# Nested Pattern Queries Processing Optimization over Multi-Dimensional Event Streams

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Abstract—Recently, many modern applications have required complex event processing technology to analyze multidimensional stream big data available in real-time data feeds. To address the above requirement, we develop a novel real-time event stream processing method called multi-query optimization strategy (MQOS). MQOS aims at exploiting not only common sub-expressions among nested event pattern queries, but also replicas of the appropriate common operators' results for the queries needed to minimize recalculation and re-communication costs.

We first design a triaxial hierarchy consisting of nested query pattern, nested query concept and operator type hierarchies to specify the relationship among the sub-expressions of queries. Next, based on the triaxial hierarchy, we devise a cost-based heuristic to find an optimized query execution plan with minimum costs of operators and communications. We then propose three reuse schemes of common sub-expressions: nested query pattern-based, nested query concept-based and operator type-based reuse schemes. By integrating the optimized query execution plan-find approach with the three reuse schemes, we present the MQOS to achieve nested pattern queries processing optimization. Finally, our experiments tested on StreamBase under different workload conditions demonstrate the superiority of MQOS.

Keywords-Complex event processing (CEP); Multidimensional event stream; Nested pattern query;

#### I. Introduction

The complex event processing (CEP) over event streams called as event stream processing (ESP) has gained a lot of attentions in recent years, due to their expected capabilities to help business detection, online financial transactions, and sensor networks. Various systems have been proposed in recent years, such as Aurora [1], Borealis [2], STREAM [3], Telegraph [4], SASE [5], Cayuga [6], and PIPES [7] as academic research systems, and Coral8 & Aleri [8], Stream-Base [9], and Oracle CEP [10] as products in the industry. However, there are still many open issues to be solved in the CEP and ESP fields [11].

One of the issues is how to process complex pattern matching over stream big data efficiently. As described in [11], ESP systems have both characteristics of CEP and data stream processing (DSP) systems. CEP systems [12], [13], [14], [15] must be able to support sophisticated pattern

matching over real time event streams, while DSP systems [4], [16], [17] must be able to handle high volume data and continuous data streams with low latency. Fig. 1 shows a concept hierarchy of stock companies and examples of complex event pattern queries, which are written in a query language based on related work [18], [12], [15] as explained in Section III. Such complex pattern queries should be able to involve nests of sequence (SEQ), conjunction (AND), negation (NEG), and combination of them, namely, SEQ NEG and AND NEG operators. Also, stream big data would have many such complex dimensions that objects, time, location, and event type, in nature. For example, time of sale may be organized as a day-month-quarter-year hierarchy and product may be organized as a product-categoryindustry hierarchy. We therefore propose optimization of nested pattern queries over multi-dimensional event streams in this paper.

Our proposal in this paper is based on online analytical processing (OLAP) systems [19] and multi-query optimization [20], and can optimize nested pattern queries over multi-dimensional event streams. Similar to E-cube [18], we design a new model to introduce OLAP functionality for multi-dimensional event stream analysis. We also design reuse schemes of sub-expressions among nested event pattern queries for high throughput of CEP systems. We attempt to exploit the sub-expressions of multiple queries in terms of not only hierarchical events but also SEQ, AND, NEG and their combination operators. To our knowledge, there is no optimization study of processing multiple nested event pattern queries in which all of the above operators can appear. Main contributions of this paper are as follows.

- We design a triaxial hierarchy consisting of nested query pattern, nested query concept and operator type hierarchies to specify the relationship among the subexpressions of queries which can have nested SEQ, AND, NEG and their combination operators.
- On the foundation of the triaxial hierarchy, we design an integrated directed acyclic graph (IDAG) cost model to estimate relative costs of different reuse cases. This cost model allows us to find an optimized query exe-



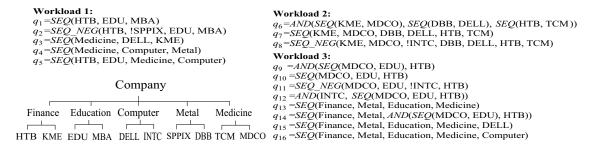


Figure 1. A concept hierarchy of stock companies and event pattern query workloads.

cution plan.

- We design three reuse schemes to alternatively get the replicas number of common sub-expressions and to prepare for computing the rest of queries. The schemes are nested query pattern-based reuse scheme (NQPRS), nested query concept-based reuse scheme (NQCRS), and operator type-based reuse scheme (OTRS).
- By integrating the optimized query execution plan approach with the three reuse schemes, a multi-query optimization strategy (MQOS) is proposed to achieve high throughput of nested pattern queries processing. MQOS reuses not only common sub-expressions among nested pattern queries but also replicas of the appropriate common operators' results for the queries needed to minimize recalculation and re-communication costs.
- We did experiments of the workloads shown in Fig. 1.
   The results show that MQOS can outperform other alternate processing strategies.

The rest of this paper is organized as follows. We review necessary related work in Section II. Nested pattern query processing basics are introduced in Section III. In Section IV, we propose a triaxial hierarchy in terms of nested query pattern, nested query concept and operator type hierarchies. In Section V, we first devise IDAG cost model to find an optimized query execution plan. Next, we design three reuse schemes: NQPRS, NQCRS and OTRS. Then, by integrating the cost model with the three reuse schemes, we propose MQOS. We compare MQOS with related approaches under different workload conditions in the StreamBase system and report the experiment results in Section VI. We conclude our paper in Section VII.

#### II. RELATED WORK

Although there have been studies of CEP systems [5], [6], [18], [12], [13], they can only support flat queries with SEQ operators. For example, ZStream [12] focuses on searching for an optimal execution plan of a single pattern query, but it does not consider multiple nested queries. Cayuga [6] supports sub-queries in FROM clause, but it does not allow us to apply NEG operators over composite event types.

Liu et al. [15] support nested pattern detection queries with SEQ, AND, NEG, and OR operators. However, they

focus on optimization of a single pattern query and do not treat with multiple pattern queries. In addition, they do not support OLAP functionality for multi-dimensional event analysis.

Cuzzocrea et al. [21], [22] try to support efficient OLAP analysis on multidimensional data streams. However, they do not focus on complex event pattern query processing.

E-cube [18] introduces OLAP for multi-dimensional event stream analysis. An event concept hierarchy and E-Cube hierarchy of queries with query concept refinement and query pattern refinement are introduced for supporting OLAP operations over multi-dimensional event streams. However, it focuses only on SEQ operators with NEG operators.

In contrast to these studies, our work supports OLAP functionality for multi-dimensional event stream analysis and focuses on optimization of multiple nested queries with SEQ, AND, NEG and their combination operators.

#### III. NESTED PATTERN QUERY PROCESSING BASICS

In this section, we introduce basic event model, nested pattern query language, types of operators and their formal semantics. They all are based on related studies, e.g., [18], [12], [13], [15].

#### A. Event Model

An event which represents an instance is an occurrence of interest at a point in time. Basically, events can be classified into primitive events and composite events.

**Definition 1:** A primitive event  $e_i$  is typically modeled multi-dimensionally denoted as  $e_i = e(e_i.t, (e_i.st = e_i.et), < a_1, \ldots, a_m >)$ , where  $e_i.t$  is event type that describes the essential features of  $e_i$ ,  $e_i.st$  is the start time-stamp of  $e_i$ ,  $e_i.et$  is the end time-stamp of  $e_i$ ,  $< a_1, \ldots, a_m >$  are other attributes of  $e_i$  and the number of attributes in  $e(\cdot)$  denotes the dimensions of interest.

**Definition 2:** Based on Definition 1, a composite event is denoted as  $e=e(e.t, (\min_{1\leq i\leq n}e_i.st \neq \max_{1\leq i\leq n}e_i.et), < a_1, \ldots, a_q >).$ 

#### B. Nested Pattern Query Language

We introduce the following language for specifying nested pattern queries which supports nests of SEQ, AND, NEG and their combination operators: PATTERN (Event Expression: composite event expressed by nesting of SEQ, AND, NEG and their combination operators)

WHERE (Qualification: value constraint) WITHIN (Window: time constraint)

#### C. Types of Operators and their Formal Semantics

We define operators that appear in the PATTERN clause of a query. In the following,  $E_i$  denotes an event type.

**Definition 3:** A SEQ operator [18], [15] specifies a particular order according with the start time-stamps in which the event must occur to match the pattern and thus form a composite event:

$$SEQ(E_1, ..., E_i, ..., E_n) = \{ \langle e_1, ..., e_i, ..., e_n \rangle \mid (e_1.st < ... < e_i.st < ... < e_n.st) \land (e_1.t = E_1) \land ... \land (e_i.t = E_n) \}.$$

A  $SEQ(E_1, ..., SEQ(E_i, ..., E_j), ..., E_n)$  expression can be flattened as  $SEQ(E_1, ..., E_i, ..., E_j, ..., E_n)$ .

**Definition 4:** An AND operator [15] takes a set of event types as input and events occur within a specified time window without specified time order:

$$AND(E_1, ..., E_i, ..., E_n) = \{ \langle e_1, ..., e_i, ..., e_n \rangle |$$
  
 $(e_1.t = E_1) \wedge ... \wedge (e_i.t = E_i) \wedge ... \wedge (e_n.t = E_n) \}.$ 

An  $AND(E_1, ..., AND(E_i, ..., E_j), ..., E_n)$  expression can be flattened as  $AND(E_1, ..., E_i, ..., E_j, ..., E_n)$ 

**Definition 5:** The symbol "!" before an event type  $E_i$  expresses the negation of  $E_i$  and indicates that  $E_i$  is not allowed to appear in the specified position. The operator with symbol "!" denotes as NEG operator [18], [13], [15].

**Definition 6:** A  $SEQ\_NEG(E_{i-1}, !E_i, E_{i+1})$  operator specifies that no event of  $E_i$  can appear between  $E_{i-1}$  and  $E_{i+1}$  with specified time order:

$$SEQ\_NEG(E_{i-1}, !E_i, E_{i+1}) = \{ \langle e_{i-1}, e_{i+1} \rangle \mid (e_{i-1}.st \langle e_{i+1}.st) \wedge (e_{i-1}.t = E_{i-1}) \wedge (e_{i+1}.t = E_{i+1}) \wedge (\neg \exists e_i where (e_i.t = E_i) \wedge (e_{i-1}.et \langle e_i.st \leq e_i.et \langle e_{i+1}.st)) \}.$$

This operator can be interpreted as  $NEG(SEQ(E_{i-1}, E_{i+1}), !E_i)$  with time constraint  $e_{i-1}.et < e_i.st \le e_i.et < e_{i+1}.st$ .

**Definition 7:** An  $AND\_NEG(E_i, !E_k, E_j)$  operator specifies that no event of  $E_k$  can appear between  $E_i$  and  $E_j$  without specified time order:

$$\begin{split} AND\_NEG(E_i, !E_k, E_j) &= \{ < e_i, e_j > | (e_i.t = E_i) \land (e_j.t = E_j) \land (\neg \exists e_k \ where \ (e_k.t = E_k) \land ((e_i.et < e_k.st \leq e_k.et < e_j.st) \lor (e_j.et < e_k.st \leq e_k.et < e_i.st))) \}. \end{split}$$

This operator can be interpreted as  $NEG(AND(E_i, E_j), !E_k)$  with time constraint  $(e_i.et < e_k.st \le e_k.et < e_j.st)$  $\lor (e_j.et < e_k.st \le e_k.et < e_i.st).$ 

Table I NOTATION

Notation	Meaning		
$EPQ(E_i, E_j)$	abstract expression of event pattern query with		
	event types $E_i$ and $E_j$		
$R_{E_i}$	input rate of source data of $E_i$		
$\lambda(s_c)$	input rate of stream $s_c$		
$L(s_c)$	network latency of stream $s_c$		
$TW_p$	time window specified in a given pattern query		
$P_{E_i}$	selectivity of all single-class predicates for $E_i$		
\( \ell \)	number of streams		
$N_{E_i}$	number of events of $E_i$ within $TW_p$		
$\begin{array}{ c c }\hline N_{E_i} \\ P_{E_i,E_j}^t \end{array}$	selectivity of the implicit time predicate between		
"	$E_i$ and $E_j$ , with $e_i.et < e_j.st$		
$P_{E_i,E_j}$	selectivity of multi-class predicates between $E_i$		
	and $E_j$		
$C^i_{O_h}$ $C^o_{O_h}$	cost of operator $O_h$ to access its input data		
$C_{O_h}^o$	cost of operator $O_h$ to generate its output data		
$\mid C_{O_h} \mid$	total cost of operator $O_h$		
$C_{s_c}$	communication cost used for stream $s_c$		
$P_k$	candidate query execution plan		
$G_k$	integrated directed acyclic graph $P_k$		
$Total\ Cost(G_k)$	total operator cost of $P_k$		
$PT_{q_t}$	expression or sub-expression of query $q_t$		
$R_{PT_{q_{t}}}$	results of $PT_{q_t}$		
$ P_{opt} $	optimized query execution plan		
$PL_{P_k}$	number of subsets of $P_k$		
$P^s$	set of $P_k$ with the smallest $PL_{P_k}$		

#### IV. TRIAXIAL HIERARCHY MODEL

An event concept hierarchy is commonly used to summarize information at different levels of abstraction. Based on the hierarchies introduced in [18], for efficiently and directly reusing common operators' results, we define a novel triaxial hierarchy to specify the relationship among the sub-expressions of queries. Dissimilar to [18], in our new definitions of nested query pattern and concept hierarchies, (i) we focus on nests of SEQ, AND, NEG and their combination operators, not just pure SEQ operator, and (ii) the finer level nested query pattern can be formed from its coarser level directly, rather than after eliminating some event types from its coarser level. Here, we define event type  $E_{ni}$  is a finer level (resp. coarser level) of an event type  $E_n$  (resp.  $E_{nij}$ ) in an event concept hierarchy expressed as  $E_{nij} \subset E_{ni} \subset E_n$ . Fig. 1 depicts a concept hierarchy of stock companies which is organized as (stock category)-(company category)-(company) hierarchy. And event type Finance is a finer level of Company and coarser level of HTB, expressed as HTB ⊂ Finance ⊂ Company. Table I shows key notations used in the rest of this paper. We introduce  $EPQ(E_i, E_i)$ , which is an abstract event pattern query expression with event types  $E_i$  and  $E_j$ . This is only necessary for the discussions in this paper.

**Definition 8:** A nested query pattern hierarchy (NQPH) is a directed acyclic graph (DAG) where nodes correspond to expressions or sub-expressions of queries denoted as  $PT_{q_i}$ . A pattern query is formed by combining primitive

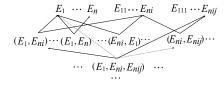


Figure 2. A directed acyclic graph of NQPH.

$$PT_{q_9}^{=AND(SEQ(\mathrm{MDCO,EDU}),\mathrm{HTB})}$$
  $PT_{q_{13}}^{=SEQ(\mathrm{Finance,Metal})}$ 

$$PT_{q_{13}}^{=SEQ(\mathrm{Finance,Metal},AND(SEQ(\mathrm{MDCO,EDU}),\mathrm{HTB}))}$$

Figure 3. Relationship based on NQPH.

Figure 4. A tree of NQCH of event types.

or composite event types. The longest pattern queries reside at the bottom of NQPH model, while shorter pattern queries progressively reside higher (say EPQ( $E_1$ ,  $E_{ni}$ ,  $E_{nij}$ )) and much higher (say EPQ( $E_1$ ,  $E_{ni}$ )) in NQPH model as shown in Fig. 2.  $PT_{q_i}$  is a coarser level of  $PT_{q_j}$ , denoted by  $PT_{q_j}$  control of  $PT_{q_j}$ , (ii)  $\forall$  EPQ( $E_k$ , ...,  $E_{kp}$ , ...,  $E_{kpf}$ )  $\in$   $PT_{q_i}$  ( $1 \le k \le n$ ,  $1 \le p \le i$ ,  $1 \le f \le j$ ),  $\exists$  EPQ( $E_m$ , ...,  $E_{mp}$ , ...,  $E_{mp}$ )  $\in$   $PT_{q_j}$  ( $1 \le m \le n$ ), such that  $E_k = E_m$ ,  $E_{kp} = E_{mp}$ ,  $E_{kpf} = E_{mpf}$ , and (iii)  $\exists$  EPQ( $E_h$ , ...,  $E_{hp}$ , ...,  $E_{hpf}$ )  $\in$   $PT_{q_j}$ , and  $\notin$   $PT_{q_i}$ , such that  $E_h \ne E_k$ ,  $E_{hp} \ne E_{kp}$ ,  $E_{hpf} \ne E_{kpf}$  ( $1 \le h \le n$ ).

In other words, we can drill down  $PT_{q_i}$  to a finer level  $PT_{q_j}$  by adding one or more event types from  $PT_{q_i}$ . For example, as shown in Fig. 1, let us consider  $q_9 = AND(SEQ(\text{MDCO}, \text{EDU}), \text{HTB}), \ q_{13} = SEQ(\text{Finance}, \text{Metal}, \text{Education}, \text{Medicine})$  and  $q_{14} = SEQ(\text{Finance}, \text{Metal}, AND(SEQ(\text{MDCO}, \text{EDU}), \text{HTB}))$ . The text in box of Fig. 3 specifies the relationship among those expressions or sub-expressions of pattern queries in terms of Definition 8. Queries  $q_9$  and  $q_{13}$  has the same kind of expression with part of  $q_{14}$ , i.e.,  $AND(SEQ(\cdot))$  and  $SEQ(\cdot)$ , respectively. We can see that query  $q_{14}$  is a finer level of query  $q_9$  and sub-expression of query  $q_{13}$ . Hence,  $q_{14}$  can be formed by reusing sub-expressions of  $q_{13}$  and  $q_9$ 's results, SEQ(Finance, Metal) and AND(SEQ(MDCO, EDU), HTB), and joining them by SEQ operator.

**Definition 9:** A nested query concept hierarchy (NQCH) is a tree where the apex node has empty episode and the other nodes correspond to expressions or sub-expressions

 $PT_{q_4}$ =SEQ(Medicine, Computer)  $\uparrow$   $PT_{q_3}$ =SEQ(Medicine, DELL)

Figure 5. Relationship based on NQCH.



Figure 6. OTH and containment relationships among pattern queries based on it.

of queries. The pattern queries with the most specific event types reside at the leaves of the tree, while pattern queries with more general event types progressively reside higher (say  $\mathrm{EPQ}(E_1,\,E_2,\,\ldots,\,E_{ni1})$ ) and much higher (say  $\mathrm{EPQ}(E_1,\,E_2,\,\ldots,\,E_{ni})$ ) in NQCH model as shown in Fig. 4.  $PT_{q_i}$  is a finer level of  $PT_{q_j}$ , denoted by  $PT_{q_i}\subset_C PT_{q_j}$ , if (i)  $PT_{q_i}$  has the same kind of expression with part of  $PT_{q_j}$ , (ii)  $\forall$   $\mathrm{EPQ}(E_{gp},\,\ldots,\,E_{hp},\,\ldots,\,E_{mp}) \in PT_{q_i},\,\exists$   $\mathrm{EPQ}(E_{d},\,\ldots,\,E_{k},\,\ldots,\,E_{n}) \in PT_{q_j},\,$  such that  $E_{gp}\subset E_{d},\,E_{hp}\subset E_{k},\,E_{mp}\subset E_{n},\,$  and (iii)  $\exists$   $\mathrm{EPQ}(E_{ap},\,\ldots,\,E_{bp},\,\ldots,\,E_{cp}) \in PT_{q_j},\,$  and  $\not\in PT_{q_i},\,$  such that  $E_{ap}\neq E_{gp},\,E_{bp}\neq E_{hp},\,E_{cp}\neq E_{mp}\,\,(1\leq a\leq b\leq c\leq d\leq g\leq n).$ 

In other words, we can roll up  $PT_{q_i}$  to a coarser level  $PT_{q_j}$  by merging  $PT_{q_i}$  with the rest expression that belongs to  $PT_{q_j}$  but is not captured by  $PT_{q_i}$ . For example, as shown in Fig. 1, let us consider  $q_3 = SEQ(\text{Medicine}, \text{DELL}, \text{KME})$  and  $q_4 = SEQ(\text{Medicine}, \text{Computer}, \text{Metal})$ . The text in box of Fig. 5 specifies the relationship among those expressions or sub-expressions of queries in terms of Definition 9. We can see that the sub-expression of query  $q_3$  is a finer level of sub-expression of query  $q_4$ . Hence, sub-expression of  $q_4$ , SEQ(Medicine, Computer), can be formed by reusing sub-expression of  $q_3$ 's results, SEQ(Medicine, DELL), and merging it with the rest sub-expression, i.e., SEQ(Medicine, INTC).

We describe three kinds of expressions of pattern queries based on the operator types it used as  $AND(SEQ(\cdot))$ ,  $SEQ(\cdot)$  and  $NEG(SEQ(\cdot))$ . Apart from mining relationships in terms of NQPH and NQCH, Fig. 6 depicts the containment relationships among the three kinds of expressions of pattern queries.

**Definition 10:** An operator type hierarchy (OTH) is shown in Fig. 6.  $AND(SEQ(\cdot))$   $PT_{q_i}$  is a coarser level of  $SEQ(\cdot)$  or  $NEG(SEQ(\cdot))$   $PT_{q_j}$ , denoted by  $PT_{q_j} \subset_O PT_{q_i}$ , if for the positive part of pattern query, (i)  $PT_{q_j}$  has the same kind of expression with part of  $PT_{q_i}$ , (ii)  $\forall$   $SEQ(E_k, \ldots, E_h, E_m, \ldots, E_n) \in PT_{q_j}$ ,  $\exists$   $SEQ(E_a, \ldots, E_b, E_c, \ldots, E_d) \in PT_{q_i}$ , such that  $E_k = E_a$ ,  $E_h = E_b$ ,  $E_m = E_c$ ,  $E_n = E_d$ , and (iii)  $\exists$   $SEQ(E_m, \ldots, E_n, E_k, \ldots$ 

 $PT_{q_{6}}^{T=AND(SEQ(\text{KME, MDCO}), SEQ(\text{DBB, DELL}), SEQ(\text{HTB, TCM}))} \\ | \text{prepared type} \\ PT_{q_{7}}^{T=SEQ(\text{KME, MDCO, DBB, DELL, HTB, TCM})} \\ | \text{prepared type} \\ PT_{q_{7}}^{T=SEQ\_NEG(\text{KME, MDCO, !INTC, DBB, DELL, HTB, TCM})} \\ | \text{prepared type} \\ | \text{prepared type$ 

Figure 7. Relationship based on OTH.

 $E_h$ )  $\in PT_{q_i}$ , and  $\notin PT_{q_j}$ , such that  $E_m \neq E_a$ ,  $E_n \neq E_b$ ,  $E_k \neq E_c$ ,  $E_h \neq E_d$ .

 $SEQ(\cdot)$   $PT_{q_i}$  is a coarser level of  $NEG(SEQ(\cdot))$   $PT_{q_i}$ , denoted by  $PT_{q_i} \subset_O PT_{q_i}$ , if for the positive part of pattern query, (i)  $\forall SEQ(E_k, ..., E_h, E_m, ..., E_n) \in PT_{q_i}, \exists$  $SEQ(E_a, ..., E_b, E_c, ..., E_d) \in P_{PT_{q_i}}$ , such that  $E_k = E_a$ ,  $E_h = E_b, E_m = E_c, E_n = E_d, (ii) \forall SEQ(E_a, ..., E_b,$  $E_c, ..., E_d \in PT_{q_i}, \exists SEQ(E_k, ..., E_h, E_m, ..., E_n) \in$  $P_{PT_{q_i}}$ , such that  $E_a = E_k$ ,  $E_b = E_h$ ,  $E_c = E_m$ ,  $E_d = E_n$ . In other words, we can drill down  $PT_{q_i}$  to a finer level  $PT_{q_i}$  by filtering out some data that are not captured by  $PT_{q_i}$ . For example, as shown in Fig. 1, let us consider  $q_6 = AND(SEQ(KME, MDCO), SEQ(DBB,$ DELL), SEQ(HTB, TCM)),  $q_7 = SEQ(KME, MDCO,$ DBB, DELL, HTB, TCM) and  $q_8 = SEQ\_NEG(KME,$ MDCO, !INTC, DBB, DELL, HTB, TCM). The text in box of Fig. 7 specifies the relationship among those expressions or sub-expressions of queries in terms of Definition 10. We can see that query  $q_7$  is a finer level of query  $q_6$  and coarser level of query  $q_8$ . Thus,  $q_7$  can be formed by reusing  $q_6$ 's results, i.e., filtering some data that are not captured by  $q_7$ . After that, we can generate  $q_8$  by reusing  $q_7$ 's results, namely, filtering out some data in accordance with INTC negative event type.

**Definition 11:** A triaxial hierarchy is an integrated directed acyclic graph (IDAG), denoted by  $G_k(P_k, S_k)$ , where (i)  $P_k$  is a finite set of expressions or sub-expressions of queries  $\{PT_{q_1}, \ldots, PT_{q_t}, \ldots, PT_{q_r}\}$ , denoted by a candidate query execution plan, which corresponds to a set of operators  $\{O_1, \ldots, O_h, \ldots, O_n\}$  called  $G_k$ 's vertices, and (ii)  $S_k$  denotes a finite set of streams  $\{s_1, \ldots, s_c, \ldots, s_\ell\}$  called  $G_k$ 's edges, and the stream  $s_c$  labeled with a relationship between expressions or sub-expressions of queries is in terms of Definitions 8, 9 and 10 like as shown in Figs. 3, 5 and 7.

#### V. MULTI-QUERY OPTIMIZATION STRATEGY

In this section, we first devise an IDAG cost estimation model to generate an optimized query execution plan on the basis of the triaxial hierarchy. After getting the optimized query execution plan, we need to record each expression or sub-expression's reuse condition and prepare for computing the rest of sub-expression for the query needed. Therefore, we propose three reuse schemes below. Then, by integrating the above two proposals, we present the MQOS to achieve nested pattern queries processing optimization.

#### A. Finding an Optimized Query Execution Plan

 $R_{E_i}$  represents the number of events of  $E_i$  per unit time.  $P_{E_i}$  represents the selectivity of all single-class predicates for the event type  $E_i$ .  $T_{W_p}$  specifies the time window in a given pattern query. We denote  $N_{E_i}$  as the number of events of  $E_i$  that are within time constraint  $T_{W_p}$  as  $R_{E_i} \times T_{W_p} \times P_{E_i}$ . Let  $C_{O_h}^i$  and  $C_{O_h}^o$  be input and output costs of operator  $O_h$ , respectively. We measure CPU cost of  $O_h$ ,  $C_{O_h}$ , as follows:

$$C_{O_h} = C_{O_h}^i + C_{O_h}^o. (1)$$

Let  $\lambda(s_c)$  be the input rate of stream  $s_c$  and  $L(s_c)$  be the network latency of stream  $s_c$ . We define the communication cost of stream  $s_c$ ,  $C_{s_c}$ , as follows:

$$C_{s_c} = \lambda(s_c) \times L(s_c), \quad 1 \le c \le \ell.$$
 (2)

$$\lambda(s_c) = \begin{cases} N_{E_i}, & \text{if } s_c \text{ connects data source of } E_i \text{ with an} \\ & \text{operator} \\ C_{O_h}^o, & \text{if } s_c \text{ connects two operators} \end{cases}$$

Table II summarizes the input and output cost formulas for each operator.  $P_{E_i,E_j}^t$  represents the selectivity of the implicit time predicate between  $E_i$  and  $E_j$ , with time constraint  $e_i.et < e_j.st.$   $P_{E_i,E_j}$  represents the selectivity of multi-class predicates that can be defined in advance [12]. For example, we can set  $e_i.price < e_j.price$  and the selectivity of multi-class predicates as 1/2 in advance.

**Definition 12:** We define  $P = \{P_1, \dots, P_k, \dots, P_m\}$  as a set of candidate query execution plans where  $P_k$  represents a kind of way to form query  $q_j$ . Based on Definition 11, we define  $G = \{G_1, \dots, G_k, \dots, G_m\}$  as a set of IDAGs corresponding to P.  $G_k$  is with a set of operators  $\{O_1, \dots, O_h, \dots, O_n\}$  and a set of streams  $\{s_1, \dots, s_c, \dots, s_\ell\}$ . Each operator has a total cost  $C_{O_h}$  as (1). Each stream has a communication cost as (2). An IDAG,  $G_k$ , has the associated operator computation and communication cost, denoted by  $Total\ Cost(G_k)$ :

$$Total\ Cost(G_k) = \sum_{h=1}^{n} C_{O_h} + \sum_{c=1}^{\ell} C_{s_c}.$$
 (4)

Optimized Query Execution Plan-Finder Problem: Given a set of expressions or sub-expressions of queries  $\{PT_{q_1}, \ldots, PT_{q_i}\}$  and a provisioned query  $q_j$ , we can find some relationships between  $PT_{q_i}$  and  $PT_{q_j}$  in terms of NQPH, NQCH and OTH alternatively. Those expressions or sub-expressions can be grouped along with their remaining sub-expressions as a set of candidate query execution plans  $P = \{P_1, \ldots, P_k, \ldots, P_m\}$  to perform  $q_j$ . We aim to find a  $P_{opt}$  from P to perform  $q_j$  where the  $P_{opt}$  is with  $\{PT_{q_1}, \ldots, PT_{q_t}, \ldots, PT_{q_t}, \ldots, PT_{q_t}\}$ , and its IDAG is with minimum  $Total\ Cost(\cdot)$ , denoted by  $G_{opt}$ .  $G_{opt}$  is the execution way,

Table II Cost formulas for operators

Operator	Meaning	Input Cost $C_{O_h}^i$	Output Cost $C_{O_h}^o$
$SEQ(E_i, E_j)$	combine primitive $e_i$ of $E_i$ with $e_j$ of	$N_{E_i} \times N_{E_j} \times P_{E_i, E_j}^t$	$N_{E_i} \times N_{E_j} \times P_{E_i, E_j}^t \times P_{E_i, E_j}$
	$E_j$ that $e_i.et < e_j.st$ within $TW_p$	,	
$AND(E_i, E_j)$	combine primitive $e_i$ of $E_i$ with	$N_{E_i} \times N_{E_j}$	$N_{E_i} \times N_{E_j} \times P_{E_i,E_j}$
	any $e_j$ of $E_j$ within $TW_p$		, , ,
$SEQ\_NEG(E_i, !E_k, E_j) \Longrightarrow$	remove the results from $SEQ\_NEG$ operator	$C_{O_{seq}}^{i} + C_{O_{seq}}^{o}$	$C_{O_{seg}}^{o} + C_{O_{seg}}^{o} \times (1 -$
$NEG(SEQ(E_i, E_j), !E_k)$	where $e_k$ of $E_k$ appears between $E_i$ and $E_j$	,	$ \begin{vmatrix} C_{O_{seq}}^{o} + C_{O_{seq}}^{o} \times (1 - P_{E_{i}, E_{k}}^{t} \times P_{E_{k}, E_{j}}^{t}) \times P_{E_{i}, E_{j}}^{t} \end{vmatrix} $
$AND\_NEG(E_i, !E_k, E_j) \Longrightarrow$	remove the results from $AND\_NEG$ operator	$C_{O_{and}}^i + C_{O_{and}}^o$	$C_{Q_{and}}^{o} + C_{Q_{and}}^{o} \times (1 -$
$NEG(AND(E_i, E_j), !E_k)$	where $e_k$ of $E_k$ appears between $E_i$ and $E_j$	- unu - unu	$ \begin{vmatrix} C_{O_{and}}^{o} + C_{O_{and}}^{o} \times (1 - P_{E_{i}, E_{k}}^{t} \times P_{E_{k}, E_{j}}^{t} - P_{E_{j}, E_{k}}^{t} \times \end{vmatrix} $
			$P_{E_k,E_i}^t) \times P_{E_i,E_j}^t$

such that  $\forall k, Total\ Cost(G_{opt}) \leq Total\ Cost(G_k)$  defined in Definition 12.

A candidate  $P_k$  must satisfy the following constraints:

**Constraint 1:** Each  $PT_{q_t}$  in  $P_k$  satisfies the relationship with provisioned processing query in terms of Definitions 8, 9 and 10:  $\forall \ PT_{q_t} \in P_k$ ,  $\exists \ q_j$  such that  $PT_{q_j} \subset_P PT_{q_t}$  or  $PT_{q_t} \subset_C PT_{q_j}$  or  $PT_{q_j} \subset_O PT_{q_t}$ ;

**Constraint 2:** Those expressions or sub-expressions are non-identical:  $\forall (PT_{q_t}, PT_{q_r} \in P_k), \exists PT_{q_t} \neq PT_{q_r}.$ 

In order to avoid exponential complexity of search space, we design a novel iterative refinement methodology adopting a cost-based heuristic for finding a good quality solution within reasonable time rather than enumerating entire search space. When processing query  $q_j$ , the optimized query execution plan-finder performs as follows:

#### Phase 1: Ordering and clustering candidate plans.

This phase first sorts candidate plans in ascending order according to the number of operators corresponding to  $P_k$ , denoted as  $PL_{P_k}$ , then clusters the candidate query execution plan  $P_k$  with the same and smallest number of operators as a set of  $P^s$ .

# Phase 2: Estimating candidate plans' costs by the IDAG cost model.

On the context of Phase 1, we can search a small group space rather than enumerating all possible expressions or sub-expressions of queries. Then, we can estimate the costs of those candidate plans in  $P^s$  by the IDAG cost model as (4). We assume there exists at least one candidate plan in  $P^s$ . The reason for choosing  $P_k$  with the smallest number of operators to process given queries is that the less number of operators is used to perform query  $q_j$ , the less total cost will be consumed, because using more operators for processing the same nested pattern queries will result in the increase of the total cost according to the IDAG cost model described above.

# Phase 3: Searching an optimized query execution plan based on the IDAG cost model.

In general, we can find an optimized query execution plan  $P_{opt}$ , and the total cost of its IDAG such that  $Total\ Cost(G_{opt}) \leq Total\ Cost(G_k)$ .

Theorem 1: For a given set of queries, if all sub DAG

Algorithm 1. Nested query pattern-based reuse scheme

```
\begin{array}{lll} \textbf{Input:} & P_{opt} \colon \text{a set of } \{PT_{q_1}, \ldots, PT_{q_t}, \ldots, PT_{q_r}\} \text{ where each } \\ & PT_{q_t} \text{ in } P_{opt} \text{ has relationship with } q_j \text{ based on NQPH model}; \\ & R_{PT_{q_t}} \colon \text{the results of } PT_{q_t}; \\ \textbf{Output:} Num \ R_{PT_{q_t}} \colon \text{the replicas number of } R_{PT_{q_t}}; \\ \textbf{1 for each } PT_{q_t} \text{ in } P_{opt} \\ \textbf{2} & Num \ R_{PT_{q_t}} + +; \\ \textbf{3 end for} \\ \textbf{4 for } PT_{q_t} = \text{EPQ}(E_h, \ldots, E_{hp}, \ldots, E_{hpf}) \in q_j \text{ and } \not\in PT_{q_i} \\ \textbf{5} & \text{preparing for computing } PT_{q_t} \text{ by efficient stack-based join;} \\ \textbf{6} & \textit{//assuming joining events between } PT_{q_r} \text{ and } PT_{q_t} \text{ are sorted and pointers exist} \\ \textbf{7} & \text{if EPQ}(E_h, \ldots, E_{hp}, \ldots, E_{hpf}) \text{ is followed by } PT_{q_r} \\ \textbf{8} & q_j = \text{EPQ}(E_h, \ldots, E_{hp}, \ldots, E_{hpf}, PT_{q_r}); \\ \textbf{9} & \text{else } PT_{q_r} \text{ is followed by EPQ}(E_h, \ldots, E_{hp}, \ldots, E_{hpf});} \\ \textbf{10} & q_j = \text{EPQ}(PT_{q_r}, E_h, \ldots, E_{hp}, \ldots, E_{hpf});} \\ \textbf{11 end for} \end{array}
```

#### Algorithm 2. Nested query concept-based reuse scheme

plans  $G_k$  in G is optimal for their corresponding expressions or sub-expressions as well, then an IDAG G must be optimal.

**Proof:** We prove this by contradiction. Suppose the theorem is not true; then it should be possible to find an IDAG G' with lower cost than G, but with the same output cardinality. Using G' as a substitute for G, we would then obtain the sub DAG plans  $G'_k$  with lower total cost for their corresponding expressions or sub-expressions, which contradicts the assumption that  $G_k$  is optimal.

#### B. The Algorithms of Reuse Schemes

In this subsection, we design three reuse schemes to alternatively get the replicas number of common sub-expressions

```
Algorithm 3. Operator type-based reuse scheme
```

```
 \begin{array}{lll} \textbf{Input:} & P_{opt} \text{: a set of } \{PT_{q_1}, \ldots, PT_{q_t}, \ldots, PT_{q_r}\} \text{ where each } \\ & PT_{q_t} \text{ in } P_{opt} \text{ has relationship with } q_j \text{ based on OTH model; } \\ & R_{PT_{q_t}} \text{: the results of } PT_{q_t}; \\ \textbf{Output:} Num \ R_{PT_{q_t}} \text{: the replicas number of } R_{PT_{q_t}}; \\ 1 & \text{for each } PT_{q_t} \text{ in } P_{opt} \\ 2 & Num \ R_{PT_{q_t}} + +; \\ 3 & \text{end for} \end{array}
```

and prepare for computing the rest of sub-expression for the query needed. They are nested query pattern-based reuse scheme (NQPRS), nested query concept-based reuse scheme (NQCRS), and operator type-based reuse scheme (OTRS). The pseudocodes of them are shown in Algorithms 1, 2 and 3, respectively.

In Algorithm 1, given an optimized query execution plan  $P_{opt}$ , we first update the value of  $Num\ R_{PT_{q_{t}}}$  for each  $PT_{q_t}$  in  $P_{opt}$  (lines 1-3), then prepare for computing sub-expression  $PT_{q_t} = \text{EPQ}(E_h, ..., E_{hp}, ..., E_{hpf})$  that belongs to  $q_i$  but is not captured by  $PT_{q_i}$ . Based on different conditions (lines 7 and 9),  $q_i$  can be formed by using EPQ(·) to join  $PT_{q_r}$  with  $PT_{q_t}$  as  $EPQ(E_h, ..., E_{hp}, ..., E_{hpf},$  $PT_{q_r}$ ) or  $EPQ(PT_{q_r}, E_h, ..., E_{hp}, ..., E_{hpf})$  (lines 4-11). In Algorithm 2, we first update the value of  $Num R_{PT_{g_{+}}}$  for each  $PT_{q_t}$  in  $P_{opt}$  (lines 1-3), then prepare for computing sub-expression  $PT_{q_t} = \text{EPQ}(E_{ap}, \ldots, E_{bp}, \ldots, E_{cp})$  that belongs to  $q_j$  but is not captured by  $PT_{q_i}$  (lines 4-7).  $q_j$ can be formed by merging  $PT_{q_r}$  with  $PT_{q_t}$ . In Algorithm 3, because we try to reuse coarser level query's replicate results to generate finer level query by filtering some data that are not captured by the finer level query, there is no rest subexpression that needs to be prepared. Hence, we just need to update the value of  $Num\ R_{PT_{q_t}}$  for each  $PT_{q_t}$  in  $P_{opt}$ (lines 1-3).

#### C. The MQOS Algorithm

Through integrating the optimized query execution planfind approach with the three reuse schemes described in the above two subsections, respectively, we present here a multi-query optimization strategy (MQOS). MQOS is to produce query results quickly and improve computational efficiency by exploiting not only common sub-expressions among nested event pattern queries, but also replicas of the appropriate common operators' results for the queries needed. The steps of MQOS Algorithm are as follows (Algorithm 4):

#### Phase 1: Ordering queries.

This phase first sorts queries in ascending order based on the number of their positive event types in terms of NQPH. Next, this phase orders the queries with the same number of positive event types from finer level to coarser level in terms of NQCH. Then, this phase orders the queries with the same positive event types from coarser level to finer level in terms of OTH. The reason is that a query's results from

Algorithm 4. Multi-query optimization strategy

```
1 //Phase 1: Ordering Queries
   ordering queries in terms of NQPH, NQPH and OTH, then getting
   //Phase 2: Setting expressions or sub-expressions of queries
    for the optimized query execution plan-finder
   listing \{PT_{q_1}, \ldots, PT_{q_i}\} which are the most finer, and coarser
    level of provisioned queries in trems of NQCH, NQPH and OTH,
    then computing each PT_{q_i} and recording its intermediate operators
   //Phase 3: Processing the provisioned queries
   for j=1,\ldots,\hbar //classify provisioned query
       invoking the optimized query execution plan-finder to get
       \begin{array}{l} P_{opt} = \{PT_{q_1}, \ldots, PT_{q_t}, \ldots, PT_{q_r}\} \\ \text{if } \forall \ PT_{q_t} \in P_{opt}, \ \exists \ PT_{q_j} \subset_P \ PT_{q_t} \ \text{//satisfy NQPH} \end{array}
8
          invoking Algorithm 1;
10
       if \forall PT_{q_t} \in P_{opt}, \exists PT_{q_t} \subset_C PT_{q_j} //satisfy NQCH
          invoking Algorithm 2;
11
       if \forall PT_{q_t} \in P_{opt}, \exists PT_{q_i} \subset_O PT_{q_t} //satisfy OTH
12
          invoking Algorithm 3;
13
14
       else
           for each PT_{q_t} in P_{opt}
15
              Num \ R_{PT_{q_t}} + +;
16
17
          for PT_{q_j} \subset_P PT_{q_t}, and PT_{q_t} = \text{EPQ}(E_h, \ldots, E_{hp}, \ldots, E_{hpf}) \in q_j and \not\in PT_{q_i} //satisfy NQPH
18
              preparing for computing PT_{q_t} by efficient stack-based join; if PT_{q_t} is followed by PT_{q_r}
19
20
21
                     PT_{q_j} = \text{EPQ}(E_h, \ldots, E_{hp}, \ldots, E_{hpf}, PT_{q_r});
                 else PT_{q_r} is followed by PT_{q_t}
22
23
                      PT_{q_i} = \text{EPQ}(PT_{q_r}, E_h, ..., E_{hp}, ..., E_{hpf});
24
25
          for PT_{q_t} \subset_C PT_{q_j}, and PT_{q_t} = \text{EPQ}(E_{ap}, \ldots, E_{bp}, \ldots, E_{cp}) \in q_j and \not\in PT_{q_i} //satisfy NQCH
26
             preparing for computing PT_{q_t} by efficient stack-based join; PT_{q_j} is formed by merging PT_{q_r} with \mathrm{EPQ}(E_{ap},\ldots,E_{bp},
27
          end for
       updating \{PT_{q_1}, ..., PT_{q_i}\} by adding new ones into it
29
30 end for
31 storing Num\ R_{PT_{q_t}} in optArray;
32 parallel processing multiple queries by Num R_{PT_{q_{+}}}'s in optArray
```

coarser level in NQPH and OTH can be reused for a query from finer level, while a query's results with finer level event types in NQCH can be reused for a query with coarser level event types. After that, we get an ordered set of queries  $Q = \{q_1, \ldots, q_i, \ldots, q_h\}$  (lines 1-2).

# Phase 2: Setting expressions or sub-expressions of queries for the optimized query execution plan-finder.

This phase lists the expressions or sub-expressions of queries  $\{PT_{q_1}, \ldots, PT_{q_i}\}$  which are the most finer, and coarser level of provisioned queries in terms of NQCH, NQPH and OTH alternatively. Then, this phase computes those expressions or sub-expressions of queries by efficient stack-based join [13] and records intermediate operators that belong to the set of operators corresponding to  $\{PT_{q_1}, \ldots, PT_{q_i}\}$ . The purpose is to provide a set of expressions or sub-expressions of queries for next phase to find an optimized query execution plan that can be used to perform the provisioned query  $q_i$  (lines 3-4).

Phase 3: Processing the provisioned queries.

Table III PARAMETERS FOR EVENT GENERATION

Parameter	Values
$R_{E_i}$	10 <sup>2</sup> -10 <sup>5</sup> tuples/sec
$TW_p$	10 -10 <sup>10</sup> sec
$P_{E_i,E_j}^t$	1/2
$P_{E_i,E_i}$	1

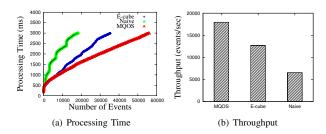


Figure 8. Workload 1 with pure SEQ pattern queries under NQPH and NQCH variations.

This phase goes through the ordered list of provisioned queries and iteratively processes them to an optimized query execution plan for given queries. We handle the ordered queries in Q iteratively. For j = 1, based on the IDAG cost estimation model (Subsection V-A), this phase tries to find an optimized query execution plan  $P_{opt}$  for generating  $q_j$ in terms of  $\{PT_{q_1}, ..., PT_{q_i}\}$  (line 7). Henceforth, we can find an optimized plan  $P_{opt} = \{PT_{q_1}, ..., PT_{q_t}, ..., PT_{q_r}\}$ with the minimum cost of operators and communications. If each  $PT_{q_t}$  in  $P_{opt}$  satisfies the NQPH, NQCH or OTH with query  $q_j$ , the system will invoke Algorithm 1, 2 or 3, respectively, to get  $Num\ R_{PT_{q_t}}$  and prepare for computing the sub-expression that belongs to  $q_j$  but is not captured by  $PT_{q_i}$  (lines 8-9, 10-11, or 12-13, respectively). If the subsets of  $P_{opt}$  do not meet the above conditions, the system updates  $Num R_{PT_{q_t}}$  for each  $PT_{q_t}$  in  $P_{opt}$  (lines 14-16) and prepares for computing the sub-expression that belongs to  $q_i$  but is not captured by  $PT_{q_i}$  based on NQPH or NQCH models (lines 18-28). Afterwards, the system updates expressions or sub-expressions of queries  $\{PT_{q_1}, ..., PT_{q_i}\}$ by adding new ones into it (line 29). Finally,  $Num R_{PT_{g_*}}$  is stored in optArray (line 31) and the system processes the given nested pattern queries over multi-dimensional event streams by the final optimized query execution plan, namely, Num  $R_{PT_{q_t}}$ 's in optArray (line 32).

#### VI. EXPERIMENTAL EVALUATION

By comparing MQOS with related approaches under different workload conditions alternately, we demonstrate the superiority and performance of our proposal. We implemented all approaches within StreamBase system [9]. We ran the experiments on an Intel®Core<sup>TM</sup>duo CPU 3.33 GHz and 12.00 GB main memory. In each stream, we set stock ticker, timestamp and price information attributes. We define

the processing time as the difference between the system time of the number of events output and the system time to process initial event contributing to the output. Table III summarizes the main parameters for event generation. We set the parameters and representative query workloads 1-3 shown in Fig. 1 based on [18], [12], [15].

# A. Comparing over Pure SEQ Pattern Queries with NQPH and NQCH Variations

In this experiment, we evaluated query workload 1 with query pattern and query concept variations. Because E-cube is currently the most efficient method to treat with pure SEQ pattern queries under NQPH and NQCH variations, we attempt to compare MQOS with E-cube and Naive methods meanwhile. E-cube [18] is a kind of reuse-based scheme, that is, sharing query' results among given pure SEQ pattern queries. Naive [13] processes queries independently using stack-based query evaluation. Here, we set time window size of each operator as 10 sec and each input rate as 1000 tuples/sec.

Fig. 8 shows the processing time and throughput of the three methods, respectively. We observe that MQOS and E-cube generate results faster than Naive, because they avoid results re-computation by applying conditional computation. We also notice the speedup of MQOS over E-cube. The reason is that MQOS not only avoids query result re-computation, but also processes given queries by reusing common operators' results. In addition, because of cardinality of operator's output within  $TW_p$ , the relationship between the number of events and processing time is nonlinear and, exactly, quadratic when processing time is less than time window size.

Specifically,  $q_2$  can be performed by processing replicate results of  $q_1$ . The sub-expression of  $q_3$ 's results can be replicated and reused for performing  $q_4$  by processing replicate results from SEQ(Medicine, DELL) operator. The results of sub-expression of  $q_1$  and  $q_4$  can be reused for query  $q_5$ by processing replicate results from SEQ(HTB, EDU) and SEQ(Medicine, Computer) operators, respectively. However, when performing queries  $q_4$  and  $q_5$ , E-cube introduced extra delay due to removing partial event types from given queries and eliminating duplicated tuples, in order to satisfy the requirements of processing next queries. Consequently, MQOS used 9 operators, i.e., 7 SEQ, 1 SEQ\_NEG and 1 UNION operators, E-cube used 15 operators, i.e., 7 SEQ, 1 SEQ\_NEG, 3 MAP (removing event type KME from  $q_3$ , MBA from  $q_1$  and Metal from  $q_4$ ), 3 FILTER (filtering the duplicate tuples caused by MAP operator) and 1 UNION operators, while Naive used 12 operators, i.e., 11 SEQ and 1 SEQ NEG operators for processing the given queries.

#### B. Varying Time Window Sizes of Operators

In this experiment, we examined the effect of time window sizes of operators for MQOS, E-cube and Naive on

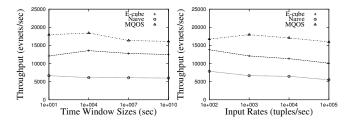


Figure 9. Varying time window Figure 10. Varying input rates. sizes.

throughput based on Workload 1. We fixed each input rate as 1000 tuples/sec, and varied time window size from 10 up to  $10^{10}$  sec.

The results are shown in Fig. 9. The throughput of MQOS is higher than the others no matter the time window size. As we set time window sizes from  $10 \text{ to } 10^4 \text{ sec}$ , MQOS and E-cube can treat with queries more efficiently than Naive. However, when increasing time window sizes from  $10^4$  to  $10^{10}$  sec, the runtime stack grows large, causing memory overhead so that the throughput of MQOS and E-cube decrease. Whereas, Naive cannot handle with the input rate variation as it increases from  $10 \text{ up to } 10^{10} \text{ tuples/sec}$ . Consequently, we concluded that MQOS outperforms E-cube and Naive even under time window sizes variation.

#### C. Varying Input Rates of Streams

In this experiment, we examined the effect of input rate of streams for MQOS, E-cube and Naive on throughput based on Workload 1. We fixed time window size of operators as 10 sec, and varied input rate of streams from  $10^2 \text{ up to } 10^5 \text{ tuples/sec}$ .

The results are shown in Fig. 10, and the throughput of MQOS is more higher than the others as the variation of input rates. We can notice that as we set input rate of streams from  $10^2$  up to  $10^3$  tuples/sec, MQOS can treat with queries more efficiently than E-cube and Naive. As the input rate of streams vary from  $10^3$  up to  $10^5$  tuples/sec, the throughput of MQOS is decreasing. The reason is that when the input rate of streams are increased too much, the runtime stack grows large resulting in memory overhead so that the throughput of MQOS decreases. On the other hand, E-cube and Naive cannot handle with the input rate variation as it increases from  $10^2$  up to  $10^5$  tuples/sec. Consequently, we concluded that MQOS outperforms E-cube and Naive even under input rates variation.

### D. Comparing over Nested Pattern Queries with OTH Variation

In this experiment, we evaluated query workload 2 with only operator type variation. Since there are no related approaches that makes study of relationship among different operator types, we compare MQOS with Middle-to-both-sides which comes from part of our work, and Naive mean-

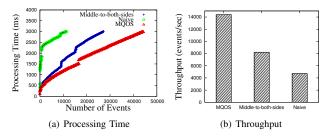


Figure 11. Workload 2 with nested pattern queries under OTH variation.

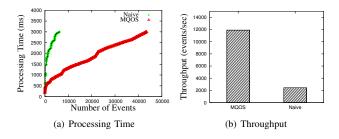


Figure 12. Workload 3 with nested pattern queries under triaxial mixed variation.

while. Based on OTH model, Middle-to-both-sides means  $SEQ(\cdot)$  query will be processed first, then, its results are reused for  $AND(SEQ(\cdot))$  and  $NEG(SEQ(\cdot))$  queries, as shown in Fig. 6. Here, we set time window size of each operator as 10 sec and each input rate as 1000 tuples/sec.

Fig. 11 shows the processing time and throughput of the three methods, respectively. We observe that MQOS and Middle-to-both-sides generate results faster than Naive, because they avoid result re-computation. We also observe that MQOS produces results faster than Middle-to-bothsides. This is because MQOS uses Top-to-down method, namely,  $AND(SEQ(\cdot))$  query will be processed first, then, its results can be reused for  $SEQ(\cdot)$  query, whose results in turn can be reused for  $NEG(SEQ(\cdot))$  query. Specifically, AND operator of  $q_6$  does not care about the sequence of event types so that it can output more results than SEQ operator of  $q_7$ . Then, the results of  $q_6$  can be replicated and reused for  $q_7$ . After that, we can perform  $q_8$  by processing replicate results from  $q_7$ . On the contrary, because SEQ operator is related to the sequence of event types, it has implicit time predicate described in Subsection V-A. Consequently, Middle-to-both-sides works worse than MQOS.

# E. Comparing over Nested Pattern Queries with Triaxial Mixed Variation

In this experiment, we evaluated a query workload 3 involving nested query pattern, nested query concept and operator type variations. Due to the complex of workload 3, there are no existing methods to efficiently treat with it under nested query pattern, nested query concept and operator

type variations. We therefore attempt to compare MQOS with Naive method. Here, we set time window size of each operator as 10 sec and each input rate as 1000 tuples/sec.

Fig. 12 shows the processing time and throughput of the two methods. As expected, MQOS outperforms Naive. On closer analysis in MQOS in terms of workload 3, because the results of  $q_9$  cannot be reused for query  $q_{13}$ ,  $q_9$  and  $q_{13}$  should be executed in parallel first. Next, the results of  $q_9$  can be replicated and reused for performing  $q_{10}$ . Then, the results of  $q_{10}$  can be replicated and reused for  $q_{11}$  by adding predicate "!" and  $q_{12}$  can be performed by joining event type INTC with replicate results from  $q_{10}$  by  $AND(\cdot)$  operator. The results of  $q_{14}$  can be generated by joining the sub-expression of  $q_{13}$ 's results, i.e., SEQ(Finance, Metal) with replicate results from  $q_9$  by  $SEQ(\cdot)$  operator. On the other hand, the replicate results of  $q_{13}$  can be reused for  $q_{15}$  and  $q_{16}$  in parallel.

#### VII. CONCLUSIONS

MQOS integrates OLAP with CEP functionalities for realizing (i) technologies that allow users to efficiently query large amounts of event stream data in multi-dimensions where each of which may be at different levels of abstraction, and (ii) technologies that allow CEP systems to process nested pattern queries by leveraging appropriate replicas of common operators' results. The experimental results showed that MQOS has faster processing time and higher throughput than E-cube, Naive and Middle-to-both-sides methods. In addition, the performance of MQOS keeps better than that of E-cube when varying time window sizes of operators or input rates of streams. Interesting future work includes considering optimizing nested pattern queries over live and archived multi-dimensional event streams.

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