoch 87 MSE: 4.912710573989898e-05 Epoch 88 MSE: 4.637303572962992e-05 Epoch 89 MSE: 4.47807033197023e-05 Epoch 90 MSE: 4.5187574869487435e-05 Epoch 91 MSE: 4.565707786241546e-05 Epoch 92 MSE: 4.455666567082517e-05 Epoch 93 MSE: 4.272762089385651e-05 Epoch 94 MSE: 4.201464253128506e-05 Epoch 95 MSE: 4.264771268935874e-05 Epoch 96 MSE: 4.315274418331683e-05 Epoch 97 MSE: 4.254098530509509e-05 Epoch 98 MSE: 4.149098094785586e-05 Epoch 99 MSE: 4.1096078348346055e-05 T-time: 5.675626039505005

Train Score: 0.19 RMSE

Validation Score: 4.93 RMSE

Epoch 0 MSE: 0.11837781220674515 Epoch 1 MSE: 0.09170772135257721 Epoch 2 MSE: 0.06772030889987946 Epoch 3 MSE: 0.04684718698263168 Epoch 4 MSE: 0.030036889016628265 Epoch 5 MSE: 0.02001727558672428 Epoch 6 MSE: 0.020158864557743073 Epoch 7 MSE: 0.027314167469739914 Epoch 8 MSE: 0.030450504273176193 Epoch 9 MSE: 0.02642448991537094 Epoch 10 MSE: 0.019344253465533257 Epoch 11 MSE: 0.012726797722280025 Epoch 12 MSE: 0.008827732875943184 Epoch 13 MSE: 0.006731756497174501 Epoch 14 MSE: 0.005575546529144049 Epoch 15 MSE: 0.004406242165714502 Epoch 16 MSE: 0.003260029247030616 Epoch 17 MSE: 0.0020435932092368603

```
Epoch
       18 MSE:
                0.0013429205864667892
Epoch
       19 MSE:
                0.0017330643022432923
Epoch
       20 MSE:
                0.002445710590109229
       21 MSE:
Epoch
                0.002230728743597865
Epoch
       22 MSE:
                0.0017903039697557688
Epoch
       23 MSE:
                0.0019183693220838904
Epoch
       24 MSE:
                0.0023459051735699177
Epoch
       25 MSE:
                0.0025322232395410538
      26 MSE:
Epoch
                0.00229846965521574
Epoch
       27 MSE:
                0.0017998996190726757
       28 MSE:
Epoch
                0.0013362329918891191
       29 MSE:
Epoch
                0.001109876437112689
Epoch
       30 MSE:
                0.0011286423541605473
Epoch
       31 MSE:
                0.0011711844708770514
Epoch
       32 MSE:
                0.0010610781610012054
Epoch
      33 MSE:
                0.0008542826399207115
Epoch
       34 MSE:
                0.0007018379401415586
                0.0006668834248557687
       35 MSE:
Epoch
Epoch
       36 MSE:
                0.0007031720597296953
Epoch
       37 MSE:
                0.0007260054117068648
       38 MSE:
Epoch
                0.0006805112352594733
       39 MSE:
Epoch
                0.0005828909925185144
Epoch
       40 MSE:
                0.0004793155239894986
       41 MSE:
Epoch
                0.00039136980194598436
Epoch
       42 MSE:
                0.00033165502827614546
Epoch
       43 MSE:
                0.0002828448486980051
       44 MSE:
Epoch
                0.00022590119624510407
Epoch
       45 MSE:
                0.00016700786363799125
       46 MSE:
Epoch
                0.00013159227091819048
Epoch 47 MSE:
                0.00013282072904985398
Epoch
      48 MSE:
                0.00015328962763305753
Epoch
       49 MSE:
                0.00015745572454761714
       50 MSE:
Epoch
                0.00013294436212163419
       51 MSE:
                0.00010373975965194404
Epoch
Epoch
       52 MSE:
                9.544124623062089e-05
Epoch
       53 MSE:
                0.00010089040733873844
Epoch
       54 MSE:
                9.908053471008316e-05
Epoch
       55 MSE:
                8.714669820619747e-05
       56 MSE:
Epoch
                8.034604979911819e-05
Epoch
      57 MSE:
                8.653281111037359e-05
      58 MSE:
Epoch
                9.564332867739722e-05
Epoch
       59 MSE:
                9.476490231463686e-05
Epoch
       60 MSE:
                8.431828609900549e-05
Epoch
       61 MSE:
                7.523352542193606e-05
Epoch
       62 MSE:
                7.364069460891187e-05
Epoch
       63 MSE:
                7.423987699439749e-05
       64 MSE:
Epoch
                7.02601537341252e-05
       65 MSE:
                6.412403308786452e-05
Epoch
```

```
Epoch 66 MSE: 6.271014717640355e-05
Epoch 67 MSE: 6.625935930060223e-05
Epoch 68 MSE:
               6.836317334091291e-05
Epoch 69 MSE:
               6.554339051945135e-05
Epoch 70 MSE:
               6.128794484538957e-05
Epoch 71 MSE:
               5.9739268181147054e-05
Epoch 72 MSE:
               5.968887489871122e-05
Epoch 73 MSE:
               5.776868056273088e-05
Epoch 74 MSE:
               5.441494067781605e-05
Epoch 75 MSE:
               5.2832077926723287e-05
Epoch 76 MSE:
               5.366573532228358e-05
Epoch 77 MSE:
               5.431301178759895e-05
Epoch 78 MSE:
               5.310223423293792e-05
Epoch 79 MSE:
               5.132859223522246e-05
Epoch 80 MSE:
               5.0593578635016456e-05
Epoch 81 MSE:
               5.029164094594307e-05
Epoch 82 MSE:
               4.903706212644465e-05
Epoch 83 MSE:
               4.71862695121672e-05
Epoch 84 MSE:
               4.6182929509086534e-05
Epoch 85 MSE:
               4.617670856532641e-05
Epoch 86 MSE:
               4.598693340085447e-05
Epoch 87 MSE:
               4.511100996751338e-05
Epoch 88 MSE:
               4.4271513615967706e-05
Epoch 89 MSE:
               4.391911352286115e-05
Epoch 90 MSE:
               4.3483796616783366e-05
Epoch 91 MSE:
               4.251650534570217e-05
Epoch 92 MSE:
               4.149408414377831e-05
Epoch 93 MSE:
               4.0957544115372e-05
Epoch 94 MSE:
               4.066606561536901e-05
Epoch 95 MSE:
               4.01527649955824e-05
Epoch 96 MSE:
               3.951215330744162e-05
Epoch 97 MSE:
               3.908166763721965e-05
               3.8770991523051634e-05
Epoch 98 MSE:
Epoch 99 MSE:
               3.825699968729168e-05
T-time: 5.3828041553497314
```

Train Score: 0.18 RMSE _____

Validation Score: 1.44 RMSE _____

______ Time Step = 30 | Hidden States = 16 | Num Layers = 2 _____

Epoch 0 MSE: 0.1067127138376236 Epoch 1 MSE: 0.041797880083322525

```
Epoch 2 MSE:
               0.0635981634259224
Epoch
       3 MSE:
               0.051264479756355286
Epoch
      4 MSE:
               0.034963108599185944
       5 MSE:
Epoch
               0.03419181704521179
Epoch
       6 MSE:
               0.03854495659470558
Epoch 7 MSE:
               0.03637799993157387
Epoch
       8 MSE:
               0.029408304020762444
Epoch
      9 MSE:
               0.024768918752670288
Epoch 10 MSE:
                0.025908634066581726
Epoch
       11 MSE:
                0.025984447449445724
Epoch
       12 MSE:
                0.020140763372182846
Epoch
       13 MSE:
                0.014651145786046982
Epoch
       14 MSE:
                0.014552832581102848
Epoch
       15 MSE:
                0.014279761351644993
Epoch
       16 MSE:
                0.00771391112357378
Epoch 17 MSE:
                0.003523818915709853
Epoch
       18 MSE:
                0.0063589029014110565
       19 MSE:
Epoch
                0.0019636109936982393
Epoch
       20 MSE:
                0.0062391567043960094
Epoch
       21 MSE:
                0.005020209588110447
Epoch
       22 MSE:
                0.0036720086354762316
       23 MSE:
Epoch
                0.005154712591320276
Epoch
       24 MSE:
                0.0013923653168603778
       25 MSE:
Epoch
                0.0013857195153832436
Epoch
       26 MSE:
                0.002607685513794422
Epoch
       27 MSE:
                0.0017668388318270445
       28 MSE:
Epoch
                0.0010972602758556604
Epoch
       29 MSE:
                0.001852358807809651
       30 MSE:
Epoch
                0.0025682055857032537
Epoch
       31 MSE:
                0.002132253721356392
                0.0013702419819310308
Epoch
       32 MSE:
Epoch
       33 MSE:
                0.0012778699165210128
Epoch
       34 MSE:
                0.001471176277846098
       35 MSE:
                0.0011001521488651633
Epoch
Epoch
       36 MSE:
                0.00045901889097876847
Epoch
       37 MSE:
                0.0004824106290470809
Epoch
       38 MSE:
                0.0009202268556691706
Epoch
       39 MSE:
                0.0008517063106410205
       40 MSE:
Epoch
                0.0006408887566067278
Epoch
       41 MSE:
                0.0008642466855235398
       42 MSE:
Epoch
                0.0009140026522800326
       43 MSE:
Epoch
                0.0005436803912743926
Epoch
       44 MSE:
                0.00036934754461981356
Epoch
       45 MSE:
                0.0004759846779052168
Epoch
       46 MSE:
                0.0004554733168333769
Epoch
       47 MSE:
                0.00034055119613185525
       48 MSE:
Epoch
                0.0003929841914214194
       49 MSE:
                0.0005249769310466945
Epoch
```

```
50 MSE:
Epoch
                0.0005079376860521734
Epoch
       51 MSE:
                0.00038965255953371525
Epoch
       52 MSE:
                0.0003535627038218081
       53 MSE:
Epoch
                0.0003726370050571859
Epoch
       54 MSE:
                0.0003114719584118575
Epoch
       55 MSE:
                0.0002301374770468101
Epoch
       56 MSE:
                0.0002570475044194609
Epoch
      57 MSE:
                0.000315123877953738
Epoch 58 MSE:
                0.00029253592947497964
Epoch
       59 MSE:
                0.00026482297107577324
       60 MSE:
                0.0002893961500376463
Epoch
       61 MSE:
Epoch
                0.00027877421234734356
Epoch
       62 MSE:
                0.00022101838840171695
Epoch
       63 MSE:
                0.00020457810023799539
Epoch
       64 MSE:
                0.00022397158318199217
       65 MSE:
                0.00021654341253452003
Epoch
Epoch
       66 MSE:
                0.00020099437097087502
                0.00021481259318534285
       67 MSE:
Epoch
Epoch
       68 MSE:
                0.00022541206271853298
Epoch
       69 MSE:
                0.00020492398471105844
Epoch
       70 MSE:
                0.00018672729493118823
Epoch
      71 MSE:
                0.00018863238801714033
Epoch 72 MSE:
                0.0001830397523008287
     73 MSE:
Epoch
                0.00016830737877171487
Epoch
      74 MSE:
                0.00017045659478753805
Epoch
      75 MSE:
                0.00017958617536351085
       76 MSE:
Epoch
                0.00017343656509183347
Epoch
       77 MSE:
                0.00016561656957492232
       78 MSE:
Epoch
                0.00016662388225086033
Epoch
      79 MSE:
                0.0001613549975445494
       80 MSE:
Epoch
                0.00015087313659023494
Epoch
       81 MSE:
                0.00014986598398536444
Epoch
       82 MSE:
                0.00015226495452225208
       83 MSE:
                0.00014847041165921837
Epoch
Epoch
       84 MSE:
                0.00014596266555599868
Epoch
       85 MSE:
                0.00014711235417053103
Epoch
       86 MSE:
                0.0001435540325473994
Epoch
       87 MSE:
                0.00013745347678195685
       88 MSE:
Epoch
                0.00013587177090812474
       89 MSE:
Epoch
                0.00013486496754921973
      90 MSE:
Epoch
                0.00013146302080713212
       91 MSE:
Epoch
                0.00013048757682554424
Epoch
       92 MSE:
                0.00013083552767056972
       93 MSE:
Epoch
                0.0001280757860513404
Epoch
       94 MSE:
                0.0001251223002327606
Epoch
       95 MSE:
                0.0001239947887370363
Epoch
       96 MSE:
                0.00012171274283900857
       97 MSE:
                0.00011916290532099083
Epoch
```

Epoch 98 MSE: 0.00011859015648951754 Epoch 99 MSE: 0.00011772439029300585

T-time: 11.162540197372437

Train Score: 0.32 RMSE

Validation Score: 8.21 RMSE

Epoch 0 MSE: 0.05051815137267113 Epoch 1 MSE: 0.035026248544454575 Epoch 2 MSE: 0.034311823546886444 Epoch 3 MSE: 0.036925725638866425 Epoch 4 MSE: 0.03144912049174309 Epoch 5 MSE: 0.028038011863827705 Epoch 6 MSE: 0.027341146022081375 Epoch 7 MSE: 0.02668996900320053 Epoch 8 MSE: 0.02452930063009262 Epoch 9 MSE: 0.021306157112121582 Epoch 10 MSE: 0.018578611314296722 Epoch 11 MSE: 0.016846414655447006 Epoch 12 MSE: 0.014181463047862053 Epoch 13 MSE: 0.009277529083192348 Epoch 14 MSE: 0.004900599364191294 Epoch 15 MSE: 0.002928005065768957 Epoch 16 MSE: 0.0010474803857505322 Epoch 17 MSE: 0.000958760385401547 Epoch 18 MSE: 0.003941815346479416 Epoch 19 MSE: 0.0045535569079220295 Epoch 20 MSE: 0.003580390941351652 Epoch 21 MSE: 0.0035638194531202316 Epoch 22 MSE: 0.0034907415974885225 Epoch 23 MSE: 0.002395112067461014 Epoch 24 MSE: 0.0011871416354551911 Epoch 25 MSE: 0.0011355956085026264 Epoch 26 MSE: 0.001957820961251855 Epoch 27 MSE: 0.0022134706377983093 Epoch 28 MSE: 0.0018272611778229475 Epoch 29 MSE: 0.0017083290731534362 Epoch 30 MSE: 0.0016933076549321413 Epoch 31 MSE: 0.001414899481460452 Epoch 32 MSE: 0.0008862881222739816 Epoch 33 MSE: 0.00043419579742476344 Epoch 34 MSE: 0.00038480141665786505 Epoch 35 MSE: 0.0005942038842476904 Epoch 36 MSE: 0.0006243662792257965 Epoch 37 MSE: 0.0005102031282149255

```
Epoch
       38 MSE:
                0.0005328659317456186
Epoch
       39 MSE:
                0.0006228481070138514
Epoch
       40 MSE:
                0.0005523687577806413
       41 MSE:
Epoch
                0.0003279162338003516
Epoch
       42 MSE:
                0.000254482205491513
Epoch
       43 MSE:
                0.0004491614527069032
Epoch
       44 MSE:
                0.0003988945099990815
Epoch
       45 MSE:
                0.0002906854497268796
Epoch 46 MSE:
                0.00039125443436205387
Epoch
       47 MSE:
                0.00043944932986050844
       48 MSE:
                0.0002942840219475329
Epoch
       49 MSE:
Epoch
                0.00020787429821211845
Epoch
       50 MSE:
                0.0002661723119672388
Epoch
       51 MSE:
                0.00023390684509649873
Epoch 52 MSE:
                0.00015311651804950088
                0.00020498853700701147
Epoch 53 MSE:
Epoch
      54 MSE:
                0.00024728922289796174
       55 MSE:
                0.00018020212883129716
Epoch
Epoch
       56 MSE:
                0.0001582519616931677
Epoch
       57 MSE:
                0.00018766222638078034
Epoch
       58 MSE:
                0.00014601738075725734
       59 MSE:
Epoch
                0.00011337372416164726
Epoch
       60 MSE:
                0.0001476851903134957
       61 MSE:
Epoch
                0.00015330656606238335
       62 MSE:
                0.000125233200378716
Epoch
Epoch
       63 MSE:
                0.00013434022548608482
       64 MSE:
Epoch
                0.00014379576896317303
Epoch
       65 MSE:
                0.00011400896619306877
       66 MSE:
Epoch
                0.00010404930071672425
Epoch
       67 MSE:
                0.0001173647033283487
       68 MSE:
                0.00010715925600379705
Epoch
Epoch
       69 MSE:
                9.91116976365447e-05
Epoch
      70 MSE:
                0.00011296290904283524
       71 MSE:
                0.00010845866927411407
Epoch
Epoch
       72 MSE:
                9.486645285505801e-05
Epoch
      73 MSE:
                9.900712029775605e-05
Epoch
      74 MSE:
                9.657310147304088e-05
Epoch
      75 MSE:
                8.644742047181353e-05
Epoch 76 MSE:
                9.072443208424374e-05
Epoch
      77 MSE:
                9.377735841553658e-05
Epoch 78 MSE:
                8.68986826390028e-05
       79 MSE:
Epoch
                8.721862104721367e-05
Epoch
       80 MSE:
                8.812166925054044e-05
Epoch
       81 MSE:
                8.103139407467097e-05
Epoch
       82 MSE:
                7.930185529403389e-05
Epoch
       83 MSE:
                8.11227728263475e-05
       84 MSE:
Epoch
                7.718617416685447e-05
       85 MSE:
Epoch
                7.617699884576723e-05
```

Epoch 86 MSE: 7.7380558650475e-05 Epoch 87 MSE: 7.341608579736203e-05 Epoch 88 MSE: 7.105417171260342e-05 Epoch 89 MSE: 7.095611363183707e-05 Epoch 90 MSE: 6.77508651278913e-05 Epoch 91 MSE: 6.626292451983318e-05 Epoch 92 MSE: 6.651211879216135e-05 Epoch 93 MSE: 6.411681533791125e-05 Epoch 94 MSE: 6.251839658943936e-05 Epoch 95 MSE: 6.193121953401715e-05 Epoch 96 MSE: 5.940639675827697e-05 Epoch 97 MSE: 5.78860126552172e-05 Epoch 98 MSE: 5.7255980209447443e-05 Epoch 99 MSE: 5.531753777177073e-05

T-time: 11.950053930282593

Train Score: 0.22 RMSE

Validation Score: 2.30 RMSE

Time Step = 30 | Hidden States = 32 | Num Layers = 1

Epoch 0 MSE: 0.049295082688331604 Epoch 1 MSE: 0.03979667276144028 Epoch 2 MSE: 0.03974452242255211 Epoch 3 MSE: 0.023254582658410072 Epoch 4 MSE: 0.021575437858700752 Epoch 5 MSE: 0.019107364118099213 Epoch 6 MSE: 0.008192019537091255 Epoch 7 MSE: 0.013318395242094994 Epoch 8 MSE: 0.0034822612069547176 Epoch 9 MSE: 0.005840053781867027 Epoch 10 MSE: 0.004316344391554594 Epoch 11 MSE: 0.0023619290441274643 Epoch 12 MSE: 0.0046929907985031605 Epoch 13 MSE: 0.00036526081385090947 Epoch 14 MSE: 0.0011299800826236606 Epoch 15 MSE: 0.0025745341554284096 Epoch 16 MSE: 0.001749901450239122 Epoch 17 MSE: 0.000853529607411474 Epoch 18 MSE: 0.0012326834257692099 Epoch 19 MSE: 0.0018111097160726786 Epoch 20 MSE: 0.0013629747554659843 Epoch 21 MSE: 0.0003909874358214438

```
Epoch
       22 MSE:
                0.00018431215721648186
Epoch
       23 MSE:
                0.0007419657194986939
       24 MSE:
Epoch
                0.0008447710424661636
       25 MSE:
Epoch
                0.0003508182126097381
Epoch
       26 MSE:
                0.00030557686113752425
Epoch
       27 MSE:
                0.0006934496341273189
Epoch
       28 MSE:
                0.0006217446643859148
Epoch
       29 MSE:
                0.00018074306717608124
Epoch
       30 MSE:
                6.108441448304802e-05
Epoch
       31 MSE:
                0.0002820733352564275
       32 MSE:
                0.0003859972348436713
Epoch
Epoch
       33 MSE:
                0.00025249135796912014
Epoch
       34 MSE:
                0.0001474153104936704
Epoch
       35 MSE:
                0.00021882273722440004
Epoch
       36 MSE:
                0.00030577965662814677
Epoch 37 MSE:
                0.00023264679475687444
Epoch
       38 MSE:
                8.122420695144683e-05
       39 MSE:
Epoch
                4.816541695618071e-05
Epoch
       40 MSE:
                0.00013549184950534254
Epoch
       41 MSE:
                0.00016957487969193608
Epoch
       42 MSE:
                0.00010483156074769795
Epoch
       43 MSE:
                7.444737275363877e-05
Epoch 44 MSE:
                0.00012279406655579805
       45 MSE:
Epoch
                0.00013821429456584156
       46 MSE:
                7.723113958491012e-05
Epoch
Epoch
       47 MSE:
                3.288984589744359e-05
       48 MSE:
Epoch
                5.815542317577638e-05
Epoch
       49 MSE:
                9.093456174014136e-05
       50 MSE:
Epoch
                7.76853266870603e-05
Epoch 51 MSE:
                5.247525405138731e-05
Epoch 52 MSE:
                5.921120828134008e-05
Epoch
       53 MSE:
                7.631830521859229e-05
Epoch
       54 MSE:
                6.41039150650613e-05
       55 MSE:
Epoch
                3.6733497836394235e-05
Epoch
       56 MSE:
                3.421527799218893e-05
Epoch
       57 MSE:
                5.204253830015659e-05
Epoch
       58 MSE:
                5.4925087169976905e-05
Epoch
       59 MSE:
                4.189806350041181e-05
Epoch
       60 MSE:
                4.001975685241632e-05
Epoch
       61 MSE:
                4.880649066762999e-05
       62 MSE:
Epoch
                4.588577212416567e-05
Epoch
       63 MSE:
                3.3286603866145015e-05
Epoch
       64 MSE:
                3.125104558421299e-05
Epoch
       65 MSE:
                3.938682857551612e-05
Epoch
       66 MSE:
                4.109355722903274e-05
Epoch
       67 MSE:
                3.52856659446843e-05
Epoch
       68 MSE:
                3.409859345993027e-05
       69 MSE:
                3.775236109504476e-05
Epoch
```

```
Epoch 70 MSE:
               3.6372963222675025e-05
Epoch 71 MSE:
               3.0770865123486146e-05
Epoch 72 MSE:
               3.0196833904483356e-05
Epoch 73 MSE:
               3.400662535568699e-05
Epoch 74 MSE:
               3.421611472731456e-05
Epoch 75 MSE:
               3.138730608043261e-05
Epoch 76 MSE:
               3.144778747810051e-05
Epoch 77 MSE:
               3.2933676266111434e-05
Epoch 78 MSE:
               3.1378705898532644e-05
Epoch 79 MSE:
               2.912171657953877e-05
Epoch 80 MSE:
               2.9923921829322353e-05
Epoch 81 MSE:
               3.141873821732588e-05
Epoch 82 MSE:
               3.062776158913039e-05
Epoch 83 MSE:
               2.9565762815764174e-05
Epoch 84 MSE:
               3.0105193218332715e-05
Epoch 85 MSE:
               3.0269355193013325e-05
Epoch 86 MSE:
               2.907308589783497e-05
Epoch 87 MSE:
               2.8611751986318268e-05
Epoch 88 MSE:
               2.941269485745579e-05
Epoch 89 MSE:
               2.9551893021562137e-05
Epoch 90 MSE:
               2.885109461203683e-05
Epoch 91 MSE:
               2.877604310924653e-05
Epoch 92 MSE:
               2.904696339101065e-05
Epoch 93 MSE:
               2.861639586626552e-05
Epoch 94 MSE:
               2.8142445444245823e-05
Epoch 95 MSE:
               2.8395321351126768e-05
Epoch 96 MSE:
               2.8606389605556615e-05
Epoch 97 MSE:
               2.8277741876081564e-05
Epoch 98 MSE:
               2.8092867069062777e-05
Epoch 99 MSE:
               2.8213875339133665e-05
```

T-time: 11.027218103408813

Train Score: 0.16 RMSE

-----Validation Score: 3.26 RMSE

Epoch 0 MSE: 0.04205101728439331 Epoch 1 MSE: 0.04135453328490257 Epoch 2 MSE: 0.03230201452970505 Epoch 3 MSE: 0.030650507658720016 Epoch 4 MSE: 0.0293758325278759 Epoch 5 MSE: 0.024880150333046913 Epoch 6 MSE: 0.022773221135139465 Epoch 7 MSE: 0.020975029096007347 Epoch 8 MSE: 0.016452781856060028 Epoch 9 MSE: 0.012916277162730694

```
Epoch
       10 MSE:
                0.0110430046916008
Epoch
       11 MSE:
                0.006241408176720142
Epoch
       12 MSE:
                0.002685930347070098
       13 MSE:
Epoch
                0.0012929978547617793
Epoch
       14 MSE:
                0.001336737652309239
Epoch
       15 MSE:
                0.00462092412635684
Epoch
       16 MSE:
                0.004720503930002451
Epoch
       17 MSE:
                0.002505316399037838
Epoch 18 MSE:
                0.0007192942430265248
Epoch
       19 MSE:
                0.0005070383194833994
       20 MSE:
                0.0009156455053016543
Epoch
       21 MSE:
Epoch
                0.0016080888453871012
Epoch
       22 MSE:
                0.0021905868779867887
Epoch
       23 MSE:
                0.0022385595366358757
Epoch
      24 MSE:
                0.0018214626470580697
Epoch 25 MSE:
                0.001206043642014265
Epoch
       26 MSE:
                0.000660247344058007
       27 MSE:
Epoch
                0.0003468524955678731
Epoch
       28 MSE:
                0.00025468264357186854
Epoch
       29 MSE:
                0.0004709401691798121
Epoch
       30 MSE:
                0.0008092123898677528
Epoch
       31 MSE:
                0.0009333147318102419
       32 MSE:
Epoch
                0.0006665056571364403
       33 MSE:
Epoch
                0.00040989150875248015
Epoch
       34 MSE:
                0.00029659169376827776
Epoch
       35 MSE:
                0.00017309167014900595
       36 MSE:
Epoch
                0.00023010258155409247
Epoch
       37 MSE:
                0.0003980014007538557
       38 MSE:
Epoch
                0.00044235336827114224
Epoch
      39 MSE:
                0.00039810093585401773
Epoch 40 MSE:
                0.0003637470945250243
Epoch
       41 MSE:
                0.0002727460814639926
Epoch
       42 MSE:
                0.00013942648365627974
       43 MSE:
                0.00010942869266727939
Epoch
Epoch
       44 MSE:
                0.00015030332724563777
Epoch
       45 MSE:
                0.00016952621808741242
Epoch
       46 MSE:
                0.00021233675943221897
Epoch
       47 MSE:
                0.00022135199105832726
       48 MSE:
Epoch
                0.0001490727299824357
Epoch
       49 MSE:
                0.00010267207835568115
Epoch 50 MSE:
                8.47571573103778e-05
       51 MSE:
Epoch
                7.083558011800051e-05
Epoch
       52 MSE:
                9.883721941150725e-05
Epoch
       53 MSE:
                0.0001286415645154193
Epoch
       54 MSE:
                0.00012023618910461664
Epoch
       55 MSE:
                0.00010710935021052137
Epoch
       56 MSE:
                8.736267773201689e-05
       57 MSE:
                5.6622186093591154e-05
Epoch
```

```
Epoch 58 MSE:
                5.462953413370997e-05
Epoch 59 MSE:
                6.734654016327113e-05
Epoch 60 MSE:
                7.255403033923358e-05
Epoch
      61 MSE:
                8.22818255983293e-05
Epoch
      62 MSE:
                7.443981303367764e-05
Epoch
      63 MSE:
                5.6022090575424954e-05
Epoch
       64 MSE:
                5.032271656091325e-05
Epoch 65 MSE:
                4.575284765451215e-05
Epoch 66 MSE:
                4.9553418648429215e-05
Epoch 67 MSE:
                5.865525236004032e-05
      68 MSE:
                5.67960123589728e-05
Epoch
Epoch 69 MSE:
                5.298872201819904e-05
Epoch 70 MSE:
                4.717795309261419e-05
Epoch 71 MSE:
                3.940904207411222e-05
Epoch 72 MSE:
                4.0637660276843235e-05
Epoch 73 MSE:
                4.296216866350733e-05
Epoch 74 MSE:
                4.4601601985050365e-05
Epoch 75 MSE:
                4.581660687108524e-05
Epoch 76 MSE:
                4.095325493835844e-05
Epoch 77 MSE:
                3.7711139157181606e-05
Epoch
     78 MSE:
                3.607963662943803e-05
Epoch 79 MSE:
                3.567721068975516e-05
Epoch 80 MSE:
                3.8203445001272485e-05
Epoch 81 MSE:
                3.801744605880231e-05
Epoch 82 MSE:
                3.690956509672105e-05
Epoch 83 MSE:
                3.5053715691901743e-05
Epoch 84 MSE:
                3.259530058130622e-05
Epoch
      85 MSE:
                3.275676499470137e-05
Epoch 86 MSE:
                3.290958557045087e-05
Epoch 87 MSE:
                3.3434822398703545e-05
Epoch 88 MSE:
                3.32073905155994e-05
Epoch
      89 MSE:
                3.157847822876647e-05
                3.0724422686034814e-05
Epoch 90 MSE:
Epoch 91 MSE:
                2.98330432997318e-05
Epoch
      92 MSE:
                3.0044902814552188e-05
Epoch
      93 MSE:
                3.027205093530938e-05
Epoch 94 MSE:
                2.987736115755979e-05
Epoch 95 MSE:
                2.9382288630586118e-05
Epoch 96 MSE:
                2.8336336981737986e-05
Epoch 97 MSE:
                2.798439163598232e-05
Epoch 98 MSE:
                2.7783244149759412e-05
      99 MSE:
                2.7784430130850524e-05
T-time: 10.320210695266724
```

Train Score: 0.16 RMSE

Validation Score: 2.01 RMSE

Time Step = 30 | Hidden States = 32 | Num Layers = 2

Epoch 0 MSE: 0.057030294090509415 Epoch 1 MSE: 0.19113998115062714 Epoch 2 MSE: 0.03379056602716446 Epoch 3 MSE: 0.053339164704084396 Epoch 4 MSE: 0.05368189886212349 Epoch 5 MSE: 0.035264745354652405 Epoch 6 MSE: 0.026704389601945877 Epoch 7 MSE: 0.03654397651553154 Epoch 8 MSE: 0.03494611382484436 Epoch 9 MSE: 0.02331729419529438 Epoch 10 MSE: 0.01910550147294998 Epoch 11 MSE: 0.020969608798623085 Epoch 12 MSE: 0.01989055797457695 Epoch 13 MSE: 0.012157928198575974 Epoch 14 MSE: 0.004503715317696333 Epoch 15 MSE: 0.008814998902380466 Epoch 16 MSE: 0.0042708744294941425 Epoch 17 MSE: 0.004501829389482737 Epoch 18 MSE: 0.00871396716684103 Epoch 19 MSE: 0.0022550730500370264 Epoch 20 MSE: 0.0012769837630912662 Epoch 21 MSE: 0.003009222215041518 Epoch 22 MSE: 0.002214904874563217 Epoch 23 MSE: 0.001341708586551249 Epoch 24 MSE: 0.001897222246043384 Epoch 25 MSE: 0.0027596470899879932 Epoch 26 MSE: 0.002733758883550763 0.001800626632757485 Epoch 27 MSE: Epoch 28 MSE: 0.0008660684106871486 Epoch 29 MSE: 0.0007175059290602803 Epoch 30 MSE: 0.0010380229214206338 Epoch 31 MSE: 0.0008987350156530738 Epoch 32 MSE: 0.0004129858280066401 Epoch 33 MSE: 0.0004758140130434185 Epoch 34 MSE: 0.001007994287647307 Epoch 35 MSE: 0.0011268308153375983 Epoch 36 MSE: 0.0006695648771710694 Epoch 37 MSE: 0.00030792574398219585 Epoch 38 MSE: 0.0003730269381776452 Epoch 39 MSE: 0.000481205788673833 Epoch 40 MSE: 0.00035663897870108485 Epoch 41 MSE: 0.00022849316883366555

```
Epoch
       42 MSE:
                0.0003119389002677053
Epoch
       43 MSE:
                0.0004774258122779429
       44 MSE:
Epoch
                0.0004968628054484725
       45 MSE:
Epoch
                0.00035032673622481525
Epoch
       46 MSE:
                0.0002147961495211348
Epoch
       47 MSE:
                0.00021079201542306691
Epoch
       48 MSE:
                0.00025022620684467256
Epoch
       49 MSE:
                0.00020701257744804025
       50 MSE:
Epoch
                0.00013655117072630674
Epoch
       51 MSE:
                0.00016069483535829931
       52 MSE:
                0.00024159626627806574
Epoch
Epoch
       53 MSE:
                0.00025028607342392206
Epoch
       54 MSE:
                0.00017887435387820005
Epoch
       55 MSE:
                0.00013196680811233819
Epoch
       56 MSE:
                0.0001454885205021128
       57 MSE:
                0.00015198234177660197
Epoch
Epoch
       58 MSE:
                0.00012160051119280979
       59 MSE:
                0.00010572167957434431
Epoch
Epoch
       60 MSE:
                0.0001311755768256262
Epoch
       61 MSE:
                0.00015559840539935976
Epoch
       62 MSE:
                0.00014193712559062988
Epoch
       63 MSE:
                0.00011233776604058221
       64 MSE:
Epoch
                0.00010430251859361306
       65 MSE:
Epoch
                0.00011130698840133846
       66 MSE:
                0.00010461026249686256
Epoch
Epoch
       67 MSE:
                8.955403609434143e-05
       68 MSE:
Epoch
                9.18517544050701e-05
Epoch
       69 MSE:
                0.00010646247392287478
       70 MSE:
Epoch
                0.00010738568380475044
Epoch
       71 MSE:
                9.382425923831761e-05
       72 MSE:
Epoch
                8.669326052768156e-05
Epoch
       73 MSE:
                8.934784273151308e-05
Epoch
       74 MSE:
                8.730521949473768e-05
       75 MSE:
Epoch
                7.982452370924875e-05
Epoch
       76 MSE:
                7.928368722787127e-05
Epoch
       77 MSE:
                8.53856690810062e-05
Epoch
       78 MSE:
                8.628297655377537e-05
Epoch
       79 MSE:
                8.02856229711324e-05
       80 MSE:
Epoch
                7.656816887902096e-05
Epoch
       81 MSE:
                7.728430500719696e-05
       82 MSE:
                7.591867324663326e-05
Epoch
       83 MSE:
Epoch
                7.201219705166295e-05
Epoch
       84 MSE:
                7.155240018619224e-05
Epoch
       85 MSE:
                7.412180275423452e-05
Epoch
       86 MSE:
                7.383298361673951e-05
Epoch
       87 MSE:
                7.067456317599863e-05
Epoch
       88 MSE:
                6.922583997948095e-05
       89 MSE:
Epoch
                6.931586540304124e-05
```

Epoch 90 MSE: 6.783101707696915e-05 Epoch 91 MSE: 6.589944678125903e-05 Epoch 92 MSE: 6.608022522414103e-05 Epoch 93 MSE: 6.681826926069334e-05 Epoch 94 MSE: 6.576804298674688e-05 Epoch 95 MSE: 6.417343684006482e-05 Epoch 96 MSE: 6.370300252456218e-05 Epoch 97 MSE: 6.325494905468076e-05 Epoch 98 MSE: 6.197476614033803e-05 Epoch 99 MSE: 6.119403406046331e-05

T-time: 34.230958223342896

Train Score: 0.23 RMSE

Validation Score: 6.13 RMSE

Epoch 0 MSE: 0.08032264560461044 Epoch 1 MSE: 0.035551685839891434 Epoch 2 MSE: 0.05116846412420273 Epoch 3 MSE: 0.04154995083808899 Epoch 4 MSE: 0.033302243798971176 Epoch 5 MSE: 0.031155791133642197 Epoch 6 MSE: 0.031337346881628036 Epoch 7 MSE: 0.03104843571782112 Epoch 8 MSE: 0.028952408581972122 Epoch 9 MSE: 0.025274645537137985 Epoch 10 MSE: 0.021876228973269463 Epoch 11 MSE: 0.020408067852258682 Epoch 12 MSE: 0.020139390602707863 Epoch 13 MSE: 0.014192149043083191 Epoch 14 MSE: 0.008553129620850086 Epoch 15 MSE: 0.005493247415870428 Epoch 16 MSE: 0.0029248050414025784 Epoch 17 MSE: 0.00039923895383253694 Epoch 18 MSE: 0.004988205619156361 Epoch 19 MSE: 0.004192923661321402 Epoch 20 MSE: 0.003033807035535574 Epoch 21 MSE: 0.004022234585136175 Epoch 22 MSE: 0.003264114959165454 Epoch 23 MSE: 0.0011859379010275006 Epoch 24 MSE: 0.0004674609808716923 Epoch 25 MSE: 0.0023112338967621326 Epoch 26 MSE: 0.002315842779353261 Epoch 27 MSE: 0.0009322544210590422 Epoch 28 MSE: 0.0009870636276900768

0.001548962783999741

Epoch 29 MSE:

```
30 MSE:
Epoch
                0.0014694989658892155
Epoch
       31 MSE:
                0.0007473838049918413
       32 MSE:
Epoch
                0.00019985841936431825
Epoch
       33 MSE:
                0.0004861953784711659
Epoch
       34 MSE:
                0.0009089138475246727
       35 MSE:
Epoch
                0.0005565552273765206
Epoch
       36 MSE:
                0.00016840013267938048
Epoch
       37 MSE:
                0.0003518753801472485
Epoch
       38 MSE:
                0.0006105397478677332
Epoch
       39 MSE:
                0.0004665311425924301
       40 MSE:
Epoch
                0.00013540498912334442
Epoch
       41 MSE:
                0.00014247219951357692
Epoch
       42 MSE:
                0.0004337899445090443
Epoch
       43 MSE:
                0.000349457492120564
Epoch
      44 MSE:
                0.0001060503491316922
Epoch 45 MSE:
                0.0001747085334500298
Epoch
       46 MSE:
                0.0003238439094275236
       47 MSE:
Epoch
                0.0002457944501657039
Epoch
       48 MSE:
                8.178892312571406e-05
Epoch
       49 MSE:
                0.00011869287845911458
Epoch
       50 MSE:
                0.00024003033468034118
Epoch 51 MSE:
                0.00016651426267344505
       52 MSE:
Epoch
                7.306098996195942e-05
Epoch
       53 MSE:
                0.00012503174366429448
       54 MSE:
                0.00017768134421203285
Epoch
Epoch
       55 MSE:
                0.00012896090629510581
       56 MSE:
Epoch
                6.268874130910262e-05
Epoch
       57 MSE:
                8.841182716423646e-05
Epoch
       58 MSE:
                0.0001338555885013193
Epoch
      59 MSE:
                9.413640509592369e-05
       60 MSE:
Epoch
                5.910187610425055e-05
Epoch
       61 MSE:
                8.58085259096697e-05
       62 MSE:
Epoch
                0.00010465980449225754
       63 MSE:
Epoch
                7.666425517527387e-05
Epoch
       64 MSE:
                5.294810398481786e-05
Epoch
       65 MSE:
                7.063599332468584e-05
Epoch
       66 MSE:
                8.35168466437608e-05
Epoch
       67 MSE:
                6.167042010929435e-05
Epoch
       68 MSE:
                4.910775169264525e-05
Epoch
       69 MSE:
                6.256724009290338e-05
       70 MSE:
                6.610661512240767e-05
Epoch
Epoch
      71 MSE:
                4.8834524932317436e-05
Epoch
       72 MSE:
                4.2326249968027696e-05
Epoch
      73 MSE:
                5.4733034630771726e-05
Epoch
      74 MSE:
                5.139585482538678e-05
Epoch
       75 MSE:
                3.7977231841068715e-05
Epoch
       76 MSE:
                4.24158715759404e-05
       77 MSE:
Epoch
                4.7519028157694265e-05
```

```
Epoch 78 MSE: 3.794903386733495e-05
Epoch 79 MSE: 3.4167351259384304e-05
Epoch 80 MSE: 4.086664557689801e-05
Epoch 81 MSE:
               3.671753438538872e-05
Epoch 82 MSE:
               3.115051003987901e-05
Epoch 83 MSE:
               3.553550777724013e-05
Epoch 84 MSE: 3.488095899228938e-05
Epoch 85 MSE: 2.9133896532584913e-05
Epoch 86 MSE: 3.129536708001979e-05
Epoch 87 MSE:
               3.233586176065728e-05
Epoch 88 MSE:
               2.7757540010497905e-05
Epoch 89 MSE:
               2.8623830075957812e-05
Epoch 90 MSE:
               2.9776119845337234e-05
Epoch 91 MSE:
               2.624420631036628e-05
Epoch 92 MSE:
               2.6290481400792487e-05
Epoch 93 MSE: 2.736355054366868e-05
Epoch 94 MSE: 2.4705157557036728e-05
Epoch 95 MSE:
               2.4535429474781267e-05
Epoch 96 MSE: 2.5264382202294655e-05
Epoch 97 MSE:
               2.3218064598040655e-05
Epoch 98 MSE: 2.2893096684128977e-05
Epoch 99 MSE: 2.3428816348314285e-05
```

T-time: 29.321353435516357

Train Score: 0.14 RMSE

Validation Score: 1.04 RMSE

Time Step = 50 | Hidden States = 2 | Num Layers = 1

Epoch 0 MSE: 0.31157857179641724
Epoch 1 MSE: 0.274465948343277
Epoch 2 MSE: 0.24015702307224274
Epoch 3 MSE: 0.20867601037025452
Epoch 4 MSE: 0.17999505996704102
Epoch 5 MSE: 0.1540389060974121
Epoch 6 MSE: 0.13069333136081696
Epoch 7 MSE: 0.10981853306293488
Epoch 8 MSE: 0.09126532077789307
Epoch 9 MSE: 0.07489178329706192
Epoch 10 MSE: 0.060576099902391434
Epoch 11 MSE: 0.048222679644823074
Epoch 12 MSE: 0.0377601683139801
Epoch 13 MSE: 0.029132669791579247

```
Epoch
       14 MSE:
                0.022286368533968925
Epoch
       15 MSE:
                0.01715448871254921
       16 MSE:
Epoch
                0.013642610050737858
       17 MSE:
Epoch
                0.011616221629083157
Epoch
       18 MSE:
                0.010891943238675594
       19 MSE:
Epoch
                0.011234398931264877
Epoch
       20 MSE:
                0.012361180037260056
Epoch
       21 MSE:
                0.013957939110696316
                0.015703720971941948
Epoch
      22 MSE:
Epoch
       23 MSE:
                0.0173029862344265
       24 MSE:
                0.018517430871725082
Epoch
       25 MSE:
Epoch
                0.01918960176408291
Epoch
       26 MSE:
                0.01925242878496647
Epoch
       27 MSE:
                0.01872378960251808
Epoch
       28 MSE:
                0.017689146101474762
      29 MSE:
                0.016277816146612167
Epoch
Epoch
       30 MSE:
                0.014638300985097885
       31 MSE:
Epoch
                0.012916686944663525
Epoch
       32 MSE:
                0.011240355670452118
Epoch
       33 MSE:
                0.009707864373922348
Epoch
       34 MSE:
                0.008384647779166698
       35 MSE:
Epoch
                0.007303559221327305
Epoch
       36 MSE:
                0.006468869745731354
       37 MSE:
Epoch
                0.0058623491786420345
       38 MSE:
                0.005450138356536627
Epoch
Epoch
       39 MSE:
                0.005189417861402035
       40 MSE:
Epoch
                0.005034234840422869
Epoch
       41 MSE:
                0.004940156824886799
       42 MSE:
Epoch
                0.004867653828114271
Epoch
      43 MSE:
                0.004784300457686186
Epoch
      44 MSE:
                0.004665947053581476
Epoch
       45 MSE:
                0.004497068468481302
Epoch
       46 MSE:
                0.004270454403012991
       47 MSE:
Epoch
                0.003986436408013105
Epoch
       48 MSE:
                0.003651742357760668
Epoch
       49 MSE:
                0.003278110409155488
Epoch
       50 MSE:
                0.002880724845454097
Epoch
      51 MSE:
                0.0024765883572399616
       52 MSE:
Epoch
                0.002082879189401865
Epoch
       53 MSE:
                0.001715409685857594
      54 MSE:
Epoch
                0.0013872695853933692
       55 MSE:
Epoch
                0.0011077712988480926
       56 MSE:
                0.0008817793568596244
Epoch
       57 MSE:
Epoch
                0.0007095119799487293
Epoch
       58 MSE:
                0.000586838461458683
Epoch
       59 MSE:
                0.0005060596740804613
Epoch
       60 MSE:
                0.00045707420213148
       61 MSE:
                0.00042877771193161607
Epoch
```

```
Epoch 62 MSE:
                0.00041050775325857103
Epoch 63 MSE:
                0.00039330203435383737
Epoch 64 MSE:
                0.00037082150811329484
Epoch 65 MSE:
                0.0003397826221771538
Epoch 66 MSE:
                0.0002998964337166399
Epoch 67 MSE:
                0.000253351463470608
Epoch 68 MSE:
                0.00020399711502250284
Epoch 69 MSE:
                0.00015637239266652614
Epoch 70 MSE:
                0.00011478723172331229
Epoch 71 MSE:
                8.25768947834149e-05
Epoch 72 MSE:
                6.16390971117653e-05
Epoch 73 MSE:
                5.227417204878293e-05
Epoch 74 MSE:
                5.331104694050737e-05
Epoch 75 MSE:
                6.244683027034625e-05
Epoch 76 MSE:
                7.671258208574727e-05
Epoch 77 MSE:
                9.297105862060562e-05
Epoch 78 MSE:
                0.00010836675937753171
Epoch 79 MSE:
                0.00012066662748111412
Epoch 80 MSE:
                0.0001284603786189109
Epoch 81 MSE:
                0.00013121635129209608
Epoch
      82 MSE:
                0.00012919901928398758
Epoch 83 MSE:
                0.00012329264427535236
Epoch 84 MSE:
                0.00011476130748633295
Epoch 85 MSE:
                0.00010499406198505312
Epoch 86 MSE:
                9.52768386923708e-05
Epoch 87 MSE:
                8.661391620989889e-05
Epoch 88 MSE:
                7.962813833728433e-05
Epoch 89 MSE:
                7.453519356204197e-05
Epoch 90 MSE:
                7.118922803783789e-05
Epoch 91 MSE:
                6.917998689459637e-05
Epoch 92 MSE:
                6.795713125029579e-05
Epoch 93 MSE:
                6.69574219500646e-05
                6.571174162672833e-05
Epoch 94 MSE:
Epoch 95 MSE:
                6.391639180947095e-05
Epoch 96 MSE:
                6.146222585812211e-05
Epoch 97 MSE:
                5.842357131768949e-05
Epoch 98 MSE:
                5.501417399500497e-05
Epoch 99 MSE:
                5.152740050107241e-05
T-time: 4.240572452545166
```

1 01mc. 1.2100/2102010100

Train Score: 0.21 RMSE

Validation Score: 7.29 RMSE

Epoch 0 MSE: 0.38251420855522156 Epoch 1 MSE: 0.35181182622909546

```
Epoch 2 MSE:
               0.32369449734687805
Epoch
       3 MSE:
               0.29795703291893005
Epoch 4 MSE:
               0.27435585856437683
Epoch
      5 MSE:
               0.25269076228141785
Epoch
       6 MSE:
               0.23277676105499268
Epoch 7 MSE:
               0.21447035670280457
Epoch
       8 MSE:
               0.19763889908790588
Epoch 9 MSE:
               0.18216072022914886
Epoch 10 MSE:
                0.16792914271354675
Epoch
       11 MSE:
                0.15484730899333954
       12 MSE:
Epoch
                0.14282549917697906
Epoch
       13 MSE:
                0.13177983462810516
Epoch
       14 MSE:
                0.12163210660219193
Epoch
       15 MSE:
                0.11241607367992401
Epoch 16 MSE:
                0.10674384981393814
Epoch 17 MSE:
                0.10176607966423035
Epoch
       18 MSE:
                0.09720056504011154
       19 MSE:
Epoch
                0.09293875098228455
Epoch
       20 MSE:
                0.0889308825135231
Epoch
       21 MSE:
                0.0851457342505455
Epoch
       22 MSE:
                0.08155158907175064
      23 MSE:
Epoch
                0.07812110334634781
Epoch
      24 MSE:
                0.0748385414481163
Epoch
      25 MSE:
                0.07168788462877274
Epoch
      26 MSE:
                0.06865624338388443
Epoch
      27 MSE:
                0.06573276966810226
      28 MSE:
Epoch
                0.06290300190448761
Epoch
       29 MSE:
                0.06014883890748024
       30 MSE:
Epoch
                0.057457197457551956
Epoch
      31 MSE:
                0.05481176823377609
      32 MSE:
Epoch
                0.05219603329896927
Epoch
       33 MSE:
                0.0496007464826107
Epoch
       34 MSE:
                0.047019828110933304
Epoch
      35 MSE:
                0.04444627836346626
Epoch
       36 MSE:
                0.04187759384512901
Epoch
       37 MSE:
                0.039318766444921494
Epoch
       38 MSE:
                0.03678276017308235
Epoch
       39 MSE:
                0.03429441154003143
       40 MSE:
Epoch
                0.03191019967198372
Epoch
       41 MSE:
                0.02968771383166313
      42 MSE:
                0.028316570445895195
Epoch
Epoch
       43 MSE:
                0.02701506018638611
Epoch
       44 MSE:
                0.025083182379603386
      45 MSE:
Epoch
                0.022663593292236328
Epoch
      46 MSE:
                0.02073654532432556
Epoch
       47 MSE:
                0.01917991042137146
Epoch
       48 MSE:
                0.01772434450685978
       49 MSE:
                0.01634795404970646
Epoch
```

```
50 MSE:
                0.015054458752274513
Epoch
Epoch
       51 MSE:
                0.013852948322892189
Epoch
       52 MSE:
                0.012752470560371876
Epoch
       53 MSE:
                0.011765259318053722
Epoch
       54 MSE:
                0.010898460634052753
       55 MSE:
Epoch
                0.010146119631826878
Epoch
       56 MSE:
                0.009485051035881042
Epoch
       57 MSE:
                0.008878364227712154
Epoch
       58 MSE:
                0.008290158584713936
Epoch
       59 MSE:
                0.007703706622123718
       60 MSE:
                0.007127203047275543
Epoch
Epoch
       61 MSE:
                0.006583131849765778
Epoch
       62 MSE:
                0.006092946045100689
Epoch
       63 MSE:
                0.005664940923452377
Epoch
       64 MSE:
                0.0052930619567632675
       65 MSE:
                0.0049612876027822495
Epoch
Epoch
       66 MSE:
                0.0046510170213878155
       67 MSE:
Epoch
                0.004347875714302063
Epoch
       68 MSE:
                0.004045389126986265
Epoch
       69 MSE:
                0.0037450266536325216
Epoch
       70 MSE:
                0.0034532533027231693
Epoch
       71 MSE:
                0.0031791527289897203
Epoch
       72 MSE:
                0.002928272122517228
       73 MSE:
Epoch
                0.002703549340367317
       74 MSE:
                0.0025004770141094923
Epoch
Epoch
       75 MSE:
                0.0023096289951354265
       76 MSE:
Epoch
                0.002122241538017988
Epoch
       77 MSE:
                0.0019351367373019457
       78 MSE:
Epoch
                0.001752719865180552
Epoch
       79 MSE:
                0.0015813243808224797
       80 MSE:
                0.0014249839587137103
Epoch
Epoch
       81 MSE:
                0.0012850681087002158
       82 MSE:
Epoch
                0.0011599594727158546
       83 MSE:
Epoch
                0.0010466203093528748
Epoch
       84 MSE:
                0.0009426139295101166
Epoch
       85 MSE:
                0.000846589682623744
Epoch
       86 MSE:
                0.000758872483856976
Epoch
       87 MSE:
                0.00068130117142573
       88 MSE:
Epoch
                0.0006149869877845049
Epoch
       89 MSE:
                0.0005647081416100264
       90 MSE:
Epoch
                0.0005570084904320538
       91 MSE:
Epoch
                0.0005467167356982827
       92 MSE:
Epoch
                0.0005037646624259651
Epoch
       93 MSE:
                0.0004442764911800623
Epoch
       94 MSE:
                0.0003969528479501605
Epoch
       95 MSE:
                0.0003748251765500754
Epoch
       96 MSE:
                0.0003600818454287946
       97 MSE:
                0.00033583410549908876
Epoch
```

Epoch 98 MSE: 0.0003020145813934505 Epoch 99 MSE: 0.00026648290804587305

T-time: 4.318633794784546

Train Score: 0.49 RMSE

Validation Score: 1.16 RMSE

Time Step = 50 | Hidden States = 2 | Num Layers = 2

Epoch 0 MSE: 0.32251274585723877 Epoch 1 MSE: 0.2792542278766632 Epoch 2 MSE: 0.2405688315629959 Epoch 3 MSE: 0.20606914162635803 Epoch 4 MSE: 0.17512376606464386 Epoch 5 MSE: 0.14710022509098053 Epoch 6 MSE: 0.12166575342416763 Epoch 7 MSE: 0.09881794452667236 Epoch 8 MSE: 0.07874841243028641 Epoch 9 MSE: 0.06172080338001251 Epoch 10 MSE: 0.04798701032996178 Epoch 11 MSE: 0.037721067667007446 Epoch 12 MSE: 0.030959995463490486 Epoch 13 MSE: 0.027551651000976562 Epoch 14 MSE: 0.027117421850562096 Epoch 15 MSE: 0.029043367132544518 Epoch 16 MSE: 0.032517775893211365 Epoch 17 MSE: 0.036629583686590195 Epoch 18 MSE: 0.04051677882671356 Epoch 19 MSE: 0.043513208627700806 Epoch 20 MSE: 0.04523171856999397 Epoch 21 MSE: 0.04556409269571304 Epoch 22 MSE: 0.044624317437410355 Epoch 23 MSE: 0.04267236962914467 Epoch 24 MSE: 0.040041688829660416 Epoch 25 MSE: 0.037079647183418274 Epoch 26 MSE: 0.03410286828875542 Epoch 27 MSE: 0.03136730566620827 Epoch 28 MSE: 0.029051903635263443 Epoch 29 MSE: 0.027254745364189148 Epoch 30 MSE: 0.025999432429671288 Epoch 31 MSE: 0.025248751044273376 Epoch 32 MSE: 0.024922223761677742 Epoch 33 MSE: 0.024914326146245003

```
Epoch
       34 MSE:
                0.025110838934779167
Epoch
       35 MSE:
                0.02540198341012001
       36 MSE:
Epoch
                0.025691751390695572
       37 MSE:
Epoch
                0.025903666391968727
Epoch
       38 MSE:
                0.025983499363064766
Epoch
       39 MSE:
                0.025899583473801613
Epoch
       40 MSE:
                0.0256413035094738
Epoch
      41 MSE:
                0.025216370820999146
Epoch 42 MSE:
                0.024647200480103493
Epoch
       43 MSE:
                0.023966707289218903
       44 MSE:
                0.02321387268602848
Epoch
      45 MSE:
Epoch
                0.022429270669817924
Epoch
      46 MSE:
                0.021650811657309532
       47 MSE:
Epoch
                0.020910030230879784
Epoch
      48 MSE:
                0.020229164510965347
                0.019619306549429893
Epoch 49 MSE:
Epoch
      50 MSE:
                0.019079899415373802
       51 MSE:
Epoch
                0.018599584698677063
Epoch
       52 MSE:
                0.01815849170088768
Epoch
       53 MSE:
                0.017731571570038795
Epoch
       54 MSE:
                0.017292629927396774
Epoch 55 MSE:
                0.01681847684085369
Epoch 56 MSE:
                0.016292452812194824
Epoch 57 MSE:
                0.015706876292824745
Epoch
       58 MSE:
                0.015063927508890629
Epoch
       59 MSE:
                0.014374884776771069
       60 MSE:
Epoch
                0.013657861389219761
Epoch
       61 MSE:
                0.01293446496129036
       62 MSE:
Epoch
                0.012225968763232231
Epoch
       63 MSE:
                0.011549688875675201
Epoch
       64 MSE:
                0.010916161350905895
Epoch
       65 MSE:
                0.010327653959393501
       66 MSE:
                0.009778282605111599
Epoch
       67 MSE:
Epoch
                0.009255764074623585
Epoch
       68 MSE:
                0.008744578808546066
Epoch
       69 MSE:
                0.008229954168200493
Epoch
      70 MSE:
                0.007701869588345289
Epoch
      71 MSE:
                0.007158142048865557
      72 MSE:
Epoch
                0.0066056884825229645
Epoch
      73 MSE:
                0.006059448234736919
      74 MSE:
Epoch
                0.005538989789783955
Epoch
      75 MSE:
                0.005063504446297884
Epoch
       76 MSE:
                0.004646682180464268
      77 MSE:
Epoch
                0.004293165169656277
Epoch
       78 MSE:
                0.003998064436018467
Epoch
       79 MSE:
                0.0037499896716326475
Epoch
       80 MSE:
                0.0035365717485547066
       81 MSE:
                0.003350053681060672
Epoch
```

Epoch 82 MSE: 0.0031901546753942966 Epoch 83 MSE: 0.0030624661594629288 Epoch 84 MSE: 0.0029729953967034817 Epoch 85 MSE: 0.0029218827839940786 Epoch 86 MSE: 0.0029002961236983538 Epoch 87 MSE: 0.002892895136028528 Epoch 88 MSE: 0.0028846762143075466 Epoch 89 MSE: 0.002867706585675478 Epoch 90 MSE: 0.0028431485407054424 Epoch 91 MSE: 0.0028173974715173244 Epoch 92 MSE: 0.002795462729409337 Epoch 93 MSE: 0.002776520559564233 Epoch 94 MSE: 0.002754449611529708 Epoch 95 MSE: 0.002722322242334485 Epoch 96 MSE: 0.00267709675244987 Epoch 97 MSE: 0.0026212306693196297 Epoch 98 MSE: 0.0025605913251638412 Epoch 99 MSE: 0.002500686328858137 T-time: 9.37781286239624

Train Score: 1.49 RMSE

Validation Score: 18.89 RMSE

Epoch 0 MSE: 0.2983146607875824 Epoch 1 MSE: 0.2624007761478424 Epoch 2 MSE: 0.22686342895030975 Epoch 3 MSE: 0.19191820919513702 Epoch 4 MSE: 0.15793351829051971 Epoch 5 MSE: 0.12529034912586212 Epoch 6 MSE: 0.0944267213344574 Epoch 7 MSE: 0.06490244716405869 Epoch 8 MSE: 0.038068484514951706 Epoch 9 MSE: 0.016979778185486794 Epoch 10 MSE: 0.003872390603646636 Epoch 11 MSE: 0.0014087590388953686 Epoch 12 MSE: 0.010706746950745583 Epoch 13 MSE: 0.025127451866865158 Epoch 14 MSE: 0.03399338200688362 Epoch 15 MSE: 0.03452271595597267 Epoch 16 MSE: 0.029263250529766083 Epoch 17 MSE: 0.021767577156424522 Epoch 18 MSE: 0.014605884440243244 Epoch 19 MSE: 0.009087803773581982 Epoch 20 MSE: 0.005623484030365944 Epoch 21 MSE: 0.0040473793633282185

```
Epoch
       22 MSE:
                0.0039305840618908405
Epoch
       23 MSE:
                0.004777329508215189
       24 MSE:
Epoch
                0.0061150360852479935
       25 MSE:
Epoch
                0.007545291446149349
Epoch
       26 MSE:
                0.008729521185159683
Epoch
       27 MSE:
                0.009535643272101879
Epoch
       28 MSE:
                0.009926186874508858
Epoch
       29 MSE:
                0.009911119937896729
       30 MSE:
Epoch
                0.009537366218864918
Epoch
       31 MSE:
                0.008879153057932854
Epoch
       32 MSE:
                0.008027161471545696
       33 MSE:
Epoch
                0.0070787048898637295
Epoch
       34 MSE:
                0.006128082983195782
Epoch
       35 MSE:
                0.005257563199847937
Epoch
       36 MSE:
                0.004529489669948816
Epoch
      37 MSE:
                0.003981311805546284
Epoch
       38 MSE:
                0.003622346092015505
       39 MSE:
Epoch
                0.003435406368225813
Epoch
       40 MSE:
                0.003380151931196451
Epoch
       41 MSE:
                0.003399500623345375
Epoch
       42 MSE:
                0.0034316335804760456
Epoch
       43 MSE:
                0.0034317488316446543
Epoch 44 MSE:
                0.003384263953194022
      45 MSE:
Epoch
                0.0032308166846632957
       46 MSE:
                0.0029413083102554083
Epoch
Epoch
       47 MSE:
                0.0025401890743523836
       48 MSE:
Epoch
                0.0020859965588897467
Epoch
       49 MSE:
                0.0016459834296256304
       50 MSE:
Epoch
                0.0012752197217196226
Epoch 51 MSE:
                0.001003024517558515
Epoch 52 MSE:
                0.0008244698401540518
Epoch
       53 MSE:
                0.0007186877191998065
Epoch
       54 MSE:
                0.0006613301229663193
       55 MSE:
                0.0006270020385272801
Epoch
Epoch
       56 MSE:
                0.0005936726229265332
Epoch
       57 MSE:
                0.0005459401290863752
Epoch
       58 MSE:
                0.00047731431550346315
Epoch
       59 MSE:
                0.00038997395313344896
       60 MSE:
Epoch
                0.00029245333280414343
Epoch
       61 MSE:
                0.00019848736701533198
       62 MSE:
Epoch
                0.0001243402366526425
Epoch
       63 MSE:
                8.257530862465501e-05
Epoch
       64 MSE:
                7.802040636306629e-05
       65 MSE:
Epoch
                0.00010452608694322407
Epoch
       66 MSE:
                0.00014782341895624995
Epoch
       67 MSE:
                0.00019073208386544138
       68 MSE:
Epoch
                0.0002189613733207807
       69 MSE:
                0.0002255552972201258
Epoch
```

```
Epoch 70 MSE: 0.00021210774139035493
Epoch 71 MSE: 0.00018674314196687192
Epoch 72 MSE:
               0.0001599619135959074
Epoch 73 MSE:
               0.0001403318892698735
Epoch 74 MSE:
               0.00013171635509934276
Epoch 75 MSE:
               0.00013287222827784717
Epoch 76 MSE:
               0.00013889042020309716
Epoch 77 MSE:
               0.00014376295439433306
Epoch 78 MSE:
               0.0001427890092600137
               0.00013407555525191128
Epoch 79 MSE:
Epoch 80 MSE:
               0.00011881363025167957
Epoch 81 MSE:
               0.00010041182395070791
Epoch 82 MSE:
               8.30229910206981e-05
Epoch 83 MSE:
               7.001378253335133e-05
Epoch 84 MSE:
               6.294310151133686e-05
Epoch 85 MSE:
               6.13116062595509e-05
Epoch 86 MSE:
               6.306925206445158e-05
Epoch 87 MSE:
               6.559772737091407e-05
Epoch 88 MSE:
               6.673425377812237e-05
Epoch 89 MSE:
               6.546001532115042e-05
Epoch 90 MSE:
               6.204426608746871e-05
Epoch 91 MSE:
               5.767198672401719e-05
Epoch 92 MSE: 5.3791081882081926e-05
Epoch 93 MSE:
               5.1507526222849265e-05
Epoch 94 MSE: 5.118721310282126e-05
Epoch 95 MSE: 5.2438459533732384e-05
Epoch 96 MSE: 5.436624269350432e-05
Epoch 97 MSE: 5.597719064098783e-05
Epoch 98 MSE:
               5.655979839502834e-05
Epoch 99 MSE: 5.5887867347337306e-05
T-time: 8.846726655960083
```

Train Score: 0.22 RMSE _____ Validation Score: 1.18 RMSE _____

_____ Time Step = 50 | Hidden States = 4 | Num Layers = 1 ______

Epoch 0 MSE: 0.1314907819032669 Epoch 1 MSE: 0.09966854006052017 Epoch 2 MSE: 0.07924362272024155 Epoch 3 MSE: 0.06773138791322708 Epoch 4 MSE: 0.06244795024394989 Epoch 5 MSE: 0.06076423078775406

```
6 MSE:
               0.060443390160799026
Epoch
Epoch
       7 MSE:
               0.059954721480607986
      8 MSE:
Epoch
               0.05856472626328468
Epoch
       9 MSE:
               0.056177157908678055
Epoch
       10 MSE:
                0.053069353103637695
Epoch
       11 MSE:
                0.049662377685308456
Epoch
       12 MSE:
                0.046368636190891266
Epoch
       13 MSE:
                0.04350566491484642
Epoch 14 MSE:
                0.04125552624464035
Epoch
       15 MSE:
                0.03965604677796364
       16 MSE:
                0.038617126643657684
Epoch
       17 MSE:
Epoch
                0.037957366555929184
Epoch
       18 MSE:
                0.03745410591363907
       19 MSE:
Epoch
                0.03689640760421753
Epoch
       20 MSE:
                0.03612853214144707
Epoch
       21 MSE:
                0.035074397921562195
Epoch
       22 MSE:
                0.033740054816007614
       23 MSE:
Epoch
                0.032198015600442886
Epoch
       24 MSE:
                0.030560683459043503
Epoch
       25 MSE:
                0.028950003907084465
Epoch
       26 MSE:
                0.02746882103383541
       27 MSE:
Epoch
                0.0261781495064497
Epoch
       28 MSE:
                0.02508438564836979
       29 MSE:
Epoch
                0.024140246212482452
Epoch
       30 MSE:
                0.023261072114109993
Epoch
       31 MSE:
                0.022353120148181915
       32 MSE:
Epoch
                0.021344264969229698
Epoch
       33 MSE:
                0.02020561695098877
       34 MSE:
Epoch
                0.018956728279590607
Epoch
       35 MSE:
                0.01765436865389347
       36 MSE:
Epoch
                0.016370443627238274
Epoch
       37 MSE:
                0.01516662072390318
Epoch
       38 MSE:
                0.014073211699724197
       39 MSE:
Epoch
                0.013078787364065647
Epoch
       40 MSE:
                0.012135105207562447
Epoch
       41 MSE:
                0.011177808046340942
Epoch
       42 MSE:
                0.010156177915632725
Epoch
       43 MSE:
                0.009058460593223572
       44 MSE:
Epoch
                0.00791933760046959
Epoch
       45 MSE:
                0.006804853677749634
       46 MSE:
                0.005781357642263174
Epoch
       47 MSE:
Epoch
                0.0048830388113856316
Epoch
       48 MSE:
                0.0040961443446576595
       49 MSE:
Epoch
                0.003373140934854746
Epoch
       50 MSE:
                0.002671568188816309
                0.0019905902445316315
Epoch
       51 MSE:
Epoch
       52 MSE:
                0.0013769366778433323
       53 MSE:
                0.0008941838750615716
Epoch
```

Epoch 54 MSE: 0.0005750379059463739 Epoch 55 MSE: 0.00039275368908420205 Epoch 56 MSE: 0.00028323952574282885 57 MSE: Epoch 0.00020520255202427506 Epoch 58 MSE: 0.00017478095833212137 Epoch 59 MSE: 0.00023226845951285213 Epoch 60 MSE: 0.00037709411117248237 Epoch 61 MSE: 0.000547943520359695 Epoch 62 MSE: 0.0006765733705833554 Epoch 63 MSE: 0.0007496765465475619 Epoch 64 MSE: 0.0008012211183086038 Epoch 65 MSE: 0.0008516547386534512 Epoch 66 MSE: 0.0008767443359829485 Epoch 67 MSE: 0.0008438759832642972 Epoch 68 MSE: 0.0007587819127365947 Epoch 69 MSE: 0.0006586650852113962 Epoch 70 MSE: 0.000570029194932431 Epoch 71 MSE: 0.0004890807322226465 Epoch 72 MSE: 0.0004019462794531137 Epoch 73 MSE: 0.0003107734664808959 Epoch 74 MSE: 0.00023309970856644213 Epoch 75 MSE: 0.00018170010298490524 Epoch 76 MSE: 0.00015277392230927944 Epoch 77 MSE: 0.00013397543807514012 Epoch 78 MSE: 0.00011887882283190265 Epoch 79 MSE: 0.00011068520689150319 Epoch 80 MSE: 0.00011411037849029526 Epoch 81 MSE: 0.00012733715993817896 Epoch 82 MSE: 0.00014285888755694032 Epoch 83 MSE: 0.0001545045815873891 Epoch 84 MSE: 0.00016192416660487652 Epoch 85 MSE: 0.000168340586242266 Epoch 86 MSE: 0.0001753364340402186 87 MSE: 0.00018078014545608312 Epoch Epoch 88 MSE: 0.00018150020332541317 Epoch 89 MSE: 0.000176933579496108 Epoch 90 MSE: 0.00016955456521827728 Epoch 91 MSE: 0.00016207627777475864 92 MSE: Epoch 0.00015496491687372327 Epoch 93 MSE: 0.0001469301205361262 Epoch 94 MSE: 0.0001373344857711345 Epoch 95 MSE: 0.0001274484966415912 Epoch 96 MSE: 0.00011923016427317634 97 MSE: Epoch 0.00011337002797517926 Epoch 98 MSE: 0.00010898695472860709 99 MSE: Epoch 0.00010511052096262574 T-time: 4.362284183502197

Train Score: 0.31 RMSE

Validation Score: 10.12 RMSE

Epoch 0 MSE: 0.1186971515417099 Epoch 1 MSE: 0.10855698585510254 Epoch 2 MSE: 0.0993562862277031 Epoch 3 MSE: 0.09089664369821548 Epoch 4 MSE: 0.08318821340799332 Epoch 5 MSE: 0.07627323269844055 Epoch 6 MSE: 0.07021825015544891 Epoch 7 MSE: 0.06503153592348099 Epoch 8 MSE: 0.06077319383621216 Epoch 9 MSE: 0.057484809309244156 Epoch 10 MSE: 0.055149517953395844 Epoch 11 MSE: 0.05363272875547409 Epoch 12 MSE: 0.052679698914289474 Epoch 13 MSE: 0.05203123390674591 Epoch 14 MSE: 0.051500193774700165 Epoch 15 MSE: 0.05096609890460968 Epoch 16 MSE: 0.050358984619379044 Epoch 17 MSE: 0.04964883625507355 Epoch 18 MSE: 0.04883632808923721 Epoch 19 MSE: 0.047943368554115295 Epoch 20 MSE: 0.04700392484664917 Epoch 21 MSE: 0.04605603963136673 Epoch 22 MSE: 0.0451357327401638 Epoch 23 MSE: 0.044272806495428085 Epoch 24 MSE: 0.04348861053586006 Epoch 25 MSE: 0.042795367538928986 Epoch 26 MSE: 0.04219669848680496 Epoch 27 MSE: 0.04168892651796341 Epoch 28 MSE: 0.04126286134123802 Epoch 29 MSE: 0.04090571030974388 Epoch 30 MSE: 0.04060285910964012 Epoch 31 MSE: 0.04033953696489334 Epoch 32 MSE: 0.0401020348072052 Epoch 33 MSE: 0.03987859934568405 Epoch 34 MSE: 0.03966003656387329 Epoch 35 MSE: 0.03943987190723419 Epoch 36 MSE: 0.039214327931404114 Epoch 37 MSE: 0.038982052356004715 Epoch 38 MSE: 0.038743700832128525 Epoch 39 MSE: 0.03850141912698746 Epoch 40 MSE: 0.038258325308561325 Epoch 41 MSE: 0.03801795467734337

```
Epoch 42 MSE:
                0.03778379410505295
Epoch
      43 MSE:
                0.03755887225270271
Epoch 44 MSE:
                0.037345483899116516
       45 MSE:
Epoch
                0.037144966423511505
Epoch 46 MSE:
                0.03695766255259514
Epoch 47 MSE:
                0.03678296506404877
Epoch
       48 MSE:
                0.036619435995817184
Epoch 49 MSE:
                0.03646504878997803
Epoch 50 MSE:
                0.03631743788719177
Epoch 51 MSE:
                0.03617416322231293
Epoch
      52 MSE:
                0.036032941192388535
Epoch 53 MSE:
                0.03589187189936638
Epoch 54 MSE:
                0.03574955090880394
Epoch
       55 MSE:
                0.03560509905219078
Epoch 56 MSE:
                0.03545816242694855
Epoch 57 MSE:
                0.035308837890625
Epoch 58 MSE:
                0.03515751287341118
      59 MSE:
                0.035004738718271255
Epoch
Epoch
       60 MSE:
                0.03485110029578209
Epoch
       61 MSE:
                0.03469707816839218
Epoch
       62 MSE:
                0.034542959183454514
Epoch
      63 MSE:
                0.034388795495033264
Epoch 64 MSE:
                0.03423440456390381
       65 MSE:
Epoch
                0.03407935053110123
Epoch
       66 MSE:
                0.03392305597662926
Epoch
      67 MSE:
                0.0337647870182991
       68 MSE:
Epoch
                0.03360379487276077
Epoch
       69 MSE:
                0.033439334481954575
      70 MSE:
Epoch
                0.033270709216594696
Epoch 71 MSE:
                0.03309732303023338
Epoch 72 MSE:
                0.03291868418455124
Epoch 73 MSE:
                0.03273439779877663
Epoch
      74 MSE:
                0.032544154673814774
Epoch 75 MSE:
                0.03234768286347389
Epoch
      76 MSE:
                0.032144755125045776
Epoch
      77 MSE:
                0.03193512186408043
Epoch
     78 MSE:
                0.031718481332063675
Epoch
      79 MSE:
                0.03149449825286865
      80 MSE:
Epoch
                0.03126273676753044
Epoch 81 MSE:
                0.031022697687149048
      82 MSE:
                0.030773824080824852
Epoch
Epoch
       83 MSE:
                0.030515475198626518
Epoch
       84 MSE:
                0.030247000977396965
       85 MSE:
Epoch
                0.02996770478785038
Epoch
      86 MSE:
                0.029676880687475204
Epoch
       87 MSE:
                0.029373839497566223
Epoch
       88 MSE:
                0.02905786782503128
       89 MSE:
                0.02872828207910061
Epoch
```

```
Epoch 90 MSE: 0.028384385630488396
Epoch 91 MSE: 0.028025459498167038
Epoch 92 MSE: 0.027650775387883186
Epoch 93 MSE:
               0.02725955843925476
Epoch 94 MSE:
               0.026850996538996696
Epoch 95 MSE:
               0.02642422541975975
Epoch 96 MSE:
               0.025978934019804
Epoch 97 MSE: 0.025520185008645058
Epoch 98 MSE: 0.025064624845981598
Epoch 99 MSE:
               0.024600712582468987
T-time: 5.367801666259766
```

Train Score: 4.68 RMSE

Validation Score: 29.73 RMSE

Time Step = 50 | Hidden States = 4 | Num Layers = 2

```
Epoch 0 MSE: 0.14323055744171143
Epoch 1 MSE: 0.07705433666706085
Epoch 2 MSE: 0.03166572004556656
Epoch 3 MSE: 0.011026088148355484
Epoch 4 MSE: 0.013545108959078789
Epoch 5 MSE: 0.027578530833125114
Epoch 6 MSE: 0.037618063390254974
Epoch 7 MSE: 0.03799058869481087
Epoch 8 MSE: 0.031024808064103127
Epoch 9 MSE: 0.02121022716164589
Epoch 10 MSE: 0.012492011301219463
Epoch 11 MSE: 0.007211839780211449
Epoch 12 MSE:
               0.005841749254614115
Epoch 13 MSE:
               0.007379276677966118
Epoch 14 MSE:
               0.010138778947293758
Epoch 15 MSE:
               0.012511922046542168
Epoch 16 MSE:
               0.013440679758787155
Epoch 17 MSE:
               0.01257496327161789
Epoch 18 MSE:
               0.01020087394863367
Epoch 19 MSE:
               0.007039500866085291
Epoch 20 MSE:
               0.003984368871897459
Epoch 21 MSE:
               0.0018196848686784506
Epoch 22 MSE:
               0.0009704874246381223
Epoch 23 MSE:
               0.001363926799967885
Epoch 24 MSE:
               0.002479343209415674
Epoch 25 MSE: 0.003592022694647312
```

```
Epoch
       26 MSE:
                0.004100796300917864
Epoch
       27 MSE:
                0.003770773531869054
       28 MSE:
Epoch
                0.002780571114271879
       29 MSE:
Epoch
                0.0015824810834601521
Epoch
       30 MSE:
                0.000667296932078898
Epoch
       31 MSE:
                0.0003436586994212121
Epoch
       32 MSE:
                0.0006208047270774841
Epoch
       33 MSE:
                0.0012386811431497335
       34 MSE:
Epoch
                0.001822423655539751
Epoch
       35 MSE:
                0.0020742283668369055
       36 MSE:
                0.0019003915367648005
Epoch
       37 MSE:
Epoch
                0.001419444801285863
Epoch
       38 MSE:
                0.0008690347312949598
Epoch
       39 MSE:
                0.0004749122599605471
Epoch
       40 MSE:
                0.0003495789133012295
Epoch 41 MSE:
                0.0004617781669367105
Epoch
       42 MSE:
                0.0006785224541090429
       43 MSE:
Epoch
                0.0008470647153444588
Epoch
       44 MSE:
                0.0008705742657184601
Epoch
       45 MSE:
                0.0007427729433402419
Epoch
       46 MSE:
                0.0005332704749889672
Epoch
      47 MSE:
                0.0003402528236620128
Epoch 48 MSE:
                0.0002389542496530339
       49 MSE:
Epoch
                0.0002505249867681414
       50 MSE:
                0.00034173906897194684
Epoch
Epoch
       51 MSE:
                0.00044979582889936864
       52 MSE:
Epoch
                0.0005161336739547551
Epoch
       53 MSE:
                0.0005122342263348401
       54 MSE:
Epoch
                0.0004472764558158815
Epoch 55 MSE:
                0.000357348209945485
Epoch 56 MSE:
                0.0002840677625499666
Epoch
       57 MSE:
                0.00025390228256583214
Epoch
       58 MSE:
                0.00026773728313855827
       59 MSE:
                0.0003043886099476367
Epoch
Epoch
       60 MSE:
                0.00033465467276982963
Epoch
       61 MSE:
                0.0003375581873115152
Epoch
       62 MSE:
                0.0003101397305727005
Epoch
       63 MSE:
                0.0002664741186890751
       64 MSE:
Epoch
                0.00022777999402023852
Epoch
       65 MSE:
                0.00021005324379075319
       66 MSE:
Epoch
                0.00021619917242787778
       67 MSE:
Epoch
                0.00023634197714272887
Epoch
       68 MSE:
                0.0002550533099565655
Epoch
       69 MSE:
                0.00026058609364554286
Epoch
       70 MSE:
                0.0002507063327357173
Epoch
       71 MSE:
                0.00023234209220390767
Epoch
       72 MSE:
                0.00021611321426462382
       73 MSE:
                0.00020959069661330432
Epoch
```

Epoch 74 MSE: 0.0002133645029971376 Epoch 75 MSE: 0.00022181090025696903 Epoch 76 MSE: 0.00022742869623471051 Epoch 77 MSE: 0.00022563280072063208 Epoch 78 MSE: 0.00021705632389057428 Epoch 79 MSE: 0.0002063507417915389 Epoch 80 MSE: 0.00019875199359375983 Epoch 81 MSE: 0.00019684812286868691 Epoch 82 MSE: 0.00019947908003814518 Epoch 83 MSE: 0.00020308526291046292 Epoch 84 MSE: 0.00020428551943041384 Epoch 85 MSE: 0.00020189967472106218 Epoch 86 MSE: 0.000197271685465239 Epoch 87 MSE: 0.00019297281687613577 Epoch 88 MSE: 0.00019095301104243845 Epoch 89 MSE: 0.0001913907181005925 Epoch 90 MSE: 0.0001928560232045129 Epoch 91 MSE: 0.0001934835163410753 Epoch 92 MSE: 0.00019224493007641286 Epoch 93 MSE: 0.00018948328215628862 Epoch 94 MSE: 0.00018647241813596338 Epoch 95 MSE: 0.00018443813314661384 Epoch 96 MSE: 0.0001837677409639582 Epoch 97 MSE: 0.0001839007600210607 Epoch 98 MSE: 0.00018386775627732277 Epoch 99 MSE: 0.0001830144174164161 T-time: 7.643624782562256

Train Score: 0.40 RMSE

Validation Score: 10.24 RMSE

Epoch 0 MSE: 0.2548750638961792 Epoch 1 MSE: 0.20947271585464478 Epoch 2 MSE: 0.17074038088321686 Epoch 3 MSE: 0.1392860859632492 Epoch 4 MSE: 0.11247456073760986 Epoch 5 MSE: 0.08983669430017471 Epoch 6 MSE: 0.07093240320682526 Epoch 7 MSE: 0.05536279454827309 Epoch 8 MSE: 0.04273531585931778 Epoch 9 MSE: 0.03266267850995064 Epoch 10 MSE: 0.024774374440312386 Epoch 11 MSE: 0.018675347790122032 Epoch 12 MSE: 0.013988408260047436 13 MSE: Epoch 0.010368702933192253

```
Epoch
       14 MSE:
                0.007540044374763966
Epoch
       15 MSE:
                0.005556996446102858
       16 MSE:
Epoch
                0.003597826464101672
       17 MSE:
Epoch
                0.0018764069536700845
Epoch
       18 MSE:
                0.0009370867046527565
       19 MSE:
Epoch
                0.0009127174271270633
Epoch
      20 MSE:
                0.0012795000802725554
Epoch
      21 MSE:
                0.0013538140337914228
Epoch
      22 MSE:
                0.0012608020333573222
Epoch
      23 MSE:
                0.0013220853870734572
      24 MSE:
                0.0016310728387907147
Epoch
Epoch
      25 MSE:
                0.0020313384011387825
Epoch
      26 MSE:
                0.002232971368357539
Epoch
       27 MSE:
                0.002091008936986327
Epoch
      28 MSE:
                0.001665716990828514
Epoch 29 MSE:
                0.0011438473593443632
Epoch
      30 MSE:
                0.0007185135036706924
      31 MSE:
Epoch
                0.00048261554911732674
Epoch
       32 MSE:
                0.0004241899587213993
Epoch
       33 MSE:
                0.00042441801633685827
Epoch
       34 MSE:
                0.0003465802874416113
Epoch
      35 MSE:
                0.00022195346537046134
Epoch
      36 MSE:
                0.00016692615463398397
      37 MSE:
Epoch
                0.00023414872703142464
      38 MSE:
                0.00037366707692854106
Epoch
Epoch
       39 MSE:
                0.0004899949417449534
      40 MSE:
Epoch
                0.0005202196771278977
Epoch
       41 MSE:
                0.00047153938794508576
      42 MSE:
Epoch
                0.0004000832268502563
Epoch 43 MSE:
                0.0003584879741538316
Epoch 44 MSE:
                0.0003576953604351729
Epoch
       45 MSE:
                0.00035617954563349485
Epoch
      46 MSE:
                0.00029604663723148406
      47 MSE:
                0.0001965480187209323
Epoch
Epoch
       48 MSE:
                0.00012560213508550078
Epoch
       49 MSE:
                0.0001120456654462032
Epoch
       50 MSE:
                0.0001240015117218718
Epoch
      51 MSE:
                0.00012031615915475413
Epoch
      52 MSE:
                9.406748722540215e-05
Epoch
      53 MSE:
                7.367852958850563e-05
Epoch 54 MSE:
                8.66732225404121e-05
       55 MSE:
Epoch
                0.00011907225416507572
Epoch
       56 MSE:
                0.000131021675770171
       57 MSE:
Epoch
                0.00011256567086093128
Epoch
      58 MSE:
                9.193331788992509e-05
Epoch
       59 MSE:
                8.860564412316307e-05
Epoch
       60 MSE:
                9.012631926452741e-05
       61 MSE:
Epoch
                7.674513472011313e-05
```

```
Epoch 62 MSE: 5.09872697875835e-05
Epoch 63 MSE: 3.3276020985795185e-05
Epoch 64 MSE:
               3.3359607186866924e-05
Epoch 65 MSE:
               3.822182770818472e-05
Epoch 66 MSE:
               3.3725857065292075e-05
Epoch 67 MSE:
               2.6756553779705428e-05
Epoch 68 MSE:
               2.9733075280091725e-05
Epoch 69 MSE:
               3.8597165257669985e-05
Epoch 70 MSE:
               4.116951458854601e-05
Epoch 71 MSE:
               3.5667231713887304e-05
Epoch 72 MSE:
               3.1022045732242987e-05
Epoch 73 MSE:
               3.1680145184509456e-05
Epoch 74 MSE:
               3.144107904518023e-05
Epoch 75 MSE:
               2.57006522588199e-05
Epoch 76 MSE:
               1.9562159650376998e-05
Epoch 77 MSE:
               1.8304715922567993e-05
Epoch 78 MSE:
               1.969542063307017e-05
Epoch 79 MSE:
               1.9236835214542225e-05
Epoch 80 MSE:
               1.744870314723812e-05
Epoch 81 MSE:
               1.7863099856185727e-05
Epoch 82 MSE:
               2.0439592844923027e-05
Epoch 83 MSE:
               2.1669125999324024e-05
Epoch 84 MSE:
               2.0480476450757124e-05
Epoch 85 MSE:
               1.9369263100088574e-05
Epoch 86 MSE:
               1.9604658518801443e-05
Epoch 87 MSE:
               1.9490445993142202e-05
Epoch 88 MSE:
               1.7903559637488797e-05
Epoch 89 MSE:
               1.633459032746032e-05
Epoch 90 MSE:
               1.620220791664906e-05
Epoch 91 MSE:
               1.663383409322705e-05
Epoch 92 MSE:
               1.6380989109165967e-05
Epoch 93 MSE:
               1.5988274753908627e-05
Epoch 94 MSE:
               1.641104245209135e-05
Epoch 95 MSE:
               1.710785727482289e-05
Epoch 96 MSE:
               1.7090227629523724e-05
Epoch 97 MSE:
               1.66273439390352e-05
Epoch 98 MSE:
               1.6515581592102535e-05
Epoch 99 MSE:
               1.6583604519837536e-05
T-time: 8.104247093200684
```

Train Score: 0.12 RMSE

Validation Score: 5.93 RMSE

Time Chan - FO | Hidden Chahan - O | Num I arrang - 1

Time Step = 50 | Hidden States = 8 | Num Layers = 1

Epoch	O MSE:	0.05277542769908905
Epoch	1 MSE:	0.033643484115600586
Epoch	2 MSE:	0.027371756732463837
Epoch	3 MSE:	0.03110847808420658
Epoch	4 MSE:	0.03099544160068035
Epoch	5 MSE:	0.026062138378620148
Epoch	6 MSE:	0.02096349373459816
Epoch	7 MSE:	0.01812741532921791
Epoch	8 MSE:	0.017313720658421516
Epoch	9 MSE:	0.017013566568493843
Epoch	10 MSE:	0.015765618532896042
Epoch	11 MSE:	0.013008645735681057
Epoch	12 MSE:	0.009321438148617744
Epoch	13 MSE:	0.006111638154834509
Epoch	14 MSE:	0.004736440721899271
Epoch	15 MSE:	0.0047627962194383144
Epoch	16 MSE:	0.0036732531152665615
Epoch	17 MSE:	0.001121554640121758
Epoch	18 MSE:	0.0004215968365315348
Epoch	19 MSE:	0.0027332317549735308
Epoch	20 MSE:	0.003404169110581279
Epoch	21 MSE:	0.002193282125517726
Epoch	22 MSE:	0.00280025159008801
Epoch	23 MSE:	0.003317943075671792
Epoch	24 MSE:	0.001857275958172977
Epoch	25 MSE:	0.0007255722885020077
Epoch	26 MSE:	0.0007261766586452723
Epoch	27 MSE:	0.0008296555606648326
Epoch	28 MSE:	0.0005625989870168269
Epoch	29 MSE:	0.0002929701586253941
Epoch	30 MSE:	0.00038014983874745667
Epoch	31 MSE:	0.0007270808564499021
Epoch	32 MSE:	0.0009805804584175348
Epoch	33 MSE:	0.0009560370817780495
Epoch	34 MSE:	0.0007747067138552666
Epoch	35 MSE:	0.000650860252790153
Epoch	36 MSE:	0.0006476761191152036
Epoch	37 MSE:	0.0006514543201774359
Epoch	38 MSE:	0.0005367387784644961
Epoch	39 MSE:	0.0003211994480807334
Epoch	40 MSE:	0.0003211994400007334
Epoch	40 MSE:	0.00014080419330873098
Epoch	41 MSE:	0.00012414437100046187
_	42 MSE:	0.0001877350093922704
Epoch		
Epoch		0.00015503466420341283
Epoch	45 MSE:	0.0001450743293389678

```
Epoch
       46 MSE:
                0.00021962146274745464
Epoch
       47 MSE:
                0.00028736284002661705
Epoch
       48 MSE:
                0.0002641823666635901
       49 MSE:
Epoch
                0.00019160451483912766
Epoch
       50 MSE:
                0.0001557231298647821
Epoch
       51 MSE:
                0.00015864960732869804
Epoch
       52 MSE:
                0.00014088339230511338
Epoch
      53 MSE:
                9.086015052162111e-05
Epoch 54 MSE:
                5.7289325923193246e-05
Epoch
      55 MSE:
                6.79414879414253e-05
       56 MSE:
                9.484769543632865e-05
Epoch
Epoch
       57 MSE:
                0.00010238772665616125
Epoch
       58 MSE:
                9.294885239796713e-05
Epoch
       59 MSE:
                9.154921281151474e-05
Epoch
       60 MSE:
                0.0001040769275277853
Epoch 61 MSE:
                0.00011062443809350953
Epoch
       62 MSE:
                9.747299191076308e-05
       63 MSE:
Epoch
                7.676213863305748e-05
Epoch
       64 MSE:
                6.695127376588061e-05
Epoch
       65 MSE:
                6.73809481668286e-05
Epoch
       66 MSE:
                6.432925874833018e-05
Epoch
       67 MSE:
                5.489083196152933e-05
Epoch
       68 MSE:
                5.044543286203407e-05
       69 MSE:
Epoch
                5.670894461218268e-05
      70 MSE:
                6.421079888241366e-05
Epoch
Epoch
      71 MSE:
                6.383925210684538e-05
      72 MSE:
Epoch
                5.989987766952254e-05
Epoch
     73 MSE:
                5.991043144604191e-05
Epoch 74 MSE:
                6.147837120806798e-05
Epoch 75 MSE:
                5.8233730669599026e-05
Epoch 76 MSE:
                5.1664203056134284e-05
Epoch 77 MSE:
                4.8274796426994726e-05
Epoch
      78 MSE:
                4.898921542917378e-05
       79 MSE:
Epoch
                4.9195838073501363e-05
Epoch
       80 MSE:
                4.739441646961495e-05
Epoch
       81 MSE:
                4.680105848819949e-05
Epoch
       82 MSE:
                4.8723410145612434e-05
Epoch
       83 MSE:
                5.022453478886746e-05
Epoch
       84 MSE:
                4.922527296002954e-05
Epoch
       85 MSE:
                4.74858570669312e-05
       86 MSE:
Epoch
                4.699717464973219e-05
Epoch
       87 MSE:
                4.679109406424686e-05
       88 MSE:
                4.535051994025707e-05
Epoch
Epoch
       89 MSE:
                4.3596843170234933e-05
Epoch
       90 MSE:
                4.3175263272132725e-05
Epoch
       91 MSE:
                4.363906919024885e-05
Epoch
       92 MSE:
                4.3555912270676345e-05
Epoch
       93 MSE:
                4.3029118387494236e-05
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Epoch 94 MSE: 4.305935726733878e-05 Epoch 95 MSE: 4.34273861174006e-05 4.3146741518285125e-05 Epoch 96 MSE: Epoch 97 MSE: 4.230616832501255e-05 Epoch 98 MSE: 4.176564470981248e-05 Epoch 99 MSE: 4.158173760515638e-05

T-time: 8.075310945510864

Train Score: 0.19 RMSE ______ Validation Score: 6.50 RMSE _____

Epoch 0 MSE: 0.05107605829834938 Epoch 1 MSE: 0.04004030302166939 Epoch 2 MSE: 0.03527151793241501 Epoch 3 MSE: 0.03595487400889397 Epoch 4 MSE: 0.03649058938026428 Epoch 5 MSE: 0.03463391587138176 Epoch 6 MSE: 0.03175199031829834 Epoch 7 MSE: 0.029292870312929153 Epoch 8 MSE: 0.027760183438658714 Epoch 9 MSE: 0.02689700946211815 Epoch 10 MSE: 0.02612174116075039 Epoch 11 MSE: 0.02497224695980549 Epoch 12 MSE: 0.023285744711756706 Epoch 13 MSE: 0.02113979309797287 Epoch 14 MSE: 0.018769217655062675 Epoch 15 MSE: 0.016430851072072983 Epoch 16 MSE: 0.014494338072836399 Epoch 17 MSE: 0.013307006098330021 Epoch 18 MSE: 0.012073840014636517 Epoch 19 MSE: 0.010792993940412998 Epoch 20 MSE: 0.009489445015788078 Epoch 21 MSE: 0.008210168220102787 Epoch 22 MSE: 0.006959737744182348 Epoch 23 MSE: 0.005710451398044825 Epoch 24 MSE: 0.0044453502632677555 Epoch 25 MSE: 0.0032381669152528048 Epoch 26 MSE: 0.002202258910983801 Epoch 27 MSE: 0.001387683441862464 Epoch 28 MSE: 0.000759642047341913 Epoch 29 MSE: 0.00038715353002771735 Epoch 30 MSE: 0.00040948999230749905 Epoch 31 MSE: 0.0006827000761404634 Epoch 32 MSE: 0.0011508691823109984 33 MSE: 0.0017028958536684513

Epoch

```
Epoch
       34 MSE:
                0.001996823586523533
Epoch
       35 MSE:
                0.002097015269100666
       36 MSE:
Epoch
                0.001881587551906705
       37 MSE:
Epoch
                0.0015412576030939817
Epoch
       38 MSE:
                0.001161094638518989
Epoch
       39 MSE:
                0.0007943956297822297
Epoch
       40 MSE:
                0.000552199489902705
Epoch
       41 MSE:
                0.0003902899334207177
Epoch 42 MSE:
                0.0003178273618686944
Epoch
       43 MSE:
                0.0003285071870777756
       44 MSE:
Epoch
                0.0003647264966275543
Epoch
      45 MSE:
                0.00042428795131854713
Epoch
      46 MSE:
                0.0004958066856488585
Epoch
       47 MSE:
                0.000546063354704529
Epoch
       48 MSE:
                0.0005780674400739372
Epoch 49 MSE:
                0.0005925691220909357
Epoch
      50 MSE:
                0.0005734305595979095
       51 MSE:
Epoch
                0.0005283391219563782
Epoch
       52 MSE:
                0.0004651464114431292
Epoch
       53 MSE:
                0.00037587559199891984
Epoch
       54 MSE:
                0.00026980318943969905
Epoch
       55 MSE:
                0.00016475051234010607
Epoch
       56 MSE:
                8.502617129124701e-05
      57 MSE:
Epoch
                8.508393511874601e-05
       58 MSE:
                0.00016993246390484273
Epoch
Epoch
       59 MSE:
                0.0002237538283225149
       60 MSE:
Epoch
                0.00019740679999813437
Epoch
       61 MSE:
                0.00012682298256549984
Epoch
       62 MSE:
                6.5899635956157e-05
Epoch
      63 MSE:
                5.141031215316616e-05
Epoch
       64 MSE:
                6.564151408383623e-05
Epoch
       65 MSE:
                7.967980491230264e-05
Epoch
       66 MSE:
                9.341305849375203e-05
       67 MSE:
Epoch
                0.00010398658196208999
Epoch
       68 MSE:
                9.903024329105392e-05
Epoch
       69 MSE:
                8.732677815714851e-05
Epoch
       70 MSE:
                7.763064786558971e-05
Epoch
      71 MSE:
                6.357915845001116e-05
Epoch
       72 MSE:
                4.773249747813679e-05
Epoch
      73 MSE:
                4.050463030580431e-05
Epoch 74 MSE:
                3.5890039725927636e-05
Epoch
      75 MSE:
                3.5949356970377266e-05
Epoch
       76 MSE:
                4.342601096141152e-05
Epoch
      77 MSE:
                4.5397489884635434e-05
Epoch
       78 MSE:
                4.4929776777280495e-05
Epoch
       79 MSE:
                3.7954891013214365e-05
Epoch
       80 MSE:
                2.7990405214950442e-05
       81 MSE:
Epoch
                2.3677735953242518e-05
```

Epoch 82 MSE: 2.1412579371826723e-05 Epoch 83 MSE: 2.3944041458889842e-05 Epoch 84 MSE: 2.77411727438448e-05 Epoch 85 MSE: 2.9489809094229713e-05 Epoch 86 MSE: 3.103975541307591e-05 Epoch 87 MSE: 2.915106961154379e-05 Epoch 88 MSE: 2.6598685508361086e-05 Epoch 89 MSE: 2.4301105440827087e-05 Epoch 90 MSE: 2.237541957583744e-05 2.3244279873324558e-05 Epoch 91 MSE: Epoch 92 MSE: 2.427177423669491e-05 Epoch 93 MSE: 2.548043630667962e-05 Epoch 94 MSE: 2.5487539460300468e-05 Epoch 95 MSE: 2.376167321926914e-05 Epoch 96 MSE: 2.234421481261961e-05 Epoch 97 MSE: 2.083552499243524e-05 Epoch 98 MSE: 2.0603296434273943e-05 Epoch 99 MSE: 2.093413786496967e-05

T-time: 7.4773783683776855

Train Score: 0.14 RMSE

Validation Score: 2.07 RMSE

Time Step = 50 | Hidden States = 8 | Num Layers = 2

Epoch 0 MSE: 0.049534283578395844 Epoch 1 MSE: 0.03613725304603577 Epoch 2 MSE: 0.04224362596869469 Epoch 3 MSE: 0.03396686911582947 Epoch 4 MSE: 0.02619454823434353 Epoch 5 MSE: 0.025210566818714142 Epoch 6 MSE: 0.025679243728518486 Epoch 7 MSE: 0.021631304174661636 Epoch 8 MSE: 0.014802113175392151 Epoch 9 MSE: 0.010425366461277008 Epoch 10 MSE: 0.010052536614239216 Epoch 11 MSE: 0.007831976749002934 Epoch 12 MSE: 0.002323599997907877 Epoch 13 MSE: 0.001172170857898891 Epoch 14 MSE: 0.0048719365149736404 Epoch 15 MSE: 0.0036352600436657667 Epoch 16 MSE: 0.004670266527682543 Epoch 17 MSE: 0.005947055295109749

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Epoch
       18 MSE:
                0.002873108722269535
Epoch
       19 MSE:
                0.0017630826914682984
       20 MSE:
Epoch
                0.0019090425921604037
       21 MSE:
Epoch
                0.0010957331396639347
Epoch
       22 MSE:
                0.000485600990941748
Epoch
       23 MSE:
                0.0009746202267706394
Epoch
       24 MSE:
                0.0017804659437388182
Epoch
       25 MSE:
                0.0019863720517605543
       26 MSE:
Epoch
                0.0016921231290325522
Epoch
       27 MSE:
                0.001501346123404801
       28 MSE:
                0.0015864038141444325
Epoch
       29 MSE:
Epoch
                0.001566495280712843
Epoch
       30 MSE:
                0.0011537588434293866
Epoch
       31 MSE:
                0.0006095218705013394
Epoch
       32 MSE:
                0.0003920425660908222
       33 MSE:
                0.0005012055626139045
Epoch
Epoch
       34 MSE:
                0.0005283404607325792
       35 MSE:
Epoch
                0.00038635756936855614
Epoch
       36 MSE:
                0.00042304451926611364
Epoch
       37 MSE:
                0.0006802321295253932
       38 MSE:
Epoch
                0.0007608560263179243
       39 MSE:
Epoch
                0.0005761429783888161
Epoch
       40 MSE:
                0.0004453910223674029
       41 MSE:
Epoch
                0.00044673465890809894
       42 MSE:
                0.0003723136323969811
Epoch
Epoch
       43 MSE:
                0.00021913988166488707
       44 MSE:
Epoch
                0.00017636911070439965
Epoch
       45 MSE:
                0.0002590410294942558
       46 MSE:
Epoch
                0.0003138099564239383
Epoch
      47 MSE:
                0.0002923816500697285
Epoch
       48 MSE:
                0.00028352232766337693
Epoch
       49 MSE:
                0.0003177386533934623
       50 MSE:
Epoch
                0.0003173197037540376
       51 MSE:
                0.0002495652297511697
Epoch
Epoch
       52 MSE:
                0.00018760247621685266
Epoch
       53 MSE:
                0.00017994317749980837
Epoch
       54 MSE:
                0.0001800139871193096
Epoch
       55 MSE:
                0.00015494997205678374
       56 MSE:
Epoch
                0.00014871699386276305
Epoch
       57 MSE:
                0.00018066129996441305
       58 MSE:
                0.00019815022824332118
Epoch
       59 MSE:
Epoch
                0.00017967379244510084
Epoch
       60 MSE:
                0.00016589052393101156
Epoch
       61 MSE:
                0.0001662043941905722
Epoch
       62 MSE:
                0.00015030486974865198
Epoch
       63 MSE:
                0.00012481134035624564
Epoch
       64 MSE:
                0.00012054479884682223
       65 MSE:
Epoch
                0.00012999132741242647
```

Epoch 66 MSE: 0.00012924015754833817 Epoch 67 MSE: 0.00012531715037766844 Epoch 68 MSE: 0.00013119931099936366 Epoch 69 MSE: 0.00013417532318271697 Epoch 70 MSE: 0.0001240206038346514 Epoch 71 MSE: 0.00011405388795537874 Epoch 72 MSE: 0.00011227204231545329 Epoch 73 MSE: 0.00010869649122469127 Epoch 74 MSE: 0.00010207529703620821 Epoch 75 MSE: 0.00010240547271678224 Epoch 76 MSE: 0.00010674740769900382 Epoch 77 MSE: 0.00010560282680671662 Epoch 78 MSE: 0.00010255083907395601 Epoch 79 MSE: 0.00010248195758322254 Epoch 80 MSE: 0.00010011794802267104 Epoch 81 MSE: 9.457547275815159e-05 Epoch 82 MSE: 9.219706407748163e-05 Epoch 83 MSE: 9.238385973731056e-05 Epoch 84 MSE: 9.085761121241376e-05 Epoch 85 MSE: 8.975642413133755e-05 Epoch 86 MSE: 9.071014210348949e-05 Epoch 87 MSE: 9.013820817926899e-05 Epoch 88 MSE: 8.765001257415861e-05 Epoch 89 MSE: 8.62531887833029e-05 Epoch 90 MSE: 8.518608956364915e-05 Epoch 91 MSE: 8.304100629175082e-05 Epoch 92 MSE: 8.183359750546515e-05 Epoch 93 MSE: 8.192398672690615e-05 Epoch 94 MSE: 8.128220360958949e-05 Epoch 95 MSE: 8.033842459553853e-05 Epoch 96 MSE: 8.002785762073472e-05 Epoch 97 MSE: 7.911511056590825e-05 Epoch 98 MSE: 7.7586475526914e-05 7.672087667742744e-05 Epoch 99 MSE: T-time: 10.554943561553955

Train Score: 0.26 RMSE

Validation Score: 8.98 RMSE

Epoch 0 MSE: 0.03806096687912941 Epoch 1 MSE: 0.032404232770204544 Epoch 2 MSE: 0.03330131247639656 Epoch 3 MSE: 0.03208773955702782 Epoch 4 MSE: 0.029647933319211006 Epoch 5 MSE: 0.028005357831716537

```
6 MSE:
               0.026818061247467995
Epoch
Epoch
       7 MSE:
               0.02503168024122715
Epoch
      8 MSE:
               0.022311845794320107
       9 MSE:
Epoch
               0.019462913274765015
Epoch
       10 MSE:
                0.01761730946600437
Epoch
       11 MSE:
                0.015948673710227013
Epoch
       12 MSE:
                0.01295458059757948
Epoch
       13 MSE:
                0.010418008081614971
       14 MSE:
Epoch
                0.00891593936830759
Epoch
       15 MSE:
                0.006462664343416691
       16 MSE:
                0.004677792079746723
Epoch
       17 MSE:
Epoch
                0.0036468920297920704
Epoch
       18 MSE:
                0.0026191051583737135
Epoch
       19 MSE:
                0.002225121483206749
Epoch
       20 MSE:
                0.002811378799378872
Epoch
       21 MSE:
                0.0028137913905084133
Epoch
       22 MSE:
                0.003050109837204218
       23 MSE:
                0.0025206231512129307
Epoch
Epoch
       24 MSE:
                0.001712970668449998
Epoch
       25 MSE:
                0.001354813575744629
Epoch
       26 MSE:
                0.0011272754054516554
       27 MSE:
Epoch
                0.0016534191090613604
Epoch
       28 MSE:
                0.0019003102788701653
       29 MSE:
Epoch
                0.002000432228669524
Epoch
       30 MSE:
                0.0018033006926998496
Epoch
       31 MSE:
                0.0013373157707974315
       32 MSE:
Epoch
                0.0010966315167024732
Epoch
       33 MSE:
                0.0008370369905605912
       34 MSE:
Epoch
                0.0009382194257341325
Epoch
       35 MSE:
                0.0010494490852579474
       36 MSE:
Epoch
                0.0011276009026914835
Epoch
       37 MSE:
                0.0010753669776022434
Epoch
       38 MSE:
                0.0008606372866779566
       39 MSE:
                0.0007223477005027235
Epoch
Epoch
       40 MSE:
                0.0005585855105891824
Epoch
       41 MSE:
                0.0005760741187259555
Epoch
       42 MSE:
                0.0005773025914095342
Epoch
       43 MSE:
                0.0006344530847854912
       44 MSE:
Epoch
                0.0006374273798428476
Epoch
       45 MSE:
                0.0005923762219026685
       46 MSE:
Epoch
                0.0005467407172545791
       47 MSE:
Epoch
                0.0004556720668915659
Epoch
       48 MSE:
                0.0004280990397091955
       49 MSE:
Epoch
                0.00038855773163959384
Epoch
       50 MSE:
                0.00040942206396721303
Epoch
       51 MSE:
                0.0004132362373638898
Epoch
       52 MSE:
                0.0004298751591704786
       53 MSE:
                0.0004183154087513685
Epoch
```

Epoch 54 MSE: 0.0003963756316807121 Epoch 55 MSE: 0.00036616664147004485 56 MSE: Epoch 0.00033632389386184514 57 MSE: Epoch 0.00032095686765387654 Epoch 58 MSE: 0.00030873235664330423 Epoch 59 MSE: 0.00031281326664611697 Epoch 60 MSE: 0.00030762533424422145 Epoch 61 MSE: 0.00030846864683553576 Epoch 62 MSE: 0.0002925517037510872 Epoch 63 MSE: 0.00028148273122496903 64 MSE: Epoch 0.00025984225794672966 65 MSE: Epoch 0.00024959957227110863 Epoch 66 MSE: 0.00023657291603740305 67 MSE: Epoch 0.00023531680926680565 Epoch 68 MSE: 0.00023029305157251656 Epoch 69 MSE: 0.0002296616294188425 Epoch 70 MSE: 0.00022260675905272365 Epoch 71 MSE: 0.00021562966867350042 Epoch 72 MSE: 0.00020617901463992894 Epoch 73 MSE: 0.00019720036652870476 Epoch 74 MSE: 0.00019088812405243516 Epoch 75 MSE: 0.00018508265202399343 Epoch 76 MSE: 0.00018345934222452343 Epoch 77 MSE: 0.0001787747605703771 Epoch 78 MSE: 0.00017600099090486765 Epoch 79 MSE: 0.00016919626796152443 80 MSE: Epoch 0.00016400028835050762 Epoch 81 MSE: 0.00015760384849272668 82 MSE: Epoch 0.00015266003902070224 Epoch 83 MSE: 0.00014930088946130127 Epoch 84 MSE: 0.00014551533968187869 Epoch 85 MSE: 0.00014331407146528363 Epoch 86 MSE: 0.00013928399130236357 87 MSE: Epoch 0.0001355718559352681 88 MSE: Epoch 0.00013153019244782627 Epoch 89 MSE: 0.00012702003004960716 Epoch 90 MSE: 0.00012373088975436985 Epoch 91 MSE: 0.00012011671788059175 92 MSE: Epoch 0.00011706382792908698 Epoch 93 MSE: 0.0001142173568950966 Epoch 94 MSE: 0.00011068330059060827 95 MSE: Epoch 0.00010748096246970817 Epoch 96 MSE: 0.00010393635602667928 97 MSE: Epoch 0.00010043832298833877 Epoch 98 MSE: 9.761964611243457e-05 99 MSE: Epoch 9.477279672864825e-05 T-time: 10.383832216262817

136

Train Score: 0.29 RMSE

_____ Validation Score: 7.00 RMSE ______

Time Step = 50 | Hidden States = 16 | Num Layers = 1

Epoch 0 MSE: 0.11714629083871841 Epoch 1 MSE: 0.057736773043870926 Epoch 2 MSE: 0.030777905136346817 Epoch 3 MSE: 0.030573174357414246 Epoch 4 MSE: 0.04042964428663254 Epoch 5 MSE: 0.04061933979392052 Epoch 6 MSE: 0.03291536495089531 Epoch 7 MSE: 0.02473299950361252 Epoch 8 MSE: 0.020002957433462143 Epoch 9 MSE: 0.01911684311926365 Epoch 10 MSE: 0.02037804201245308 Epoch 11 MSE: 0.021186305209994316 Epoch 12 MSE: 0.019741756841540337 Epoch 13 MSE: 0.01609179377555847 Epoch 14 MSE: 0.01162700168788433 Epoch 15 MSE: 0.008096344769001007 Epoch 16 MSE: 0.0066353618167340755 Epoch 17 MSE: 0.006814929191023111 Epoch 18 MSE: 0.006511510815471411 Epoch 19 MSE: 0.0040574143640697 Epoch 20 MSE: 0.0008904789574444294 Epoch 21 MSE: 0.0005560461431741714 Epoch 22 MSE: 0.003562245750799775 Epoch 23 MSE: 0.004348945803940296 Epoch 24 MSE: 0.0020916066132485867 Epoch 25 MSE: 0.0013164064148440957 Epoch 26 MSE: 0.002370873000472784 Epoch 27 MSE: 0.002421070821583271 Epoch 28 MSE: 0.001158353639766574 Epoch 29 MSE: 0.0001819889002945274 Epoch 30 MSE: 0.00025067070964723825 Epoch 31 MSE: 0.0008692520204931498 Epoch 32 MSE: 0.0012598605826497078 Epoch 33 MSE: 0.001131877419538796 Epoch 34 MSE: 0.0007333914400078356 Epoch 35 MSE: 0.00046741089317947626 Epoch 36 MSE: 0.0005197841092012823 Epoch 37 MSE:

0.0007521109655499458

```
Epoch
       38 MSE:
                0.0008763636578805745
Epoch
       39 MSE:
                0.0007327336934395134
Epoch
       40 MSE:
                0.00042075649253092706
       41 MSE:
Epoch
                0.0001806303480407223
Epoch
       42 MSE:
                0.00015938268916215748
Epoch
       43 MSE:
                0.0002865457790903747
Epoch
       44 MSE:
                0.0003680272202473134
Epoch
       45 MSE:
                0.0002964991726912558
Epoch 46 MSE:
                0.0001547245483379811
Epoch
       47 MSE:
                0.00010297376866219565
       48 MSE:
                0.00018746482965070754
Epoch
       49 MSE:
Epoch
                0.0002947598113678396
Epoch
       50 MSE:
                0.00029751655529253185
Epoch
       51 MSE:
                0.00020115180814173073
Epoch
      52 MSE:
                0.00011512228229548782
Epoch 53 MSE:
                0.00011109504703199491
Epoch
       54 MSE:
                0.000153623623191379
       55 MSE:
Epoch
                0.00016531965229660273
Epoch
       56 MSE:
                0.00012282931129448116
Epoch
       57 MSE:
                7.123311661416665e-05
Epoch
       58 MSE:
                6.092475450714119e-05
Epoch
       59 MSE:
                9.208288247464225e-05
Epoch
       60 MSE:
                0.00012329797027632594
       61 MSE:
Epoch
                0.00012199141929158941
       62 MSE:
                9.578631579643115e-05
Epoch
Epoch
       63 MSE:
                7.589908636873588e-05
       64 MSE:
Epoch
                7.921109499875456e-05
Epoch
       65 MSE:
                9.284564293920994e-05
       66 MSE:
Epoch
                9.367588791064918e-05
Epoch
       67 MSE:
                7.615378126502037e-05
       68 MSE:
                5.6674809457035735e-05
Epoch
Epoch
       69 MSE:
                5.251971015240997e-05
       70 MSE:
Epoch
                6.223582022357732e-05
       71 MSE:
                6.997075252002105e-05
Epoch
Epoch
       72 MSE:
                6.598063191631809e-05
Epoch
       73 MSE:
                5.686825170414522e-05
Epoch
      74 MSE:
                5.449572563520633e-05
Epoch
      75 MSE:
                6.0202048189239576e-05
      76 MSE:
Epoch
                6.459005089709535e-05
Epoch
      77 MSE:
                6.081747778807767e-05
      78 MSE:
Epoch
                5.274186696624383e-05
       79 MSE:
Epoch
                4.859273030888289e-05
Epoch
       80 MSE:
                5.0372709665680304e-05
Epoch
       81 MSE:
                5.277956370264292e-05
Epoch
       82 MSE:
                5.125026291352697e-05
Epoch
       83 MSE:
                4.748727224068716e-05
Epoch
       84 MSE:
                4.607543451129459e-05
       85 MSE:
Epoch
                4.806206197827123e-05
```

Epoch 86 MSE: 5.00883579661604e-05 Epoch 87 MSE: 4.921566869597882e-05 Epoch 88 MSE: 4.645952139981091e-05 Epoch 89 MSE: 4.4823351345257834e-05 Epoch 90 MSE: 4.5202908950159326e-05 Epoch 91 MSE: 4.569229713524692e-05 Epoch 92 MSE: 4.4625769078265876e-05 Epoch 93 MSE: 4.280006396584213e-05 Epoch 94 MSE: 4.206367884762585e-05 Epoch 95 MSE: 4.2685296648414806e-05 Epoch 96 MSE: 4.320649532019161e-05 Epoch 97 MSE: 4.261266440153122e-05 Epoch 98 MSE: 4.155639908276498e-05 Epoch 99 MSE: 4.11409382650163e-05 T-time: 8.645240783691406

Epoch 0 MSE: 0.11857244372367859 Epoch 1 MSE: 0.09187330305576324 Epoch 2 MSE: 0.06785430759191513 Epoch 3 MSE: 0.04694848507642746 Epoch 4 MSE: 0.030105723068118095 Epoch 5 MSE: 0.02005559578537941 Epoch 6 MSE: 0.02017398364841938 Epoch 7 MSE: 0.027335796505212784 Epoch 8 MSE: 0.03049894981086254 Epoch 9 MSE: 0.026483610272407532 Epoch 10 MSE: 0.019397610798478127 Epoch 11 MSE: 0.012767206877470016 Epoch 12 MSE: 0.00885285995900631 Epoch 13 MSE: 0.0067496695555746555 Epoch 14 MSE: 0.005595796275883913 Epoch 15 MSE: 0.0044284542091190815 Epoch 16 MSE: 0.0032837484031915665 Epoch 17 MSE: 0.0020628597121685743 Epoch 18 MSE: 0.001349088503047824 Epoch 19 MSE: 0.0017258708830922842 Epoch 20 MSE: 0.0024467024486511946 Epoch 21 MSE: 0.0022413544356822968 Epoch 22 MSE: 0.001794437994249165 Epoch 23 MSE: 0.0019131364533677697 Epoch 24 MSE: 0.0023427873384207487 Epoch 25 MSE: 0.0025367895141243935

```
Epoch
       26 MSE:
                0.0023087989538908005
Epoch
       27 MSE:
                0.0018110580276697874
       28 MSE:
Epoch
                0.001343992305919528
       29 MSE:
Epoch
                0.0011131670325994492
Epoch
       30 MSE:
                0.001129120122641325
Epoch
       31 MSE:
                0.0011728514218702912
Epoch
       32 MSE:
                0.0010643890127539635
Epoch
       33 MSE:
                0.0008569419733248651
Epoch
      34 MSE:
                0.0007021728670224547
Epoch
       35 MSE:
                0.0006653633317910135
       36 MSE:
                0.0007016931776888669
Epoch
       37 MSE:
Epoch
                0.0007260696147568524
Epoch
       38 MSE:
                0.0006826590979471803
Epoch
       39 MSE:
                0.0005873364279977977
Epoch
      40 MSE:
                0.00048384899855591357
Epoch 41 MSE:
                0.00039428772288374603
Epoch
       42 MSE:
                0.000332661991706118
       43 MSE:
Epoch
                0.00028308958280831575
Epoch
       44 MSE:
                0.0002264843787997961
Epoch
       45 MSE:
                0.0001678154949331656
Epoch
       46 MSE:
                0.0001318642753176391
Epoch
       47 MSE:
                0.0001323330943705514
Epoch 48 MSE:
                0.00015265074034687132
      49 MSE:
Epoch
                0.00015745066048111767
       50 MSE:
                0.00013393801054917276
Epoch
Epoch
      51 MSE:
                0.0001048094272846356
      52 MSE:
Epoch
                9.562062768964097e-05
Epoch
       53 MSE:
                0.00010051162098534405
       54 MSE:
Epoch
                9.897124255076051e-05
Epoch 55 MSE:
                8.744072692934424e-05
Epoch 56 MSE:
                8.051204349612817e-05
Epoch
       57 MSE:
                8.630680531496182e-05
Epoch
       58 MSE:
                9.53988783294335e-05
       59 MSE:
Epoch
                9.496049460722134e-05
Epoch
       60 MSE:
                8.49020725581795e-05
Epoch
       61 MSE:
                7.576417556265369e-05
Epoch
       62 MSE:
                7.388937228824943e-05
Epoch
       63 MSE:
                7.43845957913436e-05
       64 MSE:
Epoch
                7.055962487356737e-05
Epoch
       65 MSE:
                6.449643115047365e-05
       66 MSE:
Epoch
                6.29293208476156e-05
       67 MSE:
Epoch
                6.63460887153633e-05
Epoch
       68 MSE:
                6.855476385680959e-05
Epoch
       69 MSE:
                6.595229206141084e-05
Epoch
      70 MSE:
                6.17780169704929e-05
Epoch
       71 MSE:
                6.014012251398526e-05
Epoch
       72 MSE:
                6.003858652547933e-05
       73 MSE:
                5.818668068968691e-05
Epoch
```

```
Epoch 74 MSE: 5.488047099788673e-05
Epoch 75 MSE: 5.3229767217999324e-05
Epoch 76 MSE: 5.398124267230742e-05
Epoch 77 MSE:
               5.464646892505698e-05
Epoch 78 MSE:
               5.3511870646616444e-05
Epoch 79 MSE:
               5.176444028620608e-05
Epoch 80 MSE:
               5.100094494991936e-05
Epoch 81 MSE:
               5.068739483249374e-05
Epoch 82 MSE:
               4.946560875396244e-05
Epoch 83 MSE:
               4.7637626266805455e-05
Epoch 84 MSE:
               4.661225466406904e-05
Epoch 85 MSE:
               4.657974932342768e-05
Epoch 86 MSE:
               4.6403161832131445e-05
Epoch 87 MSE:
               4.555690611596219e-05
Epoch 88 MSE:
               4.472695218282752e-05
Epoch 89 MSE: 4.436996823642403e-05
Epoch 90 MSE:
               4.394802454044111e-05
Epoch 91 MSE:
               4.3004401959478855e-05
Epoch 92 MSE:
               4.19898315158207e-05
Epoch 93 MSE:
               4.144626291235909e-05
Epoch 94 MSE:
               4.115436604479328e-05
Epoch 95 MSE:
               4.065368193550967e-05
Epoch 96 MSE: 4.0022667235461995e-05
Epoch 97 MSE:
               3.959217792726122e-05
Epoch 98 MSE:
               3.928069054381922e-05
Epoch 99 MSE:
               3.877009294228628e-05
```

T-time: 8.688666343688965

Train Score: 0.19 RMSE _____ Validation Score: 1.48 RMSE _____

Time Step = 50 | Hidden States = 16 | Num Layers = 2

Epoch 0 MSE: 0.10690668225288391 Epoch 1 MSE: 0.04187827184796333 Epoch 2 MSE: 0.06367692351341248 Epoch 3 MSE: 0.05137459933757782 Epoch 4 MSE: 0.03503628447651863 Epoch 5 MSE: 0.03422681614756584 Epoch 6 MSE: 0.038586657494306564 Epoch 7 MSE: 0.03644150123000145 Epoch 8 MSE: 0.029470885172486305 Epoch 9 MSE: 0.024804653599858284

```
Epoch
       10 MSE:
                0.02592478320002556
Epoch
       11 MSE:
                0.02601831592619419
Epoch 12 MSE:
                0.020179372280836105
       13 MSE:
Epoch
                0.014663273468613625
Epoch
       14 MSE:
                0.014546523801982403
Epoch
       15 MSE:
                0.014287414960563183
Epoch
       16 MSE:
                0.007719562854617834
Epoch 17 MSE:
                0.0035090346354991198
Epoch 18 MSE:
                0.006362343207001686
Epoch
       19 MSE:
                0.0019736564718186855
      20 MSE:
                0.006257076282054186
Epoch
      21 MSE:
Epoch
                0.005034929141402245
Epoch
      22 MSE:
                0.0036713324952870607
Epoch
      23 MSE:
                0.005150590557605028
Epoch 24 MSE:
                0.0013931413413956761
Epoch 25 MSE:
                0.0013754984829574823
Epoch
      26 MSE:
                0.0026086613070219755
      27 MSE:
Epoch
                0.001782250707037747
Epoch
      28 MSE:
                0.0011048685992136598
Epoch
      29 MSE:
                0.001850450993515551
Epoch
       30 MSE:
                0.0025720547419041395
Epoch 31 MSE:
                0.00214178953319788
Epoch 32 MSE:
                0.001372703118249774
      33 MSE:
Epoch
                0.001271974528208375
Epoch
      34 MSE:
                0.0014680117601528764
Epoch
      35 MSE:
                0.0011036132927984
      36 MSE:
Epoch
                0.000461198971606791
Epoch
       37 MSE:
                0.0004806568322237581
      38 MSE:
Epoch
                0.000922235834877938
Epoch 39 MSE:
                0.0008578207343816757
Epoch 40 MSE:
                0.0006428829510696232
Epoch
       41 MSE:
                0.0008627495262771845
Epoch
      42 MSE:
                0.000915037642698735
Epoch 43 MSE:
                0.0005451471661217511
Epoch
       44 MSE:
                0.0003677390341181308
Epoch
      45 MSE:
                0.000474937551189214
Epoch 46 MSE:
                0.0004577481304295361
Epoch 47 MSE:
                0.0003428598283790052
       48 MSE:
Epoch
                0.00039320968789979815
Epoch 49 MSE:
                0.0005253945710137486
Epoch 50 MSE:
                0.0005097324610687792
       51 MSE:
Epoch
                0.00039064878365024924
Epoch
      52 MSE:
                0.00035274270339868963
Epoch
      53 MSE:
                0.00037211895687505603
Epoch
      54 MSE:
                0.0003123291826341301
Epoch
       55 MSE:
                0.00023075990611687303
Epoch
       56 MSE:
                0.0002569821663200855
      57 MSE:
                0.00031583698000758886
Epoch
```

```
Epoch 58 MSE:
                0.0002938588731922209
Epoch 59 MSE:
                0.0002652211987879127
Epoch 60 MSE:
                0.0002891999902203679
      61 MSE:
Epoch
                0.0002791266597341746
Epoch
      62 MSE:
                0.00022141686349641532
Epoch
      63 MSE:
                0.0002044608409050852
Epoch
       64 MSE:
                0.00022412612452171743
Epoch
      65 MSE:
                0.00021729196305386722
Epoch 66 MSE:
                0.00020153986406512558
Epoch 67 MSE:
                0.0002149590727640316
      68 MSE:
                0.00022574070317205042
Epoch
Epoch
      69 MSE:
                0.00020535968360491097
Epoch 70 MSE:
                0.00018680271750781685
Epoch 71 MSE:
                0.00018862409342546016
Epoch 72 MSE:
                0.00018336597713641822
Epoch 73 MSE:
                0.00016867840895429254
Epoch 74 MSE:
                0.00017064192797988653
Epoch 75 MSE:
                0.00017987805767916143
Epoch
     76 MSE:
                0.00017383093654643744
Epoch 77 MSE:
                0.0001657972316024825
Epoch
     78 MSE:
                0.0001667094766162336
Epoch 79 MSE:
                0.0001615855871932581
Epoch 80 MSE:
                0.0001510985748609528
Epoch 81 MSE:
                0.00015000661369413137
Epoch 82 MSE:
                0.00015250450815074146
Epoch 83 MSE:
                0.0001487741101300344
Epoch 84 MSE:
                0.00014615434338338673
Epoch
      85 MSE:
                0.00014726640074513853
Epoch 86 MSE:
                0.00014376617036759853
Epoch 87 MSE:
                0.0001376244326820597
Epoch 88 MSE:
                0.0001359982998110354
Epoch
      89 MSE:
                0.00013506069080904126
Epoch
      90 MSE:
                0.0001316837006015703
Epoch 91 MSE:
                0.0001306556077906862
Epoch
       92 MSE:
                0.00013101173681207
Epoch 93 MSE:
                0.00012826919555664062
Epoch 94 MSE:
                0.0001252675283467397
Epoch 95 MSE:
                0.0001241304853465408
Epoch
      96 MSE:
                0.00012188552500447258
Epoch 97 MSE:
                0.00011932665802305564
Epoch 98 MSE:
                0.00011873988842125982
      99 MSE:
                0.0001178961611003615
```

T-time: 16.38895273208618

Train Score: 0.32 RMSE

Validation Score: 8.28 RMSE

Epoch	0 MSE:	0.050634246319532394
Epoch	1 MSE:	0.03510049730539322
Epoch	2 MSE:	0.03434639051556587
Epoch	3 MSE:	0.037003256380558014
Epoch	4 MSE:	0.031522881239652634
Epoch	5 MSE:	0.02808508649468422
Epoch	6 MSE:	0.027378741651773453
Epoch	7 MSE:	0.026729445904493332
Epoch	8 MSE:	0.024575412273406982
Epoch	9 MSE:	0.02135046198964119
Epoch	10 MSE:	0.018611229956150055
Epoch	11 MSE:	0.016867898404598236
Epoch	12 MSE:	0.014211272820830345
Epoch	13 MSE:	0.009311807341873646
Epoch	14 MSE:	0.004907217342406511
Epoch	15 MSE:	0.0029315557330846786
_		
Epoch	16 MSE:	0.0010548881255090237
Epoch	17 MSE:	0.0009564621141180396
Epoch	18 MSE:	0.003937191795557737
Epoch	19 MSE:	0.004564317408949137
Epoch	20 MSE:	0.0035959745291620493
Epoch	21 MSE:	0.0035752905532717705
Epoch	22 MSE:	0.003498719073832035
Epoch	23 MSE:	0.0024016250390559435
Epoch	24 MSE:	0.001192463911138475
Epoch	25 MSE:	0.0011402758536860347
Epoch	26 MSE:	0.0019663849379867315
Epoch	27 MSE:	0.0022208455484360456
Epoch	28 MSE:	0.0018312787869945168
Epoch	29 MSE:	0.0017164178425446153
Epoch	30 MSE:	0.0017026872374117374
Epoch	31 MSE:	0.0014208342181518674
Epoch	32 MSE:	0.0008887365111149848
Epoch	33 MSE:	0.00043702477705664933
Epoch	34 MSE:	0.00038953873445279896
Epoch	35 MSE:	0.0005990025238133967
Epoch	36 MSE:	0.0006267682765610516
Epoch	37 MSE:	0.0005118238623254001
Epoch	38 MSE:	0.0005359267233870924
-		0.0006258985376916826
Epoch	39 MSE:	
Epoch	40 MSE:	0.0005535815143957734
Epoch	41 MSE:	0.0003306053695268929
Epoch	42 MSE:	0.00025499859475530684
Epoch	43 MSE:	0.00045043762656860054
Epoch	44 MSE:	0.0004003767389804125
Epoch	45 MSE:	0.0002912092604674399

```
Epoch
       46 MSE:
                0.0003926095669157803
Epoch
       47 MSE:
                0.0004421672783792019
Epoch
       48 MSE:
                0.000296673271805048
       49 MSE:
Epoch
                0.0002091948117595166
Epoch
       50 MSE:
                0.00026756705483421683
Epoch
       51 MSE:
                0.0002356153418077156
Epoch
       52 MSE:
                0.0001537701318738982
Epoch
      53 MSE:
                0.0002055991062661633
Epoch 54 MSE:
                0.00024910588399507105
Epoch
      55 MSE:
                0.0001824411010602489
       56 MSE:
                0.00015921671001706272
Epoch
Epoch
       57 MSE:
                0.0001890282437670976
Epoch
       58 MSE:
                0.00014776863099541515
Epoch
       59 MSE:
                0.00011382700176909566
Epoch
       60 MSE:
                0.0001478573540225625
Epoch 61 MSE:
                0.0001543635007692501
Epoch
       62 MSE:
                0.0001261059514945373
       63 MSE:
                0.0001346842327620834
Epoch
Epoch
       64 MSE:
                0.00014485216524917632
Epoch
       65 MSE:
                0.0001151716205640696
Epoch
       66 MSE:
                0.0001043861557263881
Epoch
       67 MSE:
                0.00011782764340750873
Epoch
       68 MSE:
                0.00010806502541527152
       69 MSE:
Epoch
                9.945677447831258e-05
Epoch
      70 MSE:
                0.00011328623804729432
Epoch
      71 MSE:
                0.0001093865794246085
      72 MSE:
Epoch
                9.548478556098416e-05
Epoch
     73 MSE:
                9.937534923665226e-05
      74 MSE:
Epoch
                9.729409066494554e-05
Epoch 75 MSE:
                8.698321471456438e-05
Epoch 76 MSE:
                9.098863665712997e-05
Epoch
      77 MSE:
                9.435778338229284e-05
Epoch
      78 MSE:
                8.748260006541386e-05
       79 MSE:
Epoch
                8.761718345340341e-05
Epoch
       80 MSE:
                8.871342288330197e-05
Epoch
       81 MSE:
                8.168032218236476e-05
Epoch
       82 MSE:
                7.976022607181221e-05
Epoch
       83 MSE:
                8.17107647890225e-05
       84 MSE:
Epoch
                7.785221532685682e-05
Epoch
       85 MSE:
                7.672442006878555e-05
       86 MSE:
Epoch
                7.806553912814707e-05
       87 MSE:
Epoch
                7.415418804157525e-05
Epoch
       88 MSE:
                7.166530849644914e-05
Epoch
       89 MSE:
                7.167163130361587e-05
Epoch
       90 MSE:
                6.848608609288931e-05
Epoch
       91 MSE:
                6.689415749860927e-05
Epoch
       92 MSE:
                6.722666876157746e-05
       93 MSE:
Epoch
                6.48684726911597e-05
```

```
Epoch 94 MSE: 6.317563384072855e-05
Epoch 95 MSE: 6.263495743041858e-05
Epoch 96 MSE: 6.012424637447111e-05
               5.856883944943547e-05
Epoch 97 MSE:
Epoch 98 MSE:
               5.8012035879073665e-05
Epoch 99 MSE:
               5.609388608718291e-05
```

T-time: 20.35795545578003

Train Score: 0.22 RMSE Validation Score: 2.32 RMSE

Time Step = 50 | Hidden States = 32 | Num Layers = 1

Epoch 0 MSE: 0.04938553646206856 Epoch 1 MSE: 0.0403636135160923 Epoch 2 MSE: 0.03930778428912163 Epoch 3 MSE: 0.023658521473407745 Epoch 4 MSE: 0.021030224859714508 Epoch 5 MSE: 0.01939914934337139 Epoch 6 MSE: 0.008111663162708282 Epoch 7 MSE: 0.012966211885213852 Epoch 8 MSE: 0.0037918458692729473 Epoch 9 MSE: 0.005290336906909943 Epoch 10 MSE: 0.004589627962559462 Epoch 11 MSE: 0.002202775562182069 Epoch 12 MSE: 0.004661279730498791 Epoch 13 MSE: 0.00041658603004179895 Epoch 14 MSE: 0.001034254557453096 Epoch 15 MSE: 0.002530565019696951 Epoch 16 MSE: 0.001816634787246585 Epoch 17 MSE: 0.0008951216004788876 Epoch 18 MSE: 0.0011927001178264618 Epoch 19 MSE: 0.0017679434968158603 Epoch 20 MSE: 0.0013759831199422479 Epoch 21 MSE: 0.0004144229169469327 Epoch 22 MSE: 0.00016254751244559884 Epoch 23 MSE: 0.0007049534469842911 Epoch 24 MSE: 0.0008462563855573535 Epoch 25 MSE: 0.00037236191565170884 Epoch 26 MSE: 0.0003082185867242515 Epoch 27 MSE: 0.0006826466997154057 Epoch 28 MSE: 0.0006166194216348231 Epoch 29 MSE:

0.00018180927145294845

```
30 MSE:
Epoch
                5.968724872218445e-05
Epoch
      31 MSE:
                0.0002760855422820896
      32 MSE:
Epoch
                0.0003815076488535851
Epoch
      33 MSE:
                0.00025403723702766
Epoch
       34 MSE:
                0.00015225227980408818
Epoch
      35 MSE:
                0.00022134673781692982
Epoch
       36 MSE:
                0.0003040135488845408
Epoch
      37 MSE:
                0.00022939003247302026
Epoch 38 MSE:
                8.004855772014707e-05
Epoch
      39 MSE:
                4.908640403300524e-05
       40 MSE:
Epoch
                0.00013528431009035558
Epoch 41 MSE:
                0.00016712260548956692
Epoch 42 MSE:
                0.00010376678255852312
Epoch
      43 MSE:
                7.720299618085846e-05
Epoch 44 MSE:
                0.00012552404950838536
Epoch 45 MSE:
                0.0001368693046970293
Epoch 46 MSE:
                7.452776480931789e-05
      47 MSE:
Epoch
                3.322787961224094e-05
Epoch
       48 MSE:
                6.0128273617010564e-05
Epoch
      49 MSE:
                9.066300845006481e-05
Epoch
       50 MSE:
                7.589703454868868e-05
Epoch 51 MSE:
                5.278749449644238e-05
Epoch 52 MSE:
                6.157412281027064e-05
Epoch 53 MSE:
                7.72097337176092e-05
Epoch
      54 MSE:
                6.26470209681429e-05
Epoch
      55 MSE:
                3.596903115976602e-05
Epoch 56 MSE:
                3.5555436625145376e-05
Epoch
      57 MSE:
                5.2982275519752875e-05
Epoch
      58 MSE:
                5.402801252785139e-05
Epoch 59 MSE:
                4.145763523411006e-05
Epoch 60 MSE:
                4.1418483306188136e-05
Epoch
       61 MSE:
                4.988351065549068e-05
Epoch
      62 MSE:
                4.525405165622942e-05
      63 MSE:
Epoch
                3.279519296484068e-05
Epoch
       64 MSE:
                3.215969991288148e-05
Epoch
       65 MSE:
                4.017103128717281e-05
Epoch
       66 MSE:
                4.0717666706768796e-05
Epoch
       67 MSE:
                3.509640009724535e-05
Epoch
       68 MSE:
                3.498710066196509e-05
Epoch
       69 MSE:
                3.8491925806738436e-05
Epoch 70 MSE:
                3.613957596826367e-05
Epoch 71 MSE:
                3.064113843720406e-05
Epoch
      72 MSE:
                3.0867387977195904e-05
Epoch
     73 MSE:
                3.4516338928369805e-05
Epoch 74 MSE:
                3.406402174732648e-05
Epoch
      75 MSE:
                3.148836549371481e-05
Epoch
      76 MSE:
                3.2123665732797235e-05
      77 MSE:
                3.331846892251633e-05
Epoch
```

Epoch 78 MSE: 3.1286475859815255e-05 Epoch 79 MSE: 2.9314996936591342e-05 Epoch 80 MSE: 3.0459012123174034e-05 Epoch 81 MSE: 3.1653828045818955e-05 Epoch 82 MSE: 3.0632669222541153e-05 Epoch 83 MSE: 2.98832146654604e-05 Epoch 84 MSE: 3.0573413823731244e-05 Epoch 85 MSE: 3.043552533199545e-05 Epoch 86 MSE: 2.915250661317259e-05 Epoch 87 MSE: 2.8950120395165868e-05 Epoch 88 MSE: 2.975648567371536e-05 Epoch 89 MSE: 2.9673137760255486e-05 Epoch 90 MSE: 2.9030898076598532e-05 Epoch 91 MSE: 2.913546995841898e-05 Epoch 92 MSE: 2.9305665520951152e-05 Epoch 93 MSE: 2.8741233109030873e-05 Epoch 94 MSE: 2.8378395654726774e-05 Epoch 95 MSE: 2.8702192139462568e-05 Epoch 96 MSE: 2.8794183890568092e-05 Epoch 97 MSE: 2.8442898837965913e-05 Epoch 98 MSE: 2.8367161576170474e-05 Epoch 99 MSE: 2.8469907192629762e-05 T-time: 21.2182674407959

Train Score: 0.16 RMSE

Validation Score: 3.30 RMSE

Epoch 0 MSE: 0.042136915028095245 Epoch 1 MSE: 0.04138246178627014 Epoch 2 MSE: 0.032355353236198425 Epoch 3 MSE: 0.03067164495587349 Epoch 4 MSE: 0.0293932743370533 Epoch 5 MSE: 0.02489616721868515 Epoch 6 MSE: 0.02278977446258068 Epoch 7 MSE: 0.020962856709957123 Epoch 8 MSE: 0.016418462619185448 Epoch 9 MSE: 0.012891323305666447 Epoch 10 MSE: 0.01098072063177824 Epoch 11 MSE: 0.00613761693239212 Epoch 12 MSE: 0.002685515908524394 Epoch 13 MSE: 0.0012006955221295357 Epoch 14 MSE: 0.0013953566085547209 Epoch 15 MSE: 0.0046376194804906845 Epoch 16 MSE: 0.00463296240195632 Epoch 17 MSE: 0.0024147259537130594

```
Epoch
       18 MSE:
                0.000671440444210231
Epoch
       19 MSE:
                0.0005122307920828462
      20 MSE:
Epoch
                0.0009400203707627952
      21 MSE:
Epoch
                0.0016097880434244871
Epoch
       22 MSE:
                0.002156981732696295
Epoch
      23 MSE:
                0.0021582047920674086
Epoch
      24 MSE:
                0.0017256431747227907
Epoch
      25 MSE:
                0.0011345333186909556
Epoch 26 MSE:
                0.0006352355121634901
Epoch
      27 MSE:
                0.0002977454278152436
Epoch
      28 MSE:
                0.000243704067543149
      29 MSE:
Epoch
                0.0005148309865035117
Epoch
       30 MSE:
                0.0008368667913600802
Epoch
       31 MSE:
                0.0009181107743643224
Epoch
      32 MSE:
                0.0006982398335821927
Epoch 33 MSE:
                0.0004235430096741766
Epoch
       34 MSE:
                0.0002782975207082927
                0.00016929212142713368
      35 MSE:
Epoch
Epoch
       36 MSE:
                0.00023140943085309118
Epoch
       37 MSE:
                0.00038895622128620744
       38 MSE:
Epoch
                0.000443036638898775
       39 MSE:
Epoch
                0.0004130929592065513
Epoch
      40 MSE:
                0.0003704052360262722
      41 MSE:
Epoch
                0.000268552073976025
Epoch
       42 MSE:
                0.00014038705558050424
Epoch
      43 MSE:
                0.00010637506784405559
Epoch 44 MSE:
                0.00013566722918767482
Epoch
       45 MSE:
                0.00016414053970947862
      46 MSE:
Epoch
                0.00021405675215646625
Epoch 47 MSE:
                0.0002136018592864275
                0.00014674886188004166
Epoch 48 MSE:
Epoch
       49 MSE:
                0.00010160024248762056
      50 MSE:
Epoch
                7.451515557477251e-05
      51 MSE:
                6.71335292281583e-05
Epoch
Epoch
       52 MSE:
                0.00010023565118899569
Epoch
      53 MSE:
                0.0001238679833477363
Epoch
       54 MSE:
                0.00011903801350854337
Epoch
      55 MSE:
                0.00010781716264318675
Epoch
      56 MSE:
                8.053296187426895e-05
Epoch 57 MSE:
                5.312711436999962e-05
Epoch 58 MSE:
                5.4345633543562144e-05
       59 MSE:
Epoch
                6.296914943959564e-05
Epoch
       60 MSE:
                7.33805718482472e-05
Epoch
       61 MSE:
                8.20669301901944e-05
Epoch
       62 MSE:
                6.883624155307189e-05
Epoch
       63 MSE:
                5.446682189358398e-05
Epoch
       64 MSE:
                4.624928624252789e-05
       65 MSE:
                4.220332266413607e-05
Epoch
```

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Epoch 66 MSE: 5.0581209507072344e-05
Epoch 67 MSE: 5.606495324173011e-05
Epoch 68 MSE:
               5.465653885039501e-05
Epoch 69 MSE:
               5.102170689497143e-05
Epoch 70 MSE:
               4.16739349020645e-05
Epoch 71 MSE:
               3.7119687476661056e-05
Epoch 72 MSE:
               3.835559618892148e-05
Epoch 73 MSE:
               4.0190800064010546e-05
Epoch 74 MSE:
               4.374358832137659e-05
Epoch 75 MSE:
               4.1734489059308544e-05
Epoch 76 MSE:
               3.750996620510705e-05
Epoch 77 MSE:
               3.438595376792364e-05
Epoch 78 MSE:
               3.2195192034123465e-05
Epoch 79 MSE:
               3.4088981919921935e-05
Epoch 80 MSE:
               3.523441409924999e-05
Epoch 81 MSE:
               3.520174868754111e-05
Epoch 82 MSE:
               3.3797306969063357e-05
Epoch 83 MSE:
               3.0829560273559764e-05
Epoch 84 MSE:
               2.9838873160770163e-05
Epoch 85 MSE:
               2.954083538497798e-05
Epoch 86 MSE:
               3.0381155738723464e-05
Epoch 87 MSE:
               3.073598418268375e-05
Epoch 88 MSE:
               2.9617151085403748e-05
Epoch 89 MSE:
               2.8463677153922617e-05
Epoch 90 MSE:
               2.706644227146171e-05
Epoch 91 MSE:
               2.6996831365977414e-05
Epoch 92 MSE:
               2.7146741558681242e-05
Epoch 93 MSE:
               2.721221790125128e-05
Epoch 94 MSE:
               2.6788569812197238e-05
Epoch 95 MSE:
               2.573903475422412e-05
Epoch 96 MSE:
               2.5110664864769205e-05
Epoch 97 MSE:
               2.4639246475999244e-05
Epoch 98 MSE:
               2.4762128305155784e-05
Epoch 99 MSE:
               2.463878263370134e-05
```

T-time: 19.248541593551636

Train Score: 0.15 RMSE

-----Validation Score: 1.84 RMSE

Time Step = 50 | Hidden States = 32 | Num Layers = 2

Epoch 0 MSE: 0.05715813487768173 Epoch 1 MSE: 0.19102784991264343

```
Epoch 2 MSE:
               0.033844735473394394
Epoch
       3 MSE:
               0.05339650809764862
Epoch
      4 MSE:
               0.05372244492173195
      5 MSE:
Epoch
               0.03529660403728485
Epoch
       6 MSE:
               0.026738429442048073
Epoch 7 MSE:
               0.03658122941851616
Epoch
      8 MSE:
               0.03496379032731056
Epoch 9 MSE:
               0.023317405954003334
Epoch 10 MSE:
                0.019105887040495872
Epoch
       11 MSE:
                0.020971398800611496
Epoch
       12 MSE:
                0.019870638847351074
Epoch
       13 MSE:
                0.012098399922251701
Epoch
       14 MSE:
                0.004460473544895649
Epoch
       15 MSE:
                0.008861137554049492
Epoch
      16 MSE:
                0.004208647646009922
Epoch 17 MSE:
                0.004628984723240137
Epoch
       18 MSE:
                0.008663360960781574
       19 MSE:
Epoch
                0.0022024614736437798
Epoch
      20 MSE:
                0.001279544667340815
Epoch
       21 MSE:
                0.0030013525392860174
Epoch
       22 MSE:
                0.002217255998402834
Epoch
      23 MSE:
                0.001357009750790894
Epoch
      24 MSE:
                0.00190772267524153
      25 MSE:
Epoch
                0.002760215662419796
Epoch
      26 MSE:
                0.002730130683630705
Epoch
      27 MSE:
                0.0017977411625906825
       28 MSE:
Epoch
                0.0008629743242636323
Epoch
       29 MSE:
                0.0007110212463885546
       30 MSE:
Epoch
                0.0010300911962985992
Epoch
      31 MSE:
                0.0008960975101217628
      32 MSE:
Epoch
                0.0004173883644398302
Epoch
       33 MSE:
                0.0004808497033081949
Epoch
       34 MSE:
                0.0010084948735311627
      35 MSE:
Epoch
                0.0011262957705184817
Epoch
       36 MSE:
                0.0006711000460200012
Epoch
       37 MSE:
                0.00030652631539851427
Epoch
       38 MSE:
                0.00036679531331174076
Epoch
       39 MSE:
                0.0004772660613525659
       40 MSE:
Epoch
                0.0003588088438846171
Epoch
      41 MSE:
                0.0002317993639735505
      42 MSE:
Epoch
                0.00031189745641313493
       43 MSE:
Epoch
                0.00047573435585945845
Epoch
       44 MSE:
                0.0004970458685420454
Epoch
      45 MSE:
                0.0003521016624290496
Epoch
      46 MSE:
                0.00021478749113157392
Epoch
       47 MSE:
                0.00020799481717403978
Epoch
       48 MSE:
                0.0002479048853274435
       49 MSE:
                0.0002076068049063906
Epoch
```

```
50 MSE:
Epoch
                0.00013809588563162833
Epoch
       51 MSE:
                0.00016069348203018308
       52 MSE:
Epoch
                0.00024086135090328753
Epoch
       53 MSE:
                0.00025066183297894895
Epoch
       54 MSE:
                0.00017975617083720863
Epoch
       55 MSE:
                0.00013152843166608363
Epoch
       56 MSE:
                0.000144060657476075
Epoch
       57 MSE:
                0.00015148622333072126
Epoch 58 MSE:
                0.00012229193816892803
Epoch
       59 MSE:
                0.00010617181396810338
       60 MSE:
                0.00013087761180941015
Epoch
Epoch
       61 MSE:
                0.00015543207700829953
Epoch
       62 MSE:
                0.00014234526315703988
Epoch
       63 MSE:
                0.00011258694576099515
Epoch
       64 MSE:
                0.00010384424967924133
                0.00011075801739934832
Epoch
       65 MSE:
Epoch
       66 MSE:
                0.00010466326784808189
       67 MSE:
Epoch
                8.986319153336808e-05
Epoch
       68 MSE:
                9.183560177916661e-05
Epoch
       69 MSE:
                0.00010631137411110103
Epoch
       70 MSE:
                0.000107503954495769
Epoch
       71 MSE:
                9.400263661518693e-05
Epoch
      72 MSE:
                8.654740668134764e-05
      73 MSE:
Epoch
                8.906482253223658e-05
Epoch
      74 MSE:
                8.727735985303298e-05
Epoch
      75 MSE:
                7.996119529707357e-05
       76 MSE:
Epoch
                7.928680861368775e-05
Epoch
       77 MSE:
                8.530687046004459e-05
       78 MSE:
Epoch
                8.632442040834576e-05
Epoch
      79 MSE:
                8.036888903006911e-05
      80 MSE:
Epoch
                7.65033764764666e-05
Epoch
       81 MSE:
                7.714644016232342e-05
Epoch
       82 MSE:
                7.589531742269173e-05
       83 MSE:
Epoch
                7.206238660728559e-05
Epoch
       84 MSE:
                7.153757906053215e-05
Epoch
       85 MSE:
                7.407956582028419e-05
Epoch
       86 MSE:
                7.385374919977039e-05
Epoch
       87 MSE:
                7.069738785503432e-05
       88 MSE:
Epoch
                6.917108112247661e-05
       89 MSE:
Epoch
                6.924908666405827e-05
      90 MSE:
Epoch
                6.782602577004582e-05
       91 MSE:
Epoch
                6.590679549844936e-05
Epoch
       92 MSE:
                6.60521982354112e-05
Epoch
       93 MSE:
                6.679696525679901e-05
Epoch
       94 MSE:
                6.5775187977124e-05
Epoch
       95 MSE:
                6.41608057776466e-05
Epoch
       96 MSE:
                6.365749868564308e-05
       97 MSE:
Epoch
                6.32236260571517e-05
```

Epoch 98 MSE: 6.196780304890126e-05 Epoch 99 MSE: 6.11766881775111e-05

T-time: 35.99884629249573

Train Score: 0.23 RMSE

Validation Score: 6.17 RMSE

Epoch 0 MSE: 0.08047892898321152 Epoch 1 MSE: 0.03562302514910698 Epoch 2 MSE: 0.05121961608529091 Epoch 3 MSE: 0.041620392352342606 Epoch 4 MSE: 0.03336156904697418 Epoch 5 MSE: 0.031205272302031517 Epoch 6 MSE: 0.03137967362999916 Epoch 7 MSE: 0.031087026000022888 Epoch 8 MSE: 0.028986413031816483 Epoch 9 MSE: 0.02530658431351185 Epoch 10 MSE: 0.021906539797782898 Epoch 11 MSE: 0.020436305552721024 Epoch 12 MSE: 0.020154934376478195 Epoch 13 MSE: 0.014199442230165005 Epoch 14 MSE: 0.008553585968911648 Epoch 15 MSE: 0.005487404763698578 Epoch 16 MSE: 0.0029131711926311255 Epoch 17 MSE: 0.00039877466042526066 Epoch 18 MSE: 0.0050320071168243885 Epoch 19 MSE: 0.00418497808277607 Epoch 20 MSE: 0.00305158575065434 Epoch 21 MSE: 0.004048240836709738 Epoch 22 MSE: 0.003274116665124893 Epoch 23 MSE: 0.0012034106766805053 Epoch 24 MSE: 0.0003953959094360471 Epoch 25 MSE: 0.002078538527712226 Epoch 26 MSE: 0.0024147029034793377 Epoch 27 MSE: 0.0011171953519806266 Epoch 28 MSE: 0.0010551209561526775 Epoch 29 MSE: 0.0016763875028118491 Epoch 30 MSE: 0.001685582916252315 Epoch 31 MSE: 0.0009498797589913011 Epoch 32 MSE: 0.000249645410804078 Epoch 33 MSE: 0.0004046301473863423 Epoch 34 MSE: 0.000943748455028981 Epoch 35 MSE: 0.0007043899386189878 Epoch 36 MSE: 0.0002134292444679886 Epoch 37 MSE: 0.00031716644298285246

```
Epoch
       38 MSE:
                0.0006371757481247187
Epoch
       39 MSE:
                0.0005717662279494107
       40 MSE:
Epoch
                0.00021057750564068556
       41 MSE:
Epoch
                9.886403859127313e-05
Epoch
       42 MSE:
                0.0004011958371847868
Epoch
       43 MSE:
                0.0004362800973467529
Epoch
       44 MSE:
                0.00017060154641512781
Epoch
       45 MSE:
                0.00013747152115684003
Epoch 46 MSE:
                0.000313637254294008
Epoch
       47 MSE:
                0.0003149867698084563
       48 MSE:
                0.00013133428001310676
Epoch
       49 MSE:
Epoch
                8.537665416952223e-05
Epoch
       50 MSE:
                0.00022125622490420938
Epoch
       51 MSE:
                0.00022161535162013024
Epoch
      52 MSE:
                9.578822209732607e-05
Epoch 53 MSE:
                0.00010838986054295674
Epoch
       54 MSE:
                0.00018704407557379454
       55 MSE:
Epoch
                0.00015526331844739616
Epoch
       56 MSE:
                7.055028254399076e-05
Epoch
       57 MSE:
                8.946970774559304e-05
Epoch
       58 MSE:
                0.00014515500515699387
Epoch
       59 MSE:
                0.00010888940596487373
Epoch
       60 MSE:
                6.465918704634532e-05
       61 MSE:
Epoch
                9.459044667892158e-05
Epoch
       62 MSE:
                0.00011465025454526767
Epoch
       63 MSE:
                7.543915853602812e-05
       64 MSE:
Epoch
                5.509005859494209e-05
Epoch
       65 MSE:
                8.436258940491825e-05
       66 MSE:
Epoch
                8.586446347180754e-05
Epoch
       67 MSE:
                5.586202678387053e-05
Epoch
       68 MSE:
                5.92572869209107e-05
Epoch
       69 MSE:
                7.564842962892726e-05
      70 MSE:
Epoch
                6.230369035620242e-05
       71 MSE:
Epoch
                4.50704428658355e-05
Epoch
       72 MSE:
                5.596560731646605e-05
Epoch
       73 MSE:
                6.16850666119717e-05
Epoch
      74 MSE:
                4.629918475984596e-05
Epoch
      75 MSE:
                4.4542270188685507e-05
Epoch 76 MSE:
                5.342414806364104e-05
Epoch
      77 MSE:
                4.765593257616274e-05
Epoch 78 MSE:
                3.84728737117257e-05
       79 MSE:
Epoch
                4.3199805077165365e-05
Epoch
       80 MSE:
                4.61791169072967e-05
Epoch
       81 MSE:
                3.8486436096718535e-05
Epoch
       82 MSE:
                3.696620842674747e-05
Epoch
       83 MSE:
                4.124195402255282e-05
Epoch
       84 MSE:
                3.8417212635977194e-05
       85 MSE:
Epoch
                3.354704676894471e-05
```

Epoch 86 MSE: 3.58863799192477e-05 Epoch 87 MSE: 3.6870962503599e-05 Epoch 88 MSE: 3.254369585192762e-05 Epoch 89 MSE: 3.234448013245128e-05 Epoch 90 MSE: 3.415054379729554e-05 Epoch 91 MSE: 3.1600276997778565e-05 Epoch 92 MSE: 2.9754646675428376e-05 Epoch 93 MSE: 3.132691927021369e-05 Epoch 94 MSE: 3.033577922906261e-05 Epoch 95 MSE: 2.8197016945341602e-05 Epoch 96 MSE: 2.8909140382893384e-05 Epoch 97 MSE: 2.869442141673062e-05 Epoch 98 MSE: 2.678702730918303e-05 Epoch 99 MSE: 2.6934707420878112e-05 T-time: 37.408742904663086

Train Score: 0.15 RMSE

Validation Score: 1.07 RMSE

Time Step = 100 | Hidden States = 2 | Num Layers = 1

Epoch 0 MSE: 0.31130993366241455 Epoch 1 MSE: 0.27421465516090393 Epoch 2 MSE: 0.23992273211479187 Epoch 3 MSE: 0.20845869183540344 Epoch 4 MSE: 0.17979489266872406 Epoch 5 MSE: 0.15385624766349792 Epoch 6 MSE: 0.1305287629365921 Epoch 7 MSE: 0.10967273265123367 Epoch 8 MSE: 0.09113913029432297 Epoch 9 MSE: 0.07478595525026321 Epoch 10 MSE: 0.06049126759171486 Epoch 11 MSE: 0.04815917834639549 Epoch 12 MSE: 0.03771792724728584 Epoch 13 MSE: 0.029111096635460854 Epoch 14 MSE: 0.022284315899014473 Epoch 15 MSE: 0.017170190811157227 Epoch 16 MSE: 0.01367371529340744 Epoch 17 MSE: 0.011659832671284676 Epoch 18 MSE: 0.010944748297333717 Epoch 19 MSE: 0.011292870156466961 Epoch 20 MSE: 0.012421810999512672 Epoch 21 MSE: 0.014017540030181408

```
Epoch
       22 MSE:
                0.015759699046611786
Epoch
       23 MSE:
                0.01735352911055088
       24 MSE:
Epoch
                0.018561623990535736
       25 MSE:
Epoch
                0.019227318465709686
Epoch
       26 MSE:
                0.01928420178592205
Epoch
       27 MSE:
                0.018750576302409172
Epoch
       28 MSE:
                0.01771208830177784
Epoch
       29 MSE:
                0.016298076137900352
       30 MSE:
Epoch
                0.014656894840300083
Epoch
       31 MSE:
                0.012934413738548756
       32 MSE:
                0.011257749982178211
Epoch
Epoch
       33 MSE:
                0.009725207462906837
Epoch
       34 MSE:
                0.008401994593441486
Epoch
       35 MSE:
                0.007320776581764221
Epoch
       36 MSE:
                0.006485709920525551
Epoch
       37 MSE:
                0.0058784945867955685
Epoch
       38 MSE:
                0.005465253256261349
       39 MSE:
Epoch
                0.005203173030167818
Epoch
       40 MSE:
                0.0050463443621993065
Epoch
       41 MSE:
                0.004950386937707663
Epoch
       42 MSE:
                0.004875833168625832
Epoch
       43 MSE:
                0.004790322855114937
Epoch 44 MSE:
                0.004669769201427698
       45 MSE:
Epoch
                0.004498705733567476
       46 MSE:
                0.004269980825483799
Epoch
Epoch
       47 MSE:
                0.003983984235674143
       48 MSE:
Epoch
                0.0036474913358688354
Epoch
       49 MSE:
                0.0032722854521125555
       50 MSE:
Epoch
                0.0028735927771776915
Epoch
      51 MSE:
                0.0024684465024620295
      52 MSE:
Epoch
                0.0020740439649671316
Epoch
       53 MSE:
                0.0017062078695744276
Epoch
       54 MSE:
                0.001378013868816197
       55 MSE:
Epoch
                0.0010987466666847467
Epoch
       56 MSE:
                0.0008732251008041203
Epoch
       57 MSE:
                0.0007016073213890195
Epoch
       58 MSE:
                0.0005796948098577559
Epoch
       59 MSE:
                0.0004997187061235309
       60 MSE:
Epoch
                0.0004515133914537728
Epoch
       61 MSE:
                0.0004239282861817628
       62 MSE:
                0.00040627000271342695
Epoch
       63 MSE:
Epoch
                0.00038957371725700796
Epoch
       64 MSE:
                0.0003675157786346972
Epoch
       65 MSE:
                0.00033684392110444605
Epoch
       66 MSE:
                0.0002973076479975134
Epoch
       67 MSE:
                0.0002511347702238709
Epoch
       68 MSE:
                0.00020219976431690156
       69 MSE:
                0.0001550565066281706
Epoch
```

Epoch 70 MSE: 0.00011400931543903425 Epoch 71 MSE: 8.23729278636165e-05 Epoch 72 MSE: 6.201089854585007e-05 Epoch 73 MSE: 5.318405601428822e-05 Epoch 74 MSE: 5.468396557262167e-05 Epoch 75 MSE: 6.41763472231105e-05 Epoch 76 MSE: 7.867264503147453e-05 Epoch 77 MSE: 9.502915781922638e-05 Epoch 78 MSE: 0.00011039745004381984 Epoch 79 MSE: 0.0001225639571202919 Epoch 80 MSE: 0.00013014728028792888 Epoch 81 MSE: 0.00013264558219816536 Epoch 82 MSE: 0.00013035559095442295 Epoch 83 MSE: 0.00012418815458659083 Epoch 84 MSE: 0.00011542721767909825 Epoch 85 MSE: 0.00010547332203714177 Epoch 86 MSE: 9.561496699461713e-05 Epoch 87 MSE: 8.685351349413395e-05 Epoch 88 MSE: 7.980271038832143e-05 Epoch 89 MSE: 7.466681563528255e-05 Epoch 90 MSE: 7.12895198375918e-05 Epoch 91 MSE: 6.925132765900344e-05 Epoch 92 MSE: 6.799675611546263e-05 Epoch 93 MSE: 6.69612709316425e-05 Epoch 94 MSE: 6.567749369423836e-05 Epoch 95 MSE: 6.384588778018951e-05 Epoch 96 MSE: 6.136255251476541e-05 Epoch 97 MSE: 5.830674490425736e-05 Epoch 98 MSE: 5.4896179790375754e-05 Epoch 99 MSE: 5.1424893172224984e-05

T-time: 11.552145719528198

Train Score: 0.21 RMSE

-----Validation Score: 7.47 RMSE

Epoch 0 MSE: 0.38213953375816345
Epoch 1 MSE: 0.35144129395484924
Epoch 2 MSE: 0.3233320116996765
Epoch 3 MSE: 0.2976057529449463
Epoch 4 MSE: 0.27401798963546753
Epoch 5 MSE: 0.25236770510673523
Epoch 6 MSE: 0.23246948421001434
Epoch 7 MSE: 0.2141793668270111
Epoch 8 MSE: 0.19736449420452118
Epoch 9 MSE: 0.18190303444862366

```
Epoch
       10 MSE:
                0.16768811643123627
Epoch
       11 MSE:
                0.15462279319763184
                0.1426173597574234
Epoch
       12 MSE:
       13 MSE:
Epoch
                0.13158784806728363
Epoch
       14 MSE:
                0.12145599722862244
Epoch
       15 MSE:
                0.11225192248821259
Epoch
       16 MSE:
                0.10658346116542816
Epoch
       17 MSE:
                0.1016140878200531
Epoch 18 MSE:
                0.09705814719200134
Epoch
       19 MSE:
                0.09280640631914139
       20 MSE:
Epoch
                0.08880883455276489
       21 MSE:
Epoch
                0.08503402024507523
Epoch
       22 MSE:
                0.08145006746053696
Epoch
       23 MSE:
                0.07802945375442505
Epoch
      24 MSE:
                0.0747564509510994
Epoch 25 MSE:
                0.07161495089530945
Epoch
       26 MSE:
                0.06859196722507477
       27 MSE:
Epoch
                0.06567669659852982
Epoch
       28 MSE:
                0.06285455077886581
Epoch
       29 MSE:
                0.06010740250349045
Epoch
       30 MSE:
                0.057422105222940445
Epoch
      31 MSE:
                0.054782308638095856
Epoch
      32 MSE:
                0.052171409130096436
       33 MSE:
Epoch
                0.04958019033074379
Epoch
       34 MSE:
                0.04700253903865814
Epoch
       35 MSE:
                0.04443146288394928
       36 MSE:
Epoch
                0.04186450317502022
Epoch
       37 MSE:
                0.03930674120783806
       38 MSE:
Epoch
                0.0367712639272213
Epoch 39 MSE:
                0.0342831052839756
                0.031899116933345795
Epoch 40 MSE:
Epoch
       41 MSE:
                0.029677240177989006
Epoch
      42 MSE:
                0.02830512262880802
       43 MSE:
Epoch
                0.027010073885321617
Epoch
       44 MSE:
                0.025087477639317513
Epoch
       45 MSE:
                0.022673984989523888
Epoch 46 MSE:
                0.020731648430228233
Epoch
      47 MSE:
                0.019174724817276
       48 MSE:
Epoch
                0.017719663679599762
Epoch 49 MSE:
                0.016343990340828896
Epoch 50 MSE:
                0.015051232650876045
       51 MSE:
Epoch
                0.013850370422005653
Epoch
       52 MSE:
                0.012750299647450447
       53 MSE:
Epoch
                0.011763341724872589
Epoch
      54 MSE:
                0.010896708816289902
Epoch
       55 MSE:
                0.010144619271159172
Epoch
       56 MSE:
                0.00948413647711277
       57 MSE:
                0.008878529071807861
Epoch
```

```
Epoch 58 MSE:
                0.008291804231703281
Epoch 59 MSE:
                0.007706875912845135
      60 MSE:
Epoch
                0.007131569087505341
Epoch
      61 MSE:
                0.006588226184248924
Epoch
      62 MSE:
                0.006098412908613682
Epoch
      63 MSE:
                0.005670612677931786
Epoch
       64 MSE:
                0.005298968404531479
Epoch
      65 MSE:
                0.004967529326677322
Epoch 66 MSE:
                0.004657682962715626
Epoch
      67 MSE:
                0.004354986362159252
       68 MSE:
                0.004052917007356882
Epoch
Epoch
      69 MSE:
                0.003752906108275056
Epoch
      70 MSE:
                0.0034613267052918673
Epoch
     71 MSE:
                0.0031872084364295006
Epoch 72 MSE:
                0.0029362263157963753
Epoch 73 MSE:
                0.002711189677938819
Epoch 74 MSE:
                0.002507824217900634
Epoch 75 MSE:
                0.0023167601320892572
Epoch
      76 MSE:
                0.002129256958141923
Epoch 77 MSE:
                0.0019419969758018851
Epoch
      78 MSE:
                0.0017592828953638673
Epoch 79 MSE:
                0.0015875479439273477
Epoch 80 MSE:
                0.0014308353420346975
Epoch 81 MSE:
                0.0012905445182695985
      82 MSE:
Epoch
                0.0011650846572592854
Epoch
      83 MSE:
                0.0010514076566323638
Epoch 84 MSE:
                0.0009470827644690871
Epoch
      85 MSE:
                0.0008507657330483198
Epoch 86 MSE:
                0.0007627673912793398
Epoch 87 MSE:
                0.0006849058554507792
Epoch 88 MSE:
                0.0006183628574945033
Epoch
      89 MSE:
                0.0005672789411619306
      90 MSE:
Epoch
                0.0005583598976954818
      91 MSE:
Epoch
                0.0005488929455168545
Epoch
       92 MSE:
                0.0005068129394203424
Epoch
      93 MSE:
                0.0004472823056858033
Epoch 94 MSE:
                0.0003993050195276737
Epoch 95 MSE:
                0.00037672827602364123
Epoch
      96 MSE:
                0.00036208820529282093
Epoch 97 MSE:
                0.0003380415728315711
Epoch 98 MSE:
                0.0003042609023395926
      99 MSE:
                0.000268508680164814
T-time: 10.04958462715149
```

Train Score: 0.49 RMSE

Validation Score: 1.16 RMSE

Time Step = 100 | Hidden States = 2 | Num Layers = 2

Epoch 0 MSE: 0.3231036067008972 Epoch 1 MSE: 0.2798193693161011 Epoch 2 MSE: 0.24110744893550873 Epoch 3 MSE: 0.20657718181610107 Epoch 4 MSE: 0.1755928248167038 Epoch 5 MSE: 0.14752012491226196 Epoch 6 MSE: 0.12202993035316467 Epoch 7 MSE: 0.09912478178739548 Epoch 8 MSE: 0.07900048792362213 Epoch 9 MSE: 0.06192374229431152 Epoch 10 MSE: 0.0481487400829792 Epoch 11 MSE: 0.03785112872719765 Epoch 12 MSE: 0.031068820506334305 Epoch 13 MSE: 0.027649613097310066 Epoch 14 MSE: 0.027213839814066887 Epoch 15 MSE: 0.029145503416657448 Epoch 16 MSE: 0.032630011439323425 Epoch 17 MSE: 0.03675312548875809 Epoch 18 MSE: 0.040650054812431335 Epoch 19 MSE: 0.0436527356505394 Epoch 20 MSE: 0.045373208820819855 Epoch 21 MSE: 0.04570326954126358 Epoch 22 MSE: 0.044757530093193054 Epoch 23 MSE: 0.042796891182661057 Epoch 24 MSE: 0.04015588015317917 Epoch 25 MSE: 0.03718293458223343 Epoch 26 MSE: 0.0341956727206707 Epoch 27 MSE: 0.03145082667469978 Epoch 28 MSE: 0.02912789210677147 Epoch 29 MSE: 0.027325192466378212 Epoch 30 MSE: 0.026066306978464127 Epoch 31 MSE: 0.025313779711723328 Epoch 32 MSE: 0.024986738339066505 Epoch 33 MSE: 0.02497916668653488 Epoch 34 MSE: 0.025176361203193665 Epoch 35 MSE: 0.025468075647950172 Epoch 36 MSE: 0.025757931172847748 Epoch 37 MSE: 0.02596917375922203 Epoch 38 MSE: 0.026047417894005775 Epoch 39 MSE: 0.025960922241210938 Epoch 40 MSE: 0.025699123740196228 Epoch 41 MSE: 0.025269871577620506

```
Epoch
       42 MSE:
                0.02469577081501484
Epoch
       43 MSE:
                0.02400997094810009
Epoch
       44 MSE:
                0.023251712322235107
       45 MSE:
Epoch
                0.022461799904704094
Epoch
       46 MSE:
                0.021678339689970016
Epoch
       47 MSE:
                0.020932991057634354
Epoch
       48 MSE:
                0.020248031243681908
Epoch
       49 MSE:
                0.01963450200855732
      50 MSE:
Epoch
                0.01909170113503933
Epoch
       51 MSE:
                0.018608078360557556
       52 MSE:
Epoch
                0.018163517117500305
Epoch
       53 MSE:
                0.01773274876177311
Epoch
       54 MSE:
                0.017289424315094948
Epoch
       55 MSE:
                0.016810258850455284
Epoch
       56 MSE:
                0.016278641298413277
Epoch 57 MSE:
                0.015687044709920883
Epoch
       58 MSE:
                0.015037915669381618
       59 MSE:
Epoch
                0.01434286031872034
Epoch
       60 MSE:
                0.01362033374607563
Epoch
       61 MSE:
                0.012892238795757294
Epoch
       62 MSE:
                0.012180055491626263
Epoch
       63 MSE:
                0.011501159518957138
Epoch
       64 MSE:
                0.010865993797779083
       65 MSE:
Epoch
                0.01027659047394991
       66 MSE:
                0.009726730175316334
Epoch
Epoch
       67 MSE:
                0.009203776717185974
       68 MSE:
Epoch
                0.008691933006048203
Epoch
       69 MSE:
                0.008176315575838089
       70 MSE:
Epoch
                0.007647012360394001
Epoch
      71 MSE:
                0.007102194242179394
      72 MSE:
Epoch
                0.006549294572323561
Epoch
      73 MSE:
                0.006003798916935921
                0.005485672038048506
Epoch
      74 MSE:
       75 MSE:
Epoch
                0.005014200694859028
Epoch
       76 MSE:
                0.004602789878845215
Epoch
       77 MSE:
                0.004255484789609909
Epoch
      78 MSE:
                0.003966679330915213
Epoch
       79 MSE:
                0.0037244190461933613
       80 MSE:
Epoch
                0.0035161259584128857
Epoch
       81 MSE:
                0.003334234468638897
       82 MSE:
Epoch
                0.003178861690685153
       83 MSE:
Epoch
                0.0030558824073523283
Epoch
       84 MSE:
                0.002971191890537739
Epoch
       85 MSE:
                0.002924405038356781
Epoch
       86 MSE:
                0.0029060232918709517
Epoch
       87 MSE:
                0.0029003273230046034
Epoch
       88 MSE:
                0.0028924790676683187
       89 MSE:
Epoch
                0.002875141566619277
```

Epoch 90 MSE: 0.00285010295920074 Epoch 91 MSE: 0.0028240180108696222 Epoch 92 MSE: 0.002801730763167143 Epoch 93 MSE: 0.0027820635586977005 Epoch 94 MSE: 0.002758714836090803 Epoch 95 MSE: 0.002724909922108054 Epoch 96 MSE: 0.0026779905892908573 Epoch 97 MSE: 0.0026207806076854467 Epoch 98 MSE: 0.0025592967867851257 Epoch 99 MSE: 0.00249895709566772

T-time: 21.409639358520508

Train Score: 1.49 RMSE

Validation Score: 19.25 RMSE

Epoch 0 MSE: 0.2989099621772766 Epoch 1 MSE: 0.2629437744617462 Epoch 2 MSE: 0.22735147178173065 Epoch 3 MSE: 0.19234834611415863 Epoch 4 MSE: 0.15830309689044952 Epoch 5 MSE: 0.1255970001220703 Epoch 6 MSE: 0.09466824680566788 Epoch 7 MSE: 0.065078005194664 Epoch 8 MSE: 0.038183361291885376 Epoch 9 MSE: 0.017039626836776733 Epoch 10 MSE: 0.0038898405618965626 Epoch 11 MSE: 0.0014080700930207968 Epoch 12 MSE: 0.01072473544627428 Epoch 13 MSE: 0.025184214115142822 Epoch 14 MSE: 0.03407096490263939 Epoch 15 MSE: 0.034596022218465805 Epoch 16 MSE: 0.02931850589811802 Epoch 17 MSE: 0.02180331200361252 Epoch 18 MSE: 0.014627210795879364 Epoch 19 MSE: 0.009101135656237602 Epoch 20 MSE: 0.005634289234876633 Epoch 21 MSE: 0.004059221129864454 Epoch 22 MSE: 0.003945270553231239 Epoch 23 MSE: 0.0047954292967915535 Epoch 24 MSE: 0.006136258598417044 Epoch 25 MSE: 0.007569550536572933 Epoch 26 MSE: 0.008758001029491425 Epoch 27 MSE: 0.009565846063196659 Epoch 28 MSE: 0.009956233203411102 Epoch 29 MSE: 0.009939318522810936

```
Epoch
       30 MSE:
                0.009562346152961254
Epoch
       31 MSE:
                0.008899923413991928
       32 MSE:
Epoch
                0.008043266832828522
       33 MSE:
Epoch
                0.007090174127370119
Epoch
       34 MSE:
                0.0061353701166808605
       35 MSE:
Epoch
                0.005261472426354885
Epoch
       36 MSE:
                0.004531115759164095
Epoch
       37 MSE:
                0.003981894347816706
Epoch
       38 MSE:
                0.0036231211852282286
Epoch
       39 MSE:
                0.0034374480601400137
       40 MSE:
                0.0033843154087662697
Epoch
Epoch
       41 MSE:
                0.003405868075788021
Epoch
       42 MSE:
                0.003440670669078827
Epoch
       43 MSE:
                0.003446929156780243
Epoch
       44 MSE:
                0.0034053418785333633
       45 MSE:
Epoch
                0.0032485199626535177
Epoch
       46 MSE:
                0.002952347043901682
       47 MSE:
Epoch
                0.0025444156490266323
Epoch
       48 MSE:
                0.002086368855088949
Epoch
       49 MSE:
                0.001646149205043912
Epoch
       50 MSE:
                0.0012789614265784621
Epoch
       51 MSE:
                0.0010115428594872355
       52 MSE:
Epoch
                0.0008353409357368946
       53 MSE:
Epoch
                0.0007302591111510992
       54 MSE:
                0.0006723947590216994
Epoch
Epoch
       55 MSE:
                0.0006366583984345198
       56 MSE:
Epoch
                0.0006013476522639394
Epoch
       57 MSE:
                0.0005514115327969193
       58 MSE:
Epoch
                0.0004806823271792382
Epoch
       59 MSE:
                0.0003916265850421041
       60 MSE:
Epoch
                0.0002930876216851175
Epoch
       61 MSE:
                0.00019853322010021657
       62 MSE:
Epoch
                0.00012411434727255255
       63 MSE:
Epoch
                8.22544316179119e-05
Epoch
       64 MSE:
                7.768682553432882e-05
Epoch
       65 MSE:
                0.00010421320621389896
Epoch
       66 MSE:
                0.00014745525550097227
Epoch
       67 MSE:
                0.0001902407529996708
       68 MSE:
Epoch
                0.00021834119979757816
Epoch
       69 MSE:
                0.0002248344972031191
       70 MSE:
                0.00021138580632396042
Epoch
       71 MSE:
Epoch
                0.000186136006959714
Epoch
       72 MSE:
                0.00015956239076331258
Epoch
       73 MSE:
                0.00014017615467309952
Epoch
       74 MSE:
                0.00013182336988393217
Epoch
       75 MSE:
                0.00013320728612598032
       76 MSE:
Epoch
                0.00013940293865744025
       77 MSE:
                0.00014439098595175892
Epoch
```

```
Epoch 78 MSE: 0.00014346567331813276
Epoch 79 MSE: 0.00013475253945216537
Epoch 80 MSE:
               0.00011945460573770106
Epoch 81 MSE:
               0.00010100200597662479
Epoch 82 MSE:
               8.355112368008122e-05
Epoch 83 MSE:
               7.047559483908117e-05
Epoch 84 MSE:
               6.333713827189058e-05
Epoch 85 MSE:
               6.163550278870389e-05
Epoch 86 MSE: 6.332021439447999e-05
Epoch 87 MSE:
               6.577063322765753e-05
Epoch 88 MSE:
               6.683027459075674e-05
Epoch 89 MSE:
               6.54886825941503e-05
Epoch 90 MSE:
               6.201995711307973e-05
Epoch 91 MSE:
               5.760356361861341e-05
Epoch 92 MSE:
               5.3699968702858314e-05
Epoch 93 MSE: 5.1405539124971256e-05
Epoch 94 MSE: 5.108871482661925e-05
Epoch 95 MSE: 5.234957643551752e-05
Epoch 96 MSE: 5.428643271443434e-05
Epoch 97 MSE: 5.591213994193822e-05
Epoch 98 MSE:
               5.651186074828729e-05
Epoch 99 MSE: 5.5857959523564205e-05
```

T-time: 19.064570903778076

Train Score: 0.22 RMSE

Validation Score: 1.19 RMSE

Time Step = 100 | Hidden States = 4 | Num Layers = 1

Epoch 0 MSE: 0.13147138059139252 Epoch 1 MSE: 0.09974874556064606

Epoch 2 MSE: 0.07940835505723953 Epoch 3 MSE: 0.06796365231275558

Epoch 4 MSE: 0.06272579729557037 Epoch 5 MSE: 0.061060693114995956

Epoch 6 MSE: 0.060731299221515656

Epoch 7 MSE: 0.0602140799164772 Epoch 8 MSE: 0.058787066489458084

Epoch 9 MSE: 0.05636468902230263 Epoch 10 MSE: 0.05323122441768646

Epoch 11 MSE: 0.04981053248047829 Epoch 12 MSE: 0.046514611691236496

Epoch 13 MSE: 0.04365834966301918

```
Epoch
       14 MSE:
                0.041419826447963715
Epoch
       15 MSE:
                0.03983239084482193
       16 MSE:
Epoch
                0.03880184516310692
       17 MSE:
Epoch
                0.0381438210606575
Epoch
       18 MSE:
                0.037634462118148804
Epoch
       19 MSE:
                0.03706352785229683
Epoch
       20 MSE:
                0.036277540028095245
Epoch
      21 MSE:
                0.03520350903272629
Epoch
      22 MSE:
                0.033850591629743576
Epoch
       23 MSE:
                0.03229374811053276
       24 MSE:
                0.030646737664937973
Epoch
Epoch
       25 MSE:
                0.02903159148991108
Epoch
       26 MSE:
                0.027550015598535538
Epoch
       27 MSE:
                0.026260899379849434
Epoch
       28 MSE:
                0.025167999789118767
Epoch 29 MSE:
                0.02422153204679489
Epoch
       30 MSE:
                0.023335324600338936
       31 MSE:
Epoch
                0.022415611892938614
Epoch
       32 MSE:
                0.02139182947576046
Epoch
       33 MSE:
                0.020237628370523453
Epoch
       34 MSE:
                0.01897515542805195
Epoch
       35 MSE:
                0.017662981525063515
Epoch
       36 MSE:
                0.01637345924973488
       37 MSE:
Epoch
                0.01516722422093153
       38 MSE:
                0.014072366990149021
Epoch
Epoch
       39 MSE:
                0.013074779883027077
       40 MSE:
Epoch
                0.012124111875891685
Epoch
       41 MSE:
                0.011155516840517521
       42 MSE:
Epoch
                0.010119888931512833
Epoch 43 MSE:
                0.009008672088384628
Epoch 44 MSE:
                0.007859895005822182
Epoch
       45 MSE:
                0.006741470657289028
Epoch
       46 MSE:
                0.0057190642692148685
       47 MSE:
Epoch
                0.004823789000511169
Epoch
       48 MSE:
                0.00403817230835557
Epoch
       49 MSE:
                0.0033129879739135504
Epoch
       50 MSE:
                0.0026077658403664827
Epoch
      51 MSE:
                0.0019262159476056695
       52 MSE:
Epoch
                0.0013189006131142378
Epoch
      53 MSE:
                0.0008493505301885307
Epoch 54 MSE:
                0.0005456316866911948
       55 MSE:
Epoch
                0.000375046074623242
Epoch
       56 MSE:
                0.0002719303302001208
       57 MSE:
Epoch
                0.0001996740757022053
Epoch
       58 MSE:
                0.00017975049559026957
Epoch
       59 MSE:
                0.0002513598883524537
Epoch
       60 MSE:
                0.00040645175613462925
       61 MSE:
                0.0005781119107268751
Epoch
```

```
Epoch 62 MSE:
                0.0007011781563051045
Epoch 63 MSE:
                0.0007698960253037512
Epoch 64 MSE:
                0.0008206527563743293
Epoch 65 MSE:
                0.0008690363611094654
Epoch 66 MSE:
                0.0008865189156495035
Epoch 67 MSE:
                0.0008433662005700171
Epoch
      68 MSE:
                0.0007514083990827203
Epoch 69 MSE:
                0.0006495376583188772
Epoch 70 MSE:
                0.0005607811035588384
Epoch 71 MSE:
                0.0004781677562277764
Epoch 72 MSE:
                0.0003887093917001039
Epoch 73 MSE:
                0.00029740273021161556
Epoch 74 MSE:
                0.0002225721109425649
Epoch 75 MSE:
                0.00017498056695330888
Epoch 76 MSE:
                0.00014862501120660454
Epoch 77 MSE:
                0.00013100987416692078
Epoch 78 MSE:
                0.0001170800969703123
Epoch 79 MSE:
                0.00011089711188105866
Epoch 80 MSE:
                0.00011658610310405493
Epoch 81 MSE:
                0.00013117444177623838
Epoch
      82 MSE:
                0.00014677885337732732
Epoch 83 MSE:
                0.00015789673489052802
Epoch 84 MSE:
                0.00016501008940394968
Epoch 85 MSE:
                0.0001714718237053603
Epoch 86 MSE:
                0.00017834585742093623
Epoch 87 MSE:
                0.00018307770369574428
Epoch 88 MSE:
                0.0001826854277169332
Epoch 89 MSE:
                0.0001771689421730116
Epoch 90 MSE:
                0.00016931808204390109
Epoch 91 MSE:
                0.00016164779663085938
Epoch 92 MSE:
                0.00015424584853462875
Epoch 93 MSE:
                0.0001457423495594412
Epoch 94 MSE:
                0.000135783149744384
Epoch 95 MSE:
                0.00012590715778060257
Epoch 96 MSE:
                0.00011800262291217223
Epoch 97 MSE:
                0.00011245893983868882
Epoch 98 MSE:
                0.00010822879266925156
Epoch 99 MSE:
                0.00010446419764775783
```

T-time: 10.28565502166748

Train Score: 0.30 RMSE

Validation Score: 10.34 RMSE

Epoch 0 MSE: 0.11859618127346039 Epoch 1 MSE: 0.1084759458899498

```
Epoch 2 MSE:
               0.09930511564016342
Epoch
       3 MSE:
               0.09087906777858734
Epoch 4 MSE:
               0.08320387452840805
      5 MSE:
Epoch
               0.07632068544626236
Epoch
       6 MSE:
               0.07029535621404648
Epoch 7 MSE:
               0.06513529270887375
Epoch
       8 MSE:
               0.06089991703629494
Epoch 9 MSE:
               0.057629842311143875
Epoch 10 MSE:
                0.055306289345026016
Epoch
       11 MSE:
                0.05379191413521767
Epoch
       12 MSE:
                0.05283217877149582
Epoch
       13 MSE:
                0.05217231437563896
Epoch
       14 MSE:
                0.05162941664457321
Epoch
       15 MSE:
                0.05108548328280449
Epoch
      16 MSE:
                0.0504717193543911
Epoch 17 MSE:
                0.04975840449333191
Epoch
       18 MSE:
                0.04894590750336647
       19 MSE:
Epoch
                0.04805551469326019
Epoch
       20 MSE:
                0.04712037742137909
Epoch
       21 MSE:
                0.04617774114012718
Epoch
       22 MSE:
                0.0452628917992115
Epoch
       23 MSE:
                0.04440508410334587
Epoch
      24 MSE:
                0.04362529516220093
       25 MSE:
Epoch
                0.042935557663440704
Epoch
       26 MSE:
                0.042339444160461426
Epoch
       27 MSE:
                0.04183335602283478
       28 MSE:
Epoch
                0.04140825569629669
Epoch
       29 MSE:
                0.04105153679847717
       30 MSE:
Epoch
                0.04074880853295326
Epoch
       31 MSE:
                0.04048547521233559
       32 MSE:
Epoch
                0.04024796560406685
Epoch
       33 MSE:
                0.04002469405531883
Epoch
       34 MSE:
                0.03980650007724762
       35 MSE:
Epoch
                0.039586976170539856
Epoch
       36 MSE:
                0.0393623523414135
Epoch
       37 MSE:
                0.039131246507167816
Epoch
       38 MSE:
                0.038894277065992355
Epoch
       39 MSE:
                0.03865355625748634
       40 MSE:
Epoch
                0.038412123918533325
Epoch
       41 MSE:
                0.03817346692085266
      42 MSE:
Epoch
                0.037941016256809235
Epoch
       43 MSE:
                0.03771776705980301
Epoch
       44 MSE:
                0.03750596195459366
Epoch
       45 MSE:
                0.037306930869817734
Epoch
       46 MSE:
                0.0371210053563118
Epoch
       47 MSE:
                0.0369475856423378
Epoch
       48 MSE:
                0.03678525611758232
       49 MSE:
Epoch
                0.036632005125284195
```

```
Epoch 50 MSE:
                0.03648550063371658
Epoch
      51 MSE:
                0.03634331375360489
Epoch 52 MSE:
                0.036203205585479736
Epoch
      53 MSE:
                0.036063291132450104
Epoch
      54 MSE:
                0.03592216223478317
Epoch
      55 MSE:
                0.03577895835042
Epoch
       56 MSE:
                0.035633333027362823
Epoch 57 MSE:
                0.03548534959554672
Epoch 58 MSE:
                0.03533539921045303
Epoch 59 MSE:
                0.035184022039175034
       60 MSE:
Epoch
                0.03503178805112839
Epoch
      61 MSE:
                0.034879159182310104
Epoch
       62 MSE:
                0.03472642973065376
Epoch
       63 MSE:
                0.03457362949848175
Epoch
      64 MSE:
                0.03442058712244034
Epoch 65 MSE:
                0.034266866743564606
Epoch
       66 MSE:
                0.03411188721656799
       67 MSE:
Epoch
                0.0339549295604229
Epoch
       68 MSE:
                0.033795248717069626
Epoch
       69 MSE:
                0.03363209590315819
Epoch
      70 MSE:
                0.033464785665273666
Epoch 71 MSE:
                0.033292725682258606
Epoch 72 MSE:
                0.033115413039922714
Epoch 73 MSE:
                0.03293246030807495
Epoch 74 MSE:
                0.032743554562330246
Epoch
     75 MSE:
                0.03254842013120651
      76 MSE:
Epoch
                0.03234682232141495
Epoch
      77 MSE:
                0.03213850036263466
      78 MSE:
Epoch
                0.031923167407512665
Epoch 79 MSE:
                0.031700458377599716
Epoch 80 MSE:
                0.03146995231509209
Epoch
      81 MSE:
                0.031231148168444633
      82 MSE:
Epoch
                0.030983470380306244
      83 MSE:
                0.030726296827197075
Epoch
Epoch
       84 MSE:
                0.030458956956863403
Epoch
      85 MSE:
                0.030180761590600014
Epoch
      86 MSE:
                0.0298909954726696
Epoch
      87 MSE:
                0.029588960111141205
      88 MSE:
Epoch
                0.029273951426148415
Epoch
      89 MSE:
                0.02894526533782482
Epoch 90 MSE:
                0.028602194041013718
       91 MSE:
Epoch
                0.0282440222799778
Epoch
      92 MSE:
                0.027870003134012222
Epoch
      93 MSE:
                0.027479348704218864
Epoch
      94 MSE:
                0.027071243152022362
Epoch
       95 MSE:
                0.02664480172097683
Epoch
      96 MSE:
                0.026199398562312126
      97 MSE:
Epoch
                0.025738658383488655
```

Epoch 98 MSE: 0.025278866291046143 Epoch 99 MSE: 0.024813251569867134

T-time: 10.425376653671265

Train Score: 4.70 RMSE

Validation Score: 30.15 RMSE

Time Step = 100 | Hidden States = 4 | Num Layers = 2

Epoch 0 MSE: 0.1430378258228302 Epoch 1 MSE: 0.07693720608949661 Epoch 2 MSE: 0.031622499227523804 Epoch 3 MSE: 0.011049512773752213 Epoch 4 MSE: 0.013612537644803524 Epoch 5 MSE: 0.027644114568829536 Epoch 6 MSE: 0.037642866373062134 Epoch 7 MSE: 0.037966422736644745 Epoch 8 MSE: 0.030965788289904594 Epoch 9 MSE: 0.021140893921256065 Epoch 10 MSE: 0.012436799705028534 Epoch 11 MSE: 0.007185955066233873 Epoch 12 MSE: 0.005846691317856312 Epoch 13 MSE: 0.0074048410169780254 Epoch 14 MSE: 0.010168688371777534 Epoch 15 MSE: 0.01252957433462143 Epoch 16 MSE: 0.013433768413960934 Epoch 17 MSE: 0.01253867894411087 Epoch 18 MSE: 0.010139255784451962 Epoch 19 MSE: 0.006964762229472399 Epoch 20 MSE: 0.003913754131644964 Epoch 21 MSE: 0.0017700808821246028 Epoch 22 MSE: 0.0009519588784314692 Epoch 23 MSE: 0.0013749684439972043 Epoch 24 MSE: 0.0025069962721318007 Epoch 25 MSE: 0.0036178019363433123 Epoch 26 MSE: 0.004109582398086786 Epoch 27 MSE: 0.003757740370929241 Epoch 28 MSE: 0.0027525904588401318 Epoch 29 MSE: 0.0015539025189355016 Epoch 30 MSE: 0.0006525843637064099 Epoch 31 MSE: 0.0003502995823509991 Epoch 32 MSE: 0.0006458056159317493 Epoch 33 MSE: 0.0012704705586656928

```
Epoch
       34 MSE:
                0.001847126055508852
Epoch
       35 MSE:
                0.0020826528780162334
      36 MSE:
Epoch
                0.001891821506433189
      37 MSE:
Epoch
                0.0014006670098751783
Epoch
       38 MSE:
                0.0008499042596668005
Epoch
      39 MSE:
                0.00046326578012667596
Epoch
       40 MSE:
                0.0003480477025732398
Epoch 41 MSE:
                0.0004676615644712001
Epoch 42 MSE:
                0.00068622303660959
Epoch
      43 MSE:
                0.0008514178916811943
       44 MSE:
                0.0008692992851138115
Epoch
Epoch 45 MSE:
                0.0007370426901616156
Epoch 46 MSE:
                0.0005265134968794882
Epoch
      47 MSE:
                0.00033610890386626124
Epoch 48 MSE:
                0.00023948773741722107
Epoch 49 MSE:
                0.0002554926904849708
Epoch 50 MSE:
                0.00034903912455774844
      51 MSE:
                0.00045667693484574556
Epoch
Epoch
      52 MSE:
                0.0005204864428378642
Epoch
      53 MSE:
                0.0005133823142386973
Epoch
       54 MSE:
                0.0004460102063603699
Epoch 55 MSE:
                0.0003553171409294009
Epoch 56 MSE:
                0.00028287683380767703
Epoch 57 MSE:
                0.0002543629379943013
      58 MSE:
                0.0002695950970519334
Epoch
Epoch
      59 MSE:
                0.000306617293972522
       60 MSE:
Epoch
                0.00033611274557188153
Epoch
       61 MSE:
                0.0003376381646376103
      62 MSE:
Epoch
                0.0003090652171522379
Epoch 63 MSE:
                0.000265115755610168
      64 MSE:
Epoch
                0.00022713404905516654
Epoch
       65 MSE:
                0.00021069408103358
       66 MSE:
Epoch
                0.0002180135197704658
      67 MSE:
Epoch
                0.00023866433184593916
Epoch
       68 MSE:
                0.00025708790053613484
Epoch
       69 MSE:
                0.0002618463186081499
Epoch 70 MSE:
                0.000251227495027706
Epoch 71 MSE:
                0.00023256671556737274
Epoch 72 MSE:
                0.00021655850287061185
Epoch 73 MSE:
                0.00021052405645605177
Epoch 74 MSE:
                0.00021467340411618352
Epoch
     75 MSE:
                0.00022312600049190223
Epoch
      76 MSE:
                0.0002283899812027812
      77 MSE:
Epoch
                0.0002261161571368575
Epoch
      78 MSE:
                0.00021722563542425632
Epoch
       79 MSE:
                0.00020652667444664985
       80 MSE:
Epoch
                0.0001992050965782255
       81 MSE:
                0.00019765015167649835
Epoch
```

Epoch 82 MSE: 0.00020049582235515118 Epoch 83 MSE: 0.00020409433636814356 Epoch 84 MSE: 0.00020512494666036218 Epoch 85 MSE: 0.00020255429262761027 Epoch 86 MSE: 0.00019785262702498585 Epoch 87 MSE: 0.0001936209009727463 Epoch 88 MSE: 0.0001917387271532789 Epoch 89 MSE: 0.00019227426673751324 Epoch 90 MSE: 0.00019372614042367786 Epoch 91 MSE: 0.0001942384260473773 Epoch 92 MSE: 0.0001928568526636809 Epoch 93 MSE: 0.00019000806787516922 Epoch 94 MSE: 0.00018700308282859623 Epoch 95 MSE: 0.00018504104809835553 Epoch 96 MSE: 0.00018444607849232852 Epoch 97 MSE: 0.00018460462160874158 Epoch 98 MSE: 0.00018453829397913069 Epoch 99 MSE: 0.00018362636910751462

T-time: 16.862977027893066

Train Score: 0.40 RMSE

Validation Score: 10.48 RMSE

Epoch 0 MSE: 0.25452083349227905 Epoch 1 MSE: 0.20916756987571716 Epoch 2 MSE: 0.17047804594039917 Epoch 3 MSE: 0.13906444609165192 Epoch 4 MSE: 0.11229383200407028 Epoch 5 MSE: 0.08969568461179733 Epoch 6 MSE: 0.07082884758710861 Epoch 7 MSE: 0.05529358983039856 Epoch 8 MSE: 0.0426965206861496 Epoch 9 MSE: 0.032649483531713486 Epoch 10 MSE: 0.024781275540590286 Epoch 11 MSE: 0.018695948645472527 Epoch 12 MSE: 0.014015793800354004 Epoch 13 MSE: 0.010395782999694347 Epoch 14 MSE: 0.007559140212833881 Epoch 15 MSE: 0.0055657727643847466 Epoch 16 MSE: 0.0035964257549494505 Epoch 17 MSE: 0.0018728901632130146 Epoch 18 MSE: 0.0009375683148391545 Epoch 19 MSE: 0.0009218588820658624 Epoch 20 MSE: 0.0012911104131489992 21 MSE: Epoch 0.0013609880115836859

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Epoch 22 MSE:
                0.0012630043784156442
Epoch
      23 MSE:
                0.0013212631456553936
      24 MSE:
Epoch
                0.0016322213923558593
      25 MSE:
Epoch
                0.002036736812442541
Epoch
      26 MSE:
                0.002242014743387699
Epoch
      27 MSE:
                0.0021013342775404453
Epoch
      28 MSE:
                0.0016750541981309652
Epoch
      29 MSE:
                0.0011511044576764107
Epoch 30 MSE:
                0.0007241112180054188
Epoch
      31 MSE:
                0.0004883521469309926
Epoch
      32 MSE:
                0.0004285263130441308
Epoch
      33 MSE:
                0.0004285695031285286
Epoch
       34 MSE:
                0.0003493299300316721
Epoch
       35 MSE:
                0.00022226931469049305
Epoch
      36 MSE:
                0.0001659430708969012
Epoch 37 MSE:
                0.0002331295982003212
Epoch
      38 MSE:
                0.00037336276727728546
      39 MSE:
                0.000490793667268008
Epoch
Epoch
       40 MSE:
                0.0005220070597715676
Epoch
      41 MSE:
                0.0004739889409393072
Epoch
       42 MSE:
                0.00040270996396429837
Epoch
      43 MSE:
                0.0003609791456256062
Epoch 44 MSE:
                0.00036003056447952986
Epoch 45 MSE:
                0.00035864327219314873
Epoch 46 MSE:
                0.000298698345432058
Epoch
      47 MSE:
                0.00019877147860825062
Epoch 48 MSE:
                0.00012683292152360082
Epoch
       49 MSE:
                0.00011226439528400078
Epoch 50 MSE:
                0.0001238432596437633
Epoch 51 MSE:
                0.00012060988956363872
Epoch 52 MSE:
                9.504747140454128e-05
Epoch
      53 MSE:
                7.430243567796424e-05
Epoch 54 MSE:
                8.615037222625688e-05
      55 MSE:
Epoch
                0.00011851701856357977
Epoch
       56 MSE:
                0.00013198770466260612
Epoch
      57 MSE:
                0.00011459337110863999
Epoch
      58 MSE:
                9.321865218225867e-05
Epoch
      59 MSE:
                8.865517156664282e-05
Epoch
       60 MSE:
                9.019664867082611e-05
Epoch
      61 MSE:
                7.79620386310853e-05
      62 MSE:
Epoch
                5.261636761133559e-05
       63 MSE:
Epoch
                3.371151979081333e-05
Epoch
       64 MSE:
                3.254317562095821e-05
Epoch
       65 MSE:
                3.780103361350484e-05
       66 MSE:
Epoch
                3.458702121861279e-05
Epoch
       67 MSE:
                2.7493257221067324e-05
Epoch
       68 MSE:
                2.922449493780732e-05
       69 MSE:
Epoch
                3.790163464145735e-05
```

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Epoch 70 MSE: 4.168358282186091e-05
Epoch 71 MSE: 3.6940135032637045e-05
Epoch 72 MSE: 3.157382889185101e-05
Epoch 73 MSE:
               3.139945329166949e-05
Epoch 74 MSE:
               3.171915886923671e-05
Epoch 75 MSE:
               2.684970968402922e-05
Epoch 76 MSE:
               2.0315068468335085e-05
Epoch 77 MSE:
               1.814650750020519e-05
Epoch 78 MSE:
               1.9514855011948384e-05
Epoch 79 MSE:
               1.967233583854977e-05
Epoch 80 MSE:
               1.795180833141785e-05
Epoch 81 MSE:
               1.7793712686398067e-05
Epoch 82 MSE:
               2.016461075982079e-05
Epoch 83 MSE:
               2.1855295926798135e-05
Epoch 84 MSE:
               2.0960744222975336e-05
Epoch 85 MSE:
               1.9561301087378524e-05
Epoch 86 MSE:
               1.953223727468867e-05
               1.9607679860200733e-05
Epoch 87 MSE:
Epoch 88 MSE:
               1.8251765141030774e-05
Epoch 89 MSE:
               1.6525464161532e-05
Epoch 90 MSE:
               1.6133697499753907e-05
Epoch 91 MSE:
               1.6621022950857878e-05
Epoch 92 MSE: 1.655544292589184e-05
Epoch 93 MSE: 1.611725747352466e-05
               1.6388392396038398e-05
Epoch 94 MSE:
Epoch 95 MSE:
               1.7124997611972503e-05
Epoch 96 MSE: 1.7253934856853448e-05
Epoch 97 MSE:
               1.6787575077614747e-05
Epoch 98 MSE:
               1.657145912759006e-05
Epoch 99 MSE: 1.6647629308863543e-05
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T-time: 19.422314167022705

Time Step = 100 | Hidden States = 8 | Num Layers = 1

Epoch 0 MSE: 0.052758246660232544 Epoch 1 MSE: 0.03370301425457001 Epoch 2 MSE: 0.027502691373229027 Epoch 3 MSE: 0.0312129408121109 Epoch 4 MSE: 0.031028863042593002 Epoch 5 MSE: 0.02607070654630661

```
6 MSE:
               0.02098289504647255
Epoch
Epoch
       7 MSE:
               0.01816316321492195
      8 MSE:
Epoch
               0.017349887639284134
Epoch
       9 MSE:
               0.017024796456098557
Epoch
       10 MSE:
                0.01572861336171627
Epoch
       11 MSE:
                0.012917103245854378
Epoch
       12 MSE:
                0.009198262356221676
Epoch
       13 MSE:
                0.006009088363498449
Epoch 14 MSE:
                0.004698739852756262
Epoch
       15 MSE:
                0.004736165050417185
       16 MSE:
Epoch
                0.003560083918273449
       17 MSE:
Epoch
                0.001005821512080729
Epoch
       18 MSE:
                0.0005007185391150415
Epoch
       19 MSE:
                0.002890951232984662
Epoch
       20 MSE:
                0.0033850865438580513
Epoch
      21 MSE:
                0.002188516315072775
Epoch
       22 MSE:
                0.002893658820539713
       23 MSE:
Epoch
                0.0032696842681616545
Epoch
       24 MSE:
                0.0017492207698523998
Epoch
       25 MSE:
                0.0006862803711555898
Epoch
       26 MSE:
                0.0007238128455355763
       27 MSE:
Epoch
                0.000816847721580416
Epoch
       28 MSE:
                0.0005477856611832976
       29 MSE:
Epoch
                0.000298538914648816
Epoch
       30 MSE:
                0.000407306884881109
Epoch
       31 MSE:
                0.0007576416828669608
       32 MSE:
Epoch
                0.0009980618488043547
Epoch
       33 MSE:
                0.0009592025307938457
       34 MSE:
Epoch
                0.0007726755575276911
Epoch
       35 MSE:
                0.0006504410412162542
       36 MSE:
                0.0006470066728070378
Epoch
Epoch
       37 MSE:
                0.0006441306904889643
Epoch
       38 MSE:
                0.0005206864443607628
Epoch
       39 MSE:
                0.0003029796644113958
Epoch
       40 MSE:
                0.00013836374273523688
Epoch
       41 MSE:
                0.00012417386460583657
Epoch
       42 MSE:
                0.0001913132146000862
Epoch
       43 MSE:
                0.00020507239969447255
       44 MSE:
Epoch
                0.00015617924509570003
Epoch
       45 MSE:
                0.0001527784625068307
      46 MSE:
                0.00023048697039484978
Epoch
Epoch
       47 MSE:
                0.0002921074628829956
Epoch
       48 MSE:
                0.00026077224174514413
       49 MSE:
Epoch
                0.00018668088887352496
Epoch
       50 MSE:
                0.00015367315791081637
Epoch
       51 MSE:
                0.00015664829697925597
Epoch
       52 MSE:
                0.00013611768372356892
       53 MSE:
Epoch
                8.610267104813829e-05
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Epoch 54 MSE: 5.6497345212846994e-05 Epoch 55 MSE: 7.069025014061481e-05 Epoch 56 MSE: 9.773895726539195e-05 Epoch 57 MSE: 0.00010375407146057114 Epoch 58 MSE: 9.399465488968417e-05 Epoch 59 MSE: 9.347120794700459e-05 Epoch 60 MSE: 0.00010589262819848955 Epoch 61 MSE: 0.00011059387179557234 Epoch 62 MSE: 9.567154484102502e-05 Epoch 63 MSE: 7.495981844840571e-05 Epoch 64 MSE: 6.620064959861338e-05 Epoch 65 MSE: 6.700378435198218e-05 Epoch 66 MSE: 6.354784272843972e-05 Epoch 67 MSE: 5.430732198874466e-05 Epoch 68 MSE: 5.105148011352867e-05 Epoch 69 MSE: 5.815177064505406e-05 Epoch 70 MSE: 6.522845797007903e-05 Epoch 71 MSE: 6.409314664779231e-05 Epoch 72 MSE: 6.010821016388945e-05 Epoch 73 MSE: 6.0318408941384405e-05 Epoch 74 MSE: 6.148170359665528e-05 Epoch 75 MSE: 5.760142084909603e-05 Epoch 76 MSE: 5.104093725094572e-05 Epoch 77 MSE: 4.8189900553552434e-05 4.918296690448187e-05 Epoch 78 MSE: Epoch 79 MSE: 4.927756526740268e-05 Epoch 80 MSE: 4.751200685859658e-05 Epoch 81 MSE: 4.723247548099607e-05 Epoch 82 MSE: 4.928407724946737e-05 Epoch 83 MSE: 5.0528298743302e-05 Epoch 84 MSE: 4.925778557662852e-05 Epoch 85 MSE: 4.752033419208601e-05 Epoch 86 MSE: 4.709775748779066e-05 Epoch 87 MSE: 4.678349432651885e-05 Epoch 88 MSE: 4.522770905168727e-05 Epoch 89 MSE: 4.3582767830230296e-05 Epoch 90 MSE: 4.335939956945367e-05 Epoch 91 MSE: 4.386331420391798e-05 Epoch 92 MSE: 4.371700561023317e-05 Epoch 93 MSE: 4.321482265368104e-05 Epoch 94 MSE: 4.331305171945132e-05 Epoch 95 MSE: 4.363021798781119e-05 Epoch 96 MSE: 4.32275228376966e-05 Epoch 97 MSE: 4.235742744640447e-05 Epoch 98 MSE: 4.186639125691727e-05 Epoch 99 MSE: 4.168635496171191e-05 T-time: 12.743440628051758

Train Score: 0.19 RMSE

Validation Score: 6.65 RMSE

Epoch 0 MSE: 0.05109736695885658 Epoch 1 MSE: 0.040121905505657196 Epoch 2 MSE: 0.03541479632258415 Epoch 3 MSE: 0.036108292639255524 Epoch 4 MSE: 0.0365922786295414 Epoch 5 MSE: 0.034704841673374176 Epoch 6 MSE: 0.031825095415115356 Epoch 7 MSE: 0.029382888227701187 Epoch 8 MSE: 0.02786346711218357 Epoch 9 MSE: 0.02700050361454487 Epoch 10 MSE: 0.026211902499198914 Epoch 11 MSE: 0.02504120022058487 Epoch 12 MSE: 0.023334143683314323 Epoch 13 MSE: 0.02117413654923439 Epoch 14 MSE: 0.01879858784377575 Epoch 15 MSE: 0.016462940722703934 Epoch 16 MSE: 0.014535697177052498 Epoch 17 MSE: 0.01334160752594471 Epoch 18 MSE: 0.012098581530153751 Epoch 19 MSE: 0.01080717146396637 Epoch 20 MSE: 0.009496034123003483 Epoch 21 MSE: 0.00821207370609045 Epoch 22 MSE: 0.00695671234279871 Epoch 23 MSE: 0.0056976573541760445 Epoch 24 MSE: 0.004421565216034651 Epoch 25 MSE: 0.003209504997357726 0.0021774808410555124 Epoch 26 MSE: Epoch 27 MSE: 0.0013674997026100755 Epoch 28 MSE: 0.000741584983188659 Epoch 29 MSE: 0.0003823319566436112 Epoch 30 MSE: 0.00042484179721213877 Epoch 31 MSE: 0.000704567413777113 Epoch 32 MSE: 0.0011890815803781152 Epoch 33 MSE: 0.0017360675847157836 Epoch 34 MSE: 0.002020458457991481 Epoch 35 MSE: 0.00210923096165061 Epoch 36 MSE: 0.0018773205811157823 Epoch 37 MSE: 0.0015339866513386369 Epoch 38 MSE: 0.0011479214299470186 Epoch 39 MSE: 0.0007834815187379718 Epoch 40 MSE: 0.0005459145759232342 0.00038621900603175163 Epoch 41 MSE:

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Epoch
       42 MSE:
                0.0003189997805748135
Epoch
       43 MSE:
                0.0003327029407955706
       44 MSE:
Epoch
                0.00036984452162869275
       45 MSE:
Epoch
                0.00043137752800248563
Epoch
       46 MSE:
                0.0005029657040722668
Epoch
       47 MSE:
                0.0005517334211617708
Epoch
       48 MSE:
                0.0005828880821354687
Epoch
       49 MSE:
                0.0005953789805062115
Epoch 50 MSE:
                0.0005730378907173872
Epoch
      51 MSE:
                0.0005253053386695683
       52 MSE:
Epoch
                0.0004586531431414187
Epoch
      53 MSE:
                0.0003650575818028301
Epoch
      54 MSE:
                0.00025610937154851854
Epoch
       55 MSE:
                0.00015071380767039955
Epoch
      56 MSE:
                7.900640048319474e-05
Epoch 57 MSE:
                9.684777614893392e-05
Epoch
      58 MSE:
                0.00018937278946395963
       59 MSE:
                0.00022779343998990953
Epoch
Epoch
       60 MSE:
                0.00018820184050127864
Epoch
       61 MSE:
                0.00011387122503947467
Epoch
       62 MSE:
                6.0225531342439353e-05
Epoch
       63 MSE:
                5.3598607337335125e-05
Epoch
       64 MSE:
                6.739997479598969e-05
       65 MSE:
Epoch
                8.163657184923068e-05
Epoch
       66 MSE:
                9.67164451139979e-05
Epoch
       67 MSE:
                0.00010472640860825777
       68 MSE:
Epoch
                9.866491745924577e-05
Epoch
       69 MSE:
                8.850340236676857e-05
      70 MSE:
Epoch
                7.786873175064102e-05
Epoch 71 MSE:
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Epoch 72 MSE:
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Epoch 73 MSE:
                3.8755715650040656e-05
Epoch
      74 MSE:
                3.302036566310562e-05
      75 MSE:
Epoch
                3.677017230074853e-05
Epoch
      76 MSE:
                4.4277807319303975e-05
Epoch
      77 MSE:
                4.6914705308154225e-05
Epoch
      78 MSE:
                4.633888602256775e-05
Epoch
      79 MSE:
                3.6809338780585676e-05
       80 MSE:
Epoch
                2.7751722882385366e-05
Epoch
      81 MSE:
                2.3243252144311555e-05
      82 MSE:
Epoch
                2.1568630472756922e-05
Epoch
       83 MSE:
                2.5301435016444884e-05
Epoch
       84 MSE:
                2.844770460797008e-05
Epoch
       85 MSE:
                3.069187732762657e-05
Epoch
       86 MSE:
                3.164150984957814e-05
Epoch
       87 MSE:
                2.9125150831532665e-05
Epoch
       88 MSE:
                2.6715555577538908e-05
       89 MSE:
                2.3754057110636495e-05
Epoch
```

```
Epoch 90 MSE: 2.220932765339967e-05
Epoch 91 MSE: 2.311996286152862e-05
Epoch 92 MSE:
               2.4241604478447698e-05
Epoch 93 MSE:
               2.5880292014335282e-05
Epoch 94 MSE:
               2.555760511313565e-05
Epoch 95 MSE:
               2.4031020075199194e-05
Epoch 96 MSE:
               2.2392745449906215e-05
Epoch 97 MSE:
               2.087215762003325e-05
Epoch 98 MSE:
               2.0833655071328394e-05
Epoch 99 MSE:
               2.104732448060531e-05
```

T-time: 13.914803266525269

Train Score: 0.14 RMSE

-----Validation Score: 2.16 RMSE

Time Step = 100 | Hidden States = 8 | Num Layers = 2

```
Epoch 0 MSE: 0.04955081269145012
Epoch 1 MSE: 0.03634528070688248
Epoch 2 MSE: 0.04230405017733574
Epoch 3 MSE: 0.03395857289433479
Epoch 4 MSE: 0.026234731078147888
Epoch 5 MSE: 0.025297123938798904
Epoch 6 MSE: 0.025684325024485588
Epoch 7 MSE: 0.021505629643797874
Epoch 8 MSE: 0.014640149660408497
Epoch 9 MSE: 0.01035577803850174
Epoch 10 MSE: 0.010022811591625214
Epoch 11 MSE: 0.007632232271134853
Epoch 12 MSE:
               0.0021179078612476587
Epoch 13 MSE:
               0.0013066281098872423
Epoch 14 MSE:
               0.004965323023498058
Epoch 15 MSE:
               0.0035793636925518513
Epoch 16 MSE:
               0.004890638869255781
Epoch 17 MSE:
               0.005850678775459528
Epoch 18 MSE:
               0.0027305453550070524
Epoch 19 MSE:
               0.0017630283255130053
Epoch 20 MSE:
               0.0018750455928966403
Epoch 21 MSE:
               0.0010380642488598824
Epoch 22 MSE:
               0.0004938273341394961
Epoch 23 MSE:
               0.0010367565555498004
Epoch 24 MSE:
               0.0018276871414855123
Epoch 25 MSE: 0.001994062215089798
```

```
Epoch
       26 MSE:
                0.0016888407990336418
Epoch
       27 MSE:
                0.0015121519099920988
       28 MSE:
Epoch
                0.0015987835358828306
       29 MSE:
Epoch
                0.001553111826069653
Epoch
       30 MSE:
                0.001115224789828062
Epoch
       31 MSE:
                0.0005782873486168683
Epoch
       32 MSE:
                0.0003897836431860924
Epoch
       33 MSE:
                0.0005090973572805524
       34 MSE:
                0.0005227264482527971
Epoch
Epoch
       35 MSE:
                0.0003835480601992458
       36 MSE:
                0.0004452413122635335
Epoch
       37 MSE:
Epoch
                0.0007045202073641121
Epoch
       38 MSE:
                0.0007578636286780238
       39 MSE:
Epoch
                0.000562043976970017
Epoch
       40 MSE:
                0.00044319246080704033
Epoch
       41 MSE:
                0.00044489590800367296
Epoch
       42 MSE:
                0.0003587294486351311
                0.0002084727311739698
       43 MSE:
Epoch
Epoch
       44 MSE:
                0.00018107790674548596
Epoch
       45 MSE:
                0.00026896537747234106
       46 MSE:
Epoch
                0.00031688084709458053
       47 MSE:
Epoch
                0.0002924614818766713
Epoch
       48 MSE:
                0.00028794544050469995
       49 MSE:
Epoch
                0.000322183157550171
       50 MSE:
                0.0003140948247164488
Epoch
Epoch
       51 MSE:
                0.00024199605104513466
       52 MSE:
Epoch
                0.0001842779602156952
Epoch
       53 MSE:
                0.00018044172611553222
       54 MSE:
Epoch
                0.00017845991533249617
Epoch
       55 MSE:
                0.00015300371160265058
       56 MSE:
Epoch
                0.00015171768609434366
Epoch
       57 MSE:
                0.00018546033243183047
Epoch
       58 MSE:
                0.00019860183238051832
       59 MSE:
                0.00017798662884160876
Epoch
       60 MSE:
Epoch
                0.00016611797036603093
Epoch
       61 MSE:
                0.00016574868641328067
Epoch
       62 MSE:
                0.00014721071056555957
Epoch
       63 MSE:
                0.00012289003643672913
       64 MSE:
Epoch
                0.00012164708459749818
       65 MSE:
Epoch
                0.00013100673095323145
       66 MSE:
                0.00012904270261060447
Epoch
       67 MSE:
Epoch
                0.00012606206291820854
Epoch
       68 MSE:
                0.00013261561980471015
       69 MSE:
Epoch
                0.00013390764070209116
Epoch
       70 MSE:
                0.00012258582864888012
Epoch
       71 MSE:
                0.00011354466550983489
       72 MSE:
Epoch
                0.00011218975123483688
       73 MSE:
                0.00010789754014695063
Epoch
```

Epoch 74 MSE: 0.00010173345799557865 Epoch 75 MSE: 0.00010324117465643212 Epoch 76 MSE: 0.00010728617780841887 Epoch 77 MSE: 0.00010537539492361248 Epoch 78 MSE: 0.00010261990973958746 Epoch 79 MSE: 0.00010259784176014364 Epoch 80 MSE: 9.950710227712989e-05 Epoch 81 MSE: 9.400874114362523e-05 Epoch 82 MSE: 9.227946429746225e-05 Epoch 83 MSE: 9.242090891348198e-05 Epoch 84 MSE: 9.072060493053868e-05 Epoch 85 MSE: 8.999174315249547e-05 Epoch 86 MSE: 9.098466398427263e-05 Epoch 87 MSE: 8.996463293442503e-05 Epoch 88 MSE: 8.744437946006656e-05 Epoch 89 MSE: 8.623376197647303e-05 Epoch 90 MSE: 8.49937423481606e-05 Epoch 91 MSE: 8.282058843178675e-05 Epoch 92 MSE: 8.191809320123866e-05 Epoch 93 MSE: 8.202838216675445e-05 Epoch 94 MSE: 8.123437874019146e-05 Epoch 95 MSE: 8.038568194024265e-05 Epoch 96 MSE: 8.007428550627083e-05 Epoch 97 MSE: 7.897074829088524e-05 Epoch 98 MSE: 7.747475319774821e-05 Epoch 99 MSE: 7.672120409552008e-05

T-time: 26.838262796401978

Train Score: 0.26 RMSE

-----Validation Score: 9.18 RMSE

Epoch 0 MSE: 0.03814024105668068 Epoch 1 MSE: 0.03255724161863327 Epoch 2 MSE: 0.0334225632250309 Epoch 3 MSE: 0.03216390684247017 Epoch 4 MSE: 0.02972523495554924 Epoch 5 MSE: 0.02808365412056446 Epoch 6 MSE: 0.026865366846323013 Epoch 7 MSE: 0.02502509579062462 Epoch 8 MSE: 0.02226242609322071 Epoch 9 MSE: 0.01942112296819687 Epoch 10 MSE: 0.017589300870895386 Epoch 11 MSE: 0.01580456644296646 Epoch 12 MSE: 0.012759333476424217 13 MSE: Epoch 0.010367884300649166

```
Epoch
       14 MSE:
                0.008634249679744244
Epoch
       15 MSE:
                0.006265830248594284
       16 MSE:
Epoch
                0.004591174423694611
       17 MSE:
Epoch
                0.003527256892994046
Epoch
       18 MSE:
                0.0024632601998746395
Epoch
       19 MSE:
                0.0022792730014771223
Epoch
       20 MSE:
                0.0027830288745462894
Epoch
       21 MSE:
                0.0028451071120798588
Epoch
       22 MSE:
                0.0031160556245595217
Epoch
       23 MSE:
                0.0024038543924689293
       24 MSE:
                0.0017193291569128633
Epoch
       25 MSE:
Epoch
                0.0012765114661306143
Epoch
       26 MSE:
                0.0012255915207788348
Epoch
       27 MSE:
                0.0017374976305291057
Epoch
       28 MSE:
                0.0019392067333683372
Epoch
      29 MSE:
                0.0020768940448760986
Epoch
       30 MSE:
                0.0017260892782360315
       31 MSE:
                0.0013341237790882587
Epoch
Epoch
       32 MSE:
                0.0010398642625659704
Epoch
       33 MSE:
                0.0008424335974268615
Epoch
       34 MSE:
                0.0009887132328003645
Epoch
       35 MSE:
                0.0010539896320551634
Epoch
       36 MSE:
                0.001175962039269507
       37 MSE:
Epoch
                0.0010219232644885778
       38 MSE:
                0.0008733487920835614
Epoch
Epoch
       39 MSE:
                0.0006699134246446192
       40 MSE:
Epoch
                0.0005738312029279768
Epoch
       41 MSE:
                0.0005676192231476307
       42 MSE:
Epoch
                0.0005844699335284531
Epoch
      43 MSE:
                0.0006463667377829552
Epoch
      44 MSE:
                0.0006184910307638347
Epoch
       45 MSE:
                0.0006064834888093174
Epoch
       46 MSE:
                0.0005199135048314929
       47 MSE:
Epoch
                0.00046616396866738796
Epoch
       48 MSE:
                0.00041031278669834137
Epoch
       49 MSE:
                0.00039369918522424996
Epoch
       50 MSE:
                0.0004033374134451151
Epoch
       51 MSE:
                0.0004139204102102667
Epoch
       52 MSE:
                0.00042978956480510533
Epoch
       53 MSE:
                0.00041342468466609716
      54 MSE:
Epoch
                0.0003975971485488117
       55 MSE:
Epoch
                0.0003576391318347305
Epoch
       56 MSE:
                0.00033812917536124587
       57 MSE:
Epoch
                0.0003132112033199519
Epoch
       58 MSE:
                0.0003139838809147477
Epoch
       59 MSE:
                0.0003070438397116959
Epoch
       60 MSE:
                0.00031359324930235744
       61 MSE:
                0.0003030591760762036
Epoch
```

```
Epoch 62 MSE: 0.00029714309494011104
Epoch 63 MSE: 0.00027603833586908877
Epoch 64 MSE:
               0.0002634139091242105
Epoch 65 MSE:
               0.00024516595294699073
Epoch 66 MSE:
               0.00023973510542418808
Epoch 67 MSE:
               0.00023206035257317126
Epoch 68 MSE:
               0.00023215280089061707
Epoch 69 MSE:
               0.00022695255756843835
Epoch 70 MSE:
               0.0002219052257714793
Epoch 71 MSE:
               0.00021312448370736092
Epoch 72 MSE:
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Epoch 73 MSE:
               0.00019617103680502623
Epoch 74 MSE:
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Epoch 75 MSE:
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Epoch 76 MSE:
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Epoch 77 MSE:
               0.00017755807493813336
Epoch 78 MSE:
               0.0001724316825857386
Epoch 79 MSE:
               0.00016682503337506205
Epoch 80 MSE:
               0.00016062974464148283
Epoch 81 MSE:
               0.00015370383334811777
Epoch 82 MSE:
               0.00014909604215063155
Epoch 83 MSE:
               0.00014397245831787586
Epoch 84 MSE:
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Epoch 85 MSE:
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Epoch 86 MSE:
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Epoch 87 MSE:
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Epoch 88 MSE:
               0.00012395024532452226
Epoch 89 MSE:
               0.00011981411080341786
Epoch 90 MSE:
               0.00011626816558418795
Epoch 91 MSE:
               0.00011241053289268166
Epoch 92 MSE:
               0.00010926958930213004
Epoch 93 MSE:
               0.00010595876665320247
Epoch 94 MSE:
               0.00010223319986835122
Epoch 95 MSE:
               9.883377060759813e-05
Epoch 96 MSE:
               9.516964928479865e-05
Epoch 97 MSE:
               9.1548114141915e-05
Epoch 98 MSE:
               8.844841067912057e-05
Epoch 99 MSE:
               8.538104157196358e-05
T-time: 27.54952907562256
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1 01mc. 27.01002007002200

Train Score: 0.28 RMSE

-----Validation Score: 6.96 RMSE

Time Chan = 100 | Hidden Chates = 10 | Num I arrange = 1

Time Step = 100 | Hidden States = 16 | Num Layers = 1

Epoch	O MSE:	0.11758647859096527
Epoch	1 MSE:	0.05803706496953964
Epoch	2 MSE:	0.030944831669330597
Epoch	3 MSE:	0.030643410980701447
Epoch	4 MSE:	0.04052218049764633
Epoch	5 MSE:	0.04076533019542694
Epoch	6 MSE:	0.033062707632780075
Epoch	7 MSE:	0.024847136810421944
Epoch	8 MSE:	0.02007955312728882
Epoch	9 MSE:	0.01916746236383915
Epoch	10 MSE:	0.020420417189598083
Epoch	11 MSE:	0.02123548649251461
Epoch	12 MSE:	0.019798552617430687
Epoch	13 MSE:	0.016144033521413803
Epoch	14 MSE:	0.011660048738121986
Epoch	15 MSE:	0.008103952743113041
Epoch	16 MSE:	0.0066263810731470585
Epoch	17 MSE:	0.0068076918832957745
Epoch	18 MSE:	0.006512082647532225
Epoch	19 MSE:	0.00405347952619195
Epoch	20 MSE:	0.0008810206782072783
Epoch	21 MSE:	0.000566395407076925
Epoch	22 MSE:	0.003596528898924589
Epoch	23 MSE:	0.0043672011233866215
Epoch	24 MSE:	0.002095557050779462
Epoch	25 MSE:	0.001317783142440021
Epoch	26 MSE:	0.0023658499121665955
Epoch	27 MSE:	0.0024154444690793753
Epoch	28 MSE:	0.0011583995074033737
Epoch	29 MSE:	0.00018338537483941764
Epoch	30 MSE:	0.00024888821644708514
Epoch	31 MSE:	0.0008671754039824009
Epoch	32 MSE:	0.0012631546705961227
Epoch	33 MSE:	0.0011413266183808446
Epoch	34 MSE:	0.0007438190514221787
Epoch	35 MSE:	0.00047288130735978484
Epoch	36 MSE:	0.0005189362564124167
Epoch	37 MSE:	0.0007487731636501849
Epoch	38 MSE:	0.0008753315778449178
Epoch	39 MSE:	0.0007351385429501534
Epoch	40 MSE:	0.00042363404645584524
Epoch	41 MSE:	0.00018060010916087776
Epoch	42 MSE:	0.00015628359687980264
Epoch	43 MSE:	0.00028347971965558827
Epoch	44 MSE:	0.0003680596128106117
Epoch	45 MSE:	0.0002995951799675822
-		

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Epoch
       46 MSE:
                0.00015811111370567232
Epoch
       47 MSE:
                0.00010428462701383978
Epoch
       48 MSE:
                0.0001870493433671072
       49 MSE:
Epoch
                0.00029474624898284674
Epoch
       50 MSE:
                0.00029900865047238767
Epoch
       51 MSE:
                0.0002030063042184338
Epoch
       52 MSE:
                0.00011555827222764492
Epoch
       53 MSE:
                0.00010989107249770314
Epoch
       54 MSE:
                0.00015229017299134284
Epoch
       55 MSE:
                0.00016530303400941193
       56 MSE:
                0.0001240126439370215
Epoch
Epoch
       57 MSE:
                7.234953227452934e-05
Epoch
       58 MSE:
                6.113363633630797e-05
Epoch
       59 MSE:
                9.180145571008325e-05
Epoch
       60 MSE:
                0.0001235009840456769
       61 MSE:
Epoch
                0.00012298715591896325
Epoch
       62 MSE:
                9.691436571301892e-05
       63 MSE:
Epoch
                7.635901420144364e-05
Epoch
       64 MSE:
                7.894635200500488e-05
Epoch
       65 MSE:
                9.250585571862757e-05
Epoch
       66 MSE:
                9.382109419675544e-05
Epoch
       67 MSE:
                7.667767204111442e-05
Epoch
       68 MSE:
                5.7056371588259935e-05
       69 MSE:
Epoch
                5.2511422836687416e-05
       70 MSE:
                6.213389860931784e-05
Epoch
Epoch
      71 MSE:
                7.019493205007166e-05
       72 MSE:
Epoch
                6.654296157648787e-05
Epoch
      73 MSE:
                5.739309926866554e-05
      74 MSE:
Epoch
                5.470553514896892e-05
Epoch
      75 MSE:
                6.021930312272161e-05
     76 MSE:
Epoch
                6.471433880506083e-05
Epoch
      77 MSE:
                6.112811388447881e-05
Epoch
       78 MSE:
                5.30413853994105e-05
       79 MSE:
Epoch
                4.870944394497201e-05
                5.0387479859637097e-05
Epoch
       80 MSE:
Epoch
       81 MSE:
                5.289973705657758e-05
Epoch
       82 MSE:
                5.153686652192846e-05
Epoch
       83 MSE:
                4.780182644026354e-05
Epoch
       84 MSE:
                4.6280660171760246e-05
Epoch
       85 MSE:
                4.818617890123278e-05
       86 MSE:
Epoch
                5.0254162488272414e-05
Epoch
       87 MSE:
                4.946241097059101e-05
       88 MSE:
Epoch
                4.670177077059634e-05
Epoch
       89 MSE:
                4.497995905694552e-05
Epoch
       90 MSE:
                4.5304634113563225e-05
Epoch
       91 MSE:
                4.583031477523036e-05
Epoch
       92 MSE:
                4.482888107304461e-05
Epoch
       93 MSE:
                4.3010742956539616e-05
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Epoch 94 MSE: 4.222968709655106e-05 Epoch 95 MSE: 4.2828538425965235e-05 Epoch 96 MSE: 4.33793684351258e-05 Epoch 97 MSE: 4.281914152670652e-05 Epoch 98 MSE: 4.1750659875106066e-05 Epoch 99 MSE: 4.12955523643177e-05

T-time: 21.05155897140503

Train Score: 0.19 RMSE

-----Validation Score: 5.09 RMSE

Epoch 0 MSE: 0.11906330287456512 Epoch 1 MSE: 0.09229088574647903 Epoch 2 MSE: 0.06819219887256622 Epoch 3 MSE: 0.04720387980341911 Epoch 4 MSE: 0.030279239639639854 Epoch 5 MSE: 0.020152108743786812 Epoch 6 MSE: 0.020211825147271156 Epoch 7 MSE: 0.027389658614993095 Epoch 8 MSE: 0.030620332807302475 Epoch 9 MSE: 0.0266322772949934 Epoch 10 MSE: 0.019531983882188797 Epoch 11 MSE: 0.012870531529188156 Epoch 12 MSE: 0.008912532590329647 Epoch 13 MSE: 0.006780112162232399 Epoch 14 MSE: 0.005625840276479721 Epoch 15 MSE: 0.004456528462469578 Epoch 16 MSE: 0.0033140445593744516 Epoch 17 MSE: 0.0020863397512584925 Epoch 18 MSE: 0.0013528363779187202 Epoch 19 MSE: 0.00170896016061306 Epoch 20 MSE: 0.0024419911205768585 Epoch 21 MSE: 0.00225307559594512 Epoch 22 MSE: 0.0017978708492591977 Epoch 23 MSE: 0.001903480850160122 Epoch 24 MSE: 0.002334408462047577 Epoch 25 MSE: 0.0025381436571478844 Epoch 26 MSE: 0.0023182458244264126 Epoch 27 MSE: 0.0018224152736365795 Epoch 28 MSE: 0.0013512101722881198 Epoch 29 MSE: 0.001113801496103406 Epoch 30 MSE: 0.0011258339509367943 Epoch 31 MSE: 0.0011705233482643962 Epoch 32 MSE: 0.0010640276595950127 33 MSE: 0.0008563718874938786 Epoch

```
Epoch
       34 MSE:
                0.0006997244781814516
Epoch
       35 MSE:
                0.000661548285279423
       36 MSE:
Epoch
                0.0006982600316405296
Epoch
       37 MSE:
                0.0007243792060762644
Epoch
       38 MSE:
                0.0006832677754573524
Epoch
       39 MSE:
                0.0005907443119212985
Epoch
       40 MSE:
                0.00048745478852652013
Epoch
       41 MSE:
                0.00039641655166633427
Epoch 42 MSE:
                0.0003330361796543002
Epoch
       43 MSE:
                0.0002826506970450282
       44 MSE:
Epoch
                0.00022631818137597293
Epoch
      45 MSE:
                0.0001680764544289559
Epoch
      46 MSE:
                0.00013199601380620152
Epoch
       47 MSE:
                0.00013201800175011158
Epoch
      48 MSE:
                0.0001521243975730613
Epoch 49 MSE:
                0.00015721919771749526
Epoch
      50 MSE:
                0.0001346568897133693
       51 MSE:
Epoch
                0.00010601524991216138
Epoch
       52 MSE:
                9.609245898900554e-05
Epoch
       53 MSE:
                0.0001002774151857011
Epoch
       54 MSE:
                9.886072075460106e-05
Epoch
      55 MSE:
                8.778563642408699e-05
Epoch
       56 MSE:
                8.085501758614555e-05
      57 MSE:
Epoch
                8.624893962405622e-05
       58 MSE:
                9.517552825855091e-05
Epoch
Epoch
       59 MSE:
                9.507334470981732e-05
       60 MSE:
Epoch
                8.546841854695231e-05
Epoch
       61 MSE:
                7.640525291208178e-05
Epoch
       62 MSE:
                7.425591320497915e-05
Epoch 63 MSE:
                7.4594201578293e-05
       64 MSE:
Epoch
                7.089712016750127e-05
Epoch
       65 MSE:
                6.496074638562277e-05
Epoch
       66 MSE:
                6.32770752417855e-05
       67 MSE:
Epoch
                6.650955765508115e-05
Epoch
       68 MSE:
                6.875198596389964e-05
Epoch
       69 MSE:
                6.635399768128991e-05
Epoch
      70 MSE:
                6.228369602467865e-05
Epoch
      71 MSE:
                6.0570189816644415e-05
Epoch
      72 MSE:
                6.039312211214565e-05
Epoch
      73 MSE:
                5.8585799706634134e-05
Epoch 74 MSE:
                5.534162119147368e-05
Epoch
      75 MSE:
                5.3653584473067895e-05
Epoch
       76 MSE:
                5.432766192825511e-05
Epoch
      77 MSE:
                5.499847247847356e-05
Epoch
      78 MSE:
                5.3944582759868354e-05
Epoch
       79 MSE:
                5.2240102377254516e-05
Epoch
       80 MSE:
                5.144476017449051e-05
       81 MSE:
                5.1107788749504834e-05
Epoch
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Epoch 82 MSE: 4.9908761866390705e-05 Epoch 83 MSE: 4.809626625501551e-05 Epoch 84 MSE: 4.70402737846598e-05 Epoch 85 MSE: 4.697146141552366e-05 Epoch 86 MSE: 4.680078927776776e-05 Epoch 87 MSE: 4.598536906996742e-05 Epoch 88 MSE: 4.516167246038094e-05 Epoch 89 MSE: 4.479105336940847e-05 Epoch 90 MSE: 4.436971357790753e-05 Epoch 91 MSE: 4.3442356400191784e-05 Epoch 92 MSE: 4.243043076712638e-05 Epoch 93 MSE: 4.187031663605012e-05 Epoch 94 MSE: 4.156784052611329e-05 Epoch 95 MSE: 4.107357744942419e-05 Epoch 96 MSE: 4.044989327667281e-05 Epoch 97 MSE: 4.001558045274578e-05 Epoch 98 MSE: 3.9702197682345286e-05 Epoch 99 MSE: 3.92000401916448e-05

T-time: 22.38549017906189

Train Score: 0.19 RMSE

Validation Score: 1.51 RMSE

Time Step = 100 | Hidden States = 16 | Num Layers = 2

Epoch 0 MSE: 0.10739584267139435 Epoch 1 MSE: 0.04208068922162056 Epoch 2 MSE: 0.06387277692556381 Epoch 3 MSE: 0.05165105685591698 Epoch 4 MSE: 0.03522034361958504 Epoch 5 MSE: 0.03431427478790283 Epoch 6 MSE: 0.03869042545557022 Epoch 7 MSE: 0.03660016134381294 Epoch 8 MSE: 0.029627542942762375 Epoch 9 MSE: 0.02489411272108555 Epoch 10 MSE: 0.025964519008994102 Epoch 11 MSE: 0.02610187791287899 Epoch 12 MSE: 0.020274996757507324 Epoch 13 MSE: 0.014692681841552258 Epoch 14 MSE: 0.01452951692044735 Epoch 15 MSE: 0.014304916374385357 Epoch 16 MSE: 0.007731779478490353 Epoch 17 MSE: 0.003471479984000325

```
Epoch
       18 MSE:
                0.006371133029460907
Epoch
       19 MSE:
                0.001998658524826169
       20 MSE:
Epoch
                0.006304416339844465
       21 MSE:
Epoch
                0.0050708334892988205
Epoch
       22 MSE:
                0.003669625846669078
Epoch
       23 MSE:
                0.00513914879411459
Epoch
       24 MSE:
                0.0013947589322924614
Epoch
       25 MSE:
                0.0013500502100214362
       26 MSE:
Epoch
                0.002610921859741211
Epoch
       27 MSE:
                0.0018213365692645311
       28 MSE:
                0.001124784117564559
Epoch
       29 MSE:
Epoch
                0.0018457244150340557
Epoch
       30 MSE:
                0.0025812448002398014
Epoch
       31 MSE:
                0.0021656963508576155
Epoch
       32 MSE:
                0.0013791058445349336
Epoch
       33 MSE:
                0.0012569569516927004
Epoch
       34 MSE:
                0.0014595986576750875
       35 MSE:
Epoch
                0.0011122594587504864
Epoch
       36 MSE:
                0.0004669853951781988
Epoch
       37 MSE:
                0.00047635086230002344
       38 MSE:
Epoch
                0.0009272071183659136
       39 MSE:
Epoch
                0.0008733256254345179
Epoch
       40 MSE:
                0.0006480040610767901
       41 MSE:
Epoch
                0.0008587614865973592
       42 MSE:
                0.0009174438891932368
Epoch
Epoch
       43 MSE:
                0.0005489252507686615
       44 MSE:
Epoch
                0.00036374886985868216
Epoch
       45 MSE:
                0.0004721950099337846
       46 MSE:
Epoch
                0.00046349127660505474
Epoch
      47 MSE:
                0.00034883845364674926
Epoch
       48 MSE:
                0.00039380230009555817
Epoch
       49 MSE:
                0.0005263059865683317
       50 MSE:
Epoch
                0.0005141963483765721
       51 MSE:
                0.00039321600343100727
Epoch
Epoch
       52 MSE:
                0.00035065863630734384
Epoch
       53 MSE:
                0.0003707143187057227
Epoch
       54 MSE:
                0.0003144973306916654
Epoch
       55 MSE:
                0.0002324186934856698
       56 MSE:
Epoch
                0.00025681345141492784
Epoch
       57 MSE:
                0.00031757622491568327
      58 MSE:
                0.0002972086367662996
Epoch
       59 MSE:
Epoch
                0.0002662403858266771
Epoch
       60 MSE:
                0.0002886411384679377
Epoch
       61 MSE:
                0.0002799767826218158
Epoch
       62 MSE:
                0.00022245946456678212
Epoch
       63 MSE:
                0.00020417760242708027
       64 MSE:
Epoch
                0.00022448334493674338
       65 MSE:
                0.00021918343554716557
Epoch
```

Epoch 66 MSE: 0.00020294214482419193 Epoch 67 MSE: 0.00021530532103497535 Epoch 68 MSE: 0.00022652954794466496 Epoch 69 MSE: 0.0002064625732600689 Epoch 70 MSE: 0.00018700254440773278 Epoch 71 MSE: 0.0001885831297840923 Epoch 72 MSE: 0.00018418268882669508 Epoch 73 MSE: 0.00016963380039669573 Epoch 74 MSE: 0.00017110619228333235 Epoch 75 MSE: 0.00018059200374409556 Epoch 76 MSE: 0.00017482371185906231 Epoch 77 MSE: 0.00016625368152745068 Epoch 78 MSE: 0.00016690779011696577 Epoch 79 MSE: 0.00016216066433116794 Epoch 80 MSE: 0.00015167711535468698 0.0001503582752775401 Epoch 81 MSE: Epoch 82 MSE: 0.0001530971931060776 Epoch 83 MSE: 0.00014954055950511247 Epoch 84 MSE: 0.00014663553156424314 Epoch 85 MSE: 0.00014764121442567557 Epoch 86 MSE: 0.00014429558359552175 Epoch 87 MSE: 0.0001380584144499153 Epoch 88 MSE: 0.0001363119954476133 Epoch 89 MSE: 0.00013554799079429358 Epoch 90 MSE: 0.00013224122812971473 Epoch 91 MSE: 0.0001310749357799068 Epoch 92 MSE: 0.0001314461842412129 Epoch 93 MSE: 0.0001287533377762884 Epoch 94 MSE: 0.00012563132622744888 Epoch 95 MSE: 0.00012446509208530188 Epoch 96 MSE: 0.00012231766595505178 Epoch 97 MSE: 0.00011973824439337477 Epoch 98 MSE: 0.00011911108595086262 Epoch 99 MSE: 0.0001183226631837897

T-time: 33.54967999458313

Epoch 0 MSE: 0.05092690885066986 Epoch 1 MSE: 0.03528755530714989 Epoch 2 MSE: 0.034432653337717056 Epoch 3 MSE: 0.03719818592071533 Epoch 4 MSE: 0.031708378344774246 Epoch 5 MSE: 0.028204036876559258

```
6 MSE:
Epoch
               0.027473818510770798
Epoch
       7 MSE:
               0.026829559355974197
Epoch
       8 MSE:
               0.024692125618457794
       9 MSE:
Epoch
               0.02146199531853199
Epoch
       10 MSE:
                0.018693381920456886
Epoch
       11 MSE:
                0.016921963542699814
Epoch
       12 MSE:
                0.014287603087723255
Epoch
       13 MSE:
                0.009400847367942333
       14 MSE:
Epoch
                0.004926210734993219
Epoch
       15 MSE:
                0.0029466624837368727
       16 MSE:
Epoch
                0.00108068878762424
       17 MSE:
Epoch
                0.0009470731602050364
Epoch
       18 MSE:
                0.003914252854883671
Epoch
       19 MSE:
                0.004606359638273716
Epoch
       20 MSE:
                0.00364746549166739
       21 MSE:
Epoch
                0.003607851918786764
Epoch
       22 MSE:
                0.003527795197442174
       23 MSE:
Epoch
                0.002430333523079753
Epoch
       24 MSE:
                0.0012139625614508986
Epoch
       25 MSE:
                0.001152781886048615
Epoch
       26 MSE:
                0.0019913138821721077
Epoch
       27 MSE:
                0.002248132135719061
Epoch
       28 MSE:
                0.001854863134212792
       29 MSE:
Epoch
                0.0017438799841329455
       30 MSE:
                0.001742288819514215
Epoch
Epoch
       31 MSE:
                0.001456441474147141
       32 MSE:
Epoch
                0.0009113001287914813
Epoch
       33 MSE:
                0.0004532079619821161
       34 MSE:
Epoch
                0.00041006470564752817
Epoch
       35 MSE:
                0.000623503525275737
       36 MSE:
Epoch
                0.0006515819113701582
Epoch
       37 MSE:
                0.0005240674945525825
                0.0005385950207710266
Epoch
       38 MSE:
       39 MSE:
                0.0006428777705878019
Epoch
Epoch
       40 MSE:
                0.0005943435826338828
Epoch
       41 MSE:
                0.0003732202167157084
Epoch
       42 MSE:
                0.00024310224398504943
Epoch
       43 MSE:
                0.00045985489850863814
       44 MSE:
Epoch
                0.00043635809561237693
Epoch
       45 MSE:
                0.0002912674390245229
       46 MSE:
Epoch
                0.0003828643530141562
       47 MSE:
Epoch
                0.0004631921765394509
       48 MSE:
Epoch
                0.00032190955244004726
       49 MSE:
Epoch
                0.00020765083900187165
Epoch
       50 MSE:
                0.0002704405633267015
Epoch
       51 MSE:
                0.0002582975721452385
Epoch
       52 MSE:
                0.00015933020040392876
       53 MSE:
                0.00019957638869527727
Epoch
```

Epoch 54 MSE: 0.00026061004609800875 Epoch 55 MSE: 0.00019999359210487455 Epoch 56 MSE: 0.00015679090574849397 Epoch 57 MSE: 0.00019311797223053873 Epoch 58 MSE: 0.00016518596385139972 Epoch 59 MSE: 0.00011623600585153326 Epoch 60 MSE: 0.00014510915207210928 Epoch 61 MSE: 0.00016502727521583438 Epoch 62 MSE: 0.00013515687896870077 Epoch 63 MSE: 0.0001318279973929748 Epoch 64 MSE: 0.00015113841800484806 Epoch 65 MSE: 0.00011690441169776022 Epoch 66 MSE: 8.887537114787847e-05 Epoch 67 MSE: 0.00010365759953856468 Epoch 68 MSE: 0.0001177578087663278 Epoch 69 MSE: 9.73153582890518e-05 Epoch 70 MSE: 7.780202577123418e-05 Epoch 71 MSE: 9.15409837034531e-05 Epoch 72 MSE: 9.481146844336763e-05 Epoch 73 MSE: 7.510209979955107e-05 Epoch 74 MSE: 6.90729939378798e-05 Epoch 75 MSE: 7.939028000691906e-05 Epoch 76 MSE: 7.898031617514789e-05 Epoch 77 MSE: 6.993168062763289e-05 Epoch 78 MSE: 6.945968925720081e-05 Epoch 79 MSE: 7.491319411201403e-05 Epoch 80 MSE: 7.125816773623228e-05 Epoch 81 MSE: 6.106992805143818e-05 Epoch 82 MSE: 6.249854050111026e-05 Epoch 83 MSE: 6.611461867578328e-05 Epoch 84 MSE: 5.789220813312568e-05 Epoch 85 MSE: 5.2656992920674384e-05 Epoch 86 MSE: 5.443906775326468e-05 Epoch 87 MSE: 5.402250826591626e-05 Epoch 88 MSE: 4.8699726903578267e-05 Epoch 89 MSE: 4.6118471800582483e-05 Epoch 90 MSE: 4.7815115976845846e-05 Epoch 91 MSE: 4.5576391130452976e-05 Epoch 92 MSE: 4.1615716327214614e-05 Epoch 93 MSE: 4.067354529979639e-05 Epoch 94 MSE: 4.0941602492239326e-05 Epoch 95 MSE: 3.8483885873574764e-05 Epoch 96 MSE: 3.5707835195353255e-05 Epoch 97 MSE: 3.5689121432369575e-05 Epoch 98 MSE: 3.5227276384830475e-05 Epoch 99 MSE: 3.2907180866459385e-05 T-time: 40.497334003448486

Train Score: 0.17 RMSE

Validation Score: 0.85 RMSE

Time Step = 100 | Hidden States = 32 | Num Layers = 1

Epoch 0 MSE: 0.04961331561207771 Epoch 1 MSE: 0.04231122508645058 Epoch 2 MSE: 0.037849485874176025 Epoch 3 MSE: 0.025049127638339996 Epoch 4 MSE: 0.019310185685753822 Epoch 5 MSE: 0.020375283434987068 Epoch 6 MSE: 0.008212931454181671 Epoch 7 MSE: 0.011695710942149162 Epoch 8 MSE: 0.004995762370526791 Epoch 9 MSE: 0.003490310860797763 Epoch 10 MSE: 0.005875629372894764 Epoch 11 MSE: 0.001654355670325458 Epoch 12 MSE: 0.004835286643356085 Epoch 13 MSE: 0.0007491392316296697 Epoch 14 MSE: 0.0006920200539752841 Epoch 15 MSE: 0.0024085610639303923 0.0021511854138225317 Epoch 16 MSE: Epoch 17 MSE: 0.0011289742542430758 Epoch 18 MSE: 0.0010799915762618184 Epoch 19 MSE: 0.0016434910940006375 Epoch 20 MSE: 0.001534970011562109 Epoch 21 MSE: 0.0006356062949635088 Epoch 22 MSE: 0.00010212308552581817 Epoch 23 MSE: 0.0005032940534874797 Epoch 24 MSE: 0.0008823747048154473 Epoch 25 MSE: 0.0005383741809055209 Epoch 26 MSE: 0.00028884061612188816 Epoch 27 MSE: 0.0005956814275123179 Epoch 28 MSE: 0.0006837818073108792 Epoch 29 MSE: 0.0002885963476728648 Epoch 30 MSE: 4.386375439935364e-05 Epoch 31 MSE: 0.00019881351909134537 Epoch 32 MSE: 0.0003701697278302163 Epoch 33 MSE: 0.00030413747299462557 Epoch 34 MSE: 0.00017781763745006174 Epoch 35 MSE: 0.00020003480312880129 Epoch 36 MSE: 0.0002939168771263212 Epoch 37 MSE: 0.0002657690492924303

```
Epoch
       38 MSE:
                0.00011969820479862392
Epoch
       39 MSE:
                4.1886811231961474e-05
       40 MSE:
                0.0001041810101014562
Epoch
Epoch
       41 MSE:
                0.0001647861354285851
Epoch
       42 MSE:
                0.0001239691919181496
Epoch
       43 MSE:
                7.956500485306606e-05
Epoch
       44 MSE:
                0.00011460944369900972
Epoch
       45 MSE:
                0.0001443949731765315
Epoch 46 MSE:
                9.533513366477564e-05
Epoch
       47 MSE:
                3.863906749757007e-05
       48 MSE:
                4.8648067604517564e-05
Epoch
Epoch
       49 MSE:
                8.389363210881129e-05
Epoch
       50 MSE:
                8.07499818620272e-05
Epoch
       51 MSE:
                5.697529559256509e-05
Epoch 52 MSE:
                5.935883746133186e-05
Epoch 53 MSE:
                7.749412179691717e-05
Epoch
       54 MSE:
                7.045998063404113e-05
       55 MSE:
Epoch
                4.2555930122034624e-05
Epoch
       56 MSE:
                3.349563485244289e-05
Epoch
       57 MSE:
                4.831198384636082e-05
Epoch
       58 MSE:
                5.4358843044610694e-05
Epoch
       59 MSE:
                4.3752952478826046e-05
Epoch
       60 MSE:
                4.104020990780555e-05
       61 MSE:
Epoch
                5.001559839001857e-05
       62 MSE:
                4.8897858505370095e-05
Epoch
Epoch
       63 MSE:
                3.602657307055779e-05
       64 MSE:
Epoch
                3.1525436497759074e-05
Epoch
       65 MSE:
                3.831116555375047e-05
       66 MSE:
Epoch
                4.075697506777942e-05
Epoch
       67 MSE:
                3.598331022658385e-05
       68 MSE:
Epoch
                3.513898263918236e-05
Epoch
       69 MSE:
                3.903851757058874e-05
       70 MSE:
Epoch
                3.8009744457667693e-05
       71 MSE:
Epoch
                3.2165520678972825e-05
Epoch
       72 MSE:
                3.068286969210021e-05
Epoch
       73 MSE:
                3.387010656297207e-05
Epoch
      74 MSE:
                3.426377588766627e-05
Epoch
      75 MSE:
                3.194983582943678e-05
Epoch
      76 MSE:
                3.2367828680435196e-05
Epoch
      77 MSE:
                3.4001193853328004e-05
      78 MSE:
Epoch
                3.2399901101598516e-05
       79 MSE:
Epoch
                2.9899736546212807e-05
Epoch
       80 MSE:
                3.0358747608261183e-05
Epoch
       81 MSE:
                3.1623556424165145e-05
Epoch
       82 MSE:
                3.0929604690754786e-05
Epoch
       83 MSE:
                3.02038333757082e-05
Epoch
       84 MSE:
                3.0952334782341495e-05
       85 MSE:
                3.1066942028701305e-05
Epoch
```

Epoch 86 MSE: 2.9759516110061668e-05 Epoch 87 MSE: 2.919752660091035e-05 Epoch 88 MSE: 2.983736339956522e-05 Epoch 89 MSE: 2.988868254760746e-05 Epoch 90 MSE: 2.9333690690691583e-05 Epoch 91 MSE: 2.9457003620336764e-05 Epoch 92 MSE: 2.973604205180891e-05 Epoch 93 MSE: 2.9213966627139598e-05 Epoch 94 MSE: 2.870261414500419e-05 Epoch 95 MSE: 2.889749885071069e-05 Epoch 96 MSE: 2.901703555835411e-05 Epoch 97 MSE: 2.8724474759656005e-05 Epoch 98 MSE: 2.8673017368419096e-05 Epoch 99 MSE: 2.882234548451379e-05

T-time: 40.045154333114624

Train Score: 0.16 RMSE

Validation Score: 3.41 RMSE

Epoch 0 MSE: 0.04235329478979111 Epoch 1 MSE: 0.04148237779736519 Epoch 2 MSE: 0.03250628709793091 Epoch 3 MSE: 0.030720818787813187 Epoch 4 MSE: 0.029450614005327225 Epoch 5 MSE: 0.024962497875094414 Epoch 6 MSE: 0.02283196523785591 Epoch 7 MSE: 0.020952962338924408 Epoch 8 MSE: 0.016370777040719986 Epoch 9 MSE: 0.012849899008870125 Epoch 10 MSE: 0.010859186761081219 Epoch 11 MSE: 0.005938454996794462 Epoch 12 MSE: 0.0026727858930826187 Epoch 13 MSE: 0.00110047054477036 Epoch 14 MSE: 0.0015469426289200783 Epoch 15 MSE: 0.0046912748366594315 Epoch 16 MSE: 0.004475160501897335 Epoch 17 MSE: 0.0022244618739932775 Epoch 18 MSE: 0.0006728872540406883 Epoch 19 MSE: 0.0006319080712273717 Epoch 20 MSE: 0.0010196040384471416 Epoch 21 MSE: 0.0016441503539681435 Epoch 22 MSE: 0.00217806245200336 Epoch 23 MSE: 0.0020650706719607115 Epoch 24 MSE: 0.001573525951243937 25 MSE: 0.0011379310162737966 Epoch

```
Epoch
       26 MSE:
                0.0006503112963400781
Epoch
       27 MSE:
                0.00028572860173881054
       28 MSE:
Epoch
                0.000289676187094301
       29 MSE:
Epoch
                0.000575780461076647
Epoch
       30 MSE:
                0.0008643281762488186
Epoch
       31 MSE:
                0.0009268794674426317
Epoch
       32 MSE:
                0.0007625491707585752
Epoch
       33 MSE:
                0.0005003939149901271
Epoch
       34 MSE:
                0.000278905441518873
Epoch
       35 MSE:
                0.0001862833451014012
       36 MSE:
                0.00022924055519979447
Epoch
Epoch
       37 MSE:
                0.00033642910420894623
Epoch
       38 MSE:
                0.00042448058957234025
Epoch
       39 MSE:
                0.0004511683073360473
Epoch
       40 MSE:
                0.0003973634447902441
     41 MSE:
Epoch
                0.0002859567175619304
Epoch
       42 MSE:
                0.00017272168770432472
                0.00010270663187839091
       43 MSE:
Epoch
Epoch
       44 MSE:
                0.00010180022945860401
Epoch
       45 MSE:
                0.00015261762018781155
Epoch
       46 MSE:
                0.0001995404454646632
Epoch
       47 MSE:
                0.00020378397312015295
       48 MSE:
Epoch
                0.0001624852156965062
       49 MSE:
Epoch
                9.970458631869406e-05
       50 MSE:
                6.210972060216591e-05
Epoch
Epoch
       51 MSE:
                6.275101623032242e-05
       52 MSE:
Epoch
                8.620174776297063e-05
Epoch
       53 MSE:
                0.00011352657020324841
       54 MSE:
Epoch
                0.00012120523024350405
Epoch 55 MSE:
                0.00010342764289816841
Epoch 56 MSE:
                7.561131496913731e-05
Epoch
       57 MSE:
                5.216117642703466e-05
                4.580480890581384e-05
Epoch
       58 MSE:
       59 MSE:
Epoch
                5.797909398097545e-05
Epoch
       60 MSE:
                7.215637742774561e-05
Epoch
       61 MSE:
                7.629176980117336e-05
Epoch
       62 MSE:
                6.642293010372669e-05
Epoch
       63 MSE:
                4.9399321142118424e-05
Epoch
       64 MSE:
                3.914160333806649e-05
Epoch
       65 MSE:
                3.883461977238767e-05
       66 MSE:
Epoch
                4.552555765258148e-05
Epoch
       67 MSE:
                5.1713388529606164e-05
       68 MSE:
Epoch
                5.057349699200131e-05
Epoch
       69 MSE:
                4.373801493784413e-05
Epoch
      70 MSE:
                3.5309734812472016e-05
Epoch
       71 MSE:
                3.078398367506452e-05
Epoch
       72 MSE:
                3.227499109925702e-05
       73 MSE:
                3.5828208638122305e-05
Epoch
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Epoch 74 MSE: 3.7698406231356785e-05
Epoch 75 MSE: 3.511830072966404e-05
Epoch 76 MSE:
               3.021473457920365e-05
Epoch 77 MSE:
               2.6689272999647073e-05
Epoch 78 MSE:
               2.6110588805750012e-05
Epoch 79 MSE:
               2.799241519824136e-05
Epoch 80 MSE:
               2.9258158974698745e-05
Epoch 81 MSE:
               2.8568612833623774e-05
Epoch 82 MSE:
               2.6086921934620477e-05
Epoch 83 MSE:
               2.3641759980819188e-05
Epoch 84 MSE:
               2.290473821631167e-05
Epoch 85 MSE:
               2.3578233594889753e-05
Epoch 86 MSE:
               2.4572851543780416e-05
Epoch 87 MSE:
               2.4339824449270964e-05
Epoch 88 MSE:
               2.3089078240445815e-05
Epoch 89 MSE:
               2.16975840885425e-05
Epoch 90 MSE:
               2.1208707039477304e-05
Epoch 91 MSE:
               2.160015719709918e-05
Epoch 92 MSE:
               2.2069916667533107e-05
Epoch 93 MSE:
               2.1982239559292793e-05
Epoch 94 MSE:
               2.1223773728706874e-05
Epoch 95 MSE:
               2.0476090867305174e-05
Epoch 96 MSE:
               2.0163013687124476e-05
Epoch 97 MSE:
               2.0388728444231674e-05
Epoch 98 MSE:
               2.060825499938801e-05
Epoch 99 MSE:
               2.049726026598364e-05
```

T-time: 44.000553369522095

Train Score: 0.14 RMSE _____ Validation Score: 1.80 RMSE _____

Time Step = 100 | Hidden States = 32 | Num Layers = 2 ______

```
Epoch 0 MSE: 0.05748049542307854
Epoch 1 MSE: 0.1907445639371872
Epoch 2 MSE: 0.03398081660270691
Epoch 3 MSE: 0.05354035645723343
Epoch 4 MSE:
              0.05382396653294563
Epoch 5 MSE: 0.035376351326704025
Epoch 6 MSE: 0.026823725551366806
Epoch 7 MSE: 0.036674436181783676
Epoch 8 MSE: 0.03500763326883316
Epoch 9 MSE: 0.02331707440316677
```

```
Epoch
       10 MSE:
                0.019106382504105568
Epoch
       11 MSE:
                0.02097553014755249
Epoch
       12 MSE:
                0.019819794222712517
       13 MSE:
Epoch
                0.011947859078645706
Epoch
       14 MSE:
                0.004354006145149469
Epoch
       15 MSE:
                0.008975885808467865
Epoch
       16 MSE:
                0.004057454410940409
Epoch
       17 MSE:
                0.004951869137585163
Epoch 18 MSE:
                0.008545905351638794
Epoch
       19 MSE:
                0.0020786274690181017
       20 MSE:
                0.0012905470794066787
Epoch
       21 MSE:
Epoch
                0.002983827143907547
Epoch
       22 MSE:
                0.0022207065485417843
Epoch
       23 MSE:
                0.0013954747701063752
Epoch
       24 MSE:
                0.0019393907859921455
Epoch
      25 MSE:
                0.0027682874351739883
Epoch
       26 MSE:
                0.0027245355304330587
       27 MSE:
Epoch
                0.0017899865051731467
Epoch
       28 MSE:
                0.0008544017910026014
Epoch
       29 MSE:
                0.0006978004821576178
       30 MSE:
Epoch
                0.0010141239035874605
       31 MSE:
Epoch
                0.0008877490763552487
       32 MSE:
Epoch
                0.00042523181764408946
       33 MSE:
Epoch
                0.0004995320923626423
Epoch
       34 MSE:
                0.0010210690088570118
Epoch
       35 MSE:
                0.0011241699103266
       36 MSE:
Epoch
                0.0006631024298258126
Epoch
       37 MSE:
                0.00030142805189825594
       38 MSE:
Epoch
                0.0003619993512984365
Epoch
       39 MSE:
                0.0004713368834927678
      40 MSE:
Epoch
                0.0003577501338440925
Epoch
       41 MSE:
                0.00023788401449564844
Epoch
       42 MSE:
                0.00031971532735042274
       43 MSE:
                0.00047980083036236465
Epoch
Epoch
       44 MSE:
                0.0004968976136296988
Epoch
       45 MSE:
                0.0003504099149722606
Epoch
       46 MSE:
                0.00021331929019652307
Epoch
       47 MSE:
                0.00020619285351131111
       48 MSE:
Epoch
                0.00024513847893103957
Epoch
       49 MSE:
                0.00020568368199747056
Epoch 50 MSE:
                0.00013946136459708214
       51 MSE:
Epoch
                0.00016444287030026317
Epoch
       52 MSE:
                0.00024338994990102947
       53 MSE:
Epoch
                0.00025041832122951746
Epoch
       54 MSE:
                0.00017859529179986566
Epoch
       55 MSE:
                0.00013102412049192935
Epoch
       56 MSE:
                0.00014345847012009472
       57 MSE:
                0.00015030555368866771
Epoch
```

```
Epoch 58 MSE:
                0.00012190359848318622
Epoch 59 MSE:
                0.00010742284939624369
      60 MSE:
Epoch
                0.00013256329111754894
Epoch
       61 MSE:
                0.00015607695968355983
Epoch
       62 MSE:
                0.0001420268090441823
Epoch
      63 MSE:
                0.00011229531810386106
Epoch
       64 MSE:
                0.00010382018808741122
Epoch
      65 MSE:
                0.00011044740676879883
Epoch 66 MSE:
                0.00010413186100777239
Epoch
      67 MSE:
                8.995588723337278e-05
       68 MSE:
                9.267980931326747e-05
Epoch
Epoch
      69 MSE:
                0.00010698170808609575
Epoch
      70 MSE:
                0.0001074887186405249
Epoch
      71 MSE:
                9.382289135828614e-05
Epoch 72 MSE:
                8.661529864184558e-05
Epoch 73 MSE:
                8.905716822482646e-05
Epoch 74 MSE:
                8.7040985818021e-05
Epoch 75 MSE:
                7.995298074092716e-05
Epoch
      76 MSE:
                7.970364094944671e-05
Epoch
      77 MSE:
                8.570306818000972e-05
Epoch
      78 MSE:
                8.637834980618209e-05
Epoch
      79 MSE:
                8.032078767428175e-05
      80 MSE:
Epoch
                7.659263064851984e-05
Epoch 81 MSE:
                7.720592839177698e-05
      82 MSE:
                7.580759120173752e-05
Epoch
Epoch
      83 MSE:
                7.20735260983929e-05
      84 MSE:
Epoch
                7.178141822805628e-05
Epoch
      85 MSE:
                7.430541882058606e-05
      86 MSE:
Epoch
                7.389291567960754e-05
Epoch 87 MSE:
                7.071471191011369e-05
Epoch 88 MSE:
                6.92711619194597e-05
Epoch
      89 MSE:
                6.930054951226339e-05
      90 MSE:
Epoch
                6.780679541407153e-05
      91 MSE:
Epoch
                6.597751780645922e-05
                6.622350338147953e-05
Epoch
       92 MSE:
Epoch
      93 MSE:
                6.691143789794296e-05
Epoch 94 MSE:
                6.580920307897031e-05
Epoch
      95 MSE:
                6.422309525078163e-05
Epoch
      96 MSE:
                6.374516669893637e-05
Epoch
      97 MSE:
                6.325939466478303e-05
      98 MSE:
Epoch
                6.199551717145368e-05
      99 MSE:
                6.127332744654268e-05
T-time: 68.60026049613953
```

Train Score: 0.23 RMSE

Validation Score: 6.31 RMSE

Epoch	0 MSE:	0.08087299019098282
Epoch	1 MSE:	0.03580334782600403
Epoch	2 MSE:	0.051343366503715515
Epoch	3 MSE:	0.04179958254098892
Epoch	4 MSE:	0.03351326286792755
Epoch	5 MSE:	0.031329404562711716
Epoch	6 MSE:	0.03148583695292473
Epoch	7 MSE:	0.031184352934360504
Epoch	8 MSE:	0.029072392731904984
Epoch	9 MSE:	0.025387607514858246
Epoch	10 MSE:	0.021982882171869278
Epoch	11 MSE:	0.02050633355975151
Epoch	12 MSE:	0.02020001783967018
Epoch	13 MSE:	0.014215677976608276
Epoch	14 MSE:	0.008556066080927849
Epoch	15 MSE:	0.005473265424370766
Epoch	16 MSE:	0.0028886711224913597
Epoch	10 MSE:	0.0028888711224913397
-	17 MSE:	0.005129105877131224
Epoch Epoch		0.003129103877131224
-	19 MSE:	0.00310357753187418
Epoch	20 MSE:	
Epoch	21 MSE:	0.00411528954282403
Epoch	22 MSE:	0.003285537241026759
Epoch	23 MSE:	0.0011851469753310084
Epoch	24 MSE:	0.0004039251944050193
Epoch	25 MSE:	0.0021105969790369272
Epoch	26 MSE:	0.002397578675299883
Epoch	27 MSE:	0.0011009302688762546
Epoch	28 MSE:	0.0010719405254349113
Epoch	29 MSE:	0.0017189482459798455
Epoch	30 MSE:	0.0017011506715789437
Epoch	31 MSE:	0.000935732270590961
Epoch	32 MSE:	0.0002436516952002421
Epoch	33 MSE:	0.00042543496238067746
Epoch	34 MSE:	0.0009488478535786271
Epoch	35 MSE:	0.0006745128775946796
Epoch	36 MSE:	0.0001924145472003147
Epoch	37 MSE:	0.0003221024526283145
Epoch	38 MSE:	0.0006468025385402143
Epoch	39 MSE:	0.0005706902011297643
Epoch	40 MSE:	0.0002002580586122349
Epoch	41 MSE:	0.0001103943504858762
Epoch	42 MSE:	0.0004130940942559391
Epoch	43 MSE:	0.00042720072087831795
Epoch	44 MSE:	0.00016218294331338257
Epoch	45 MSE:	0.00014258033479563892
Phoon	10 11011.	3.00011200000 f1 0000092

```
46 MSE:
                0.00031479651806876063
Epoch
Epoch
      47 MSE:
                0.0003152928838972002
      48 MSE:
                0.00013648565800394863
Epoch
       49 MSE:
Epoch
                8.336199971381575e-05
Epoch
      50 MSE:
                0.00021412860951386392
Epoch
      51 MSE:
                0.00022793276002630591
Epoch
       52 MSE:
                0.0001040798015310429
Epoch 53 MSE:
                9.922678873408586e-05
Epoch 54 MSE:
                0.0001821752084651962
Epoch 55 MSE:
                0.00016587189747951925
      56 MSE:
Epoch
                7.995316991582513e-05
Epoch
      57 MSE:
                8.099137630779296e-05
Epoch
      58 MSE:
                0.00014096770610194653
Epoch
      59 MSE:
                0.00011969777551712468
Epoch
      60 MSE:
                6.82939135003835e-05
Epoch 61 MSE:
                8.776311005931348e-05
Epoch
      62 MSE:
                0.00011774839367717505
       63 MSE:
Epoch
                8.935591176850721e-05
Epoch
       64 MSE:
                5.757935286965221e-05
Epoch
       65 MSE:
                7.800303865224123e-05
Epoch
       66 MSE:
                9.268551366403699e-05
Epoch
      67 MSE:
                6.584578659385443e-05
Epoch
      68 MSE:
                5.7584689784562215e-05
      69 MSE:
Epoch
                7.670072955079377e-05
Epoch 70 MSE:
                7.337648276006803e-05
Epoch
     71 MSE:
                5.25620453117881e-05
      72 MSE:
Epoch
                5.538268669624813e-05
Epoch
     73 MSE:
                6.709248555125669e-05
Epoch 74 MSE:
                5.644110933644697e-05
Epoch 75 MSE:
                4.797702786163427e-05
Epoch 76 MSE:
                5.689889076165855e-05
Epoch 77 MSE:
                5.73463476030156e-05
Epoch
      78 MSE:
                4.6331973862834275e-05
      79 MSE:
Epoch
                4.661304774344899e-05
                5.233173578744754e-05
Epoch
      80 MSE:
Epoch
      81 MSE:
                4.665992673835717e-05
Epoch
      82 MSE:
                4.2415238567627966e-05
Epoch
      83 MSE:
                4.695963434642181e-05
Epoch
      84 MSE:
                4.60598457721062e-05
Epoch
      85 MSE:
                4.035587335238233e-05
      86 MSE:
Epoch
                4.1476690967101604e-05
Epoch
      87 MSE:
                4.3302541598677635e-05
      88 MSE:
Epoch
                3.9350172301055863e-05
Epoch
      89 MSE:
                3.836225369013846e-05
Epoch
      90 MSE:
                4.04716374760028e-05
Epoch
       91 MSE:
                3.834975359495729e-05
Epoch
      92 MSE:
                3.59980040229857e-05
      93 MSE:
                3.728302908712067e-05
Epoch
```

Epoch 94 MSE: 3.6579236621037126e-05 Epoch 95 MSE: 3.4328779292991385e-05 Epoch 96 MSE: 3.4856384445447475e-05 Epoch 97 MSE: 3.484273111098446e-05 Epoch 98 MSE: 3.2855969038791955e-05 Epoch 99 MSE: 3.257604475948028e-05

T-time: 140.92648124694824

Train Score: 0.17 RMSE

----Validation Score: 1.11 RMSE

```
[25]: tanh_results = pd.DataFrame(tanh_results, columns=['time_step', 'num_layers', \cdot\ \cdot\'nidden_dim', 'trainScore', 'valScore'], index = None)

relu_results = pd.DataFrame(relu_results, columns=['time_step', 'num_layers', \cdot\ \cdot\'nidden_dim', 'trainScore', 'valScore'], index = None)
```

[26]:	time_step	num_layers	hidden_dim	trainScore	valScore
0	20.0	1.0	32.0	0.157601	3.239338
1	30.0	1.0	32.0	0.158502	3.263731
2	50.0	1.0	32.0	0.159220	3.302811
3	100.0	1.0	32.0	0.160202	3.406101
4	20.0	1.0	16.0	0.190952	4.905224
5	30.0	1.0	16.0	0.191295	4.934485
6	50.0	1.0	16.0	0.191400	4.976959
7	100.0	1.0	16.0	0.191759	5.091980
8	20.0	2.0	32.0	0.234232	6.114390
9	30.0	2.0	32.0	0.233431	6.126396
10	50.0	2.0	32.0	0.233398	6.173006
11	100.0	2.0	32.0	0.233582	6.307074
12	20.0	1.0	8.0	0.189662	6.405687
13	30.0	1.0	8.0	0.192436	6.439338
14	50.0	1.0	8.0	0.192422	6.496586
15	100.0	1.0	8.0	0.192664	6.647655
16	20.0	1.0	2.0	0.214332	7.186258
17	30.0	1.0	2.0	0.214289	7.219084
18	50.0	1.0	2.0	0.214202	7.287281
19	100.0	1.0	2.0	0.213989	7.468269
20	20.0	2.0	16.0	0.323674	8.185782
21	30.0	2.0	16.0	0.323771	8.214138

```
22
         50.0
                       2.0
                                                      8.281423
                                  16.0
                                           0.324007
23
        100.0
                       2.0
                                  16.0
                                          0.324592
                                                      8.468461
24
         20.0
                       2.0
                                   8.0
                                           0.261688
                                                      8.877346
                       2.0
25
         30.0
                                   8.0
                                           0.261400
                                                      8.907015
26
         50.0
                       2.0
                                   8.0
                                           0.261373
                                                      8.980628
27
        100.0
                       2.0
                                   8.0
                                          0.261374
                                                      9.182593
28
         20.0
                       1.0
                                   4.0
                                                      9.999781
                                          0.306535
29
         30.0
                       1.0
                                   4.0
                                           0.306323 10.037119
         20.0
                       2.0
                                           0.403289 10.109327
30
                                   4.0
31
         50.0
                       1.0
                                   4.0
                                           0.305934
                                                     10.116324
32
         30.0
                       2.0
                                   4.0
                                                     10.150412
                                          0.403421
33
         50.0
                       2.0
                                   4.0
                                          0.403689 10.237104
                       1.0
34
        100.0
                                   4.0
                                          0.304992 10.335959
35
        100.0
                       2.0
                                   4.0
                                          0.404363 10.476549
36
         20.0
                       2.0
                                   2.0
                                           1.492525
                                                     18.716492
37
         30.0
                       2.0
                                   2.0
                                           1.492423 18.771202
         50.0
38
                       2.0
                                   2.0
                                           1.492223 18.888865
                                   2.0
39
        100.0
                       2.0
                                           1.491707 19.245143
```

```
[27]: relu_results = relu_results.sort_values('valScore', ascending=True, _ ignore_index = True)
relu_results
```

[27]:	time_step	num_layers	hidden_dim	trainScore	valScore
0	20.0	2.0	32.0	0.133012	0.831369
1	100.0	2.0	16.0	0.171179	0.846573
2	30.0	2.0	32.0	0.144437	1.044344
3	50.0	2.0	32.0	0.154867	1.069251
4	100.0	2.0	32.0	0.170315	1.112106
5	20.0	1.0	2.0	0.485984	1.162175
6	30.0	1.0	2.0	0.486454	1.162243
7	100.0	1.0	2.0	0.488971	1.163013
8	20.0	2.0	2.0	0.223151	1.163247
9	50.0	1.0	2.0	0.487123	1.164787
10	30.0	2.0	2.0	0.223139	1.169142
11	50.0	2.0	2.0	0.223081	1.179064
12	100.0	2.0	2.0	0.223021	1.192291
13	20.0	1.0	16.0	0.183820	1.420421
14	30.0	1.0	16.0	0.184569	1.441064
15	50.0	1.0	16.0	0.185803	1.478651
16	100.0	1.0	16.0	0.186830	1.513478
17	100.0	1.0	32.0	0.135099	1.798861
18	20.0	1.0	32.0	0.144630	1.800635
19	50.0	1.0	32.0	0.148120	1.835724
20	30.0	1.0	32.0	0.157291	2.007290
21	30.0	1.0	8.0	0.136792	2.007576
22	50.0	1.0	8.0	0.136531	2.066542

```
23
         20.0
                       1.0
                                    8.0
                                           0.135812
                                                       2.070019
24
                       1.0
                                    8.0
        100.0
                                           0.136900
                                                       2.159652
25
         20.0
                       2.0
                                   16.0
                                           0.219959
                                                       2.293014
                       2.0
26
         30.0
                                   16.0
                                           0.221940
                                                       2.300989
27
         50.0
                       2.0
                                   16.0
                                           0.223492
                                                       2.315893
                       2.0
28
         20.0
                                    4.0
                                           0.121351
                                                       5.846859
29
         30.0
                       2.0
                                    4.0
                                           0.121407
                                                       5.875183
                       2.0
30
         50.0
                                    4.0
                                           0.121519
                                                       5.933123
                       2.0
                                    4.0
31
        100.0
                                           0.121753
                                                       6.084521
32
         20.0
                       2.0
                                    8.0
                                           0.289726
                                                       6.894939
33
                       2.0
                                    8.0
         30.0
                                           0.291008
                                                       6.938869
34
        100.0
                       2.0
                                    8.0
                                           0.275730
                                                       6.964060
35
         50.0
                       2.0
                                    8.0
                                           0.290500
                                                       6.999930
36
         20.0
                       1.0
                                    4.0
                                           4.668379
                                                      29.531164
37
                       1.0
                                    4.0
         30.0
                                           4.672350
                                                      29.592619
38
         50.0
                       1.0
                                    4.0
                                           4.680345
                                                      29.726151
                                    4.0
39
        100.0
                       1.0
                                           4.700520
                                                      30.148492
```

0.9 Selecting best model (Vanilla RNN with ReLU)

```
[28]: best_rnn_model = relu_results.iloc[0]
      best_rnn_model
[28]: time_step
                    20.000000
      num_layers
                     2.000000
      hidden_dim
                    32.000000
      trainScore
                     0.133012
      valScore
                     0.831369
      Name: 0, dtype: float64
[29]: input dim = 1
      output_dim = 1
      num epochs = 100
      lr = 0.01
      loss_type = torch.nn.MSELoss(reduction='mean')
      optimiser = torch.optim.Adam
      hidden_dim = int(best_rnn_model['hidden_dim'])
      num_layers = int(best_rnn_model['num_layers'])
      time_step = int(best_rnn_model['time_step'])
      torch.manual_seed(42)
      tuned_rnn = RNN_relu(input_dim = input_dim, hidden_dim = hidden_dim, output_dim_
       →= output_dim, layer_dim = num_layers)
      tuned rnn = to device(tuned rnn, device)
```



```
Epoch 0 MSE:
              0.08024495095014572
Epoch 1 MSE:
              0.03558538109064102
Epoch 2 MSE: 0.0503331758081913
Epoch 3 MSE: 0.04169435054063797
Epoch 4 MSE:
              0.03350633382797241
Epoch 5 MSE:
              0.031117025762796402
Epoch 6 MSE:
              0.031270455569028854
Epoch 7 MSE:
              0.03104744292795658
Epoch 8 MSE:
              0.029027357697486877
Epoch 9 MSE:
              0.02533632703125477
Epoch 10 MSE: 0.021798761561512947
Epoch 11 MSE:
               0.02015637420117855
Epoch 12 MSE:
               0.0201789028942585
Epoch 13 MSE:
               0.014230762608349323
Epoch 14 MSE:
               0.008676717057824135
Epoch 15 MSE:
               0.006079191341996193
Epoch 16 MSE:
               0.003683346090838313
Epoch 17 MSE:
               0.0006208492559380829
Epoch 18 MSE:
               0.004154627211391926
Epoch 19 MSE:
               0.004882219713181257
Epoch 20 MSE:
               0.002827702322974801
Epoch 21 MSE:
               0.003504342632368207
Epoch 22 MSE:
               0.0034184579271823168
               0.0017453309847041965
Epoch 23 MSE:
Epoch 24 MSE:
               0.0005337395123206079
Epoch 25 MSE:
               0.0013181816320866346
Epoch 26 MSE:
               0.002431813394650817
Epoch 27 MSE:
               0.002032879274338484
Epoch 28 MSE:
               0.0012406788300722837
Epoch 29 MSE:
               0.001183325075544417
Epoch 30 MSE:
               0.0014736357843503356
Epoch 31 MSE:
               0.0013759627472609282
Epoch 32 MSE:
               0.0007443660870194435
Epoch 33 MSE:
               0.00014996422396507114
Epoch 34 MSE:
               0.00028573846793733537
Epoch 35 MSE:
               0.0007765700574964285
Epoch 36 MSE:
               0.000618414138443768
Epoch 37 MSE:
               0.00021101327729411423
Epoch 38 MSE:
               0.0002916563826147467
Epoch 39 MSE:
               0.0005375298205763102
Epoch 40 MSE:
               0.0004483023367356509
Epoch 41 MSE:
               0.00012213132868055254
Epoch
      42 MSE:
               0.0001581912365509197
Epoch
      43 MSE:
               0.00046684592962265015
Epoch
      44 MSE:
               0.00022419630840886384
```

```
45 MSE:
                8.901473484002054e-05
Epoch
Epoch
      46 MSE:
                0.00025506390375085175
Epoch
      47 MSE:
                0.0002659439924173057
       48 MSE:
Epoch
                0.00010108391870744526
Epoch
       49 MSE:
                5.79161242058035e-05
Epoch
       50 MSE:
                0.00018963411275763065
Epoch
       51 MSE:
                0.0001914934255182743
Epoch 52 MSE:
                6.727626896463335e-05
Epoch 53 MSE:
                6.736813520547003e-05
Epoch 54 MSE:
                0.0001427126699127257
       55 MSE:
                0.0001256572868442163
Epoch
Epoch
      56 MSE:
                4.880207052337937e-05
Epoch
      57 MSE:
                5.5134787544375286e-05
Epoch
       58 MSE:
                0.00011268393427599221
Epoch 59 MSE:
                9.053738176589832e-05
Epoch 60 MSE:
                4.051646828884259e-05
Epoch
       61 MSE:
                5.857679934706539e-05
       62 MSE:
Epoch
                8.658769365865737e-05
Epoch
       63 MSE:
                6.191692227730528e-05
Epoch
       64 MSE:
                3.3862317650346085e-05
Epoch
       65 MSE:
                5.3126677812542766e-05
Epoch
       66 MSE:
                6.932936230441555e-05
Epoch
       67 MSE:
                4.5448698074324057e-05
       68 MSE:
Epoch
                3.396104875719175e-05
       69 MSE:
                5.025982318329625e-05
Epoch
Epoch
     70 MSE:
                5.2327803132357076e-05
      71 MSE:
Epoch
                3.4172127925558016e-05
Epoch
     72 MSE:
                3.1567116820951924e-05
Epoch 73 MSE:
                4.456937676877715e-05
Epoch 74 MSE:
                3.967718657804653e-05
Epoch 75 MSE:
                2.7792331820819527e-05
Epoch 76 MSE:
                3.262158497818746e-05
Epoch
      77 MSE:
                3.765518340514973e-05
      78 MSE:
Epoch
                2.936461714853067e-05
                2.48701217060443e-05
Epoch
       79 MSE:
Epoch
       80 MSE:
                3.105514406342991e-05
Epoch
       81 MSE:
                3.0276685720309615e-05
Epoch
       82 MSE:
                2.3680069716647267e-05
Epoch
       83 MSE:
                2.5393228497705422e-05
Epoch
       84 MSE:
                2.8241129257366993e-05
      85 MSE:
Epoch
                2.3966947992448695e-05
Epoch
       86 MSE:
                2.1963602193864062e-05
Epoch
       87 MSE:
                2.5264771466027014e-05
Epoch
       88 MSE:
                2.4164741262211464e-05
Epoch
       89 MSE:
                2.1144418496987782e-05
Epoch
       90 MSE:
                2.2795939003117383e-05
Epoch
       91 MSE:
                2.3507613150286488e-05
       92 MSE:
Epoch
                2.094406409014482e-05
```

Epoch 93 MSE: 2.10711732506752e-05
Epoch 94 MSE: 2.2501160856336355e-05
Epoch 95 MSE: 2.1023724912083708e-05
Epoch 96 MSE: 2.0319546820246615e-05
Epoch 97 MSE: 2.1516820197575726e-05
Epoch 98 MSE: 2.0886549464194104e-05
Epoch 99 MSE: 1.986884126381483e-05

T-time: 15.593940258026123

Train Score: 0.13 RMSE

-----Validation Score: 0.83 RMSE



0.10 Model Architecture (LSTM)

```
[30]: class LSTM_model(nn.Module):
    def __init__(self, input_dim, hidden_dim, layer_dim, output_dim):
        super(LSTM_model, self).__init__()
        self.hidden_dim = hidden_dim
        self.layer_dim = layer_dim
```

```
self.lstm = nn.LSTM(input_dim, hidden_dim, layer_dim, batch_first=True)
self.fc = nn.Linear(hidden_dim, output_dim)

def forward(self, x):
   h0 = Variable(torch.zeros(self.layer_dim, x.size(0), self.hidden_dim,u
device = device))
   c0 = Variable(torch.zeros(self.layer_dim, x.size(0), self.hidden_dim,u
device = device))
   out, (hn, cn) = self.lstm(x, (h0.detach(), c0.detach()))
   out = self.fc(out[:, -1, :])
   return out
```

```
[31]: gc.collect() torch.cuda.empty_cache()
```

0.11 LSTM Model

```
Epoch 1 MSE: 0.04281147941946983
Epoch 2 MSE: 0.036195024847984314
Epoch 3 MSE: 0.03292616829276085
Epoch 4 MSE: 0.032557085156440735
Epoch 5 MSE: 0.030960144475102425
Epoch 6 MSE: 0.026295436546206474
Epoch 7 MSE: 0.019574686884880066
Epoch 8 MSE: 0.014389541931450367
Epoch 9 MSE: 0.007475757040083408
Epoch 10 MSE: 0.0008210205123759806
Epoch 11 MSE: 0.010090870782732964
Epoch 12 MSE: 0.0070607322268188
```

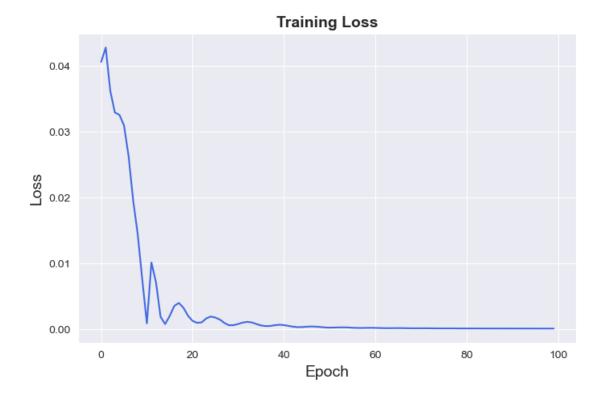
Epoch 0 MSE: 0.040618978440761566

```
Epoch
       13 MSE:
                0.0018260730430483818
Epoch
       14 MSE:
                0.0007192532648332417
       15 MSE:
Epoch
                0.001957071479409933
       16 MSE:
Epoch
                0.0034813072998076677
Epoch
       17 MSE:
                0.0039337510243058205
Epoch
       18 MSE:
                0.0032134391367435455
Epoch
       19 MSE:
                0.0019866065122187138
Epoch
       20 MSE:
                0.0012014649109914899
       21 MSE:
Epoch
                0.0009045402985066175
Epoch
       22 MSE:
                0.000983517151325941
       23 MSE:
                0.0015868934569880366
Epoch
       24 MSE:
Epoch
                0.00186759268399328
Epoch
       25 MSE:
                0.0017075836658477783
Epoch
       26 MSE:
                0.0013904622755944729
Epoch
       27 MSE:
                0.0008669569506309927
                0.0005355679895728827
Epoch
       28 MSE:
Epoch
       29 MSE:
                0.0005577965057455003
       30 MSE:
Epoch
                0.0007416111184284091
Epoch
       31 MSE:
                0.000952484377194196
Epoch
       32 MSE:
                0.0010651820339262486
Epoch
       33 MSE:
                0.000964015256613493
       34 MSE:
Epoch
                0.0007188546005636454
       35 MSE:
Epoch
                0.000508075871039182
       36 MSE:
Epoch
                0.0004137598443776369
       37 MSE:
                0.0004381434991955757
Epoch
Epoch
       38 MSE:
                0.00054739456390962
       39 MSE:
Epoch
                0.0006173465517349541
Epoch
       40 MSE:
                0.0005628871149383485
       41 MSE:
Epoch
                0.00044543895637616515
Epoch
      42 MSE:
                0.00032515102066099644
       43 MSE:
Epoch
                0.0002531992504373193
Epoch
       44 MSE:
                0.0002722999488469213
Epoch
       45 MSE:
                0.0003296692157164216
       46 MSE:
                0.00035123637644574046
Epoch
Epoch
       47 MSE:
                0.00033084998722188175
Epoch
       48 MSE:
                0.00027451166533865035
Epoch
       49 MSE:
                0.00020464873523451388
Epoch
       50 MSE:
                0.00017633654351811856
       51 MSE:
Epoch
                0.0001937545748660341
Epoch
       52 MSE:
                0.00021363218547776341
      53 MSE:
                0.00022324759629555047
Epoch
       54 MSE:
Epoch
                0.00020291823602747172
Epoch
       55 MSE:
                0.00015792869089636952
       56 MSE:
Epoch
                0.00013213518832344562
Epoch
       57 MSE:
                0.00013046184903942049
Epoch
       58 MSE:
                0.00013931546709500253
       59 MSE:
Epoch
                0.00015011505456641316
       60 MSE:
Epoch
                0.00014165484753903002
```

```
Epoch 61 MSE:
                0.00011667511716950685
Epoch 62 MSE:
                9.995536674978212e-05
Epoch 63 MSE:
                9.635627793613821e-05
Epoch
      64 MSE:
                0.00010215606016572565
Epoch 65 MSE:
                0.00010930553253274411
Epoch
      66 MSE:
                0.0001021002244669944
Epoch
      67 MSE:
                8.75506448210217e-05
                7.922462100395933e-05
Epoch 68 MSE:
Epoch 69 MSE:
                7.783198816468939e-05
Epoch 70 MSE:
                8.237096335506067e-05
Epoch 71 MSE:
                8.350572170456871e-05
Epoch
     72 MSE:
                7.578958320664242e-05
Epoch 73 MSE:
                6.776477675884962e-05
Epoch 74 MSE:
                6.405951717169955e-05
Epoch 75 MSE:
                6.484367622761056e-05
Epoch 76 MSE:
                6.721611134707928e-05
Epoch 77 MSE:
                6.424181628972292e-05
Epoch 78 MSE:
                5.865002458449453e-05
Epoch 79 MSE:
                5.511551717063412e-05
Epoch 80 MSE:
                5.4543936130357906e-05
Epoch
      81 MSE:
                5.61417436983902e-05
Epoch 82 MSE:
                5.509438778972253e-05
Epoch 83 MSE:
                5.172540477360599e-05
Epoch 84 MSE:
                4.908813934889622e-05
Epoch 85 MSE:
                4.818529851036146e-05
Epoch 86 MSE:
                4.9039434088626876e-05
Epoch 87 MSE:
                4.837533560930751e-05
Epoch 88 MSE:
                4.616101068677381e-05
Epoch 89 MSE:
                4.4178199459565803e-05
Epoch 90 MSE:
                4.345014167483896e-05
Epoch 91 MSE:
                4.385017746244557e-05
Epoch 92 MSE:
                4.3200554500799626e-05
Epoch 93 MSE:
                4.1761846659937873e-05
Epoch 94 MSE:
                4.043874650960788e-05
Epoch 95 MSE:
                4.012057252111845e-05
Epoch 96 MSE:
                4.0292685298481956e-05
Epoch 97 MSE:
                3.9715570892440155e-05
Epoch 98 MSE:
                3.875664697261527e-05
Epoch 99 MSE:
                3.797909812419675e-05
T-time: 38.01822757720947
```

Train Score: 0.18 RMSE

Validation Score: 3.35 RMSE



```
[33]: gc.collect() torch.cuda.empty_cache()
```

0.12 Hyper Parameter Tuning

```
[34]: input_dim = 1
  output_dim = 1
  num_epochs = 100
lr = 0.01
loss_type = torch.nn.MSELoss(reduction = 'mean')
  optimiser = torch.optim.Adam

num_layers = [1, 2]
  sliding_windows = [20, 30, 50, 100]
  hidden_dims = [2, 4, 8, 16, 32]

LSTM_results=[]

for time_step in sliding_windows:
  for hidden_dim in hidden_dims:
    for layers in num_layers:

    gc.collect()
```

Time Step = 20 | Hidden States = 2 | Num Layers = 1

```
Epoch 0 MSE: 0.09312347322702408
Epoch 1 MSE: 0.08503765612840652
Epoch 2 MSE: 0.07806186378002167
Epoch 3 MSE: 0.0720396339893341
Epoch 4 MSE: 0.06683067977428436
Epoch 5 MSE: 0.06231401860713959
Epoch 6 MSE: 0.058388471603393555
Epoch 7 MSE: 0.05497036874294281
Epoch 8 MSE: 0.05199102312326431
Epoch 9 MSE: 0.04939426854252815
Epoch 10 MSE: 0.047134049236774445
Epoch 11 MSE: 0.04517238214612007
Epoch 12 MSE: 0.043477535247802734
Epoch 13 MSE: 0.042022496461868286
Epoch 14 MSE: 0.04078375920653343
Epoch 15 MSE: 0.039740364998579025
Epoch 16 MSE: 0.03887315094470978
Epoch 17 MSE: 0.038164205849170685
Epoch 18 MSE: 0.03759652003645897
Epoch 19 MSE: 0.037153735756874084
Epoch 20 MSE: 0.03682004287838936
Epoch 21 MSE: 0.0365801565349102
Epoch 22 MSE: 0.036419350653886795
Epoch 23 MSE: 0.03632358834147453
Epoch 24 MSE: 0.03627965226769447
```

```
Epoch
       25 MSE:
                0.03627524897456169
Epoch
       26 MSE:
                0.0362992100417614
Epoch
       27 MSE:
                0.03634156659245491
       28 MSE:
Epoch
                0.0363936722278595
Epoch
       29 MSE:
                0.03644823282957077
Epoch
       30 MSE:
                0.03649933263659477
Epoch
       31 MSE:
                0.03654240071773529
Epoch
       32 MSE:
                0.03657414764165878
Epoch 33 MSE:
                0.03659243509173393
                0.03659617528319359
Epoch
       34 MSE:
       35 MSE:
Epoch
                0.03658517450094223
       36 MSE:
Epoch
                0.03655995428562164
Epoch
       37 MSE:
                0.03652162104845047
       38 MSE:
Epoch
                0.0364716574549675
Epoch
       39 MSE:
                0.0364118255674839
Epoch 40 MSE:
                0.03634398803114891
Epoch
       41 MSE:
                0.03627000376582146
       42 MSE:
Epoch
                0.03619164600968361
Epoch
       43 MSE:
                0.03611047938466072
Epoch
       44 MSE:
                0.036027852445840836
Epoch
       45 MSE:
                0.03594481572508812
      46 MSE:
Epoch
                0.03586212173104286
Epoch 47 MSE:
                0.035780224949121475
Epoch 48 MSE:
                0.035699255764484406
Epoch
       49 MSE:
                0.035619061440229416
Epoch
      50 MSE:
                0.03553924337029457
Epoch 51 MSE:
                0.03545915335416794
Epoch
       52 MSE:
                0.03537796065211296
       53 MSE:
Epoch
                0.035294659435749054
Epoch 54 MSE:
                0.03520810604095459
Epoch 55 MSE:
                0.03511705622076988
Epoch
       56 MSE:
                0.03502017632126808
      57 MSE:
Epoch
                0.03491605818271637
Epoch
      58 MSE:
                0.03480321168899536
Epoch
       59 MSE:
                0.0346800871193409
Epoch
       60 MSE:
                0.03454504534602165
Epoch
       61 MSE:
                0.034396328032016754
Epoch
       62 MSE:
                0.03423202410340309
       63 MSE:
Epoch
                0.03405003249645233
Epoch
       64 MSE:
                0.03384796902537346
       65 MSE:
Epoch
                0.033623140305280685
Epoch
       66 MSE:
                0.033372413367033005
Epoch
       67 MSE:
                0.03309211879968643
       68 MSE:
Epoch
                0.03277793526649475
Epoch
       69 MSE:
                0.03242475166916847
Epoch
       70 MSE:
                0.032026488333940506
Epoch
       71 MSE:
                0.03157590329647064
       72 MSE:
                0.03106437437236309
Epoch
```

```
Epoch 73 MSE:
               0.030481664463877678
Epoch 74 MSE:
               0.02981564588844776
Epoch 75 MSE:
               0.029052045196294785
Epoch 76 MSE:
               0.028174251317977905
Epoch 77 MSE:
               0.027163276448845863
Epoch 78 MSE:
               0.025998102501034737
Epoch 79 MSE:
               0.02465655282139778
Epoch 80 MSE:
               0.023117046803236008
Epoch 81 MSE:
               0.021361498162150383
Epoch 82 MSE:
               0.019379764795303345
Epoch 83 MSE:
               0.017175637185573578
Epoch 84 MSE:
               0.014774050563573837
Epoch 85 MSE:
               0.012228799983859062
Epoch 86 MSE:
               0.009630962274968624
Epoch 87 MSE:
               0.007118766196072102
Epoch 88 MSE:
               0.004888874478638172
Epoch 89 MSE:
               0.003196943551301956
Epoch 90 MSE:
               0.002307554939761758
Epoch 91 MSE:
               0.0023410769645124674
Epoch 92 MSE:
               0.0030904854647815228
Epoch 93 MSE:
               0.004101990722119808
Epoch 94 MSE:
               0.004962090868502855
Epoch 95 MSE:
               0.00533760292455554
Epoch 96 MSE:
               0.005040076095610857
Epoch 97 MSE:
               0.004229704849421978
Epoch 98 MSE:
               0.0032733476255089045
Epoch 99 MSE:
               0.002437604358419776
```

T-time: 3.1610684394836426

Train Score: 1.47 RMSE Validation Score: 16.39 RMSE

Time Step = 20 | Hidden States = 2 | Num Layers = 2 ______

Epoch 0 MSE: 0.03741060569882393 Epoch 1 MSE: 0.03556329756975174 Epoch 2 MSE: 0.034476738423109055 Epoch 3 MSE: 0.034121859818696976 Epoch 4 MSE: 0.03401393070816994 Epoch 5 MSE: 0.03354020044207573 Epoch 6 MSE: 0.03255666792392731 Epoch 7 MSE: 0.031215161085128784 Epoch 8 MSE: 0.029733188450336456

```
Epoch
       9 MSE:
               0.028329679742455482
Epoch
       10 MSE:
                0.027070775628089905
Epoch
       11 MSE:
                0.02563047595322132
       12 MSE:
Epoch
                0.023624664172530174
Epoch
       13 MSE:
                0.02111716754734516
Epoch
       14 MSE:
                0.018670404329895973
Epoch
       15 MSE:
                0.016784844920039177
Epoch
       16 MSE:
                0.014772159047424793
Epoch 17 MSE:
                0.011975259520113468
Epoch
       18 MSE:
                0.009322406724095345
       19 MSE:
                0.008011757396161556
Epoch
       20 MSE:
Epoch
                0.006455334834754467
Epoch
       21 MSE:
                0.0053104860708117485
Epoch
       22 MSE:
                0.005635484121739864
Epoch
       23 MSE:
                0.005105094984173775
Epoch
      24 MSE:
                0.006002330686897039
Epoch
       25 MSE:
                0.005842443555593491
       26 MSE:
Epoch
                0.00595932686701417
Epoch
       27 MSE:
                0.005818617530167103
Epoch
       28 MSE:
                0.004967294167727232
Epoch
       29 MSE:
                0.004364573862403631
       30 MSE:
Epoch
                0.003722385736182332
Epoch
       31 MSE:
                0.002884102752432227
       32 MSE:
Epoch
                0.002287705661728978
Epoch
       33 MSE:
                0.0020101089030504227
Epoch
       34 MSE:
                0.0018945704214274883
       35 MSE:
Epoch
                0.0018744965782389045
Epoch
       36 MSE:
                0.0019543233793228865
       37 MSE:
Epoch
                0.0021019543055444956
Epoch
       38 MSE:
                0.0022341059520840645
       39 MSE:
Epoch
                0.0022771162912249565
Epoch
       40 MSE:
                0.002214409876614809
Epoch
       41 MSE:
                0.0020758891478180885
       42 MSE:
                0.0018987004877999425
Epoch
Epoch
       43 MSE:
                0.0017068389570340514
Epoch
       44 MSE:
                0.001521158730611205
Epoch
       45 MSE:
                0.001373528502881527
Epoch
       46 MSE:
                0.0012973977718502283
       47 MSE:
Epoch
                0.0012996182776987553
Epoch
       48 MSE:
                0.0013485403032973409
Epoch 49 MSE:
                0.0013998413924127817
       50 MSE:
Epoch
                0.0014293681597337127
Epoch
       51 MSE:
                0.0014305050717666745
Epoch
       52 MSE:
                0.0013945832615718246
Epoch
       53 MSE:
                0.0013175298226997256
Epoch
       54 MSE:
                0.0012180840130895376
Epoch
       55 MSE:
                0.0011275821598246694
       56 MSE:
                0.0010627994779497385
Epoch
```

```
Epoch 57 MSE:
                0.0010221871780231595
Epoch 58 MSE:
                0.0010025978554040194
Epoch 59 MSE:
                0.0010020349873229861
Epoch
      60 MSE:
                0.001009102095849812
Epoch 61 MSE:
                0.0010067271068692207
Epoch 62 MSE:
                0.0009878977434709668
Epoch
      63 MSE:
                0.0009575225994922221
Epoch 64 MSE:
                0.0009201793582178652
Epoch 65 MSE:
                0.0008776998147368431
Epoch 66 MSE:
                0.0008374525932595134
Epoch
      67 MSE:
                0.0008087988826446235
Epoch 68 MSE:
                0.0007916488102637231
Epoch 69 MSE:
                0.0007805172353982925
Epoch 70 MSE:
                0.0007740383734926581
Epoch 71 MSE:
                0.0007693621446378529
Epoch 72 MSE:
                0.0007592898327857256
Epoch 73 MSE:
                0.0007427686359733343
Epoch 74 MSE:
                0.0007236749515868723
Epoch 75 MSE:
                0.0007023606449365616
Epoch 76 MSE:
                0.0006807553581893444
Epoch
     77 MSE:
                0.0006636265316046774
Epoch 78 MSE:
                0.0006507841171696782
Epoch 79 MSE:
                0.0006401201826520264
Epoch 80 MSE:
                0.0006318048108369112
Epoch 81 MSE:
                0.000623609172180295
Epoch 82 MSE:
                0.0006127976230345666
Epoch 83 MSE:
                0.0006002678419463336
Epoch
      84 MSE:
                0.000586525711696595
Epoch 85 MSE:
                0.0005715891602449119
Epoch 86 MSE:
                0.0005577430129051208
Epoch 87 MSE:
                0.0005458130617626011
Epoch
      88 MSE:
                0.0005351038416847587
Epoch 89 MSE:
                0.0005260297330096364
Epoch 90 MSE:
                0.000517552369274199
Epoch
      91 MSE:
                0.0005083277937956154
Epoch 92 MSE:
                0.0004986839485354722
Epoch 93 MSE:
                0.0004882697539869696
Epoch 94 MSE:
                0.00047738742432557046
Epoch 95 MSE:
                0.0004671572532970458
Epoch 96 MSE:
                0.0004575165512505919
Epoch 97 MSE:
                0.00044874826562590897
Epoch 98 MSE:
                0.0004408386303111911
Epoch 99 MSE:
                0.00043299238313920796
T-time: 6.1838698387146
```

Train Score: 0.62 RMSE

Validation Score: 13.35 RMSE

Time Step = 20 | Hidden States = 4 | Num Layers = 1

Epoch 0 MSE: 0.0476691909134388 Epoch 1 MSE: 0.04031091183423996 Epoch 2 MSE: 0.0353727713227272 Epoch 3 MSE: 0.03228141367435455 Epoch 4 MSE: 0.030462227761745453 Epoch 5 MSE: 0.029329154640436172 Epoch 6 MSE: 0.028265638276934624 Epoch 7 MSE: 0.026802033185958862 Epoch 8 MSE: 0.02471897006034851 Epoch 9 MSE: 0.022013423964381218 Epoch 10 MSE: 0.018835794180631638 Epoch 11 MSE: 0.015446249395608902 Epoch 12 MSE: 0.0121819619089365 Epoch 13 MSE: 0.009398289024829865 Epoch 14 MSE: 0.007339555770158768 Epoch 15 MSE: 0.005936325062066317 Epoch 16 MSE: 0.00476225558668375 Epoch 17 MSE: 0.003475409699603915 Epoch 18 MSE: 0.0022553580347448587 Epoch 19 MSE: 0.0016735362587496638 Epoch 20 MSE: 0.0021435911767184734 Epoch 21 MSE: 0.0033493235241621733 Epoch 22 MSE: 0.004397901240736246 Epoch 23 MSE: 0.004697822965681553 Epoch 24 MSE: 0.004306400194764137 Epoch 25 MSE: 0.003626349149271846 Epoch 26 MSE: 0.0030288593843579292 Epoch 27 MSE: 0.002633433323353529 Epoch 28 MSE: 0.00232895789667964 Epoch 29 MSE: 0.001985090086236596 Epoch 30 MSE: 0.001604872290045023 Epoch 31 MSE: 0.001288596075028181 Epoch 32 MSE: 0.0011267525842413306 Epoch 33 MSE: 0.0011394666507840157 Epoch 34 MSE: 0.0012776257935911417 Epoch 35 MSE: 0.0014575390378013253 Epoch 36 MSE: 0.0016005780780687928 Epoch 37 MSE: 0.0016598358051851392 Epoch 38 MSE: 0.0016276946989819407 Epoch 39 MSE: 0.001527489977888763Epoch 40 MSE: 0.0013966637197881937

```
Epoch
       41 MSE:
                0.0012691259616985917
Epoch
       42 MSE:
                0.0011630617082118988
Epoch
       43 MSE:
                0.0010781921446323395
       44 MSE:
Epoch
                0.001002966775558889
Epoch
       45 MSE:
                0.0009272439638152719
Epoch
       46 MSE:
                0.0008523438591510057
Epoch
       47 MSE:
                0.000791627389844507
Epoch
       48 MSE:
                0.0007611485198140144
Epoch 49 MSE:
                0.0007670848281122744
Epoch
      50 MSE:
                0.0007990785525180399
       51 MSE:
                0.0008344135712832212
Epoch
Epoch
       52 MSE:
                0.0008502000127919018
Epoch
       53 MSE:
                0.0008352378499694169
Epoch
       54 MSE:
                0.0007940737414173782
Epoch
       55 MSE:
                0.0007417165907099843
Epoch 56 MSE:
                0.000693676236551255
Epoch
       57 MSE:
                0.0006581316702067852
       58 MSE:
Epoch
                0.0006344766588881612
Epoch
       59 MSE:
                0.0006175278103910387
Epoch
       60 MSE:
                0.000603084044996649
Epoch
       61 MSE:
                0.0005906199221499264
Epoch
       62 MSE:
                0.0005820220103487372
Epoch
       63 MSE:
                0.0005783993401564658
       64 MSE:
Epoch
                0.0005779106286354363
       65 MSE:
                0.000576186808757484
Epoch
Epoch
       66 MSE:
                0.0005688189994543791
       67 MSE:
Epoch
                0.0005540263373404741
Epoch
       68 MSE:
                0.0005337024922482669
       69 MSE:
Epoch
                0.0005122337606735528
Epoch
      70 MSE:
                0.000493955856654793
Epoch 71 MSE:
                0.0004809240344911814
Epoch
       72 MSE:
                0.00047235345118679106
Epoch
      73 MSE:
                0.00046587447286583483
      74 MSE:
Epoch
                0.0004594610654748976
Epoch
       75 MSE:
                0.0004525370604824275
Epoch
       76 MSE:
                0.00044560772948898375
Epoch
      77 MSE:
                0.0004390606773085892
Epoch
      78 MSE:
                0.0004323889734223485
      79 MSE:
Epoch
                0.0004245254385750741
Epoch
       80 MSE:
                0.00041487280395813286
       81 MSE:
Epoch
                0.00040401038131676614
       82 MSE:
Epoch
                0.00039342170930467546
Epoch
       83 MSE:
                0.00038448895793408155
       84 MSE:
Epoch
                0.0003776047669816762
Epoch
       85 MSE:
                0.000372076581697911
Epoch
       86 MSE:
                0.0003667909768410027
Epoch
       87 MSE:
                0.00036101051955483854
       88 MSE:
                0.00035468567511998117
Epoch
```

```
Epoch 89 MSE: 0.0003481664170976728
Epoch 90 MSE: 0.00034171357401646674
Epoch 91 MSE:
               0.0003352834319230169
Epoch 92 MSE:
               0.0003287134750280529
Epoch 93 MSE:
               0.00032204369199462235
Epoch 94 MSE:
               0.00031560685602016747
Epoch 95 MSE:
               0.00030978964059613645
Epoch 96 MSE:
               0.00030469545163214207
Epoch 97 MSE: 0.00030003764550201595
Epoch 98 MSE:
               0.0002953621151391417
Epoch 99 MSE:
               0.0002903850399889052
```

T-time: 4.63914680480957

Train Score: 0.51 RMSE

Validation Score: 10.26 RMSE

Time Step = 20 | Hidden States = 4 | Num Layers = 2

```
Epoch 0 MSE: 0.3314470052719116
Epoch 1 MSE: 0.2895655930042267
Epoch 2 MSE: 0.25215527415275574
Epoch 3 MSE: 0.21890045702457428
Epoch 4 MSE: 0.18922480940818787
Epoch 5 MSE: 0.16251906752586365
Epoch 6 MSE: 0.13822953402996063
Epoch 7 MSE: 0.11594878882169724
Epoch 8 MSE: 0.09545944631099701
Epoch 9 MSE: 0.07677548378705978
Epoch 10 MSE: 0.06018766760826111
Epoch 11 MSE: 0.04628366976976395
Epoch 12 MSE:
               0.03590754047036171
Epoch 13 MSE: 0.03000040538609028
Epoch 14 MSE: 0.029201937839388847
Epoch 15 MSE: 0.033059291541576385
Epoch 16 MSE: 0.03924023360013962
Epoch 17 MSE: 0.04450882598757744
Epoch 18 MSE:
               0.046926554292440414
Epoch 19 MSE:
               0.04635290056467056
Epoch 20 MSE:
               0.043653108179569244
Epoch 21 MSE:
               0.03995268791913986
Epoch 22 MSE:
               0.03621889278292656
Epoch 23 MSE:
               0.0330883227288723
Epoch 24 MSE: 0.030851956456899643
```

```
Epoch
      25 MSE:
                0.029529618099331856
Epoch
      26 MSE:
                0.02897460013628006
Epoch
      27 MSE:
                0.028967594727873802
      28 MSE:
Epoch
                0.029281869530677795
Epoch
      29 MSE:
                0.029719509184360504
Epoch
      30 MSE:
                0.03012651391327381
Epoch
       31 MSE:
                0.030395211651921272
Epoch
      32 MSE:
                0.030460434034466743
Epoch 33 MSE:
                0.03029320389032364
                0.02989385649561882
Epoch
      34 MSE:
      35 MSE:
                0.029285456985235214
Epoch
Epoch
       36 MSE:
                0.02850763313472271
Epoch
      37 MSE:
                0.027610791847109795
Epoch
       38 MSE:
                0.02665044739842415
Epoch
      39 MSE:
                0.0256815105676651
Epoch 40 MSE:
                0.02475237473845482
Epoch 41 MSE:
                0.02389901503920555
      42 MSE:
Epoch
                0.023139510303735733
Epoch
       43 MSE:
                0.022470014169812202
Epoch
      44 MSE:
                0.0218634232878685
Epoch
       45 MSE:
                0.021272191777825356
Epoch 46 MSE:
                0.020636167377233505
Epoch 47 MSE:
                0.019894815981388092
Epoch 48 MSE:
                0.019001543521881104
Epoch 49 MSE:
                0.017935728654265404
Epoch 50 MSE:
                0.01670856401324272
Epoch 51 MSE:
                0.015360022895038128
Epoch
       52 MSE:
                0.013947776518762112
Epoch 53 MSE:
                0.012531949207186699
Epoch 54 MSE:
                0.011160898953676224
Epoch 55 MSE:
                0.009862413629889488
Epoch 56 MSE:
                0.008642690256237984
Epoch 57 MSE:
                0.007492608856409788
Epoch 58 MSE:
                0.006399011705070734
Epoch
       59 MSE:
                0.005357502028346062
Epoch
       60 MSE:
                0.0043825567699968815
Epoch
       61 MSE:
                0.0035107603762298822
Epoch
       62 MSE:
                0.00279443571344018
       63 MSE:
Epoch
                0.0022860649041831493
Epoch
       64 MSE:
                0.0020178291015326977
Epoch 65 MSE:
                0.0019835960119962692
       66 MSE:
Epoch
                0.0021318658255040646
Epoch
       67 MSE:
                0.002376530086621642
       68 MSE:
Epoch
                0.0026245536282658577
Epoch
      69 MSE:
                0.002806229516863823
Epoch
      70 MSE:
                0.0028888678643852472
Epoch
      71 MSE:
                0.002869753632694483
      72 MSE:
Epoch
                0.0027614776045084
```

```
Epoch 73 MSE:
               0.0025825551711022854
Epoch 74 MSE:
               0.002354794181883335
Epoch 75 MSE:
               0.002102434169501066
Epoch 76 MSE:
               0.0018499356228858232
Epoch 77 MSE:
               0.0016188282752409577
Epoch 78 MSE:
               0.0014251484535634518
Epoch 79 MSE:
               0.0012781880795955658
Epoch 80 MSE:
               0.001180431921966374
Epoch 81 MSE:
               0.0011283335043117404
Epoch 82 MSE:
               0.0011136899702250957
Epoch 83 MSE:
               0.0011254535056650639
Epoch 84 MSE:
               0.0011517409002408385
Epoch 85 MSE:
               0.0011816861806437373
Epoch 86 MSE:
               0.0012067868374288082
Epoch 87 MSE:
               0.0012215296737849712
Epoch 88 MSE:
               0.001223295577801764
Epoch 89 MSE:
               0.0012117772130295634
Epoch 90 MSE:
               0.0011882188264280558
Epoch 91 MSE:
               0.0011547630419954658
Epoch 92 MSE:
               0.0011140452697873116
Epoch 93 MSE:
               0.001068995683453977
Epoch 94 MSE:
               0.001022734446451068
Epoch 95 MSE:
               0.0009783946443349123
Epoch 96 MSE:
               0.0009388247271999717
Epoch 97 MSE:
               0.0009061988675966859
Epoch 98 MSE:
               0.0008816739427857101
Epoch 99 MSE:
               0.0008652282995171845
T-time: 8.572082757949829
```

Train Score: 0.88 RMSE

Validation Score: 15.17 RMSE

_____ Time Step = 20 | Hidden States = 8 | Num Layers = 1

Epoch 0 MSE: 0.05825553834438324 Epoch 1 MSE: 0.043158553540706635 Epoch 2 MSE: 0.03295919671654701 Epoch 3 MSE: 0.027600597590208054 Epoch 4 MSE: 0.026622261852025986 Epoch 5 MSE: 0.028469804674386978 Epoch 6 MSE: 0.030398914590477943 Epoch 7 MSE: 0.030631273984909058 Epoch 8 MSE: 0.029163261875510216

```
Epoch 9 MSE:
               0.026775440201163292
Epoch
       10 MSE:
                0.024265071377158165
Epoch
       11 MSE:
                0.022158166393637657
       12 MSE:
Epoch
                0.020665429532527924
Epoch
       13 MSE:
                0.019741494208574295
Epoch
       14 MSE:
                0.019177567213773727
Epoch
       15 MSE:
                0.018694598227739334
Epoch 16 MSE:
                0.018022865056991577
Epoch 17 MSE:
                0.016962334513664246
Epoch
       18 MSE:
                0.015420733019709587
       19 MSE:
                0.01342847291380167
Epoch
      20 MSE:
Epoch
                0.0111320149153471
Epoch
      21 MSE:
                0.00876751821488142
Epoch
       22 MSE:
                0.006611123215407133
Epoch
      23 MSE:
                0.004893188830465078
Epoch 24 MSE:
                0.0036720118951052427
Epoch
      25 MSE:
                0.0027532484382390976
      26 MSE:
Epoch
                0.0018820111872628331
Epoch
      27 MSE:
                0.0011631317902356386
Epoch
       28 MSE:
                0.0010896854801103473
       29 MSE:
Epoch
                0.0019411685643717647
      30 MSE:
Epoch
                0.0031294170767068863
Epoch
      31 MSE:
                0.0036110426299273968
       32 MSE:
Epoch
                0.003002812620252371
Epoch
      33 MSE:
                0.0017706271028146148
Epoch
       34 MSE:
                0.0006660091457888484
      35 MSE:
Epoch
                0.00019253331993240863
Epoch
       36 MSE:
                0.0003538781020324677
      37 MSE:
Epoch
                0.0007639992400072515
Epoch 38 MSE:
                0.001027119462378323
      39 MSE:
Epoch
                0.0010249929036945105
Epoch
       40 MSE:
                0.0008845517295412719
Epoch
      41 MSE:
                0.0007781816530041397
       42 MSE:
                0.0007803333573974669
Epoch
Epoch
       43 MSE:
                0.0008475292706862092
Epoch
      44 MSE:
                0.0008790342835709453
Epoch
      45 MSE:
                0.0007954585016705096
Epoch
      46 MSE:
                0.0005910788895562291
      47 MSE:
Epoch
                0.00033970436197705567
Epoch
      48 MSE:
                0.000153801724081859
Epoch 49 MSE:
                0.0001139388041337952
       50 MSE:
Epoch
                0.00020751552074216306
Epoch
       51 MSE:
                0.0003314586647320539
Epoch
       52 MSE:
                0.00037845526821911335
Epoch
      53 MSE:
                0.0003311529872007668
Epoch
       54 MSE:
                0.0002591580559965223
Epoch
       55 MSE:
                0.00023045105626806617
       56 MSE:
                0.0002466205332893878
Epoch
```

```
Epoch 57 MSE:
                0.00025977694895118475
Epoch 58 MSE:
                0.00023122831771615893
Epoch 59 MSE:
                0.0001673258957453072
Epoch
      60 MSE:
                0.0001086046831915155
Epoch 61 MSE:
                9.194685844704509e-05
Epoch
      62 MSE:
                0.00012041290756314993
Epoch
      63 MSE:
                0.00016374020196963102
Epoch 64 MSE:
                0.00018601964984554797
Epoch 65 MSE:
                0.00017436363850720227
Epoch 66 MSE:
                0.0001439887419110164
Epoch 67 MSE:
                0.00011951993656111881
Epoch 68 MSE:
                0.00011309246474411339
Epoch 69 MSE:
                0.00011793054727604613
Epoch 70 MSE:
                0.00011904719576705247
Epoch 71 MSE:
                0.00010867404489545152
Epoch 72 MSE:
                9.274765034206212e-05
Epoch 73 MSE:
                8.406941924476996e-05
Epoch 74 MSE:
                8.930880721891299e-05
Epoch 75 MSE:
                0.0001023005970637314
Epoch 76 MSE:
                0.00011016665666829795
Epoch
     77 MSE:
                0.00010580290836514905
Epoch 78 MSE:
                9.362892888020724e-05
Epoch 79 MSE:
                8.355755562661216e-05
Epoch 80 MSE:
                8.105902088573202e-05
Epoch 81 MSE:
                8.362023800145835e-05
Epoch 82 MSE:
                8.532070205546916e-05
Epoch 83 MSE:
                8.324914961121976e-05
Epoch 84 MSE:
                7.947967969812453e-05
Epoch 85 MSE:
                7.785147317918018e-05
Epoch 86 MSE:
                7.961165101733059e-05
Epoch 87 MSE:
                8.228226215578616e-05
Epoch 88 MSE:
                8.243647607741877e-05
Epoch 89 MSE:
                7.91824422776699e-05
Epoch 90 MSE:
                7.480111526092514e-05
Epoch
      91 MSE:
                7.224494765978307e-05
Epoch 92 MSE:
                7.237038516905159e-05
Epoch 93 MSE:
                7.360773452091962e-05
Epoch 94 MSE:
                7.395144348265603e-05
Epoch 95 MSE:
                7.292721420526505e-05
Epoch 96 MSE:
                7.16338909114711e-05
Epoch 97 MSE:
               7.118537905625999e-05
Epoch
      98 MSE:
                7.14432098902762e-05
Epoch 99 MSE:
                7.134530460461974e-05
T-time: 4.921580076217651
```

Train Score: 0.25 RMSE

Time Step = 20 | Hidden States = 8 | Num Layers = 2

Epoch 0 MSE: 0.12994571030139923 Epoch 1 MSE: 0.0994478389620781 Epoch 2 MSE: 0.07569443434476852 Epoch 3 MSE: 0.05788685753941536 Epoch 4 MSE: 0.045414961874485016 Epoch 5 MSE: 0.037923723459243774 Epoch 6 MSE: 0.03514662757515907 Epoch 7 MSE: 0.03640522062778473 Epoch 8 MSE: 0.039832279086112976 Epoch 9 MSE: 0.042751289904117584 Epoch 10 MSE: 0.04362796992063522 Epoch 11 MSE: 0.04252170771360397 Epoch 12 MSE: 0.04023510217666626 Epoch 13 MSE: 0.037635479122400284 Epoch 14 MSE: 0.0353538952767849 Epoch 15 MSE: 0.03371354937553406 Epoch 16 MSE: 0.03277355432510376 Epoch 17 MSE: 0.03241555765271187 Epoch 18 MSE: 0.032428279519081116 Epoch 19 MSE: 0.03256998956203461 Epoch 20 MSE: 0.032610125839710236 Epoch 21 MSE: 0.03235846012830734 Epoch 22 MSE: 0.031681936234235764 Epoch 23 MSE: 0.030505232512950897 Epoch 24 MSE: 0.028799353167414665 Epoch 25 MSE: 0.026572324335575104 Epoch 26 MSE: 0.02388254553079605 Epoch 27 MSE: 0.02088451012969017 Epoch 28 MSE: 0.017876796424388885 Epoch 29 MSE: 0.015182023867964745 Epoch 30 MSE: 0.01264833565801382 Epoch 31 MSE: 0.009577754884958267 Epoch 32 MSE: 0.0059660738334059715 Epoch 33 MSE: 0.003719171741977334 Epoch 34 MSE: 0.004525795578956604 Epoch 35 MSE: 0.006471995264291763 Epoch 36 MSE: 0.00730649009346962 Epoch 37 MSE: 0.006957707926630974 Epoch 38 MSE: 0.006032193079590797 Epoch 39 MSE: 0.00510413758456707 Epoch 40 MSE: 0.004479322582483292

```
Epoch
       41 MSE:
                0.004130595829337835
Epoch
       42 MSE:
                0.0038935192860662937
       43 MSE:
Epoch
                0.0036046309396624565
       44 MSE:
Epoch
                0.0031888887751847506
Epoch
       45 MSE:
                0.002893792698159814
Epoch
       46 MSE:
                0.0029255289118736982
Epoch
       47 MSE:
                0.0032006404362618923
Epoch
       48 MSE:
                0.0035050734877586365
Epoch 49 MSE:
                0.0036383706610649824
Epoch
       50 MSE:
                0.0035148663446307182
       51 MSE:
                0.0031801918521523476
Epoch
Epoch
       52 MSE:
                0.0027622508350759745
Epoch
       53 MSE:
                0.0024011079221963882
Epoch
       54 MSE:
                0.002186909317970276
Epoch
       55 MSE:
                0.0021251945290714502
Epoch 56 MSE:
                0.002145368605852127
Epoch
       57 MSE:
                0.002153625711798668
       58 MSE:
Epoch
                0.0020956448279321194
Epoch
       59 MSE:
                0.001979268854483962
Epoch
       60 MSE:
                0.0018479942809790373
Epoch
       61 MSE:
                0.0017374414019286633
Epoch
       62 MSE:
                0.0016504242084920406
Epoch
       63 MSE:
                0.0015643162187188864
       64 MSE:
Epoch
                0.001458246260881424
       65 MSE:
                0.0013357948046177626
Epoch
Epoch
       66 MSE:
                0.0012255286565050483
       67 MSE:
Epoch
                0.001158796134404838
Epoch
       68 MSE:
                0.00114130147267133
       69 MSE:
Epoch
                0.0011423772666603327
Epoch
      70 MSE:
                0.0011155246756970882
      71 MSE:
Epoch
                0.001036631758324802
Epoch
       72 MSE:
                0.0009249103022739291
Epoch
      73 MSE:
                0.0008253629202954471
       74 MSE:
                0.000770055630709976
Epoch
Epoch
       75 MSE:
                0.0007545240805484354
Epoch
       76 MSE:
                0.0007474928861483932
Epoch
      77 MSE:
                0.0007205851725302637
Epoch
      78 MSE:
                0.0006701528327539563
       79 MSE:
Epoch
                0.0006143125356175005
Epoch
       80 MSE:
                0.0005714285071007907
       81 MSE:
                0.0005423253169283271
Epoch
       82 MSE:
Epoch
                0.0005139620043337345
Epoch
       83 MSE:
                0.0004785172059200704
       84 MSE:
Epoch
                0.0004433322756085545
Epoch
       85 MSE:
                0.0004196815425530076
Epoch
       86 MSE:
                0.0004065359244123101
       87 MSE:
Epoch
                0.0003905880148522556
       88 MSE:
                0.00036180380266159773
Epoch
```

Epoch 89 MSE: 0.0003253490722272545 Epoch 90 MSE: 0.0002959334524348378 Epoch 91 MSE: 0.00028098520124331117 Epoch 92 MSE: 0.00027260713977739215 Epoch 93 MSE: 0.00025842615286819637 Epoch 94 MSE: 0.00023676789714954793 Epoch 95 MSE: 0.00021586731600109488 Epoch 96 MSE: 0.0002007576695177704 Epoch 97 MSE: 0.0001880618219729513 Epoch 98 MSE: 0.00017398047202732414 0.00016078643966466188 Epoch 99 MSE:

T-time: 8.467175245285034

Train Score: 0.38 RMSE

Validation Score: 12.32 RMSE

Time Step = 20 | Hidden States = 16 | Num Layers = 1

Epoch 0 MSE: 0.03276994824409485 Epoch 1 MSE: 0.030665095895528793 Epoch 2 MSE: 0.02820461057126522 Epoch 3 MSE: 0.025931522250175476 Epoch 4 MSE: 0.02304583042860031 Epoch 5 MSE: 0.020216332748532295 Epoch 6 MSE: 0.016421645879745483 Epoch 7 MSE: 0.011813461780548096 Epoch 8 MSE: 0.006941511295735836 Epoch 9 MSE: 0.0017938256496563554 Epoch 10 MSE: 0.0009985202923417091 Epoch 11 MSE: 0.008369500748813152 Epoch 12 MSE: 0.006530001759529114 Epoch 13 MSE: 0.003844093531370163 Epoch 14 MSE: 0.0005515284719876945 Epoch 15 MSE: 0.0007174302591010928 Epoch 16 MSE: 0.0011479513486847281 Epoch 17 MSE: 0.001312021166086197 Epoch 18 MSE: 0.0019177976064383984 Epoch 19 MSE: 0.0025622029788792133 Epoch 20 MSE: 0.0026190553326159716 Epoch 21 MSE: 0.0022416606079787016 Epoch 22 MSE: 0.0018987029325217009 Epoch 23 MSE: 0.0016421128530055285 Epoch 24 MSE: 0.001196470926515758

```
Epoch
      25 MSE:
                0.0005822759703733027
Epoch
      26 MSE:
                0.00021332601318135858
Epoch
      27 MSE:
                0.00023780783521942794
      28 MSE:
Epoch
                0.00031020137248560786
Epoch
      29 MSE:
                0.0003875640977639705
Epoch
      30 MSE:
                0.0006926088244654238
Epoch
       31 MSE:
                0.0008866877760738134
Epoch
      32 MSE:
                0.0007205175934359431
Epoch 33 MSE:
                0.000524865579791367
Epoch
      34 MSE:
                0.00038882874650880694
      35 MSE:
                0.00018657397595234215
Epoch
Epoch
      36 MSE:
                6.500500603578985e-05
Epoch
      37 MSE:
                0.00011949735198868439
Epoch
       38 MSE:
                0.00020634061365853995
Epoch
      39 MSE:
                0.00024057121481746435
Epoch 40 MSE:
                0.00027965556364506483
Epoch
      41 MSE:
                0.0003317320079077035
      42 MSE:
Epoch
                0.00032263522734865546
Epoch
       43 MSE:
                0.00024628863320685923
Epoch
      44 MSE:
                0.000177295645698905
Epoch
       45 MSE:
                0.00013757936540059745
Epoch
      46 MSE:
                9.087140642805025e-05
Epoch 47 MSE:
                5.373802196118049e-05
      48 MSE:
Epoch
                7.144011033233255e-05
      49 MSE:
                0.00011273685231572017
Epoch
Epoch 50 MSE:
                0.00012818754476029426
Epoch 51 MSE:
                0.00013610247697215527
Epoch
      52 MSE:
                0.0001434089062968269
Epoch 53 MSE:
                0.00011993023508694023
Epoch 54 MSE:
                8.16081155790016e-05
Epoch 55 MSE:
                6.394574302248657e-05
Epoch
      56 MSE:
                5.7671753893373534e-05
Epoch 57 MSE:
                5.1428854931145906e-05
      58 MSE:
Epoch
                5.885305654373951e-05
Epoch
       59 MSE:
                7.571359310531989e-05
Epoch
       60 MSE:
                8.178706048056483e-05
Epoch
       61 MSE:
                7.82418719609268e-05
Epoch
       62 MSE:
                7.538565114373341e-05
Epoch
       63 MSE:
                6.807868339819834e-05
Epoch
       64 MSE:
                5.4416606872109696e-05
      65 MSE:
Epoch
                4.659507976612076e-05
       66 MSE:
Epoch
                4.7115310735534877e-05
Epoch
       67 MSE:
                4.790042294189334e-05
Epoch
       68 MSE:
                5.035730646341108e-05
Epoch
      69 MSE:
                5.636470450554043e-05
Epoch
      70 MSE:
                5.80581727263052e-05
Epoch
      71 MSE:
                5.429987868410535e-05
      72 MSE:
                5.114873420097865e-05
Epoch
```

```
Epoch 73 MSE: 4.7759374865563586e-05
Epoch 74 MSE: 4.338206417742185e-05
Epoch 75 MSE:
               4.250931669957936e-05
Epoch 76 MSE:
               4.453271321835928e-05
Epoch 77 MSE:
               4.562840695143677e-05
Epoch 78 MSE:
               4.6628811105620116e-05
Epoch 79 MSE:
               4.779420851264149e-05
Epoch 80 MSE:
               4.670589987654239e-05
Epoch 81 MSE:
               4.439886470208876e-05
Epoch 82 MSE:
               4.3125528463860974e-05
Epoch 83 MSE:
               4.206654193694703e-05
Epoch 84 MSE:
               4.127145803067833e-05
Epoch 85 MSE:
               4.199579052510671e-05
Epoch 86 MSE:
               4.295536928111687e-05
Epoch 87 MSE:
               4.304940011934377e-05
Epoch 88 MSE:
               4.3082221964141354e-05
Epoch 89 MSE:
               4.2715604649856687e-05
Epoch 90 MSE:
               4.160636672168039e-05
Epoch 91 MSE:
               4.090703441761434e-05
Epoch 92 MSE:
               4.074715980095789e-05
Epoch 93 MSE:
               4.059166167280637e-05
Epoch 94 MSE:
               4.081426959601231e-05
Epoch 95 MSE:
               4.12047520512715e-05
Epoch 96 MSE:
               4.1120409150607884e-05
Epoch 97 MSE:
               4.086610351805575e-05
Epoch 98 MSE:
               4.061046274728142e-05
Epoch 99 MSE:
               4.0142993384506553e-05
```

T-time: 12.791428804397583

Train Score: 0.19 RMSE Validation Score: 5.12 RMSE

_____ Time Step = 20 | Hidden States = 16 | Num Layers = 2 ______

```
Epoch 0 MSE: 0.055617596954107285
Epoch 1 MSE: 0.040461476892232895
Epoch 2 MSE: 0.03614800050854683
Epoch 3 MSE:
              0.03908803313970566
Epoch 4 MSE:
              0.03798329457640648
Epoch 5 MSE: 0.03556669503450394
Epoch 6 MSE: 0.03417842090129852
Epoch 7 MSE:
              0.03373211994767189
Epoch 8 MSE: 0.033635273575782776
```

```
Epoch
      9 MSE:
               0.03343185409903526
Epoch
       10 MSE:
                0.03285475820302963
Epoch
       11 MSE:
                0.03176776319742203
       12 MSE:
Epoch
                0.030107436701655388
Epoch
       13 MSE:
                0.027857108041644096
Epoch
       14 MSE:
                0.025073327124118805
Epoch
       15 MSE:
                0.021848665550351143
Epoch
       16 MSE:
                0.01788274012506008
Epoch 17 MSE:
                0.012161249294877052
Epoch
       18 MSE:
                0.005137161817401648
       19 MSE:
                0.0012971122050657868
Epoch
       20 MSE:
Epoch
                0.004584522917866707
Epoch
       21 MSE:
                0.008680528029799461
Epoch
       22 MSE:
                0.008846175856888294
Epoch
       23 MSE:
                0.006379065569490194
Epoch
      24 MSE:
                0.0034846095368266106
Epoch
       25 MSE:
                0.0016557638300582767
       26 MSE:
Epoch
                0.001415078528225422
Epoch
       27 MSE:
                0.0022226660512387753
Epoch
       28 MSE:
                0.003062036819756031
       29 MSE:
Epoch
                0.003463856177404523
       30 MSE:
Epoch
                0.00352539517916739
Epoch
       31 MSE:
                0.0032754039857536554
       32 MSE:
Epoch
                0.002669117646291852
Epoch
       33 MSE:
                0.001893228036351502
Epoch
       34 MSE:
                0.001357685076072812
       35 MSE:
Epoch
                0.00130429957062006
Epoch
       36 MSE:
                0.0014579185517504811
       37 MSE:
Epoch
                0.001524752820841968
Epoch
       38 MSE:
                0.0016521288780495524
       39 MSE:
Epoch
                0.0018523557810112834
Epoch
       40 MSE:
                0.001813726150430739
Epoch
       41 MSE:
                0.0014741899212822318
       42 MSE:
                0.0011370973661541939
Epoch
Epoch
       43 MSE:
                0.0009572810959070921
Epoch
       44 MSE:
                0.0008054820937104523
Epoch
       45 MSE:
                0.0007004032959230244
Epoch
       46 MSE:
                0.0007721668807789683
       47 MSE:
Epoch
                0.0009131281985901296
Epoch
       48 MSE:
                0.0009244944085367024
      49 MSE:
Epoch
                0.0008081443957053125
       50 MSE:
Epoch
                0.0006669650902040303
Epoch
       51 MSE:
                0.0005049013998359442
Epoch
       52 MSE:
                0.0003425285394769162
Epoch
       53 MSE:
                0.000297767692245543
Epoch
       54 MSE:
                0.00034978706389665604
Epoch
       55 MSE:
                0.0003694285114761442
       56 MSE:
                0.00034754324587993324
Epoch
```

```
Epoch 57 MSE:
                0.0002812344755511731
Epoch 58 MSE:
                0.00015871231153141707
Epoch 59 MSE:
                0.00010163098340854049
Epoch 60 MSE:
                0.00012164582585683092
Epoch 61 MSE:
                0.00017082707199733704
Epoch 62 MSE:
                0.00020692349062301219
Epoch
      63 MSE:
                0.00015023062587715685
Epoch 64 MSE:
                8.737985626794398e-05
Epoch 65 MSE:
                7.144839037209749e-05
Epoch 66 MSE:
                0.00010701202700147405
Epoch 67 MSE:
                0.00014858583745080978
Epoch 68 MSE:
                0.00013561882951762527
Epoch 69 MSE:
                0.00010310432116966695
Epoch 70 MSE:
                6.959307938814163e-05
Epoch 71 MSE:
                8.790752326603979e-05
Epoch 72 MSE:
                0.00010773472604341805
Epoch 73 MSE:
                0.00011232728138566017
Epoch 74 MSE:
                8.515261288266629e-05
Epoch 75 MSE:
                6.445386679843068e-05
Epoch 76 MSE:
                6.880739965708926e-05
Epoch 77 MSE:
                7.931187428766862e-05
Epoch 78 MSE:
                8.44935784698464e-05
Epoch 79 MSE:
                6.823447620263323e-05
Epoch 80 MSE:
                5.777169280918315e-05
Epoch 81 MSE:
                5.4394429753301665e-05
Epoch 82 MSE:
                6.334391218842939e-05
Epoch 83 MSE:
                6.72365931677632e-05
Epoch 84 MSE:
                6.0493959608720616e-05
Epoch 85 MSE:
                5.339373092283495e-05
Epoch 86 MSE:
                5.0261642172699794e-05
Epoch 87 MSE:
                5.584623431786895e-05
Epoch 88 MSE:
                5.830606824019924e-05
Epoch 89 MSE:
                5.637291178572923e-05
Epoch 90 MSE:
                5.141127621755004e-05
Epoch 91 MSE:
                4.900311250821687e-05
Epoch 92 MSE:
                5.1650276873260736e-05
Epoch 93 MSE:
                5.3452800784725696e-05
Epoch 94 MSE:
                5.2950839744880795e-05
Epoch 95 MSE:
                4.936274854117073e-05
Epoch 96 MSE:
                4.78304318676237e-05
Epoch 97 MSE:
                4.870588963967748e-05
Epoch 98 MSE:
                4.99523121106904e-05
Epoch 99 MSE:
                4.9463280447525904e-05
T-time: 17.17224931716919
```

Train Score: 0.21 RMSE

Time Step = 20 | Hidden States = 32 | Num Layers = 1

Epoch 0 MSE: 0.054647479206323624 Epoch 1 MSE: 0.03648120164871216 Epoch 2 MSE: 0.032304421067237854 Epoch 3 MSE: 0.03474355861544609 Epoch 4 MSE: 0.03280533477663994 Epoch 5 MSE: 0.028274912387132645 Epoch 6 MSE: 0.02457757294178009 Epoch 7 MSE: 0.022285714745521545 Epoch 8 MSE: 0.02035769447684288 Epoch 9 MSE: 0.017211314290761948 Epoch 10 MSE: 0.011273961514234543 Epoch 11 MSE: 0.0032086812425404787 Epoch 12 MSE: 0.01175837591290474 Epoch 13 MSE: 0.003141402965411544 Epoch 14 MSE: 0.0015027684858068824 Epoch 15 MSE: 0.005173086654394865 Epoch 16 MSE: 0.006386267952620983 Epoch 17 MSE: 0.0044372957199811935 Epoch 18 MSE: 0.0014774819137528539 Epoch 19 MSE: 0.00033436642843298614 Epoch 20 MSE: 0.002040162682533264 Epoch 21 MSE: 0.0034192902967333794 Epoch 22 MSE: 0.002188729587942362 Epoch 23 MSE: 0.0006446552579291165 Epoch 24 MSE: 0.0004921055515296757 Epoch 25 MSE: 0.0012262987438589334 Epoch 26 MSE: 0.0018178564496338367 Epoch 27 MSE: 0.0017250403761863708 Epoch 28 MSE: 0.0010487979743629694 Epoch 29 MSE: 0.0003498228034004569 Epoch 30 MSE: 0.00022648346202913672 Epoch 31 MSE: 0.0007135641644708812 Epoch 32 MSE: 0.0011146441102027893 Epoch 33 MSE: 0.0008929803152568638 Epoch 34 MSE: 0.00039733698940835893 Epoch 35 MSE: 0.00020610468345694244 Epoch 36 MSE: 0.0003865587350446731 Epoch 37 MSE: 0.0006218919297680259 Epoch 38 MSE: 0.000648828805424273 Epoch 39 MSE: 0.0004640010301955044 Epoch 40 MSE: 0.00025815394474193454

```
Epoch 41 MSE:
                0.00021735051996074617
Epoch
      42 MSE:
                0.00034306812449358404
                0.0004533316823653877
Epoch
      43 MSE:
       44 MSE:
Epoch
                0.0004004799702670425
Epoch 45 MSE:
                0.00024673412553966045
Epoch
      46 MSE:
                0.00016018908354453743
Epoch
       47 MSE:
                0.0002037107915384695
Epoch
      48 MSE:
                0.0002918366517405957
Epoch 49 MSE:
                0.0003127134405076504
Epoch 50 MSE:
                0.00024566028150729835
      51 MSE:
                0.00016535223403479904
Epoch
Epoch
      52 MSE:
                0.0001497129414929077
Epoch
      53 MSE:
                0.0001934567844728008
Epoch
       54 MSE:
                0.00022388208890333772
Epoch 55 MSE:
                0.00019788571808021516
Epoch 56 MSE:
                0.00014941080007702112
Epoch 57 MSE:
                0.00013261126878205687
      58 MSE:
                0.00015394826186820865
Epoch
Epoch
      59 MSE:
                0.00017575659148860723
Epoch
       60 MSE:
                0.00016693015641067177
Epoch
       61 MSE:
                0.0001358155277557671
Epoch
      62 MSE:
                0.0001156265425379388
Epoch
      63 MSE:
                0.00012355137732811272
       64 MSE:
Epoch
                0.00014131284842733294
       65 MSE:
                0.00014129254850558937
Epoch
Epoch
       66 MSE:
                0.00012279611837584525
       67 MSE:
Epoch
                0.00010846887016668916
Epoch
       68 MSE:
                0.00011115415691165254
      69 MSE:
Epoch
                0.00012020060239592567
Epoch 70 MSE:
                0.00011973019718425348
Epoch 71 MSE:
                0.0001090204605134204
Epoch
      72 MSE:
                0.00010052078869193792
Epoch
      73 MSE:
                0.000102076111943461
      74 MSE:
                0.00010737152479123324
Epoch
Epoch
      75 MSE:
                0.00010602917609503493
Epoch
      76 MSE:
                9.805918671190739e-05
Epoch
     77 MSE:
                9.240830695489421e-05
Epoch
      78 MSE:
                9.364397556055337e-05
      79 MSE:
Epoch
                9.666867845226079e-05
      80 MSE:
Epoch
                9.50694375205785e-05
      81 MSE:
                8.971377246780321e-05
Epoch
       82 MSE:
Epoch
                8.633673860458657e-05
Epoch
       83 MSE:
                8.70184157975018e-05
Epoch
       84 MSE:
                8.794452151050791e-05
Epoch
      85 MSE:
                8.573003287892789e-05
Epoch
       86 MSE:
                8.213185355998576e-05
Epoch
       87 MSE:
                8.064151916187257e-05
       88 MSE:
                8.121036080410704e-05
Epoch
```

Epoch 89 MSE: 8.091860945569351e-05 Epoch 90 MSE: 7.856896263547242e-05 Epoch 91 MSE: 7.611598266521469e-05 Epoch 92 MSE: 7.541648665210232e-05 Epoch 93 MSE: 7.557746721431613e-05 Epoch 94 MSE: 7.467650721082464e-05 Epoch 95 MSE: 7.273762457771227e-05 Epoch 96 MSE: 7.133638428058475e-05 Epoch 97 MSE: 7.097133493516594e-05 Epoch 98 MSE: 7.053482113406062e-05 Epoch 99 MSE: 6.928383663762361e-05

T-time: 19.999114751815796

Train Score: 0.25 RMSE

_____ Validation Score: 6.06 RMSE _____

Time Step = 20 | Hidden States = 32 | Num Layers = 2

Epoch 0 MSE: 0.040618978440761566 Epoch 1 MSE: 0.04281147941946983 Epoch 2 MSE: 0.036195024847984314 Epoch 3 MSE: 0.03292616829276085 Epoch 4 MSE: 0.032557085156440735 Epoch 5 MSE: 0.030960144475102425 Epoch 6 MSE: 0.026295436546206474 Epoch 7 MSE: 0.019574686884880066 Epoch 8 MSE: 0.014389541931450367 Epoch 9 MSE: 0.007475757040083408 Epoch 10 MSE: 0.0008210205123759806 Epoch 11 MSE: 0.010090870782732964 Epoch 12 MSE: 0.0070607322268188 Epoch 13 MSE: 0.0018260730430483818 Epoch 14 MSE: 0.0007192532648332417 Epoch 15 MSE: 0.001957071479409933 Epoch 16 MSE: 0.0034813072998076677 Epoch 17 MSE: 0.0039337510243058205 Epoch 18 MSE: 0.0032134391367435455 Epoch 19 MSE: 0.0019866065122187138 Epoch 20 MSE: 0.0012014649109914899 Epoch 21 MSE: 0.0009045402985066175 Epoch 22 MSE: 0.000983517151325941 Epoch 23 MSE: 0.0015868934569880366 Epoch 24 MSE: 0.00186759268399328

```
Epoch
       25 MSE:
                0.0017075836658477783
Epoch
       26 MSE:
                0.0013904622755944729
Epoch
       27 MSE:
                0.0008669569506309927
       28 MSE:
Epoch
                0.0005355679895728827
Epoch
       29 MSE:
                0.0005577965057455003
       30 MSE:
Epoch
                0.0007416111184284091
Epoch
       31 MSE:
                0.000952484377194196
Epoch
       32 MSE:
                0.0010651820339262486
       33 MSE:
Epoch
                0.000964015256613493
Epoch
       34 MSE:
                0.0007188546005636454
       35 MSE:
                0.000508075871039182
Epoch
Epoch
       36 MSE:
                0.0004137598443776369
Epoch
       37 MSE:
                0.0004381434991955757
Epoch
       38 MSE:
                0.00054739456390962
Epoch
       39 MSE:
                0.0006173465517349541
      40 MSE:
                0.0005628871149383485
Epoch
Epoch
       41 MSE:
                0.00044543895637616515
       42 MSE:
Epoch
                0.00032515102066099644
Epoch
       43 MSE:
                0.0002531992504373193
Epoch
       44 MSE:
                0.0002722999488469213
Epoch
       45 MSE:
                0.0003296692157164216
Epoch
       46 MSE:
                0.00035123637644574046
Epoch
      47 MSE:
                0.00033084998722188175
       48 MSE:
Epoch
                0.00027451166533865035
       49 MSE:
                0.00020464873523451388
Epoch
       50 MSE:
Epoch
                0.00017633654351811856
       51 MSE:
Epoch
                0.0001937545748660341
Epoch
       52 MSE:
                0.00021363218547776341
       53 MSE:
Epoch
                0.00022324759629555047
Epoch
      54 MSE:
                0.00020291823602747172
Epoch 55 MSE:
                0.00015792869089636952
Epoch
       56 MSE:
                0.00013213518832344562
       57 MSE:
Epoch
                0.00013046184903942049
       58 MSE:
                0.00013931546709500253
Epoch
Epoch
       59 MSE:
                0.00015011505456641316
Epoch
       60 MSE:
                0.00014165484753903002
Epoch
       61 MSE:
                0.00011667511716950685
Epoch
       62 MSE:
                9.995536674978212e-05
       63 MSE:
Epoch
                9.635627793613821e-05
Epoch
       64 MSE:
                0.00010215606016572565
       65 MSE:
Epoch
                0.00010930553253274411
       66 MSE:
Epoch
                0.0001021002244669944
       67 MSE:
                8.75506448210217e-05
Epoch
Epoch
       68 MSE:
                7.922462100395933e-05
Epoch
       69 MSE:
                7.783198816468939e-05
Epoch
       70 MSE:
                8.237096335506067e-05
Epoch
       71 MSE:
                8.350572170456871e-05
       72 MSE:
                7.578958320664242e-05
Epoch
```

```
Epoch 73 MSE:
               6.776477675884962e-05
Epoch 74 MSE:
               6.405951717169955e-05
Epoch 75 MSE:
               6.484367622761056e-05
Epoch 76 MSE:
               6.721611134707928e-05
Epoch 77 MSE:
               6.424181628972292e-05
Epoch 78 MSE:
               5.865002458449453e-05
Epoch 79 MSE:
               5.511551717063412e-05
               5.4543936130357906e-05
Epoch 80 MSE:
Epoch 81 MSE:
               5.61417436983902e-05
               5.509438778972253e-05
Epoch 82 MSE:
Epoch 83 MSE:
               5.172540477360599e-05
Epoch 84 MSE:
               4.908813934889622e-05
Epoch 85 MSE:
               4.818529851036146e-05
Epoch 86 MSE:
               4.9039434088626876e-05
Epoch 87 MSE:
               4.837533560930751e-05
Epoch 88 MSE:
               4.616101068677381e-05
Epoch 89 MSE:
               4.4178199459565803e-05
Epoch 90 MSE:
               4.345014167483896e-05
Epoch 91 MSE:
               4.385017746244557e-05
Epoch 92 MSE:
               4.3200554500799626e-05
Epoch 93 MSE:
               4.1761846659937873e-05
Epoch 94 MSE:
               4.043874650960788e-05
Epoch 95 MSE:
               4.012057252111845e-05
Epoch 96 MSE:
               4.0292685298481956e-05
Epoch 97 MSE:
               3.9715570892440155e-05
Epoch 98 MSE:
               3.875664697261527e-05
Epoch 99 MSE:
               3.797909812419675e-05
```

T-time: 38.14018797874451

Train Score: 0.18 RMSE Validation Score: 3.35 RMSE

_____ Time Step = 30 | Hidden States = 2 | Num Layers = 1 ______

```
Epoch 0 MSE: 0.0931047797203064
Epoch 1 MSE: 0.08502224832773209
Epoch 2 MSE: 0.07804983854293823
Epoch 3 MSE:
              0.07203090190887451
Epoch 4 MSE:
              0.06682506948709488
Epoch 5 MSE:
              0.06231138855218887
Epoch 6 MSE:
              0.05838865041732788
Epoch 7 MSE:
              0.05497321859002113
Epoch 8 MSE: 0.05199643224477768
```

```
Epoch 9 MSE:
               0.04940212145447731
Epoch
       10 MSE:
                0.04714424908161163
Epoch
       11 MSE:
                0.045184843242168427
       12 MSE:
Epoch
                0.043492164462804794
Epoch
       13 MSE:
                0.04203920066356659
Epoch
       14 MSE:
                0.040802448987960815
Epoch
       15 MSE:
                0.039760932326316833
Epoch
       16 MSE:
                0.03889548406004906
Epoch 17 MSE:
                0.038188185542821884
Epoch
       18 MSE:
                0.03762201964855194
       19 MSE:
                0.037180621176958084
Epoch
       20 MSE:
Epoch
                0.03684817627072334
Epoch
       21 MSE:
                0.03660937771201134
Epoch
       22 MSE:
                0.03644951805472374
Epoch
       23 MSE:
                0.03635454922914505
Epoch 24 MSE:
                0.036311253905296326
Epoch
       25 MSE:
                0.03630734980106354
       26 MSE:
Epoch
                0.036331672221422195
Epoch
       27 MSE:
                0.036374274641275406
Epoch
       28 MSE:
                0.03642651438713074
Epoch
       29 MSE:
                0.036481112241744995
       30 MSE:
Epoch
                0.036532171070575714
Epoch
       31 MSE:
                0.03657514229416847
       32 MSE:
Epoch
                0.03660673648118973
Epoch
       33 MSE:
                0.03662484139204025
Epoch
       34 MSE:
                0.03662838041782379
       35 MSE:
Epoch
                0.03661717474460602
Epoch
       36 MSE:
                0.03659175708889961
       37 MSE:
Epoch
                0.036553237587213516
Epoch
      38 MSE:
                0.03650311008095741
       39 MSE:
                0.036443136632442474
Epoch
Epoch
       40 MSE:
                0.03637517988681793
Epoch
       41 MSE:
                0.03630111366510391
       42 MSE:
                0.03622270002961159
Epoch
Epoch
       43 MSE:
                0.03614149987697601
Epoch
       44 MSE:
                0.036058858036994934
Epoch
       45 MSE:
                0.03597583621740341
Epoch
       46 MSE:
                0.035893164575099945
       47 MSE:
Epoch
                0.035811301320791245
Epoch
       48 MSE:
                0.03573036193847656
Epoch 49 MSE:
                0.03565020486712456
       50 MSE:
Epoch
                0.0355704128742218
Epoch
       51 MSE:
                0.03549035266041756
Epoch
       52 MSE:
                0.035409167408943176
Epoch
       53 MSE:
                0.03532585874199867
Epoch
       54 MSE:
                0.035239286720752716
Epoch
       55 MSE:
                0.035148199647665024
       56 MSE:
Epoch
                0.03505126014351845
```

```
Epoch 57 MSE:
                0.034947045147418976
Epoch 58 MSE:
                0.03483409434556961
Epoch 59 MSE:
                0.0347108356654644
Epoch 60 MSE:
                0.034575626254081726
Epoch 61 MSE:
                0.034426718950271606
Epoch 62 MSE:
                0.034262191504240036
Epoch
      63 MSE:
                0.034079935401678085
Epoch 64 MSE:
                0.03387758135795593
Epoch 65 MSE:
                0.033652424812316895
Epoch 66 MSE:
                0.033401310443878174
      67 MSE:
Epoch
                0.03312057629227638
Epoch 68 MSE:
                0.03280589357018471
Epoch 69 MSE:
                0.032452140003442764
Epoch 70 MSE:
                0.032053206115961075
Epoch 71 MSE:
                0.031601835042238235
Epoch 72 MSE:
                0.031089389696717262
Epoch 73 MSE:
                0.030505599454045296
Epoch 74 MSE:
                0.029838306829333305
Epoch 75 MSE:
                0.029073188081383705
Epoch 76 MSE:
                0.028193579986691475
Epoch
     77 MSE:
                0.027180442586541176
Epoch 78 MSE:
                0.026012670248746872
Epoch 79 MSE:
                0.02466801181435585
Epoch 80 MSE:
                0.02312478981912136
Epoch 81 MSE:
                0.021364819258451462
Epoch 82 MSE:
                0.019377870485186577
Epoch 83 MSE:
                0.01716766320168972
Epoch 84 MSE:
                0.014759106561541557
Epoch 85 MSE:
                0.012206139974296093
Epoch 86 MSE:
                0.009600398130714893
Epoch 87 MSE:
                0.007081704679876566
Epoch 88 MSE:
                0.004850620403885841
Epoch 89 MSE:
                0.003170698182657361
Epoch 90 MSE:
                0.0023175168316811323
Epoch
      91 MSE:
                0.0024164870847016573
Epoch 92 MSE:
                0.0032443059608340263
Epoch 93 MSE:
                0.004305259324610233
Epoch 94 MSE:
                0.005118384957313538
Epoch 95 MSE:
                0.005328201223164797
Epoch 96 MSE:
                0.004848814103752375
Epoch 97 MSE:
                0.003943135961890221
Epoch 98 MSE:
                0.002982157515361905
Epoch 99 MSE:
                0.0021929971408098936
T-time: 4.738654851913452
```

1 01mc. 1.700001001310102

Train Score: 1.40 RMSE

Validation Score: 16.53 RMSE

Time Step = 30 | Hidden States = 2 | Num Layers = 2

Epoch 0 MSE: 0.03743020445108414 Epoch 1 MSE: 0.0355871319770813 Epoch 2 MSE: 0.03450414910912514 Epoch 3 MSE: 0.03415123373270035 Epoch 4 MSE: 0.03404003754258156 Epoch 5 MSE: 0.033559445291757584 Epoch 6 MSE: 0.03256857395172119 Epoch 7 MSE: 0.03121930919587612 Epoch 8 MSE: 0.029728256165981293 Epoch 9 MSE: 0.028313659131526947 Epoch 10 MSE: 0.027036404237151146 Epoch 11 MSE: 0.02555874176323414 Epoch 12 MSE: 0.023495953530073166 Epoch 13 MSE: 0.020929627120494843 Epoch 14 MSE: 0.018468277528882027 Epoch 15 MSE: 0.016617123037576675 Epoch 16 MSE: 0.01456636842340231 Epoch 17 MSE: 0.011684935539960861 Epoch 18 MSE: 0.009090748615562916 Epoch 19 MSE: 0.00794270634651184 Epoch 20 MSE: 0.006333993282169104 Epoch 21 MSE: 0.005575692746788263 Epoch 22 MSE: 0.005905823316425085 Epoch 23 MSE: 0.005458590108901262 Epoch 24 MSE: 0.006385055370628834 Epoch 25 MSE: 0.006017789244651794 Epoch 26 MSE: 0.00586643535643816 Epoch 27 MSE: 0.005482946988195181 Epoch 28 MSE: 0.0045054336078464985 Epoch 29 MSE: 0.003699104068800807 Epoch 30 MSE: 0.0031471154652535915 Epoch 31 MSE: 0.002577594481408596 Epoch 32 MSE: 0.0021188054233789444 Epoch 33 MSE: 0.0019277167739346623 Epoch 34 MSE: 0.0019430303946137428 Epoch 35 MSE: 0.00203618872910738 Epoch 36 MSE: 0.0021299428772181273 Epoch 37 MSE: 0.00220085890032351 Epoch 38 MSE: 0.002239403547719121 Epoch 39 MSE: 0.0022227929439395666Epoch 40 MSE: 0.002125674393028021

```
Epoch
       41 MSE:
                0.0019518095068633556
Epoch
       42 MSE:
                0.0017453855834901333
Epoch
       43 MSE:
                0.0015644885133951902
       44 MSE:
Epoch
                0.0014430875889956951
Epoch
       45 MSE:
                0.0013799029402434826
Epoch
       46 MSE:
                0.0013597701909020543
Epoch
       47 MSE:
                0.0013743534218519926
Epoch
       48 MSE:
                0.001413844176568091
Epoch 49 MSE:
                0.0014485323335975409
Epoch
       50 MSE:
                0.001442047650925815
       51 MSE:
                0.0013869603862985969
Epoch
Epoch
       52 MSE:
                0.0013064377708360553
Epoch
       53 MSE:
                0.0012208258267492056
Epoch
       54 MSE:
                0.0011358140036463737
Epoch
       55 MSE:
                0.001060860580764711
       56 MSE:
                0.0010128882713615894
Epoch
Epoch
       57 MSE:
                0.0009954317938536406
       58 MSE:
Epoch
                0.0009921352611854672
Epoch
       59 MSE:
                0.0009873128728941083
Epoch
       60 MSE:
                0.0009780462132766843
Epoch
       61 MSE:
                0.0009625210077501833
Epoch
       62 MSE:
                0.0009339737007394433
Epoch
       63 MSE:
                0.0008929171599447727
       64 MSE:
Epoch
                0.0008509823819622397
       65 MSE:
                0.0008161578443832695
Epoch
Epoch
       66 MSE:
                0.0007872273563407362
       67 MSE:
Epoch
                0.0007654805667698383
Epoch
       68 MSE:
                0.0007544835680164397
       69 MSE:
Epoch
                0.0007486286922357976
Epoch
       70 MSE:
                0.0007399423629976809
       71 MSE:
Epoch
                0.0007287512999027967
Epoch
       72 MSE:
                0.0007148710428737104
Epoch
       73 MSE:
                0.0006950623355805874
       74 MSE:
Epoch
                0.0006730344612151384
Epoch
       75 MSE:
                0.0006537439185194671
Epoch
       76 MSE:
                0.0006362751009874046
Epoch
       77 MSE:
                0.0006215344765223563
Epoch
       78 MSE:
                0.0006113455747254193
       79 MSE:
Epoch
                0.000602387881372124
Epoch
       80 MSE:
                0.0005924353026784956
       81 MSE:
                0.0005821567610837519
Epoch
       82 MSE:
Epoch
                0.0005699064349755645
Epoch
       83 MSE:
                0.0005554214003495872
       84 MSE:
Epoch
                0.0005412617465481162
Epoch
       85 MSE:
                0.0005276907468214631
Epoch
       86 MSE:
                0.000514964631292969
       87 MSE:
Epoch
                0.000504525494761765
       88 MSE:
                0.000495183456223458
Epoch
```

```
Epoch 89 MSE: 0.0004859785840380937
Epoch 90 MSE: 0.00047710436047054827
Epoch 91 MSE: 0.0004673246876336634
Epoch 92 MSE:
               0.00045680641778744757
Epoch 93 MSE:
               0.00044643765431828797
Epoch 94 MSE:
               0.0004360149323474616
Epoch 95 MSE:
               0.0004263759474270046
Epoch 96 MSE:
               0.00041772486292757094
Epoch 97 MSE: 0.00040944688953459263
Epoch 98 MSE:
               0.00040168905979953706
Epoch 99 MSE:
               0.0003938573063351214
```

T-time: 8.240160703659058

Train Score: 0.59 RMSE

Validation Score: 13.14 RMSE

Time Step = 30 | Hidden States = 4 | Num Layers = 1

```
Epoch 0 MSE: 0.04768358916044235
Epoch 1 MSE: 0.04032931476831436
Epoch 2 MSE: 0.03539516404271126
Epoch 3 MSE: 0.03230658173561096
Epoch 4 MSE: 0.030488386750221252
Epoch 5 MSE: 0.029353486374020576
Epoch 6 MSE: 0.028284458443522453
Epoch 7 MSE: 0.02681155502796173
Epoch 8 MSE: 0.02471536211669445
Epoch 9 MSE: 0.021992499008774757
Epoch 10 MSE: 0.018793504685163498
Epoch 11 MSE: 0.015380756929516792
Epoch 12 MSE: 0.012096523307263851
Epoch 13 MSE: 0.009302636608481407
Epoch 14 MSE: 0.007247005123645067
Epoch 15 MSE:
               0.0058562736958265305
Epoch 16 MSE:
               0.0047002024948596954
Epoch 17 MSE:
               0.003452395088970661
Epoch 18 MSE:
               0.0023222363088279963
Epoch 19 MSE:
               0.0018869355553761125
Epoch 20 MSE:
               0.0024983964394778013
Epoch 21 MSE:
               0.0037401968147605658
Epoch 22 MSE:
               0.004705153405666351
Epoch 23 MSE:
               0.0048709437251091
Epoch 24 MSE: 0.004348276648670435
```

```
Epoch
       25 MSE:
                0.00355468038469553
Epoch
       26 MSE:
                0.0028616113122552633
Epoch
       27 MSE:
                0.0024030141066759825
       28 MSE:
Epoch
                0.002096304204314947
Epoch
       29 MSE:
                0.0018178171012550592
Epoch
       30 MSE:
                0.001538876909762621
Epoch
       31 MSE:
                0.0013157770736142993
Epoch
       32 MSE:
                0.001211556838825345
       33 MSE:
Epoch
                0.0012428341433405876
Epoch
       34 MSE:
                0.0013726343167945743
       35 MSE:
                0.0015327882720157504
Epoch
       36 MSE:
Epoch
                0.0016548993298783898
Epoch
       37 MSE:
                0.001694605452939868
Epoch
       38 MSE:
                0.0016417906153947115
Epoch
       39 MSE:
                0.0015167758101597428
Epoch
      40 MSE:
                0.001357093802653253
Epoch
       41 MSE:
                0.0012010388309136033
       42 MSE:
Epoch
                0.001073990948498249
Epoch
       43 MSE:
                0.000982323894277215
Epoch
       44 MSE:
                0.0009170204866677523
Epoch
       45 MSE:
                0.0008645985508337617
       46 MSE:
Epoch
                0.0008184402831830084
Epoch 47 MSE:
                0.0007829301757737994
       48 MSE:
Epoch
                0.0007677828543819487
       49 MSE:
                0.0007773470133543015
Epoch
Epoch
       50 MSE:
                0.0008034452912397683
       51 MSE:
Epoch
                0.0008275149157270789
Epoch
       52 MSE:
                0.0008305917144753039
       53 MSE:
Epoch
                0.0008039528038352728
Epoch
       54 MSE:
                0.0007532594026997685
      55 MSE:
Epoch
                0.0006941388128325343
Epoch
       56 MSE:
                0.0006429271888919175
       57 MSE:
Epoch
                0.0006087152869440615
       58 MSE:
                0.0005910219042561948
Epoch
Epoch
       59 MSE:
                0.0005832096794620156
Epoch
       60 MSE:
                0.0005781917134299874
Epoch
       61 MSE:
                0.0005723327631130815
Epoch
       62 MSE:
                0.0005656683933921158
       63 MSE:
Epoch
                0.0005594874965026975
Epoch
       64 MSE:
                0.0005537805845960975
       65 MSE:
                0.0005465205758810043
Epoch
       66 MSE:
Epoch
                0.0005350173451006413
Epoch
       67 MSE:
                0.0005180928856134415
Epoch
       68 MSE:
                0.0004973631585016847
Epoch
       69 MSE:
                0.00047666492173448205
Epoch
       70 MSE:
                0.0004599762614816427
Epoch
       71 MSE:
                0.00044922379311174154
       72 MSE:
                0.0004434347210917622
Epoch
```

```
Epoch 73 MSE:
               0.00043972901767119765
Epoch 74 MSE:
               0.00043531920528039336
Epoch 75 MSE:
               0.00042901127017103136
Epoch 76 MSE:
               0.00042124351602979004
Epoch 77 MSE:
               0.00041297596180811524
Epoch 78 MSE:
               0.0004046024405397475
Epoch 79 MSE:
               0.00039579978329129517
Epoch 80 MSE:
               0.0003862298035528511
Epoch 81 MSE:
               0.0003762508858926594
Epoch 82 MSE:
               0.00036690745037049055
Epoch 83 MSE:
               0.00035921050584875047
Epoch 84 MSE:
               0.0003533698327373713
Epoch 85 MSE:
               0.0003486369678284973
Epoch 86 MSE:
               0.0003438586136326194
Epoch 87 MSE:
               0.000338249170454219
Epoch 88 MSE:
               0.0003317746741231531
Epoch 89 MSE:
               0.00032493588514626026
Epoch 90 MSE:
               0.00031824735924601555
Epoch 91 MSE:
               0.00031189253786578774
Epoch 92 MSE:
               0.0003057824505958706
Epoch 93 MSE:
               0.00029984748107381165
Epoch 94 MSE:
               0.00029421329963952303
Epoch 95 MSE:
               0.00028908310923725367
Epoch 96 MSE:
               0.0002844745758920908
Epoch 97 MSE:
               0.00028010824462398887
Epoch 98 MSE:
               0.000275581784080714
Epoch 99 MSE:
               0.00027067199698649347
```

T-time: 7.86789608001709

Train Score: 0.49 RMSE

Validation Score: 10.05 RMSE

_____ Time Step = 30 | Hidden States = 4 | Num Layers = 2

Epoch 0 MSE: 0.3315909206867218 Epoch 1 MSE: 0.28969618678092957 Epoch 2 MSE: 0.25227662920951843 Epoch 3 MSE: 0.2190193086862564 Epoch 4 MSE: 0.18934200704097748 Epoch 5 MSE: 0.16263273358345032 Epoch 6 MSE: 0.13833776116371155 Epoch 7 MSE: 0.11604934930801392 Epoch 8 MSE: 0.09554965049028397

```
Epoch 9 MSE:
               0.07685249298810959
Epoch
       10 MSE:
                0.0602487251162529
Epoch
       11 MSE:
                0.04632691293954849
       12 MSE:
Epoch
                0.03593353182077408
Epoch
       13 MSE:
                0.030014272779226303
Epoch
       14 MSE:
                0.02921491675078869
Epoch
       15 MSE:
                0.03308423236012459
Epoch 16 MSE:
                0.03927772492170334
Epoch 17 MSE:
                0.044544901698827744
Epoch
       18 MSE:
                0.046947821974754333
       19 MSE:
Epoch
                0.04635532572865486
      20 MSE:
Epoch
                0.043640799820423126
Epoch
      21 MSE:
                0.039933301508426666
Epoch
       22 MSE:
                0.03619994595646858
Epoch
      23 MSE:
                0.03307488188147545
Epoch 24 MSE:
                0.030846115201711655
Epoch
      25 MSE:
                0.029531115666031837
      26 MSE:
                0.028981784358620644
Epoch
Epoch
      27 MSE:
                0.02897823043167591
Epoch
       28 MSE:
                0.02929363027215004
Epoch
       29 MSE:
                0.029730241745710373
      30 MSE:
Epoch
                0.030134323984384537
Epoch 31 MSE:
                0.030398540198802948
       32 MSE:
Epoch
                0.030458081513643265
Epoch
      33 MSE:
                0.03028438240289688
Epoch
       34 MSE:
                0.029878191649913788
      35 MSE:
Epoch
                0.02926301769912243
Epoch
       36 MSE:
                0.02847890369594097
      37 MSE:
Epoch
                0.02757660672068596
Epoch 38 MSE:
                0.02661190554499626
      39 MSE:
Epoch
                0.02563980594277382
Epoch
       40 MSE:
                0.024708623066544533
Epoch
      41 MSE:
                0.02385401725769043
Epoch
      42 MSE:
                0.023093514144420624
Epoch
       43 MSE:
                0.02242247574031353
Epoch
      44 MSE:
                0.021812841296195984
Epoch
      45 MSE:
                0.02121611125767231
Epoch
      46 MSE:
                0.020571328699588776
      47 MSE:
Epoch
                0.019817564636468887
      48 MSE:
Epoch
                0.018908360973000526
Epoch 49 MSE:
                0.01782393455505371
Epoch
       50 MSE:
                0.016576804220676422
Epoch
       51 MSE:
                0.015208461321890354
Epoch
       52 MSE:
                0.013777991756796837
Epoch
      53 MSE:
                0.01234647911041975
Epoch
       54 MSE:
                0.010962605476379395
Epoch
       55 MSE:
                0.009653990156948566
       56 MSE:
                0.008426513522863388
Epoch
```

```
Epoch 57 MSE:
                0.007271153386682272
Epoch 58 MSE:
                0.00617600092664361
Epoch 59 MSE:
                0.005139636807143688
Epoch 60 MSE:
                0.004181316588073969
Epoch 61 MSE:
                0.0033432231284677982
Epoch 62 MSE:
                0.002681861398741603
Epoch
      63 MSE:
                0.002249526558443904
Epoch 64 MSE:
                0.0020713743288069963
Epoch 65 MSE:
                0.002126856241375208
Epoch 66 MSE:
                0.002345130080357194
Epoch 67 MSE:
                0.002622263738885522
Epoch 68 MSE:
                0.0028575188480317593
Epoch 69 MSE:
                0.0029873454477638006
Epoch 70 MSE:
                0.002994094742462039
Epoch 71 MSE:
                0.0028911568224430084
Epoch 72 MSE:
                0.002704416401684284
Epoch 73 MSE:
                0.002462470205500722
Epoch 74 MSE:
                0.0021939200814813375
Epoch 75 MSE:
                0.0019258251413702965
Epoch 76 MSE:
                0.0016809216467663646
Epoch 77 MSE:
                0.0014752080896869302
Epoch 78 MSE:
                0.001317396992817521
Epoch 79 MSE:
                0.0012097555445507169
Epoch 80 MSE:
                0.001149256364442408
Epoch 81 MSE:
                0.0011285949731245637
Epoch 82 MSE:
                0.0011372918961569667
Epoch 83 MSE:
                0.0011631760280579329
Epoch 84 MSE:
                0.0011942230630666018
Epoch 85 MSE:
                0.00122037751134485
Epoch 86 MSE:
                0.0012348388554528356
Epoch 87 MSE:
                0.0012344642309471965
Epoch 88 MSE:
                0.0012192772701382637
Epoch 89 MSE:
                0.0011914059286937118
Epoch 90 MSE:
                0.0011539425468072295
Epoch
      91 MSE:
                0.0011101117124781013
Epoch 92 MSE:
                0.0010629200842231512
Epoch 93 MSE:
                0.0010151645401492715
Epoch 94 MSE:
                0.0009695594781078398
Epoch 95 MSE:
                0.0009287098655477166
Epoch 96 MSE:
                0.000894845521543175
Epoch 97 MSE:
                0.0008693881682120264
Epoch 98 MSE:
                0.0008525796583853662
Epoch 99 MSE:
                0.000843378365971148
T-time: 14.687498569488525
```

Train Score: 0.87 RMSE

Validation Score: 15.07 RMSE

Time Step = 30 | Hidden States = 8 | Num Layers = 1

Epoch 0 MSE: 0.05830710008740425 Epoch 1 MSE: 0.04319801181554794 Epoch 2 MSE: 0.03298809751868248 Epoch 3 MSE: 0.027621813118457794 Epoch 4 MSE: 0.02664072997868061 Epoch 5 MSE: 0.028489967808127403 Epoch 6 MSE: 0.03042115457355976 Epoch 7 MSE: 0.030652599409222603 Epoch 8 MSE: 0.02918129228055477 Epoch 9 MSE: 0.026789866387844086 Epoch 10 MSE: 0.02427689917385578 Epoch 11 MSE: 0.022168666124343872 Epoch 12 MSE: 0.020675277337431908 Epoch 13 MSE: 0.019750501960515976 Epoch 14 MSE: 0.019184933975338936 Epoch 15 MSE: 0.018699269741773605 Epoch 16 MSE: 0.018023833632469177 Epoch 17 MSE: 0.016958730295300484 Epoch 18 MSE: 0.015411796048283577 Epoch 19 MSE: 0.013413450680673122 Epoch 20 MSE: 0.011110161431133747 Epoch 21 MSE: 0.008738277480006218 Epoch 22 MSE: 0.006574634928256273 Epoch 23 MSE: 0.004851405508816242 Epoch 24 MSE: 0.0036309717688709497 Epoch 25 MSE: 0.002727038459852338 Epoch 26 MSE: 0.0018949871882796288 Epoch 27 MSE: 0.0012286227429285645 Epoch 28 MSE: 0.0011715007713064551 Epoch 29 MSE: 0.0019882519263774157 Epoch 30 MSE: 0.003120464039966464 Epoch 31 MSE: 0.0035563751589506865 Epoch 32 MSE: 0.0029258837457746267 Epoch 33 MSE: 0.0016933819279074669 Epoch 34 MSE: 0.0006076114950701594 Epoch 35 MSE: 0.0001712307275738567 Epoch 36 MSE: 0.00038035493344068527 Epoch 37 MSE: 0.0008281996706500649 Epoch 38 MSE: 0.001097658067010343 Epoch 39 MSE: 0.001068838289938867 Epoch 40 MSE: 0.0008871317259036005

```
Epoch 41 MSE:
                0.0007472841534763575
Epoch
       42 MSE:
                0.0007358352304436266
       43 MSE:
Epoch
                0.0008078821701928973
       44 MSE:
Epoch
                0.0008529640035703778
Epoch
       45 MSE:
                0.0007814120035618544
Epoch
       46 MSE:
                0.0005823375540785491
Epoch
       47 MSE:
                0.00033112018718384206
Epoch
       48 MSE:
                0.0001460440835217014
Epoch 49 MSE:
                0.00011262156476732343
Epoch
      50 MSE:
                0.00021734654728788882
       51 MSE:
                0.0003498413134366274
Epoch
Epoch
       52 MSE:
                0.0003953797568101436
Epoch
       53 MSE:
                0.0003365898737683892
Epoch
       54 MSE:
                0.00025048901443369687
Epoch
      55 MSE:
                0.00021330371964722872
Epoch 56 MSE:
                0.0002300985506735742
Epoch
      57 MSE:
                0.00025075156008824706
       58 MSE:
Epoch
                0.00023112430062610656
Epoch
       59 MSE:
                0.00017255335114896297
Epoch
       60 MSE:
                0.00011382836237316951
Epoch
       61 MSE:
                9.392945503350347e-05
Epoch
       62 MSE:
                0.00011975511733908206
Epoch
       63 MSE:
                0.00016325755859725177
       64 MSE:
Epoch
                0.00018736998026724905
Epoch
       65 MSE:
                0.00017625004693400115
Epoch
       66 MSE:
                0.0001436006132280454
       67 MSE:
Epoch
                0.00011548212933121249
Epoch
       68 MSE:
                0.00010695721721276641
       69 MSE:
Epoch
                0.00011299804464215413
Epoch
      70 MSE:
                0.00011777529289247468
Epoch 71 MSE:
                0.00011089642066508532
Epoch
      72 MSE:
                9.601886267773807e-05
Epoch
      73 MSE:
                8.573175000492483e-05
      74 MSE:
                8.854078623699024e-05
Epoch
Epoch
       75 MSE:
                0.00010042238136520609
Epoch
       76 MSE:
                0.00010900451161433011
Epoch
      77 MSE:
                0.00010582134564174339
Epoch
      78 MSE:
                9.37376607907936e-05
      79 MSE:
Epoch
                8.258123853011057e-05
Epoch
       80 MSE:
                7.910842396086082e-05
       81 MSE:
                8.196032285923138e-05
Epoch
       82 MSE:
Epoch
                8.506155427312478e-05
Epoch
       83 MSE:
                8.427391003351659e-05
Epoch
       84 MSE:
                8.059835090534762e-05
Epoch
       85 MSE:
                7.792432006681338e-05
Epoch
       86 MSE:
                7.852623821236193e-05
Epoch
       87 MSE:
                8.089409675449133e-05
       88 MSE:
Epoch
                8.163245365722105e-05
```

Epoch 89 MSE: 7.906415703473613e-05
Epoch 90 MSE: 7.476947212126106e-05
Epoch 91 MSE: 7.176354120019823e-05
Epoch 92 MSE: 7.152914622565731e-05
Epoch 93 MSE: 7.294148963410407e-05
Epoch 94 MSE: 7.380501483567059e-05
Epoch 95 MSE: 7.308138447115198e-05
Epoch 96 MSE: 7.155525963753462e-05
Epoch 97 MSE: 7.0587957452517e-05
Epoch 98 MSE: 7.05539423506707e-05
Epoch 99 MSE: 7.062112126732245e-05

T-time: 6.5735087394714355

Train Score: 0.25 RMSE

-----Validation Score: 5.80 RMSE

Time Step = 30 | Hidden States = 8 | Num Layers = 2

Epoch 0 MSE: 0.1300494223833084 Epoch 1 MSE: 0.09953387081623077 Epoch 2 MSE: 0.07576581835746765 Epoch 3 MSE: 0.057945769280195236 Epoch 4 MSE: 0.04546254500746727 Epoch 5 MSE: 0.03796081990003586 Epoch 6 MSE: 0.0351751372218132 Epoch 7 MSE: 0.036429472267627716 Epoch 8 MSE: 0.03985827788710594 Epoch 9 MSE: 0.04278193786740303 Epoch 10 MSE: 0.0436619408428669 Epoch 11 MSE: 0.04255641624331474 Epoch 12 MSE: 0.04026862233877182 Epoch 13 MSE: 0.03766671195626259 Epoch 14 MSE: 0.035382479429244995 Epoch 15 MSE: 0.03373955190181732 Epoch 16 MSE: 0.032797280699014664 Epoch 17 MSE: 0.032437391579151154 Epoch 18 MSE: 0.032448574900627136 Epoch 19 MSE: 0.03258895501494408 Epoch 20 MSE: 0.032627690583467484 Epoch 21 MSE: 0.03237408772110939 Epoch 22 MSE: 0.03169442340731621 Epoch 23 MSE: 0.030512342229485512 Epoch 24 MSE: 0.028797175735235214

```
Epoch 25 MSE:
                0.026554090902209282
Epoch
      26 MSE:
                0.023837115615606308
Epoch
      27 MSE:
                0.020796095952391624
      28 MSE:
Epoch
                0.0177303459495306
Epoch
      29 MSE:
                0.014974850229918957
Epoch
      30 MSE:
                0.012396407313644886
Epoch
       31 MSE:
                0.009321870282292366
Epoch
      32 MSE:
                0.005870421417057514
Epoch 33 MSE:
                0.004070761147886515
Epoch
      34 MSE:
                0.005253431387245655
Epoch
      35 MSE:
                0.007208575028926134
      36 MSE:
Epoch
                0.0077842650935053825
Epoch
      37 MSE:
                0.007167050614953041
Epoch
       38 MSE:
                0.006029353942722082
Epoch
      39 MSE:
                0.004854240920394659
                0.004056863021105528
Epoch 40 MSE:
Epoch 41 MSE:
                0.003737029852345586
      42 MSE:
Epoch
                0.0035468998830765486
Epoch
       43 MSE:
                0.00327903195284307
Epoch
      44 MSE:
                0.003115979256108403
Epoch
       45 MSE:
                0.0031828295905143023
Epoch 46 MSE:
                0.003396661253646016
Epoch 47 MSE:
                0.0036187663208693266
Epoch 48 MSE:
                0.0037005252670496702
Epoch 49 MSE:
                0.003563558217138052
Epoch 50 MSE:
                0.00323143950663507
Epoch 51 MSE:
                0.00280407490208745
Epoch
       52 MSE:
                0.002407819963991642
      53 MSE:
Epoch
                0.0021407180465757847
Epoch 54 MSE:
                0.002030876697972417
Epoch 55 MSE:
                0.0020304254721850157
Epoch
      56 MSE:
                0.002047371817752719
Epoch 57 MSE:
                0.002005287678912282
Epoch 58 MSE:
                0.001887033460661769
Epoch
       59 MSE:
                0.001726918970234692
Epoch
       60 MSE:
                0.0015691373264417052
Epoch
       61 MSE:
                0.0014344076626002789
Epoch
       62 MSE:
                0.0013182924594730139
       63 MSE:
Epoch
                0.001212786533869803
Epoch
       64 MSE:
                0.0011240056483075023
Epoch 65 MSE:
                0.00106747483368963
Epoch
       66 MSE:
                0.0010473327711224556
Epoch
       67 MSE:
                0.0010421492625027895
       68 MSE:
Epoch
                0.0010153399780392647
Epoch
      69 MSE:
                0.0009448613272979856
Epoch
      70 MSE:
                0.0008440824458375573
Epoch
      71 MSE:
                0.0007511386647820473
      72 MSE:
                0.0006963096675463021
Epoch
```

```
Epoch 73 MSE:
               0.0006787938182242215
Epoch 74 MSE:
               0.000672296853736043
Epoch 75 MSE:
               0.0006503849872387946
Epoch 76 MSE:
               0.0006069624796509743
Epoch 77 MSE:
               0.0005555611569434404
Epoch 78 MSE:
               0.0005118214758113027
Epoch 79 MSE:
               0.0004782472678925842
Epoch 80 MSE:
               0.0004464737721718848
Epoch 81 MSE:
               0.0004119609948247671
Epoch 82 MSE:
               0.00038102411781437695
Epoch 83 MSE:
               0.00036125080077908933
Epoch 84 MSE:
               0.0003493304247967899
Epoch 85 MSE:
               0.0003330550971440971
Epoch 86 MSE:
               0.00030511137447319925
Epoch 87 MSE:
               0.00027184654027223587
Epoch 88 MSE:
               0.00024648834369145334
Epoch 89 MSE:
               0.00023436792253050953
Epoch 90 MSE:
               0.0002276333252666518
Epoch 91 MSE:
               0.00021590496180579066
Epoch 92 MSE:
               0.0001983940601348877
Epoch 93 MSE:
               0.00018163725326303393
Epoch 94 MSE:
               0.00016873845015652478
Epoch 95 MSE:
               0.00015682469529565424
Epoch 96 MSE:
               0.0001442001957911998
Epoch 97 MSE:
               0.00013384973863139749
Epoch 98 MSE:
               0.00012754503404721618
Epoch 99 MSE:
               0.00012116150901420042
```

T-time: 11.877559900283813

Train Score: 0.33 RMSE

------Validation Score: 12.10 RMSE

Time Step = 30 | Hidden States = 16 | Num Layers = 1

Epoch 0 MSE: 0.03280074521899223
Epoch 1 MSE: 0.030688747763633728
Epoch 2 MSE: 0.0282236114144432526
Epoch 3 MSE: 0.025945521891117096
Epoch 4 MSE: 0.023057380691170692
Epoch 5 MSE: 0.020216742530465126
Epoch 6 MSE: 0.016408327966928482
Epoch 7 MSE: 0.011782833375036716
Epoch 8 MSE: 0.0068675195798277855

```
Epoch
      9 MSE:
               0.00167743896599859
Epoch
       10 MSE:
                0.0012243869714438915
       11 MSE:
Epoch
                0.009534423239529133
       12 MSE:
Epoch
                0.005961210932582617
Epoch
       13 MSE:
                0.0036349850706756115
Epoch
       14 MSE:
                0.000371886562788859
Epoch
       15 MSE:
                0.0006170365959405899
Epoch
       16 MSE:
                0.0015756768407300115
Epoch 17 MSE:
                0.0017671105451881886
Epoch
       18 MSE:
                0.0019920116756111383
       19 MSE:
                0.0025295407976955175
Epoch
       20 MSE:
Epoch
                0.0027896156534552574
Epoch
       21 MSE:
                0.002443931996822357
Epoch
       22 MSE:
                0.001866919337771833
Epoch
       23 MSE:
                0.001481905928812921
Epoch 24 MSE:
                0.0012076423736289144
Epoch
       25 MSE:
                0.0007517654448747635
       26 MSE:
Epoch
                0.00023919958039186895
Epoch
       27 MSE:
                0.00010877213208004832
Epoch
       28 MSE:
                0.0003461726591922343
       29 MSE:
Epoch
                0.0004942378727719188
       30 MSE:
Epoch
                0.0005734095466323197
Epoch
       31 MSE:
                0.0007965457625687122
       32 MSE:
Epoch
                0.0008422203827649355
Epoch
       33 MSE:
                0.0005706222145818174
Epoch
       34 MSE:
                0.00033739974605850875
       35 MSE:
Epoch
                0.00025112341972999275
Epoch
       36 MSE:
                0.00014808526611886919
       37 MSE:
Epoch
                6.950321403564885e-05
Epoch
      38 MSE:
                0.00012719356163870543
       39 MSE:
Epoch
                0.00024090603983495384
Epoch
       40 MSE:
                0.00028710748301818967
                0.00028150028083473444
Epoch
       41 MSE:
       42 MSE:
                0.00028913296409882605
Epoch
Epoch
       43 MSE:
                0.00028784488677047193
Epoch
       44 MSE:
                0.00022641062969341874
Epoch
       45 MSE:
                0.00013911040150560439
Epoch
       46 MSE:
                9.39742021728307e-05
       47 MSE:
Epoch
                8.34099409985356e-05
Epoch
       48 MSE:
                6.718535587424412e-05
Epoch 49 MSE:
                6.499709706986323e-05
       50 MSE:
Epoch
                0.00010230411862721667
Epoch
       51 MSE:
                0.00013571100134868175
Epoch
       52 MSE:
                0.00013091351138427854
Epoch
       53 MSE:
                0.00011768293188652024
Epoch
       54 MSE:
                0.00010897273750742897
Epoch
       55 MSE:
                8.383749809581786e-05
       56 MSE:
                5.4140622523846105e-05
Epoch
```

```
Epoch 57 MSE:
               4.7611494665034115e-05
Epoch 58 MSE:
               5.5066626373445615e-05
Epoch 59 MSE:
               5.7906327128876e-05
Epoch 60 MSE:
                6.282963295234367e-05
Epoch 61 MSE:
                7.417233427986503e-05
Epoch 62 MSE:
                7.768218347337097e-05
Epoch
      63 MSE:
                6.891259545227513e-05
Epoch 64 MSE:
                6.0271639085840434e-05
Epoch 65 MSE:
                5.523308936972171e-05
Epoch 66 MSE:
                4.7454243031097576e-05
Epoch 67 MSE:
                4.116450509172864e-05
Epoch 68 MSE:
                4.3529129470698535e-05
Epoch 69 MSE:
                4.8518184485146776e-05
Epoch 70 MSE:
                4.992575486539863e-05
Epoch 71 MSE:
                5.144866372575052e-05
Epoch 72 MSE:
                5.298330506775528e-05
Epoch 73 MSE:
                4.970190275344066e-05
Epoch 74 MSE:
                4.459008414414711e-05
Epoch 75 MSE:
                4.248643745086156e-05
Epoch 76 MSE:
                4.134280243306421e-05
Epoch 77 MSE:
                4.010135307908058e-05
Epoch 78 MSE:
                4.1322065953863785e-05
Epoch 79 MSE:
                4.3666703277267516e-05
Epoch 80 MSE:
                4.402926788316108e-05
Epoch 81 MSE:
                4.34601133747492e-05
Epoch 82 MSE:
                4.3149455450475216e-05
Epoch 83 MSE:
                4.173212801106274e-05
Epoch 84 MSE:
                3.9766284317011014e-05
Epoch 85 MSE:
                3.921073584933765e-05
Epoch 86 MSE:
                3.940981696359813e-05
Epoch 87 MSE:
                3.9392340113408864e-05
Epoch 88 MSE:
                3.992976053268649e-05
Epoch 89 MSE:
                4.0627928683534265e-05
Epoch 90 MSE:
                4.034208905068226e-05
Epoch 91 MSE:
                3.9702073991065845e-05
Epoch 92 MSE:
                3.9311791624641046e-05
Epoch 93 MSE:
                3.868888597935438e-05
Epoch 94 MSE:
                3.8179427065188065e-05
Epoch 95 MSE:
                3.831719732261263e-05
Epoch 96 MSE:
                3.8530455640284345e-05
Epoch 97 MSE:
               3.854845272144303e-05
Epoch 98 MSE:
                3.86751999030821e-05
Epoch 99 MSE:
                3.8631678762612864e-05
T-time: 12.761028528213501
```

Train Score: 0.19 RMSE

Time Step = 30 | Hidden States = 16 | Num Layers = 2

Epoch 0 MSE: 0.055677399039268494 Epoch 1 MSE: 0.040503811091184616 Epoch 2 MSE: 0.03618287295103073 Epoch 3 MSE: 0.03912533447146416 Epoch 4 MSE: 0.03800801560282707 Epoch 5 MSE: 0.0355929397046566 Epoch 6 MSE: 0.03420901671051979 Epoch 7 MSE: 0.033764105290174484 Epoch 8 MSE: 0.03366672620177269 Epoch 9 MSE: 0.03346261382102966 Epoch 10 MSE: 0.03288586810231209 Epoch 11 MSE: 0.031801071017980576 Epoch 12 MSE: 0.030145179480314255 Epoch 13 MSE: 0.027899902313947678 Epoch 14 MSE: 0.02511209435760975 Epoch 15 MSE: 0.021848421543836594 Epoch 16 MSE: 0.017792847007513046 Epoch 17 MSE: 0.01196269504725933 Epoch 18 MSE: 0.004973718896508217 Epoch 19 MSE: 0.0016540931537747383 Epoch 20 MSE: 0.0049809678457677364 Epoch 21 MSE: 0.008692225441336632 Epoch 22 MSE: 0.008817782625555992 Epoch 23 MSE: 0.006266159936785698 Epoch 24 MSE: 0.0033147712238132954 Epoch 25 MSE: 0.0016409946838393807 Epoch 26 MSE: 0.001533445087261498 Epoch 27 MSE: 0.002230450976639986 Epoch 28 MSE: 0.0029366740491241217 Epoch 29 MSE: 0.003370483871549368 Epoch 30 MSE: 0.003472281387075782 Epoch 31 MSE: 0.0031549991108477116 Epoch 32 MSE: 0.0024629198014736176 Epoch 33 MSE: 0.0016888439422473311 Epoch 34 MSE: 0.0012349814642220736 Epoch 35 MSE: 0.0012144397478550673 Epoch 36 MSE: 0.0013073538430035114 Epoch 37 MSE: 0.0013889052206650376 Epoch 38 MSE: 0.0016057435423135757 Epoch 39 MSE: 0.0017785397358238697 Epoch 40 MSE: 0.0016250221524387598

```
Epoch 41 MSE:
                0.001265931990928948
Epoch
      42 MSE:
                0.0009930352680385113
      43 MSE:
Epoch
                0.0008105839369818568
       44 MSE:
Epoch
                0.0006444983300752938
Epoch
       45 MSE:
                0.000617695041000843
Epoch
      46 MSE:
                0.000749667757190764
Epoch
       47 MSE:
                0.0008564441814087331
Epoch
      48 MSE:
                0.0008264322532340884
Epoch 49 MSE:
                0.0007106576813384891
Epoch
      50 MSE:
                0.0005649556987918913
      51 MSE:
                0.0003955152933485806
Epoch
Epoch
      52 MSE:
                0.0002761985524557531
Epoch
      53 MSE:
                0.00028132234001532197
Epoch
       54 MSE:
                0.0003392184153199196
Epoch 55 MSE:
                0.000359881145413965
                0.00033746351255103946
Epoch 56 MSE:
Epoch 57 MSE:
                0.0002538826083764434
      58 MSE:
                0.0001430270349374041
Epoch
Epoch
       59 MSE:
                9.947580110747367e-05
Epoch
       60 MSE:
                0.00012158887693658471
Epoch
       61 MSE:
                0.0001715253893053159
Epoch
       62 MSE:
                0.00019678282842505723
Epoch
      63 MSE:
                0.0001476809848099947
       64 MSE:
Epoch
                8.280356996692717e-05
       65 MSE:
                5.92003452766221e-05
Epoch
Epoch
       66 MSE:
                8.276724111055955e-05
       67 MSE:
Epoch
                0.00012398183753248304
Epoch
       68 MSE:
                0.0001228511391673237
      69 MSE:
Epoch
                9.368485189042985e-05
Epoch 70 MSE:
                5.957946632406674e-05
Epoch 71 MSE:
                6.0087553720222786e-05
Epoch 72 MSE:
                8.660316962050274e-05
Epoch
      73 MSE:
                9.70651744864881e-05
      74 MSE:
Epoch
                8.488124149153009e-05
Epoch
      75 MSE:
                5.843230610480532e-05
Epoch
      76 MSE:
                5.572663576458581e-05
Epoch
     77 MSE:
                6.661871884716675e-05
Epoch 78 MSE:
                7.614732021465898e-05
      79 MSE:
Epoch
                7.016583549557254e-05
Epoch
      80 MSE:
                5.424419941846281e-05
      81 MSE:
Epoch
                4.963499304722063e-05
Epoch
       82 MSE:
                5.329150371835567e-05
Epoch
       83 MSE:
                6.1557482695207e-05
Epoch
       84 MSE:
                5.824673280585557e-05
Epoch
      85 MSE:
                4.9865957407746464e-05
Epoch
       86 MSE:
                4.536324559012428e-05
Epoch
       87 MSE:
                4.7456756874453276e-05
       88 MSE:
Epoch
                5.256841177470051e-05
```

Epoch 89 MSE: 5.1165978220524266e-05
Epoch 90 MSE: 4.707567495643161e-05
Epoch 91 MSE: 4.3243861000519246e-05
Epoch 92 MSE: 4.465473466552794e-05
Epoch 93 MSE: 4.7454908781219274e-05
Epoch 94 MSE: 4.737619019579142e-05
Epoch 95 MSE: 4.484019518713467e-05
Epoch 96 MSE: 4.232069477438927e-05
Epoch 97 MSE: 4.317292768973857e-05
Epoch 98 MSE: 4.456492024473846e-05
Epoch 99 MSE: 4.4821561459684744e-05

T-time: 26.2824227809906

Train Score: 0.20 RMSE

Validation Score: 5.29 RMSE

Time Step = 30 | Hidden States = 32 | Num Layers = 1

Epoch 0 MSE: 0.05470864847302437 Epoch 1 MSE: 0.036521151661872864 Epoch 2 MSE: 0.0323270820081234 Epoch 3 MSE: 0.03476791828870773 Epoch 4 MSE: 0.03283500298857689 Epoch 5 MSE: 0.02830059453845024 Epoch 6 MSE: 0.0245965588837862 Epoch 7 MSE: 0.02229919843375683 Epoch 8 MSE: 0.020366504788398743 Epoch 9 MSE: 0.017207302153110504 Epoch 10 MSE: 0.011177390813827515 Epoch 11 MSE: 0.002853731159120798 Epoch 12 MSE: 0.01857912354171276 Epoch 13 MSE: 0.002731408691033721 Epoch 14 MSE: 0.0025078372564166784 Epoch 15 MSE: 0.007131141144782305 Epoch 16 MSE: 0.008809547871351242 Epoch 17 MSE: 0.007310802582651377 Epoch 18 MSE: 0.0042012473568320274 Epoch 19 MSE: 0.0015075996052473783 Epoch 20 MSE: 0.00108303630258888 Epoch 21 MSE: 0.003040881594642997 Epoch 22 MSE: 0.004525488708168268 Epoch 23 MSE: 0.0033464115113019943 Epoch 24 MSE: 0.0011872209142893553

```
Epoch
       25 MSE:
                0.0002509352925699204
Epoch
       26 MSE:
                0.0007829103851690888
Epoch
       27 MSE:
                0.0017963368445634842
       28 MSE:
Epoch
                0.0023104152642190456
Epoch
       29 MSE:
                0.0019738844130188227
Epoch
       30 MSE:
                0.0011101920390501618
Epoch
       31 MSE:
                0.0003889810177497566
Epoch
       32 MSE:
                0.0003182347572874278
       33 MSE:
Epoch
                0.0008075948571786284
Epoch
       34 MSE:
                0.001228843117132783
       35 MSE:
                0.0011098356917500496
Epoch
       36 MSE:
Epoch
                0.0006317998631857336
Epoch
       37 MSE:
                0.0002763795491773635
Epoch
       38 MSE:
                0.0002739683259278536
Epoch
       39 MSE:
                0.0005055696237832308
Epoch
       40 MSE:
                0.000719877309165895
Epoch
       41 MSE:
                0.0007443659123964608
       42 MSE:
Epoch
                0.0005712505080737174
Epoch
       43 MSE:
                0.00033099157735705376
Epoch
       44 MSE:
                0.00019156307098455727
Epoch
       45 MSE:
                0.00023239065194502473
       46 MSE:
Epoch
                0.0003758188395295292
Epoch
       47 MSE:
                0.00045825494453310966
       48 MSE:
Epoch
                0.00039614835986867547
       49 MSE:
                0.00026106322184205055
Epoch
       50 MSE:
Epoch
                0.00017998585826717317
       51 MSE:
Epoch
                0.00020134798251092434
Epoch
       52 MSE:
                0.00027185663930140436
       53 MSE:
Epoch
                0.00030934979440644383
Epoch
       54 MSE:
                0.0002779447822831571
       55 MSE:
Epoch
                0.00020721962209790945
Epoch
       56 MSE:
                0.0001565559214213863
       57 MSE:
Epoch
                0.00016073670121841133
       58 MSE:
                0.0002013572520809248
Epoch
Epoch
       59 MSE:
                0.00022872760018799454
Epoch
       60 MSE:
                0.00021289402502588928
Epoch
       61 MSE:
                0.00017014981131069362
Epoch
       62 MSE:
                0.0001395737926941365
       63 MSE:
Epoch
                0.00014153328083921224
Epoch
       64 MSE:
                0.00016270403284579515
       65 MSE:
                0.0001753073011059314
Epoch
       66 MSE:
Epoch
                0.0001651574275456369
Epoch
       67 MSE:
                0.00014217189163900912
       68 MSE:
Epoch
                0.00012724872794933617
Epoch
       69 MSE:
                0.00013039351324550807
Epoch
       70 MSE:
                0.00014193450624588877
Epoch
       71 MSE:
                0.00014503482088912278
       72 MSE:
Epoch
                0.00013450204278342426
```

```
0.00012048503413097933
Epoch 73 MSE:
Epoch 74 MSE:
               0.00011513882782310247
Epoch 75 MSE:
               0.0001197191231767647
Epoch 76 MSE:
               0.00012542733747977763
Epoch 77 MSE:
               0.000124073339975439
Epoch 78 MSE:
               0.00011604299652390182
Epoch 79 MSE:
               0.00010844051575986668
Epoch 80 MSE:
               0.00010681503772502765
Epoch 81 MSE:
               0.00010962025407934561
Epoch 82 MSE:
               0.00011092679051216692
Epoch 83 MSE:
               0.00010757789277704433
Epoch 84 MSE:
               0.00010223565914202482
Epoch 85 MSE:
               9.938442963175476e-05
Epoch 86 MSE:
               9.996162407333031e-05
Epoch 87 MSE:
               0.00010093436867464334
Epoch 88 MSE:
               9.938366565620527e-05
Epoch 89 MSE:
               9.574959403835237e-05
Epoch 90 MSE:
               9.280792437493801e-05
Epoch 91 MSE:
               9.218666673405096e-05
Epoch 92 MSE:
               9.268477151636034e-05
Epoch 93 MSE:
               9.206966933561489e-05
Epoch 94 MSE:
               8.98023572517559e-05
Epoch 95 MSE:
               8.736984455026686e-05
Epoch 96 MSE:
               8.620377775514498e-05
Epoch 97 MSE:
               8.603101741755381e-05
Epoch 98 MSE:
               8.550818893127143e-05
Epoch 99 MSE:
               8.399422949878499e-05
```

T-time: 32.613932371139526

Train Score: 0.27 RMSE

Validation Score: 6.35 RMSE

_____ Time Step = 30 | Hidden States = 32 | Num Layers = 2 ______

Epoch 0 MSE: 0.04066479206085205 Epoch 1 MSE: 0.04282337427139282 Epoch 2 MSE: 0.03622611612081528 Epoch 3 MSE: 0.03295174241065979 Epoch 4 MSE: 0.032573405653238297 Epoch 5 MSE: 0.030970308929681778 Epoch 6 MSE: 0.02628113515675068 Epoch 7 MSE: 0.019454628229141235 Epoch 8 MSE: 0.014128321781754494

```
Epoch 9 MSE:
               0.008237452246248722
Epoch
       10 MSE:
                0.0007816554279997945
Epoch 11 MSE:
                0.009618021547794342
       12 MSE:
Epoch
                0.0068541052751243114
Epoch
       13 MSE:
                0.0023689197842031717
Epoch
       14 MSE:
                0.0008074096986092627
Epoch
       15 MSE:
                0.0017288925591856241
Epoch 16 MSE:
                0.0033664735965430737
Epoch 17 MSE:
                0.003948204219341278
Epoch
       18 MSE:
                0.0033132373355329037
       19 MSE:
Epoch
                0.002091200789436698
      20 MSE:
Epoch
                0.0012272250605747104
Epoch
      21 MSE:
                0.0008903286652639508
Epoch
      22 MSE:
                0.0008613553363829851
Epoch
      23 MSE:
                0.0014672279357910156
Epoch 24 MSE:
                0.0019035344012081623
Epoch
      25 MSE:
                0.001712633529677987
      26 MSE:
Epoch
                0.0013297213008627295
Epoch
      27 MSE:
                0.0008715148433111608
Epoch
      28 MSE:
                0.000475468608783558
Epoch
       29 MSE:
                0.00047271509538404644
Epoch
      30 MSE:
                0.0007184622809290886
Epoch 31 MSE:
                0.0009349229512736201
      32 MSE:
Epoch
                0.0009985348442569375
Epoch
      33 MSE:
                0.0008878808002918959
Epoch
       34 MSE:
                0.0006474917754530907
      35 MSE:
Epoch
                0.000412375753512606
Epoch
       36 MSE:
                0.00032761870534159243
      37 MSE:
Epoch
                0.0004058636259287596
Epoch 38 MSE:
                0.0005338805494830012
      39 MSE:
Epoch
                0.0005942605785094202
Epoch
       40 MSE:
                0.0005368897691369057
Epoch
      41 MSE:
                0.000394916016375646
      42 MSE:
                0.0002667429798748344
Epoch
Epoch
       43 MSE:
                0.00022818561410531402
Epoch
      44 MSE:
                0.00027062196750193834
Epoch
      45 MSE:
                0.000332094234181568
Epoch
      46 MSE:
                0.00035305367782711983
Epoch 47 MSE:
                0.0003120574401691556
Epoch
      48 MSE:
                0.0002359386853640899
Epoch 49 MSE:
                0.00017592588847037405
       50 MSE:
Epoch
                0.00016472756396979094
Epoch
      51 MSE:
                0.00019344253814779222
Epoch
      52 MSE:
                0.0002239882742287591
Epoch
      53 MSE:
                0.0002221837203251198
Epoch
       54 MSE:
                0.00018617014575283974
Epoch
       55 MSE:
                0.00014425927656702697
       56 MSE:
Epoch
                0.0001252415095223114
```

```
Epoch 57 MSE:
                0.0001341134775429964
Epoch 58 MSE:
                0.00015219670603983104
Epoch 59 MSE:
                0.00015635331510566175
Epoch
      60 MSE:
                0.0001395325525663793
Epoch 61 MSE:
                0.00011437480134190992
Epoch
      62 MSE:
                9.917836723616347e-05
Epoch
      63 MSE:
                0.00010134679905604571
Epoch 64 MSE:
                0.00011165325122419745
Epoch 65 MSE:
                0.00011432361498009413
Epoch 66 MSE:
                0.00010377053695265204
Epoch 67 MSE:
                8.87196947587654e-05
Epoch 68 MSE:
                8.098907710518688e-05
Epoch 69 MSE:
                8.359929051948711e-05
Epoch 70 MSE:
                8.898750820662826e-05
Epoch 71 MSE:
                8.809736027615145e-05
Epoch 72 MSE:
                8.007174619706348e-05
Epoch 73 MSE:
                7.161980465753004e-05
Epoch 74 MSE:
                6.892096280353144e-05
Epoch 75 MSE:
                7.148572331061587e-05
Epoch 76 MSE:
                7.321628072531894e-05
Epoch 77 MSE:
                6.988851964706555e-05
Epoch 78 MSE:
                6.387493340298533e-05
Epoch 79 MSE:
                6.013064557919279e-05
Epoch 80 MSE:
                6.031760494806804e-05
Epoch 81 MSE:
                6.160903285490349e-05
Epoch 82 MSE:
                6.039479558239691e-05
Epoch 83 MSE:
                5.6693548685871065e-05
Epoch 84 MSE:
                5.356086330721155e-05
Epoch 85 MSE:
                5.2929637604393065e-05
Epoch 86 MSE:
                5.362962474464439e-05
Epoch 87 MSE:
                5.312350913300179e-05
Epoch 88 MSE:
                5.079582842881791e-05
Epoch 89 MSE:
                4.851071207667701e-05
Epoch 90 MSE:
                4.77678986499086e-05
Epoch
      91 MSE:
                4.79848422401119e-05
Epoch 92 MSE:
                4.755291956826113e-05
Epoch 93 MSE:
                4.596020880853757e-05
Epoch 94 MSE:
                4.435632945387624e-05
Epoch 95 MSE:
                4.374930722406134e-05
Epoch 96 MSE:
                4.372949479147792e-05
Epoch 97 MSE:
                4.32433262176346e-05
Epoch 98 MSE:
                4.205634104437195e-05
Epoch 99 MSE:
                4.0997343603521585e-05
T-time: 74.39237594604492
```

Train Score: 0.19 RMSE

Time Step = 50 | Hidden States = 2 | Num Layers = 1

Epoch 0 MSE: 0.09306449443101883 Epoch 1 MSE: 0.0849897563457489 Epoch 2 MSE: 0.07802458107471466 Epoch 3 MSE: 0.07201243191957474 Epoch 4 MSE: 0.06681295484304428 Epoch 5 MSE: 0.0623052716255188 Epoch 6 MSE: 0.058388225734233856 Epoch 7 MSE: 0.05497819930315018 Epoch 8 MSE: 0.05200657993555069 Epoch 9 MSE: 0.049417223781347275 Epoch 10 MSE: 0.04716411605477333 Epoch 11 MSE: 0.04520928114652634 Epoch 12 MSE: 0.0435209795832634 Epoch 13 MSE: 0.042072221636772156 Epoch 14 MSE: 0.04083946719765663 Epoch 15 MSE: 0.03980174660682678 Epoch 16 MSE: 0.03893987089395523 Epoch 17 MSE: 0.03823590278625488 Epoch 18 MSE: 0.03767281025648117 Epoch 19 MSE: 0.03723420575261116 Epoch 20 MSE: 0.036904264241456985 Epoch 21 MSE: 0.036667678505182266 Epoch 22 MSE: 0.03650972247123718 Epoch 23 MSE: 0.03641635179519653 Epoch 24 MSE: 0.036374349147081375 Epoch 25 MSE: 0.03637146204710007 Epoch 26 MSE: 0.03639652580022812 Epoch 27 MSE: 0.03643961623311043 Epoch 28 MSE: 0.03649212419986725 Epoch 29 MSE: 0.03654680401086807 Epoch 30 MSE: 0.036597780883312225 Epoch 31 MSE: 0.03664054349064827 Epoch 32 MSE: 0.03667183220386505 Epoch 33 MSE: 0.036689575761556625 Epoch 34 MSE: 0.03669270873069763 Epoch 35 MSE: 0.03668108955025673 Epoch 36 MSE: 0.03665526956319809 Epoch 37 MSE: 0.03661637008190155 Epoch 38 MSE: 0.036565907299518585 Epoch 39 MSE: 0.036505650728940964 Epoch 40 MSE: 0.036437466740608215

```
Epoch 41 MSE:
                0.03636322543025017
Epoch
       42 MSE:
                0.0362846814095974
Epoch
       43 MSE:
                0.03620341792702675
       44 MSE:
Epoch
                0.03612075746059418
Epoch
       45 MSE:
                0.036037739366292953
Epoch
       46 MSE:
                0.03595511615276337
Epoch
       47 MSE:
                0.03587330877780914
Epoch
       48 MSE:
                0.03579244390130043
Epoch 49 MSE:
                0.035712357610464096
Epoch
      50 MSE:
                0.035632628947496414
       51 MSE:
                0.03555260971188545
Epoch
Epoch
       52 MSE:
                0.03547144681215286
Epoch
       53 MSE:
                0.035388123244047165
Epoch
       54 MSE:
                0.03530150279402733
Epoch
       55 MSE:
                0.035210322588682175
Epoch 56 MSE:
                0.03511323779821396
Epoch
      57 MSE:
                0.03500884771347046
       58 MSE:
Epoch
                0.034895654767751694
Epoch
       59 MSE:
                0.034772101789712906
Epoch
       60 MSE:
                0.034636545926332474
Epoch
       61 MSE:
                0.034487225115299225
Epoch
       62 MSE:
                0.03432222828269005
Epoch
       63 MSE:
                0.03413942828774452
       64 MSE:
Epoch
                0.03393644839525223
Epoch
       65 MSE:
                0.03371056541800499
Epoch
       66 MSE:
                0.03345863148570061
       67 MSE:
Epoch
                0.03317695111036301
Epoch
       68 MSE:
                0.03286118060350418
       69 MSE:
Epoch
                0.032506152987480164
Epoch
      70 MSE:
                0.03210574761033058
     71 MSE:
Epoch
                0.03165265917778015
Epoch
       72 MSE:
                0.031138190999627113
Epoch
      73 MSE:
                0.030552007257938385
      74 MSE:
                0.029881874099373817
Epoch
Epoch
       75 MSE:
                0.02911338210105896
Epoch
       76 MSE:
                0.028229745104908943
Epoch
      77 MSE:
                0.027211803942918777
Epoch
      78 MSE:
                0.026038315147161484
      79 MSE:
Epoch
                0.02468690648674965
       80 MSE:
Epoch
                0.023135803639888763
       81 MSE:
Epoch
                0.02136680856347084
       82 MSE:
Epoch
                0.0193698201328516
Epoch
       83 MSE:
                0.017148876562714577
       84 MSE:
Epoch
                0.014729505404829979
Epoch
       85 MSE:
                0.012166552245616913
Epoch
       86 MSE:
                0.009552966803312302
Epoch
       87 MSE:
                0.007030440028756857
       88 MSE:
                0.004802271258085966
Epoch
```

Epoch 89 MSE: 0.0031357314437627792 Epoch 90 MSE: 0.0023097796365618706 Epoch 91 MSE: 0.002448957646265626 Epoch 92 MSE: 0.0033204867504537106 Epoch 93 MSE: 0.0044088102877140045 Epoch 94 MSE: 0.005187137518078089 Epoch 95 MSE: 0.005293034948408604 Epoch 96 MSE: 0.004716341383755207 Epoch 97 MSE: 0.0037752287462353706 Epoch 98 MSE: 0.0028285295702517033 Epoch 99 MSE: 0.0020741221960633993

T-time: 9.331153631210327

Train Score: 1.36 RMSE

Validation Score: 16.67 RMSE

Time Step = 50 | Hidden States = 2 | Num Layers = 2

Epoch 0 MSE: 0.0374700129032135 Epoch 1 MSE: 0.035636018961668015 Epoch 2 MSE: 0.03456078842282295 Epoch 3 MSE: 0.0342121347784996 Epoch 4 MSE: 0.034095849841833115 Epoch 5 MSE: 0.03360501676797867 Epoch 6 MSE: 0.032605238258838654 Epoch 7 MSE: 0.03124971315264702 Epoch 8 MSE: 0.029755575582385063 Epoch 9 MSE: 0.028341135010123253 Epoch 10 MSE: 0.02706003189086914 Epoch 11 MSE: 0.02556374855339527 Epoch 12 MSE: 0.02347387559711933 Epoch 13 MSE: 0.020887890830636024 Epoch 14 MSE: 0.018430909141898155 Epoch 15 MSE: 0.016589932143688202 Epoch 16 MSE: 0.014509572647511959 Epoch 17 MSE: 0.011592104099690914 Epoch 18 MSE: 0.00901746191084385 Epoch 19 MSE: 0.007894869893789291 Epoch 20 MSE: 0.006267156917601824 Epoch 21 MSE: 0.005734356585890055 Epoch 22 MSE: 0.005994143430143595 Epoch 23 MSE: 0.005611819215118885 Epoch 24 MSE: 0.006483857519924641

```
Epoch
       25 MSE:
                0.005994000006467104
Epoch
       26 MSE:
                0.005704986862838268
Epoch
       27 MSE:
                0.005203791428357363
       28 MSE:
Epoch
                0.004206954035907984
Epoch
       29 MSE:
                0.0033789407461881638
Epoch
       30 MSE:
                0.002876091282814741
Epoch
       31 MSE:
                0.002442718017846346
Epoch
       32 MSE:
                0.0020840668585151434
Epoch
       33 MSE:
                0.0019269302720203996
Epoch
       34 MSE:
                0.0019582752138376236
       35 MSE:
                0.002069185022264719
Epoch
Epoch
       36 MSE:
                0.002164281904697418
Epoch
       37 MSE:
                0.0022064747754484415
Epoch
       38 MSE:
                0.0022001229226589203
Epoch
       39 MSE:
                0.0021492403466254473
      40 MSE:
                0.0020412702579051256
Epoch
Epoch
       41 MSE:
                0.0018725128611549735
       42 MSE:
Epoch
                0.0016766488552093506
Epoch
       43 MSE:
                0.0015122051117941737
Epoch
       44 MSE:
                0.001417440944351256
Epoch
       45 MSE:
                0.001384751871228218
Epoch
       46 MSE:
                0.0013834858546033502
Epoch 47 MSE:
                0.0013969378778710961
       48 MSE:
Epoch
                0.0014217628631740808
       49 MSE:
                0.0014384770765900612
Epoch
Epoch
       50 MSE:
                0.0014137240359559655
       51 MSE:
Epoch
                0.001341594266705215
Epoch
       52 MSE:
                0.001252122106961906
       53 MSE:
Epoch
                0.001170194591395557
Epoch
       54 MSE:
                0.001096745952963829
Epoch 55 MSE:
                0.0010339501313865185
Epoch
       56 MSE:
                0.0009962789481505752
       57 MSE:
Epoch
                0.0009863509330898523
       58 MSE:
                0.0009847191395238042
Epoch
Epoch
       59 MSE:
                0.0009750258759595454
Epoch
       60 MSE:
                0.0009586772648617625
Epoch
       61 MSE:
                0.0009374641813337803
Epoch
       62 MSE:
                0.0009047389612533152
       63 MSE:
Epoch
                0.0008620447479188442
Epoch
       64 MSE:
                0.0008231191895902157
       65 MSE:
Epoch
                0.0007940633222460747
       66 MSE:
Epoch
                0.0007700684363953769
       67 MSE:
Epoch
                0.000752618012484163
Epoch
       68 MSE:
                0.000745066674426198
Epoch
       69 MSE:
                0.0007389666279777884
Epoch
       70 MSE:
                0.0007276950054802
Epoch
       71 MSE:
                0.000714835012331605
       72 MSE:
                0.0006990848924033344
Epoch
```

```
Epoch 73 MSE:
               0.0006777335656806827
Epoch 74 MSE:
               0.0006571949925273657
Epoch 75 MSE:
               0.0006402835133485496
Epoch 76 MSE:
               0.0006243998650461435
Epoch 77 MSE:
               0.00061206822283566
Epoch 78 MSE:
               0.000603445980232209
Epoch 79 MSE:
               0.0005938744288869202
Epoch 80 MSE:
               0.000583516142796725
Epoch 81 MSE:
               0.0005727694369852543
Epoch 82 MSE:
               0.0005592731176875532
Epoch 83 MSE:
               0.0005449820891954005
Epoch 84 MSE:
               0.0005318266921676695
Epoch 85 MSE:
               0.0005188162322156131
Epoch 86 MSE:
               0.0005075685912743211
Epoch 87 MSE:
               0.0004982661921530962
Epoch 88 MSE:
               0.0004889235715381801
Epoch 89 MSE:
               0.00048009949387051165
Epoch 90 MSE:
               0.00047096985508687794
Epoch 91 MSE:
               0.00046066983486525714
Epoch 92 MSE:
               0.0004505457472987473
Epoch 93 MSE:
               0.00044028344564139843
Epoch 94 MSE:
               0.0004303696332499385
Epoch 95 MSE:
               0.00042162128374911845
Epoch 96 MSE:
               0.00041320189484395087
Epoch 97 MSE:
               0.0004053777956869453
Epoch 98 MSE:
               0.0003977388550993055
Epoch 99 MSE:
               0.0003896840789820999
```

T-time: 15.219264030456543

Train Score: 0.59 RMSE

Validation Score: 13.21 RMSE

_____ Time Step = 50 | Hidden States = 4 | Num Layers = 1 ______

Epoch 0 MSE: 0.047699227929115295 Epoch 1 MSE: 0.0403577946126461 Epoch 2 MSE: 0.03543386235833168 Epoch 3 MSE: 0.0323510505259037 Epoch 4 MSE: 0.030534114688634872 Epoch 5 MSE: 0.02939521335065365 Epoch 6 MSE: 0.028316548094153404 Epoch 7 MSE: 0.02683001011610031 Epoch 8 MSE: 0.024718645960092545

```
9 MSE:
               0.021981289610266685
Epoch
Epoch
       10 MSE:
                0.018770406022667885
Epoch
       11 MSE:
                0.015350286848843098
       12 MSE:
Epoch
                0.012064987793564796
Epoch
       13 MSE:
                0.009276753291487694
Epoch
       14 MSE:
                0.007230101153254509
Epoch
       15 MSE:
                0.005843719933182001
Epoch
       16 MSE:
                0.004685766529291868
Epoch 17 MSE:
                0.003446610178798437
Epoch
       18 MSE:
                0.0023557357490062714
       19 MSE:
                0.0019882600754499435
Epoch
       20 MSE:
Epoch
                0.002656686119735241
Epoch
       21 MSE:
                0.0039013498462736607
Epoch
       22 MSE:
                0.004817979875952005
Epoch
       23 MSE:
                0.004910567309707403
                0.004311470780521631
Epoch
      24 MSE:
Epoch
       25 MSE:
                0.0034501031041145325
       26 MSE:
                0.0027057016268372536
Epoch
Epoch
       27 MSE:
                0.002224933821707964
Epoch
       28 MSE:
                0.00193732266779989
       29 MSE:
Epoch
                0.0017132823122665286
       30 MSE:
Epoch
                0.0014996333047747612
Epoch
       31 MSE:
                0.0013276210520416498
       32 MSE:
Epoch
                0.0012483777245506644
       33 MSE:
                0.0012804073048755527
Epoch
Epoch
       34 MSE:
                0.0013961991062387824
       35 MSE:
Epoch
                0.001537673408165574
Epoch
       36 MSE:
                0.0016427887603640556
       37 MSE:
Epoch
                0.0016688858158886433
Epoch
       38 MSE:
                0.001604556804522872
       39 MSE:
                0.0014683620538562536
Epoch
Epoch
       40 MSE:
                0.0012975090648978949
Epoch
       41 MSE:
                0.0011319806799292564
       42 MSE:
                0.001000057440251112
Epoch
Epoch
       43 MSE:
                0.0009105589706450701
Epoch
       44 MSE:
                0.0008548147161491215
Epoch
       45 MSE:
                0.0008169591310434043
Epoch
       46 MSE:
                0.0007861144258640707
       47 MSE:
Epoch
                0.0007623882265761495
Epoch
       48 MSE:
                0.0007529360009357333
       49 MSE:
                0.0007619571988470852
Epoch
       50 MSE:
Epoch
                0.0007830730173736811
Epoch
       51 MSE:
                0.0008003425900824368
Epoch
       52 MSE:
                0.0007971310988068581
Epoch
       53 MSE:
                0.0007661162526346743
Epoch
       54 MSE:
                0.0007133962935768068
Epoch
       55 MSE:
                0.0006544270436279476
       56 MSE:
                0.0006051636883057654
Epoch
```

```
Epoch 57 MSE:
                0.0005742881330661476
Epoch 58 MSE:
                0.0005608081701211631
Epoch 59 MSE:
                0.0005573479575105011
Epoch
      60 MSE:
                0.0005559190758503973
Epoch 61 MSE:
                0.0005521267303265631
Epoch 62 MSE:
                0.0005457376828417182
Epoch
      63 MSE:
                0.0005383959505707026
Epoch 64 MSE:
                0.0005308915278874338
Epoch 65 MSE:
                0.0005220581660978496
Epoch
      66 MSE:
                0.0005097832181490958
      67 MSE:
                0.0004930439754389226
Epoch
Epoch 68 MSE:
                0.0004732786910608411
Epoch 69 MSE:
                0.00045401195529848337
Epoch 70 MSE:
                0.000438940420281142
Epoch 71 MSE:
                0.00042979035060852766
Epoch 72 MSE:
                0.0004254326631780714
Epoch 73 MSE:
                0.00042283631046302617
Epoch 74 MSE:
                0.00041909157880581915
Epoch 75 MSE:
                0.0004129809094592929
Epoch 76 MSE:
                0.00040506725781597197
Epoch
     77 MSE:
                0.0003965538926422596
Epoch 78 MSE:
                0.0003880947479046881
Epoch 79 MSE:
                0.0003795314987655729
Epoch 80 MSE:
                0.0003705378039740026
Epoch 81 MSE:
                0.00036135411937721074
Epoch 82 MSE:
                0.0003528547240421176
Epoch 83 MSE:
                0.00034591020084917545
Epoch
      84 MSE:
                0.0003406602772884071
Epoch 85 MSE:
                0.0003363509604241699
Epoch 86 MSE:
                0.0003318586095701903
Epoch 87 MSE:
                0.00032643985468894243
Epoch 88 MSE:
                0.00032011119765229523
Epoch 89 MSE:
                0.00031343201408162713
Epoch 90 MSE:
                0.00030697256443090737
Epoch
      91 MSE:
                0.00030094769317656755
Epoch 92 MSE:
                0.00029525786521844566
Epoch 93 MSE:
                0.00028978486079722643
Epoch 94 MSE:
                0.000284588779322803
Epoch 95 MSE:
                0.00027982122264802456
Epoch 96 MSE:
                0.0002754808811005205
Epoch 97 MSE:
                0.00027130290982313454
Epoch 98 MSE:
                0.00026692109531722963
Epoch 99 MSE:
                0.000262151297647506
```

T-time: 12.319850444793701

Train Score: 0.48 RMSE

Time Step = 50 | Hidden States = 4 | Num Layers = 2

Epoch 0 MSE: 0.33187252283096313 Epoch 1 MSE: 0.28996092081069946 Epoch 2 MSE: 0.25252556800842285 Epoch 3 MSE: 0.21925488114356995 Epoch 4 MSE: 0.18956483900547028 Epoch 5 MSE: 0.1628427505493164 Epoch 6 MSE: 0.13853462040424347 Epoch 7 MSE: 0.1162320002913475 Epoch 8 MSE: 0.09571653604507446 Epoch 9 MSE: 0.07700160145759583 Epoch 10 MSE: 0.060377754271030426 Epoch 11 MSE: 0.04643342271447182 Epoch 12 MSE: 0.03601546585559845 Epoch 13 MSE: 0.03007112443447113 Epoch 14 MSE: 0.02924986556172371 Epoch 15 MSE: 0.03310723602771759 Epoch 16 MSE: 0.039304859936237335 Epoch 17 MSE: 0.0445881150662899 Epoch 18 MSE: 0.04700835794210434 Epoch 19 MSE: 0.046427492052316666 Epoch 20 MSE: 0.04371706396341324 Epoch 21 MSE: 0.04000725969672203 Epoch 22 MSE: 0.0362674854695797 Epoch 23 MSE: 0.0331343375146389 Epoch 24 MSE: 0.030897734686732292 Epoch 25 MSE: 0.029576284810900688 Epoch 26 MSE: 0.029022306203842163 Epoch 27 MSE: 0.029015829786658287 Epoch 28 MSE: 0.029329683631658554 Epoch 29 MSE: 0.02976566180586815 Epoch 30 MSE: 0.030169591307640076 Epoch 31 MSE: 0.030433764681220055 Epoch 32 MSE: 0.030493076890707016 Epoch 33 MSE: 0.030318740755319595 Epoch 34 MSE: 0.029911397024989128 Epoch 35 MSE: 0.02929447963833809 Epoch 36 MSE: 0.028508035466074944 Epoch 37 MSE: 0.02760288119316101 Epoch 38 MSE: 0.026634905487298965 Epoch 39 MSE: 0.025659242644906044 Epoch 40 MSE: 0.02472436986863613

```
Epoch
       41 MSE:
                0.02386610023677349
Epoch
       42 MSE:
                0.02310207672417164
       43 MSE:
                0.022427696734666824
Epoch
       44 MSE:
Epoch
                0.02181483805179596
Epoch
       45 MSE:
                0.02121479995548725
       46 MSE:
Epoch
                0.020566359162330627
Epoch
       47 MSE:
                0.019808275625109673
Epoch
       48 MSE:
                0.018893908709287643
Epoch 49 MSE:
                0.01780346967279911
Epoch
       50 MSE:
                0.016549719497561455
       51 MSE:
Epoch
                0.015174604021012783
Epoch
       52 MSE:
                0.013737772591412067
Epoch
       53 MSE:
                0.012300800532102585
Epoch
       54 MSE:
                0.010912704281508923
Epoch
       55 MSE:
                0.009601225145161152
                0.008372189477086067
      56 MSE:
Epoch
Epoch
       57 MSE:
                0.007216496858745813
       58 MSE:
Epoch
                0.006122284103184938
Epoch
       59 MSE:
                0.005088508129119873
Epoch
       60 MSE:
                0.00413524080067873
Epoch
       61 MSE:
                0.0033058577682822943
Epoch
       62 MSE:
                0.0026580553967505693
Epoch
       63 MSE:
                0.002244590548798442
       64 MSE:
Epoch
                0.002089456422254443
       65 MSE:
                0.0021686239633709192
Epoch
Epoch
       66 MSE:
                0.0024054262321442366
       67 MSE:
Epoch
                0.0026894640177488327
Epoch
       68 MSE:
                0.002916505793109536
       69 MSE:
Epoch
                0.0030248723924160004
Epoch
      70 MSE:
                0.0030026810709387064
      71 MSE:
Epoch
                0.0028699280228465796
Epoch
       72 MSE:
                0.0026579583063721657
Epoch
       73 MSE:
                0.0023988094180822372
       74 MSE:
                0.0021226005628705025
Epoch
Epoch
       75 MSE:
                0.0018561258912086487
Epoch
       76 MSE:
                0.001620094757527113
Epoch
      77 MSE:
                0.001427411218173802
Epoch
       78 MSE:
                0.0012837734539061785
       79 MSE:
Epoch
                0.001189259928651154
       80 MSE:
Epoch
                0.0011395749170333147
       81 MSE:
                0.0011268112575635314
Epoch
       82 MSE:
Epoch
                0.0011402784148231149
       83 MSE:
Epoch
                0.0011678457958623767
       84 MSE:
Epoch
                0.0011977722169831395
Epoch
       85 MSE:
                0.0012205514358356595
Epoch
       86 MSE:
                0.0012301786337047815
Epoch
       87 MSE:
                0.0012244347017258406
       88 MSE:
Epoch
                0.0012042165035381913
```

Epoch 89 MSE: 0.0011723109055310488 Epoch 90 MSE: 0.0011321547208353877 Epoch 91 MSE: 0.0010870136320590973 Epoch 92 MSE: 0.0010397210717201233 Epoch 93 MSE: 0.0009928109357133508 Epoch 94 MSE: 0.0009487365023232996 Epoch 95 MSE: 0.0009098851005546749 Epoch 96 MSE: 0.0008782932418398559 Epoch 97 MSE: 0.0008551795035600662 0.0008405499975197017 Epoch 98 MSE: Epoch 99 MSE: 0.0008331199060194194

T-time: 21.50165367126465

Train Score: 0.86 RMSE

Validation Score: 15.13 RMSE

Time Step = 50 | Hidden States = 8 | Num Layers = 1

Epoch 0 MSE: 0.058424100279808044 Epoch 1 MSE: 0.04329431429505348 Epoch 2 MSE: 0.033064231276512146 Epoch 3 MSE: 0.027678778395056725 Epoch 4 MSE: 0.026682056486606598 Epoch 5 MSE: 0.02852580137550831 Epoch 6 MSE: 0.03046368435025215 Epoch 7 MSE: 0.03070507012307644 Epoch 8 MSE: 0.029239682480692863 Epoch 9 MSE: 0.02684829942882061 Epoch 10 MSE: 0.024330683052539825 Epoch 11 MSE: 0.02221529744565487 Epoch 12 MSE: 0.020714357495307922 Epoch 13 MSE: 0.01978319138288498 Epoch 14 MSE: 0.01921330951154232 Epoch 15 MSE: 0.01872563362121582 Epoch 16 MSE: 0.018050063401460648 Epoch 17 MSE: 0.016985759139060974 Epoch 18 MSE: 0.015439293347299099 Epoch 19 MSE: 0.013439802452921867 Epoch 20 MSE: 0.011132773011922836 Epoch 21 MSE: 0.008754229173064232 Epoch 22 MSE: 0.0065818182192742825 Epoch 23 MSE: 0.004850185476243496 Epoch 24 MSE: 0.0036259121261537075

```
Epoch
       25 MSE:
                0.0027268456760793924
Epoch
       26 MSE:
                0.0019086222164332867
Epoch
       27 MSE:
                0.0012554904678836465
       28 MSE:
Epoch
                0.0011920296819880605
Epoch
       29 MSE:
                0.0019867578521370888
Epoch
       30 MSE:
                0.0031046196818351746
Epoch
       31 MSE:
                0.0035410772543400526
Epoch
       32 MSE:
                0.002916240831837058
       33 MSE:
Epoch
                0.0016865157522261143
Epoch
       34 MSE:
                0.0006008659256622195
       35 MSE:
                0.0001670877099968493
Epoch
       36 MSE:
Epoch
                0.0003845070314127952
Epoch
       37 MSE:
                0.0008423026883974671
Epoch
       38 MSE:
                0.0011152394581586123
Epoch
       39 MSE:
                0.0010800636373460293
Epoch 40 MSE:
                0.0008864811388775706
Epoch
       41 MSE:
                0.000736396701540798
       42 MSE:
Epoch
                0.0007210024632513523
Epoch
       43 MSE:
                0.0007955388864502311
Epoch
       44 MSE:
                0.000846494163852185
Epoch
       45 MSE:
                0.0007804576889611781
       46 MSE:
Epoch
                0.0005841376259922981
Epoch 47 MSE:
                0.000332698633428663
       48 MSE:
Epoch
                0.00014600876602344215
       49 MSE:
                0.00011173709208378568
Epoch
       50 MSE:
Epoch
                0.00021754682529717684
       51 MSE:
Epoch
                0.0003522115875966847
Epoch
       52 MSE:
                0.00039872725028544664
       53 MSE:
Epoch
                0.00033821017132140696
Epoch 54 MSE:
                0.00024858381948433816
Epoch 55 MSE:
                0.00020865142869297415
Epoch
       56 MSE:
                0.00022544532839674503
       57 MSE:
Epoch
                0.00024867671891115606
       58 MSE:
                0.00023224939650390297
Epoch
Epoch
       59 MSE:
                0.0001753529504640028
Epoch
       60 MSE:
                0.0001159582388936542
Epoch
       61 MSE:
                9.398382826475427e-05
Epoch
       62 MSE:
                0.00011814806930487975
       63 MSE:
Epoch
                0.00016158765356522053
Epoch
       64 MSE:
                0.0001868795952759683
       65 MSE:
Epoch
                0.00017680057499092072
       66 MSE:
Epoch
                0.0001440385967725888
Epoch
       67 MSE:
                0.0001148698793258518
Epoch
       68 MSE:
                0.00010543044481892139
Epoch
       69 MSE:
                0.00011156315304106101
Epoch
       70 MSE:
                0.00011737544264178723
Epoch
       71 MSE:
                0.00011160735448356718
       72 MSE:
Epoch
                9.701968519948423e-05
```

```
Epoch 73 MSE:
               8.603122114436701e-05
Epoch 74 MSE:
               8.782828808762133e-05
Epoch 75 MSE:
               9.9282777227927e-05
Epoch 76 MSE:
               0.00010829667735379189
Epoch 77 MSE:
               0.00010584817209746689
Epoch 78 MSE:
               9.40537138376385e-05
Epoch 79 MSE:
               8.256221190094948e-05
Epoch 80 MSE:
               7.859499601181597e-05
Epoch 81 MSE:
               8.133298251777887e-05
Epoch 82 MSE:
               8.477984374621883e-05
Epoch 83 MSE:
               8.441498357569799e-05
Epoch 84 MSE:
               8.082251588348299e-05
Epoch 85 MSE:
               7.783895125612617e-05
Epoch 86 MSE:
               7.8062221291475e-05
Epoch 87 MSE:
               8.034038910409436e-05
Epoch 88 MSE:
               8.132613584166393e-05
Epoch 89 MSE:
               7.906816608738154e-05
Epoch 90 MSE:
               7.485458627343178e-05
Epoch 91 MSE:
               7.16753420419991e-05
Epoch 92 MSE:
               7.123666000552475e-05
Epoch 93 MSE:
               7.262633153004572e-05
Epoch 94 MSE:
               7.364207704085857e-05
Epoch 95 MSE:
               7.306024781428277e-05
Epoch 96 MSE:
               7.151623140089214e-05
Epoch 97 MSE:
               7.040942728053778e-05
Epoch 98 MSE:
               7.027840183582157e-05
Epoch 99 MSE:
               7.039428601274267e-05
T-time: 10.873689413070679
```

Train Score: 0.25 RMSE Validation Score: 5.84 RMSE

_____ Time Step = 50 | Hidden States = 8 | Num Layers = 2 ______

```
Epoch 0 MSE: 0.1302509605884552
Epoch 1 MSE: 0.09970978647470474
Epoch 2 MSE: 0.07591716945171356
Epoch 3 MSE:
              0.05807344242930412
Epoch 4 MSE:
              0.04556714743375778
Epoch 5 MSE:
              0.0380430594086647
Epoch 6 MSE:
              0.035237036645412445
Epoch 7 MSE:
              0.036477115005254745
Epoch 8 MSE:
              0.03990400955080986
```

```
Epoch 9 MSE:
               0.042836952954530716
Epoch
       10 MSE:
                0.043728332966566086
Epoch 11 MSE:
                0.04262995347380638
       12 MSE:
Epoch
                0.04034360498189926
Epoch
       13 MSE:
                0.03773856908082962
Epoch
       14 MSE:
                0.03544874116778374
Epoch
       15 MSE:
                0.03379964828491211
Epoch 16 MSE:
                0.03285196051001549
Epoch 17 MSE:
                0.03248804807662964
Epoch
       18 MSE:
                0.032496653497219086
       19 MSE:
                0.03263560310006142
Epoch
      20 MSE:
Epoch
                0.03267347812652588
Epoch
      21 MSE:
                0.03241885080933571
Epoch
      22 MSE:
                0.031737178564071655
Epoch
      23 MSE:
                0.03055131807923317
Epoch 24 MSE:
                0.02882988750934601
Epoch
      25 MSE:
                0.026577472686767578
      26 MSE:
                0.023847924545407295
Epoch
Epoch
      27 MSE:
                0.02079167403280735
Epoch
      28 MSE:
                0.01770988292992115
Epoch
       29 MSE:
                0.014939893037080765
      30 MSE:
Epoch
                0.012350838631391525
Epoch 31 MSE:
                0.009291018359363079
      32 MSE:
Epoch
                0.0059777116402983665
Epoch
      33 MSE:
                0.00443768547847867
Epoch
       34 MSE:
                0.005606395658105612
      35 MSE:
Epoch
                0.007542717270553112
Epoch
       36 MSE:
                0.007951632142066956
      37 MSE:
Epoch
                0.007135819178074598
Epoch 38 MSE:
                0.005597361829131842
      39 MSE:
Epoch
                0.004608544055372477
Epoch
       40 MSE:
                0.003936560358852148
                0.003633882850408554
Epoch
      41 MSE:
      42 MSE:
                0.0035270629450678825
Epoch
Epoch
       43 MSE:
                0.0033467255998402834
Epoch
      44 MSE:
                0.0032698484137654305
Epoch 45 MSE:
                0.003345335368067026
Epoch
      46 MSE:
                0.003491020994260907
      47 MSE:
Epoch
                0.003601304953917861
      48 MSE:
Epoch
                0.0035669179633259773
Epoch 49 MSE:
                0.0033383548725396395
      50 MSE:
Epoch
                0.00294800428673625
Epoch
      51 MSE:
                0.0024944536853581667
Epoch
      52 MSE:
                0.0021047794725745916
Epoch
      53 MSE:
                0.0018792720511555672
Epoch
       54 MSE:
                0.0018367223674431443
Epoch
       55 MSE:
                0.001901602023281157
      56 MSE:
                0.0019465495133772492
Epoch
```

```
Epoch 57 MSE:
                0.0018815959338098764
Epoch 58 MSE:
                0.0017107551684603095
Epoch 59 MSE:
                0.0015026973560452461
Epoch 60 MSE:
                0.0013226866722106934
Epoch 61 MSE:
                0.0011943303979933262
Epoch 62 MSE:
                0.0011082314886152744
Epoch
      63 MSE:
                0.0010491559514775872
Epoch 64 MSE:
                0.001010664738714695
Epoch 65 MSE:
                0.0009902295423671603
Epoch 66 MSE:
                0.0009777839295566082
Epoch 67 MSE:
                0.0009537209407426417
Epoch 68 MSE:
                0.0009011283982545137
Epoch 69 MSE:
                0.0008213697001338005
Epoch 70 MSE:
                0.000736365735065192
Epoch 71 MSE:
                0.000672969501465559
Epoch 72 MSE:
                0.0006427824264392257
Epoch 73 MSE:
                0.0006350618787109852
Epoch 74 MSE:
                0.000627503206487745
Epoch 75 MSE:
                0.0006039714789949358
Epoch 76 MSE:
                0.0005641220486722887
Epoch 77 MSE:
                0.0005188637296669185
Epoch 78 MSE:
                0.0004783199692610651
Epoch 79 MSE:
                0.000444484525360167
Epoch 80 MSE:
                0.00041437186882831156
Epoch 81 MSE:
                0.00038732821121811867
Epoch 82 MSE:
                0.00036622246261686087
Epoch 83 MSE:
                0.0003516400174703449
Epoch 84 MSE:
                0.0003380428534001112
Epoch 85 MSE:
                0.00031805530306883156
Epoch 86 MSE:
                0.0002903818094637245
Epoch 87 MSE:
                0.00026206386974081397
Epoch 88 MSE:
                0.00024185270012822002
Epoch 89 MSE:
                0.00023145404702518135
Epoch 90 MSE:
                0.00022439785243477672
Epoch
      91 MSE:
                0.00021371310867834836
Epoch 92 MSE:
                0.00019877530576195568
Epoch 93 MSE:
                0.00018348291632719338
Epoch 94 MSE:
                0.00017015618504956365
Epoch 95 MSE:
                0.00015805869770701975
Epoch 96 MSE:
                0.00014684362395200878
Epoch 97 MSE:
                0.00013795019185636193
Epoch 98 MSE:
                0.00013148356811143458
Epoch 99 MSE:
                0.00012434954987838864
```

T-time: 21.277970790863037

Train Score: 0.33 RMSE

Validation Score: 12.09 RMSE

Time Step = 50 | Hidden States = 16 | Num Layers = 1

Epoch 0 MSE: 0.03285951912403107 Epoch 1 MSE: 0.03075476549565792 Epoch 2 MSE: 0.02826731838285923 Epoch 3 MSE: 0.026006106287240982 Epoch 4 MSE: 0.02310761623084545 Epoch 5 MSE: 0.020261136814951897 Epoch 6 MSE: 0.01646673120558262 Epoch 7 MSE: 0.011825131252408028 Epoch 8 MSE: 0.006906010210514069 Epoch 9 MSE: 0.0016963323578238487 Epoch 10 MSE: 0.0012760853860527277 Epoch 11 MSE: 0.00948462262749672 Epoch 12 MSE: 0.005685037933290005 Epoch 13 MSE: 0.0034057290758937597 Epoch 14 MSE: 0.00034108763793483377 Epoch 15 MSE: 0.0005842677201144397 Epoch 16 MSE: 0.0015792474150657654 Epoch 17 MSE: 0.0018052472732961178 Epoch 18 MSE: 0.0020006918348371983 Epoch 19 MSE: 0.002487612422555685 Epoch 20 MSE: 0.0027224007062613964 Epoch 21 MSE: 0.002370781498029828 Epoch 22 MSE: 0.0017896348144859076 Epoch 23 MSE: 0.0014007420977577567 Epoch 24 MSE: 0.001126701943576336 Epoch 25 MSE: 0.0006815172964707017 Epoch 26 MSE: 0.0002007434522965923 Epoch 27 MSE: 0.00011182519665453583 Epoch 28 MSE: 0.0003617595648393035 Epoch 29 MSE: 0.0005002116085961461 Epoch 30 MSE: 0.0005865277489647269 Epoch 31 MSE: 0.0008008908480405807 Epoch 32 MSE: 0.0008070911862887442 Epoch 33 MSE: 0.0005263633211143315 Epoch 34 MSE: 0.000316180638037622 Epoch 35 MSE: 0.0002359907957725227 Epoch 36 MSE: 0.00013046414824202657 Epoch 37 MSE: 6.694182229693979e-05 Epoch 38 MSE: 0.00013862131163477898 Epoch 39 MSE: 0.000245537084992975 Epoch 40 MSE: 0.0002798286732286215

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Epoch 41 MSE:
                0.00027530008810572326
Epoch
      42 MSE:
                0.00028733391081914306
      43 MSE:
Epoch
                0.000279270694591105
       44 MSE:
Epoch
                0.00020983406284358352
Epoch
      45 MSE:
                0.0001281245640711859
Epoch
      46 MSE:
                9.245367982657626e-05
Epoch
       47 MSE:
                8.051433542277664e-05
Epoch
      48 MSE:
                6.1412101786118e-05
Epoch 49 MSE:
                6.619438499910757e-05
Epoch 50 MSE:
                0.0001072640807251446
      51 MSE:
                0.00013296958059072495
Epoch
Epoch 52 MSE:
                0.00012485070328693837
Epoch
      53 MSE:
                0.00011626279592746869
Epoch
      54 MSE:
                0.000106322746432852
Epoch 55 MSE:
                7.698859553784132e-05
                5.086490273242816e-05
Epoch 56 MSE:
Epoch 57 MSE:
                4.889835690846667e-05
      58 MSE:
Epoch
                5.412191603682004e-05
Epoch
      59 MSE:
                5.5292563047260046e-05
Epoch
       60 MSE:
                6.307630246737972e-05
Epoch
       61 MSE:
                7.464266673196107e-05
Epoch
      62 MSE:
                7.475032907677814e-05
Epoch
      63 MSE:
                6.580259650945663e-05
       64 MSE:
Epoch
                5.957728353678249e-05
Epoch
       65 MSE:
                5.387235069065355e-05
Epoch
      66 MSE:
                4.46718986495398e-05
      67 MSE:
Epoch
                4.027943577966653e-05
Epoch
       68 MSE:
                4.393967174110003e-05
      69 MSE:
Epoch
                4.726933184429072e-05
Epoch 70 MSE:
                4.841410191147588e-05
Epoch 71 MSE:
                5.1254068239359185e-05
Epoch 72 MSE:
                5.195894482312724e-05
Epoch
      73 MSE:
                4.760604497278109e-05
Epoch 74 MSE:
                4.361172250355594e-05
Epoch
      75 MSE:
                4.198585884296335e-05
Epoch
      76 MSE:
                3.9968228520592675e-05
Epoch 77 MSE:
                3.9096325053833425e-05
Epoch 78 MSE:
                4.1098166548181325e-05
Epoch 79 MSE:
                4.280464781913906e-05
Epoch
      80 MSE:
                4.276079198461957e-05
      81 MSE:
Epoch
                4.2798677895916626e-05
Epoch
       82 MSE:
                4.238582550897263e-05
Epoch
      83 MSE:
                4.0459144656779245e-05
Epoch
       84 MSE:
                3.891009328071959e-05
Epoch
      85 MSE:
                3.867215491482057e-05
Epoch
       86 MSE:
                3.846829349640757e-05
Epoch
       87 MSE:
                3.852800728054717e-05
       88 MSE:
Epoch
                3.939838643418625e-05
```

Epoch 89 MSE: 3.97976218664553e-05
Epoch 90 MSE: 3.937021756428294e-05
Epoch 91 MSE: 3.903059405274689e-05
Epoch 92 MSE: 3.8551606849068776e-05
Epoch 93 MSE: 3.777026722673327e-05
Epoch 94 MSE: 3.750300675164908e-05
Epoch 95 MSE: 3.7669597077183425e-05
Epoch 96 MSE: 3.770220428123139e-05
Epoch 97 MSE: 3.783533611567691e-05
Epoch 98 MSE: 3.802502396865748e-05
Epoch 99 MSE: 3.782587009482086e-05

T-time: 19.1439528465271

Train Score: 0.18 RMSE

Validation Score: 5.01 RMSE

Time Step = 50 | Hidden States = 16 | Num Layers = 2

Epoch 0 MSE: 0.055803071707487106 Epoch 1 MSE: 0.04059523716568947 Epoch 2 MSE: 0.03624124825000763 Epoch 3 MSE: 0.03919117897748947 Epoch 4 MSE: 0.0380801260471344 Epoch 5 MSE: 0.03565781190991402 Epoch 6 MSE: 0.034267254173755646 Epoch 7 MSE: 0.03381923958659172 Epoch 8 MSE: 0.03372098505496979 Epoch 9 MSE: 0.033516764640808105 Epoch 10 MSE: 0.032939642667770386 Epoch 11 MSE: 0.031853482127189636 Epoch 12 MSE: 0.030194642022252083 Epoch 13 MSE: 0.027944287285208702 Epoch 14 MSE: 0.025148732587695122 Epoch 15 MSE: 0.02187371999025345 Epoch 16 MSE: 0.017800379544496536 Epoch 17 MSE: 0.011946016922593117 Epoch 18 MSE: 0.004980036057531834 Epoch 19 MSE: 0.001874722307547927 Epoch 20 MSE: 0.0050443727523088455 Epoch 21 MSE: 0.008630452677607536 Epoch 22 MSE: 0.00877425353974104 Epoch 23 MSE: 0.006138664670288563 Epoch 24 MSE: 0.003178745973855257

```
Epoch
       25 MSE:
                0.00162295822519809
Epoch
       26 MSE:
                0.0015493737300857902
Epoch
       27 MSE:
                0.002158679300919175
       28 MSE:
Epoch
                0.002810870064422488
Epoch
       29 MSE:
                0.003262718440964818
Epoch
       30 MSE:
                0.0033794716000556946
Epoch
       31 MSE:
                0.0030550009105354548
Epoch
       32 MSE:
                0.0023591765202581882
       33 MSE:
Epoch
                0.0015965043567121029
Epoch
       34 MSE:
                0.0011583867017179728
       35 MSE:
                0.0011432109167799354
Epoch
       36 MSE:
Epoch
                0.0012348229065537453
Epoch
       37 MSE:
                0.0013243977446109056
Epoch
       38 MSE:
                0.0015509017976000905
Epoch
       39 MSE:
                0.0017215160187333822
Epoch
      40 MSE:
                0.0015660750214010477
Epoch
       41 MSE:
                0.0012093037366867065
       42 MSE:
                0.0009430420468561351
Epoch
Epoch
       43 MSE:
                0.0007874839939177036
Epoch
       44 MSE:
                0.0006541757611557841
Epoch
       45 MSE:
                0.0006325896247290075
Epoch
       46 MSE:
                0.0007552306051366031
Epoch
      47 MSE:
                0.0008674318669363856
       48 MSE:
Epoch
                0.0008464900311082602
       49 MSE:
                0.0007269553607329726
Epoch
       50 MSE:
Epoch
                0.0005913266213610768
       51 MSE:
Epoch
                0.00045657847658731043
Epoch
       52 MSE:
                0.0003421059809625149
       53 MSE:
Epoch
                0.00032040776568464935
Epoch
       54 MSE:
                0.00037921854527667165
       55 MSE:
Epoch
                0.0004142190737184137
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       57 MSE:
Epoch
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       58 MSE:
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Epoch
Epoch
       59 MSE:
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Epoch
       60 MSE:
                0.00015040092694107443
Epoch
       61 MSE:
                0.00018307840218767524
Epoch
       62 MSE:
                0.00020863320969510823
       63 MSE:
Epoch
                0.00020313699496909976
Epoch
       64 MSE:
                0.0001514190371381119
       65 MSE:
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Epoch
       66 MSE:
Epoch
                7.53811837057583e-05
Epoch
       67 MSE:
                9.183634392684326e-05
Epoch
       68 MSE:
                0.00011768362310249358
Epoch
       69 MSE:
                0.00011743413051590323
Epoch
       70 MSE:
                8.590637298766524e-05
Epoch
       71 MSE:
                5.749673073296435e-05
       72 MSE:
                5.113667430123314e-05
Epoch
```

```
Epoch 73 MSE:
               7.103079406078905e-05
Epoch 74 MSE: 8.471649925922975e-05
Epoch 75 MSE:
               7.427162199746817e-05
Epoch 76 MSE:
               5.429471275419928e-05
Epoch 77 MSE:
               4.440270276973024e-05
Epoch 78 MSE:
               5.614446854451671e-05
Epoch 79 MSE:
               6.575937732122838e-05
Epoch 80 MSE:
               6.40798025415279e-05
Epoch 81 MSE:
               5.059872637502849e-05
Epoch 82 MSE:
               4.4118980440543965e-05
Epoch 83 MSE:
               4.964014806319028e-05
Epoch 84 MSE:
               5.620254160021432e-05
Epoch 85 MSE:
               5.5105541832745075e-05
Epoch 86 MSE:
               4.583523332257755e-05
Epoch 87 MSE:
               4.287223782739602e-05
Epoch 88 MSE:
               4.543570685200393e-05
Epoch 89 MSE:
               4.9855098041007295e-05
Epoch 90 MSE:
               4.729110878542997e-05
Epoch 91 MSE:
               4.239525878801942e-05
Epoch 92 MSE:
               4.02678779209964e-05
Epoch 93 MSE:
               4.259427441866137e-05
Epoch 94 MSE:
               4.459390038391575e-05
Epoch 95 MSE:
               4.2485127778491005e-05
Epoch 96 MSE:
               3.961606489610858e-05
Epoch 97 MSE:
               3.873397872666828e-05
Epoch 98 MSE:
               4.070414797752164e-05
Epoch 99 MSE:
               4.1201830754289404e-05
```

T-time: 45.053837299346924

Train Score: 0.19 RMSE Validation Score: 4.53 RMSE

_____ Time Step = 50 | Hidden States = 32 | Num Layers = 1 ______

```
Epoch 0 MSE: 0.054831381887197495
Epoch 1 MSE: 0.03660176694393158
Epoch 2 MSE: 0.032372523099184036
Epoch 3 MSE:
              0.034817032516002655
Epoch 4 MSE:
              0.032896529883146286
Epoch 5 MSE:
              0.02835434302687645
Epoch 6 MSE:
              0.024636749178171158
Epoch 7 MSE:
              0.022329257801175117
Epoch 8 MSE: 0.02039140649139881
```

```
Epoch 9 MSE:
               0.017229245975613594
Epoch
       10 MSE:
                0.011185265146195889
       11 MSE:
Epoch
                0.0027695035096257925
       12 MSE:
Epoch
                0.023742202669382095
Epoch
       13 MSE:
                0.002632385352626443
Epoch
       14 MSE:
                0.0030763025861233473
Epoch
       15 MSE:
                0.00814159493893385
Epoch 16 MSE:
                0.010175475850701332
Epoch 17 MSE:
                0.009152109734714031
Epoch
       18 MSE:
                0.006416885647922754
       19 MSE:
                0.003540203906595707
Epoch
      20 MSE:
Epoch
                0.0020009500440210104
Epoch
      21 MSE:
                0.0025878127198666334
Epoch
       22 MSE:
                0.00435244757682085
Epoch
      23 MSE:
                0.004914658144116402
                0.003362047951668501
Epoch 24 MSE:
Epoch
      25 MSE:
                0.0012448944617062807
      26 MSE:
                0.0002544672170188278
Epoch
Epoch
      27 MSE:
                0.0006865999312140048
Epoch
       28 MSE:
                0.0017446683486923575
       29 MSE:
Epoch
                0.002436249516904354
      30 MSE:
Epoch
                0.002275325357913971
Epoch 31 MSE:
                0.0014789963606745005
       32 MSE:
Epoch
                0.0006731877219863236
Epoch
      33 MSE:
                0.00039057445246726274
Epoch
       34 MSE:
                0.0006768318708054721
      35 MSE:
Epoch
                0.001088457414880395
Epoch
       36 MSE:
                0.0011549743358045816
      37 MSE:
Epoch
                0.0008373437449336052
Epoch 38 MSE:
                0.0004552750615403056
      39 MSE:
Epoch
                0.0002944599837064743
Epoch
       40 MSE:
                0.0003942231123801321
Epoch
      41 MSE:
                0.0006081132451072335
      42 MSE:
                0.0007571107125841081
Epoch
Epoch
       43 MSE:
                0.000740201969165355
Epoch
      44 MSE:
                0.000570731412153691
Epoch
      45 MSE:
                0.00035157069214619696
Epoch
      46 MSE:
                0.0002086346794385463
      47 MSE:
Epoch
                0.0002099591656588018
Epoch
      48 MSE:
                0.0003165457455907017
Epoch 49 MSE:
                0.0004134720948059112
       50 MSE:
Epoch
                0.00041081238305196166
Epoch
       51 MSE:
                0.00032002420630306005
Epoch
       52 MSE:
                0.00022663624258711934
Epoch
      53 MSE:
                0.0001994183985516429
Epoch
       54 MSE:
                0.00023606611648574471
Epoch
       55 MSE:
                0.00028307962929829955
       56 MSE:
                0.00029052834725007415
Epoch
```

```
Epoch 57 MSE:
                0.00024958403082564473
Epoch 58 MSE:
                0.00019139026699122041
Epoch 59 MSE:
                0.00015724514378234744
Epoch 60 MSE:
                0.0001654002262512222
Epoch 61 MSE:
                0.0001988519506994635
Epoch 62 MSE:
                0.0002226808137493208
Epoch
      63 MSE:
                0.00021507339261006564
Epoch 64 MSE:
                0.00018364464631304145
Epoch 65 MSE:
                0.0001540029188618064
Epoch 66 MSE:
                0.00014510267646983266
Epoch 67 MSE:
                0.00015524936316069216
Epoch 68 MSE:
                0.00016796936688479036
Epoch 69 MSE:
                0.00016849118401296437
Epoch 70 MSE:
                0.00015558874292764813
Epoch 71 MSE:
                0.00014029211888555437
Epoch 72 MSE:
                0.0001343795156572014
Epoch 73 MSE:
                0.00013950772699899971
Epoch 74 MSE:
                0.0001467464171582833
Epoch 75 MSE:
                0.00014627815107814968
Epoch 76 MSE:
                0.0001369289238937199
Epoch 77 MSE:
                0.00012607501412276179
Epoch 78 MSE:
                0.00012138515012338758
Epoch 79 MSE:
                0.0001237910910276696
Epoch 80 MSE:
                0.00012796830560546368
Epoch 81 MSE:
                0.00012825288285966963
Epoch 82 MSE:
                0.00012363039422780275
Epoch 83 MSE:
                0.00011768559488700703
Epoch 84 MSE:
                0.00011449571320554242
Epoch 85 MSE:
                0.00011476911458885297
Epoch 86 MSE:
                0.00011575558892218396
Epoch 87 MSE:
                0.0001145353089668788
Epoch 88 MSE:
                0.0001110053199226968
Epoch 89 MSE:
                0.00010756103438325226
Epoch 90 MSE:
                0.00010625612776493654
Epoch
      91 MSE:
                0.00010673615906853229
Epoch 92 MSE:
                0.00010693367948988453
Epoch 93 MSE:
                0.0001053813612088561
Epoch 94 MSE:
                0.00010257307440042496
Epoch 95 MSE:
                0.00010017088789027184
Epoch 96 MSE:
                9.917482384480536e-05
Epoch 97 MSE:
                9.904593753162771e-05
Epoch 98 MSE:
                9.853077062871307e-05
Epoch 99 MSE:
                9.70731271081604e-05
```

T-time: 42.455177307128906

Train Score: 0.29 RMSE

Time Step = 50 | Hidden States = 32 | Num Layers = 2

Epoch 0 MSE: 0.04075655713677406 Epoch 1 MSE: 0.04284535348415375 Epoch 2 MSE: 0.03628775104880333 Epoch 3 MSE: 0.03300190716981888 Epoch 4 MSE: 0.03260623663663864 Epoch 5 MSE: 0.030995318666100502 Epoch 6 MSE: 0.026288257911801338 Epoch 7 MSE: 0.01941317692399025 Epoch 8 MSE: 0.01401967741549015 Epoch 9 MSE: 0.008915595710277557 Epoch 10 MSE: 0.0010283333249390125 Epoch 11 MSE: 0.009885257109999657 Epoch 12 MSE: 0.006996167823672295 Epoch 13 MSE: 0.0023384871892631054 Epoch 14 MSE: 0.0014383298112079501 Epoch 15 MSE: 0.0016941205831244588 Epoch 16 MSE: 0.003233431838452816 Epoch 17 MSE: 0.0040593575686216354 Epoch 18 MSE: 0.0036329030990600586 Epoch 19 MSE: 0.002303705085068941 Epoch 20 MSE: 0.0010384410852566361 Epoch 21 MSE: 0.000944638391956687 Epoch 22 MSE: 0.001131431432440877 Epoch 23 MSE: 0.0011630028020590544 Epoch 24 MSE: 0.0017636758275330067 Epoch 25 MSE: 0.001896482310257852 Epoch 26 MSE: 0.0012234507594257593 Epoch 27 MSE: 0.000605455890763551 Epoch 28 MSE: 0.0005808566347695887 Epoch 29 MSE: 0.0006536227301694453 Epoch 30 MSE: 0.0006583320209756494 Epoch 31 MSE: 0.0008069886243902147 Epoch 32 MSE: 0.0009560697362758219 Epoch 33 MSE: 0.0008751584682613611 Epoch 34 MSE: 0.0005768679548054934 Epoch 35 MSE: 0.00031856345594860613 Epoch 36 MSE: 0.0003299250965937972 Epoch 37 MSE: 0.0004728894855361432 Epoch 38 MSE: 0.0004995386698283255 Epoch 39 MSE: 0.00048607285134494305 Epoch 40 MSE: 0.0004820390895474702

```
Epoch
       41 MSE:
                0.00038917901110835373
Epoch
       42 MSE:
                0.00024799376842565835
       43 MSE:
Epoch
                0.00022006651852279902
       44 MSE:
Epoch
                0.0003166179230902344
Epoch
       45 MSE:
                0.0003656914923340082
Epoch
       46 MSE:
                0.00030934519600123167
Epoch
       47 MSE:
                0.0002524334704503417
Epoch
       48 MSE:
                0.00023302419867832214
       49 MSE:
Epoch
                0.00020568695617839694
Epoch
       50 MSE:
                0.00017770285194274038
       51 MSE:
                0.00020212039817124605
Epoch
Epoch
       52 MSE:
                0.0002402968966634944
Epoch
       53 MSE:
                0.00020895634952466935
Epoch
       54 MSE:
                0.00015435910609085113
Epoch
       55 MSE:
                0.00014562375145033002
       56 MSE:
                0.00015625639935024083
Epoch
Epoch
       57 MSE:
                0.00015453518426511437
       58 MSE:
                0.00015440127754118294
Epoch
Epoch
       59 MSE:
                0.00015799846732988954
Epoch
       60 MSE:
                0.00014059807290323079
Epoch
       61 MSE:
                0.00011362275836290792
Epoch
       62 MSE:
                0.00011234173143748194
       63 MSE:
Epoch
                0.00012676768528763205
       64 MSE:
Epoch
                0.00012633661390282214
       65 MSE:
                0.00011498777166707441
Epoch
Epoch
       66 MSE:
                0.00010838118760148063
       67 MSE:
Epoch
                0.00010136724449694157
Epoch
       68 MSE:
                9.452662197872996e-05
       69 MSE:
Epoch
                9.791782213142142e-05
Epoch
       70 MSE:
                0.00010281218419549987
       71 MSE:
Epoch
                9.625746315577999e-05
Epoch
       72 MSE:
                8.583860471844673e-05
Epoch
       73 MSE:
                8.340943168150261e-05
       74 MSE:
Epoch
                8.440535748377442e-05
Epoch
       75 MSE:
                8.320466440636665e-05
Epoch
       76 MSE:
                8.254626300185919e-05
Epoch
       77 MSE:
                8.009742305148393e-05
Epoch
       78 MSE:
                7.412712147925049e-05
       79 MSE:
Epoch
                7.15123096597381e-05
Epoch
       80 MSE:
                7.358710718108341e-05
       81 MSE:
                7.310714136110619e-05
Epoch
       82 MSE:
Epoch
                6.953116826480255e-05
Epoch
       83 MSE:
                6.719074735883623e-05
Epoch
       84 MSE:
                6.551983096869662e-05
Epoch
       85 MSE:
                6.406907050404698e-05
Epoch
       86 MSE:
                6.425779429264367e-05
Epoch
       87 MSE:
                6.349282921291888e-05
       88 MSE:
Epoch
                6.041178494342603e-05
```

Epoch 89 MSE: 5.863324258825742e-05
Epoch 90 MSE: 5.855519702890888e-05
Epoch 91 MSE: 5.7753361033974215e-05
Epoch 92 MSE: 5.657515794155188e-05
Epoch 93 MSE: 5.542938379221596e-05
Epoch 94 MSE: 5.378471178119071e-05
Epoch 95 MSE: 5.2909286750946194e-05
Epoch 96 MSE: 5.285746738081798e-05
Epoch 97 MSE: 5.1871349569410086e-05
Epoch 98 MSE: 5.046280057285912e-05
Epoch 99 MSE: 4.968004577676767656e-05

T-time: 118.29136538505554

Train Score: 0.21 RMSE

Validation Score: 4.30 RMSE

Time Step = 100 | Hidden States = 2 | Num Layers = 1

Epoch 0 MSE: 0.09296241402626038 Epoch 1 MSE: 0.08490736037492752 Epoch 2 MSE: 0.07796050608158112 Epoch 3 MSE: 0.07196546345949173 Epoch 4 MSE: 0.06678205728530884 Epoch 5 MSE: 0.0622895248234272 Epoch 6 MSE: 0.058386825025081635 Epoch 7 MSE: 0.054990459233522415 Epoch 8 MSE: 0.05203188210725784 Epoch 9 MSE: 0.04945502430200577 Epoch 10 MSE: 0.04721391201019287 Epoch 11 MSE: 0.04527059942483902 Epoch 12 MSE: 0.04359336197376251 Epoch 13 MSE: 0.042155180126428604 Epoch 14 MSE: 0.04093251749873161 Epoch 15 MSE: 0.03990435227751732 Epoch 16 MSE: 0.03905146196484566 Epoch 17 MSE: 0.03835587576031685 Epoch 18 MSE: 0.03780050575733185 Epoch 19 MSE: 0.037368934601545334 Epoch 20 MSE: 0.03704529255628586 Epoch 21 MSE: 0.03681425005197525 Epoch 22 MSE: 0.0366610586643219 Epoch 23 MSE: 0.0365716926753521 Epoch 24 MSE: 0.0365329384803772

```
Epoch
       25 MSE:
                0.03653256595134735
Epoch
       26 MSE:
                0.03655946999788284
Epoch
       27 MSE:
                0.03660377487540245
       28 MSE:
Epoch
                0.0366569384932518
Epoch
       29 MSE:
                0.03671179339289665
Epoch
       30 MSE:
                0.0367625467479229
Epoch
       31 MSE:
                0.036804769188165665
Epoch
       32 MSE:
                0.036835283041000366
Epoch 33 MSE:
                0.03685208037495613
Epoch
       34 MSE:
                0.036854200065135956
       35 MSE:
                0.03684153035283089
Epoch
       36 MSE:
Epoch
                0.03681469336152077
Epoch
       37 MSE:
                0.03677484765648842
Epoch
       38 MSE:
                0.036723542958498
Epoch
       39 MSE:
                0.036662567406892776
                0.03659380227327347
Epoch 40 MSE:
Epoch
       41 MSE:
                0.0365191288292408
       42 MSE:
Epoch
                0.03644028678536415
Epoch
       43 MSE:
                0.03635885566473007
Epoch
       44 MSE:
                0.03627614304423332
Epoch
       45 MSE:
                0.03619317337870598
Epoch
      46 MSE:
                0.036110661923885345
Epoch 47 MSE:
                0.03602901101112366
      48 MSE:
Epoch
                0.03594832494854927
Epoch
       49 MSE:
                0.03586842119693756
Epoch
       50 MSE:
                0.035788845270872116
      51 MSE:
Epoch
                0.03570893779397011
Epoch
       52 MSE:
                0.0356278195977211
       53 MSE:
Epoch
                0.03554445877671242
Epoch 54 MSE:
                0.035457707941532135
Epoch 55 MSE:
                0.03536628931760788
Epoch
       56 MSE:
                0.035268861800432205
      57 MSE:
Epoch
                0.035163991153240204
      58 MSE:
Epoch
                0.03505019471049309
Epoch
       59 MSE:
                0.034925904124975204
Epoch
       60 MSE:
                0.03478946164250374
Epoch
       61 MSE:
                0.03463910147547722
Epoch
       62 MSE:
                0.03447289019823074
       63 MSE:
Epoch
                0.03428870067000389
Epoch
       64 MSE:
                0.034084126353263855
       65 MSE:
Epoch
                0.03385641425848007
       66 MSE:
Epoch
                0.033602386713027954
Epoch
       67 MSE:
                0.03331829607486725
       68 MSE:
Epoch
                0.03299974650144577
Epoch
       69 MSE:
                0.03264150395989418
Epoch
       70 MSE:
                0.03223734721541405
Epoch
       71 MSE:
                0.03177986666560173
       72 MSE:
                0.031260229647159576
Epoch
```

```
Epoch 73 MSE: 0.03066794015467167
Epoch 74 MSE:
               0.029990559443831444
Epoch 75 MSE:
               0.02921343222260475
Epoch 76 MSE:
               0.028319498524069786
Epoch 77 MSE:
               0.027289269492030144
Epoch 78 MSE:
               0.02610117197036743
Epoch 79 MSE:
               0.02473251335322857
Epoch 80 MSE:
               0.023161297664046288
Epoch 81 MSE:
               0.021369310095906258
Epoch 82 MSE:
               0.019346803426742554
Epoch 83 MSE:
               0.017098741605877876
Epoch 84 MSE:
               0.014652257785201073
Epoch 85 MSE:
               0.012064670212566853
Epoch 86 MSE:
               0.009432402439415455
Epoch 87 MSE:
               0.00690201623365283
Epoch 88 MSE:
               0.004683455917984247
Epoch 89 MSE:
               0.003051463980227709
Epoch 90 MSE:
               0.002287411829456687
Epoch 91 MSE:
               0.002501443726941943
Epoch 92 MSE:
               0.0034281257539987564
Epoch 93 MSE:
               0.004526535049080849
Epoch 94 MSE:
               0.005260735750198364
Epoch 95 MSE:
               0.005291784647852182
Epoch 96 MSE:
               0.004657451529055834
Epoch 97 MSE:
               0.003696856088936329
Epoch 98 MSE:
               0.0027559753507375717
Epoch 99 MSE:
               0.002018391154706478
```

T-time: 19.67540192604065

Train Score: 1.34 RMSE

Validation Score: 17.04 RMSE

_____ Time Step = 100 | Hidden States = 2 | Num Layers = 2 ______

Epoch 0 MSE: 0.03757014870643616 Epoch 1 MSE: 0.035759087651968 Epoch 2 MSE: 0.03470347076654434 Epoch 3 MSE: 0.034365344792604446 Epoch 4 MSE: 0.03423583135008812 Epoch 5 MSE: 0.033719275146722794 Epoch 6 MSE: 0.03269758075475693 Epoch 7 MSE: 0.031327392905950546 Epoch 8 MSE: 0.029827622696757317

```
Epoch
      9 MSE:
               0.028416592627763748
Epoch
       10 MSE:
                0.027128664776682854
       11 MSE:
Epoch
                0.02559136040508747
       12 MSE:
Epoch
                0.023448366671800613
Epoch
       13 MSE:
                0.020838482305407524
Epoch
       14 MSE:
                0.01840825565159321
Epoch
       15 MSE:
                0.016567770391702652
Epoch
       16 MSE:
                0.014401930384337902
Epoch 17 MSE:
                0.011436816304922104
Epoch
       18 MSE:
                0.008930226787924767
       19 MSE:
                0.00781531073153019
Epoch
       20 MSE:
Epoch
                0.006154195871204138
Epoch
       21 MSE:
                0.0058225481770932674
Epoch
       22 MSE:
                0.005974465515464544
Epoch
       23 MSE:
                0.005686506163328886
                0.006510378327220678
Epoch 24 MSE:
Epoch
       25 MSE:
                0.0059570688754320145
       26 MSE:
Epoch
                0.005662937648594379
Epoch
       27 MSE:
                0.005092678125947714
Epoch
       28 MSE:
                0.004084356129169464
Epoch
       29 MSE:
                0.003281258512288332
       30 MSE:
Epoch
                0.0028001833707094193
Epoch
       31 MSE:
                0.002393109258264303
       32 MSE:
Epoch
                0.0020651654340326786
Epoch
       33 MSE:
                0.001931160455569625
Epoch
       34 MSE:
                0.0019768422935158014
       35 MSE:
Epoch
                0.002096262527629733
Epoch
       36 MSE:
                0.0021933584939688444
       37 MSE:
Epoch
                0.0022300512064248323
Epoch
       38 MSE:
                0.002213100902736187
       39 MSE:
Epoch
                0.002150636864826083
Epoch
       40 MSE:
                0.0020331861451268196
Epoch
       41 MSE:
                0.0018589104292914271
       42 MSE:
                0.0016633066115900874
Epoch
Epoch
       43 MSE:
                0.001505827298387885
Epoch
       44 MSE:
                0.0014224156038835645
Epoch
       45 MSE:
                0.0014003143878653646
Epoch
       46 MSE:
                0.0014050272293388844
       47 MSE:
Epoch
                0.0014197819400578737
Epoch
       48 MSE:
                0.001442149979993701
Epoch 49 MSE:
                0.001451926538720727
       50 MSE:
Epoch
                0.0014167896006256342
Epoch
       51 MSE:
                0.0013361700112000108
Epoch
       52 MSE:
                0.0012440261198207736
Epoch
       53 MSE:
                0.0011633863905444741
Epoch
       54 MSE:
                0.001092401216737926
Epoch
       55 MSE:
                0.0010337869171053171
       56 MSE:
                0.001002084813080728
Epoch
```

```
Epoch 57 MSE:
                0.0009962784824892879
Epoch 58 MSE:
                0.0009943183977156878
Epoch 59 MSE:
                0.0009822127176448703
Epoch
      60 MSE:
                0.0009639847557991743
Epoch 61 MSE:
                0.0009403831791132689
Epoch
      62 MSE:
                0.0009044234175235033
Epoch
       63 MSE:
                0.0008606864721514285
Epoch 64 MSE:
                0.00082381785614416
Epoch 65 MSE:
                0.0007967219571582973
Epoch
      66 MSE:
                0.00077393080573529
Epoch
      67 MSE:
                0.0007589589222334325
Epoch 68 MSE:
                0.0007531272131018341
Epoch 69 MSE:
                0.0007458498002961278
Epoch 70 MSE:
                0.0007334661786444485
Epoch 71 MSE:
                0.0007202313863672316
Epoch 72 MSE:
                0.000702688645105809
Epoch 73 MSE:
                0.0006804171134717762
Epoch 74 MSE:
                0.0006609608535654843
Epoch 75 MSE:
                0.0006443773745559156
Epoch 76 MSE:
                0.0006289047887548804
Epoch
     77 MSE:
                0.0006180350319482386
Epoch 78 MSE:
                0.0006094941636547446
Epoch 79 MSE:
                0.0005992921069264412
Epoch 80 MSE:
                0.0005890168249607086
Epoch 81 MSE:
                0.0005774687160737813
Epoch 82 MSE:
                0.0005631148815155029
Epoch 83 MSE:
                0.000549165706615895
Epoch
      84 MSE:
                0.0005359533824957907
Epoch 85 MSE:
                0.0005230863462202251
Epoch 86 MSE:
                0.0005126994219608605
Epoch 87 MSE:
                0.0005033726920373738
Epoch
      88 MSE:
                0.0004940424696542323
Epoch 89 MSE:
                0.00048536784015595913
Epoch 90 MSE:
                0.00047562248073518276
Epoch
      91 MSE:
                0.0004652483039535582
Epoch 92 MSE:
                0.00045510014751926064
Epoch 93 MSE:
                0.0004446381935849786
Epoch 94 MSE:
                0.0004351628595031798
Epoch 95 MSE:
                0.00042649023816920817
Epoch 96 MSE:
                0.0004181626718491316
Epoch 97 MSE:
                0.0004105399420950562
Epoch 98 MSE:
                0.0004026142123620957
Epoch 99 MSE:
                0.00039456156082451344
T-time: 36.11147928237915
```

Train Score: 0.59 RMSE

Time Step = 100 | Hidden States = 4 | Num Layers = 1

Epoch 0 MSE: 0.047738198190927505 Epoch 1 MSE: 0.040429241955280304 Epoch 2 MSE: 0.03553101792931557 Epoch 3 MSE: 0.03246256336569786 Epoch 4 MSE: 0.0306486077606678 Epoch 5 MSE: 0.029499348253011703 Epoch 6 MSE: 0.028396207839250565 Epoch 7 MSE: 0.026875413954257965 Epoch 8 MSE: 0.02472655288875103 Epoch 9 MSE: 0.02195456065237522Epoch 10 MSE: 0.01871735416352749 Epoch 11 MSE: 0.01528440322726965 Epoch 12 MSE: 0.012003621086478233 Epoch 13 MSE: 0.00923629105091095 Epoch 14 MSE: 0.007214946206659079 Epoch 15 MSE: 0.005834117531776428 Epoch 16 MSE: 0.004652660805732012 Epoch 17 MSE: 0.003391194622963667 Epoch 18 MSE: 0.0023170365020632744 Epoch 19 MSE: 0.0020118425600230694 Epoch 20 MSE: 0.002746606944128871 Epoch 21 MSE: 0.004003746900707483 Epoch 22 MSE: 0.004875405691564083 Epoch 23 MSE: 0.004906369373202324 Epoch 24 MSE: 0.004260003101080656 Epoch 25 MSE: 0.003375283908098936 Epoch 26 MSE: 0.002627784851938486 Epoch 27 MSE: 0.002156247152015567 Epoch 28 MSE: 0.001883818069472909 Epoch 29 MSE: 0.0016774075338616967 Epoch 30 MSE: 0.0014813164016231894 Epoch 31 MSE: 0.0013242029817774892 Epoch 32 MSE: 0.0012551528634503484 Epoch 33 MSE: 0.0012917779386043549 Epoch 34 MSE: 0.0014068282907828689 Epoch 35 MSE: 0.0015432883519679308 Epoch 36 MSE: 0.0016406342620030046 Epoch 37 MSE: 0.0016579123912379146 Epoch 38 MSE: 0.0015854082303121686 Epoch 39 MSE: 0.0014431336894631386Epoch 40 MSE: 0.0012692498276010156

```
Epoch 41 MSE:
                0.0011039464734494686
Epoch
      42 MSE:
                0.0009748924057930708
Epoch
      43 MSE:
                0.0008896940271370113
       44 MSE:
Epoch
                0.000838382460642606
Epoch
      45 MSE:
                0.0008042805711738765
Epoch
      46 MSE:
                0.0007763918838463724
Epoch
       47 MSE:
                0.000755088112782687
Epoch
      48 MSE:
                0.0007476064492948353
Epoch 49 MSE:
                0.0007577589130960405
Epoch
      50 MSE:
                0.0007785861380398273
      51 MSE:
Epoch
                0.00079396553337574
Epoch
      52 MSE:
                0.0007878605392761528
Epoch
      53 MSE:
                0.0007541421218775213
Epoch
       54 MSE:
                0.0007000665063969791
Epoch
      55 MSE:
                0.0006415907992050052
Epoch 56 MSE:
                0.0005942978314124048
Epoch
      57 MSE:
                0.0005659176968038082
      58 MSE:
Epoch
                0.0005544981686398387
Epoch
       59 MSE:
                0.0005521701532416046
Epoch
       60 MSE:
                0.0005510322516784072
Epoch
       61 MSE:
                0.0005471139447763562
Epoch
       62 MSE:
                0.0005405788542702794
Epoch
      63 MSE:
                0.0005332086584530771
       64 MSE:
Epoch
                0.0005256850854493678
Epoch
       65 MSE:
                0.0005166832706891
Epoch
       66 MSE:
                0.0005040796240791678
       67 MSE:
Epoch
                0.000487044540932402
Epoch
       68 MSE:
                0.00046729345922358334
       69 MSE:
Epoch
                0.00044850539416074753
Epoch 70 MSE:
                0.000434272427810356
Epoch 71 MSE:
                0.0004259988490957767
Epoch
      72 MSE:
                0.00042221855255775154
                0.0004197638772893697
Epoch
      73 MSE:
      74 MSE:
                0.0004158549418207258
Epoch
Epoch
      75 MSE:
                0.0004095397307537496
Epoch
      76 MSE:
                0.00040157148032449186
Epoch
     77 MSE:
                0.0003931584069505334
Epoch
      78 MSE:
                0.00038483331445604563
      79 MSE:
Epoch
                0.00037634256295859814
Epoch
      80 MSE:
                0.0003673832688946277
      81 MSE:
                0.0003582986246328801
Epoch
       82 MSE:
Epoch
                0.0003500301099848002
Epoch
       83 MSE:
                0.0003434023237787187
       84 MSE:
Epoch
                0.00033842588891275227
Epoch
      85 MSE:
                0.00033423909917473793
Epoch
       86 MSE:
                0.00032971560722216964
Epoch
       87 MSE:
                0.00032420840580016375
       88 MSE:
                0.0003178456681780517
Epoch
```

Epoch 89 MSE: 0.0003112302510999143 Epoch 90 MSE: 0.0003048937942367047 Epoch 91 MSE: 0.00029898426146246493 Epoch 92 MSE: 0.0002933725481852889 Epoch 93 MSE: 0.0002879634266719222 Epoch 94 MSE: 0.00028285355074331164 Epoch 95 MSE: 0.0002781953080557287 Epoch 96 MSE: 0.0002739467890933156 Epoch 97 MSE: 0.0002698028110899031 Epoch 98 MSE: 0.00026539983809925616 Epoch 99 MSE: 0.0002606010821182281

T-time: 23.211425065994263

Train Score: 0.48 RMSE

Validation Score: 10.24 RMSE

Time Step = 100 | Hidden States = 4 | Num Layers = 2

Epoch 0 MSE: 0.33258312940597534 Epoch 1 MSE: 0.29062601923942566 Epoch 2 MSE: 0.2531641125679016 Epoch 3 MSE: 0.21987710893154144 Epoch 4 MSE: 0.19017575681209564 Epoch 5 MSE: 0.16344496607780457 Epoch 6 MSE: 0.1391313672065735 Epoch 7 MSE: 0.11682521551847458 Epoch 8 MSE: 0.09630223363637924 Epoch 9 MSE: 0.07756947726011276 Epoch 10 MSE: 0.06090836226940155 Epoch 11 MSE: 0.04689425230026245 Epoch 12 MSE: 0.03636058419942856 Epoch 13 MSE: 0.030248815193772316 Epoch 14 MSE: 0.0292274821549654 Epoch 15 MSE: 0.032922111451625824 Epoch 16 MSE: 0.03909347578883171 Epoch 17 MSE: 0.044492024928331375 Epoch 18 MSE: 0.047076307237148285 Epoch 19 MSE: 0.04663035273551941 Epoch 20 MSE: 0.04399454966187477 Epoch 21 MSE: 0.04029930755496025 Epoch 22 MSE: 0.03652936592698097 Epoch 23 MSE: 0.033341217786073685 Epoch 24 MSE: 0.031042836606502533

```
Epoch
      25 MSE:
                0.02966557815670967
Epoch
      26 MSE:
                0.02906852960586548
Epoch
      27 MSE:
                0.02903353050351143
      28 MSE:
Epoch
                0.029331985861063004
Epoch
      29 MSE:
                0.02976262755692005
Epoch
      30 MSE:
                0.030167700722813606
Epoch
       31 MSE:
                0.030436092987656593
Epoch
      32 MSE:
                0.030499888584017754
Epoch 33 MSE:
                0.03032820299267769
Epoch
      34 MSE:
                0.029920300468802452
       35 MSE:
Epoch
                0.029298918321728706
Epoch
       36 MSE:
                0.02850397862493992
Epoch
      37 MSE:
                0.02758663147687912
Epoch
       38 MSE:
                0.026603475213050842
Epoch
      39 MSE:
                0.025610627606511116
Epoch 40 MSE:
                0.02465767227113247
Epoch
      41 MSE:
                0.02378149889409542
       42 MSE:
Epoch
                0.023000568151474
Epoch
       43 MSE:
                0.022310558706521988
Epoch
      44 MSE:
                0.021682891994714737
Epoch
       45 MSE:
                0.02106757089495659
Epoch 46 MSE:
                0.02040144056081772
Epoch 47 MSE:
                0.01962118037045002
Epoch 48 MSE:
                0.01867874339222908
      49 MSE:
                0.017554378136992455
Epoch
Epoch
      50 MSE:
                0.0162627175450325
Epoch 51 MSE:
                0.014849340543150902
Epoch
       52 MSE:
                0.013378355652093887
      53 MSE:
Epoch
                0.011915639042854309
Epoch 54 MSE:
                0.010513297282159328
Epoch 55 MSE:
                0.009200314991176128
Epoch
      56 MSE:
                0.007981760427355766
      57 MSE:
Epoch
                0.006846279837191105
      58 MSE:
                0.005779368337243795
Epoch
Epoch
       59 MSE:
                0.004778633359819651
Epoch
       60 MSE:
                0.00386548088863492
Epoch
       61 MSE:
                0.003087251912802458
Epoch
       62 MSE:
                0.0025059652980417013
       63 MSE:
Epoch
                0.002175077795982361
Epoch
       64 MSE:
                0.002111639128997922
      65 MSE:
                0.002275001723319292
Epoch
       66 MSE:
Epoch
                0.0025655378121882677
       67 MSE:
Epoch
                0.00285543967038393
Epoch
       68 MSE:
                0.0030417221132665873
Epoch
      69 MSE:
                0.0030816704966127872
Epoch
      70 MSE:
                0.002986377105116844
Epoch
      71 MSE:
                0.0027920331340283155
      72 MSE:
Epoch
                0.0025376547127962112
```

```
Epoch 73 MSE:
               0.0022573587484657764
Epoch 74 MSE:
               0.0019800940062850714
Epoch 75 MSE:
               0.0017285466892644763
Epoch 76 MSE:
               0.0015173471765592694
Epoch 77 MSE:
               0.001353548956103623
Epoch 78 MSE:
               0.001238701050169766
Epoch 79 MSE:
               0.0011704335920512676
Epoch 80 MSE:
               0.0011429558508098125
Epoch 81 MSE:
               0.00114717916585505
Epoch 82 MSE:
               0.0011714097345247865
Epoch 83 MSE:
               0.0012029851786792278
Epoch 84 MSE:
               0.001230497844517231
Epoch 85 MSE:
               0.0012457927223294973
Epoch 86 MSE:
               0.0012449806090444326
Epoch 87 MSE:
               0.0012281632516533136
Epoch 88 MSE:
               0.0011981581337749958
Epoch 89 MSE:
               0.0011588805355131626
Epoch 90 MSE:
               0.0011140656424686313
Epoch 91 MSE:
               0.0010667078895494342
Epoch 92 MSE:
               0.001019171206280589
Epoch 93 MSE:
               0.0009736159117892385
Epoch 94 MSE:
               0.0009322951082140207
Epoch 95 MSE:
               0.0008974524680525064
Epoch 96 MSE:
               0.000870835967361927
Epoch 97 MSE:
               0.0008531032362952828
Epoch 98 MSE:
               0.0008434776682406664
Epoch 99 MSE:
               0.0008398796198889613
```

T-time: 44.2719566822052

Train Score: 0.86 RMSE

Validation Score: 15.40 RMSE

_____ Time Step = 100 | Hidden States = 8 | Num Layers = 1 ______

Epoch 0 MSE: 0.05871938541531563 Epoch 1 MSE: 0.04353747144341469 Epoch 2 MSE: 0.03325658291578293 Epoch 3 MSE: 0.027822744101285934 Epoch 4 MSE: 0.026786265894770622 Epoch 5 MSE: 0.0286156814545393 Epoch 6 MSE: 0.03057032823562622 Epoch 7 MSE: 0.03083725832402706Epoch 8 MSE: 0.02938738651573658

```
Epoch 9 MSE:
               0.0269965548068285
Epoch
       10 MSE:
                0.024467412382364273
       11 MSE:
Epoch
                0.02233392745256424
       12 MSE:
Epoch
                0.02081373706459999
Epoch
       13 MSE:
                0.019866300746798515
Epoch
       14 MSE:
                0.01928551308810711
Epoch
       15 MSE:
                0.018792912364006042
Epoch
       16 MSE:
                0.01811734214425087
Epoch 17 MSE:
                0.0170555729418993
Epoch
       18 MSE:
                0.015511000528931618
       19 MSE:
                0.013509504497051239
Epoch
       20 MSE:
Epoch
                0.01119410153478384
Epoch
       21 MSE:
                0.008800046518445015
Epoch
       22 MSE:
                0.00660706078633666
Epoch
       23 MSE:
                0.004855883773416281
Epoch 24 MSE:
                0.0036227693781256676
Epoch
       25 MSE:
                0.002732496475800872
       26 MSE:
Epoch
                0.001933024381287396
Epoch
       27 MSE:
                0.0012859932612627745
Epoch
       28 MSE:
                0.0012038347776979208
       29 MSE:
Epoch
                0.0019754169043153524
       30 MSE:
Epoch
                0.0030916875693947077
Epoch
       31 MSE:
                0.0035461783409118652
       32 MSE:
Epoch
                0.00293860980309546
Epoch
       33 MSE:
                0.0017121084965765476
Epoch
       34 MSE:
                0.000615960278082639
       35 MSE:
Epoch
                0.00016764744941610843
Epoch
       36 MSE:
                0.0003779013641178608
       37 MSE:
Epoch
                0.0008396260673180223
Epoch
      38 MSE:
                0.0011209191288799047
       39 MSE:
                0.0010897974716499448
Epoch
Epoch
       40 MSE:
                0.0008933315984904766
Epoch
       41 MSE:
                0.0007368969381786883
       42 MSE:
                0.0007166825234889984
Epoch
Epoch
       43 MSE:
                0.0007908034021966159
Epoch
       44 MSE:
                0.0008454860653728247
Epoch
       45 MSE:
                0.0007847151136957109
Epoch
       46 MSE:
                0.0005919371033087373
       47 MSE:
Epoch
                0.00034016818972304463
Epoch
       48 MSE:
                0.00014951196499168873
Epoch 49 MSE:
                0.00011041483230656013
       50 MSE:
Epoch
                0.00021423200087156147
Epoch
       51 MSE:
                0.0003512078255880624
Epoch
       52 MSE:
                0.0004017511964775622
Epoch
       53 MSE:
                0.0003428218769840896
Epoch
       54 MSE:
                0.00025104175438173115
Epoch
       55 MSE:
                0.0002077051904052496
       56 MSE:
                0.00022308871848508716
Epoch
```

```
Epoch 57 MSE:
                0.00024785444838926196
Epoch 58 MSE:
                0.00023423777020070702
Epoch 59 MSE:
                0.00017898279475048184
Epoch
      60 MSE:
                0.00011886670836247504
Epoch 61 MSE:
                9.461567969992757e-05
Epoch
      62 MSE:
                0.00011691165855154395
Epoch
      63 MSE:
                0.00016031123232096434
Epoch 64 MSE:
                0.00018712003657128662
Epoch 65 MSE:
                0.00017857567581813782
Epoch 66 MSE:
                0.00014606190961785614
Epoch 67 MSE:
                0.0001158704690169543
Epoch 68 MSE:
                0.00010522508819121867
Epoch 69 MSE:
                0.00011103033466497436
Epoch 70 MSE:
                0.00011755001469282433
Epoch 71 MSE:
                0.00011277392331976444
Epoch 72 MSE:
                9.854247764451429e-05
Epoch 73 MSE:
                8.699481259100139e-05
Epoch 74 MSE:
                8.788908598944545e-05
Epoch 75 MSE:
                9.894956019707024e-05
Epoch 76 MSE:
                0.00010837974696187302
Epoch
     77 MSE:
                0.00010665575973689556
Epoch 78 MSE:
                9.516729915048927e-05
Epoch 79 MSE:
                8.335062739206478e-05
Epoch 80 MSE:
                7.884449587436393e-05
Epoch 81 MSE:
                8.136353426380083e-05
Epoch 82 MSE:
                8.504605648340657e-05
Epoch 83 MSE:
                8.506185258738697e-05
Epoch 84 MSE:
                8.160459401551634e-05
Epoch 85 MSE:
                7.841096521588042e-05
Epoch 86 MSE:
                7.832174014765769e-05
Epoch 87 MSE:
                8.04966693976894e-05
Epoch 88 MSE:
                8.166061161318794e-05
Epoch 89 MSE:
                7.965227268869057e-05
Epoch 90 MSE:
                7.550739974249154e-05
Epoch
      91 MSE:
                7.217404345283285e-05
Epoch
      92 MSE:
                7.153813930926844e-05
Epoch 93 MSE:
                7.287967309821397e-05
Epoch 94 MSE:
                7.401148468488827e-05
Epoch 95 MSE:
                7.356157584581524e-05
Epoch 96 MSE:
                7.202611595857888e-05
Epoch 97 MSE:
               7.081301009748131e-05
Epoch
      98 MSE:
                7.058781920932233e-05
Epoch 99 MSE:
                7.071816071402282e-05
T-time: 22.46944284439087
```

_ . _ _ _ _ _ _

Train Score: 0.25 RMSE

Time Step = 100 | Hidden States = 8 | Num Layers = 2

Epoch 0 MSE: 0.13075894117355347 Epoch 1 MSE: 0.10015342384576797 Epoch 2 MSE: 0.07629898190498352 Epoch 3 MSE: 0.05839548259973526 Epoch 4 MSE: 0.045830946415662766 Epoch 5 MSE: 0.03825041651725769 Epoch 6 MSE: 0.03539297357201576 Epoch 7 MSE: 0.036596767604351044 Epoch 8 MSE: 0.04001840949058533 Epoch 9 MSE: 0.04297458007931709Epoch 10 MSE: 0.04389478638768196 Epoch 11 MSE: 0.04281473532319069 Epoch 12 MSE: 0.04053224250674248 Epoch 13 MSE: 0.03791951760649681 Epoch 14 MSE: 0.03561560437083244 Epoch 15 MSE: 0.033950939774513245 Epoch 16 MSE: 0.03298955038189888 Epoch 17 MSE: 0.032615430653095245 Epoch 18 MSE: 0.032617516815662384 Epoch 19 MSE: 0.032752860337495804 Epoch 20 MSE: 0.032788608223199844 Epoch 21 MSE: 0.032531462609767914 Epoch 22 MSE: 0.031844861805438995 Epoch 23 MSE: 0.030649691820144653 Epoch 24 MSE: 0.02891286462545395 Epoch 25 MSE: 0.026637956500053406 Epoch 26 MSE: 0.023879487067461014 Epoch 27 MSE: 0.020791860297322273 Epoch 28 MSE: 0.017684681341052055 Epoch 29 MSE: 0.014902613125741482 Epoch 30 MSE: 0.012307497672736645 Epoch 31 MSE: 0.009241415187716484 Epoch 32 MSE: 0.005995589308440685 Epoch 33 MSE: 0.004672303795814514 Epoch 34 MSE: 0.005806285887956619 Epoch 35 MSE: 0.007529782596975565 Epoch 36 MSE: 0.007813637144863605 Epoch 37 MSE: 0.006814444437623024 Epoch 38 MSE: 0.0058206734247505665 Epoch 39 MSE: 0.004657034296542406 Epoch 40 MSE: 0.0037331702187657356

```
Epoch
       41 MSE:
                0.003141269786283374
Epoch
       42 MSE:
                0.00284378114156425
       43 MSE:
Epoch
                0.003028601175174117
       44 MSE:
Epoch
                0.003375150728970766
Epoch
       45 MSE:
                0.0036793502513319254
       46 MSE:
Epoch
                0.003819623263552785
Epoch
       47 MSE:
                0.003733944147825241
Epoch
       48 MSE:
                0.003440840868279338
Epoch 49 MSE:
                0.003012491390109062
Epoch
       50 MSE:
                0.00254845037125051
       51 MSE:
                0.002149657579138875
Epoch
Epoch
       52 MSE:
                0.001890439074486494
Epoch
       53 MSE:
                0.0017907461151480675
Epoch
       54 MSE:
                0.0018027947517111897
Epoch
       55 MSE:
                0.0018354766070842743
Epoch 56 MSE:
                0.0018078446155413985
Epoch
       57 MSE:
                0.001689172233454883
       58 MSE:
                0.0015012259827926755
Epoch
Epoch
       59 MSE:
                0.0012924200855195522
Epoch
       60 MSE:
                0.0011097835376858711
Epoch
       61 MSE:
                0.0009835674427449703
Epoch
       62 MSE:
                0.0009224585955962539
Epoch
       63 MSE:
                0.0009138882160186768
       64 MSE:
Epoch
                0.0009293488692492247
       65 MSE:
                0.0009363980498164892
Epoch
Epoch
       66 MSE:
                0.0009136807639151812
       67 MSE:
Epoch
                0.00085994484834373
Epoch
       68 MSE:
                0.0007906720275059342
       69 MSE:
Epoch
                0.0007254399824887514
Epoch
      70 MSE:
                0.0006760186515748501
     71 MSE:
Epoch
                0.0006429825443774462
Epoch
       72 MSE:
                0.000620487320702523
Epoch
       73 MSE:
                0.0006027084891684353
       74 MSE:
Epoch
                0.000586078327614814
Epoch
       75 MSE:
                0.0005672219558618963
Epoch
       76 MSE:
                0.0005414015613496304
Epoch
      77 MSE:
                0.0005052406922914088
Epoch
      78 MSE:
                0.000461429386632517
       79 MSE:
Epoch
                0.0004191585467197001
Epoch
       80 MSE:
                0.0003878757415805012
       81 MSE:
                0.0003697190259117633
Epoch
       82 MSE:
Epoch
                0.0003581104683689773
Epoch
       83 MSE:
                0.00034377191332168877
Epoch
       84 MSE:
                0.0003221968945581466
Epoch
       85 MSE:
                0.00029595629894174635
Epoch
       86 MSE:
                0.0002708534593693912
Epoch
       87 MSE:
                0.00025062114582397044
       88 MSE:
                0.00023523569689132273
Epoch
```

Epoch 89 MSE: 0.00022313122462946922 Epoch 90 MSE: 0.00021329012815840542 Epoch 91 MSE: 0.00020463964028749615 Epoch 92 MSE: 0.00019494745356496423 Epoch 93 MSE: 0.0001822451886255294 Epoch 94 MSE: 0.0001675381645327434 Epoch 95 MSE: 0.00015468036872334778 Epoch 96 MSE: 0.00014645629562437534 Epoch 97 MSE: 0.00014128095062915236 Epoch 98 MSE: 0.0001349310332443565 Epoch 99 MSE: 0.0001253420632565394

T-time: 57.300408124923706

Train Score: 0.33 RMSE

Validation Score: 12.26 RMSE

Time Step = 100 | Hidden States = 16 | Num Layers = 1

Epoch 0 MSE: 0.033007457852363586 Epoch 1 MSE: 0.03091491013765335 Epoch 2 MSE: 0.02837585099041462 Epoch 3 MSE: 0.026143671944737434 Epoch 4 MSE: 0.023220224305987358 Epoch 5 MSE: 0.020351404324173927 Epoch 6 MSE: 0.016576416790485382 Epoch 7 MSE: 0.011893784627318382 Epoch 8 MSE: 0.006953970063477755 Epoch 9 MSE: 0.0017223827308043838 Epoch 10 MSE: 0.0013125704135745764 Epoch 11 MSE: 0.009196791797876358 Epoch 12 MSE: 0.0055700428783893585 Epoch 13 MSE: 0.0032399592455476522 Epoch 14 MSE: 0.00031839017174206674 Epoch 15 MSE: 0.0005764124798588455 Epoch 16 MSE: 0.001517368364147842 Epoch 17 MSE: 0.0017492903862148523 Epoch 18 MSE: 0.00199122354388237 Epoch 19 MSE: 0.0024767257273197174 Epoch 20 MSE: 0.0026487696450203657 Epoch 21 MSE: 0.0022579950746148825 Epoch 22 MSE: 0.001706449082121253 Epoch 23 MSE: 0.0013539415085688233 Epoch 24 MSE: 0.0010543138487264514

```
Epoch
       25 MSE:
                0.0005725394585169852
Epoch
       26 MSE:
                0.00014546909369528294
Epoch
       27 MSE:
                0.0001523545797681436
       28 MSE:
Epoch
                0.0003923018812201917
Epoch
       29 MSE:
                0.0004900931962765753
Epoch
       30 MSE:
                0.0006314293714240193
Epoch
       31 MSE:
                0.0008382342057302594
Epoch
       32 MSE:
                0.0007413790444843471
Epoch
      33 MSE:
                0.0004564863338600844
Epoch
       34 MSE:
                0.0003044781042262912
       35 MSE:
                0.00020962183771189302
Epoch
Epoch
       36 MSE:
                9.004815365187824e-05
Epoch
       37 MSE:
                7.70361875765957e-05
Epoch
       38 MSE:
                0.00018023853772319853
Epoch
       39 MSE:
                0.0002591356751509011
Epoch 40 MSE:
                0.00027108623180538416
Epoch
       41 MSE:
                0.00028217636281624436
       42 MSE:
Epoch
                0.00029861938674002886
Epoch
       43 MSE:
                0.0002603227330837399
Epoch
       44 MSE:
                0.00017500758985988796
Epoch
       45 MSE:
                0.00011495018407003954
Epoch
       46 MSE:
                9.315997158410028e-05
Epoch 47 MSE:
                6.925844354555011e-05
       48 MSE:
Epoch
                5.489864997798577e-05
       49 MSE:
                8.475816866848618e-05
Epoch
       50 MSE:
Epoch
                0.00012363979476504028
      51 MSE:
Epoch
                0.00012850981147494167
Epoch
       52 MSE:
                0.00012260876246728003
       53 MSE:
Epoch
                0.0001190205366583541
Epoch 54 MSE:
                9.450591460336e-05
Epoch 55 MSE:
                6.148278043838218e-05
Epoch
       56 MSE:
                5.051636617281474e-05
      57 MSE:
Epoch
                5.269060784485191e-05
       58 MSE:
                5.208008224144578e-05
Epoch
Epoch
       59 MSE:
                5.824834079248831e-05
Epoch
       60 MSE:
                7.204093708423898e-05
Epoch
       61 MSE:
                7.644862489541993e-05
Epoch
       62 MSE:
                6.985025538597256e-05
Epoch
       63 MSE:
                6.423674494726583e-05
Epoch
       64 MSE:
                5.858202348463237e-05
       65 MSE:
Epoch
                4.8044832510640845e-05
Epoch
       66 MSE:
                4.122583050047979e-05
       67 MSE:
Epoch
                4.3134481529705226e-05
Epoch
       68 MSE:
                4.5853415940655395e-05
Epoch
       69 MSE:
                4.726354018202983e-05
Epoch
       70 MSE:
                5.1199367590015754e-05
Epoch
       71 MSE:
                5.3080344514455646e-05
       72 MSE:
                4.936729237670079e-05
Epoch
```

```
Epoch 73 MSE: 4.555728446575813e-05
Epoch 74 MSE: 4.3411084334366024e-05
Epoch 75 MSE: 4.040699786855839e-05
Epoch 76 MSE:
               3.901268064510077e-05
Epoch 77 MSE:
               4.0871440432965755e-05
Epoch 78 MSE:
               4.243810326443054e-05
Epoch 79 MSE:
               4.274189268471673e-05
               4.3413896491983905e-05
Epoch 80 MSE:
Epoch 81 MSE:
               4.310686563258059e-05
               4.106956475879997e-05
Epoch 82 MSE:
Epoch 83 MSE:
               3.9579474105266854e-05
Epoch 84 MSE:
               3.9053120417520404e-05
Epoch 85 MSE:
               3.841067518806085e-05
Epoch 86 MSE:
               3.852399822790176e-05
Epoch 87 MSE:
               3.9513273804914206e-05
Epoch 88 MSE:
               3.984130671597086e-05
Epoch 89 MSE:
               3.962711707572453e-05
Epoch 90 MSE:
               3.94948037865106e-05
Epoch 91 MSE:
               3.883907265844755e-05
Epoch 92 MSE:
               3.7981633795425296e-05
Epoch 93 MSE:
               3.775999721256085e-05
Epoch 94 MSE:
               3.7747679016320035e-05
Epoch 95 MSE:
               3.7722173146903515e-05
Epoch 96 MSE:
               3.80156998289749e-05
               3.819164339802228e-05
Epoch 97 MSE:
Epoch 98 MSE:
               3.7964946386637166e-05
Epoch 99 MSE:
               3.774505603360012e-05
```

T-time: 40.32364630699158

Train Score: 0.18 RMSE

Validation Score: 5.10 RMSE

Time Step = 100 | Hidden States = 16 | Num Layers = 2

Epoch 0 MSE: 0.05612000823020935 Epoch 1 MSE: 0.040825534611940384 Epoch 2 MSE: 0.036387186497449875 Epoch 3 MSE: 0.0393560491502285 Epoch 4 MSE: 0.038261983543634415 Epoch 5 MSE: 0.035820700228214264 Epoch 6 MSE: 0.03441285714507103 Epoch 7 MSE: 0.03395697474479675 Epoch 8 MSE: 0.033856626600027084

```
9 MSE:
               0.033652182668447495
Epoch
Epoch
       10 MSE:
                0.03307400271296501
Epoch
       11 MSE:
                0.031984031200408936
       12 MSE:
Epoch
                0.030316993594169617
Epoch
       13 MSE:
                0.028052616864442825
Epoch
       14 MSE:
                0.02523685246706009
Epoch
       15 MSE:
                0.02193993516266346
Epoch
       16 MSE:
                0.017852814868092537
       17 MSE:
Epoch
                0.011992462910711765
Epoch
       18 MSE:
                0.0050193630158901215
       19 MSE:
                0.0019249601755291224
Epoch
       20 MSE:
Epoch
                0.005014969035983086
Epoch
       21 MSE:
                0.00858478806912899
Epoch
       22 MSE:
                0.008789739571511745
Epoch
       23 MSE:
                0.006146143190562725
                0.003181742038577795
Epoch
       24 MSE:
Epoch
       25 MSE:
                0.0016477768076583743
       26 MSE:
Epoch
                0.0015514163533225656
Epoch
       27 MSE:
                0.0021096887066960335
Epoch
       28 MSE:
                0.0027487846091389656
       29 MSE:
Epoch
                0.0032250836957246065
       30 MSE:
Epoch
                0.003366369754076004
Epoch
       31 MSE:
                0.003054184839129448
       32 MSE:
Epoch
                0.002364411950111389
       33 MSE:
                0.0016039781039580703
Epoch
Epoch
       34 MSE:
                0.0011582180159166455
       35 MSE:
Epoch
                0.0011258212616667151
Epoch
       36 MSE:
                0.0012073814868927002
       37 MSE:
Epoch
                0.0012979598250240088
Epoch
       38 MSE:
                0.001528239226900041
       39 MSE:
                0.001707576448097825
Epoch
Epoch
       40 MSE:
                0.0015654080780223012
Epoch
       41 MSE:
                0.0012145832879468799
       42 MSE:
                0.0009441454894840717
Epoch
Epoch
       43 MSE:
                0.0007875671144574881
Epoch
       44 MSE:
                0.0006568100652657449
Epoch
       45 MSE:
                0.0006310896133072674
Epoch
       46 MSE:
                0.0007485960959456861
       47 MSE:
Epoch
                0.0008649544906802475
Epoch
       48 MSE:
                0.0008532965439371765
       49 MSE:
                0.000738271395675838
Epoch
       50 MSE:
Epoch
                0.0006036448758095503
Epoch
       51 MSE:
                0.00047335520503111184
Epoch
       52 MSE:
                0.0003596632450353354
Epoch
       53 MSE:
                0.0003292229084763676
Epoch
       54 MSE:
                0.0003842818841803819
Epoch
       55 MSE:
                0.00042623362969607115
       56 MSE:
                0.00040683706174604595
Epoch
```

```
Epoch 57 MSE:
                0.00035065438714809716
Epoch 58 MSE:
                0.0002621755702421069
Epoch 59 MSE:
                0.00017883522377815098
Epoch 60 MSE:
                0.00016204423445742577
Epoch 61 MSE:
                0.00019108592823613435
Epoch 62 MSE:
                0.00021690888388548046
Epoch
      63 MSE:
                0.00021717888012062758
Epoch 64 MSE:
                0.00017623172607272863
Epoch 65 MSE:
                0.00011559934500837699
Epoch 66 MSE:
                8.6177620687522e-05
Epoch 67 MSE:
                9.424237941857427e-05
Epoch 68 MSE:
                0.00011704571807058528
Epoch 69 MSE:
                0.00012625240196939558
Epoch 70 MSE:
                0.00010153144830837846
Epoch 71 MSE:
                6.935966666787863e-05
Epoch 72 MSE:
                5.3974075854057446e-05
Epoch 73 MSE:
                6.393851072061807e-05
Epoch 74 MSE:
                8.24724993435666e-05
Epoch 75 MSE:
               7.99925546743907e-05
Epoch 76 MSE:
                6.214877794263884e-05
Epoch 77 MSE:
                4.5683329517487437e-05
Epoch 78 MSE:
                4.8481746489414945e-05
Epoch 79 MSE:
                6.107030640123412e-05
Epoch 80 MSE:
                6.412016955437139e-05
                5.556858377531171e-05
Epoch 81 MSE:
Epoch 82 MSE:
                4.363113112049177e-05
Epoch 83 MSE:
               4.520146831055172e-05
Epoch 84 MSE:
                5.198198778089136e-05
Epoch 85 MSE:
                5.570732901105657e-05
Epoch 86 MSE:
                4.885900125373155e-05
Epoch 87 MSE:
               4.253157749189995e-05
Epoch 88 MSE:
                4.316795093473047e-05
Epoch 89 MSE:
                4.775456545758061e-05
Epoch 90 MSE:
                4.874771912000142e-05
Epoch 91 MSE:
                4.3873664253624156e-05
Epoch 92 MSE:
                4.049495328217745e-05
Epoch 93 MSE:
                4.104908657609485e-05
Epoch 94 MSE:
                4.412795169628225e-05
Epoch 95 MSE:
                4.324260225985199e-05
Epoch 96 MSE:
                4.0357947000302374e-05
Epoch 97 MSE:
               3.8291669625323266e-05
Epoch 98 MSE:
                3.970882607973181e-05
Epoch 99 MSE:
                4.082772647961974e-05
T-time: 96.80281043052673
```

Train Score: 0.19 RMSE

Time Step = 100 | Hidden States = 32 | Num Layers = 1

```
Epoch 0 MSE: 0.05514080077409744
Epoch 1 MSE: 0.03680483251810074
Epoch 2 MSE: 0.03248664364218712
Epoch 3 MSE:
              0.034939780831336975
Epoch 4 MSE:
              0.033051010221242905
Epoch 5 MSE:
              0.028489310294389725
Epoch 6 MSE: 0.024737447500228882
Epoch 7 MSE:
              0.022404339164495468
Epoch 8 MSE:
              0.020453404635190964
Epoch 9 MSE:
              0.017284277826547623
Epoch 10 MSE: 0.01122631411999464
Epoch 11 MSE: 0.002772070001810789
Epoch 12 MSE:
               0.025505080819129944
Epoch 13 MSE:
               0.0025287307798862457
Epoch 14 MSE:
               0.003223186358809471
Epoch 15 MSE:
               0.008347534574568272
Epoch 16 MSE:
               0.010463183745741844
Epoch 17 MSE:
               0.009586819447577
Epoch 18 MSE:
               0.007009110413491726
Epoch 19 MSE:
               0.004196471069008112
Epoch 20 MSE:
               0.002506537828594446
Epoch 21 MSE:
               0.0027336992789059877
Epoch 22 MSE:
               0.004276775289326906
Epoch 23 MSE:
               0.005116014275699854
Epoch 24 MSE:
               0.003982208669185638
Epoch 25 MSE:
               0.0018489181529730558
Epoch 26 MSE:
               0.0004248559707775712
Epoch 27 MSE:
               0.0004209510807413608
Epoch 28 MSE:
               0.0013618790544569492
Epoch 29 MSE:
               0.0022700177505612373
Epoch 30 MSE:
               0.00243561714887619
Epoch 31 MSE:
               0.0018296110210940242
Epoch 32 MSE:
               0.0009753741323947906
Epoch 33 MSE:
               0.00048026468721218407
Epoch 34 MSE:
               0.0005769110866822302
Epoch 35 MSE:
               0.0009738946100696921
Epoch 36 MSE:
               0.0011721730697900057
Epoch 37 MSE:
               0.0009679895592853427
Epoch 38 MSE:
               0.0005756299360655248
Epoch 39 MSE:
               0.00031497771851718426
Epoch 40 MSE:
               0.0003196657926309854
```

```
Epoch
       41 MSE:
                0.0005070872139185667
Epoch
       42 MSE:
                0.000704207515809685
       43 MSE:
                0.0007737756823189557
Epoch
       44 MSE:
Epoch
                0.0006773490458726883
Epoch
       45 MSE:
                0.0004755813570227474
       46 MSE:
Epoch
                0.00028319910052232444
Epoch
       47 MSE:
                0.00019943130610045046
Epoch
       48 MSE:
                0.0002450211613904685
Epoch 49 MSE:
                0.0003486427594907582
Epoch
      50 MSE:
                0.0004056979960296303
       51 MSE:
                0.00036749590071849525
Epoch
Epoch
       52 MSE:
                0.0002752554719336331
Epoch
       53 MSE:
                0.00020819748169742525
Epoch
       54 MSE:
                0.00020802089420612901
Epoch
       55 MSE:
                0.0002529455814510584
                0.00028962548822164536
Epoch 56 MSE:
Epoch
       57 MSE:
                0.0002811622398439795
       58 MSE:
Epoch
                0.0002316344325663522
Epoch
       59 MSE:
                0.0001762215979397297
Epoch
       60 MSE:
                0.0001507862762082368
Epoch
       61 MSE:
                0.0001648826291784644
Epoch
       62 MSE:
                0.00019736927060876042
Epoch
       63 MSE:
                0.0002165812038583681
       64 MSE:
Epoch
                0.0002068586618406698
       65 MSE:
                0.0001782803883543238
Epoch
Epoch
       66 MSE:
                0.00015354788047261536
       67 MSE:
Epoch
                0.00014724383072461933
Epoch
       68 MSE:
                0.00015614062431268394
       69 MSE:
Epoch
                0.00016572153253946453
Epoch
      70 MSE:
                0.00016414849960710853
     71 MSE:
                0.00015143907512538135
Epoch
Epoch
       72 MSE:
                0.0001376225263811648
Epoch
      73 MSE:
                0.00013279738777782768
       74 MSE:
                0.00013810672680847347
Epoch
Epoch
       75 MSE:
                0.0001454928278690204
Epoch
       76 MSE:
                0.00014595576794818044
Epoch
      77 MSE:
                0.0001378853339701891
Epoch
      78 MSE:
                0.0001274741516681388
       79 MSE:
Epoch
                0.0001219045152538456
Epoch
       80 MSE:
                0.00012289703590795398
       81 MSE:
                0.00012638041516765952
Epoch
       82 MSE:
Epoch
                0.00012722429528366774
       83 MSE:
Epoch
                0.00012384251749608666
       84 MSE:
Epoch
                0.00011879372323164716
Epoch
       85 MSE:
                0.00011565864406293258
Epoch
       86 MSE:
                0.00011555750825209543
       87 MSE:
Epoch
                0.0001164903151220642
       88 MSE:
                0.00011574193922569975
Epoch
```

Epoch 89 MSE: 0.00011266471119597554 Epoch 90 MSE: 0.00010906199167948216 Epoch 91 MSE: 0.00010709855996537954 Epoch 92 MSE: 0.00010714538802858442 Epoch 93 MSE: 0.00010767691856017336 Epoch 94 MSE: 0.00010700178245315328 Epoch 95 MSE: 0.00010487296822248027 Epoch 96 MSE: 0.00010246042074868456 Epoch 97 MSE: 0.00010097625636262819 Epoch 98 MSE: 0.0001004978985292837 Epoch 99 MSE: 0.00010011578706325963

T-time: 114.4332389831543

Train Score: 0.30 RMSE

Validation Score: 6.77 RMSE

Time Step = 100 | Hidden States = 32 | Num Layers = 2

Epoch 0 MSE: 0.04098782315850258 Epoch 1 MSE: 0.04290059208869934 Epoch 2 MSE: 0.036442894488573074 Epoch 3 MSE: 0.0331280343234539 Epoch 4 MSE: 0.03268846496939659 Epoch 5 MSE: 0.031057482585310936 Epoch 6 MSE: 0.026306288316845894 Epoch 7 MSE: 0.019328348338603973 Epoch 8 MSE: 0.013887966051697731 Epoch 9 MSE: 0.009003966115415096 Epoch 10 MSE: 0.0012328331358730793 Epoch 11 MSE: 0.01022490207105875 Epoch 12 MSE: 0.007071347441524267 Epoch 13 MSE: 0.00198581675067544 Epoch 14 MSE: 0.001956649124622345 Epoch 15 MSE: 0.0018859220435842872 Epoch 16 MSE: 0.003131464822217822 Epoch 17 MSE: 0.004039675462990999 Epoch 18 MSE: 0.003790466347709298 Epoch 19 MSE: 0.002522542607039213 Epoch 20 MSE: 0.0010272635845467448 Epoch 21 MSE: 0.0007319175638258457 Epoch 22 MSE: 0.0014505661092698574 Epoch 23 MSE: 0.001264269114471972 Epoch 24 MSE: 0.0014669690281152725

```
Epoch
       25 MSE:
                0.0018170725088566542
Epoch
       26 MSE:
                0.0013878023019060493
       27 MSE:
                0.0005819277139380574
Epoch
       28 MSE:
Epoch
                0.00035537168150767684
Epoch
       29 MSE:
                0.0007637825328856707
       30 MSE:
Epoch
                0.0009391079656779766
Epoch
       31 MSE:
                0.0007736757397651672
Epoch
       32 MSE:
                0.0007155466009862721
      33 MSE:
Epoch
                0.0007591740577481687
Epoch
       34 MSE:
                0.0006654232856817544
       35 MSE:
                0.0004100064397789538
Epoch
       36 MSE:
Epoch
                0.00026211427757516503
Epoch
       37 MSE:
                0.00043497595470398664
Epoch
       38 MSE:
                0.0006242632516659796
Epoch
       39 MSE:
                0.0004971547168679535
                0.00032200218993239105
      40 MSE:
Epoch
Epoch
       41 MSE:
                0.00031003530602902174
       42 MSE:
Epoch
                0.00033296082983724773
Epoch
       43 MSE:
                0.0002996637485921383
Epoch
       44 MSE:
                0.0002792877785395831
Epoch
       45 MSE:
                0.0003244302642997354
Epoch
       46 MSE:
                0.00034329656045883894
Epoch 47 MSE:
                0.00025819247821345925
       48 MSE:
Epoch
                0.00017091778863687068
       49 MSE:
                0.0001850099506555125
Epoch
Epoch
       50 MSE:
                0.00024023013247642666
       51 MSE:
Epoch
                0.00024037256662268192
Epoch
       52 MSE:
                0.00019916730525437742
       53 MSE:
Epoch
                0.00018046483455691487
Epoch
      54 MSE:
                0.00017566421593073756
Epoch 55 MSE:
                0.00015344523126259446
Epoch
       56 MSE:
                0.00014380928769242018
       57 MSE:
Epoch
                0.0001643252617213875
       58 MSE:
                0.00017542358546052128
Epoch
Epoch
       59 MSE:
                0.00015084365440998226
Epoch
       60 MSE:
                0.00012063344911439344
Epoch
       61 MSE:
                0.00012006692122668028
Epoch
       62 MSE:
                0.00013236081576906145
       63 MSE:
Epoch
                0.00012896247790195048
Epoch
       64 MSE:
                0.00012134990538470447
       65 MSE:
Epoch
                0.000119765245472081
       66 MSE:
Epoch
                0.00011171623191330582
       67 MSE:
                9.978882007999346e-05
Epoch
Epoch
       68 MSE:
                0.00010087693226523697
Epoch
       69 MSE:
                0.00010919192573055625
Epoch
       70 MSE:
                0.00010507577826501802
Epoch
       71 MSE:
                9.307213622378185e-05
       72 MSE:
Epoch
                8.93928954610601e-05
```

```
Epoch 73 MSE:
               9.116641012951732e-05
Epoch 74 MSE:
               8.921301923692226e-05
Epoch 75 MSE:
               8.684850763529539e-05
Epoch 76 MSE:
               8.659071318106726e-05
Epoch 77 MSE:
               8.256512955995277e-05
Epoch 78 MSE:
               7.697152614127845e-05
Epoch 79 MSE:
               7.71156046539545e-05
Epoch 80 MSE:
               7.91876227594912e-05
Epoch 81 MSE:
               7.652526255697012e-05
Epoch 82 MSE:
               7.222809654194862e-05
Epoch 83 MSE:
               7.09464366082102e-05
Epoch 84 MSE:
               7.034221198409796e-05
Epoch 85 MSE:
               6.880534056108445e-05
Epoch 86 MSE:
               6.817879329901189e-05
Epoch 87 MSE:
               6.70961890136823e-05
Epoch 88 MSE:
               6.425727042369545e-05
Epoch 89 MSE:
               6.264723197091371e-05
Epoch 90 MSE:
               6.30088834441267e-05
Epoch 91 MSE:
               6.217448390088975e-05
Epoch 92 MSE:
               6.006090552546084e-05
Epoch 93 MSE:
               5.885513382963836e-05
Epoch 94 MSE:
               5.807931302115321e-05
Epoch 95 MSE:
               5.703369606635533e-05
Epoch 96 MSE:
               5.644217526423745e-05
Epoch 97 MSE:
               5.56419872737024e-05
Epoch 98 MSE:
               5.408280048868619e-05
Epoch 99 MSE:
               5.315728412824683e-05
T-time: 229.83534979820251
```

Train Score: 0.22 RMSE

-----Validation Score: 4.94 RMSE

```
[35]: LSTM_results = pd.DataFrame(LSTM_results, columns=['time_step', 'num_layers', \cup \'hidden_dim', 'trainScore', 'valScore'], index = None)
```

```
[36]:
          time_step num_layers hidden_dim trainScore
                                                           valScore
               20.0
                            2.0
                                       32.0
      0
                                                0.183898
                                                           3.353715
               30.0
                            2.0
                                       32.0
      1
                                                0.191065
                                                           3.398010
               50.0
                            2.0
                                       32.0
                                                0.210327
                                                           4.301537
```

3	100.0	2.0	16.0	0.190670	4.511294
4	50.0	2.0	16.0	0.191541	4.528789
5	100.0	2.0	32.0	0.217563	4.937522
6	50.0	1.0	16.0	0.183526	5.014984
7	30.0	1.0	16.0	0.185471	5.037486
8	100.0	1.0	16.0	0.183330	5.103107
9	20.0	1.0	16.0	0.189064	5.119752
10	30.0	2.0	16.0	0.199778	5.293988
11	30.0	1.0	8.0	0.250768	5.803946
12	50.0	1.0	8.0	0.250364	5.835172
13	20.0	1.0	8.0	0.252050	5.862777
14	100.0	1.0	8.0	0.250940	5.981001
15	20.0	1.0	32.0	0.248382	6.055101
16	20.0	2.0	16.0	0.209868	6.119395
17	30.0	1.0	32.0	0.273482	6.347491
18	50.0	1.0	32.0	0.294004	6.640990
19	100.0	1.0	32.0	0.298576	6.774301
20	50.0	1.0	4.0	0.483148	10.029259
21	30.0	1.0	4.0	0.490937	10.049406
22	100.0	1.0	4.0	0.481717	10.236452
23	20.0	1.0	4.0	0.508500	10.256740
24	50.0	2.0	8.0	0.332756	12.093705
25	30.0	2.0	8.0	0.328463	12.103140
26	100.0	2.0	8.0	0.334082	12.263771
27	20.0	2.0	8.0	0.378380	12.322964
28	30.0	2.0	2.0	0.592207	13.141265
29	50.0	2.0	2.0	0.589061	13.207722
30	20.0	2.0	2.0	0.620932	13.352711
31	100.0	2.0	2.0	0.592736	13.520443
32	30.0	2.0	4.0	0.866593	15.074994
33	50.0	2.0	4.0	0.861307	15.130204
34	20.0	2.0	4.0	0.877747	15.173122
35	100.0	2.0	4.0	0.864794	15.404663
36	20.0	1.0	2.0	1.473281	16.385214
37	30.0	1.0	2.0	1.397408	16.527496
38	50.0	1.0	2.0	1.359005	16.672426
39	100.0	1.0	2.0	1.340623	17.035766

0.13 Selecting Best Model (LSTM Model)

```
[37]: best_lstm_model = LSTM_results.iloc[0]
best_lstm_model
```

```
[37]: time_step 20.000000
num_layers 2.000000
hidden_dim 32.000000
trainScore 0.183898
```

```
valScore 3.353715
Name: 0, dtype: float64
```

```
[38]: input_dim = 1
  output_dim = 1
  num_epochs = 100
  lr = 0.01
  loss_type = torch.nn.MSELoss(reduction='mean')
  optimiser = torch.optim.Adam

hidden_dim = int(best_lstm_model['hidden_dim'])
  num_layers = int(best_lstm_model['num_layers'])
  time_step = int(best_lstm_model['time_step'])

torch.manual_seed(42)
  tuned_lstm = LSTM_model(input_dim = input_dim, hidden_dim = hidden_dim,u_loutput_dim = output_dim, layer_dim = num_layers)
  tuned_lstm = to_device(tuned_lstm, device)

evaluate_single_model(tuned_lstm, num_epochs, lr, loss_type, optimiser,u_lotime_step)
```

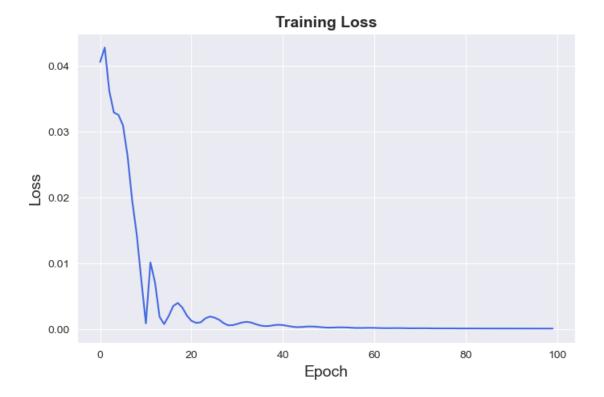
```
Epoch 0 MSE: 0.040618978440761566
Epoch 1 MSE: 0.04281147941946983
Epoch 2 MSE: 0.036195024847984314
Epoch 3 MSE: 0.03292616829276085
Epoch 4 MSE: 0.032557085156440735
Epoch 5 MSE: 0.030960144475102425
Epoch 6 MSE: 0.026295436546206474
Epoch 7 MSE: 0.019574686884880066
Epoch 8 MSE: 0.014389541931450367
Epoch 9 MSE: 0.007475757040083408
Epoch 10 MSE: 0.0008210205123759806
Epoch 11 MSE: 0.010090870782732964
Epoch 12 MSE: 0.0070607322268188
Epoch 13 MSE:
               0.0018260730430483818
Epoch 14 MSE: 0.0007192532648332417
Epoch 15 MSE: 0.001957071479409933
Epoch 16 MSE:
               0.0034813072998076677
Epoch 17 MSE:
               0.0039337510243058205
Epoch 18 MSE: 0.0032134391367435455
Epoch 19 MSE:
               0.0019866065122187138
Epoch 20 MSE:
               0.0012014649109914899
Epoch 21 MSE: 0.0009045402985066175
Epoch 22 MSE: 0.000983517151325941
Epoch 23 MSE:
               0.0015868934569880366
Epoch 24 MSE:
               0.00186759268399328
Epoch 25 MSE: 0.0017075836658477783
```

```
Epoch
       26 MSE:
                0.0013904622755944729
Epoch
       27 MSE:
                0.0008669569506309927
       28 MSE:
Epoch
                0.0005355679895728827
       29 MSE:
Epoch
                0.0005577965057455003
Epoch
       30 MSE:
                0.0007416111184284091
Epoch
       31 MSE:
                0.000952484377194196
Epoch
       32 MSE:
                0.0010651820339262486
Epoch
       33 MSE:
                0.000964015256613493
       34 MSE:
Epoch
                0.0007188546005636454
Epoch
       35 MSE:
                0.000508075871039182
       36 MSE:
                0.0004137598443776369
Epoch
       37 MSE:
Epoch
                0.0004381434991955757
Epoch
       38 MSE:
                0.00054739456390962
Epoch
       39 MSE:
                0.0006173465517349541
Epoch
       40 MSE:
                0.0005628871149383485
Epoch 41 MSE:
                0.00044543895637616515
Epoch
       42 MSE:
                0.00032515102066099644
       43 MSE:
                0.0002531992504373193
Epoch
Epoch
       44 MSE:
                0.0002722999488469213
Epoch
       45 MSE:
                0.0003296692157164216
Epoch
       46 MSE:
                0.00035123637644574046
Epoch
       47 MSE:
                0.00033084998722188175
      48 MSE:
Epoch
                0.00027451166533865035
       49 MSE:
Epoch
                0.00020464873523451388
       50 MSE:
                0.00017633654351811856
Epoch
Epoch
       51 MSE:
                0.0001937545748660341
       52 MSE:
Epoch
                0.00021363218547776341
Epoch
       53 MSE:
                0.00022324759629555047
       54 MSE:
Epoch
                0.00020291823602747172
Epoch 55 MSE:
                0.00015792869089636952
Epoch 56 MSE:
                0.00013213518832344562
Epoch
       57 MSE:
                0.00013046184903942049
Epoch
       58 MSE:
                0.00013931546709500253
       59 MSE:
Epoch
                0.00015011505456641316
Epoch
       60 MSE:
                0.00014165484753903002
Epoch
       61 MSE:
                0.00011667511716950685
Epoch
       62 MSE:
                9.995536674978212e-05
Epoch
       63 MSE:
                9.635627793613821e-05
       64 MSE:
Epoch
                0.00010215606016572565
Epoch
       65 MSE:
                0.00010930553253274411
       66 MSE:
                0.0001021002244669944
Epoch
       67 MSE:
Epoch
                8.75506448210217e-05
Epoch
       68 MSE:
                7.922462100395933e-05
Epoch
       69 MSE:
                7.783198816468939e-05
Epoch
       70 MSE:
                8.237096335506067e-05
Epoch
       71 MSE:
                8.350572170456871e-05
Epoch
       72 MSE:
                7.578958320664242e-05
       73 MSE:
                6.776477675884962e-05
Epoch
```

```
Epoch 74 MSE: 6.405951717169955e-05
Epoch 75 MSE: 6.484367622761056e-05
Epoch 76 MSE:
               6.721611134707928e-05
Epoch 77 MSE:
               6.424181628972292e-05
Epoch 78 MSE:
               5.865002458449453e-05
Epoch 79 MSE:
               5.511551717063412e-05
Epoch 80 MSE:
               5.4543936130357906e-05
Epoch 81 MSE:
               5.61417436983902e-05
Epoch 82 MSE:
               5.509438778972253e-05
Epoch 83 MSE:
               5.172540477360599e-05
Epoch 84 MSE:
               4.908813934889622e-05
Epoch 85 MSE:
               4.818529851036146e-05
Epoch 86 MSE:
               4.9039434088626876e-05
Epoch 87 MSE:
               4.837533560930751e-05
Epoch 88 MSE:
               4.616101068677381e-05
Epoch 89 MSE: 4.4178199459565803e-05
Epoch 90 MSE:
               4.345014167483896e-05
Epoch 91 MSE:
               4.385017746244557e-05
Epoch 92 MSE:
               4.3200554500799626e-05
Epoch 93 MSE:
               4.1761846659937873e-05
Epoch 94 MSE:
               4.043874650960788e-05
Epoch 95 MSE:
               4.012057252111845e-05
Epoch 96 MSE: 4.0292685298481956e-05
Epoch 97 MSE:
               3.9715570892440155e-05
Epoch 98 MSE:
               3.875664697261527e-05
Epoch 99 MSE:
               3.797909812419675e-05
T-time: 35.99087166786194
```

Train Score: 0.18 RMSE

Validation Score: 3.35 RMSE



0.14 Model Architecture (GRU)

```
class GRU_model(nn.Module):
    def __init__(self, input_dim, hidden_dim, layer_dim, output_dim):
        super(GRU_model, self).__init__()
        self.hidden_dim = hidden_dim
        self.layer_dim = layer_dim

        self.gru = nn.GRU(input_dim, hidden_dim, layer_dim, batch_first=True)
        self.fc = nn.Linear(hidden_dim, output_dim)

    def forward(self, x):
        h0 = Variable(torch.zeros(self.layer_dim, x.size(0), self.hidden_dim,_u
        device = device))
        out, (hn) = self.gru(x, (h0.detach()))
        out = self.fc(out[:, -1, :])
        return out
```

```
[40]: gc.collect() torch.cuda.empty_cache()
```

0.15 GRU Model

```
[41]: | input_dim = 1
     output_dim = 1
     num_epochs = 100
     lr = 0.01
     loss_type = torch.nn.MSELoss(reduction = 'mean')
     optimiser = torch.optim.Adam
     hidden_dim = int(best_lstm_model['hidden_dim'])
     num_layers = int(best_lstm_model['num_layers'])
     time_step = int(best_lstm_model['time_step'])
     torch.manual seed(42)
     gru = GRU_model(input_dim = input_dim, hidden_dim = hidden_dim, output_dim = __
      →output_dim, layer_dim = num_layers)
     gru = to_device(gru, device)
     evaluate_single_model(gru, num_epochs, lr, loss_type, optimiser, time_step)
     Epoch 0 MSE:
                   0.07179559022188187
     Epoch 1 MSE: 0.053293388336896896
     Epoch 2 MSE: 0.04245859757065773
     Epoch 3 MSE: 0.02891470678150654
     Epoch 4 MSE: 0.028615588322281837
     Epoch 5 MSE: 0.028290200978517532
     Epoch 6 MSE: 0.020927928388118744
     Epoch 7 MSE: 0.011481642723083496
     Epoch 8 MSE: 0.008736717514693737
     Epoch 9 MSE:
                   0.009971647523343563
     Epoch 10 MSE: 0.002672072034329176
     Epoch 11 MSE: 0.002599109197035432
     Epoch 12 MSE: 0.009029964916408062
     Epoch 13 MSE:
                    0.0048012034967541695
     Epoch 14 MSE:
                    0.000365995365427807
     Epoch 15 MSE:
                    0.0012147922534495592
     Epoch 16 MSE:
                    0.0032251854427158833
     Epoch 17 MSE:
                    0.003329699393361807
     Epoch 18 MSE:
                    0.0024801664985716343
     Epoch 19 MSE: 0.0020592212677001953
                    0.0021666716784238815
     Epoch 20 MSE:
     Epoch 21 MSE:
                    0.0021524960175156593
     Epoch 22 MSE:
                    0.0015332387993112206
     Epoch 23 MSE:
                    0.0005607558996416628
     Epoch 24 MSE:
                    0.0001422767381882295
     Epoch 25 MSE:
                    0.0008216415881179273
     Epoch 26 MSE:
                    0.001618026290088892
```

Epoch 27 MSE: 0.001312705921009183

```
Epoch
      28 MSE:
                0.00048756232718005776
Epoch
      29 MSE:
                0.00017417124763596803
Epoch 30 MSE:
                0.00037566316314041615
      31 MSE:
Epoch
                0.0005903263227082789
Epoch
       32 MSE:
                0.00057415192713961
Epoch
      33 MSE:
                0.00044022814836353064
Epoch
       34 MSE:
                0.0003897933929692954
Epoch
      35 MSE:
                0.00045812551979906857
Epoch 36 MSE:
                0.000488189427414909
Epoch
      37 MSE:
                0.0003477517166174948
      38 MSE:
                0.0001291118242079392
Epoch
Epoch
      39 MSE:
                4.772728789248504e-05
Epoch
      40 MSE:
                0.00016554231115151197
Epoch
      41 MSE:
                0.0003175752644892782
Epoch 42 MSE:
                0.0003260724770370871
Epoch 43 MSE:
                0.00020462312386371195
Epoch 44 MSE:
                0.00010212827328359708
      45 MSE:
                9.807762398850173e-05
Epoch
Epoch
       46 MSE:
                0.0001326723286183551
Epoch
      47 MSE:
                0.00013018090976402164
Epoch
       48 MSE:
                0.00010243273572996259
Epoch 49 MSE:
                0.00010117741476278752
Epoch 50 MSE:
                0.00013013722491450608
Epoch 51 MSE:
                0.0001431655400665477
      52 MSE:
                0.00010955549078062177
Epoch
Epoch 53 MSE:
                5.572067675529979e-05
Epoch 54 MSE:
                3.4837958082789555e-05
Epoch
      55 MSE:
                6.10963543294929e-05
      56 MSE:
Epoch
                9.267429413739592e-05
Epoch 57 MSE:
                8.996023098006845e-05
Epoch 58 MSE:
                6.48604691377841e-05
Epoch
      59 MSE:
                5.12432525283657e-05
Epoch
       60 MSE:
                5.43672067578882e-05
      61 MSE:
Epoch
                5.522068022401072e-05
Epoch
       62 MSE:
                4.6621895307907835e-05
Epoch
       63 MSE:
                4.1491861338727176e-05
Epoch
       64 MSE:
                4.876060120295733e-05
Epoch
       65 MSE:
                5.7778754126047716e-05
       66 MSE:
Epoch
                5.371328006731346e-05
Epoch
      67 MSE:
                3.9405083953170106e-05
Epoch 68 MSE:
                3.0961389711592346e-05
       69 MSE:
Epoch
                3.514246054692194e-05
Epoch
      70 MSE:
                4.230751801514998e-05
Epoch
     71 MSE:
                4.2306124669266865e-05
Epoch 72 MSE:
                3.7418903957586735e-05
Epoch
      73 MSE:
                3.515679782140069e-05
Epoch
      74 MSE:
                3.5786368243861943e-05
      75 MSE:
                3.440362706896849e-05
Epoch
```

```
Epoch 76 MSE: 3.100948015344329e-05
Epoch 77 MSE: 3.0363396945176646e-05
Epoch 78 MSE:
               3.333540735184215e-05
Epoch 79 MSE:
               3.516208380460739e-05
Epoch 80 MSE:
               3.276917777839117e-05
Epoch 81 MSE:
               2.9066435672575608e-05
Epoch 82 MSE:
               2.8185382689116523e-05
Epoch 83 MSE:
               2.968939588754438e-05
Epoch 84 MSE:
               3.0328046705108136e-05
Epoch 85 MSE:
               2.9376946258707903e-05
Epoch 86 MSE:
               2.8730630219797604e-05
Epoch 87 MSE:
               2.8911943445564248e-05
Epoch 88 MSE:
               2.8512082280940376e-05
Epoch 89 MSE:
               2.725705417105928e-05
Epoch 90 MSE:
               2.6677844289224595e-05
Epoch 91 MSE:
               2.7400868930271827e-05
Epoch 92 MSE:
               2.802954077196773e-05
Epoch 93 MSE:
               2.7431246053311042e-05
Epoch 94 MSE:
               2.638915611896664e-05
Epoch 95 MSE:
               2.6084591809194535e-05
Epoch 96 MSE:
               2.6323717975174077e-05
Epoch 97 MSE:
               2.6283149054506794e-05
Epoch 98 MSE: 2.5976780307246372e-05
Epoch 99 MSE: 2.5904790163622238e-05
```

T-time: 56.14676237106323

Train Score: 0.15 RMSE

Validation Score: 4.23 RMSE



```
[42]: gc.collect() torch.cuda.empty_cache()
```

0.16 Hyper Parameters Tuning

```
[43]: input_dim = 1
  output_dim = 1
  num_epochs = 100
  lr = 0.01
  loss_type = torch.nn.MSELoss(reduction = 'mean')
  optimiser = torch.optim.Adam

num_layers = [1, 2]
  sliding_windows = [20, 30, 50, 100]
  hidden_dims = [2, 4, 8, 16, 32]

GRU_results=[]

for time_step in sliding_windows:
    for hidden_dim in hidden_dims:
        for layers in num_layers:
        gc.collect()
```

Time Step = 20 | Hidden States = 2 | Num Layers = 1

```
Epoch 0 MSE: 0.07427381724119186
Epoch 1 MSE: 0.06199593096971512
Epoch 2 MSE: 0.052362293004989624
Epoch 3 MSE: 0.04557616263628006
Epoch 4 MSE: 0.04164762794971466
Epoch 5 MSE: 0.04021786153316498
Epoch 6 MSE: 0.040409237146377563
Epoch 7 MSE: 0.040988076478242874
Epoch 8 MSE: 0.04094001278281212
Epoch 9 MSE: 0.03987399488687515
Epoch 10 MSE: 0.03793422877788544
Epoch 11 MSE: 0.03552033379673958
Epoch 12 MSE: 0.03306340053677559
Epoch 13 MSE: 0.03089897148311138
Epoch 14 MSE: 0.029210686683654785
Epoch 15 MSE: 0.02802242711186409
Epoch 16 MSE: 0.02722751721739769
Epoch 17 MSE: 0.02664337493479252
Epoch 18 MSE: 0.026074957102537155
Epoch 19 MSE: 0.025368213653564453
Epoch 20 MSE: 0.024440977722406387
Epoch 21 MSE: 0.023288598284125328
Epoch 22 MSE: 0.021969566121697426
Epoch 23 MSE: 0.02057962864637375
Epoch 24 MSE: 0.019222039729356766
```

```
Epoch
       25 MSE:
                0.017980000004172325
Epoch
       26 MSE:
                0.016896188259124756
Epoch
       27 MSE:
                0.01596393994987011
       28 MSE:
Epoch
                0.015133019536733627
Epoch
       29 MSE:
                0.014329414814710617
Epoch
       30 MSE:
                0.013482862152159214
Epoch
       31 MSE:
                0.012551860883831978
Epoch
       32 MSE:
                0.011536533944308758
Epoch
      33 MSE:
                0.010475149378180504
Epoch
       34 MSE:
                0.009427042677998543
       35 MSE:
                0.008449368178844452
Epoch
Epoch
       36 MSE:
                0.007576439063996077
Epoch
       37 MSE:
                0.006808874197304249
Epoch
       38 MSE:
                0.0061164796352386475
Epoch
       39 MSE:
                0.005453894380480051
Epoch
      40 MSE:
                0.00478263758122921
Epoch
       41 MSE:
                0.004089698661118746
       42 MSE:
                0.0033938074484467506
Epoch
Epoch
       43 MSE:
                0.0027362515684217215
Epoch
       44 MSE:
                0.00216062949039042
Epoch
       45 MSE:
                0.001691576442681253
Epoch
       46 MSE:
                0.0013237284729257226
Epoch 47 MSE:
                0.0010275529930368066
       48 MSE:
Epoch
                0.0007691361242905259
       49 MSE:
                0.0005316450260579586
Epoch
Epoch
       50 MSE:
                0.00032424204982817173
       51 MSE:
Epoch
                0.00017240027955267578
Epoch
       52 MSE:
                9.640928328735754e-05
       53 MSE:
Epoch
                9.336364746559411e-05
Epoch
       54 MSE:
                0.00013602017133962363
Epoch 55 MSE:
                0.00018968460790347308
Epoch
       56 MSE:
                0.00023372108989860862
       57 MSE:
Epoch
                0.00027021983987651765
       58 MSE:
                0.0003136376617476344
Epoch
Epoch
       59 MSE:
                0.00037180280196480453
Epoch
       60 MSE:
                0.00043533139978535473
Epoch
       61 MSE:
                0.00048393019824288785
Epoch
       62 MSE:
                0.0005024914862588048
       63 MSE:
Epoch
                0.0004918229533359408
Epoch
       64 MSE:
                0.0004653285723179579
       65 MSE:
                0.00043641813681460917
Epoch
       66 MSE:
Epoch
                0.0004087611159775406
Epoch
       67 MSE:
                0.0003770762123167515
Epoch
       68 MSE:
                0.0003357111709192395
Epoch
       69 MSE:
                0.00028592508169822395
Epoch
       70 MSE:
                0.00023562849673908204
Epoch
       71 MSE:
                0.00019317348778713495
       72 MSE:
                0.0001616086228750646
Epoch
```

```
Epoch 73 MSE:
               0.0001381462934659794
Epoch 74 MSE:
               0.00011823291424661875
Epoch 75 MSE:
               9.990417311200872e-05
Epoch 76 MSE:
               8.478669042233378e-05
Epoch 77 MSE:
               7.567019201815128e-05
Epoch 78 MSE:
               7.342913886532187e-05
Epoch 79 MSE:
               7.604226266266778e-05
Epoch 80 MSE:
               8.016462379600853e-05
Epoch 81 MSE:
               8.350540156243369e-05
Epoch 82 MSE:
               8.592683298047632e-05
Epoch 83 MSE:
               8.8622429757379e-05
Epoch 84 MSE:
               9.242795931641012e-05
Epoch 85 MSE:
               9.68316089711152e-05
Epoch 86 MSE:
               0.00010038333130069077
Epoch 87 MSE:
               0.00010190946341026574
Epoch 88 MSE:
               0.00010136658238479868
Epoch 89 MSE:
               9.96645976556465e-05
Epoch 90 MSE:
               9.77692543528974e-05
Epoch 91 MSE:
               9.59543467615731e-05
Epoch 92 MSE:
               9.380844130646437e-05
Epoch 93 MSE:
               9.085464262170717e-05
Epoch 94 MSE:
               8.71349693625234e-05
Epoch 95 MSE:
               8.323891961481422e-05
Epoch 96 MSE:
               7.982892566360533e-05
Epoch 97 MSE:
               7.715661195106804e-05
Epoch 98 MSE:
               7.50015169614926e-05
Epoch 99 MSE:
               7.302097947103903e-05
T-time: 7.868276357650757
```

Train Score: 0.25 RMSE Validation Score: 7.23 RMSE

_____ Time Step = 20 | Hidden States = 2 | Num Layers = 2 ______

```
Epoch 0 MSE: 0.045359112322330475
Epoch 1 MSE: 0.039316803216934204
Epoch 2 MSE: 0.03677363321185112
Epoch 3 MSE:
              0.036986544728279114
Epoch 4 MSE:
              0.038217950612306595
Epoch 5 MSE: 0.0388665571808815
Epoch 6 MSE: 0.03855627775192261
Epoch 7 MSE:
              0.03766573593020439
Epoch 8 MSE: 0.036702487617731094
```

```
Epoch 9 MSE:
               0.03603684902191162
Epoch
      10 MSE:
                0.035816438496112823
Epoch 11 MSE:
                0.03596315532922745
       12 MSE:
Epoch
                0.03624643012881279
Epoch
       13 MSE:
                0.03641818091273308
Epoch
       14 MSE:
                0.036337342113256454
Epoch
       15 MSE:
                0.0360105074942112
Epoch 16 MSE:
                0.03554949909448624
Epoch 17 MSE:
                0.035095442086458206
Epoch 18 MSE:
                0.03475082665681839
       19 MSE:
                0.03453965485095978
Epoch
      20 MSE:
Epoch
                0.0344054140150547
Epoch
      21 MSE:
                0.034246426075696945
Epoch
      22 MSE:
                0.03397081047296524
Epoch 23 MSE:
                0.03354085609316826
Epoch 24 MSE:
                0.03298453614115715
Epoch
      25 MSE:
                0.03237337991595268
      26 MSE:
Epoch
                0.031780943274497986
Epoch
      27 MSE:
                0.03124014474451542
Epoch
      28 MSE:
                0.030720017850399017
Epoch
       29 MSE:
                0.03014206327497959
      30 MSE:
Epoch
                0.029434675350785255
Epoch 31 MSE:
                0.028583258390426636
      32 MSE:
Epoch
                0.027634739875793457
Epoch
      33 MSE:
                0.026658780872821808
Epoch
       34 MSE:
                0.02569584734737873
      35 MSE:
Epoch
                0.02472626604139805
Epoch
       36 MSE:
                0.023686202242970467
      37 MSE:
Epoch
                0.02252454310655594
Epoch 38 MSE:
                0.021250350400805473
      39 MSE:
                0.019922493025660515
Epoch
Epoch
       40 MSE:
                0.018588155508041382
Epoch
      41 MSE:
                0.01723315566778183
      42 MSE:
                0.015812352299690247
Epoch
Epoch
       43 MSE:
                0.014328480698168278
Epoch
      44 MSE:
                0.012849307619035244
Epoch 45 MSE:
                0.011434501968324184
Epoch 46 MSE:
                0.01006469689309597
Epoch 47 MSE:
                0.008695329539477825
Epoch 48 MSE:
                0.007367945741862059
Epoch 49 MSE:
                0.006181653123348951
      50 MSE:
Epoch
                0.005161214619874954
Epoch
      51 MSE:
                0.004270038101822138
Epoch
      52 MSE:
                0.003549232380464673
Epoch
      53 MSE:
                0.0030483962036669254
Epoch
       54 MSE:
                0.002696921583265066
Epoch
       55 MSE:
                0.0024582487531006336
       56 MSE:
                0.0023713998962193727
Epoch
```

```
Epoch 57 MSE:
                0.002362725790590048
Epoch 58 MSE:
                0.0023585420567542315
Epoch 59 MSE:
                0.0023586605675518513
Epoch
      60 MSE:
                0.002313755452632904
Epoch 61 MSE:
                0.0021858953405171633
Epoch
      62 MSE:
                0.0020013595931231976
Epoch
       63 MSE:
                0.0017750668339431286
Epoch 64 MSE:
                0.0015156699810177088
Epoch 65 MSE:
                0.0012660635402426124
Epoch
      66 MSE:
                0.001069521065801382
Epoch
      67 MSE:
                0.0009378553950227797
Epoch 68 MSE:
                0.0008730322006158531
Epoch
      69 MSE:
                0.0008755728485994041
Epoch 70 MSE:
                0.0009236691403202713
Epoch 71 MSE:
                0.0009811271447688341
Epoch 72 MSE:
                0.0010236420203000307
Epoch 73 MSE:
                0.00103769451379776
Epoch 74 MSE:
                0.0010133739560842514
Epoch
     75 MSE:
                0.0009530010866001248
Epoch 76 MSE:
                0.000873230688739568
Epoch
     77 MSE:
                0.0007918361807242036
Epoch 78 MSE:
                0.0007207508897408843
Epoch 79 MSE:
                0.0006698269280605018
Epoch 80 MSE:
                0.000644032668787986
Epoch 81 MSE:
                0.0006383350701071322
Epoch 82 MSE:
                0.0006440553697757423
Epoch 83 MSE:
                0.0006543242488987744
Epoch
      84 MSE:
                0.0006608282565139234
Epoch 85 MSE:
                0.0006565372459590435
Epoch 86 MSE:
                0.0006409371853806078
Epoch 87 MSE:
                0.0006162203499116004
Epoch
      88 MSE:
                0.0005852091126143932
      89 MSE:
Epoch
                0.0005536253447644413
      90 MSE:
Epoch
                0.0005266482476145029
Epoch
      91 MSE:
                0.0005060643889009953
Epoch 92 MSE:
                0.0004926988622173667
Epoch 93 MSE:
                0.0004859081527683884
Epoch 94 MSE:
                0.0004823938070330769
Epoch 95 MSE:
                0.0004791116516571492
Epoch 96 MSE:
                0.0004741851589642465
Epoch 97 MSE:
                0.0004658664111047983
Epoch
      98 MSE:
                0.0004539701039902866
     99 MSE:
                0.0004399411554913968
T-time: 14.854719877243042
```

Train Score: 0.63 RMSE

Validation Score: 13.78 RMSE

Time Step = 20 | Hidden States = 4 | Num Layers = 1 ______

Epoch 0 MSE: 0.10166198760271072 Epoch 1 MSE: 0.07806313782930374 Epoch 2 MSE: 0.05883245915174484 Epoch 3 MSE: 0.04377719759941101 Epoch 4 MSE: 0.03265264630317688 Epoch 5 MSE: 0.025117725133895874 Epoch 6 MSE: 0.020722882822155952 Epoch 7 MSE: 0.018919575959444046 Epoch 8 MSE: 0.019068384543061256 Epoch 9 MSE: 0.020457273349165916 Epoch 10 MSE: 0.0223575159907341 Epoch 11 MSE: 0.024120664224028587 Epoch 12 MSE: 0.02527637593448162 Epoch 13 MSE: 0.025580625981092453 Epoch 14 MSE: 0.025000352412462234 Epoch 15 MSE: 0.02365824207663536 Epoch 16 MSE: 0.02176825702190399 Epoch 17 MSE: 0.019579490646719933 Epoch 18 MSE: 0.0173338633030653 Epoch 19 MSE: 0.01523686945438385 Epoch 20 MSE: 0.013439159840345383 Epoch 21 MSE: 0.012027110904455185 Epoch 22 MSE: 0.011021466925740242 Epoch 23 MSE: 0.01038355752825737 Epoch 24 MSE: 0.010028253309428692 Epoch 25 MSE: 0.009842008352279663 Epoch 26 MSE: 0.009703303687274456 Epoch 27 MSE: 0.009502442553639412 Epoch 28 MSE: 0.009157726541161537 Epoch 29 MSE: 0.008625898510217667 Epoch 30 MSE: 0.007905689999461174 Epoch 31 MSE: 0.0070346142165362835 Epoch 32 MSE: 0.006079884711652994 Epoch 33 MSE: 0.00512509373947978 Epoch 34 MSE: 0.004254325293004513 Epoch 35 MSE: 0.0035358506720513105 Epoch 36 MSE: 0.0030078254640102386 Epoch 37 MSE: 0.0026691833045333624 Epoch 38 MSE: 0.002479171846061945 Epoch 39 MSE: 0.002367986598983407 Epoch 40 MSE:

0.0022576460614800453

```
Epoch
       41 MSE:
                0.002087211702018976
Epoch
       42 MSE:
                0.0018327593570575118
       43 MSE:
Epoch
                0.0015134746208786964
       44 MSE:
Epoch
                0.0011813404271379113
Epoch
       45 MSE:
                0.0008991578943096101
       46 MSE:
Epoch
                0.0007161666289903224
Epoch
       47 MSE:
                0.0006506379577331245
Epoch
       48 MSE:
                0.0006853343802504241
Epoch 49 MSE:
                0.0007764505571685731
Epoch
       50 MSE:
                0.0008714900468476117
       51 MSE:
                0.0009284497937187552
Epoch
Epoch
       52 MSE:
                0.00092888786457479
Epoch
       53 MSE:
                0.000880623294506222
Epoch
       54 MSE:
                0.000810269033536315
Epoch
       55 MSE:
                0.0007495417376048863
       56 MSE:
                0.0007212022901512682
Epoch
Epoch
       57 MSE:
                0.0007302173762582242
       58 MSE:
                0.0007634639041498303
Epoch
Epoch
       59 MSE:
                0.0007975375046953559
Epoch
       60 MSE:
                0.0008104608859866858
Epoch
       61 MSE:
                0.0007913341396488249
Epoch
       62 MSE:
                0.0007435626466758549
Epoch
       63 MSE:
                0.0006811103667132556
       64 MSE:
Epoch
                0.000620791397523135
       65 MSE:
                0.0005748863914050162
Epoch
Epoch
       66 MSE:
                0.0005472490447573364
       67 MSE:
Epoch
                0.0005337849725037813
Epoch
       68 MSE:
                0.0005260804900899529
       69 MSE:
Epoch
                0.0005159564898349345
Epoch
       70 MSE:
                0.0004988853470422328
      71 MSE:
Epoch
                0.0004751472733914852
Epoch
       72 MSE:
                0.0004487660771701485
Epoch
       73 MSE:
                0.0004251095524523407
       74 MSE:
                0.00040837915730662644
Epoch
Epoch
       75 MSE:
                0.0004000109329354018
Epoch
       76 MSE:
                0.0003984702634625137
Epoch
       77 MSE:
                0.0004002848581876606
Epoch
       78 MSE:
                0.0004016882448922843
       79 MSE:
Epoch
                0.0004000976332463324
Epoch
       80 MSE:
                0.00039485006709583104
       81 MSE:
Epoch
                0.0003870254149660468
       82 MSE:
Epoch
                0.0003785977605730295
       83 MSE:
Epoch
                0.00037139010964892805
Epoch
       84 MSE:
                0.0003663043607957661
Epoch
       85 MSE:
                0.00036308926064521074
Epoch
       86 MSE:
                0.00036064497544430196
Epoch
       87 MSE:
                0.0003576378512661904
       88 MSE:
                0.0003531143011059612
Epoch
```

Epoch 89 MSE: 0.00034685645368881524 Epoch 90 MSE: 0.0003393735096324235 Epoch 91 MSE: 0.0003315881476737559 Epoch 92 MSE: 0.00032440011273138225 Epoch 93 MSE: 0.000318326783599332 Epoch 94 MSE: 0.0003133659192826599 Epoch 95 MSE: 0.0003091025573667139 Epoch 96 MSE: 0.0003049775550607592 Epoch 97 MSE: 0.00030057146796025336 Epoch 98 MSE: 0.00029577489476650953 Epoch 99 MSE: 0.00029078577063046396

T-time: 7.513941287994385

Train Score: 0.51 RMSE

Validation Score: 11.72 RMSE

Time Step = 20 | Hidden States = 4 | Num Layers = 2

Epoch 0 MSE: 0.14354208111763 Epoch 1 MSE: 0.1094016283750534 Epoch 2 MSE: 0.08209074288606644 Epoch 3 MSE: 0.061887696385383606 Epoch 4 MSE: 0.04875456169247627 Epoch 5 MSE: 0.04232359305024147 Epoch 6 MSE: 0.04159177467226982 Epoch 7 MSE: 0.04451731964945793 Epoch 8 MSE: 0.04833493009209633 Epoch 9 MSE: 0.050794053822755814 Epoch 10 MSE: 0.05097775533795357 Epoch 11 MSE: 0.04909618943929672 Epoch 12 MSE: 0.045912984758615494 Epoch 13 MSE: 0.042290203273296356 Epoch 14 MSE: 0.03893335163593292 Epoch 15 MSE: 0.036288369446992874 Epoch 16 MSE: 0.03453632444143295 Epoch 17 MSE: 0.033642590045928955 Epoch 18 MSE: 0.03342723101377487 Epoch 19 MSE: 0.03363541141152382 Epoch 20 MSE: 0.03399727866053581 Epoch 21 MSE: 0.03427331522107124 Epoch 22 MSE: 0.03428471088409424 Epoch 23 MSE: 0.03392963483929634 Epoch 24 MSE: 0.03318701311945915

```
Epoch
       25 MSE:
                0.03210940212011337
Epoch
       26 MSE:
                0.03080698847770691
Epoch
       27 MSE:
                0.029424214735627174
       28 MSE:
Epoch
                0.028110815212130547
Epoch
       29 MSE:
                0.02698957547545433
Epoch
       30 MSE:
                0.026125628501176834
Epoch
       31 MSE:
                0.02550508826971054
Epoch
       32 MSE:
                0.02503308095037937
Epoch
       33 MSE:
                0.02455822192132473
Epoch
       34 MSE:
                0.023920834064483643
       35 MSE:
                0.023008620366454124
Epoch
       36 MSE:
Epoch
                0.021797023713588715
Epoch
       37 MSE:
                0.02035764791071415
Epoch
       38 MSE:
                0.018831858411431313
Epoch
       39 MSE:
                0.017378490418195724
Epoch 40 MSE:
                0.016110775992274284
Epoch
       41 MSE:
                0.015041886828839779
       42 MSE:
Epoch
                0.014064633287489414
Epoch
       43 MSE:
                0.01299327053129673
Epoch
       44 MSE:
                0.011671879328787327
Epoch
       45 MSE:
                0.01009434461593628
Epoch
       46 MSE:
                0.008438142016530037
Epoch 47 MSE:
                0.006958047393709421
       48 MSE:
Epoch
                0.005794252268970013
       49 MSE:
                0.004849734250456095
Epoch
Epoch
       50 MSE:
                0.0038935551419854164
       51 MSE:
Epoch
                0.0028395371045917273
Epoch
       52 MSE:
                0.0019038417376577854
       53 MSE:
Epoch
                0.0014064520364627242
Epoch
       54 MSE:
                0.0013286888133734465
Epoch 55 MSE:
                0.0012476807460188866
Epoch
       56 MSE:
                0.001022628741338849
       57 MSE:
Epoch
                0.0010440998012199998
       58 MSE:
                0.0014522321289405227
Epoch
Epoch
       59 MSE:
                0.0017911741742864251
Epoch
       60 MSE:
                0.0018480918370187283
Epoch
       61 MSE:
                0.001967518124729395
Epoch
       62 MSE:
                0.002215736312791705
       63 MSE:
Epoch
                0.002222658833488822
Epoch
       64 MSE:
                0.00201100530102849
       65 MSE:
                0.0018792476039379835
Epoch
       66 MSE:
Epoch
                0.00178143463563174
       67 MSE:
                0.0015429704217240214
Epoch
       68 MSE:
Epoch
                0.001263863523490727
Epoch
       69 MSE:
                0.0011021568207070231
Epoch
       70 MSE:
                0.0010056104511022568
Epoch
       71 MSE:
                0.0008740611374378204
       72 MSE:
                0.0007483737426809967
Epoch
```

```
Epoch 73 MSE:
               0.0007046855171211064
Epoch 74 MSE:
               0.0007201741682365537
Epoch 75 MSE:
               0.0007280966965481639
Epoch 76 MSE:
               0.0007207093294709921
Epoch 77 MSE:
               0.0007347110658884048
Epoch 78 MSE:
               0.000776006723754108
Epoch 79 MSE:
               0.0008094629156403244
Epoch 80 MSE:
               0.0008131163194775581
Epoch 81 MSE:
               0.0008035387727431953
Epoch 82 MSE:
               0.00080142542719841
Epoch 83 MSE:
               0.000799578323494643
Epoch 84 MSE:
               0.0007792931282892823
Epoch 85 MSE:
               0.0007420675246976316
Epoch 86 MSE:
               0.0007067152764648199
Epoch 87 MSE:
               0.0006810595514252782
Epoch 88 MSE:
               0.0006545695359818637
Epoch 89 MSE:
               0.0006206498364917934
Epoch 90 MSE:
               0.0005893167108297348
Epoch 91 MSE:
               0.0005705606890842319
Epoch 92 MSE:
               0.0005591451190412045
Epoch 93 MSE:
               0.0005460354732349515
Epoch 94 MSE:
               0.0005339609924703836
Epoch 95 MSE:
               0.0005300022894516587
Epoch 96 MSE:
               0.0005310289561748505
Epoch 97 MSE:
               0.0005288598476909101
Epoch 98 MSE:
               0.0005237737204879522
Epoch 99 MSE:
               0.0005210444796830416
```

T-time: 14.80426573753357

Train Score: 0.68 RMSE

Validation Score: 12.69 RMSE

_____ Time Step = 20 | Hidden States = 8 | Num Layers = 1

Epoch 0 MSE: 0.21357010304927826 Epoch 1 MSE: 0.16476970911026 Epoch 2 MSE: 0.12439016997814178 Epoch 3 MSE: 0.09209439903497696 Epoch 4 MSE: 0.0675990954041481 Epoch 5 MSE: 0.05050116032361984 Epoch 6 MSE: 0.040242090821266174 Epoch 7 MSE: 0.03601611405611038 Epoch 8 MSE: 0.036574043333530426

```
Epoch
      9 MSE:
               0.040004193782806396
Epoch
       10 MSE:
                0.04396714270114899
Epoch
       11 MSE:
                0.04660268500447273
       12 MSE:
Epoch
                0.04711340740323067
Epoch
       13 MSE:
                0.0455918163061142
Epoch
       14 MSE:
                0.042598381638526917
Epoch
       15 MSE:
                0.03882305324077606
Epoch
       16 MSE:
                0.03488631546497345
Epoch 17 MSE:
                0.031248940154910088
Epoch
       18 MSE:
                0.02819124609231949
       19 MSE:
Epoch
                0.025831513106822968
       20 MSE:
Epoch
                0.024162452667951584
Epoch
       21 MSE:
                0.023092053830623627
Epoch
       22 MSE:
                0.022480985149741173
Epoch
       23 MSE:
                0.022172782570123672
Epoch
      24 MSE:
                0.02201603539288044
Epoch
       25 MSE:
                0.02187914028763771
       26 MSE:
Epoch
                0.021658923476934433
Epoch
       27 MSE:
                0.02128439210355282
Epoch
       28 MSE:
                0.020716864615678787
Epoch
       29 MSE:
                0.019947415217757225
       30 MSE:
Epoch
                0.01899244450032711
Epoch
       31 MSE:
                0.01788805052638054
       32 MSE:
Epoch
                0.01668361946940422
Epoch
       33 MSE:
                0.015435146167874336
Epoch
       34 MSE:
                0.014198536984622478
       35 MSE:
Epoch
                0.013023347593843937
Epoch
       36 MSE:
                0.01194726675748825
       37 MSE:
Epoch
                0.0109918974339962
Epoch
       38 MSE:
                0.010160406120121479
       39 MSE:
Epoch
                0.009437615983188152
Epoch
       40 MSE:
                0.008793056942522526
Epoch
       41 MSE:
                0.008186914026737213
       42 MSE:
                0.007578228134661913
Epoch
Epoch
       43 MSE:
                0.006933859083801508
Epoch
       44 MSE:
                0.006236116401851177
Epoch
       45 MSE:
                0.00548703083768487
Epoch
       46 MSE:
                0.004707919899374247
       47 MSE:
Epoch
                0.003934202715754509
Epoch
       48 MSE:
                0.0032067543361335993
      49 MSE:
                0.0025620823726058006
Epoch
       50 MSE:
Epoch
                0.0020239041186869144
Epoch
       51 MSE:
                0.0015983176417648792
Epoch
       52 MSE:
                0.0012737925862893462
Epoch
       53 MSE:
                0.0010259362170472741
Epoch
       54 MSE:
                0.0008256698492914438
Epoch
       55 MSE:
                0.000648415822070092
       56 MSE:
                0.0004814508429262787
Epoch
```

```
Epoch 57 MSE:
                0.00032696983544155955
Epoch 58 MSE:
                0.00019958008488174528
Epoch 59 MSE:
                0.00011873256153194234
Epoch
      60 MSE:
                9.856017277343199e-05
Epoch 61 MSE:
                0.00013914768351241946
Epoch
      62 MSE:
                0.00022350013023242354
Epoch
      63 MSE:
                0.00032253231620416045
Epoch 64 MSE:
                0.00040639538201503456
Epoch 65 MSE:
                0.0004564113332889974
Epoch 66 MSE:
                0.00047098571667447686
Epoch 67 MSE:
                0.0004624681605491787
Epoch 68 MSE:
                0.00044761024764738977
Epoch 69 MSE:
                0.00043779032421298325
Epoch 70 MSE:
                0.0004342893953435123
Epoch 71 MSE:
                0.00043006223859265447
                0.0004156184440944344
Epoch 72 MSE:
Epoch 73 MSE:
                0.0003850734210573137
Epoch 74 MSE:
                0.00033927688491530716
Epoch 75 MSE:
                0.00028509259573183954
Epoch 76 MSE:
                0.0002319329942110926
Epoch
     77 MSE:
                0.00018766960420180112
Epoch 78 MSE:
                0.0001559013908263296
Epoch 79 MSE:
                0.00013555301120504737
Epoch 80 MSE:
                0.00012254375906195492
Epoch 81 MSE:
                0.00011236253340030089
Epoch 82 MSE:
                0.00010218763054581359
Epoch 83 MSE:
                9.16842618607916e-05
Epoch 84 MSE:
                8.241654722951353e-05
Epoch 85 MSE:
                7.647716847714037e-05
Epoch 86 MSE:
                7.515507604693994e-05
Epoch 87 MSE:
                7.824917702237144e-05
Epoch 88 MSE:
                8.419922960456461e-05
Epoch 89 MSE:
                9.080717427423224e-05
Epoch 90 MSE:
                9.611817222321406e-05
Epoch
      91 MSE:
                9.905851038638502e-05
Epoch 92 MSE:
                9.961108298739418e-05
Epoch 93 MSE:
                9.854306699708104e-05
Epoch 94 MSE:
                9.688025602372363e-05
Epoch 95 MSE:
                9.539252641843632e-05
Epoch 96 MSE:
                9.430580394109711e-05
Epoch 97 MSE:
                9.332597983302549e-05
Epoch 98 MSE:
                9.191109711537138e-05
Epoch 99 MSE:
                8.962277206592262e-05
T-time: 9.294182538986206
```

Train Score: 0.28 RMSE

Time Step = 20 | Hidden States = 8 | Num Layers = 2

Epoch 0 MSE: 0.03697124868631363 Epoch 1 MSE: 0.03310519829392433 Epoch 2 MSE: 0.03370271250605583 Epoch 3 MSE: 0.0292363204061985 Epoch 4 MSE: 0.026478365063667297 Epoch 5 MSE: 0.02623298391699791 Epoch 6 MSE: 0.02466888353228569 Epoch 7 MSE: 0.020860018208622932 Epoch 8 MSE: 0.017303481698036194 Epoch 9 MSE: 0.01545956265181303Epoch 10 MSE: 0.01325792446732521 Epoch 11 MSE: 0.009229110553860664 Epoch 12 MSE: 0.005698396358639002 Epoch 13 MSE: 0.004287221468985081 Epoch 14 MSE: 0.0022116259206086397 Epoch 15 MSE: 0.00017716115689836442 Epoch 16 MSE: 0.0017980221891775727 Epoch 17 MSE: 0.0022097118198871613 Epoch 18 MSE: 0.003261921927332878 Epoch 19 MSE: 0.0048162611201405525 Epoch 20 MSE: 0.003567339386790991 Epoch 21 MSE: 0.0032535989303141832 Epoch 22 MSE: 0.0023133631329983473 Epoch 23 MSE: 0.0008471875335089862 Epoch 24 MSE: 0.000561899330932647 Epoch 25 MSE: 0.0005047200829721987 Epoch 26 MSE: 0.00027102173771709204 Epoch 27 MSE: 0.0004863405483774841 Epoch 28 MSE: 0.0009667814010754228 Epoch 29 MSE: 0.001148776151239872 Epoch 30 MSE: 0.0011245205532759428 Epoch 31 MSE: 0.0012109491508454084 Epoch 32 MSE: 0.0012875939719378948 Epoch 33 MSE: 0.0011082090204581618 Epoch 34 MSE: 0.0008059577667154372 Epoch 35 MSE: 0.0006329651223495603 Epoch 36 MSE: 0.0005119871348142624 Epoch 37 MSE: 0.0002885629655793309 Epoch 38 MSE: 0.00012694988981820643 Epoch 39 MSE: 0.0001676496467553079 Epoch 40 MSE: 0.0002222883194917813

```
Epoch 41 MSE:
                0.0002260654146084562
Epoch
       42 MSE:
                0.0003318098606541753
       43 MSE:
Epoch
                0.0004344201006460935
       44 MSE:
Epoch
                0.00039851164910942316
Epoch
       45 MSE:
                0.0003646730328910053
Epoch
       46 MSE:
                0.0003434359678067267
Epoch
       47 MSE:
                0.00024028825282584876
Epoch
       48 MSE:
                0.00015548683586530387
Epoch 49 MSE:
                0.00014135798846837133
Epoch
      50 MSE:
                0.00011559011181816459
       51 MSE:
                9.758918167790398e-05
Epoch
Epoch
       52 MSE:
                0.00013356999261304736
Epoch
       53 MSE:
                0.0001659326662775129
Epoch
       54 MSE:
                0.00016821706958580762
Epoch
      55 MSE:
                0.00018074281979352236
Epoch 56 MSE:
                0.0001909102575154975
Epoch
      57 MSE:
                0.00016751013754401356
       58 MSE:
Epoch
                0.0001406693336321041
Epoch
       59 MSE:
                0.0001283565943595022
Epoch
       60 MSE:
                0.00010625593131408095
Epoch
       61 MSE:
                8.563076698919758e-05
Epoch
       62 MSE:
                8.831775630824268e-05
Epoch
       63 MSE:
                9.250492439605296e-05
       64 MSE:
Epoch
                9.264267282560468e-05
Epoch
       65 MSE:
                0.00010458280303282663
Epoch
       66 MSE:
                0.00011160228314111009
       67 MSE:
Epoch
                0.00010620127432048321
Epoch
       68 MSE:
                0.00010424284846521914
       69 MSE:
Epoch
                9.851909271674231e-05
Epoch
     70 MSE:
                8.588974014855921e-05
Epoch 71 MSE:
                8.046526636462659e-05
Epoch
      72 MSE:
                7.784190529491752e-05
Epoch
      73 MSE:
                7.367717626038939e-05
      74 MSE:
Epoch
                7.590307359350845e-05
Epoch
       75 MSE:
                7.952110900077969e-05
Epoch
       76 MSE:
                7.933591405162588e-05
Epoch
      77 MSE:
                8.0687808804214e-05
Epoch
      78 MSE:
                8.081377018243074e-05
      79 MSE:
Epoch
                7.678500696783885e-05
Epoch
       80 MSE:
                7.397957961075008e-05
       81 MSE:
Epoch
                7.153808837756515e-05
Epoch
       82 MSE:
                6.778415263397619e-05
Epoch
       83 MSE:
                6.67253989377059e-05
Epoch
       84 MSE:
                6.68322536512278e-05
Epoch
       85 MSE:
                6.619439227506518e-05
Epoch
       86 MSE:
                6.70701265335083e-05
Epoch
       87 MSE:
                6.742119148839265e-05
       88 MSE:
                6.625705282203853e-05
Epoch
```

Epoch 89 MSE: 6.558900349773467e-05
Epoch 90 MSE: 6.409321213141084e-05
Epoch 91 MSE: 6.208506965776905e-05
Epoch 92 MSE: 6.11495051998645e-05
Epoch 93 MSE: 6.0092545027146116e-05
Epoch 94 MSE: 5.93443910474889e-05
Epoch 95 MSE: 5.941394192632288e-05
Epoch 96 MSE: 5.904004137846641e-05
Epoch 97 MSE: 5.866582796443254e-05
Epoch 98 MSE: 5.835271440446377e-05
Epoch 99 MSE: 5.739877087762579e-05

T-time: 17.47054648399353

Train Score: 0.23 RMSE

Validation Score: 6.10 RMSE

Time Step = 20 | Hidden States = 16 | Num Layers = 1

Epoch 0 MSE: 0.06648924201726913 Epoch 1 MSE: 0.04395616799592972 Epoch 2 MSE: 0.03344652056694031 Epoch 3 MSE: 0.033223707228899 Epoch 4 MSE: 0.035296231508255005 Epoch 5 MSE: 0.033633045852184296 Epoch 6 MSE: 0.029451798647642136 Epoch 7 MSE: 0.025384046137332916 Epoch 8 MSE: 0.022762421518564224 Epoch 9 MSE: 0.021611005067825317 Epoch 10 MSE: 0.021197443827986717 Epoch 11 MSE: 0.02060309424996376 Epoch 12 MSE: 0.01924586296081543 Epoch 13 MSE: 0.0171081330627203 Epoch 14 MSE: 0.014598134905099869 Epoch 15 MSE: 0.012272704392671585 Epoch 16 MSE: 0.01055016741156578 Epoch 17 MSE: 0.009449181146919727 Epoch 18 MSE: 0.00850654672831297 Epoch 19 MSE: 0.0071274940855801105 Epoch 20 MSE: 0.005141337867826223 Epoch 21 MSE: 0.002995114540681243 Epoch 22 MSE: 0.001472181174904108 Epoch 23 MSE: 0.0010693584335967898 Epoch 24 MSE: 0.0013061255449429154

```
0.0011848757276311517
Epoch
       25 MSE:
Epoch
       26 MSE:
                0.0008524227887392044
Epoch
       27 MSE:
                0.0013726659817621112
       28 MSE:
Epoch
                0.0025197607465088367
Epoch
       29 MSE:
                0.0027213995344936848
Epoch
       30 MSE:
                0.0019265215378254652
Epoch
       31 MSE:
                0.0012608575634658337
Epoch
       32 MSE:
                0.001071047387085855
Epoch
      33 MSE:
                0.0009050466469489038
Epoch
       34 MSE:
                0.0005379050853662193
       35 MSE:
                0.00018235128663945943
Epoch
Epoch
       36 MSE:
                6.970119284233078e-05
Epoch
       37 MSE:
                0.00019274164515081793
Epoch
       38 MSE:
                0.00037587815313600004
Epoch
       39 MSE:
                0.0004723197198472917
                0.000467958947410807
Epoch 40 MSE:
Epoch
       41 MSE:
                0.0004378685844130814
       42 MSE:
Epoch
                0.00044640814303420484
Epoch
       43 MSE:
                0.000490716309286654
Epoch
       44 MSE:
                0.0005179885774850845
Epoch
       45 MSE:
                0.0004826568183489144
Epoch
       46 MSE:
                0.00038801247137598693
Epoch 47 MSE:
                0.00028030649991706014
       48 MSE:
Epoch
                0.0002065077133011073
       49 MSE:
                0.00017574962112121284
Epoch
Epoch
       50 MSE:
                0.0001593558699823916
       51 MSE:
Epoch
                0.00012760733079630882
Epoch
       52 MSE:
                8.361668005818501e-05
       53 MSE:
Epoch
                5.759382474934682e-05
Epoch 54 MSE:
                6.976453005336225e-05
Epoch 55 MSE:
                0.00010585397103568539
Epoch
       56 MSE:
                0.0001330512313870713
      57 MSE:
Epoch
                0.00013552367454394698
       58 MSE:
                0.00012646069808397442
Epoch
Epoch
       59 MSE:
                0.00012534877168945968
Epoch
       60 MSE:
                0.00013227768067736179
Epoch
       61 MSE:
                0.00013091650907881558
Epoch
       62 MSE:
                0.00011225107300560921
Epoch
       63 MSE:
                8.625470945844427e-05
Epoch
       64 MSE:
                6.88745712977834e-05
       65 MSE:
Epoch
                6.427834159694612e-05
       66 MSE:
Epoch
                6.395452510332689e-05
       67 MSE:
                5.988231714582071e-05
Epoch
Epoch
       68 MSE:
                5.3604224376613274e-05
Epoch
       69 MSE:
                5.196978599997237e-05
Epoch
       70 MSE:
                5.738906475016847e-05
Epoch
       71 MSE:
                6.489389488706365e-05
       72 MSE:
Epoch
                6.81945457472466e-05
```

```
Epoch 73 MSE: 6.63202881696634e-05
Epoch 74 MSE:
               6.324027344817296e-05
Epoch 75 MSE:
               6.21814324404113e-05
Epoch 76 MSE:
               6.208828563103452e-05
Epoch 77 MSE:
               5.9895304730162024e-05
Epoch 78 MSE:
               5.4928190365899354e-05
Epoch 79 MSE:
               4.982583413948305e-05
Epoch 80 MSE:
               4.7301673475885764e-05
Epoch 81 MSE:
               4.716640614788048e-05
Epoch 82 MSE:
               4.719466232927516e-05
Epoch 83 MSE:
               4.624006760423072e-05
Epoch 84 MSE:
               4.5380875235423446e-05
Epoch 85 MSE:
               4.594510392053053e-05
Epoch 86 MSE:
               4.746209015138447e-05
Epoch 87 MSE:
               4.827204975299537e-05
Epoch 88 MSE:
               4.7651810746174306e-05
Epoch 89 MSE:
               4.6471937821479514e-05
Epoch 90 MSE:
               4.576073115458712e-05
Epoch 91 MSE:
               4.539205110631883e-05
Epoch 92 MSE:
               4.458713374333456e-05
Epoch 93 MSE:
               4.3223695683991536e-05
Epoch 94 MSE:
               4.2031551856780425e-05
Epoch 95 MSE:
               4.1577848605811596e-05
Epoch 96 MSE:
               4.1596889786887914e-05
Epoch 97 MSE:
               4.149624874116853e-05
Epoch 98 MSE:
               4.11616092605982e-05
Epoch 99 MSE:
               4.094864925718866e-05
```

T-time: 13.776725769042969

Train Score: 0.19 RMSE Validation Score: 4.30 RMSE

_____ Time Step = 20 | Hidden States = 16 | Num Layers = 2 ______

Epoch 0 MSE: 0.12328866869211197 Epoch 1 MSE: 0.06399630755186081 Epoch 2 MSE: 0.03484782576560974 Epoch 3 MSE: 0.034026168286800385 Epoch 4 MSE: 0.04490096867084503 Epoch 5 MSE: 0.04332171753048897 Epoch 6 MSE: 0.03539249673485756 Epoch 7 MSE: 0.029287295415997505 Epoch 8 MSE: 0.02712470293045044

```
9 MSE:
               0.0275803841650486
Epoch
Epoch
       10 MSE:
                0.028538474813103676
Epoch
       11 MSE:
                0.028441565111279488
       12 MSE:
Epoch
                0.02676238678395748
Epoch
       13 MSE:
                0.02377472072839737
Epoch
       14 MSE:
                0.02014775015413761
Epoch
       15 MSE:
                0.016654236242175102
Epoch
       16 MSE:
                0.013944784179329872
Epoch 17 MSE:
                0.012207362800836563
Epoch
       18 MSE:
                0.010729984380304813
       19 MSE:
                0.008195501752197742
Epoch
       20 MSE:
Epoch
                0.004250070545822382
Epoch
       21 MSE:
                0.0007388817030005157
Epoch
       22 MSE:
                0.0009408073965460062
Epoch
       23 MSE:
                0.004700010176748037
Epoch
      24 MSE:
                0.005593719892203808
Epoch
       25 MSE:
                0.003732556477189064
       26 MSE:
Epoch
                0.0026981825940310955
Epoch
       27 MSE:
                0.0024409431498497725
Epoch
       28 MSE:
                0.0015879969578236341
       29 MSE:
Epoch
                0.0006066819187253714
       30 MSE:
Epoch
                0.00036019826075062156
Epoch
       31 MSE:
                0.0008541498682461679
       32 MSE:
Epoch
                0.0015538420993834734
Epoch
       33 MSE:
                0.0019754308741539717
Epoch
       34 MSE:
                0.0019425315549597144
       35 MSE:
Epoch
                0.0015671401051804423
Epoch
       36 MSE:
                0.0011091757332906127
       37 MSE:
Epoch
                0.0008007483556866646
Epoch
       38 MSE:
                0.0007004154613241553
       39 MSE:
Epoch
                0.0006713524926453829
Epoch
       40 MSE:
                0.0005402854876592755
Epoch
       41 MSE:
                0.00030795394559390843
       42 MSE:
                0.00016091442375909537
Epoch
Epoch
       43 MSE:
                0.000248368683969602
Epoch
       44 MSE:
                0.0004915003664791584
Epoch
       45 MSE:
                0.0006583323702216148
Epoch
       46 MSE:
                0.0006081382744014263
       47 MSE:
Epoch
                0.0004141439567320049
Epoch
       48 MSE:
                0.0002494911605026573
      49 MSE:
                0.0002004373091040179
Epoch
       50 MSE:
Epoch
                0.00021473260130733252
Epoch
       51 MSE:
                0.00020631070947274566
Epoch
       52 MSE:
                0.00016185565618798137
Epoch
       53 MSE:
                0.00013252045027911663
Epoch
       54 MSE:
                0.0001563814003020525
Epoch
       55 MSE:
                0.00021500677394215018
       56 MSE:
                0.000256413099123165
Epoch
```

```
Epoch 57 MSE:
                0.00024483268498443067
Epoch 58 MSE:
                0.00018862156139221042
Epoch 59 MSE:
                0.00012792962661478668
Epoch 60 MSE:
                9.758980013430119e-05
Epoch 61 MSE:
                9.902477904688567e-05
Epoch 62 MSE:
                0.00010683561413316056
Epoch 63 MSE:
                0.00010148681758437306
Epoch 64 MSE:
                8.9943379862234e-05
Epoch 65 MSE:
                9.106417564908043e-05
Epoch 66 MSE:
                0.00010760197619674727
Epoch 67 MSE:
                0.00012134708958910778
Epoch 68 MSE:
                0.00011499293032102287
Epoch 69 MSE:
                9.161710477201268e-05
Epoch 70 MSE:
                6.97197683621198e-05
Epoch 71 MSE:
                6.270501762628555e-05
Epoch 72 MSE:
                6.73644826747477e-05
Epoch 73 MSE:
               7.188742165453732e-05
Epoch 74 MSE:
                7.055910100461915e-05
Epoch 75 MSE:
                6.75546980346553e-05
Epoch 76 MSE:
                6.844197196187451e-05
Epoch 77 MSE:
                7.216592348413542e-05
Epoch 78 MSE:
                7.27096339687705e-05
Epoch 79 MSE:
                6.677494093310088e-05
Epoch 80 MSE:
                5.781524669146165e-05
Epoch 81 MSE:
                5.2183913794578984e-05
Epoch 82 MSE:
                5.2365907322382554e-05
Epoch 83 MSE:
                5.512389907380566e-05
Epoch 84 MSE:
                5.612011955236085e-05
Epoch 85 MSE:
                5.4768112022429705e-05
Epoch 86 MSE:
                5.3544856200460345e-05
Epoch 87 MSE:
                5.37367413926404e-05
Epoch 88 MSE:
                5.375296314014122e-05
Epoch 89 MSE:
                5.1734015869442374e-05
Epoch 90 MSE:
                4.8332763981306925e-05
Epoch 91 MSE:
                4.5976979890838265e-05
Epoch 92 MSE:
                4.5928794861538336e-05
Epoch 93 MSE:
                4.7033241571625695e-05
Epoch 94 MSE:
                4.7422407078556716e-05
Epoch 95 MSE:
                4.6652177843498066e-05
Epoch 96 MSE:
                4.567488576867618e-05
Epoch 97 MSE:
                4.5193090045358986e-05
Epoch 98 MSE:
               4.4806089135818183e-05
Epoch 99 MSE:
                4.385584907140583e-05
T-time: 26.54852604866028
```

Train Score: 0.20 RMSE

Time Step = 20 | Hidden States = 32 | Num Layers = 1

Epoch 0 MSE: 0.04279480129480362 Epoch 1 MSE: 0.032703205943107605 Epoch 2 MSE: 0.031237922608852386 Epoch 3 MSE: 0.025011612102389336 Epoch 4 MSE: 0.01927153766155243 Epoch 5 MSE: 0.01604052074253559 Epoch 6 MSE: 0.012436950579285622 Epoch 7 MSE: 0.0062834289856255054 Epoch 8 MSE: 0.0013593488838523626 Epoch 9 MSE: 0.0052099390886723995 Epoch 10 MSE: 0.003260774305090308 Epoch 11 MSE: 0.003612510859966278 Epoch 12 MSE: 0.00378512404859066 Epoch 13 MSE: 0.0012045865878462791 Epoch 14 MSE: 0.00010926204413408414 Epoch 15 MSE: 0.00119888037443161 Epoch 16 MSE: 0.0022847005166113377 Epoch 17 MSE: 0.002110561588779092 Epoch 18 MSE: 0.0013339685974642634 Epoch 19 MSE: 0.0009307835716754198 Epoch 20 MSE: 0.00108481349889189 Epoch 21 MSE: 0.001269939704798162 Epoch 22 MSE: 0.000993218389339745 Epoch 23 MSE: 0.00038003726513125 Epoch 24 MSE: 2.4624123398098163e-05 Epoch 25 MSE: 0.00026815923047252 Epoch 26 MSE: 0.000700667267665267 Epoch 27 MSE: 0.0007111811428330839 Epoch 28 MSE: 0.00039310866850428283 Epoch 29 MSE: 0.00025513788568787277 Epoch 30 MSE: 0.0003791103372350335 Epoch 31 MSE: 0.00043431652011349797 Epoch 32 MSE: 0.00026578549295663834 Epoch 33 MSE: 6.483187462436035e-05 Epoch 34 MSE: 4.7132110921666026e-05 Epoch 35 MSE: 0.00018599371833261102 Epoch 36 MSE: 0.0002905841392930597 Epoch 37 MSE: 0.00025535887107253075 Epoch 38 MSE: 0.00015428276674356312 Epoch 39 MSE: 0.00011016528151230887 Epoch 40 MSE: 0.0001424529473297298

```
Epoch 41 MSE:
                0.00016796689305920154
Epoch
       42 MSE:
                0.0001232336653629318
       43 MSE:
Epoch
                4.661830098484643e-05
Epoch
       44 MSE:
                2.3317286832025275e-05
Epoch
       45 MSE:
                7.015690789557993e-05
Epoch
       46 MSE:
                0.00011570535571081564
Epoch
       47 MSE:
                0.00010303064482286572
Epoch
       48 MSE:
                6.230948929442093e-05
Epoch 49 MSE:
                5.1163002353860065e-05
Epoch
      50 MSE:
                6.891697557875887e-05
       51 MSE:
Epoch
                7.16801660018973e-05
Epoch
      52 MSE:
                4.535085099632852e-05
Epoch
       53 MSE:
                2.1967240172671154e-05
Epoch
       54 MSE:
                2.837402280420065e-05
Epoch
      55 MSE:
                5.010570748709142e-05
Epoch 56 MSE:
                5.666236029355787e-05
Epoch
      57 MSE:
                4.360254024504684e-05
       58 MSE:
Epoch
                3.209470014553517e-05
Epoch
       59 MSE:
                3.47589302691631e-05
Epoch
       60 MSE:
                4.0383813029620796e-05
Epoch
       61 MSE:
                3.4862114262068644e-05
Epoch
       62 MSE:
                2.3096949007594958e-05
Epoch
       63 MSE:
                2.022347143793013e-05
       64 MSE:
Epoch
                2.817891800077632e-05
Epoch
       65 MSE:
                3.3935270039364696e-05
Epoch
       66 MSE:
                3.0142373361741193e-05
       67 MSE:
Epoch
                2.4385670258197933e-05
Epoch
       68 MSE:
                2.4670569473528303e-05
       69 MSE:
Epoch
                2.7331045203027315e-05
Epoch
     70 MSE:
                2.5384544642292894e-05
Epoch 71 MSE:
                2.0527286324067973e-05
Epoch
      72 MSE:
                1.9459863324300386e-05
                2.2802531020715833e-05
Epoch
      73 MSE:
      74 MSE:
Epoch
                2.4888426196412183e-05
Epoch
      75 MSE:
                2.3081649487721734e-05
Epoch
      76 MSE:
                2.0882391254417598e-05
Epoch
      77 MSE:
                2.1242591174086556e-05
Epoch
      78 MSE:
                2.2167767383507453e-05
      79 MSE:
Epoch
                2.0994846636313014e-05
Epoch
       80 MSE:
                1.9056094970437698e-05
      81 MSE:
Epoch
                1.9101604266325012e-05
Epoch
       82 MSE:
                2.061637678707484e-05
Epoch
       83 MSE:
                2.0996607418055646e-05
Epoch
       84 MSE:
                1.9923052605008706e-05
Epoch
       85 MSE:
                1.9324330423842184e-05
Epoch
       86 MSE:
                1.9752549633267336e-05
Epoch
       87 MSE:
                1.9804654584731907e-05
       88 MSE:
                1.8968890799442306e-05
Epoch
```

Epoch 89 MSE: 1.8457771147950552e-05
Epoch 90 MSE: 1.8919534340966493e-05
Epoch 91 MSE: 1.9397410142119043e-05
Epoch 92 MSE: 1.9118115233140998e-05
Epoch 93 MSE: 1.8666358300833963e-05
Epoch 94 MSE: 1.870349660748616e-05
Epoch 95 MSE: 1.884495941339992e-05
Epoch 96 MSE: 1.8570235624792986e-05
Epoch 97 MSE: 1.821903424570337e-05
Epoch 98 MSE: 1.8294214896741323e-05
Epoch 99 MSE: 1.8544651538832113e-05

T-time: 26.019545316696167

Train Score: 0.13 RMSE

Validation Score: 1.51 RMSE

Time Step = 20 | Hidden States = 32 | Num Layers = 2

Epoch 0 MSE: 0.07179559022188187 Epoch 1 MSE: 0.053293388336896896 Epoch 2 MSE: 0.04245859757065773 Epoch 3 MSE: 0.02891470678150654 Epoch 4 MSE: 0.028615588322281837 Epoch 5 MSE: 0.028290200978517532 Epoch 6 MSE: 0.020927928388118744 Epoch 7 MSE: 0.011481642723083496 Epoch 8 MSE: 0.008736717514693737 Epoch 9 MSE: 0.009971647523343563 Epoch 10 MSE: 0.002672072034329176 Epoch 11 MSE: 0.002599109197035432 Epoch 12 MSE: 0.009029964916408062 Epoch 13 MSE: 0.0048012034967541695 Epoch 14 MSE: 0.000365995365427807 Epoch 15 MSE: 0.0012147922534495592 Epoch 16 MSE: 0.0032251854427158833 Epoch 17 MSE: 0.003329699393361807 Epoch 18 MSE: 0.0024801664985716343 Epoch 19 MSE: 0.0020592212677001953 Epoch 20 MSE: 0.0021666716784238815 Epoch 21 MSE: 0.0021524960175156593 Epoch 22 MSE: 0.0015332387993112206 Epoch 23 MSE: 0.0005607558996416628 Epoch 24 MSE: 0.0001422767381882295

```
Epoch
      25 MSE:
                0.0008216415881179273
Epoch
      26 MSE:
                0.001618026290088892
Epoch
      27 MSE:
                0.001312705921009183
      28 MSE:
Epoch
                0.00048756232718005776
Epoch
      29 MSE:
                0.00017417124763596803
Epoch
      30 MSE:
                0.00037566316314041615
Epoch
       31 MSE:
                0.0005903263227082789
Epoch
      32 MSE:
                0.00057415192713961
Epoch 33 MSE:
                0.00044022814836353064
Epoch
      34 MSE:
                0.0003897933929692954
      35 MSE:
                0.00045812551979906857
Epoch
Epoch
      36 MSE:
                0.000488189427414909
Epoch
      37 MSE:
                0.0003477517166174948
Epoch
       38 MSE:
                0.0001291118242079392
Epoch
      39 MSE:
                4.772728789248504e-05
Epoch 40 MSE:
                0.00016554231115151197
Epoch
      41 MSE:
                0.0003175752644892782
      42 MSE:
                0.0003260724770370871
Epoch
Epoch
       43 MSE:
                0.00020462312386371195
Epoch
      44 MSE:
                0.00010212827328359708
Epoch
       45 MSE:
                9.807762398850173e-05
Epoch
      46 MSE:
                0.0001326723286183551
Epoch 47 MSE:
                0.00013018090976402164
Epoch 48 MSE:
                0.00010243273572996259
      49 MSE:
                0.00010117741476278752
Epoch
Epoch 50 MSE:
                0.00013013722491450608
Epoch 51 MSE:
                0.0001431655400665477
Epoch
      52 MSE:
                0.00010955549078062177
Epoch
      53 MSE:
                5.572067675529979e-05
Epoch 54 MSE:
                3.4837958082789555e-05
Epoch 55 MSE:
                6.10963543294929e-05
Epoch
      56 MSE:
                9.267429413739592e-05
Epoch 57 MSE:
                8.996023098006845e-05
      58 MSE:
Epoch
                6.48604691377841e-05
                5.12432525283657e-05
Epoch
       59 MSE:
Epoch
       60 MSE:
                5.43672067578882e-05
Epoch
       61 MSE:
                5.522068022401072e-05
Epoch
       62 MSE:
                4.6621895307907835e-05
Epoch
       63 MSE:
                4.1491861338727176e-05
Epoch
       64 MSE:
                4.876060120295733e-05
      65 MSE:
Epoch
                5.7778754126047716e-05
       66 MSE:
Epoch
                5.371328006731346e-05
       67 MSE:
Epoch
                3.9405083953170106e-05
Epoch
      68 MSE:
                3.0961389711592346e-05
Epoch
      69 MSE:
                3.514246054692194e-05
Epoch
      70 MSE:
                4.230751801514998e-05
Epoch
      71 MSE:
                4.2306124669266865e-05
      72 MSE:
Epoch
                3.7418903957586735e-05
```

```
Epoch 73 MSE:
               3.515679782140069e-05
Epoch 74 MSE:
               3.5786368243861943e-05
Epoch 75 MSE:
               3.440362706896849e-05
Epoch 76 MSE:
               3.100948015344329e-05
Epoch 77 MSE:
               3.0363396945176646e-05
Epoch 78 MSE:
               3.333540735184215e-05
Epoch 79 MSE:
               3.516208380460739e-05
Epoch 80 MSE:
               3.276917777839117e-05
Epoch 81 MSE:
               2.9066435672575608e-05
Epoch 82 MSE:
               2.8185382689116523e-05
Epoch 83 MSE:
               2.968939588754438e-05
Epoch 84 MSE:
               3.0328046705108136e-05
Epoch 85 MSE:
               2.9376946258707903e-05
Epoch 86 MSE:
               2.8730630219797604e-05
Epoch 87 MSE:
               2.8911943445564248e-05
Epoch 88 MSE:
               2.8512082280940376e-05
Epoch 89 MSE:
               2.725705417105928e-05
Epoch 90 MSE:
               2.6677844289224595e-05
Epoch 91 MSE:
               2.7400868930271827e-05
Epoch 92 MSE:
               2.802954077196773e-05
Epoch 93 MSE:
               2.7431246053311042e-05
Epoch 94 MSE:
               2.638915611896664e-05
Epoch 95 MSE:
               2.6084591809194535e-05
Epoch 96 MSE:
               2.6323717975174077e-05
Epoch 97 MSE:
               2.6283149054506794e-05
Epoch 98 MSE:
               2.5976780307246372e-05
Epoch 99 MSE:
               2.5904790163622238e-05
```

T-time: 53.807433128356934

Train Score: 0.15 RMSE Validation Score: 4.23 RMSE

_____ Time Step = 30 | Hidden States = 2 | Num Layers = 1 ______

Epoch 0 MSE: 0.07426975667476654 Epoch 1 MSE: 0.062000639736652374 Epoch 2 MSE: 0.05237584561109543 Epoch 3 MSE: 0.04559844732284546 Epoch 4 MSE: 0.04167785868048668 Epoch 5 MSE: 0.04025387018918991 Epoch 6 MSE: 0.04044682905077934 Epoch 7 MSE: 0.04102233052253723Epoch 8 MSE: 0.04096795618534088

```
9 MSE:
               0.03989556431770325
Epoch
Epoch
       10 MSE:
                0.03795135021209717
Epoch
       11 MSE:
                0.03553568571805954
       12 MSE:
Epoch
                0.03307943418622017
Epoch
       13 MSE:
                0.03091735951602459
Epoch
       14 MSE:
                0.029232043772935867
Epoch
       15 MSE:
                0.028046315535902977
Epoch
       16 MSE:
                0.02725265920162201
Epoch 17 MSE:
                0.026668118312954903
Epoch
       18 MSE:
                0.026097716763615608
       19 MSE:
                0.02538789063692093
Epoch
       20 MSE:
Epoch
                0.024457156658172607
Epoch
       21 MSE:
                0.02330155298113823
Epoch
       22 MSE:
                0.021980099380016327
Epoch
       23 MSE:
                0.02058880589902401
Epoch
       24 MSE:
                0.019230898469686508
Epoch
       25 MSE:
                0.017989255487918854
       26 MSE:
Epoch
                0.016906043514609337
Epoch
       27 MSE:
                0.015974009409546852
Epoch
       28 MSE:
                0.015142470598220825
Epoch
       29 MSE:
                0.014337236993014812
       30 MSE:
Epoch
                0.013488230295479298
Epoch
       31 MSE:
                0.012554431334137917
       32 MSE:
Epoch
                0.011536561883985996
       33 MSE:
                0.010473373346030712
Epoch
Epoch
       34 MSE:
                0.009424394927918911
       35 MSE:
Epoch
                0.008446639403700829
Epoch
       36 MSE:
                0.007573997136205435
       37 MSE:
Epoch
                0.006806546822190285
Epoch
       38 MSE:
                0.006113657262176275
       39 MSE:
Epoch
                0.005449836608022451
Epoch
       40 MSE:
                0.004776856862008572
Epoch
       41 MSE:
                0.004082249011844397
       42 MSE:
Epoch
                0.003385331481695175
Epoch
       43 MSE:
                0.0027277341578155756
Epoch
       44 MSE:
                0.0021529707591980696
Epoch
       45 MSE:
                0.0016852000262588263
Epoch
       46 MSE:
                0.0013184379786252975
       47 MSE:
Epoch
                0.0010227622697129846
Epoch
       48 MSE:
                0.0007643487770110369
       49 MSE:
                0.000526878226082772
Epoch
       50 MSE:
Epoch
                0.00032009449205361307
Epoch
       51 MSE:
                0.00016968441195786
Epoch
       52 MSE:
                9.55969444476068e-05
Epoch
       53 MSE:
                9.423273149877787e-05
Epoch
       54 MSE:
                0.00013779947767034173
Epoch
       55 MSE:
                0.00019160134252160788
       56 MSE:
                0.00023551513731945306
Epoch
```

```
Epoch 57 MSE:
                0.0002721938362810761
Epoch 58 MSE:
                0.00031620936351828277
Epoch 59 MSE:
                0.0003749807656276971
Epoch
      60 MSE:
                0.00043858392746187747
Epoch 61 MSE:
                0.00048655507271178067
Epoch
      62 MSE:
                0.0005041291587986052
Epoch
      63 MSE:
                0.0004926525289192796
Epoch 64 MSE:
                0.0004658012476284057
Epoch 65 MSE:
                0.00043682492105290294
Epoch 66 MSE:
                0.0004090256989002228
Epoch 67 MSE:
                0.00037692641490139067
Epoch 68 MSE:
                0.0003350116603542119
Epoch 69 MSE:
                0.00028484471840783954
Epoch 70 MSE:
                0.00023451828747056425
Epoch 71 MSE:
                0.00019230120233260095
Epoch 72 MSE:
                0.00016100452921818942
Epoch 73 MSE:
                0.00013766600750386715
Epoch 74 MSE:
                0.00011774702579714358
Epoch 75 MSE:
                9.942724864231423e-05
Epoch 76 MSE:
                8.445165440207347e-05
Epoch
     77 MSE:
                7.559631922049448e-05
Epoch 78 MSE:
                7.361640018643811e-05
Epoch 79 MSE:
                7.637815724592656e-05
Epoch 80 MSE:
                8.051947952480987e-05
Epoch 81 MSE:
                8.382488158531487e-05
Epoch 82 MSE:
                8.624481415608898e-05
Epoch 83 MSE:
                8.899832027964294e-05
Epoch 84 MSE:
                9.287395369028673e-05
Epoch 85 MSE:
                9.729454905027524e-05
Epoch 86 MSE:
                0.00010078714694827795
Epoch 87 MSE:
                0.00010221383126918226
Epoch 88 MSE:
                0.00010158870281884447
Epoch 89 MSE:
                9.98524046735838e-05
Epoch 90 MSE:
                9.795380174182355e-05
Epoch
      91 MSE:
                9.612715075490996e-05
Epoch 92 MSE:
                9.393812069902197e-05
Epoch 93 MSE:
                9.09233494894579e-05
Epoch 94 MSE:
                8.715822332305834e-05
Epoch 95 MSE:
                8.325346425408497e-05
Epoch 96 MSE:
                7.9863122664392e-05
Epoch 97 MSE:
               7.721227302681655e-05
Epoch
      98 MSE:
                7.506186375394464e-05
     99 MSE:
                7.307354098884389e-05
T-time: 11.532892942428589
```

1 01mc. 11.002032312120003

Train Score: 0.26 RMSE

Time Step = 30 | Hidden States = 2 | Num Layers = 2

Epoch 0 MSE: 0.045390594750642776 Epoch 1 MSE: 0.039350736886262894 Epoch 2 MSE: 0.03680720552802086 Epoch 3 MSE: 0.03701814264059067 Epoch 4 MSE: 0.03824859857559204 Epoch 5 MSE: 0.0388982854783535 Epoch 6 MSE: 0.038589753210544586 Epoch 7 MSE: 0.03770042955875397 Epoch 8 MSE: 0.03673737496137619 Epoch 9 MSE: 0.03607097640633583 Epoch 10 MSE: 0.035849325358867645 Epoch 11 MSE: 0.0359949916601181 Epoch 12 MSE: 0.036277927458286285 Epoch 13 MSE: 0.03645012155175209 Epoch 14 MSE: 0.03637011721730232 Epoch 15 MSE: 0.03604400157928467 Epoch 16 MSE: 0.03558318316936493 Epoch 17 MSE: 0.03512867912650108 Epoch 18 MSE: 0.03478314355015755 Epoch 19 MSE: 0.03457093611359596 Epoch 20 MSE: 0.034435905516147614 Epoch 21 MSE: 0.034276578575372696 Epoch 22 MSE: 0.03400101885199547 Epoch 23 MSE: 0.0335712656378746 Epoch 24 MSE: 0.03301503136754036 Epoch 25 MSE: 0.03240370377898216 Epoch 26 MSE: 0.03181092441082001 Epoch 27 MSE: 0.03126993775367737 Epoch 28 MSE: 0.030750151723623276 Epoch 29 MSE: 0.03017323836684227 Epoch 30 MSE: 0.029467524960637093 Epoch 31 MSE: 0.028618155047297478 Epoch 32 MSE: 0.027671774849295616 Epoch 33 MSE: 0.026697954162955284 Epoch 34 MSE: 0.025737443938851357 Epoch 35 MSE: 0.024771245196461678 Epoch 36 MSE: 0.023736145347356796 Epoch 37 MSE: 0.022581100463867188 Epoch 38 MSE: 0.02131466381251812 Epoch 39 MSE: 0.019995225593447685 Epoch 40 MSE: 0.018670178949832916

```
Epoch
       41 MSE:
                0.017325809225440025
Epoch
       42 MSE:
                0.015916241332888603
       43 MSE:
Epoch
                0.014441956765949726
       44 MSE:
Epoch
                0.01296877022832632
Epoch
       45 MSE:
                0.011557161808013916
Epoch
       46 MSE:
                0.010190810076892376
Epoch
       47 MSE:
                0.008824973367154598
Epoch
       48 MSE:
                0.007495538331568241
Epoch 49 MSE:
                0.006299460772424936
Epoch
       50 MSE:
                0.0052687483839690685
       51 MSE:
                0.004368013236671686
Epoch
Epoch
       52 MSE:
                0.0036305158864706755
Epoch
       53 MSE:
                0.0031113987788558006
Epoch
       54 MSE:
                0.0027501315344125032
Epoch
       55 MSE:
                0.0024988132063299417
      56 MSE:
                0.0023953800555318594
Epoch
Epoch
       57 MSE:
                0.002380162477493286
       58 MSE:
Epoch
                0.0023700492456555367
Epoch
       59 MSE:
                0.0023610915523022413
Epoch
       60 MSE:
                0.002313115866854787
Epoch
       61 MSE:
                0.002181589836254716
Epoch
       62 MSE:
                0.001987042836844921
Epoch
       63 MSE:
                0.001752917654812336
       64 MSE:
Epoch
                0.0014906941214576364
       65 MSE:
                0.0012382145505398512
Epoch
Epoch
       66 MSE:
                0.001039140741340816
       67 MSE:
Epoch
                0.0009074332192540169
Epoch
       68 MSE:
                0.0008409326546825469
       69 MSE:
Epoch
                0.0008368900744244456
Epoch
      70 MSE:
                0.0008774701273068786
      71 MSE:
Epoch
                0.0009306532447226346
Epoch
       72 MSE:
                0.0009729483281262219
Epoch
       73 MSE:
                0.000991307431831956
       74 MSE:
                0.0009741855319589376
Epoch
Epoch
       75 MSE:
                0.0009202486253343523
Epoch
       76 MSE:
                0.0008440037490800023
Epoch
      77 MSE:
                0.0007627123268321157
Epoch
       78 MSE:
                0.0006883539608679712
       79 MSE:
Epoch
                0.0006321161636151373
Epoch
       80 MSE:
                0.0006013473030179739
       81 MSE:
                0.0005925524746999145
Epoch
       82 MSE:
Epoch
                0.0005973762017674744
Epoch
       83 MSE:
                0.0006089253001846373
       84 MSE:
Epoch
                0.0006183059304021299
Epoch
       85 MSE:
                0.000617250450886786
Epoch
       86 MSE:
                0.0006043243338353932
Epoch
       87 MSE:
                0.0005812608869746327
       88 MSE:
Epoch
                0.0005505243898369372
```

Epoch 89 MSE: 0.0005180013249628246 Epoch 90 MSE: 0.0004894958692602813 Epoch 91 MSE: 0.0004672675277106464 Epoch 92 MSE: 0.00045255996519699693 Epoch 93 MSE: 0.0004451405256986618 Epoch 94 MSE: 0.00044173645437695086 Epoch 95 MSE: 0.00043909301166422665 Epoch 96 MSE: 0.00043515002471394837 Epoch 97 MSE: 0.00042786597623489797 Epoch 98 MSE: 0.0004167752340435982 Epoch 99 MSE: 0.00040325874579139054

T-time: 21.473809242248535

Train Score: 0.60 RMSE

Validation Score: 13.74 RMSE

Time Step = 30 | Hidden States = 4 | Num Layers = 1

Epoch 0 MSE: 0.10172559320926666 Epoch 1 MSE: 0.0781208872795105 Epoch 2 MSE: 0.05888362601399422 Epoch 3 MSE: 0.04382132366299629 Epoch 4 MSE: 0.03268958255648613 Epoch 5 MSE: 0.025147534906864166 Epoch 6 MSE: 0.02074587345123291 Epoch 7 MSE: 0.018936505541205406 Epoch 8 MSE: 0.019080597907304764 Epoch 9 MSE: 0.020466674119234085 Epoch 10 MSE: 0.02236625738441944 Epoch 11 MSE: 0.024130649864673615 Epoch 12 MSE: 0.025288831442594528 Epoch 13 MSE: 0.025595931336283684 Epoch 14 MSE: 0.025018129497766495 Epoch 15 MSE: 0.02367762289941311 Epoch 16 MSE: 0.021788129583001137 Epoch 17 MSE: 0.019598770886659622 Epoch 18 MSE: 0.01735163852572441 Epoch 19 MSE: 0.01525251753628254 Epoch 20 MSE: 0.01345239207148552 Epoch 21 MSE: 0.012037975713610649 Epoch 22 MSE: 0.011030289344489574 Epoch 23 MSE: 0.010390848852694035 Epoch 24 MSE: 0.010034598410129547

```
Epoch
       25 MSE:
                0.009847946465015411
Epoch
       26 MSE:
                0.009709222242236137
Epoch
       27 MSE:
                0.00950848963111639
       28 MSE:
Epoch
                0.009163789451122284
Epoch
       29 MSE:
                0.008631598204374313
       30 MSE:
Epoch
                0.007910448126494884
Epoch
       31 MSE:
                0.007037723436951637
Epoch
       32 MSE:
                0.0060806372202932835
Epoch
       33 MSE:
                0.005122888367623091
Epoch
       34 MSE:
                0.004248792305588722
       35 MSE:
                0.003526927437633276
Epoch
Epoch
       36 MSE:
                0.0029957741498947144
Epoch
       37 MSE:
                0.002654524752870202
Epoch
       38 MSE:
                0.0024625505320727825
Epoch
       39 MSE:
                0.002350008813664317
       40 MSE:
                0.002238771878182888
Epoch
Epoch
       41 MSE:
                0.002067751716822386
       42 MSE:
Epoch
                0.001812955946661532
Epoch
       43 MSE:
                0.001493616495281458
Epoch
       44 MSE:
                0.0011618263088166714
Epoch
       45 MSE:
                0.0008804677636362612
Epoch
       46 MSE:
                0.0006987605593167245
Epoch
       47 MSE:
                0.0006348308525048196
       48 MSE:
Epoch
                0.0006712157046422362
       49 MSE:
                0.0007638825918547809
Epoch
Epoch
       50 MSE:
                0.0008601820445619524
       51 MSE:
Epoch
                0.0009180687484331429
Epoch
       52 MSE:
                0.0009191518765874207
       53 MSE:
Epoch
                0.0008713420829735696
Epoch
       54 MSE:
                0.0008013212936930358
       55 MSE:
                0.0007408259552903473
Epoch
Epoch
       56 MSE:
                0.0007125916890799999
       57 MSE:
Epoch
                0.0007215572404675186
       58 MSE:
Epoch
                0.0007546085980720818
Epoch
       59 MSE:
                0.0007884004735387862
Epoch
       60 MSE:
                0.0008010356104932725
Epoch
       61 MSE:
                0.0007816759753040969
Epoch
       62 MSE:
                0.0007337409188039601
       63 MSE:
Epoch
                0.0006711739697493613
Epoch
       64 MSE:
                0.000610764604061842
       65 MSE:
Epoch
                0.0005647919024340808
       66 MSE:
Epoch
                0.0005371403531171381
       67 MSE:
Epoch
                0.0005237582954578102
Epoch
       68 MSE:
                0.0005162613233551383
Epoch
       69 MSE:
                0.0005064647411927581
Epoch
       70 MSE:
                0.0004897977923974395
Epoch
       71 MSE:
                0.000466477737063542
       72 MSE:
Epoch
                0.00044046901166439056
```

```
Epoch 73 MSE:
               0.00041710646473802626
Epoch 74 MSE:
               0.00040059391176328063
Epoch 75 MSE:
               0.0003923977492377162
Epoch 76 MSE:
               0.00039102204027585685
Epoch 77 MSE:
               0.0003930222010239959
Epoch 78 MSE:
               0.00039463507710024714
Epoch 79 MSE:
               0.0003932579420506954
Epoch 80 MSE:
               0.0003881961456499994
Epoch 81 MSE:
               0.000380502751795575
Epoch 82 MSE:
               0.00037214282201603055
Epoch 83 MSE:
               0.0003649518475867808
Epoch 84 MSE:
               0.0003598583862185478
Epoch 85 MSE:
               0.00035664098686538637
Epoch 86 MSE:
               0.0003542197518981993
Epoch 87 MSE:
               0.00035126664442941546
Epoch 88 MSE:
               0.00034681917168200016
Epoch 89 MSE:
               0.0003406442410778254
Epoch 90 MSE:
               0.00033323641400784254
Epoch 91 MSE:
               0.00032551318872720003
Epoch 92 MSE:
               0.0003183778317179531
Epoch 93 MSE:
               0.0003123583155684173
Epoch 94 MSE:
               0.0003074638661928475
Epoch 95 MSE:
               0.000303286244161427
Epoch 96 MSE:
               0.00029926502611488104
Epoch 97 MSE:
               0.000294973113341257
Epoch 98 MSE:
               0.0002902905980590731
Epoch 99 MSE:
               0.0002854070335160941
```

T-time: 11.514758825302124

Train Score: 0.50 RMSE

Validation Score: 11.71 RMSE

_____ Time Step = 30 | Hidden States = 4 | Num Layers = 2

Epoch 0 MSE: 0.1436184197664261 Epoch 1 MSE: 0.1094832792878151 Epoch 2 MSE: 0.0821676105260849 Epoch 3 MSE: 0.061953507363796234 Epoch 4 MSE: 0.04880587011575699 Epoch 5 MSE: 0.04236113280057907 Epoch 6 MSE: 0.041620783507823944 Epoch 7 MSE: 0.04454553872346878 Epoch 8 MSE: 0.04836833104491234

```
Epoch 9 MSE:
               0.050834186375141144
Epoch
       10 MSE:
                0.05102282017469406
Epoch
       11 MSE:
                0.04914330691099167
       12 MSE:
Epoch
                0.04595961794257164
Epoch
       13 MSE:
                0.04233471676707268
Epoch
       14 MSE:
                0.03897499665617943
Epoch
       15 MSE:
                0.036327064037323
Epoch 16 MSE:
                0.03457234427332878
Epoch 17 MSE:
                0.03367637097835541
Epoch
       18 MSE:
                0.03345925733447075
       19 MSE:
Epoch
                0.0336662121117115
      20 MSE:
Epoch
                0.03402752801775932
Epoch
      21 MSE:
                0.03430381789803505
Epoch
       22 MSE:
                0.03431626781821251
Epoch
      23 MSE:
                0.03396279737353325
Epoch 24 MSE:
                0.03322184458374977
Epoch
      25 MSE:
                0.032145507633686066
      26 MSE:
Epoch
                0.030843621119856834
Epoch
      27 MSE:
                0.02946051023900509
Epoch
      28 MSE:
                0.02814604341983795
Epoch
       29 MSE:
                0.027023382484912872
      30 MSE:
Epoch
                0.026158176362514496
Epoch 31 MSE:
                0.02553708478808403
      32 MSE:
Epoch
                0.025065623223781586
Epoch
      33 MSE:
                0.02459254488348961
Epoch
       34 MSE:
                0.023958027362823486
      35 MSE:
Epoch
                0.023049423471093178
Epoch
       36 MSE:
                0.02184179797768593
      37 MSE:
Epoch
                0.02040644735097885
Epoch 38 MSE:
                0.018884656950831413
      39 MSE:
Epoch
                0.017435351386666298
Epoch
       40 MSE:
                0.01617189310491085
Epoch
      41 MSE:
                0.015107354149222374
      42 MSE:
Epoch
                0.014133972115814686
Epoch
       43 MSE:
                0.013064871542155743
Epoch
      44 MSE:
                0.011742875911295414
Epoch
      45 MSE:
                0.010161374695599079
Epoch
      46 MSE:
                0.00849875994026661
      47 MSE:
Epoch
                0.00701147923246026
Epoch
      48 MSE:
                0.005840460304170847
Epoch 49 MSE:
                0.004887741524726152
       50 MSE:
Epoch
                0.0039213490672409534
Epoch
      51 MSE:
                0.0028562035877257586
Epoch
       52 MSE:
                0.0019121579825878143
Epoch
      53 MSE:
                0.0014125903835520148
Epoch
       54 MSE:
                0.001334658358246088
Epoch
       55 MSE:
                0.001246785745024681
       56 MSE:
                0.0010172647889703512
Epoch
```

Epoch	57 MSE:	0.001050526974722743	
Epoch	58 MSE:	0.0014707386726513505	
Epoch	59 MSE:	0.0018027713522315025	
Epoch	60 MSE:	0.0018545115599408746	
Epoch	61 MSE:	0.001987017458304763	
Epoch	62 MSE:	0.0022370556835085154	
Epoch	63 MSE:	0.0022244032006710768	
Epoch	64 MSE:	0.0020072711631655693	
Epoch	65 MSE:	0.0018829344771802425	
Epoch	66 MSE:	0.0017760212067514658	
Epoch	67 MSE:	0.0015214604791253805	
Epoch	68 MSE:	0.0012430871138349175	
Epoch	69 MSE:	0.001089791301637888	
Epoch	70 MSE:	0.0009910570224747062	
Epoch	71 MSE:	0.0008537188987247646	
Epoch	72 MSE:	0.0007327836356125772	
Epoch	73 MSE:	0.0007001374033279717	
Epoch	74 MSE:	0.0007212503696791828	
Epoch	75 MSE:	0.0007304437458515167	
Epoch	76 MSE:	0.0007287553744390607	
Epoch	77 MSE:	0.0007523744134232402	
Epoch	78 MSE:	0.000796590989921242	
Epoch	79 MSE:	0.0008221938624046743	
Epoch	80 MSE:	0.0008166597108356655	
Epoch	81 MSE:	0.0008034627535380423	
Epoch	82 MSE:	0.0007982741808518767	
Epoch	83 MSE:	0.0007878367905505002	
Epoch	84 MSE:	0.0007574037881568074	
Epoch	85 MSE:	0.000716442649718374	
Epoch	86 MSE:	0.0006835339590907097	
Epoch	87 MSE:	0.000659369514323771	
Epoch	88 MSE:	0.0006313305930234492	
Epoch	89 MSE:	0.0005983242299407721	
Epoch	90 MSE:	0.000572973454836756	
Epoch	91 MSE:	0.0005601720185950398	
Epoch	92 MSE:	0.0005506441229954362	
Epoch	93 MSE:	0.0005385380354709923	
Epoch	94 MSE:	0.0005300610791891813	
Epoch	95 MSE:	0.0005294851725921035	
Epoch	96 MSE:	0.0005301382625475526	
Epoch	97 MSE:	0.0005260946927592158	
Epoch	98 MSE:	0.0005210416275076568	
Epoch	99 MSE:	0.0005187313654460013	
T-time: 20.742391347885132			

Train Score: 0.68 RMSE

Validation Score: 12.74 RMSE

Time Step = 30 | Hidden States = 8 | Num Layers = 1

Epoch 0 MSE: 0.21351739764213562 Epoch 1 MSE: 0.164730042219162 Epoch 2 MSE: 0.12436427921056747 Epoch 3 MSE: 0.09208180010318756 Epoch 4 MSE: 0.06759892404079437 Epoch 5 MSE: 0.050512317568063736 Epoch 6 MSE: 0.040263187140226364 Epoch 7 MSE: 0.036045171320438385 Epoch 8 MSE: 0.036608047783374786 Epoch 9 MSE: 0.04003872349858284Epoch 10 MSE: 0.043997667729854584 Epoch 11 MSE: 0.04662675783038139 Epoch 12 MSE: 0.04713103175163269 Epoch 13 MSE: 0.04560443013906479 Epoch 14 MSE: 0.042607855051755905 Epoch 15 MSE: 0.03883108124136925 Epoch 16 MSE: 0.0348941832780838 Epoch 17 MSE: 0.03125745430588722 Epoch 18 MSE: 0.028200820088386536 Epoch 19 MSE: 0.025842251256108284 Epoch 20 MSE: 0.02417420968413353 Epoch 21 MSE: 0.023104529827833176 Epoch 22 MSE: 0.02249378152191639 Epoch 23 MSE: 0.022185439243912697 Epoch 24 MSE: 0.02202806994318962 Epoch 25 MSE: 0.02189008705317974 Epoch 26 MSE: 0.02166835591197014 Epoch 27 MSE: 0.021291956305503845 Epoch 28 MSE: 0.020722297951579094 Epoch 29 MSE: 0.019950561225414276 Epoch 30 MSE: 0.01899326965212822 Epoch 31 MSE: 0.017886633053421974 Epoch 32 MSE: 0.0166801568120718 Epoch 33 MSE: 0.015429922379553318 Epoch 34 MSE: 0.01419189665466547 Epoch 35 MSE: 0.013015655800700188 Epoch 36 MSE: 0.011938859708607197 Epoch 37 MSE: 0.010983036831021309 Epoch 38 MSE: 0.01015122327953577 Epoch 39 MSE: 0.009428092278540134 Epoch 40 MSE: 0.008783013559877872

```
Epoch
       41 MSE:
                0.008176049217581749
Epoch
       42 MSE:
                0.0075661917217075825
       43 MSE:
Epoch
                0.00692035211250186
       44 MSE:
Epoch
                0.006221011281013489
Epoch
       45 MSE:
                0.0054704430513083935
       46 MSE:
Epoch
                0.0046902489848434925
Epoch
       47 MSE:
                0.0039160894230008125
Epoch
       48 MSE:
                0.0031889728270471096
Epoch 49 MSE:
                0.0025453930720686913
Epoch
       50 MSE:
                0.002008900512009859
       51 MSE:
                0.0015853125369176269
Epoch
Epoch
       52 MSE:
                0.0012627788819372654
Epoch
       53 MSE:
                0.001016636728309095
Epoch
       54 MSE:
                0.0008176728733815253
Epoch
       55 MSE:
                0.000641348771750927
Epoch 56 MSE:
                0.0004751388914883137
Epoch
       57 MSE:
                0.0003215102478861809
       58 MSE:
Epoch
                0.00019529163546394557
Epoch
       59 MSE:
                0.00011597734555834904
Epoch
       60 MSE:
                9.750857134349644e-05
Epoch
       61 MSE:
                0.00013960291107650846
Epoch
       62 MSE:
                0.00022489324328489602
Epoch
       63 MSE:
                0.0003241243539378047
       64 MSE:
Epoch
                0.0004075949836988002
       65 MSE:
                0.0004570266464725137
Epoch
Epoch
       66 MSE:
                0.000471253355499357
       67 MSE:
Epoch
                0.00046283614938147366
Epoch
       68 MSE:
                0.00044842352508567274
       69 MSE:
Epoch
                0.0004390637041069567
Epoch
      70 MSE:
                0.0004356926365289837
      71 MSE:
Epoch
                0.0004310924850869924
Epoch
       72 MSE:
                0.0004158492374699563
                0.00038433808367699385
Epoch
       73 MSE:
       74 MSE:
Epoch
                0.0003377113025635481
Epoch
       75 MSE:
                0.0002830395824275911
Epoch
       76 MSE:
                0.00022977543994784355
Epoch
      77 MSE:
                0.00018568245286587626
Epoch
       78 MSE:
                0.0001541810343042016
       79 MSE:
Epoch
                0.00013404269702732563
Epoch
       80 MSE:
                0.00012112237163819373
       81 MSE:
Epoch
                0.00011094022920588031
       82 MSE:
Epoch
                0.00010076151374960318
Epoch
       83 MSE:
                9.033432434080169e-05
Epoch
       84 MSE:
                8.125745807774365e-05
Epoch
       85 MSE:
                7.559829100500792e-05
Epoch
       86 MSE:
                7.458018808392808e-05
Epoch
       87 MSE:
                7.792992983013391e-05
       88 MSE:
                8.403970423387364e-05
Epoch
```

Epoch 89 MSE: 9.070222586160526e-05
Epoch 90 MSE: 9.598826727597043e-05
Epoch 91 MSE: 9.886678162729368e-05
Epoch 92 MSE: 9.93604990071617e-05
Epoch 93 MSE: 9.825827146414667e-05
Epoch 94 MSE: 9.658539784140885e-05
Epoch 95 MSE: 9.509457595413551e-05
Epoch 96 MSE: 9.399078408023342e-05
Epoch 97 MSE: 9.296715870732442e-05
Epoch 98 MSE: 9.148293611360714e-05
Epoch 99 MSE: 8.91140807652846e-05

T-time: 13.115161657333374

Train Score: 0.28 RMSE

Validation Score: 6.58 RMSE

Time Step = 30 | Hidden States = 8 | Num Layers = 2

Epoch 0 MSE: 0.036985356360673904 Epoch 1 MSE: 0.03314022719860077 Epoch 2 MSE: 0.03371749818325043 Epoch 3 MSE: 0.02924608625471592 Epoch 4 MSE: 0.026496101170778275 Epoch 5 MSE: 0.02625010907649994 Epoch 6 MSE: 0.024669194594025612 Epoch 7 MSE: 0.020849399268627167 Epoch 8 MSE: 0.01729733496904373 Epoch 9 MSE: 0.01545712724328041 Epoch 10 MSE: 0.013237955048680305 Epoch 11 MSE: 0.00919547863304615 Epoch 12 MSE: 0.005677820648998022 Epoch 13 MSE: 0.004274210426956415 Epoch 14 MSE: 0.00218124408274889 Epoch 15 MSE: 0.00017289200332015753 Epoch 16 MSE: 0.0018237725598737597 Epoch 17 MSE: 0.0022095083259046078 Epoch 18 MSE: 0.0033004777505993843 Epoch 19 MSE: 0.004816312808543444 Epoch 20 MSE: 0.0035554144997149706 Epoch 21 MSE: 0.003253368893638253 Epoch 22 MSE: 0.0022909604012966156 Epoch 23 MSE: 0.0008338794577866793 Epoch 24 MSE: 0.0005618659779429436

```
Epoch
       25 MSE:
                0.0005009935121051967
Epoch
       26 MSE:
                0.0002700543846003711
Epoch
       27 MSE:
                0.0004934340249747038
       28 MSE:
Epoch
                0.000973257003352046
Epoch
       29 MSE:
                0.0011502079432830215
       30 MSE:
Epoch
                0.0011257764417678118
Epoch
       31 MSE:
                0.0012138942256569862
Epoch
       32 MSE:
                0.0012878740672022104
Epoch
       33 MSE:
                0.0011043797712773085
Epoch
       34 MSE:
                0.0008022024994716048
       35 MSE:
                0.0006311459001153708
Epoch
Epoch
       36 MSE:
                0.0005090520717203617
       37 MSE:
                0.00028442012262530625
Epoch
Epoch
       38 MSE:
                0.00012559328752104193
Epoch
       39 MSE:
                0.00016858721210155636
      40 MSE:
                0.00022212717158254236
Epoch
Epoch
       41 MSE:
                0.000226540447329171
       42 MSE:
                0.0003340729745104909
Epoch
Epoch
       43 MSE:
                0.0004348524089436978
Epoch
       44 MSE:
                0.00039743815432302654
Epoch
       45 MSE:
                0.00036438563256524503
Epoch
       46 MSE:
                0.00034211541060358286
Epoch
       47 MSE:
                0.0002379098004894331
       48 MSE:
Epoch
                0.00015431895735673606
       49 MSE:
                0.00014067125448491424
Epoch
Epoch
       50 MSE:
                0.00011450525198597461
       51 MSE:
Epoch
                9.730747842695564e-05
Epoch
       52 MSE:
                0.0001339448062935844
       53 MSE:
Epoch
                0.00016578557551838458
Epoch
       54 MSE:
                0.00016791047528386116
      55 MSE:
Epoch
                0.00018071362865157425
Epoch
       56 MSE:
                0.00019042694475501776
       57 MSE:
Epoch
                0.00016653590137138963
       58 MSE:
                0.00013991919695399702
Epoch
Epoch
       59 MSE:
                0.0001276279508601874
Epoch
       60 MSE:
                0.00010527957056183368
Epoch
       61 MSE:
                8.497262024320662e-05
Epoch
       62 MSE:
                8.797337068244815e-05
       63 MSE:
Epoch
                9.201667126035318e-05
Epoch
       64 MSE:
                9.229007991962135e-05
       65 MSE:
Epoch
                0.00010439481411594898
       66 MSE:
Epoch
                0.00011114118387922645
       67 MSE:
Epoch
                0.00010566796117927879
Epoch
       68 MSE:
                0.00010377125727245584
Epoch
       69 MSE:
                9.784718713490292e-05
Epoch
       70 MSE:
                8.52206940180622e-05
Epoch
       71 MSE:
                7.995138730620965e-05
       72 MSE:
Epoch
                7.728247146587819e-05
```

```
Epoch 73 MSE:
               7.31754771550186e-05
Epoch 74 MSE:
               7.553488103440031e-05
Epoch 75 MSE:
               7.909375563031062e-05
Epoch 76 MSE:
               7.888913387432694e-05
Epoch 77 MSE:
               8.028353477129713e-05
Epoch 78 MSE:
               8.032181358430535e-05
Epoch 79 MSE:
               7.625704893143848e-05
Epoch 80 MSE:
               7.349526276811957e-05
Epoch 81 MSE:
               7.101775554474443e-05
Epoch 82 MSE:
               6.727770232828334e-05
Epoch 83 MSE:
               6.628615665249527e-05
Epoch 84 MSE:
               6.638060585828498e-05
Epoch 85 MSE:
               6.57582568237558e-05
Epoch 86 MSE:
               6.666537228738889e-05
Epoch 87 MSE:
               6.697847129544243e-05
Epoch 88 MSE:
               6.581100751645863e-05
Epoch 89 MSE:
               6.514940469060093e-05
Epoch 90 MSE:
               6.362426211126149e-05
Epoch 91 MSE:
               6.163213402032852e-05
Epoch 92 MSE:
               6.0712329286616296e-05
Epoch 93 MSE:
               5.9649690228980035e-05
Epoch 94 MSE:
               5.892682384001091e-05
Epoch 95 MSE:
               5.9003035858040676e-05
Epoch 96 MSE:
               5.862106627319008e-05
Epoch 97 MSE:
               5.825829430250451e-05
Epoch 98 MSE:
               5.793706441181712e-05
Epoch 99 MSE:
               5.697598680853844e-05
```

T-time: 26.715670347213745

Train Score: 0.23 RMSE Validation Score: 6.12 RMSE

_____ Time Step = 30 | Hidden States = 16 | Num Layers = 1 ______

Epoch 0 MSE: 0.06656069308519363 Epoch 1 MSE: 0.04400709643959999 Epoch 2 MSE: 0.033478207886219025 Epoch 3 MSE: 0.03324396535754204 Epoch 4 MSE: 0.035320982336997986 Epoch 5 MSE: 0.0336645282804966 Epoch 6 MSE: 0.02948327176272869 Epoch 7 MSE: 0.025410495698451996 Epoch 8 MSE: 0.02278260327875614

```
9 MSE:
Epoch
               0.021626513451337814
Epoch
       10 MSE:
                0.021211277693510056
Epoch
       11 MSE:
                0.02061803825199604
       12 MSE:
Epoch
                0.01926291175186634
Epoch
       13 MSE:
                0.01712622679769993
Epoch
       14 MSE:
                0.014615006744861603
Epoch
       15 MSE:
                0.012286053039133549
Epoch
       16 MSE:
                0.010558963753283024
Epoch 17 MSE:
                0.009454717859625816
Epoch
       18 MSE:
                0.008511977270245552
       19 MSE:
Epoch
                0.007135134655982256
       20 MSE:
Epoch
                0.005150482524186373
Epoch
       21 MSE:
                0.003002488287165761
Epoch
       22 MSE:
                0.0014745764201506972
Epoch
       23 MSE:
                0.0010675411904230714
Epoch
      24 MSE:
                0.0013060973724350333
Epoch
       25 MSE:
                0.0011892961338162422
       26 MSE:
Epoch
                0.0008551861974410713
Epoch
       27 MSE:
                0.0013687515165656805
Epoch
       28 MSE:
                0.002516166539862752
       29 MSE:
Epoch
                0.0027243196964263916
       30 MSE:
Epoch
                0.0019303420558571815
Epoch
       31 MSE:
                0.0012605045922100544
       32 MSE:
Epoch
                0.001069366466253996
Epoch
       33 MSE:
                0.000906355504412204
Epoch
       34 MSE:
                0.0005415533669292927
       35 MSE:
Epoch
                0.00018492508388590068
Epoch
       36 MSE:
                6.949693488422781e-05
       37 MSE:
Epoch
                0.0001910113642225042
Epoch
       38 MSE:
                0.000374839932192117
       39 MSE:
Epoch
                0.0004728281346615404
Epoch
       40 MSE:
                0.0004691320355050266
Epoch
       41 MSE:
                0.000438381772255525
       42 MSE:
                0.00044580866233445704
Epoch
Epoch
       43 MSE:
                0.0004896598402410746
Epoch
       44 MSE:
                0.0005174748366698623
Epoch
       45 MSE:
                0.0004831004480365664
Epoch
       46 MSE:
                0.00038895304896868765
       47 MSE:
Epoch
                0.00028091721469536424
Epoch
       48 MSE:
                0.00020638349815271795
      49 MSE:
                0.00017524762370157987
Epoch
       50 MSE:
Epoch
                0.00015916439588181674
Epoch
       51 MSE:
                0.0001279949938179925
Epoch
       52 MSE:
                8.416634955210611e-05
Epoch
       53 MSE:
                5.770516145275906e-05
Epoch
       54 MSE:
                6.933645636308938e-05
Epoch
       55 MSE:
                0.00010536506306380033
       56 MSE:
                0.00013297013356350362
Epoch
```

```
Epoch 57 MSE:
                0.00013577814388554543
Epoch 58 MSE:
                0.00012659208732657135
Epoch 59 MSE:
                0.00012511313252616674
Epoch 60 MSE:
                0.00013192144979257137
Epoch 61 MSE:
                0.00013081778888590634
Epoch 62 MSE:
                0.00011243904737057164
Epoch
      63 MSE:
                8.642177999718115e-05
Epoch 64 MSE:
                6.879131979076192e-05
Epoch 65 MSE:
                6.404546729754657e-05
Epoch 66 MSE:
                6.38224883005023e-05
Epoch 67 MSE:
                5.9931266150670126e-05
Epoch 68 MSE:
                5.368033089325763e-05
Epoch 69 MSE:
                5.190322917769663e-05
Epoch 70 MSE:
                5.7195535191567615e-05
Epoch 71 MSE:
                6.472896347986534e-05
Epoch 72 MSE:
                6.815384404035285e-05
Epoch 73 MSE:
                6.63401951896958e-05
Epoch 74 MSE:
                6.319882959360257e-05
Epoch 75 MSE:
                6.20513383182697e-05
Epoch 76 MSE:
                6.195447349455208e-05
Epoch 77 MSE:
                5.98369151703082e-05
Epoch 78 MSE:
                5.492320633493364e-05
Epoch 79 MSE:
                4.9790691264206544e-05
Epoch 80 MSE:
                4.7200563130900264e-05
Epoch 81 MSE:
                4.7048240958247334e-05
Epoch 82 MSE:
                4.711973815574311e-05
Epoch 83 MSE:
                4.620179970515892e-05
Epoch 84 MSE:
                4.532386446953751e-05
Epoch 85 MSE:
                4.584372800309211e-05
Epoch 86 MSE:
                4.735010224976577e-05
Epoch 87 MSE:
               4.8190286179305986e-05
Epoch 88 MSE:
                4.7593795898137614e-05
Epoch 89 MSE:
                4.6399560233112425e-05
Epoch 90 MSE:
                4.565919516608119e-05
Epoch 91 MSE:
                4.5285407395567745e-05
Epoch 92 MSE:
                4.4499440264189616e-05
Epoch 93 MSE:
                4.3145857489435e-05
Epoch 94 MSE:
                4.193802669760771e-05
Epoch 95 MSE:
                4.146286300965585e-05
Epoch 96 MSE:
                4.147799336351454e-05
Epoch 97 MSE:
                4.138601434533484e-05
Epoch 98 MSE:
               4.105043990421109e-05
Epoch 99 MSE:
                4.082003579242155e-05
T-time: 18.247771978378296
```

Train Score: 0.19 RMSE

Time Step = 30 | Hidden States = 16 | Num Layers = 2

```
Epoch 0 MSE: 0.12340614199638367
Epoch 1 MSE: 0.06406713277101517
Epoch 2 MSE: 0.03487955033779144
Epoch 3 MSE:
              0.03404304012656212
Epoch 4 MSE:
              0.044927142560482025
Epoch 5 MSE:
              0.04334626719355583
Epoch 6 MSE: 0.03541189432144165
Epoch 7 MSE:
              0.029305173084139824
Epoch 8 MSE:
              0.027143757790327072
Epoch 9 MSE:
              0.027600044384598732
Epoch 10 MSE: 0.028556503355503082
Epoch 11 MSE: 0.028456365689635277
Epoch 12 MSE:
               0.026773327961564064
Epoch 13 MSE:
               0.02378123253583908
Epoch 14 MSE:
               0.02014882117509842
Epoch 15 MSE:
               0.0166487954556942
Epoch 16 MSE:
               0.013932515867054462
Epoch 17 MSE:
               0.012189029715955257
Epoch 18 MSE:
               0.010705769062042236
Epoch 19 MSE:
               0.008163676597177982
Epoch 20 MSE:
               0.004212015774101019
Epoch 21 MSE:
               0.0007126510026864707
Epoch 22 MSE:
               0.0009732190519571304
Epoch 23 MSE:
               0.004776041489094496
Epoch 24 MSE:
               0.005584117025136948
Epoch 25 MSE:
               0.0036646679509431124
Epoch 26 MSE:
               0.0026361376512795687
Epoch 27 MSE:
               0.0023903390392661095
Epoch 28 MSE:
               0.0015552989207208157
Epoch 29 MSE:
               0.0005988231278024614
Epoch 30 MSE:
               0.0003671535523608327
Epoch 31 MSE:
               0.0008614282123744488
Epoch 32 MSE:
               0.0015532710822299123
Epoch 33 MSE:
               0.001965197967365384
Epoch 34 MSE:
               0.001923967618495226
Epoch 35 MSE:
               0.0015428685583174229
Epoch 36 MSE:
               0.0010826329234987497
Epoch 37 MSE:
               0.0007756960112601519
Epoch 38 MSE:
               0.0006797664682380855
Epoch 39 MSE:
               0.0006561516202054918
Epoch 40 MSE:
               0.0005301616620272398
```

```
Epoch 41 MSE:
                0.0003023058525286615
Epoch
       42 MSE:
                0.00015867152251303196
       43 MSE:
Epoch
                0.0002468964667059481
       44 MSE:
Epoch
                0.0004875654121860862
Epoch
       45 MSE:
                0.0006507915677502751
Epoch
       46 MSE:
                0.0005985276075080037
Epoch
       47 MSE:
                0.00040442601311951876
Epoch
       48 MSE:
                0.00024043887970037758
Epoch 49 MSE:
                0.00019233240163885057
Epoch
      50 MSE:
                0.0002082519349642098
       51 MSE:
                0.00020185763423796743
Epoch
Epoch
       52 MSE:
                0.00015863828593865037
Epoch
       53 MSE:
                0.00012903135211672634
Epoch
       54 MSE:
                0.0001516678894404322
Epoch
      55 MSE:
                0.0002092532959068194
Epoch 56 MSE:
                0.00025046011433005333
Epoch
      57 MSE:
                0.0002393423783360049
       58 MSE:
Epoch
                0.00018365733558312058
Epoch
       59 MSE:
                0.00012317337677814066
Epoch
       60 MSE:
                9.285631676902995e-05
Epoch
       61 MSE:
                9.451881487620994e-05
Epoch
       62 MSE:
                0.00010287985787726939
Epoch
       63 MSE:
                9.803999273572117e-05
       64 MSE:
Epoch
                8.651495591038838e-05
       65 MSE:
                8.717457967577502e-05
Epoch
Epoch
       66 MSE:
                0.0001032620930345729
       67 MSE:
Epoch
                0.00011700404866132885
Epoch
       68 MSE:
                0.00011102672578999773
       69 MSE:
Epoch
                8.798065391601995e-05
Epoch
     70 MSE:
                6.608860712731257e-05
Epoch 71 MSE:
                5.8880374126601964e-05
Epoch
      72 MSE:
                6.341805419651791e-05
Epoch
      73 MSE:
                6.7927387135569e-05
      74 MSE:
Epoch
                6.648371345363557e-05
Epoch
      75 MSE:
                6.312108598649502e-05
Epoch
      76 MSE:
                6.353743083309382e-05
Epoch
      77 MSE:
                6.694010517094284e-05
Epoch
      78 MSE:
                6.743925769114867e-05
      79 MSE:
Epoch
                6.164613296277821e-05
Epoch
       80 MSE:
                5.2853381930617616e-05
       81 MSE:
                4.736110713565722e-05
Epoch
Epoch
       82 MSE:
                4.7708352212794125e-05
Epoch
       83 MSE:
                5.066502853878774e-05
Epoch
       84 MSE:
                5.178520586923696e-05
Epoch
       85 MSE:
                5.0391434342600405e-05
Epoch
       86 MSE:
                4.9009438953362405e-05
Epoch
       87 MSE:
                4.9065969506045803e-05
       88 MSE:
Epoch
                4.907344191451557e-05
```

Epoch 89 MSE: 4.716778494184837e-05
Epoch 90 MSE: 4.393039125716314e-05
Epoch 91 MSE: 4.173415436525829e-05
Epoch 92 MSE: 4.182828706689179e-05
Epoch 93 MSE: 4.304547837818973e-05
Epoch 94 MSE: 4.3480646127136424e-05
Epoch 95 MSE: 4.266736868885346e-05
Epoch 96 MSE: 4.159729724051431e-05
Epoch 97 MSE: 4.105296829948202e-05
Epoch 98 MSE: 4.0685205021873116e-05
Epoch 99 MSE: 3.9824124542064965e-05

T-time: 39.022674798965454

Time Step = 30 | Hidden States = 32 | Num Layers = 1

Epoch 0 MSE: 0.042843353003263474 Epoch 1 MSE: 0.03270935267210007 Epoch 2 MSE: 0.03124498762190342 Epoch 3 MSE: 0.025008242577314377 Epoch 4 MSE: 0.019258633255958557 Epoch 5 MSE: 0.01602357067167759 Epoch 6 MSE: 0.012408273294568062 Epoch 7 MSE: 0.006237407214939594 Epoch 8 MSE: 0.0013294810196384788 Epoch 9 MSE: 0.005380404647439718 Epoch 10 MSE: 0.003150835633277893 Epoch 11 MSE: 0.0034945064689964056 Epoch 12 MSE: 0.0036857377272099257 Epoch 13 MSE: 0.0011881171958521008 Epoch 14 MSE: 0.00012308255827520043 Epoch 15 MSE: 0.0011960119009017944 Epoch 16 MSE: 0.002275234553962946 Epoch 17 MSE: 0.00209730863571167 Epoch 18 MSE: 0.0013001244515180588 Epoch 19 MSE: 0.0008742795325815678 Epoch 20 MSE: 0.0010253657819703221 Epoch 21 MSE: 0.0012263153912499547 Epoch 22 MSE: 0.0009674275061115623 Epoch 23 MSE: 0.00036626734072342515 Epoch 24 MSE: 2.199248774559237e-05

```
Epoch
       25 MSE:
                0.000276678561931476
Epoch
       26 MSE:
                0.0007096833433024585
Epoch
       27 MSE:
                0.0007076485198922455
       28 MSE:
Epoch
                0.0003773518546950072
Epoch
       29 MSE:
                0.00023356100427918136
Epoch
       30 MSE:
                0.0003572253917809576
Epoch
       31 MSE:
                0.0004187347658444196
Epoch
       32 MSE:
                0.0002599924337118864
Epoch
       33 MSE:
                6.487038626801223e-05
Epoch
       34 MSE:
                4.685270687332377e-05
       35 MSE:
                0.00018392264610156417
Epoch
Epoch
       36 MSE:
                0.00028856840799562633
Epoch
       37 MSE:
                0.00025293664657510817
Epoch
       38 MSE:
                0.00014842422388028353
Epoch
       39 MSE:
                9.997732558986172e-05
Epoch 40 MSE:
                0.00013119098730385303
Epoch
       41 MSE:
                0.00015975291898939759
       42 MSE:
Epoch
                0.00011916370567632839
Epoch
       43 MSE:
                4.474912566365674e-05
Epoch
       44 MSE:
                2.1532297978410497e-05
Epoch
       45 MSE:
                6.806514284107834e-05
Epoch
       46 MSE:
                0.00011381167132640257
Epoch 47 MSE:
                0.00010091196600114927
       48 MSE:
Epoch
                5.859638986294158e-05
       49 MSE:
                4.551849633571692e-05
Epoch
Epoch
       50 MSE:
                6.308012234512717e-05
       51 MSE:
Epoch
                6.769868923583999e-05
Epoch
       52 MSE:
                4.327630085754208e-05
       53 MSE:
Epoch
                2.0194511307636276e-05
Epoch 54 MSE:
                2.5933199140126817e-05
Epoch 55 MSE:
                4.7540917876176536e-05
Epoch
       56 MSE:
                5.4552918300032616e-05
      57 MSE:
Epoch
                4.1355415305588394e-05
       58 MSE:
Epoch
                2.8862797989859246e-05
Epoch
       59 MSE:
                3.084530180785805e-05
Epoch
       60 MSE:
                3.693790131364949e-05
Epoch
       61 MSE:
                3.2422780350316316e-05
Epoch
       62 MSE:
                2.1102938262629323e-05
Epoch
       63 MSE:
                1.7991360437008552e-05
Epoch
       64 MSE:
                2.5770119464141317e-05
       65 MSE:
Epoch
                3.173542791046202e-05
       66 MSE:
Epoch
                2.802823655656539e-05
Epoch
       67 MSE:
                2.188076905440539e-05
Epoch
       68 MSE:
                2.1766276404378004e-05
Epoch
       69 MSE:
                2.457958908053115e-05
Epoch
       70 MSE:
                2.3126533051254228e-05
Epoch
       71 MSE:
                1.849148429755587e-05
       72 MSE:
Epoch
                1.727827293507289e-05
```

```
Epoch 73 MSE:
               2.052927993645426e-05
Epoch 74 MSE:
               2.2747533876099624e-05
Epoch 75 MSE:
               2.0996923922211863e-05
Epoch 76 MSE:
               1.8605282093631104e-05
Epoch 77 MSE:
               1.8796945369103923e-05
Epoch 78 MSE:
               1.9834669728879817e-05
Epoch 79 MSE:
               1.8893922970164567e-05
Epoch 80 MSE:
               1.7019039660226554e-05
Epoch 81 MSE:
               1.6985188267426565e-05
               1.849424916144926e-05
Epoch 82 MSE:
Epoch 83 MSE:
               1.89548318303423e-05
Epoch 84 MSE:
               1.787653673090972e-05
Epoch 85 MSE:
               1.7174419554066844e-05
Epoch 86 MSE:
               1.757402060320601e-05
Epoch 87 MSE:
               1.7728389138937928e-05
Epoch 88 MSE:
               1.698232881608419e-05
Epoch 89 MSE:
               1.645882184675429e-05
Epoch 90 MSE:
               1.6893620340852067e-05
Epoch 91 MSE:
               1.7405978724127635e-05
Epoch 92 MSE:
               1.7158952687168494e-05
Epoch 93 MSE:
               1.667603282839991e-05
Epoch 94 MSE:
               1.668017102929298e-05
Epoch 95 MSE:
               1.685604001977481e-05
Epoch 96 MSE:
               1.664023511693813e-05
Epoch 97 MSE:
               1.6302572475979105e-05
Epoch 98 MSE:
               1.6365260307793505e-05
Epoch 99 MSE:
               1.6629777746857144e-05
```

T-time: 53.44296097755432

Train Score: 0.12 RMSE

Validation Score: 1.49 RMSE

Time Step = 30 | Hidden States = 32 | Num Layers = 2

Epoch 0 MSE: 0.07188298553228378
Epoch 1 MSE: 0.053305916488170624
Epoch 2 MSE: 0.04246915504336357
Epoch 3 MSE: 0.028966883197426796
Epoch 4 MSE: 0.02870110236108303
Epoch 5 MSE: 0.028383148834109306
Epoch 6 MSE: 0.021043457090854645
Epoch 7 MSE: 0.011616728268563747
Epoch 8 MSE: 0.008804050274193287

```
Epoch 9 MSE:
               0.010037313215434551
Epoch
       10 MSE:
                0.0026903352700173855
Epoch 11 MSE:
                0.0025744056329131126
       12 MSE:
Epoch
                0.008982857689261436
Epoch
       13 MSE:
                0.004716330207884312
Epoch
       14 MSE:
                0.00032993112108670175
Epoch
       15 MSE:
                0.0012185352388769388
Epoch 16 MSE:
                0.0032431792933493853
Epoch 17 MSE:
                0.0033282649237662554
Epoch
       18 MSE:
                0.0024382546544075012
       19 MSE:
                0.001991882687434554
Epoch
      20 MSE:
Epoch
                0.0021021547727286816
Epoch
      21 MSE:
                0.0021033601369708776
Epoch
      22 MSE:
                0.0014963347930461168
Epoch
      23 MSE:
                0.0005372645100578666
Epoch 24 MSE:
                0.00014023025869391859
Epoch
      25 MSE:
                0.0008262958726845682
      26 MSE:
Epoch
                0.0015983658377081156
Epoch
      27 MSE:
                0.0012770825996994972
Epoch
      28 MSE:
                0.0004601903783623129
Epoch
       29 MSE:
                0.0001586748257977888
Epoch
      30 MSE:
                0.00036582601023837924
Epoch
      31 MSE:
                0.0005807005218230188
      32 MSE:
Epoch
                0.0005612549721263349
      33 MSE:
                0.0004233001091051847
Epoch
Epoch
       34 MSE:
                0.0003709389711730182
      35 MSE:
Epoch
                0.000440480827819556
Epoch
       36 MSE:
                0.0004736969422083348
      37 MSE:
Epoch
                0.0003364176372997463
Epoch 38 MSE:
                0.00011950251064263284
      39 MSE:
Epoch
                3.7810325011378154e-05
Epoch
       40 MSE:
                0.0001539487566333264
                0.0003046983038075268
Epoch
      41 MSE:
      42 MSE:
Epoch
                0.00031355046667158604
Epoch
       43 MSE:
                0.0001935863692779094
Epoch
      44 MSE:
                9.243858221452683e-05
Epoch
      45 MSE:
                8.912904741009697e-05
Epoch
      46 MSE:
                0.00012397044338285923
      47 MSE:
Epoch
                0.00012108691589673981
Epoch
      48 MSE:
                9.238821075996384e-05
Epoch 49 MSE:
                9.046741615748033e-05
       50 MSE:
Epoch
                0.00011986259778495878
Epoch
      51 MSE:
                0.0001342788600595668
Epoch
      52 MSE:
                0.00010202200064668432
Epoch
      53 MSE:
                4.8537760449107736e-05
Epoch
       54 MSE:
                2.6892730602412485e-05
Epoch
       55 MSE:
                5.220639650360681e-05
       56 MSE:
                8.371141302632168e-05
Epoch
```

```
Epoch 57 MSE:
                8.1736667198129e-05
Epoch 58 MSE:
                5.729850090574473e-05
Epoch 59 MSE:
                4.392337359604426e-05
Epoch
      60 MSE:
                4.720429933513515e-05
Epoch 61 MSE:
                4.820691901841201e-05
Epoch 62 MSE:
                3.945517892134376e-05
Epoch
      63 MSE:
                3.3896154491230845e-05
Epoch 64 MSE:
                4.098954741493799e-05
Epoch 65 MSE:
                5.045819125371054e-05
Epoch 66 MSE:
                4.7121142415562645e-05
Epoch 67 MSE:
                3.312211993033998e-05
Epoch 68 MSE:
                2.4375502107432112e-05
Epoch 69 MSE:
                2.8136710170656443e-05
Epoch 70 MSE:
                3.5265002225060016e-05
Epoch 71 MSE:
                3.555831790436059e-05
Epoch 72 MSE:
                3.093710620305501e-05
Epoch 73 MSE:
                2.8750295314239338e-05
Epoch 74 MSE:
                2.9369322874117643e-05
Epoch 75 MSE:
                2.801564369292464e-05
Epoch 76 MSE:
                2.4668293917784467e-05
Epoch
     77 MSE:
                2.4040322387008928e-05
Epoch 78 MSE:
                2.7047341063735075e-05
Epoch 79 MSE:
                2.8982532967347652e-05
Epoch 80 MSE:
                2.6729789169621654e-05
Epoch 81 MSE:
                2.310210584255401e-05
Epoch 82 MSE:
                2.2228561647352763e-05
Epoch 83 MSE:
                2.376486918365117e-05
Epoch 84 MSE:
                2.449627936584875e-05
Epoch 85 MSE:
                2.3639911887585185e-05
Epoch 86 MSE:
                2.3043798137223348e-05
Epoch 87 MSE:
                2.3258959117811173e-05
Epoch 88 MSE:
                2.2920017727301456e-05
Epoch 89 MSE:
                2.1743075194535777e-05
Epoch 90 MSE:
                2.1224190277280286e-05
Epoch
      91 MSE:
                2.198802940256428e-05
Epoch 92 MSE:
                2.2660660761175677e-05
Epoch 93 MSE:
                2.21135178435361e-05
Epoch 94 MSE:
                2.111711546604056e-05
Epoch 95 MSE:
                2.0854098693234846e-05
Epoch 96 MSE:
                2.1143861886230297e-05
Epoch 97 MSE:
                2.1160849428270012e-05
Epoch 98 MSE:
                2.090117777697742e-05
Epoch 99 MSE:
                2.085902087856084e-05
T-time: 87.9983274936676
```

Train Score: 0.14 RMSE

Time Step = 50 | Hidden States = 2 | Num Layers = 1

Epoch 0 MSE: 0.0742608904838562 Epoch 1 MSE: 0.062009457498788834 Epoch 2 MSE: 0.052402522414922714 Epoch 3 MSE: 0.045642729848623276 Epoch 4 MSE: 0.041738227009773254 Epoch 5 MSE: 0.04032587260007858 Epoch 6 MSE: 0.04052198305726051 Epoch 7 MSE: 0.041090745478868484 Epoch 8 MSE: 0.041023656725883484 Epoch 9 MSE: 0.03993842750787735Epoch 10 MSE: 0.03798532113432884 Epoch 11 MSE: 0.03556614741683006 Epoch 12 MSE: 0.0331113375723362 Epoch 13 MSE: 0.030954057350754738 Epoch 14 MSE: 0.029274750500917435 Epoch 15 MSE: 0.028094112873077393 Epoch 16 MSE: 0.027302978560328484 Epoch 17 MSE: 0.026717592030763626 Epoch 18 MSE: 0.026143185794353485 Epoch 19 MSE: 0.02542714774608612 Epoch 20 MSE: 0.02448938600718975 Epoch 21 MSE: 0.02332731895148754 Epoch 22 MSE: 0.022001022472977638 Epoch 23 MSE: 0.020607035607099533 Epoch 24 MSE: 0.019248509779572487 Epoch 25 MSE: 0.018007680773735046 Epoch 26 MSE: 0.016925673931837082 Epoch 27 MSE: 0.015994062647223473 Epoch 28 MSE: 0.015161242336034775 Epoch 29 MSE: 0.014352691359817982 Epoch 30 MSE: 0.01349872536957264 Epoch 31 MSE: 0.012559309601783752 Epoch 32 MSE: 0.011536355130374432 Epoch 33 MSE: 0.010469580069184303 Epoch 34 MSE: 0.00941889826208353 Epoch 35 MSE: 0.008441027253866196 Epoch 36 MSE: 0.007568986155092716 Epoch 37 MSE: 0.006801762618124485 Epoch 38 MSE: 0.006107857916504145 Epoch 39 MSE: 0.005441526882350445 Epoch 40 MSE: 0.004765074234455824

```
Epoch 41 MSE:
                0.004067134577780962
Epoch
      42 MSE:
                0.003368205623701215
       43 MSE:
Epoch
                0.0027105938643217087
       44 MSE:
Epoch
                0.002137619536370039
Epoch
       45 MSE:
                0.0016724494053050876
Epoch
       46 MSE:
                0.0013078540796414018
Epoch
       47 MSE:
                0.001013146247714758
Epoch
       48 MSE:
                0.0007547180284745991
Epoch 49 MSE:
                0.0005173117388039827
Epoch
      50 MSE:
                0.00031182801467366517
       51 MSE:
                0.00016435561701655388
Epoch
Epoch
       52 MSE:
                9.411180508323014e-05
Epoch
       53 MSE:
                9.608816617401317e-05
Epoch
       54 MSE:
                0.00014141028805170208
Epoch
      55 MSE:
                0.0001954312901943922
Epoch 56 MSE:
                0.0002391002344666049
Epoch
      57 MSE:
                0.0002761791693046689
       58 MSE:
                0.00032142328564077616
Epoch
Epoch
       59 MSE:
                0.000381388672394678
Epoch
       60 MSE:
                0.00044507411075755954
Epoch
       61 MSE:
                0.0004917228361591697
Epoch
       62 MSE:
                0.000507302291225642
Epoch
       63 MSE:
                0.0004942384548485279
       64 MSE:
Epoch
                0.000466716883238405
       65 MSE:
                0.00043762067798525095
Epoch
Epoch
       66 MSE:
                0.0004095132171642035
       67 MSE:
Epoch
                0.00037655376945622265
Epoch
       68 MSE:
                0.0003335348446853459
       69 MSE:
Epoch
                0.0002826354466378689
Epoch 70 MSE:
                0.00023229036014527082
Epoch 71 MSE:
                0.0001905726094264537
Epoch
      72 MSE:
                0.0001598070521140471
Epoch
      73 MSE:
                0.00013669811596628278
      74 MSE:
Epoch
                0.00011675847053993493
Epoch
      75 MSE:
                9.846781176747754e-05
Epoch
      76 MSE:
                8.379681094083935e-05
Epoch
      77 MSE:
                7.547581481048837e-05
Epoch
      78 MSE:
                7.401246693916619e-05
      79 MSE:
Epoch
                7.705438474658877e-05
Epoch
       80 MSE:
                8.122131112031639e-05
       81 MSE:
                8.445606363238767e-05
Epoch
Epoch
       82 MSE:
                8.688116213306785e-05
Epoch
       83 MSE:
                8.975625678431243e-05
Epoch
       84 MSE:
                9.376922389492393e-05
Epoch
       85 MSE:
                9.821358980843797e-05
Epoch
       86 MSE:
                0.00010157821088796481
Epoch
       87 MSE:
                0.00010280330752721056
       88 MSE:
                0.00010201885015703738
Epoch
```

Epoch 89 MSE: 0.00010021962953032926
Epoch 90 MSE: 9.831575152929872e-05
Epoch 91 MSE: 9.646139369579032e-05
Epoch 92 MSE: 9.418145782547072e-05
Epoch 93 MSE: 9.104422497330233e-05
Epoch 94 MSE: 8.719265315448865e-05
Epoch 95 MSE: 8.327599061885849e-05
Epoch 96 MSE: 7.99274566816166e-05
Epoch 97 MSE: 7.731818914180622e-05
Epoch 98 MSE: 7.517463382100686e-05
Epoch 99 MSE: 7.317050767596811e-05

T-time: 22.606600522994995

Train Score: 0.26 RMSE

Validation Score: 7.32 RMSE

Time Step = 50 | Hidden States = 2 | Num Layers = 2

Epoch 0 MSE: 0.04541259631514549 Epoch 1 MSE: 0.03939131274819374 Epoch 2 MSE: 0.0368654690682888 Epoch 3 MSE: 0.037087757140398026 Epoch 4 MSE: 0.0383160263299942 Epoch 5 MSE: 0.038955044001340866 Epoch 6 MSE: 0.03863745927810669 Epoch 7 MSE: 0.03774527087807655 Epoch 8 MSE: 0.0367855578660965 Epoch 9 MSE: 0.036126427352428436 Epoch 10 MSE: 0.035912469029426575 Epoch 11 MSE: 0.03606269136071205 Epoch 12 MSE: 0.03634500876069069 Epoch 13 MSE: 0.03651213273406029 Epoch 14 MSE: 0.03642547130584717 Epoch 15 MSE: 0.03609423711895943 Epoch 16 MSE: 0.035631660372018814 Epoch 17 MSE: 0.03517875447869301 Epoch 18 MSE: 0.03483660891652107 Epoch 19 MSE: 0.03462718799710274 Epoch 20 MSE: 0.034492239356040955 Epoch 21 MSE: 0.03432955965399742 Epoch 22 MSE: 0.03404823690652847 Epoch 23 MSE: 0.03361248970031738 Epoch 24 MSE: 0.03305217623710632

```
Epoch
       25 MSE:
                0.03243974968791008
Epoch
       26 MSE:
                0.0318482480943203
Epoch
       27 MSE:
                0.03130878880620003
       28 MSE:
Epoch
                0.030788147822022438
Epoch
       29 MSE:
                0.030206920579075813
Epoch
       30 MSE:
                0.0294948797672987
Epoch
       31 MSE:
                0.02864006720483303
Epoch
       32 MSE:
                0.027691246941685677
Epoch
      33 MSE:
                0.0267178975045681
Epoch
       34 MSE:
                0.025758620351552963
       35 MSE:
Epoch
                0.02479189820587635
Epoch
       36 MSE:
                0.02375401183962822
Epoch
       37 MSE:
                0.022596416994929314
Epoch
       38 MSE:
                0.021331127732992172
Epoch
       39 MSE:
                0.02001775987446308
Epoch 40 MSE:
                0.018701227381825447
Epoch
       41 MSE:
                0.0173642635345459
       42 MSE:
Epoch
                0.015960650518536568
Epoch
       43 MSE:
                0.014493316411972046
Epoch
       44 MSE:
                0.013028870336711407
Epoch
       45 MSE:
                0.011624982580542564
Epoch
       46 MSE:
                0.01026271190494299
Epoch 47 MSE:
                0.008899114094674587
       48 MSE:
Epoch
                0.007572100032120943
       49 MSE:
                0.006375870667397976
Epoch
Epoch
       50 MSE:
                0.005339101422578096
       51 MSE:
Epoch
                0.004427971784025431
Epoch
       52 MSE:
                0.0036777625791728497
       53 MSE:
Epoch
                0.0031449978705495596
Epoch 54 MSE:
                0.002774723805487156
Epoch 55 MSE:
                0.0025150699075311422
Epoch
       56 MSE:
                0.0024014662485569715
      57 MSE:
Epoch
                0.0023852514568716288
       58 MSE:
Epoch
                0.0023761659394949675
Epoch
       59 MSE:
                0.0023642589803785086
Epoch
       60 MSE:
                0.002316734055057168
Epoch
       61 MSE:
                0.00218418100848794
Epoch
       62 MSE:
                0.001981725450605154
       63 MSE:
Epoch
                0.0017408677376806736
Epoch
       64 MSE:
                0.0014765679370611906
       65 MSE:
                0.001221781363710761
Epoch
       66 MSE:
Epoch
                0.0010204464197158813
Epoch
       67 MSE:
                0.0008902896661311388
Epoch
       68 MSE:
                0.0008267884841188788
Epoch
       69 MSE:
                0.0008236982394009829
Epoch
       70 MSE:
                0.0008649679366499186
Epoch
       71 MSE:
                0.0009192405850626528
       72 MSE:
Epoch
                0.0009599656914360821
```

```
Epoch 73 MSE:
               0.0009742029942572117
Epoch 74 MSE:
               0.0009535006829537451
Epoch 75 MSE:
               0.0008966558962129056
Epoch 76 MSE:
               0.0008173260139301419
Epoch 77 MSE:
               0.000734618166461587
Epoch 78 MSE:
               0.000661471567582339
Epoch 79 MSE:
               0.0006072524702176452
Epoch 80 MSE:
               0.0005786964320577681
Epoch 81 MSE:
               0.000572818098589778
Epoch 82 MSE:
               0.0005797740304842591
Epoch 83 MSE:
               0.0005915139336138964
Epoch 84 MSE:
               0.0006001044530421495
Epoch 85 MSE:
               0.0005975205567665398
Epoch 86 MSE:
               0.0005821791710332036
Epoch 87 MSE:
               0.0005570723442360759
Epoch 88 MSE:
               0.0005253797280602157
Epoch 89 MSE:
               0.0004926793626509607
Epoch 90 MSE:
               0.0004650322371162474
Epoch 91 MSE:
               0.00044461217476055026
Epoch 92 MSE:
               0.00043173431186005473
Epoch 93 MSE:
               0.00042577093699947
Epoch 94 MSE:
               0.00042334513273090124
Epoch 95 MSE:
               0.0004208330938126892
Epoch 96 MSE:
               0.00041631911881268024
Epoch 97 MSE:
               0.0004082377126906067
Epoch 98 MSE:
               0.000396306422771886
Epoch 99 MSE:
               0.0003821894933935255
```

T-time: 39.80460786819458

Train Score: 0.58 RMSE

Validation Score: 13.79 RMSE

_____ Time Step = 50 | Hidden States = 4 | Num Layers = 1

Epoch 0 MSE: 0.10186194628477097 Epoch 1 MSE: 0.07823987305164337 Epoch 2 MSE: 0.05898590758442879 Epoch 3 MSE: 0.04390754550695419 Epoch 4 MSE: 0.03276057168841362 Epoch 5 MSE: 0.025204278528690338 Epoch 6 MSE: 0.02078968472778797 Epoch 7 MSE: 0.018969278782606125 Epoch 8 MSE: 0.01910502277314663

```
9 MSE:
               0.020486164838075638
Epoch
Epoch
       10 MSE:
                0.022384488955140114
Epoch
       11 MSE:
                0.024150846526026726
       12 MSE:
Epoch
                0.02531309984624386
Epoch
       13 MSE:
                0.025624992325901985
Epoch
       14 MSE:
                0.025051454082131386
Epoch
       15 MSE:
                0.023713817819952965
Epoch
       16 MSE:
                0.02182534523308277
Epoch 17 MSE:
                0.019635073840618134
Epoch
       18 MSE:
                0.017385298386216164
       19 MSE:
                0.015282204374670982
Epoch
       20 MSE:
Epoch
                0.013477289117872715
Epoch
       21 MSE:
                0.012057820335030556
Epoch
       22 MSE:
                0.011045352555811405
Epoch
       23 MSE:
                0.01040184311568737
                0.010042531415820122
Epoch
       24 MSE:
Epoch
       25 MSE:
                0.009853936731815338
       26 MSE:
Epoch
                0.009714324027299881
Epoch
       27 MSE:
                0.00951352622359991
Epoch
       28 MSE:
                0.009169242344796658
       29 MSE:
Epoch
                0.008637571707367897
       30 MSE:
Epoch
                0.007916687987744808
Epoch
       31 MSE:
                0.007043706253170967
       32 MSE:
Epoch
                0.006085703149437904
       33 MSE:
                0.005126387346535921
Epoch
Epoch
       34 MSE:
                0.004250232595950365
       35 MSE:
Epoch
                0.003526090644299984
Epoch
       36 MSE:
                0.002992786932736635
       37 MSE:
Epoch
                0.002649854402989149
Epoch
       38 MSE:
                0.002456904388964176
       39 MSE:
                0.0023441677913069725
Epoch
Epoch
       40 MSE:
                0.0022333951201289892
Epoch
       41 MSE:
                0.002063220599666238
       42 MSE:
                0.0018093287944793701
Epoch
Epoch
       43 MSE:
                0.0014906992437317967
Epoch
       44 MSE:
                0.0011593223316594958
Epoch
       45 MSE:
                0.0008781312499195337
Epoch
       46 MSE:
                0.0006965015782043338
       47 MSE:
Epoch
                0.0006327335140667856
Epoch
       48 MSE:
                0.0006694822222925723
       49 MSE:
                0.0007627354934811592
Epoch
       50 MSE:
Epoch
                0.0008597656851634383
Epoch
       51 MSE:
                0.0009183882502838969
Epoch
       52 MSE:
                0.0009200652129948139
Epoch
       53 MSE:
                0.0008725962834432721
Epoch
       54 MSE:
                0.0008026273571886122
Epoch
       55 MSE:
                0.0007419298053719103
       56 MSE:
                0.0007133356994017959
Epoch
```

Epoch	57	MSE:	0.0007219052640721202		
Epoch	58	MSE:	0.0007546314154751599		
Epoch	59	MSE:	0.0007882255013100803		
Epoch	60	MSE:	0.0008007779251784086		
Epoch	61	MSE:	0.0007813904085196555		
Epoch	62	MSE:	0.0007334051188081503		
Epoch	63	MSE:	0.0006707143620587885		
Epoch	64	MSE:	0.0006101071485318244		
Epoch	65	MSE:	0.0005639077862724662		
Epoch	66	MSE:	0.0005360694485716522		
Epoch	67	MSE:	0.0005225985660217702		
Epoch	68	MSE:	0.0005151331424713135		
Epoch	69	MSE:	0.0005054703215137124		
Epoch	70	MSE:	0.0004889889969490469		
Epoch	71	MSE:	0.000465847784653306		
Epoch	72	MSE:	0.0004399677272886038		
Epoch	73	MSE:	0.00041666821925900877		
Epoch	74	MSE:	0.0004001675988547504		
Epoch	75	MSE:	0.0003919640730600804		
Epoch	76	MSE:	0.00039059584378264844		
Epoch	77	MSE:	0.00039263712824322283		
Epoch	78	MSE:	0.0003943225019611418		
Epoch	79	MSE:	0.00039302927325479686		
Epoch	80	MSE:	0.0003880359581671655		
Epoch	81	MSE:	0.0003803748986683786		
Epoch	82	MSE:	0.0003720048407558352		
Epoch	83	MSE:	0.00036477105459198356		
Epoch	84	MSE:	0.00035962165566161275		
Epoch	85	MSE:	0.0003563552745617926		
Epoch	86	MSE:	0.0003539053723216057		
Epoch	87	MSE:	0.00035094597842544317		
Epoch	88	MSE:	0.0003465068293735385		
Epoch	89	MSE:	0.0003403425798751414		
Epoch	90	MSE:	0.00033293815795332193		
Epoch	91	MSE:	0.0003252062597312033		
Epoch	92	MSE:	0.0003180535277351737		
Epoch	93	MSE:	0.0003120159381069243		
Epoch	94	MSE:	0.0003071112441830337		
Epoch	95	MSE:	0.00030293618328869343		
Epoch	96	MSE:	0.00029893004102632403		
Epoch	97	MSE:	0.00029466053820215166		
Epoch	98	MSE:	0.00029000089853070676		
Epoch	99	MSE:	0.00028513470897451043		
T-time			550033569336		
1 Jimo. 20.02000000000000					

 ${\tt Train~Score:~0.50~RMSE}$

Validation Score: 11.79 RMSE

Time Step = 50 | Hidden States = 4 | Num Layers = 2

Epoch 0 MSE: 0.14384600520133972 Epoch 1 MSE: 0.10968273878097534 Epoch 2 MSE: 0.08233783394098282 Epoch 3 MSE: 0.06209370866417885 Epoch 4 MSE: 0.04891606792807579 Epoch 5 MSE: 0.042443543672561646 Epoch 6 MSE: 0.0416816845536232 Epoch 7 MSE: 0.04459628462791443 Epoch 8 MSE: 0.04842166602611542 Epoch 9 MSE: 0.05089804157614708Epoch 10 MSE: 0.051098182797431946 Epoch 11 MSE: 0.049226485192775726 Epoch 12 MSE: 0.04604518413543701 Epoch 13 MSE: 0.04241759702563286 Epoch 14 MSE: 0.039051592350006104 Epoch 15 MSE: 0.03639558330178261 Epoch 16 MSE: 0.03463265299797058 Epoch 17 MSE: 0.03372956067323685 Epoch 18 MSE: 0.03350715711712837 Epoch 19 MSE: 0.033710937947034836 Epoch 20 MSE: 0.034071095287799835 Epoch 21 MSE: 0.03434785455465317 Epoch 22 MSE: 0.03436176851391792 Epoch 23 MSE: 0.03401000425219536 Epoch 24 MSE: 0.03327026590704918 Epoch 25 MSE: 0.032194070518016815 Epoch 26 MSE: 0.030890915542840958 Epoch 27 MSE: 0.029505135491490364 Epoch 28 MSE: 0.028186889365315437 Epoch 29 MSE: 0.027059907093644142 Epoch 30 MSE: 0.026190517470240593 Epoch 31 MSE: 0.02556602843105793 Epoch 32 MSE: 0.02509238012135029 Epoch 33 MSE: 0.024618348106741905 Epoch 34 MSE: 0.023983754217624664 Epoch 35 MSE: 0.023075364530086517 Epoch 36 MSE: 0.0218676645308733 Epoch 37 MSE: 0.02043168433010578 Epoch 38 MSE: 0.018908845260739326 Epoch 39 MSE: 0.017458593472838402 Epoch 40 MSE: 0.01619502529501915

```
Epoch
       41 MSE:
                0.015131797641515732
Epoch
       42 MSE:
                0.014161237515509129
Epoch
       43 MSE:
                0.013095875270664692
       44 MSE:
Epoch
                0.011777439154684544
Epoch
       45 MSE:
                0.010198339819908142
       46 MSE:
Epoch
                0.008536726236343384
Epoch
       47 MSE:
                0.007049642037600279
Epoch
       48 MSE:
                0.0058788941241800785
       49 MSE:
Epoch
                0.004926740191876888
Epoch
       50 MSE:
                0.0039602587930858135
       51 MSE:
                0.002893006894737482
Epoch
Epoch
       52 MSE:
                0.0019445501966401935
Epoch
       53 MSE:
                0.0014397894265130162
Epoch
       54 MSE:
                0.0013574365293607116
Epoch
       55 MSE:
                0.0012640401255339384
                0.001025806530378759
       56 MSE:
Epoch
Epoch
       57 MSE:
                0.001051556901074946
       58 MSE:
Epoch
                0.0014692115364596248
Epoch
       59 MSE:
                0.0018008091719821095
Epoch
       60 MSE:
                0.0018521539168432355
Epoch
       61 MSE:
                0.001988617004826665
Epoch
       62 MSE:
                0.002245491137728095
Epoch
       63 MSE:
                0.0022356314584612846
       64 MSE:
Epoch
                0.0020225855987519026
       65 MSE:
                0.001906359801068902
Epoch
Epoch
       66 MSE:
                0.0018029940547421575
       67 MSE:
Epoch
                0.0015469786012545228
Epoch
       68 MSE:
                0.0012698880163952708
       69 MSE:
Epoch
                0.0011189949000254273
Epoch
       70 MSE:
                0.0010168581502512097
       71 MSE:
Epoch
                0.0008733635186217725
Epoch
       72 MSE:
                0.0007496094331145287
Epoch
       73 MSE:
                0.0007150981691665947
       74 MSE:
                0.0007306472398340702
Epoch
Epoch
       75 MSE:
                0.0007316793198697269
Epoch
       76 MSE:
                0.0007229496259242296
Epoch
       77 MSE:
                0.0007422671187669039
Epoch
       78 MSE:
                0.0007859919569455087
       79 MSE:
Epoch
                0.0008153397357091308
       80 MSE:
Epoch
                0.000815001199953258
       81 MSE:
Epoch
                0.0008066088776104152
       82 MSE:
Epoch
                0.0008070854819379747
Epoch
       83 MSE:
                0.0008038626983761787
       84 MSE:
Epoch
                0.0007795646670274436
Epoch
       85 MSE:
                0.0007405952201224864
Epoch
       86 MSE:
                0.0007062567165121436
Epoch
       87 MSE:
                0.0006803469732403755
       88 MSE:
                0.0006507635116577148
Epoch
```

Epoch 89 MSE: 0.0006140907644294202 Epoch 90 MSE: 0.0005826511769555509 Epoch 91 MSE: 0.0005643551121465862 Epoch 92 MSE: 0.0005516782985068858 Epoch 93 MSE: 0.0005370522849261761 Epoch 94 MSE: 0.0005254466668702662 Epoch 95 MSE: 0.0005229602684266865 Epoch 96 MSE: 0.000524309347383678 Epoch 97 MSE: 0.0005217652069404721 Epoch 98 MSE: 0.0005171464290469885 Epoch 99 MSE: 0.000515017076395452

T-time: 41.557682514190674

Train Score: 0.68 RMSE

Validation Score: 12.78 RMSE

Time Step = 50 | Hidden States = 8 | Num Layers = 1

Epoch 0 MSE: 0.213391974568367 Epoch 1 MSE: 0.16463464498519897 Epoch 2 MSE: 0.12429853528738022 Epoch 3 MSE: 0.09204477071762085 Epoch 4 MSE: 0.06758939474821091 Epoch 5 MSE: 0.05052864924073219 Epoch 6 MSE: 0.04030289500951767 Epoch 7 MSE: 0.036104343831539154 Epoch 8 MSE: 0.036680180579423904 Epoch 9 MSE: 0.04011410474777222 Epoch 10 MSE: 0.04406619071960449 Epoch 11 MSE: 0.04668243229389191 Epoch 12 MSE: 0.04717293381690979 Epoch 13 MSE: 0.04563504830002785 Epoch 14 MSE: 0.04263104870915413 Epoch 15 MSE: 0.03885074332356453 Epoch 16 MSE: 0.03491348400712013 Epoch 17 MSE: 0.031278591603040695 Epoch 18 MSE: 0.02822497859597206 Epoch 19 MSE: 0.02586975507438183 Epoch 20 MSE: 0.024204744026064873 Epoch 21 MSE: 0.02313733473420143 Epoch 22 MSE: 0.022527823224663734 Epoch 23 MSE: 0.022219577804207802 Epoch 24 MSE: 0.022061171010136604

```
Epoch
       25 MSE:
                0.021921100094914436
Epoch
       26 MSE:
                0.021696388721466064
                0.02131631411612034
Epoch
       27 MSE:
       28 MSE:
Epoch
                0.020742515102028847
Epoch
       29 MSE:
                0.01996641419827938
Epoch
       30 MSE:
                0.01900477521121502
Epoch
       31 MSE:
                0.017894035205245018
Epoch
       32 MSE:
                0.016683897003531456
Epoch
       33 MSE:
                0.015430571511387825
Epoch
       34 MSE:
                0.01419011503458023
       35 MSE:
                0.013012104667723179
Epoch
       36 MSE:
Epoch
                0.011934122070670128
Epoch
       37 MSE:
                0.010977529920637608
Epoch
       38 MSE:
                0.010145128704607487
Epoch
       39 MSE:
                0.00942131970077753
Epoch 40 MSE:
                0.008775202557444572
Epoch
       41 MSE:
                0.00816663820296526
       42 MSE:
Epoch
                0.007554557174444199
Epoch
       43 MSE:
                0.006905983202159405
Epoch
       44 MSE:
                0.006203679367899895
Epoch
       45 MSE:
                0.0054503437131643295
       46 MSE:
Epoch
                0.004668035078793764
Epoch 47 MSE:
                0.003892790526151657
       48 MSE:
Epoch
                0.003165828762575984
       49 MSE:
                0.0025236038491129875
Epoch
       50 MSE:
Epoch
                0.0019893913995474577
       51 MSE:
Epoch
                0.0015685590915381908
Epoch
       52 MSE:
                0.001248756772838533
       53 MSE:
Epoch
                0.0010049211559817195
Epoch
       54 MSE:
                0.0008076591184362769
Epoch 55 MSE:
                0.0006325385766103864
Epoch
       56 MSE:
                0.0004673876101151109
       57 MSE:
Epoch
                0.00031513921567238867
       58 MSE:
                0.00019099382916465402
Epoch
Epoch
       59 MSE:
                0.00011452077160356566
Epoch
       60 MSE:
                9.932957618730143e-05
Epoch
       61 MSE:
                0.00014446552086155862
Epoch
       62 MSE:
                0.0002318117331014946
       63 MSE:
Epoch
                0.0003316478687338531
Epoch
       64 MSE:
                0.00041435190360061824
       65 MSE:
                0.0004622379201464355
Epoch
       66 MSE:
Epoch
                0.0004749165673274547
Epoch
       67 MSE:
                0.00046549565740861
       68 MSE:
Epoch
                0.0004506997065618634
Epoch
       69 MSE:
                0.00044124500709585845
Epoch
       70 MSE:
                0.0004376108990982175
Epoch
       71 MSE:
                0.00043229246512055397
       72 MSE:
                0.00041590313776396215
Epoch
```

```
Epoch 73 MSE:
               0.00038310952368192375
Epoch 74 MSE:
               0.00033544166944921017
Epoch 75 MSE:
               0.00028024439234286547
Epoch 76 MSE:
               0.0002270282420795411
Epoch 77 MSE:
               0.00018340452515985817
Epoch 78 MSE:
               0.00015253140009008348
Epoch 79 MSE:
               0.0001329386286670342
Epoch 80 MSE:
               0.00012035632971674204
Epoch 81 MSE:
               0.00011032064503524452
Epoch 82 MSE:
               0.00010020674380939454
Epoch 83 MSE:
               8.988693298306316e-05
Epoch 84 MSE:
               8.103111758828163e-05
Epoch 85 MSE:
               7.569688750663772e-05
Epoch 86 MSE:
               7.503473170800135e-05
Epoch 87 MSE:
               7.867824024287984e-05
Epoch 88 MSE:
               8.495114161632955e-05
Epoch 89 MSE:
               9.162792412098497e-05
Epoch 90 MSE:
               9.681081428425387e-05
Epoch 91 MSE:
               9.953002154361457e-05
Epoch 92 MSE:
               9.987034718506038e-05
Epoch 93 MSE:
               9.866031177807599e-05
Epoch 94 MSE:
               9.693140600575134e-05
Epoch 95 MSE:
               9.541546023683622e-05
Epoch 96 MSE:
               9.42847691476345e-05
Epoch 97 MSE:
               9.320754907093942e-05
Epoch 98 MSE:
               9.163795039057732e-05
Epoch 99 MSE:
               8.916806109482422e-05
```

T-time: 25.852683544158936

Train Score: 0.28 RMSE

Validation Score: 6.64 RMSE

_____ Time Step = 50 | Hidden States = 8 | Num Layers = 2

Epoch 0 MSE: 0.037010837346315384 Epoch 1 MSE: 0.03321288153529167 Epoch 2 MSE: 0.0337478406727314 Epoch 3 MSE: 0.029266145080327988 Epoch 4 MSE: 0.026534538716077805 Epoch 5 MSE: 0.026288606226444244 Epoch 6 MSE: 0.02467179298400879 Epoch 7 MSE: 0.02082986757159233 Epoch 8 MSE: 0.017290523275732994

```
Epoch
      9 MSE:
               0.015460016205906868
Epoch
       10 MSE:
                0.013202928006649017
Epoch
       11 MSE:
                0.00913295615464449
       12 MSE:
Epoch
                0.005645491182804108
Epoch
       13 MSE:
                0.004255844745784998
Epoch
       14 MSE:
                0.002123628044500947
Epoch
       15 MSE:
                0.0001688141783233732
Epoch
       16 MSE:
                0.0018716733902692795
Epoch 17 MSE:
                0.002205652417615056
Epoch
       18 MSE:
                0.0033757060300558805
       19 MSE:
                0.004814759362488985
Epoch
       20 MSE:
Epoch
                0.0035370897967368364
Epoch
       21 MSE:
                0.003258420852944255
Epoch
       22 MSE:
                0.0022498813923448324
Epoch
       23 MSE:
                0.0008119334816001356
Epoch
      24 MSE:
                0.0005653786356560886
Epoch
       25 MSE:
                0.0004940726212225854
       26 MSE:
                0.0002682384510990232
Epoch
Epoch
       27 MSE:
                0.0005089208134450018
Epoch
       28 MSE:
                0.000986872473731637
       29 MSE:
Epoch
                0.0011527661699801683
       30 MSE:
Epoch
                0.001129013136960566
Epoch
       31 MSE:
                0.0012218287447467446
       32 MSE:
Epoch
                0.0012900212313979864
       33 MSE:
                0.0010975541081279516
Epoch
Epoch
       34 MSE:
                0.000796231091953814
       35 MSE:
Epoch
                0.0006297420477494597
Epoch
       36 MSE:
                0.0005045545403845608
       37 MSE:
Epoch
                0.00027684145607054234
Epoch
       38 MSE:
                0.00012432601943146437
       39 MSE:
                0.00017199129797518253
Epoch
Epoch
       40 MSE:
                0.0002224078489234671
Epoch
       41 MSE:
                0.00022841317695565522
       42 MSE:
                0.00034018460428342223
Epoch
Epoch
       43 MSE:
                0.00043663798714987934
Epoch
       44 MSE:
                0.0003961579641327262
Epoch
       45 MSE:
                0.00036537539563141763
Epoch
       46 MSE:
                0.00034062322811223567
       47 MSE:
Epoch
                0.00023396995675284415
Epoch
       48 MSE:
                0.00015333468036260456
       49 MSE:
                0.00014053948689252138
Epoch
       50 MSE:
Epoch
                0.00011315897427266464
Epoch
       51 MSE:
                9.78902680799365e-05
Epoch
       52 MSE:
                0.00013601301179733127
Epoch
       53 MSE:
                0.0001664623705437407
Epoch
       54 MSE:
                0.00016831998073030263
Epoch
       55 MSE:
                0.00018194038420915604
       56 MSE:
Epoch
                0.0001905393146444112
```

```
Epoch 57 MSE:
                0.0001655233500059694
Epoch 58 MSE:
                0.00013957562623545527
Epoch 59 MSE:
                0.00012728308502119035
Epoch
      60 MSE:
                0.00010425124492030591
Epoch 61 MSE:
                8.473471825709566e-05
Epoch
      62 MSE:
                8.8421547843609e-05
Epoch
      63 MSE:
                9.201021020999178e-05
Epoch 64 MSE:
                9.264348773285747e-05
Epoch 65 MSE:
                0.00010515114263398573
Epoch 66 MSE:
                0.00011120013368781656
Epoch 67 MSE:
                0.00010561865929048508
Epoch 68 MSE:
                0.00010390443640062585
Epoch 69 MSE:
                9.745809074956924e-05
Epoch 70 MSE:
                8.486147999064997e-05
Epoch 71 MSE:
                7.996158819878474e-05
Epoch 72 MSE:
                7.711989019298926e-05
Epoch 73 MSE:
                7.314790855161846e-05
Epoch 74 MSE:
                7.582421676488593e-05
Epoch 75 MSE:
                7.919863128336146e-05
Epoch 76 MSE:
                7.895671296864748e-05
Epoch
     77 MSE:
                8.046561561059207e-05
Epoch 78 MSE:
                8.027001604204997e-05
Epoch 79 MSE:
                7.612636545673013e-05
Epoch 80 MSE:
                7.347397331614047e-05
Epoch 81 MSE:
                7.08797961124219e-05
Epoch 82 MSE:
                6.716766074532643e-05
Epoch 83 MSE:
                6.632897566305473e-05
Epoch 84 MSE:
                6.636278703808784e-05
Epoch 85 MSE:
                6.577189196832478e-05
Epoch 86 MSE:
                6.674491305602714e-05
Epoch 87 MSE:
                6.694368494208902e-05
Epoch 88 MSE:
                6.576471059815958e-05
Epoch 89 MSE:
                6.510317325592041e-05
Epoch 90 MSE:
                6.348035094561055e-05
Epoch
      91 MSE:
                6.15097233094275e-05
Epoch
      92 MSE:
                6.059315273887478e-05
Epoch 93 MSE:
                5.947193130850792e-05
Epoch 94 MSE:
                5.8764264394994825e-05
Epoch 95 MSE:
                5.878494994249195e-05
Epoch 96 MSE:
                5.829200745210983e-05
Epoch 97 MSE:
                5.7840887166094035e-05
Epoch 98 MSE:
                5.733964280807413e-05
Epoch 99 MSE:
                5.616895577986725e-05
T-time: 47.4135377407074
```

Train Score: 0.22 RMSE

Time Step = 50 | Hidden States = 16 | Num Layers = 1

Epoch 0 MSE: 0.06670422106981277 Epoch 1 MSE: 0.04410930722951889 Epoch 2 MSE: 0.03354153409600258 Epoch 3 MSE: 0.0332847535610199 Epoch 4 MSE: 0.03537086024880409 Epoch 5 MSE: 0.03372766077518463 Epoch 6 MSE: 0.029546087607741356 Epoch 7 MSE: 0.025463104248046875 Epoch 8 MSE: 0.022822828963398933 Epoch 9 MSE: 0.021657755598425865Epoch 10 MSE: 0.0212395079433918 Epoch 11 MSE: 0.02064855769276619 Epoch 12 MSE: 0.019297458231449127 Epoch 13 MSE: 0.017162589356303215 Epoch 14 MSE: 0.014648769982159138 Epoch 15 MSE: 0.012312904931604862 Epoch 16 MSE: 0.010577094741165638 Epoch 17 MSE: 0.00946669653058052 Epoch 18 MSE: 0.008523735217750072 Epoch 19 MSE: 0.007150912191718817 Epoch 20 MSE: 0.005168793257325888 Epoch 21 MSE: 0.003017059527337551 Epoch 22 MSE: 0.0014792331494390965 Epoch 23 MSE: 0.0010633869096636772 Epoch 24 MSE: 0.0013044110964983702 Epoch 25 MSE: 0.0011964845471084118 Epoch 26 MSE: 0.0008614440448582172 Epoch 27 MSE: 0.001364306197501719 Epoch 28 MSE: 0.0025119937490671873 Epoch 29 MSE: 0.0027323137037456036 Epoch 30 MSE: 0.0019408782245591283 Epoch 31 MSE: 0.001262873993255198 Epoch 32 MSE: 0.0010671233758330345 Epoch 33 MSE: 0.0009074803092516959 Epoch 34 MSE: 0.00054645084310323 Epoch 35 MSE: 0.00018881050345953554 Epoch 36 MSE: 6.946093344595283e-05 Epoch 37 MSE: 0.00018855441885534674 Epoch 38 MSE: 0.00037331186467781663 Epoch 39 MSE: 0.0004738337593153119 Epoch 40 MSE: 0.00047157699009403586

```
Epoch 41 MSE:
                0.000440188217908144
Epoch
       42 MSE:
                0.0004459950141608715
       43 MSE:
Epoch
                0.0004889605916105211
       44 MSE:
Epoch
                0.0005173585377633572
Epoch
       45 MSE:
                0.0004843252245336771
Epoch
       46 MSE:
                0.00039095443207770586
Epoch
       47 MSE:
                0.00028244638815522194
Epoch
       48 MSE:
                0.00020671087258961052
Epoch 49 MSE:
                0.00017480204405728728
Epoch
      50 MSE:
                0.00015899950813036412
       51 MSE:
Epoch
                0.0001286450569750741
Epoch
       52 MSE:
                8.512803469784558e-05
Epoch
       53 MSE:
                5.8096044085687026e-05
Epoch
       54 MSE:
                6.893897807458416e-05
Epoch
      55 MSE:
                0.00010484312224434689
Epoch 56 MSE:
                0.00013304762251209468
Epoch
      57 MSE:
                0.0001364127529086545
       58 MSE:
Epoch
                0.00012712806346826255
Epoch
       59 MSE:
                0.0001251383073395118
Epoch
       60 MSE:
                0.00013172515900805593
Epoch
       61 MSE:
                0.00013093158486299217
Epoch
       62 MSE:
                0.00011294266732875258
Epoch
       63 MSE:
                8.690358663443476e-05
       64 MSE:
Epoch
                6.89111475367099e-05
       65 MSE:
                6.391673377947882e-05
Epoch
Epoch
       66 MSE:
                6.379780825227499e-05
       67 MSE:
Epoch
                6.015361941535957e-05
Epoch
       68 MSE:
                5.396160850068554e-05
       69 MSE:
Epoch
                5.2006460464326665e-05
Epoch
      70 MSE:
                5.712340498575941e-05
Epoch 71 MSE:
                6.468783976742998e-05
Epoch
      72 MSE:
                6.82859099470079e-05
Epoch
      73 MSE:
                6.657113408436999e-05
      74 MSE:
Epoch
                6.335927173495293e-05
Epoch
      75 MSE:
                6.208896957105026e-05
Epoch
       76 MSE:
                6.197501352289692e-05
Epoch
      77 MSE:
                5.9951518778689206e-05
Epoch
      78 MSE:
                5.511193012353033e-05
Epoch
      79 MSE:
                4.994252958567813e-05
Epoch
       80 MSE:
                4.726008410216309e-05
       81 MSE:
Epoch
                4.7076446207938716e-05
Epoch
       82 MSE:
                4.720207289210521e-05
Epoch
       83 MSE:
                4.633822391042486e-05
Epoch
       84 MSE:
                4.5443070121109486e-05
Epoch
       85 MSE:
                4.590761091094464e-05
Epoch
       86 MSE:
                4.7400306357303634e-05
Epoch
       87 MSE:
                4.828372402698733e-05
       88 MSE:
Epoch
                4.77267058158759e-05
```

Epoch 89 MSE: 4.6521960030077025e-05
Epoch 90 MSE: 4.574791819322854e-05
Epoch 91 MSE: 4.5370154111878946e-05
Epoch 92 MSE: 4.4614022044697776e-05
Epoch 93 MSE: 4.328187060309574e-05
Epoch 94 MSE: 4.2062874854309484e-05
Epoch 95 MSE: 4.156781142228283e-05
Epoch 96 MSE: 4.158689625910483e-05
Epoch 97 MSE: 4.1519233491271734e-05
Epoch 98 MSE: 4.11996225011535e-05
Epoch 99 MSE: 4.096625343663618e-05

T-time: 40.462799072265625

Train Score: 0.19 RMSE

Validation Score: 4.36 RMSE

Time Step = 50 | Hidden States = 16 | Num Layers = 2

Epoch 0 MSE: 0.12359856814146042 Epoch 1 MSE: 0.06420028954744339 Epoch 2 MSE: 0.03495670482516289 Epoch 3 MSE: 0.03407468646764755 Epoch 4 MSE: 0.044979773461818695 Epoch 5 MSE: 0.04342009499669075 Epoch 6 MSE: 0.03547918424010277 Epoch 7 MSE: 0.02935691736638546 Epoch 8 MSE: 0.027183981612324715 Epoch 9 MSE: 0.02763543836772442 Epoch 10 MSE: 0.028591830283403397 Epoch 11 MSE: 0.028492946177721024 Epoch 12 MSE: 0.02680928446352482 Epoch 13 MSE: 0.02381308563053608 Epoch 14 MSE: 0.0201732125133276 Epoch 15 MSE: 0.016663968563079834 Epoch 16 MSE: 0.013939390890300274 Epoch 17 MSE: 0.012191065587103367 Epoch 18 MSE: 0.010706016793847084 Epoch 19 MSE: 0.008161318488419056 Epoch 20 MSE: 0.0042051286436617374 Epoch 21 MSE: 0.0007060931529849768 Epoch 22 MSE: 0.0009808068862184882 Epoch 23 MSE: 0.00479612872004509 Epoch 24 MSE: 0.005596034228801727

```
Epoch
       25 MSE:
                0.0036658067256212234
Epoch
       26 MSE:
                0.0026293478440493345
Epoch
       27 MSE:
                0.002381344325840473
       28 MSE:
Epoch
                0.001551461056806147
Epoch
       29 MSE:
                0.0006006614421494305
Epoch
       30 MSE:
                0.00037079761386848986
Epoch
       31 MSE:
                0.0008642704924568534
Epoch
       32 MSE:
                0.0015552558470517397
       33 MSE:
Epoch
                0.001967228716239333
Epoch
       34 MSE:
                0.0019263532012701035
       35 MSE:
                0.001544912694953382
Epoch
Epoch
       36 MSE:
                0.001083218608982861
Epoch
       37 MSE:
                0.0007742731831967831
Epoch
       38 MSE:
                0.0006770070758648217
Epoch
       39 MSE:
                0.0006536292494274676
      40 MSE:
                0.0005291432607918978
Epoch
Epoch
       41 MSE:
                0.00030283816158771515
                0.00015986734069883823
       42 MSE:
Epoch
Epoch
       43 MSE:
                0.0002479150425642729
Epoch
       44 MSE:
                0.0004882090725004673
Epoch
       45 MSE:
                0.0006513199186883867
Epoch
       46 MSE:
                0.0005990623612888157
Epoch 47 MSE:
                0.00040465156780555844
       48 MSE:
Epoch
                0.00023996188247110695
       49 MSE:
                0.0001912784209707752
Epoch
Epoch
       50 MSE:
                0.00020731246331706643
       51 MSE:
Epoch
                0.00020164081070106477
Epoch
       52 MSE:
                0.0001591081963852048
       53 MSE:
Epoch
                0.00012966804206371307
Epoch
       54 MSE:
                0.00015203333168756217
      55 MSE:
Epoch
                0.00020931148901581764
Epoch
       56 MSE:
                0.0002504432341083884
       57 MSE:
Epoch
                0.00023942238476593047
       58 MSE:
                0.0001837718882597983
Epoch
Epoch
       59 MSE:
                0.0001231333299074322
Epoch
       60 MSE:
                9.259096259484068e-05
Epoch
       61 MSE:
                9.419534035259858e-05
Epoch
       62 MSE:
                0.0001027555699693039
       63 MSE:
Epoch
                9.820392733672634e-05
Epoch
       64 MSE:
                8.681514736963436e-05
       65 MSE:
                8.740092016523704e-05
Epoch
       66 MSE:
Epoch
                0.00010335369006497785
Epoch
       67 MSE:
                0.00011706155783031136
Epoch
       68 MSE:
                0.00011116109817521647
Epoch
       69 MSE:
                8.819955110084265e-05
Epoch
       70 MSE:
                6.633884186157957e-05
Epoch
       71 MSE:
                5.917047383263707e-05
       72 MSE:
                6.386073800968006e-05
Epoch
```

```
Epoch 73 MSE:
               6.865447357995436e-05
Epoch 74 MSE:
               6.754697096766904e-05
Epoch 75 MSE:
               6.448938802350312e-05
Epoch 76 MSE:
               6.516426947200671e-05
Epoch 77 MSE:
               6.880205910420045e-05
Epoch 78 MSE:
               6.950528040761128e-05
Epoch 79 MSE:
               6.382565334206447e-05
Epoch 80 MSE:
               5.499624239746481e-05
Epoch 81 MSE:
               4.932523734169081e-05
Epoch 82 MSE:
               4.944323518429883e-05
Epoch 83 MSE:
               5.224691267358139e-05
Epoch 84 MSE:
               5.336087997420691e-05
Epoch 85 MSE:
               5.206735659157857e-05
Epoch 86 MSE:
               5.080754272057675e-05
Epoch 87 MSE:
               5.096761742606759e-05
Epoch 88 MSE:
               5.104799856781028e-05
Epoch 89 MSE:
               4.915408499073237e-05
Epoch 90 MSE:
               4.5832715841243044e-05
Epoch 91 MSE:
               4.347047070041299e-05
Epoch 92 MSE:
               4.3390704377088696e-05
Epoch 93 MSE:
               4.4510437874123454e-05
Epoch 94 MSE:
               4.495759276323952e-05
Epoch 95 MSE:
               4.4232350774109364e-05
Epoch 96 MSE:
               4.326322232373059e-05
Epoch 97 MSE:
               4.278525375411846e-05
Epoch 98 MSE:
               4.243211151333526e-05
Epoch 99 MSE:
               4.1532806790200993e-05
```

T-time: 72.54988217353821

Train Score: 0.19 RMSE

-----Validation Score: 7.11 RMSE

Time Step = 50 | Hidden States = 32 | Num Layers = 1

```
Epoch 0 MSE: 0.04294290021061897
Epoch 1 MSE: 0.03275536000728607
Epoch 2 MSE: 0.03130323067307472
Epoch 3 MSE: 0.025067200884222984
Epoch 4 MSE: 0.019294526427984238
Epoch 5 MSE: 0.016042781993746758
Epoch 6 MSE: 0.012434117496013641
Epoch 7 MSE: 0.006264178082346916
Epoch 8 MSE: 0.0013224146096035838
```

```
9 MSE:
               0.005399370566010475
Epoch
Epoch
       10 MSE:
                0.003157021477818489
Epoch
       11 MSE:
                0.0034628286957740784
       12 MSE:
Epoch
                0.0036870394833385944
Epoch
       13 MSE:
                0.0012062157038599253
Epoch
       14 MSE:
                0.00012317951768636703
Epoch
       15 MSE:
                0.00118175835814327
Epoch
       16 MSE:
                0.0022701947018504143
Epoch 17 MSE:
                0.0021045487374067307
Epoch
       18 MSE:
                0.0013053673319518566
       19 MSE:
                0.0008686492219567299
Epoch
       20 MSE:
Epoch
                0.0010138127254322171
Epoch
       21 MSE:
                0.0012196379248052835
Epoch
       22 MSE:
                0.0009697508066892624
Epoch
       23 MSE:
                0.0003716018982231617
Epoch 24 MSE:
                2.2224812710192055e-05
Epoch
       25 MSE:
                0.00027177445008419454
       26 MSE:
Epoch
                0.000707500206772238
Epoch
       27 MSE:
                0.0007111606537364423
Epoch
       28 MSE:
                0.00037999547203071415
Epoch
       29 MSE:
                0.00023022553068585694
Epoch
       30 MSE:
                0.0003515265416353941
Epoch
       31 MSE:
                0.0004168588202446699
       32 MSE:
Epoch
                0.0002623563923407346
       33 MSE:
                6.693109025945887e-05
Epoch
Epoch
       34 MSE:
                4.565603376249783e-05
       35 MSE:
Epoch
                0.0001812894770409912
Epoch
       36 MSE:
                0.0002878155210055411
       37 MSE:
Epoch
                0.00025433505652472377
Epoch
      38 MSE:
                0.00014933508646208793
       39 MSE:
Epoch
                9.858058183453977e-05
Epoch
       40 MSE:
                0.00012861429422628134
Epoch
       41 MSE:
                0.00015837156388442963
       42 MSE:
Epoch
                0.00011964613804593682
Epoch
       43 MSE:
                4.552215978037566e-05
Epoch
       44 MSE:
                2.1053714590379968e-05
Epoch
       45 MSE:
                6.680025398964062e-05
Epoch
       46 MSE:
                0.00011329409608151764
       47 MSE:
Epoch
                0.00010137206118088216
Epoch
       48 MSE:
                5.8736532082548365e-05
Epoch 49 MSE:
                4.456158058019355e-05
       50 MSE:
Epoch
                6.182891229400411e-05
Epoch
       51 MSE:
                6.724114791722968e-05
Epoch
       52 MSE:
                4.35050023952499e-05
Epoch
       53 MSE:
                2.0180417777737603e-05
Epoch
       54 MSE:
                2.531989048293326e-05
Epoch
       55 MSE:
                4.6904158807592466e-05
       56 MSE:
                5.440649692900479e-05
Epoch
```

```
Epoch 57 MSE:
               4.1407991375308484e-05
Epoch 58 MSE:
                2.8539008781081066e-05
Epoch 59 MSE:
                3.0146729841362685e-05
Epoch
      60 MSE:
                3.638034104369581e-05
Epoch 61 MSE:
                3.226367698516697e-05
Epoch
      62 MSE:
                2.103411861753557e-05
Epoch
      63 MSE:
                1.766947934811469e-05
Epoch 64 MSE:
                2.5313909645774402e-05
Epoch 65 MSE:
                3.1460174795938656e-05
Epoch 66 MSE:
                2.7915850296267308e-05
Epoch 67 MSE:
                2.1643580112140626e-05
Epoch 68 MSE:
                2.1331163225113414e-05
Epoch 69 MSE:
                2.418028270767536e-05
Epoch 70 MSE:
                2.291466989845503e-05
Epoch 71 MSE:
                1.833084024838172e-05
Epoch 72 MSE:
                1.700297070783563e-05
Epoch 73 MSE:
                2.0197234334773384e-05
Epoch 74 MSE:
                2.2502872525365092e-05
Epoch 75 MSE:
                2.0820369172724895e-05
Epoch 76 MSE:
                1.8364748029853217e-05
Epoch 77 MSE:
                1.847492421802599e-05
Epoch 78 MSE:
                1.9544700990081765e-05
Epoch 79 MSE:
                1.8688551790546626e-05
Epoch 80 MSE:
                1.682108086242806e-05
Epoch 81 MSE:
                1.6732654330553487e-05
Epoch 82 MSE:
                1.823484490159899e-05
Epoch 83 MSE:
                1.874435656645801e-05
Epoch 84 MSE:
                1.7679976735962555e-05
Epoch 85 MSE:
                1.6936592146521434e-05
Epoch 86 MSE:
                1.7316773664788343e-05
Epoch 87 MSE:
                1.7505795767647214e-05
Epoch 88 MSE:
                1.678896660450846e-05
                1.6250411135843024e-05
Epoch 89 MSE:
Epoch 90 MSE:
                1.6667063391651027e-05
Epoch 91 MSE:
                1.719502870400902e-05
Epoch 92 MSE:
                1.6967635019682348e-05
Epoch 93 MSE:
                1.6474803487653844e-05
Epoch 94 MSE:
                1.6462245184811763e-05
Epoch 95 MSE:
                1.66471454576822e-05
Epoch 96 MSE:
                1.6450934708700515e-05
Epoch 97 MSE:
                1.6113766832859255e-05
Epoch 98 MSE:
                1.6166337445611134e-05
Epoch 99 MSE:
                1.6434723875136115e-05
T-time: 70.90877223014832
```

Train Score: 0.12 RMSE

Time Step = 50 | Hidden States = 32 | Num Layers = 2

Epoch 0 MSE: 0.07202881574630737 Epoch 1 MSE: 0.053314320743083954 Epoch 2 MSE: 0.042539481073617935 Epoch 3 MSE: 0.029014969244599342 Epoch 4 MSE: 0.02872292511165142 Epoch 5 MSE: 0.028398748487234116 Epoch 6 MSE: 0.021048905327916145 Epoch 7 MSE: 0.01160453911870718 Epoch 8 MSE: 0.008795571513473988 Epoch 9 MSE: 0.010022700764238834 Epoch 10 MSE: 0.0026613923255354166 Epoch 11 MSE: 0.002630762290209532 Epoch 12 MSE: 0.008983899839222431 Epoch 13 MSE: 0.004667961969971657 Epoch 14 MSE: 0.00031647970899939537 Epoch 15 MSE: 0.0012351266341283917 Epoch 16 MSE: 0.0032555011566728354 Epoch 17 MSE: 0.003326309146359563 Epoch 18 MSE: 0.002430360997095704 Epoch 19 MSE: 0.0019862183835357428 Epoch 20 MSE: 0.002099730307236314 Epoch 21 MSE: 0.0020998921245336533 Epoch 22 MSE: 0.0014887277502566576 Epoch 23 MSE: 0.0005296168383210897 Epoch 24 MSE: 0.00014128904149401933 Epoch 25 MSE: 0.0008350773132406175 Epoch 26 MSE: 0.0016005054349079728 Epoch 27 MSE: 0.0012693683383986354 Epoch 28 MSE: 0.0004536696942523122 Epoch 29 MSE: 0.00015882925072219223 Epoch 30 MSE: 0.00036899358383379877 Epoch 31 MSE: 0.0005819723010063171 Epoch 32 MSE: 0.0005594798130914569 Epoch 33 MSE: 0.0004207526217214763 Epoch 34 MSE: 0.00037013686960563064 Epoch 35 MSE: 0.00044129276648163795 Epoch 36 MSE: 0.00047366993385367095 Epoch 37 MSE: 0.000334256881615147 Epoch 38 MSE: 0.00011708511738106608 Epoch 39 MSE: 3.76287498511374e-05 Epoch 40 MSE: 0.00015565473586320877

```
Epoch 41 MSE:
                0.0003056139685213566
Epoch
      42 MSE:
                0.00031220243545249104
       43 MSE:
Epoch
                0.00019139598589390516
Epoch
       44 MSE:
                9.156723535852507e-05
Epoch
       45 MSE:
                8.967162284534425e-05
Epoch
       46 MSE:
                0.00012428844638634473
Epoch
       47 MSE:
                0.00012035351392114535
Epoch
       48 MSE:
                9.144780051428825e-05
Epoch 49 MSE:
                9.027418855112046e-05
Epoch
      50 MSE:
                0.00012016412802040577
       51 MSE:
Epoch
                0.000134120651637204
Epoch
      52 MSE:
                0.00010107517300639302
Epoch
       53 MSE:
                4.7545374400215223e-05
Epoch
       54 MSE:
                2.6702458853833377e-05
Epoch 55 MSE:
                5.261333717498928e-05
Epoch 56 MSE:
                8.375279139727354e-05
Epoch
      57 MSE:
                8.108680776786059e-05
       58 MSE:
Epoch
                5.661608884111047e-05
Epoch
       59 MSE:
                4.3734053178923205e-05
Epoch
       60 MSE:
                4.722478843177669e-05
Epoch
       61 MSE:
                4.795711356564425e-05
Epoch
       62 MSE:
                3.8988659071037546e-05
       63 MSE:
Epoch
                3.362500137882307e-05
       64 MSE:
Epoch
                4.101977901882492e-05
                5.044822319177911e-05
       65 MSE:
Epoch
Epoch
       66 MSE:
                4.68259459012188e-05
       67 MSE:
Epoch
                3.276687129982747e-05
Epoch
       68 MSE:
                2.4305238184751943e-05
Epoch
       69 MSE:
                2.8317141186562367e-05
Epoch 70 MSE:
                3.536968506523408e-05
Epoch 71 MSE:
                3.544078572303988e-05
Epoch
      72 MSE:
                3.078533700318076e-05
Epoch
      73 MSE:
                2.8798343919334002e-05
      74 MSE:
Epoch
                2.96215384878451e-05
Epoch
      75 MSE:
                2.827159369189758e-05
Epoch
      76 MSE:
                2.478153328411281e-05
Epoch
      77 MSE:
                2.4055567337200046e-05
Epoch
      78 MSE:
                2.709144609980285e-05
Epoch
      79 MSE:
                2.9113569326000288e-05
Epoch
       80 MSE:
                2.6923336918116547e-05
      81 MSE:
Epoch
                2.3321832486544736e-05
Epoch
       82 MSE:
                2.2435860955738463e-05
Epoch
       83 MSE:
                2.3906835849629715e-05
Epoch
       84 MSE:
                2.4557195501984097e-05
Epoch
       85 MSE:
                2.367859451624099e-05
Epoch
       86 MSE:
                2.314449375262484e-05
Epoch
       87 MSE:
                2.344245331187267e-05
Epoch
       88 MSE:
                2.3117461751098745e-05
```

Epoch 89 MSE: 2.187075551773887e-05 Epoch 90 MSE: 2.1268244381644763e-05 Epoch 91 MSE: 2.200180824729614e-05 Epoch 92 MSE: 2.2697146050632e-05 Epoch 93 MSE: 2.217919609392993e-05 Epoch 94 MSE: 2.117889562214259e-05 Epoch 95 MSE: 2.0869889340247028e-05 Epoch 96 MSE: 2.1089756046421826e-05 Epoch 97 MSE: 2.1048363123554736e-05 Epoch 98 MSE: 2.0773455617018044e-05 Epoch 99 MSE: 2.0754625438712537e-05

T-time: 144.90676140785217

Train Score: 0.14 RMSE

Validation Score: 4.20 RMSE

Time Step = 100 | Hidden States = 2 | Num Layers = 1

Epoch 0 MSE: 0.07423803955316544 Epoch 1 MSE: 0.06203124672174454 Epoch 2 MSE: 0.052469413727521896 Epoch 3 MSE: 0.0457540825009346 Epoch 4 MSE: 0.04189009219408035 Epoch 5 MSE: 0.040506936609745026 Epoch 6 MSE: 0.0407106950879097 Epoch 7 MSE: 0.041262127459049225 Epoch 8 MSE: 0.041162848472595215 Epoch 9 MSE: 0.040045399218797684 Epoch 10 MSE: 0.03807011991739273 Epoch 11 MSE: 0.03564241901040077 Epoch 12 MSE: 0.033191509544849396 Epoch 13 MSE: 0.031046494841575623 Epoch 14 MSE: 0.02938239835202694 Epoch 15 MSE: 0.028214503079652786 Epoch 16 MSE: 0.02742951363325119 Epoch 17 MSE: 0.02684176340699196 Epoch 18 MSE: 0.02625700831413269 Epoch 19 MSE: 0.025525158271193504 Epoch 20 MSE: 0.024569645524024963 Epoch 21 MSE: 0.023391367867588997 Epoch 22 MSE: 0.022053049877285957 Epoch 23 MSE: 0.02065250650048256 Epoch 24 MSE: 0.01929262839257717

```
Epoch
       25 MSE:
                0.01805398240685463
Epoch
       26 MSE:
                0.016975006088614464
Epoch
       27 MSE:
                0.01604432426393032
       28 MSE:
Epoch
                0.015208051539957523
Epoch
       29 MSE:
                0.014390898868441582
       30 MSE:
Epoch
                0.013524261303246021
Epoch
       31 MSE:
                0.012570644728839397
Epoch
       32 MSE:
                0.011534991674125195
Epoch
       33 MSE:
                0.010459394194185734
Epoch
       34 MSE:
                0.009404676035046577
       35 MSE:
Epoch
                0.008426694199442863
Epoch
       36 MSE:
                0.007556214928627014
Epoch
       37 MSE:
                0.006789450999349356
Epoch
       38 MSE:
                0.006092756055295467
Epoch
       39 MSE:
                0.005419867113232613
                0.004734551068395376
       40 MSE:
Epoch
Epoch
       41 MSE:
                0.004028317518532276
       42 MSE:
Epoch
                0.003324625315144658
Epoch
       43 MSE:
                0.0026673595421016216
Epoch
       44 MSE:
                0.0020991861820220947
Epoch
       45 MSE:
                0.001640652772039175
Epoch
       46 MSE:
                0.0012813734356313944
Epoch
       47 MSE:
                0.0009888762142509222
       48 MSE:
Epoch
                0.0007303132442757487
       49 MSE:
                0.0004932325100526214
Epoch
Epoch
       50 MSE:
                0.0002914099604822695
       51 MSE:
Epoch
                0.00015171340783126652
Epoch
       52 MSE:
                9.127146768150851e-05
       53 MSE:
Epoch
                0.0001014421068248339
Epoch
       54 MSE:
                0.00015079641889315099
       55 MSE:
Epoch
                0.00020511528418865055
Epoch
       56 MSE:
                0.00024820936960168183
       57 MSE:
Epoch
                0.0002865428396034986
       58 MSE:
                0.00033503142185509205
Epoch
Epoch
       59 MSE:
                0.0003978427848778665
Epoch
       60 MSE:
                0.0004613298224285245
Epoch
       61 MSE:
                0.0005042845150455832
Epoch
       62 MSE:
                0.0005147713818587363
       63 MSE:
Epoch
                0.0004979148507118225
Epoch
       64 MSE:
                0.00046893928083591163
       65 MSE:
                0.00043958373134955764
Epoch
       66 MSE:
Epoch
                0.0004105371772311628
       67 MSE:
Epoch
                0.00037523635546676815
Epoch
       68 MSE:
                0.0003294380730949342
Epoch
       69 MSE:
                0.00027689404669217765
Epoch
       70 MSE:
                0.00022673631610814482
Epoch
       71 MSE:
                0.00018638174515217543
       72 MSE:
Epoch
                0.00015689595602452755
```

```
Epoch 73 MSE:
               0.00013425225915852934
Epoch 74 MSE:
               0.00011422581155784428
Epoch 75 MSE:
               9.608774416847154e-05
Epoch 76 MSE:
               8.230422827182338e-05
Epoch 77 MSE:
               7.538567297160625e-05
Epoch 78 MSE:
               7.517566700698808e-05
Epoch 79 MSE:
               7.882052886998281e-05
Epoch 80 MSE:
               8.297818567370996e-05
Epoch 81 MSE:
               8.603747846791521e-05
Epoch 82 MSE:
               8.852807513903826e-05
Epoch 83 MSE:
               9.174538718070835e-05
Epoch 84 MSE:
               9.608190157450736e-05
Epoch 85 MSE:
               0.00010052080324385315
Epoch 86 MSE:
               0.00010350743104936555
Epoch 87 MSE:
               0.00010421680053696036
Epoch 88 MSE:
               0.0001030650528264232
Epoch 89 MSE:
               0.0001011444692267105
Epoch 90 MSE:
               9.923225297825411e-05
Epoch 91 MSE:
               9.728129953145981e-05
Epoch 92 MSE:
               9.474386752117425e-05
Epoch 93 MSE:
               9.129689715337008e-05
Epoch 94 MSE:
               8.725529187358916e-05
Epoch 95 MSE:
               8.334159792866558e-05
Epoch 96 MSE:
               8.011083264136687e-05
Epoch 97 MSE:
               7.759446452837437e-05
Epoch 98 MSE:
               7.545122934971005e-05
Epoch 99 MSE:
               7.340600859606639e-05
```

T-time: 56.74695682525635

Train Score: 0.26 RMSE Validation Score: 7.49 RMSE

_____ Time Step = 100 | Hidden States = 2 | Num Layers = 2 ______

Epoch 0 MSE: 0.04546692967414856 Epoch 1 MSE: 0.039492737501859665 Epoch 2 MSE: 0.03701186925172806 Epoch 3 MSE: 0.037262868136167526 Epoch 4 MSE: 0.03848516196012497 Epoch 5 MSE: 0.03909674286842346 Epoch 6 MSE: 0.03875607252120972 Epoch 7 MSE: 0.03785672411322594Epoch 8 MSE: 0.03690577298402786

```
Epoch
      9 MSE:
               0.036265335977077484
Epoch
       10 MSE:
                0.03607096150517464
Epoch
       11 MSE:
                0.036232467740774155
       12 MSE:
Epoch
                0.03651275485754013
Epoch
       13 MSE:
                0.03666657209396362
Epoch
       14 MSE:
                0.03656286001205444
Epoch
       15 MSE:
                0.0362187959253788
Epoch
      16 MSE:
                0.03575211390852928
Epoch 17 MSE:
                0.035303615033626556
Epoch
       18 MSE:
                0.03497019037604332
       19 MSE:
                0.03476761654019356
Epoch
       20 MSE:
Epoch
                0.034632358700037
Epoch
       21 MSE:
                0.03446051850914955
Epoch
       22 MSE:
                0.03416404500603676
Epoch
       23 MSE:
                0.033712781965732574
Epoch 24 MSE:
                0.03314195200800896
Epoch
       25 MSE:
                0.0325264148414135
       26 MSE:
Epoch
                0.03193730115890503
Epoch
       27 MSE:
                0.031399961560964584
Epoch
       28 MSE:
                0.03087461367249489
       29 MSE:
Epoch
                0.03027934394776821
       30 MSE:
Epoch
                0.029548119753599167
Epoch
      31 MSE:
                0.028676461428403854
       32 MSE:
Epoch
                0.027718178927898407
Epoch
       33 MSE:
                0.026741987094283104
Epoch
       34 MSE:
                0.025780363008379936
       35 MSE:
Epoch
                0.024804767221212387
Epoch
       36 MSE:
                0.023749710991978645
       37 MSE:
Epoch
                0.022572260349988937
Epoch
      38 MSE:
                0.021292176097631454
       39 MSE:
                0.019971059635281563
Epoch
Epoch
       40 MSE:
                0.018647434189915657
Epoch
       41 MSE:
                0.017296766862273216
       42 MSE:
Epoch
                0.01587512530386448
Epoch
       43 MSE:
                0.014394804835319519
Epoch
       44 MSE:
                0.012926464900374413
Epoch
       45 MSE:
                0.011520176194608212
Epoch
       46 MSE:
                0.01014833152294159
       47 MSE:
Epoch
                0.008774110116064548
Epoch
       48 MSE:
                0.007447860203683376
Epoch 49 MSE:
                0.006262198090553284
       50 MSE:
Epoch
                0.005233408883213997
Epoch
       51 MSE:
                0.004330867901444435
Epoch
       52 MSE:
                0.0036014374345541
Epoch
       53 MSE:
                0.0030914756935089827
Epoch
       54 MSE:
                0.0027346331626176834
Epoch
       55 MSE:
                0.0024928415659815073
       56 MSE:
                0.0024006287567317486
Epoch
```

Epoch	57	MSE:	0.002391925547271967		
Epoch	58	MSE:	0.0023851708974689245		
Epoch	59	MSE:	0.0023738685995340347		
Epoch	60	MSE:	0.0023164749145507812		
Epoch	61	MSE:	0.0021702104713767767		
Epoch	62	MSE:	0.001958096632733941		
Epoch	63	MSE:	0.0017094245413318276		
Epoch	64	MSE:	0.0014404141111299396		
Epoch	65	MSE:	0.0011885068379342556		
Epoch	66	MSE:	0.0009959802264347672		
Epoch	67	MSE:	0.0008758686017245054		
Epoch	68	MSE:	0.0008225042838603258		
Epoch	69	MSE:	0.0008290021796710789		
Epoch	70	MSE:	0.0008760112687014043		
Epoch	71	MSE:	0.0009308027802035213		
Epoch	72	MSE:	0.0009687095298431814		
Epoch	73	MSE:	0.0009778348030522466		
Epoch	74	MSE:	0.0009502273751422763		
Epoch	75	MSE:	0.0008872014586813748		
Epoch	76	MSE:	0.0008047525770962238		
Epoch	77	MSE:	0.0007217270904220641		
Epoch	78	MSE:	0.0006502973265014589		
Epoch	79	MSE:	0.0005998355918563902		
Epoch	80	MSE:	0.0005758393090218306		
Epoch	81	MSE:	0.0005733300349675119		
Epoch	82	MSE:	0.0005821590893901885		
Epoch	83	MSE:	0.000594444340094924		
Epoch	84	MSE:	0.000601722567807883		
Epoch	85	MSE:	0.0005966474418528378		
Epoch	86	MSE:	0.0005789684946648777		
Epoch	87	MSE:	0.0005519011756405234		
Epoch	88	MSE:	0.0005189916118979454		
Epoch	89	MSE:	0.0004864619404543191		
Epoch	90	MSE:	0.00045988193596713245		
Epoch	91	MSE:	0.000440801348304376		
Epoch	92	MSE:	0.00042945839231833816		
Epoch	93	MSE:	0.0004246684839017689		
Epoch	94	MSE:	0.00042259303154423833		
Epoch	95	MSE:	0.0004198986280243844		
Epoch	96	MSE:	0.00041479148785583675		
Epoch	97	MSE:	0.0004057793412357569		
Epoch	98	MSE:	0.0003930859384126961		
Epoch	99	MSE:	0.0003785613225772977		
T-time: 77.59450316429138					

Train Score: 0.58 RMSE

Time Step = 100 | Hidden States = 4 | Num Layers = 1

Epoch 0 MSE: 0.10220576822757721 Epoch 1 MSE: 0.07853984087705612 Epoch 2 MSE: 0.059243734925985336 Epoch 3 MSE: 0.04412482678890228 Epoch 4 MSE: 0.03293940797448158 Epoch 5 MSE: 0.025347158312797546 Epoch 6 MSE: 0.020899901166558266 Epoch 7 MSE: 0.019051596522331238 Epoch 8 MSE: 0.01916619762778282 Epoch 9 MSE: 0.02053479477763176Epoch 10 MSE: 0.022429851815104485 Epoch 11 MSE: 0.02420106716454029 Epoch 12 MSE: 0.025373516604304314 Epoch 13 MSE: 0.025697452947497368 Epoch 14 MSE: 0.025134656578302383 Epoch 15 MSE: 0.02380424551665783 Epoch 16 MSE: 0.02191835455596447 Epoch 17 MSE: 0.01972578652203083 Epoch 18 MSE: 0.017469344660639763 Epoch 19 MSE: 0.015356210060417652 Epoch 20 MSE: 0.013539176434278488 Epoch 21 MSE: 0.012106914073228836 Epoch 22 MSE: 0.01108232419937849 Epoch 23 MSE: 0.010428481735289097 Epoch 24 MSE: 0.010061383247375488 Epoch 25 MSE: 0.00986784603446722 Epoch 26 MSE: 0.009725969284772873 Epoch 27 MSE: 0.009525023400783539 Epoch 28 MSE: 0.00918186642229557 Epoch 29 MSE: 0.008651645854115486 Epoch 30 MSE: 0.007931661792099476 Epoch 31 MSE: 0.007058367598801851 Epoch 32 MSE: 0.00609850836917758 Epoch 33 MSE: 0.005135832820087671 Epoch 34 MSE: 0.004255205858498812 Epoch 35 MSE: 0.003526163287460804 Epoch 36 MSE: 0.002988358959555626 Epoch 37 MSE: 0.0026421102229505777 Epoch 38 MSE: 0.002447565319016576 Epoch 39 MSE: 0.00233506690710783 Epoch 40 MSE: 0.0022260015830397606

```
41 MSE:
                0.002058287151157856
Epoch
Epoch
       42 MSE:
                0.0018067972268909216
       43 MSE:
                0.0014899043599143624
Epoch
       44 MSE:
Epoch
                0.0011593729723244905
Epoch
       45 MSE:
                0.0008783051744103432
       46 MSE:
Epoch
                0.0006964997737668455
Epoch
       47 MSE:
                0.0006327287410385907
Epoch
       48 MSE:
                0.0006699720397591591
Epoch 49 MSE:
                0.0007642891141586006
Epoch
       50 MSE:
                0.0008627736242488027
       51 MSE:
                0.0009229031857103109
Epoch
Epoch
       52 MSE:
                0.0009257762576453388
Epoch
       53 MSE:
                0.0008789279963821173
Epoch
       54 MSE:
                0.0008089102921076119
Epoch
       55 MSE:
                0.0007475875318050385
      56 MSE:
Epoch
                0.0007180253160186112
Epoch
       57 MSE:
                0.0007255761884152889
       58 MSE:
Epoch
                0.0007574784685857594
Epoch
       59 MSE:
                0.0007905612583272159
Epoch
       60 MSE:
                0.0008028799784369767
Epoch
       61 MSE:
                0.0007833780255168676
Epoch
       62 MSE:
                0.0007352196262218058
Epoch
       63 MSE:
                0.0006721830577589571
       64 MSE:
Epoch
                0.0006110584363341331
       65 MSE:
                0.0005642797332257032
Epoch
Epoch
       66 MSE:
                0.00053595524514094
       67 MSE:
Epoch
                0.000522222719155252
Epoch
       68 MSE:
                0.0005147704505361617
       69 MSE:
Epoch
                0.0005053511704318225
Epoch
      70 MSE:
                0.0004892313736490905
      71 MSE:
Epoch
                0.00046643923269584775
Epoch
       72 MSE:
                0.000440796633483842
Epoch
       73 MSE:
                0.000417589966673404
       74 MSE:
                0.00040106853703036904
Epoch
Epoch
       75 MSE:
                0.00039280415512621403
Epoch
       76 MSE:
                0.0003914093831554055
Epoch
      77 MSE:
                0.0003935022104997188
Epoch
       78 MSE:
                0.00039531258516944945
       79 MSE:
Epoch
                0.00039417247171513736
       80 MSE:
Epoch
                0.0003893002576660365
       81 MSE:
                0.00038168136961758137
Epoch
       82 MSE:
Epoch
                0.0003732599434442818
       83 MSE:
Epoch
                0.0003659017675090581
       84 MSE:
Epoch
                0.00036059843841940165
Epoch
       85 MSE:
                0.000357194512616843
Epoch
       86 MSE:
                0.0003546536900103092
Epoch
       87 MSE:
                0.0003516550059430301
       88 MSE:
                0.00034721099655143917
Epoch
```

Epoch 89 MSE: 0.000341048784321174 Epoch 90 MSE: 0.00033362957765348256 Epoch 91 MSE: 0.0003258560609538108 Epoch 92 MSE: 0.00031864148331806064 Epoch 93 MSE: 0.0003125403309240937 Epoch 94 MSE: 0.00030758912907913327 Epoch 95 MSE: 0.0003033971297554672 Epoch 96 MSE: 0.0002994030073750764 Epoch 97 MSE: 0.00029516342328861356 Epoch 98 MSE: 0.0002905353903770447 Epoch 99 MSE: 0.00028568870038725436

T-time: 40.47112464904785

Train Score: 0.50 RMSE

Validation Score: 12.05 RMSE

Time Step = 100 | Hidden States = 4 | Num Layers = 2

Epoch 0 MSE: 0.1444215029478073 Epoch 1 MSE: 0.11018645018339157 Epoch 2 MSE: 0.08276725560426712 Epoch 3 MSE: 0.06244712322950363 Epoch 4 MSE: 0.04919372871518135 Epoch 5 MSE: 0.04265103116631508 Epoch 6 MSE: 0.04183473065495491 Epoch 7 MSE: 0.0447232723236084 Epoch 8 MSE: 0.04855465143918991 Epoch 9 MSE: 0.05105692520737648 Epoch 10 MSE: 0.05128556117415428 Epoch 11 MSE: 0.04943313077092171 Epoch 12 MSE: 0.04625749588012695 Epoch 13 MSE: 0.042622923851013184 Epoch 14 MSE: 0.03924108296632767 Epoch 15 MSE: 0.03656504675745964 Epoch 16 MSE: 0.034782178699970245 Epoch 17 MSE: 0.03386238217353821 Epoch 18 MSE: 0.03362828493118286 Epoch 19 MSE: 0.03382584825158119 Epoch 20 MSE: 0.03418457880616188 Epoch 21 MSE: 0.0344633013010025 Epoch 22 MSE: 0.03448079153895378 Epoch 23 MSE: 0.03413241356611252 Epoch 24 MSE: 0.033394403755664825

```
Epoch
       25 MSE:
                0.032317277044057846
Epoch
       26 MSE:
                0.03101016767323017
Epoch
       27 MSE:
                0.02961764857172966
       28 MSE:
Epoch
                0.02829066663980484
Epoch
       29 MSE:
                0.027154089882969856
       30 MSE:
Epoch
                0.026275523006916046
Epoch
       31 MSE:
                0.025643348693847656
Epoch
       32 MSE:
                0.02516402117908001
Epoch
       33 MSE:
                0.024686094373464584
Epoch
       34 MSE:
                0.024048419669270515
       35 MSE:
                0.023136435076594353
Epoch
Epoch
       36 MSE:
                0.021923422813415527
Epoch
       37 MSE:
                0.020479852333664894
Epoch
       38 MSE:
                0.018947433680295944
Epoch
       39 MSE:
                0.01748671755194664
      40 MSE:
                0.01621326245367527
Epoch
Epoch
       41 MSE:
                0.01514194905757904
       42 MSE:
Epoch
                0.014165359549224377
Epoch
       43 MSE:
                0.01309503149241209
Epoch
       44 MSE:
                0.01177107822149992
Epoch
       45 MSE:
                0.01018507406115532
Epoch
       46 MSE:
                0.008516045287251472
Epoch
      47 MSE:
                0.007023153826594353
       48 MSE:
Epoch
                0.005849786102771759
       49 MSE:
                0.004897790495306253
Epoch
Epoch
       50 MSE:
                0.003932515624910593
       51 MSE:
Epoch
                0.0028669352177530527
Epoch
       52 MSE:
                0.0019222976407036185
       53 MSE:
Epoch
                0.0014250932727009058
Epoch
       54 MSE:
                0.0013517956249415874
      55 MSE:
Epoch
                0.0012652021832764149
Epoch
       56 MSE:
                0.0010329284705221653
       57 MSE:
Epoch
                0.0010661482810974121
       58 MSE:
Epoch
                0.0014895591884851456
Epoch
       59 MSE:
                0.0018221276113763452
Epoch
       60 MSE:
                0.001871944172307849
Epoch
       61 MSE:
                0.0020059142261743546
Epoch
       62 MSE:
                0.0022587846033275127
       63 MSE:
Epoch
                0.002244588453322649
Epoch
       64 MSE:
                0.0020266538485884666
       65 MSE:
Epoch
                0.0019052538555115461
       66 MSE:
Epoch
                0.0017994402442127466
       67 MSE:
                0.0015432026702910662
Epoch
Epoch
       68 MSE:
                0.0012647812254726887
Epoch
       69 MSE:
                0.001112647820264101
                0.0010124570690095425
Epoch
       70 MSE:
Epoch
       71 MSE:
                0.000872080447152257
       72 MSE:
                0.0007491898140870035
Epoch
```

```
Epoch 73 MSE:
                0.0007145026465877891
Epoch 74 MSE:
                0.0007316105184145272
Epoch 75 MSE:
                0.0007351094391196966
Epoch 76 MSE:
                0.0007271296926774085
Epoch 77 MSE:
                0.0007455088198184967
Epoch 78 MSE:
                0.0007888891850598156
Epoch 79 MSE:
                0.0008192001841962337
Epoch 80 MSE:
                0.0008194715483114123
Epoch 81 MSE:
                0.0008103110012598336
Epoch 82 MSE:
                0.0008098486578091979
Epoch 83 MSE:
                0.000806908356025815
Epoch 84 MSE:
                0.000783643452450633
Epoch 85 MSE:
                0.0007451748824678361
Epoch 86 MSE:
                0.0007108498830348253
Epoch 87 MSE:
                0.000685626408085227
Epoch 88 MSE:
                0.0006576431915163994
Epoch 89 MSE:
                0.0006223925738595426
Epoch 90 MSE:
                0.0005915513611398637
Epoch 91 MSE:
                0.0005736767197959125
Epoch 92 MSE:
                0.0005617919377982616
Epoch 93 MSE:
                0.0005477476515807211
Epoch 94 MSE:
                0.0005358822527341545
Epoch 95 MSE:
                0.0005327108083292842
Epoch 96 MSE:
                0.0005336332251317799
Epoch 97 MSE:
                0.0005308142863214016
Epoch 98 MSE:
                0.0005258049350231886
Epoch 99 MSE:
                0.000523637980222702
```

T-time: 85.3030617237091

Train Score: 0.68 RMSE

Validation Score: 13.13 RMSE

_____ Time Step = 100 | Hidden States = 8 | Num Layers = 1 ______

Epoch 0 MSE: 0.21307465434074402 Epoch 1 MSE: 0.16439317166805267 Epoch 2 MSE: 0.12413185834884644 Epoch 3 MSE: 0.09195061028003693 Epoch 4 MSE: 0.06756473332643509 Epoch 5 MSE: 0.05056929588317871 Epoch 6 MSE: 0.04040263965725899 Epoch 7 MSE: 0.03625325858592987 Epoch 8 MSE: 0.03686176985502243

```
9 MSE:
               0.0403037890791893
Epoch
Epoch
       10 MSE:
                0.04423845559358597
Epoch
       11 MSE:
                0.0468221940100193
       12 MSE:
Epoch
                0.04727797582745552
Epoch
       13 MSE:
                0.04571162909269333
Epoch
       14 MSE:
                0.04268897697329521
Epoch
       15 MSE:
                0.03889985382556915
Epoch
       16 MSE:
                0.03496181592345238
Epoch 17 MSE:
                0.03133165091276169
Epoch
       18 MSE:
                0.028285760432481766
       19 MSE:
                0.025939077138900757
Epoch
       20 MSE:
Epoch
                0.024281766265630722
Epoch
       21 MSE:
                0.023220090195536613
Epoch
       22 MSE:
                0.02261369116604328
Epoch
       23 MSE:
                0.022305656224489212
                0.022144578397274017
Epoch
      24 MSE:
Epoch
       25 MSE:
                0.021999189630150795
       26 MSE:
                0.021766914054751396
Epoch
Epoch
       27 MSE:
                0.021377556025981903
Epoch
       28 MSE:
                0.02079332433640957
       29 MSE:
Epoch
                0.020006267353892326
       30 MSE:
Epoch
                0.019033759832382202
Epoch
       31 MSE:
                0.01791279949247837
       32 MSE:
Epoch
                0.01669355109333992
Epoch
       33 MSE:
                0.015432585962116718
Epoch
       34 MSE:
                0.014186141081154346
       35 MSE:
Epoch
                0.01300378143787384
Epoch
       36 MSE:
                0.011922873556613922
       37 MSE:
Epoch
                0.01096434984356165
Epoch
       38 MSE:
                0.010130415670573711
       39 MSE:
Epoch
                0.009404776617884636
Epoch
       40 MSE:
                0.008755873888731003
Epoch
       41 MSE:
                0.008143097162246704
       42 MSE:
                0.007525244262069464
Epoch
Epoch
       43 MSE:
                0.006869649514555931
Epoch
       44 MSE:
                0.00615982711315155
Epoch
       45 MSE:
                0.005399538669735193
Epoch
       46 MSE:
                0.004611989948898554
       47 MSE:
Epoch
                0.003834160277619958
       48 MSE:
Epoch
                0.003107746597379446
      49 MSE:
Epoch
                0.002469075843691826
       50 MSE:
Epoch
                0.0019406956853345037
Epoch
       51 MSE:
                0.0015268274582922459
Epoch
       52 MSE:
                0.001213868847116828
Epoch
       53 MSE:
                0.000975769420620054
Epoch
       54 MSE:
                0.0007827263325452805
Epoch
       55 MSE:
                0.0006106162909418344
       56 MSE:
                0.00044818909373134375
Epoch
```

```
Epoch 57 MSE:
                0.00029955184436403215
Epoch 58 MSE:
                0.00018080505833495408
Epoch 59 MSE:
                0.00011163775343447924
Epoch
      60 MSE:
                0.00010474259033799171
Epoch 61 MSE:
                0.00015741791867185384
Epoch
      62 MSE:
                0.00024966997443698347
Epoch
      63 MSE:
                0.0003506930952426046
Epoch 64 MSE:
                0.0004311867814976722
Epoch 65 MSE:
                0.0004750486696138978
Epoch 66 MSE:
                0.0004838556924369186
      67 MSE:
                0.00047201261622831225
Epoch
Epoch 68 MSE:
                0.0004563276015687734
Epoch 69 MSE:
                0.0004466180398594588
Epoch 70 MSE:
                0.0004422167257871479
Epoch 71 MSE:
                0.0004349572991486639
Epoch 72 MSE:
                0.00041559801320545375
Epoch 73 MSE:
                0.00037958758184686303
Epoch 74 MSE:
                0.0003294071357231587
Epoch 75 MSE:
                0.0002730463456828147
Epoch 76 MSE:
                0.00022010145767126232
Epoch
     77 MSE:
                0.0001777557481545955
Epoch 78 MSE:
                0.00014849184663034976
Epoch 79 MSE:
                0.00013024781947024167
Epoch 80 MSE:
                0.00011847461428260431
Epoch 81 MSE:
                0.00010878115426748991
Epoch 82 MSE:
                9.88347819657065e-05
Epoch 83 MSE:
                8.881568646756932e-05
Epoch
      84 MSE:
                8.055246144067496e-05
Epoch 85 MSE:
                7.605756400153041e-05
Epoch 86 MSE:
                7.62856361689046e-05
Epoch 87 MSE:
                8.063781569944695e-05
Epoch 88 MSE:
                8.727635577088222e-05
                9.394437802257016e-05
Epoch 89 MSE:
Epoch 90 MSE:
                9.883580059977248e-05
Epoch
      91 MSE:
                0.00010114053293364123
Epoch 92 MSE:
                0.00010109751019626856
Epoch 93 MSE:
                9.962640615412965e-05
Epoch 94 MSE:
                9.776585648069158e-05
Epoch 95 MSE:
                9.618794138077646e-05
Epoch 96 MSE:
                9.498312283540145e-05
Epoch 97 MSE:
                9.376114030601457e-05
Epoch 98 MSE:
                9.196951577905566e-05
Epoch 99 MSE:
                8.924550638766959e-05
T-time: 51.17449331283569
```

Train Score: 0.28 RMSE

Time Step = 100 | Hidden States = 8 | Num Layers = 2

```
Epoch 0 MSE: 0.03707471862435341
Epoch 1 MSE: 0.03339564427733421
Epoch 2 MSE: 0.03382086753845215
Epoch 3 MSE:
              0.029311953112483025
Epoch 4 MSE: 0.026628896594047546
Epoch 5 MSE:
              0.026382839307188988
Epoch 6 MSE: 0.02467113919556141
Epoch 7 MSE:
              0.020772360265254974
Epoch 8 MSE:
              0.017268899828195572
Epoch 9 MSE:
              0.01546290423721075\\
Epoch 10 MSE: 0.013103884644806385
Epoch 11 MSE: 0.008965568616986275
Epoch 12 MSE:
               0.0055631957948207855
Epoch 13 MSE:
               0.004204455763101578
Epoch 14 MSE:
               0.001970494631677866
Epoch 15 MSE:
               0.00017035131168086082
Epoch 16 MSE:
               0.001989265438169241
Epoch 17 MSE:
               0.002198874717578292
Epoch 18 MSE:
               0.003577090334147215
Epoch 19 MSE:
               0.004798573441803455
Epoch 20 MSE:
               0.0034950003027915955
Epoch 21 MSE:
               0.0032668248750269413
Epoch 22 MSE:
               0.0021388300228863955
Epoch 23 MSE:
               0.0007597546791657805
Epoch 24 MSE:
               0.0005750337149947882
Epoch 25 MSE:
               0.00047475830069743097
Epoch 26 MSE:
               0.00026603866717778146
Epoch 27 MSE:
               0.0005514256190508604
Epoch 28 MSE:
               0.00102122756652534
Epoch 29 MSE:
               0.001158423605374992
Epoch 30 MSE:
               0.0011383543023839593
Epoch 31 MSE:
               0.0012428631307557225
Epoch 32 MSE:
               0.001294125453568995
Epoch 33 MSE:
               0.0010787484934553504
Epoch 34 MSE:
               0.0007814308046363294
Epoch 35 MSE:
               0.0006264981348067522
Epoch 36 MSE:
               0.0004919327911920846
Epoch 37 MSE:
               0.000257274106843397
Epoch 38 MSE:
               0.00012254850298631936
Epoch 39 MSE:
               0.0001810167741496116
Epoch 40 MSE:
               0.0002226835349574685
```

```
Epoch 41 MSE:
                0.00023431015142705292
Epoch
       42 MSE:
                0.0003563696227502078
       43 MSE:
Epoch
                0.00044023056398145854
       44 MSE:
Epoch
                0.00039304152596741915
Epoch
       45 MSE:
                0.00036826246650889516
Epoch
       46 MSE:
                0.00033599662128835917
Epoch
       47 MSE:
                0.00022387749049812555
Epoch
       48 MSE:
                0.00015149140381254256
Epoch 49 MSE:
                0.0001400683104293421
Epoch
       50 MSE:
                0.0001097247441066429
       51 MSE:
                0.00010004715295508504
Epoch
Epoch
       52 MSE:
                0.0001414777507307008
Epoch
       53 MSE:
                0.0001680078567005694
Epoch
       54 MSE:
                0.000169643375556916
Epoch
       55 MSE:
                0.00018527763313613832
                0.00019057428289670497
Epoch 56 MSE:
Epoch
       57 MSE:
                0.00016295266686938703
       58 MSE:
Epoch
                0.00013896753080189228
Epoch
       59 MSE:
                0.00012634349695872515
Epoch
       60 MSE:
                0.00010164775449084118
Epoch
       61 MSE:
                8.449011511402205e-05
Epoch
       62 MSE:
                8.968573092715815e-05
Epoch
       63 MSE:
                9.202333603752777e-05
       64 MSE:
Epoch
                9.384521399624646e-05
       65 MSE:
                0.00010718196426751092
Epoch
Epoch
       66 MSE:
                0.0001113109610741958
       67 MSE:
Epoch
                0.0001056872060871683
Epoch
       68 MSE:
                0.00010432756971567869
       69 MSE:
Epoch
                9.646008402341977e-05
Epoch
      70 MSE:
                8.415548654738814e-05
     71 MSE:
Epoch
                8.013949991436675e-05
Epoch
       72 MSE:
                7.67805686336942e-05
Epoch
      73 MSE:
                7.330214430112392e-05
       74 MSE:
                7.672999345231801e-05
Epoch
Epoch
       75 MSE:
                7.954927423270419e-05
Epoch
       76 MSE:
                7.931651634862646e-05
Epoch
      77 MSE:
                8.108190377242863e-05
Epoch
      78 MSE:
                8.023018745006993e-05
       79 MSE:
Epoch
                7.59852264309302e-05
Epoch
       80 MSE:
                7.36021320335567e-05
       81 MSE:
                7.067799742799252e-05
Epoch
Epoch
       82 MSE:
                6.712538743158802e-05
Epoch
       83 MSE:
                6.666338595096022e-05
Epoch
       84 MSE:
                6.651911826338619e-05
Epoch
       85 MSE:
                6.60781588521786e-05
Epoch
       86 MSE:
                6.720135570503771e-05
Epoch
       87 MSE:
                6.711105379508808e-05
       88 MSE:
                6.597684841835871e-05
Epoch
```

```
Epoch 89 MSE: 6.532115367008373e-05
Epoch 90 MSE: 6.350124021992087e-05
Epoch 91 MSE: 6.168305844767019e-05
Epoch 92 MSE: 6.082875916035846e-05
Epoch 93 MSE: 5.968105688225478e-05
Epoch 94 MSE: 5.9179612435400486e-05
Epoch 95 MSE: 5.924106153543107e-05
Epoch 96 MSE: 5.877306466572918e-05
Epoch 97 MSE: 5.8503224863670766e-05
Epoch 98 MSE: 5.8056681154994294e-05
Epoch 99 MSE: 5.703550050384365e-05
```

T-time: 99.33873701095581

Train Score: 0.23 RMSE

Validation Score: 6.30 RMSE

Time Step = 100 | Hidden States = 16 | Num Layers = 1

Epoch 0 MSE: 0.06706604361534119 Epoch 1 MSE: 0.04436690732836723 Epoch 2 MSE: 0.03370099887251854 Epoch 3 MSE: 0.03338708356022835 Epoch 4 MSE: 0.03549585118889809 Epoch 5 MSE: 0.03388630598783493 Epoch 6 MSE: 0.029704220592975616 Epoch 7 MSE: 0.025595663115382195 Epoch 8 MSE: 0.02292419783771038 Epoch 9 MSE: 0.021736405789852142 Epoch 10 MSE: 0.02131044492125511 Epoch 11 MSE: 0.02072521485388279 Epoch 12 MSE: 0.019384324550628662 Epoch 13 MSE: 0.017254222184419632 Epoch 14 MSE: 0.014734073542058468 Epoch 15 MSE: 0.012380959466099739 Epoch 16 MSE: 0.010623198933899403 Epoch 17 MSE: 0.009497130289673805 Epoch 18 MSE: 0.008553418330848217 Epoch 19 MSE: 0.007190728560090065 Epoch 20 MSE: 0.005215237848460674 Epoch 21 MSE: 0.003054378554224968 Epoch 22 MSE: 0.001491608563810587 Epoch 23 MSE: 0.0010530737927183509 Epoch 24 MSE: 0.0012996805598959327

```
Epoch
       25 MSE:
                0.0012142715277150273
Epoch
       26 MSE:
                0.000877538463100791
       27 MSE:
                0.001353441271930933
Epoch
       28 MSE:
Epoch
                0.0025009859818965197
Epoch
       29 MSE:
                0.002752043539658189
       30 MSE:
Epoch
                0.00196783896535635
Epoch
       31 MSE:
                0.0012694193283095956
Epoch
       32 MSE:
                0.0010614170460030437
Epoch
       33 MSE:
                0.0009098565205931664
Epoch
       34 MSE:
                0.0005585725884884596
       35 MSE:
                0.00019879775936715305
Epoch
Epoch
       36 MSE:
                6.967384979361668e-05
Epoch
       37 MSE:
                0.00018242886289954185
Epoch
       38 MSE:
                0.0003692642494570464
Epoch
       39 MSE:
                0.00047615604125894606
                0.0004777273570653051
      40 MSE:
Epoch
Epoch
       41 MSE:
                0.0004449227126315236
       42 MSE:
Epoch
                0.0004466602113097906
Epoch
       43 MSE:
                0.0004872452700510621
Epoch
       44 MSE:
                0.0005169539363123477
Epoch
       45 MSE:
                0.00048727335524745286
Epoch
       46 MSE:
                0.0003959729219786823
Epoch
      47 MSE:
                0.00028640570235438645
       48 MSE:
Epoch
                0.0002076614327961579
       49 MSE:
                0.00017369668057654053
Epoch
Epoch
       50 MSE:
                0.0001584828714840114
       51 MSE:
Epoch
                0.00013017824676353484
Epoch
       52 MSE:
                8.755193266551942e-05
       53 MSE:
Epoch
                5.917192902415991e-05
Epoch 54 MSE:
                6.800428673159331e-05
Epoch 55 MSE:
                0.00010349390504416078
Epoch
       56 MSE:
                0.00013315663090907037
       57 MSE:
Epoch
                0.00013798117288388312
       58 MSE:
Epoch
                0.00012853436055593193
Epoch
       59 MSE:
                0.00012526832870207727
Epoch
       60 MSE:
                0.00013122511154506356
Epoch
       61 MSE:
                0.00013115291949361563
Epoch
       62 MSE:
                0.00011416633060434833
       63 MSE:
Epoch
                8.813440217636526e-05
Epoch
       64 MSE:
                6.924971239641309e-05
       65 MSE:
Epoch
                6.358843529596925e-05
       66 MSE:
Epoch
                6.368599861161783e-05
       67 MSE:
                6.0667422076221555e-05
Epoch
Epoch
       68 MSE:
                5.4665451898472384e-05
Epoch
       69 MSE:
                5.2287225116742775e-05
Epoch
       70 MSE:
                5.694434730685316e-05
Epoch
       71 MSE:
                6.455151742557064e-05
       72 MSE:
Epoch
                6.857593689346686e-05
```

```
Epoch 73 MSE:
               6.713128095725551e-05
Epoch 74 MSE:
               6.37619523331523e-05
               6.217361806193367e-05
Epoch 75 MSE:
Epoch 76 MSE:
               6.198904156917706e-05
Epoch 77 MSE:
               6.018760905135423e-05
Epoch 78 MSE:
               5.5544231145177037e-05
Epoch 79 MSE:
               5.0296879635425285e-05
Epoch 80 MSE:
               4.737967537948862e-05
Epoch 81 MSE:
               4.7098674258450046e-05
Epoch 82 MSE:
               4.734839603770524e-05
Epoch 83 MSE:
               4.662638093577698e-05
Epoch 84 MSE:
               4.5698190660914406e-05
Epoch 85 MSE:
               4.602025364874862e-05
Epoch 86 MSE:
               4.746290505863726e-05
Epoch 87 MSE:
               4.8443380364915356e-05
Epoch 88 MSE:
               4.798573718289845e-05
Epoch 89 MSE:
               4.675654417951591e-05
Epoch 90 MSE:
               4.58893773611635e-05
Epoch 91 MSE:
               4.548495417111553e-05
Epoch 92 MSE:
               4.479126801015809e-05
Epoch 93 MSE:
               4.350845483713783e-05
Epoch 94 MSE:
               4.225626980769448e-05
Epoch 95 MSE:
               4.169773092144169e-05
Epoch 96 MSE:
               4.170795000391081e-05
Epoch 97 MSE:
               4.168456143816002e-05
Epoch 98 MSE:
               4.1391278500668705e-05
Epoch 99 MSE:
               4.113239629077725e-05
```

T-time: 70.78889799118042

Train Score: 0.19 RMSE Validation Score: 4.46 RMSE

_____ Time Step = 100 | Hidden States = 16 | Num Layers = 2 ______

Epoch 0 MSE: 0.12408258020877838 Epoch 1 MSE: 0.06453608721494675 Epoch 2 MSE: 0.03515148162841797 Epoch 3 MSE: 0.034154269844293594 Epoch 4 MSE: 0.04511204734444618 Epoch 5 MSE: 0.04360612854361534 Epoch 6 MSE: 0.03564880043268204 Epoch 7 MSE: 0.029487252235412598 Epoch 8 MSE: 0.02728523686528206

```
9 MSE:
Epoch
               0.027724647894501686
Epoch
       10 MSE:
                0.028681151568889618
Epoch
       11 MSE:
                0.028585800901055336
       12 MSE:
Epoch
                0.026901012286543846
Epoch
       13 MSE:
                0.02389497123658657
Epoch
       14 MSE:
                0.020236847922205925
Epoch
       15 MSE:
                0.01670481264591217
Epoch
      16 MSE:
                0.01395954005420208
Epoch 17 MSE:
                0.012199055403470993
Epoch
       18 MSE:
                0.010709742084145546
       19 MSE:
                0.008159126155078411
Epoch
       20 MSE:
Epoch
                0.004191787447780371
Epoch
       21 MSE:
                0.000692032219376415
Epoch
       22 MSE:
                0.0009982777992263436
Epoch
       23 MSE:
                0.004843182861804962
Epoch 24 MSE:
                0.0056277173571288586
Epoch
       25 MSE:
                0.003672871505841613
       26 MSE:
                0.0026158876717090607
Epoch
Epoch
       27 MSE:
                0.0023620196152478456
Epoch
       28 MSE:
                0.001544103492051363
       29 MSE:
Epoch
                0.0006061323801986873
       30 MSE:
Epoch
                0.0003800494596362114
Epoch
       31 MSE:
                0.0008715828880667686
       32 MSE:
Epoch
                0.0015608648536726832
Epoch
       33 MSE:
                0.001973407808691263
Epoch
       34 MSE:
                0.0019337314879521728
       35 MSE:
Epoch
                0.0015515782870352268
Epoch
       36 MSE:
                0.0010862150229513645
       37 MSE:
Epoch
                0.0007720896392129362
Epoch
       38 MSE:
                0.0006712692556902766
       39 MSE:
Epoch
                0.0006482896860688925
Epoch
       40 MSE:
                0.0005273931310512125
Epoch
       41 MSE:
                0.00030473674996756017
       42 MSE:
                0.0001631538907531649
Epoch
Epoch
       43 MSE:
                0.00025060708867385983
Epoch
       44 MSE:
                0.0004900599597021937
Epoch
       45 MSE:
                0.000653125171083957
Epoch
       46 MSE:
                0.0006010524230077863
       47 MSE:
Epoch
                0.0004058657796122134
Epoch
       48 MSE:
                0.00023931267787702382
Epoch 49 MSE:
                0.00018908140191342682
       50 MSE:
Epoch
                0.00020533171482384205
Epoch
       51 MSE:
                0.00020141387358307838
Epoch
       52 MSE:
                0.00016055458399932832
Epoch
       53 MSE:
                0.0001315039990004152
Epoch
       54 MSE:
                0.00015318852092605084
Epoch
       55 MSE:
                0.00020971804042346776
       56 MSE:
                0.0002506873570382595
Epoch
```

```
Epoch 57 MSE:
                0.00023992203932721168
Epoch 58 MSE:
                0.00018434414232615381
Epoch 59 MSE:
                0.00012327289732638747
Epoch
      60 MSE:
                9.210797725245357e-05
Epoch 61 MSE:
                9.352048800792545e-05
Epoch
      62 MSE:
                0.00010255491361021996
Epoch
      63 MSE:
                9.870973735814914e-05
Epoch 64 MSE:
                8.763580990489572e-05
Epoch 65 MSE:
                8.799202623777092e-05
Epoch 66 MSE:
                0.00010355298581998795
Epoch 67 MSE:
                0.00011711034312611446
Epoch 68 MSE:
                0.000111307468614541
Epoch 69 MSE:
                8.840915688779205e-05
Epoch 70 MSE:
                6.641383515670896e-05
Epoch 71 MSE:
                5.906332080485299e-05
Epoch 72 MSE:
                6.377045065164566e-05
Epoch 73 MSE:
                6.879927241243422e-05
Epoch 74 MSE:
                6.791523628635332e-05
Epoch 75 MSE:
                6.486866186605766e-05
Epoch 76 MSE:
                6.538009620271623e-05
Epoch
     77 MSE:
                6.887183553772047e-05
Epoch 78 MSE:
                6.956209836062044e-05
Epoch 79 MSE:
                6.394551746780053e-05
Epoch 80 MSE:
                5.5134310969151556e-05
Epoch 81 MSE:
                4.940983490087092e-05
Epoch 82 MSE:
                4.948896457790397e-05
Epoch 83 MSE:
                5.234123455011286e-05
Epoch 84 MSE:
                5.3549647418549284e-05
Epoch 85 MSE:
                5.2294381021056324e-05
Epoch 86 MSE:
                5.09826531924773e-05
Epoch 87 MSE:
                5.1067057938780636e-05
Epoch 88 MSE:
                5.1124010497005656e-05
Epoch 89 MSE:
                4.9258695071330294e-05
Epoch 90 MSE:
                4.5962584408698604e-05
Epoch
      91 MSE:
                4.359228478278965e-05
Epoch 92 MSE:
                4.349750452092849e-05
Epoch 93 MSE:
                4.463021832634695e-05
Epoch 94 MSE:
                4.51103514933493e-05
Epoch 95 MSE:
                4.440019984031096e-05
Epoch 96 MSE:
                4.341286330600269e-05
Epoch 97 MSE:
                4.290915603633039e-05
Epoch 98 MSE:
                4.255413296050392e-05
Epoch 99 MSE:
                4.16774237237405e-05
T-time: 164.85564827919006
```

Train Score: 0.19 RMSE

Time Step = 100 | Hidden States = 32 | Num Layers = 1

Epoch 0 MSE: 0.043193817138671875 Epoch 1 MSE: 0.0328713022172451 Epoch 2 MSE: 0.031449638307094574 Epoch 3 MSE: 0.0252162404358387 Epoch 4 MSE: 0.019385751336812973 Epoch 5 MSE: 0.01609146036207676 Epoch 6 MSE: 0.012499547563493252 Epoch 7 MSE: 0.006333150900900364 Epoch 8 MSE: 0.00130689877551049 Epoch 9 MSE: 0.0054242610931396484 Epoch 10 MSE: 0.0032019868958741426 Epoch 11 MSE: 0.0034116581082344055 Epoch 12 MSE: 0.0037063625641167164 Epoch 13 MSE: 0.0012533346889540553 Epoch 14 MSE: 0.00012438288831617683 Epoch 15 MSE: 0.0011515613878145814 Epoch 16 MSE: 0.0022644379641860723 Epoch 17 MSE: 0.0021307356655597687 Epoch 18 MSE: 0.001329698832705617 Epoch 19 MSE: 0.0008679901948198676 Epoch 20 MSE: 0.0009972482221201062 Epoch 21 MSE: 0.0012123000342398882 Epoch 22 MSE: 0.000982549856416881 Epoch 23 MSE: 0.0003899401635862887 Epoch 24 MSE: 2.4583809135947376e-05 Epoch 25 MSE: 0.0002578807179816067 Epoch 26 MSE: 0.0007007899112068117 Epoch 27 MSE: 0.0007229364709928632 Epoch 28 MSE: 0.00039246081723831594 Epoch 29 MSE: 0.0002276269078720361 Epoch 30 MSE: 0.0003421533037908375 Epoch 31 MSE: 0.00041619170224294066 Epoch 32 MSE: 0.00027100834995508194 Epoch 33 MSE: 7.345883204834536e-05 Epoch 34 MSE: 4.323372195358388e-05 Epoch 35 MSE: 0.0001751405216054991 Epoch 36 MSE: 0.00028677834779955447 Epoch 37 MSE: 0.0002595325349830091 Epoch 38 MSE: 0.00015424138109665364 Epoch 39 MSE: 9.81431730906479e-05 Epoch 40 MSE: 0.00012496391718741506

```
Epoch 41 MSE:
                0.0001571471948409453
Epoch
      42 MSE:
                0.00012262188829481602
      43 MSE:
Epoch
                4.882370922132395e-05
Epoch
       44 MSE:
                2.073196264973376e-05
Epoch
      45 MSE:
                6.415956886485219e-05
Epoch
      46 MSE:
                0.00011267148511251435
Epoch
       47 MSE:
                0.00010373230907134712
Epoch
      48 MSE:
                6.0736158047802746e-05
Epoch 49 MSE:
                4.3898671719944105e-05
Epoch
      50 MSE:
                6.025829497957602e-05
      51 MSE:
                6.741538527421653e-05
Epoch
Epoch 52 MSE:
                4.517939669312909e-05
Epoch
      53 MSE:
                2.1070671209599823e-05
Epoch
       54 MSE:
                2.4577529984526336e-05
Epoch 55 MSE:
                4.605635331245139e-05
Epoch 56 MSE:
                5.4881882533663884e-05
Epoch 57 MSE:
                4.257834007148631e-05
      58 MSE:
Epoch
                2.8912132620462216e-05
Epoch
      59 MSE:
                2.9567609090008773e-05
Epoch
       60 MSE:
                3.6037134123034775e-05
Epoch
       61 MSE:
                3.281224053353071e-05
Epoch
      62 MSE:
                2.173690518247895e-05
Epoch
      63 MSE:
                1.765979868650902e-05
       64 MSE:
Epoch
                2.490286533429753e-05
Epoch
       65 MSE:
                3.1519317417405546e-05
Epoch
      66 MSE:
                2.8475295039243065e-05
      67 MSE:
Epoch
                2.1965490304864943e-05
Epoch
       68 MSE:
                2.1153631678316742e-05
      69 MSE:
Epoch
                2.4037433831836097e-05
Epoch 70 MSE:
                2.3189702915260568e-05
Epoch 71 MSE:
                1.869862899184227e-05
Epoch 72 MSE:
                1.7047868823283352e-05
Epoch
      73 MSE:
                2.0069555830559693e-05
Epoch 74 MSE:
                2.2596925191464834e-05
Epoch
      75 MSE:
                2.112187576130964e-05
Epoch
      76 MSE:
                1.8536058632889763e-05
Epoch
      77 MSE:
                1.8433616787660867e-05
Epoch
      78 MSE:
                1.9552699086489156e-05
Epoch 79 MSE:
                1.8884154997067526e-05
Epoch
      80 MSE:
                1.7018197468132712e-05
      81 MSE:
Epoch
                1.67715461429907e-05
Epoch
       82 MSE:
                1.8239665223518386e-05
Epoch
      83 MSE:
                1.8876366084441543e-05
Epoch
       84 MSE:
                1.7863925677374937e-05
Epoch
      85 MSE:
                1.7021719031617977e-05
Epoch
       86 MSE:
                1.733940553094726e-05
Epoch
      87 MSE:
                1.7598360500414856e-05
       88 MSE:
Epoch
                1.6943493392318487e-05
```

Epoch 89 MSE: 1.6356005289708264e-05
Epoch 90 MSE: 1.6714076991775073e-05
Epoch 91 MSE: 1.7275038771913387e-05
Epoch 92 MSE: 1.7100881450460292e-05
Epoch 93 MSE: 1.65865621966077e-05
Epoch 94 MSE: 1.6525815226486884e-05
Epoch 95 MSE: 1.672210964898113e-05
Epoch 96 MSE: 1.6566553313168697e-05
Epoch 97 MSE: 1.6223437341977842e-05
Epoch 98 MSE: 1.624162177904509e-05
Epoch 99 MSE: 1.6512673028046265e-05

T-time: 153.45307683944702

Train Score: 0.12 RMSE

Validation Score: 1.53 RMSE

Time Step = 100 | Hidden States = 32 | Num Layers = 2

Epoch 0 MSE: 0.07239608466625214 Epoch 1 MSE: 0.0533328503370285 Epoch 2 MSE: 0.04271842911839485 Epoch 3 MSE: 0.02913602441549301 Epoch 4 MSE: 0.02877665124833584 Epoch 5 MSE: 0.028437921777367592 Epoch 6 MSE: 0.021063096821308136 Epoch 7 MSE: 0.011573794297873974 Epoch 8 MSE: 0.008774315938353539 Epoch 9 MSE: 0.009984697215259075 Epoch 10 MSE: 0.0025957238394767046 Epoch 11 MSE: 0.0027660687919706106 Epoch 12 MSE: 0.009001781232655048 Epoch 13 MSE: 0.004570898599922657 Epoch 14 MSE: 0.0002907304442487657 Epoch 15 MSE: 0.0012784635182470083 Epoch 16 MSE: 0.0032877177000045776 Epoch 17 MSE: 0.0033262385986745358 Epoch 18 MSE: 0.002422330202534795 Epoch 19 MSE: 0.001988090807572007 Epoch 20 MSE: 0.002108197659254074 Epoch 21 MSE: 0.0021005277521908283 Epoch 22 MSE: 0.0014739141333848238 Epoch 23 MSE: 0.0005119530251249671 Epoch 24 MSE: 0.00014569360064342618

```
Epoch
       25 MSE:
                0.0008617199491709471
Epoch
       26 MSE:
                0.0016119526699185371
Epoch
       27 MSE:
                0.0012539724120870233
       28 MSE:
Epoch
                0.0004400770412757993
Epoch
       29 MSE:
                0.00016250523913186044
Epoch
       30 MSE:
                0.00037983604124747217
Epoch
       31 MSE:
                0.0005867442232556641
Epoch
       32 MSE:
                0.0005561882862821221
Epoch
      33 MSE:
                0.0004166802973486483
Epoch
       34 MSE:
                0.0003719787928275764
       35 MSE:
Epoch
                0.00044736111885868013
Epoch
       36 MSE:
                0.00047611017362214625
Epoch
       37 MSE:
                0.00032965204445645213
Epoch
       38 MSE:
                0.00011155381798744202
Epoch
       39 MSE:
                3.864235623041168e-05
Epoch 40 MSE:
                0.00016215584764722735
Epoch
       41 MSE:
                0.00030992733081802726
       42 MSE:
                0.0003102351911365986
Epoch
Epoch
       43 MSE:
                0.0001871998974820599
Epoch
       44 MSE:
                9.100195165956393e-05
Epoch
       45 MSE:
                9.263315587304533e-05
Epoch
       46 MSE:
                0.00012612967111635953
Epoch 47 MSE:
                0.0001191837654914707
       48 MSE:
Epoch
                9.005325409816578e-05
       49 MSE:
                9.128712554229423e-05
Epoch
Epoch
       50 MSE:
                0.00012252951273694634
      51 MSE:
Epoch
                0.000134940622956492
Epoch
       52 MSE:
                9.949583909474313e-05
       53 MSE:
Epoch
                4.580480890581384e-05
Epoch 54 MSE:
                2.7197278541279957e-05
Epoch 55 MSE:
                5.469685129355639e-05
Epoch
       56 MSE:
                8.475875802105293e-05
      57 MSE:
Epoch
                8.023604459594935e-05
       58 MSE:
Epoch
                5.577812044066377e-05
Epoch
       59 MSE:
                4.4238164264243096e-05
Epoch
       60 MSE:
                4.814324711333029e-05
Epoch
       61 MSE:
                4.797943256562576e-05
Epoch
       62 MSE:
                3.840269346255809e-05
Epoch
       63 MSE:
                3.364432996022515e-05
Epoch
       64 MSE:
                4.186585283605382e-05
       65 MSE:
Epoch
                5.106940443511121e-05
Epoch
       66 MSE:
                4.652586721931584e-05
Epoch
       67 MSE:
                3.2199393899645656e-05
Epoch
       68 MSE:
                2.4409619072685018e-05
Epoch
       69 MSE:
                2.8966527679585852e-05
Epoch
       70 MSE:
                3.572823334252462e-05
Epoch
       71 MSE:
                3.526854925439693e-05
       72 MSE:
Epoch
                3.06549045490101e-05
```

```
Epoch 73 MSE:
               2.9069882657495327e-05
Epoch 74 MSE:
               2.992342342622578e-05
Epoch 75 MSE:
               2.8231610485818237e-05
Epoch 76 MSE:
               2.465201760060154e-05
Epoch 77 MSE:
               2.4231949282693677e-05
Epoch 78 MSE:
               2.74564117717091e-05
Epoch 79 MSE:
               2.9265842385939322e-05
Epoch 80 MSE:
               2.6815683668246493e-05
Epoch 81 MSE:
               2.3288099328055978e-05
Epoch 82 MSE:
               2.2641741452389397e-05
Epoch 83 MSE:
               2.413346192042809e-05
Epoch 84 MSE:
               2.461212352500297e-05
Epoch 85 MSE:
               2.3691178284934722e-05
Epoch 86 MSE:
               2.3285147108254023e-05
Epoch 87 MSE:
               2.3626877009519376e-05
Epoch 88 MSE:
               2.3193537344923243e-05
Epoch 89 MSE:
               2.189729639212601e-05
Epoch 90 MSE:
               2.1400766854640096e-05
Epoch 91 MSE:
               2.2225065549719147e-05
Epoch 92 MSE:
               2.287171082571149e-05
Epoch 93 MSE:
               2.2289423213806003e-05
Epoch 94 MSE:
               2.1346897483454086e-05
Epoch 95 MSE:
               2.1145564460312016e-05
Epoch 96 MSE:
               2.1393236238509417e-05
               2.1325811758288182e-05
Epoch 97 MSE:
Epoch 98 MSE:
               2.106836109305732e-05
Epoch 99 MSE:
               2.110070090566296e-05
T-time: 294.38343834877014
_____
Train Score: 0.14 RMSE
```

Validation Score: 4.34 RMSE

```
[45]:
          time_step num_layers hidden_dim trainScore
                                                           valScore
               30.0
                            1.0
                                       32.0
      0
                                                0.121688
                                                           1.489080
               50.0
                            1.0
                                       32.0
      1
                                                0.120972
                                                           1.502946
               20.0
                            1.0
                                       32.0
                                                0.128503
                                                           1.512104
```

3	100.0	1.0	32.0	0.121259	1.532707
4	30.0	2.0	32.0	0.136286	4.192031
5	50.0	2.0	32.0	0.135944	4.199677
6	20.0	2.0	32.0	0.151878	4.233510
7	20.0	1.0	16.0	0.190952	4.304657
8	30.0	1.0	16.0	0.190652	4.307209
9	100.0	2.0	32.0	0.137073	4.337277
10	50.0	1.0	16.0	0.190993	4.356044
11	100.0	1.0	16.0	0.191380	4.456633
12	20.0	2.0	8.0	0.226076	6.099865
13	30.0	2.0	8.0	0.225242	6.123375
14	50.0	2.0	8.0	0.223641	6.156028
15	100.0	2.0	8.0	0.225360	6.304582
16	20.0	1.0	8.0	0.282497	6.564267
17	30.0	1.0	8.0	0.281694	6.584753
18	50.0	1.0	8.0	0.281779	6.636743
19	100.0	1.0	8.0	0.281901	6.781397
20	30.0	2.0	16.0	0.188312	7.030815
21	20.0	2.0	16.0	0.197614	7.040757
22	50.0	2.0	16.0	0.192309	7.111733
23	20.0	1.0	2.0	0.254993	7.225485
24	30.0	1.0	2.0	0.255085	7.254680
25	100.0	2.0	16.0	0.192644	7.288656
26	50.0	1.0	2.0	0.255254	7.316706
27	100.0	1.0	2.0	0.255664	7.488473
28	30.0	1.0	4.0	0.504123	11.709023
29	20.0	1.0	4.0	0.508851	11.723496
30	50.0	1.0	4.0	0.503882	11.793684
31	100.0	1.0	4.0	0.504372	12.049944
32	20.0	2.0	4.0	0.681148	12.692479
33	30.0	2.0	4.0	0.679634	12.744185
34	50.0	2.0	4.0	0.677197	12.781754
35	100.0	2.0	4.0	0.682841	13.133805
36	30.0	2.0	2.0	0.599233	13.742081
37	20.0	2.0	2.0	0.625895	13.775087
38	50.0	2.0	2.0	0.583369	13.794446
39	100.0	2.0	2.0	0.580593	14.090509

0.17 Selecting Best Model (GRU Model)

```
[46]: best_gru_model = GRU_results.iloc[0]
best_gru_model
```

```
valScore 1.489080
Name: 0, dtype: float64
```

```
Epoch 0 MSE: 0.042843353003263474
Epoch 1 MSE: 0.03270935267210007
Epoch 2 MSE: 0.03124498762190342
Epoch 3 MSE: 0.025008242577314377
Epoch 4 MSE: 0.019258633255958557
Epoch 5 MSE: 0.01602357067167759
Epoch 6 MSE: 0.012408273294568062
Epoch 7 MSE: 0.006237407214939594
Epoch 8 MSE: 0.0013294810196384788
Epoch 9 MSE: 0.005380404647439718
Epoch 10 MSE: 0.003150835633277893
Epoch 11 MSE: 0.0034945064689964056
Epoch 12 MSE: 0.0036857377272099257
Epoch 13 MSE:
               0.0011881171958521008
Epoch 14 MSE:
               0.00012308255827520043
Epoch 15 MSE: 0.0011960119009017944
Epoch 16 MSE: 0.002275234553962946
Epoch 17 MSE:
               0.00209730863571167
Epoch 18 MSE:
               0.0013001244515180588
Epoch 19 MSE: 0.0008742795325815678
Epoch 20 MSE:
               0.0010253657819703221
Epoch 21 MSE:
               0.0012263153912499547
Epoch 22 MSE: 0.0009674275061115623
Epoch 23 MSE: 0.00036626734072342515
Epoch 24 MSE:
               2.199248774559237e-05
Epoch 25 MSE:
               0.000276678561931476
Epoch 26 MSE: 0.0007096833433024585
```

```
27 MSE:
Epoch
                0.0007076485198922455
Epoch
       28 MSE:
                0.0003773518546950072
       29 MSE:
Epoch
                0.00023356100427918136
       30 MSE:
Epoch
                0.0003572253917809576
Epoch
       31 MSE:
                0.0004187347658444196
Epoch
       32 MSE:
                0.0002599924337118864
Epoch
       33 MSE:
                6.487038626801223e-05
Epoch
       34 MSE:
                4.685270687332377e-05
Epoch 35 MSE:
                0.00018392264610156417
Epoch
       36 MSE:
                0.00028856840799562633
       37 MSE:
                0.00025293664657510817
Epoch
Epoch
       38 MSE:
                0.00014842422388028353
Epoch
       39 MSE:
                9.997732558986172e-05
Epoch
       40 MSE:
                0.00013119098730385303
Epoch 41 MSE:
                0.00015975291898939759
Epoch 42 MSE:
                0.00011916370567632839
Epoch
       43 MSE:
                4.474912566365674e-05
                2.1532297978410497e-05
       44 MSE:
Epoch
Epoch
       45 MSE:
                6.806514284107834e-05
Epoch
       46 MSE:
                0.00011381167132640257
Epoch
       47 MSE:
                0.00010091196600114927
Epoch
       48 MSE:
                5.859638986294158e-05
Epoch 49 MSE:
                4.551849633571692e-05
Epoch 50 MSE:
                6.308012234512717e-05
      51 MSE:
                6.769868923583999e-05
Epoch
Epoch
      52 MSE:
                4.327630085754208e-05
Epoch 53 MSE:
                2.0194511307636276e-05
Epoch
       54 MSE:
                2.5933199140126817e-05
      55 MSE:
Epoch
                4.7540917876176536e-05
Epoch 56 MSE:
                5.4552918300032616e-05
Epoch 57 MSE:
                4.1355415305588394e-05
Epoch
       58 MSE:
                2.8862797989859246e-05
      59 MSE:
Epoch
                3.084530180785805e-05
       60 MSE:
                3.693790131364949e-05
Epoch
Epoch
       61 MSE:
                3.2422780350316316e-05
Epoch
       62 MSE:
                2.1102938262629323e-05
Epoch
       63 MSE:
                1.7991360437008552e-05
Epoch
       64 MSE:
                2.5770119464141317e-05
       65 MSE:
Epoch
                3.173542791046202e-05
Epoch
       66 MSE:
                2.802823655656539e-05
      67 MSE:
Epoch
                2.188076905440539e-05
       68 MSE:
Epoch
                2.1766276404378004e-05
       69 MSE:
Epoch
                2.457958908053115e-05
Epoch
      70 MSE:
                2.3126533051254228e-05
Epoch
      71 MSE:
                1.849148429755587e-05
Epoch
       72 MSE:
                1.727827293507289e-05
Epoch
      73 MSE:
                2.052927993645426e-05
       74 MSE:
Epoch
                2.2747533876099624e-05
```

```
Epoch 75 MSE:
               2.0996923922211863e-05
Epoch 76 MSE: 1.8605282093631104e-05
Epoch 77 MSE:
               1.8796945369103923e-05
Epoch 78 MSE:
               1.9834669728879817e-05
Epoch 79 MSE:
               1.8893922970164567e-05
Epoch 80 MSE:
               1.7019039660226554e-05
Epoch 81 MSE:
               1.6985188267426565e-05
Epoch 82 MSE:
               1.849424916144926e-05
Epoch 83 MSE:
               1.89548318303423e-05
Epoch 84 MSE:
               1.787653673090972e-05
Epoch 85 MSE:
               1.7174419554066844e-05
Epoch 86 MSE:
               1.757402060320601e-05
Epoch 87 MSE:
               1.7728389138937928e-05
Epoch 88 MSE:
               1.698232881608419e-05
Epoch 89 MSE:
               1.645882184675429e-05
Epoch 90 MSE:
               1.6893620340852067e-05
Epoch 91 MSE:
               1.7405978724127635e-05
Epoch 92 MSE:
               1.7158952687168494e-05
Epoch 93 MSE:
               1.667603282839991e-05
Epoch 94 MSE:
               1.668017102929298e-05
Epoch 95 MSE:
               1.685604001977481e-05
Epoch 96 MSE:
               1.664023511693813e-05
Epoch 97 MSE:
               1.6302572475979105e-05
Epoch 98 MSE:
               1.6365260307793505e-05
Epoch 99 MSE:
               1.6629777746857144e-05
```

T-time: 41.05872082710266

Train Score: 0.12 RMSE

Validation Score: 1.49 RMSE



0.18 Test Final Model

Epoch 0 MSE: 0.09753220528364182 Epoch 1 MSE: 0.045439865440130234 Epoch 2 MSE: 0.05725377798080444

```
3 MSE:
Epoch
               0.05065715312957764
Epoch
       4 MSE:
               0.041713666170835495
Epoch 5 MSE:
               0.038108691573143005
       6 MSE:
Epoch
               0.037308428436517715
Epoch
      7 MSE:
               0.03632259741425514
Epoch 8 MSE:
               0.033460088074207306
Epoch
       9 MSE:
               0.02942574955523014
Epoch 10 MSE:
                0.02554478868842125
Epoch 11 MSE:
                0.023359300568699837
Epoch
       12 MSE:
                0.02138330787420273
       13 MSE:
                0.013197357766330242
Epoch
       14 MSE:
Epoch
                0.0068166968412697315
Epoch
       15 MSE:
                0.003802439197897911
Epoch
       16 MSE:
                0.0014066006988286972
Epoch
      17 MSE:
                0.0034302102867513895
Epoch 18 MSE:
                0.005794005002826452
Epoch
       19 MSE:
                0.003911020699888468
       20 MSE:
Epoch
                0.0050425343215465546
Epoch
      21 MSE:
                0.004476758185774088
Epoch
       22 MSE:
                0.002021227264776826
Epoch
       23 MSE:
                0.0010002510389313102
      24 MSE:
Epoch
                0.0018644134979695082
Epoch
      25 MSE:
                0.0016121662920340896
      26 MSE:
Epoch
                0.0009011440561152995
Epoch
      27 MSE:
                0.0014458342920988798
Epoch
      28 MSE:
                0.0022129896096885204
       29 MSE:
Epoch
                0.0021586234215646982
Epoch
       30 MSE:
                0.0015157395973801613
      31 MSE:
Epoch
                0.0010952606098726392
Epoch
      32 MSE:
                0.0009024976170621812
      33 MSE:
Epoch
                0.0005764422821812332
Epoch
       34 MSE:
                0.00019403033365961164
Epoch
      35 MSE:
                0.00014283591008279473
      36 MSE:
                0.0003422168083488941
Epoch
Epoch
       37 MSE:
                0.0004511061997618526
Epoch
       38 MSE:
                0.0003693542967084795
Epoch
       39 MSE:
                0.00033453336800448596
Epoch
       40 MSE:
                0.0003689259756356478
       41 MSE:
Epoch
                0.00025166032719425857
Epoch
       42 MSE:
                8.728200191399083e-05
      43 MSE:
                7.921738142613322e-05
Epoch
       44 MSE:
Epoch
                0.00013975825277157128
Epoch
       45 MSE:
                0.00014692985860165209
      46 MSE:
Epoch
                0.00015231090947054327
Epoch
      47 MSE:
                0.00020833630696870387
Epoch
       48 MSE:
                0.0001908188423840329
       49 MSE:
Epoch
                9.97269235085696e-05
       50 MSE:
                6.680258229607716e-05
Epoch
```

```
Epoch 51 MSE:
                6.819955888204277e-05
Epoch
      52 MSE:
                4.5153199607739225e-05
Epoch 53 MSE:
                5.777182741439901e-05
Epoch
      54 MSE:
                0.00010516359907342121
Epoch
      55 MSE:
                9.814016084419563e-05
Epoch
      56 MSE:
                6.346753070829436e-05
Epoch
       57 MSE:
                6.078607475501485e-05
Epoch 58 MSE:
                5.3198604291537777e-05
Epoch 59 MSE:
                2.5294366423622705e-05
Epoch
      60 MSE:
                3.267585634603165e-05
      61 MSE:
Epoch
                5.737528408644721e-05
Epoch
      62 MSE:
                4.4532327592605725e-05
Epoch
      63 MSE:
                4.2996598494937643e-05
Epoch
       64 MSE:
                5.1285467634443194e-05
Epoch 65 MSE:
                3.502670369925909e-05
Epoch 66 MSE:
                2.4239674530690536e-05
Epoch
      67 MSE:
                3.388575350982137e-05
      68 MSE:
Epoch
                3.23239692079369e-05
Epoch
       69 MSE:
                2.6476071070646867e-05
Epoch
      70 MSE:
                3.5279586882097647e-05
Epoch
      71 MSE:
                3.7377551052486524e-05
Epoch 72 MSE:
                2.8233174816705287e-05
Epoch 73 MSE:
                2.8037437004968524e-05
Epoch 74 MSE:
                2.9662693123100325e-05
Epoch 75 MSE:
                2.3611179130966775e-05
Epoch 76 MSE:
                2.4239545382442884e-05
Epoch 77 MSE:
                2.9076647479087114e-05
Epoch 78 MSE:
                2.678815508261323e-05
Epoch 79 MSE:
                2.5374663891852833e-05
Epoch 80 MSE:
                2.7432688511908054e-05
Epoch 81 MSE:
                2.4457796826027334e-05
Epoch
      82 MSE:
                2.193782347603701e-05
Epoch
      83 MSE:
                2.3935710487421602e-05
      84 MSE:
Epoch
                2.3575506929773837e-05
Epoch
       85 MSE:
                2.2655329303233884e-05
Epoch
      86 MSE:
                2.4475588361383416e-05
Epoch
      87 MSE:
                2.3855398467276245e-05
Epoch
      88 MSE:
                2.2036441805539653e-05
      89 MSE:
Epoch
                2.2613952751271427e-05
Epoch
      90 MSE:
                2.2225125576369464e-05
Epoch 91 MSE:
                2.1401459889602847e-05
Epoch
      92 MSE:
                2.2493764845421538e-05
Epoch
      93 MSE:
                2.2600854208576493e-05
Epoch
      94 MSE:
                2.183059223170858e-05
Epoch
      95 MSE:
                2.2168993382365443e-05
Epoch
       96 MSE:
                2.1786667275591753e-05
Epoch
      97 MSE:
                2.108951230184175e-05
      98 MSE:
Epoch
                2.155385482183192e-05
```

Epoch 99 MSE: 2.1572162950178608e-05

T-time: 16.239516973495483

Train Score: 0.26 RMSE

Test Score: 3.14 RMSE

