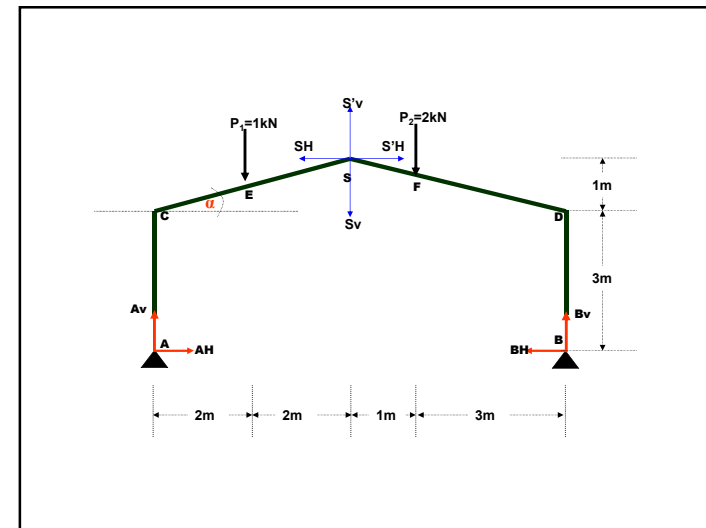


**ANALISIS STRUKTUR II**

  
**WPTS DENGAN SISI ATAS MIRING**

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**Reaksi  $\sum MB = 0$**

**$AV \cdot 8 - P_1 \cdot 6 - P_2 \cdot 3 = 0$**  (*AV dimisalkan ke atas*)

$$A_v = \frac{1.6 + 2.3}{8} = 1,5 \text{ kN (ke atas)}$$

**$\sum MA = 0$**

**$-BV \cdot 8 + P_1 \cdot 2 + P_2 \cdot 5 = 0$**  (*BV dimisalkan ke atas*)

$$B_v = \frac{1.2 + 2.5}{8} = 1,5 \text{ kN (ke atas)}$$

**Bagian kiri (ACES),**

**$\sum Ms = 0$**

**$AV \cdot 4 - AH \cdot 4 - P_1 \cdot 2 = 0$**  (*AH dimisalkan ke kanan*)

$$A_H = \frac{(1.5)4 - 1.2}{4} = 1 \text{ kN (ke kanan)}$$

**$\sum Mc = 0$**

**$-A_H \cdot 3 + P_1 \cdot 2 + S_v \cdot 4 - S_H \cdot 1 = 0$**  (*Misal Sv ke bawah dan SH ke kiri*)

$$4 S_v - S_H = A_H \cdot 3 - P_1 \cdot 2$$

$$4 S_v - S_H = 1 \cdot 3 - 1 \cdot 2$$

$$4 S_v - S_H = 1 \quad \text{..... (1)}$$


**$\sum MA = 0$**


**$P_1 \cdot 2 - S_H \cdot 4 + S_v \cdot 4 = 0$**


$$4 S_v - 4 S_H = -1 \cdot 2$$

$$4 S_v - 4 S_H = -2 \quad \text{..... (2)}$$

$$\begin{array}{rcl} \text{(1)} & 4 S_v - S_H & = 1 \\ \text{(2)} & 4 S_v - 4 S_H & = -2 \quad (-) \\ \hline & 3 S_H & = 3 \rightarrow S_H = 1 \text{ kN (ke kiri)} \end{array}$$

 (1)  $4 S_v - S_H = 1$   
 $4 S_v - 1 = 1 \Rightarrow 4 \cdot S_v = 2 \text{ kN}$   
 $\Rightarrow S_v = 0.5 \text{ kN}$  (ke Bawah)

 **Bagian kanan (SFDB)**  
 $\sum M_s = 0$   
 $-B_v \cdot 4 + B_H \cdot 4 + P_2 \cdot 1 = 0$  (Misal  $B_H$  dimisalkan ke kiri)  
 $B_H = \frac{(1,5)4 - 2 \cdot 1}{4} = 1 \text{ kN}$  (ke kiri)  
 $\sum M_D = 0$   
 $-S_v' \cdot 4 + S_H' \cdot 1 - P_2 \cdot 3 + B_H \cdot 3 = 0$  (misal  $S_v'$  ke atas &  $S_H'$  ke kanan)  
 $4 S_v' + S_H' = P_2 \cdot 3 - B_H \cdot 3$   
 $4 S_v' + S_H' = 2 \cdot 3 - 1 \cdot 3$   
 $4 S_v' + S_H' = 3$  ..... (1)



$\sum M_B = 0;$   
 $S_v' \cdot 4 + S_H' \cdot 4 - P_2 \cdot 3 = 0$   
 $4 S_v' + 4 S_H' = 2 \cdot 3$   
 $4 S_v' - 4 S_H' = 6$  ..... (2)

(1)  $4 S_v' + S_H' = 3$   
 (2)  $4 S_v' + 4 S_H' = 6$  (-)  
 $-3 S_H' = -3 \rightarrow S_H' = 1 \text{ kN}$  (ke kanan)

(1)  $4 S_v' + S_H' = 3$   
 $4 S_v' + 1 = 3$   
 $S_v' = 1/4 \cdot 2 = 0,5 \text{ KN}$  (ke atas)

**BENDING MOMENT DIAGRAM**

$M_C = -A_H \cdot 3 = -1 \cdot 3 = -3 \text{ kNm}$   
 $M_E = -A_H \cdot (3,5) + A_v \cdot 2$   
 $= -1 \cdot (3,5) + (1,5) \cdot 2 = -0,5 \text{ kNm}$   
 $M_D = -B_H \cdot 3$   
 $= -1 \cdot 3 = -3 \text{ kNm}$   
 $M_F = -B_H \cdot (3,75) + B_v \cdot 3$   
 $= -1 \cdot (3,75) + 1,5 \cdot 3 = 0,75 \text{ kNm}$

**Bila  $M_E$  dan  $M_F$  dihitung dari sendi S**

$M_E = -S_v' \cdot 2 + S_H' \cdot 0,5 = -0,5 \cdot 2 + 1 \cdot 0,5 = -0,5 \text{ kNm}$   
 $M_F = S_v' \cdot 1 + S_H' \cdot 0,25 = 0,5 \cdot 1 + 1 \cdot 0,25 = 0,75 \text{ kNm}$

**BIDANG D DAN N**

**Gaya Melintang dan Gaya Normal**

**Pada TITIK A**  
 $D_A = -A_H = 1 \text{ KN}, N_A = -A_v = -1,5 \text{ KN}$

**Pada TITIK C (Batang AC),**  
 $D_C = -S_H = -1 \text{ KN}, N_C = -P_1 - S_v = -1 - 0,5 = -1,5 \text{ KN}$

**Pada TITIK C (Batang CS),**

$A_v = 1,5 \text{ KN}$

$Tg \alpha = 1/4$   
 $\alpha = 14^\circ 2' 10''$

**Dc =  $A_v \cdot \cos \alpha - A_h \cdot \sin \alpha$**   
 $D_c = (1,5) \cdot \cos \alpha - (1) \cdot \sin \alpha$

$D_c = 1,455 - 0,242 = 1,213 \text{ KN}$

**Nc =  $-A_v \cdot \sin \alpha - A_h \cdot \cos \alpha$**   
 $N_c = (-1,5) \cdot \sin \alpha - (1) \cdot \cos \alpha$   
 $N_c = -0,364 - 0,970 = -1,334 \text{ KN}$

**Pada TITIK E**

$P_1 = 1 \text{ KN}$

**BIDANG D DAN N**

**D<sub>E</sub> kiri = D<sub>C</sub> batang CS = 1,213 KN**  
 $D_{E \text{ kn}} = D_{E \text{ kiri}} - P_1 \cdot \cos \alpha$   
 $= 1,213 - 0,970 = 0,243 \text{ kN}$

**N<sub>E</sub> kr = N<sub>C</sub> balok CS = -1,334 KN**  
 $N_{E \text{ kn}} = N_{E \text{ kr}} + P_1 \cdot \sin \alpha$   
 $= -1,334 + 0,242 = -1,092 \text{ KN}$

**Pada Titik S**

**D<sub>S</sub> kr = D<sub>E</sub> kn = 0,243 KN ;**  
 $N_{S \text{ kr}} = N_{E \text{ kn}} = -1,092 \text{ KN}$

**Dapat juga dihitung dari gaya yang bekerja pada sendi S:**

**Pada TITIK S**

$S_h = 1$

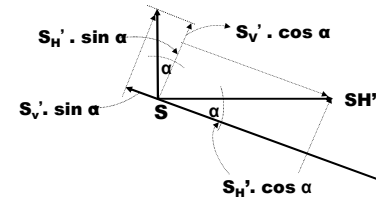
**D<sub>S</sub> kr = S<sub>v</sub> · Cos α – S<sub>h</sub> · Sin α**  
 $D_{S \text{ kr}} = (0,5) \cos \alpha - (1) \cdot \sin \alpha$   
 $D_{S \text{ kr}} = 0,485 - 0,242 = 0,243 \text{ KN}$

### GAYA NORMAL (N)

$$\begin{aligned}
 N_S \text{ kr} &= -S_v \cdot \sin \alpha - S_H \cdot \cos \alpha \\
 N_S \text{ kr} &= - (0,5) \sin \alpha - (1) \cos \alpha \\
 N_S \text{ kr} &= - 0,121 - 0,970 = - 1,091 \text{ KN}
 \end{aligned}$$

Ada sedikit perbedaan dari hasil hitungan D dan N pada titik S, tapi perbedaan ini kecil, yang diakibatkan oleh pembulatan dalam hitungan

### Pada TITIK S (batang SD),

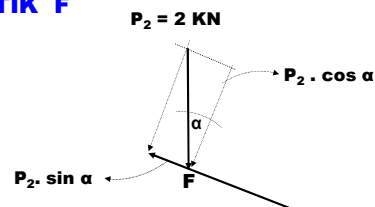


$$\begin{aligned}
 D_S \text{ kn} &= S_v' \cdot \cos \alpha + S_H' \cdot \sin \alpha \\
 D_S \text{ kn} &= (0,5) \cos \alpha + (1) \cdot \sin \alpha \\
 D_S \text{ kn} &= 0,485 + 0,242 = 0,727 \text{ KN}
 \end{aligned}$$

### GAYA NORMAL (N)

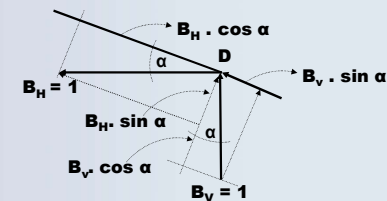
$$\begin{aligned}
 N_S \text{ kn} &= -S_v' \cdot \cos \alpha + S_H' \cdot \sin \alpha \\
 N_S \text{ kn} &= - (1) \cos \alpha + (0,5) \sin \alpha \\
 N_S \text{ kn} &= - 0,970 + (0,121) = -0,849 \text{ KN}
 \end{aligned}$$

### Pada TITIK F



### BIDANG D DAN N

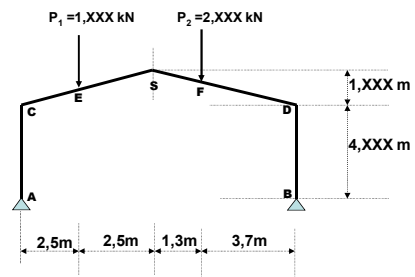
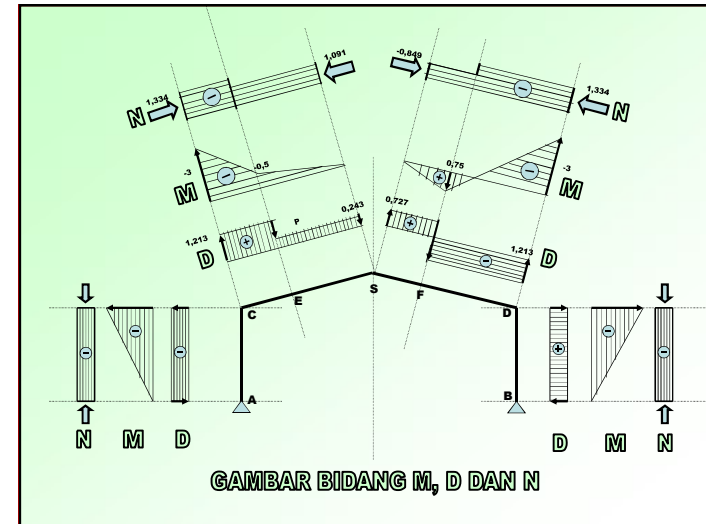
$$\begin{aligned}
 D_F \text{ kr} &= D_S \text{ kn} = 0,727 \text{ KN} \\
 D_F \text{ kn} &= D_F \text{ kr} - P_2 \cdot \cos \alpha \\
 D_F \text{ kn} &= 0,727 - 1,940 = - 1,213 \text{ KN} \\
 N_F \text{ kr} &= N_S \text{ kn} = - 0,849 \text{ KN} \\
 N_F \text{ kn} &= N_F \text{ kr} - P_2 \sin \alpha \\
 &= - 0,849 - 0,485 = - 1,334 \text{ KN}
 \end{aligned}$$



$D_D \text{ kr} = -B_v \cos \alpha + B_H \sin \alpha$   
 $D_D \text{ kr} = - (1,5) \cos \alpha + (1) \sin \alpha$   
 $D_D \text{ kr} = -1,445 + 0,242 = -1,212 \text{ KN}$

$N_D \text{ kr} = -B_v \sin \alpha - B_H \cos \alpha$   
 $N_F \text{ kn} = - (1,5) \sin \alpha - (1) \cos \alpha$   
 $= -0,364 - 0,970 = -1,334 \text{ KN}$

**PENGAMBARAN BIDANG D, M DAN N**



**HITUNG DAN GAMBARKAN BMD, SFD, NFD, deformed shaped, geometri**  
**Output excel.**  
**Manual**

**SOAL**

