

1) Internet Routing: OSPF or connecting the dots Value (15)

Given: Phase I Neighbour Identification Information,  $R_i$  is a router  $Net_i$  is a network lan.

$R_1$  neighbours  $R_2 R_3$

$R_2$  neighbours  $R_1 R_5 Net_1$

$R_3$  neighbours  $R_1 R_4 R_6 Net_4$

$R_4$  neighbours  $R_3 R_5$

$R_5$  neighbours  $R_1 R_2 R_4 R_6 R_8$

$R_6$  neighbours  $R_3 R_7 R_9$

$R_7$  neighbours  $R_6 R_8 R_9 R_{10}$

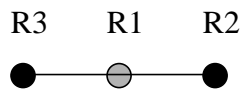
$R_8$  neighbours  $R_5 R_7 R_{10} Net_3$

$R_9$  neighbours  $R_6 R_7 Net_2$

$R_{10}$  neighbours  $R_7 R_8$

Phase I: For each router  $R_i$  draw its neighbours.

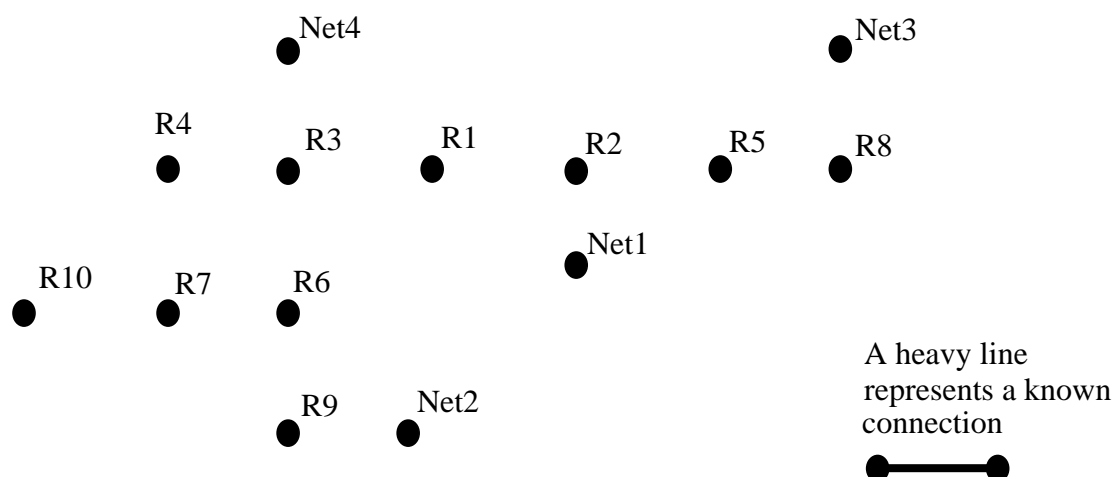
e.g.



A heavy line represents a known connection

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Phase II: Continued exchange of router connectivity. Draw the connectivity graph from R1's perspective.



From the graph of the network developed, what is the routing table for R1? Assume all edges equal weight.

What does the routing network look like from R9's perspective?

What is the routing table for R9?

2)Diffie Hellboy key exchange and ElGamal public key crypto. (15)

Part i) Diffie Hellboy (DH) key exchange.

You want to send Alice a secret 7 bit BES (Bob's encryption standard) key 1010101.

For this you are going to use DH, and decide together on the numbers  $g$  and  $n$ . ( $g=2$ ,  $n=127$ ).

You pick  $x=12$  your secret number, Alice picks  $y=5$  as her secret number.

You calculate  $2^{12} \bmod 127 = X$ , Alice calculate  $2^5 \bmod 127 = Y$ . What are  $X$  and  $Y$ ?

Exchange  $X$  and  $Y$ .

Alice calculates  $k = X^5 \bmod 127$ . What is  $k$ ?

You calculate  $k' = Y^{12} \bmod 127$ . What is  $k'$ ?

How would you use  $k$  to securely encode and send the BES key?

How would Alice decrypt the BES key?

If Eve intercepted  $g$ ,  $n$ , and  $X$ , what would she need to do to break the security of DH.

2 Part ii) ElGamal is a public key system closely related to DH key exchange. You want to send Alice the message  $m=43$ . Go through the same DH key exchange process up but not including the X,Y exchange.

Alice posts Y as her public key.

You create a cipher text c by multiplying the message by Y exponentiated by x all mod 127.

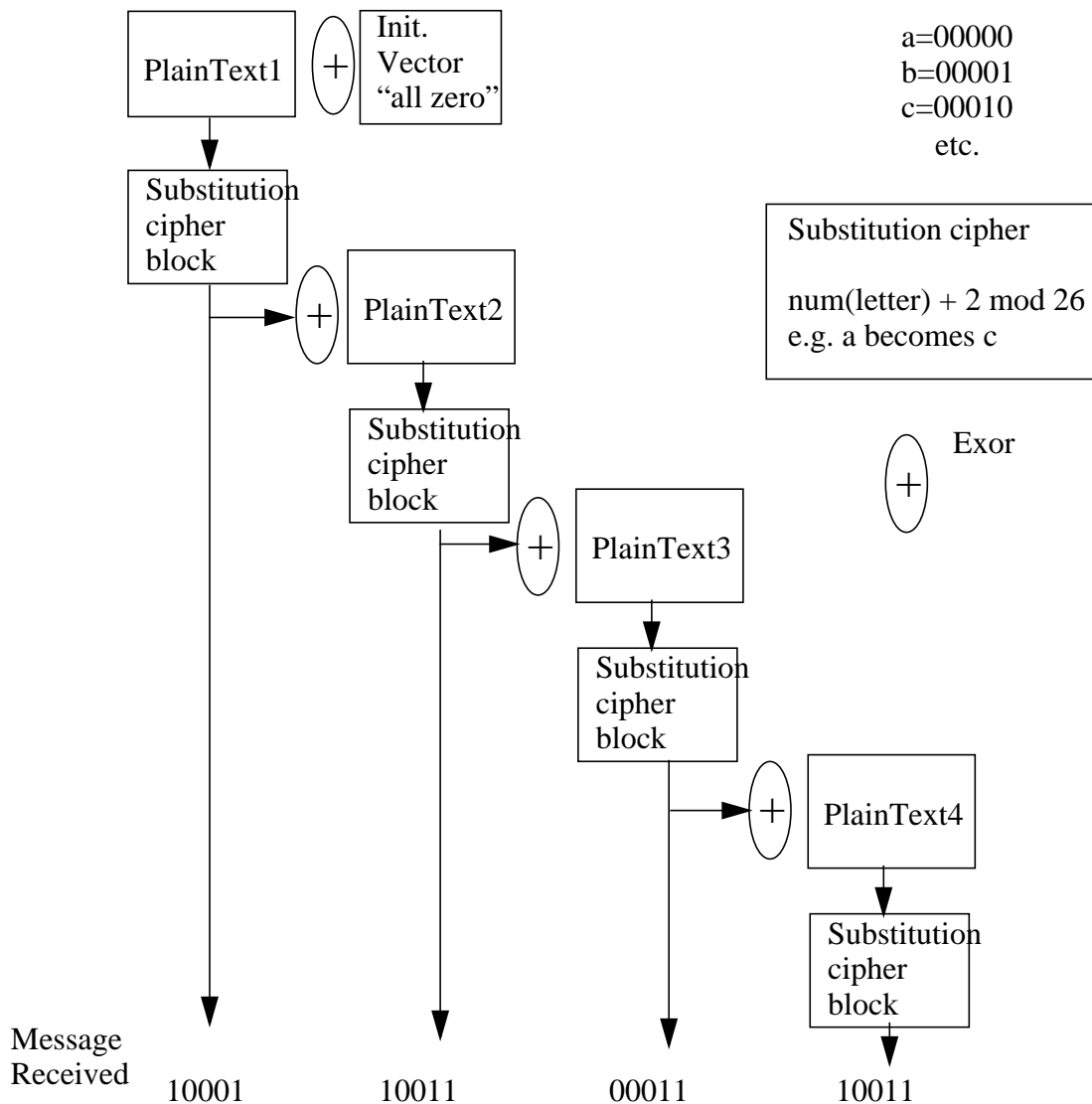
That is,  $c = m Y^x \text{ mod } 127$  and send it to Alice along with X. What is c?

Alice decrypts the cipher  $m' = c X^{-y} \text{ mod } 127$ . Expand out  $m'$  and illustrate mathematically (symbolically) why  $m'=m$ .

What is the largest message (number of bits) that can be sent in the example above.

**Bonus:** In this example what is  $-y$ , or rather how would you calculate  $c X^{-y} \text{ mod } 127$ ? This is a bonus worth 5, because I don't know the answer.

3) Substitution ciphers and block chaining. Value 15.  
Given the following encryption system.



What is the original message? (I never checked it, so it might not be a real word)

What is the point of block chaining?

How can the above scheme be used as a 5 bit hash on any number of characters?

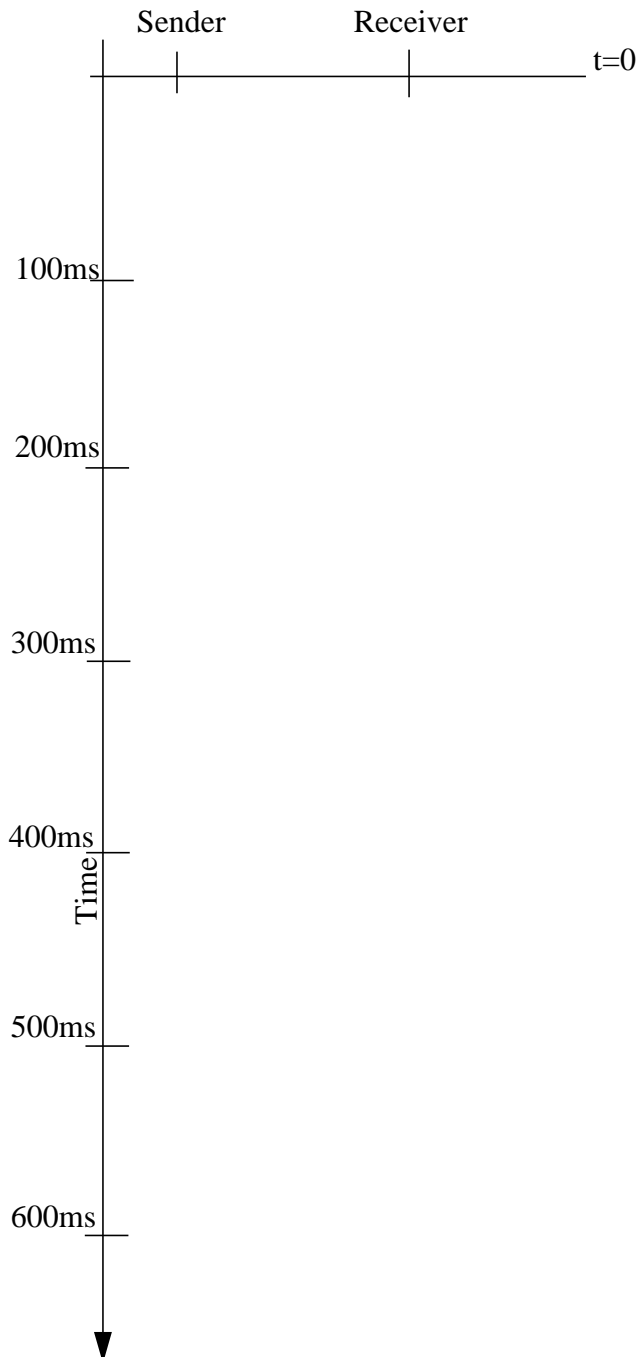
How can it be used as a keyed hash?

4) Transmission Control Protocol: Value 15.

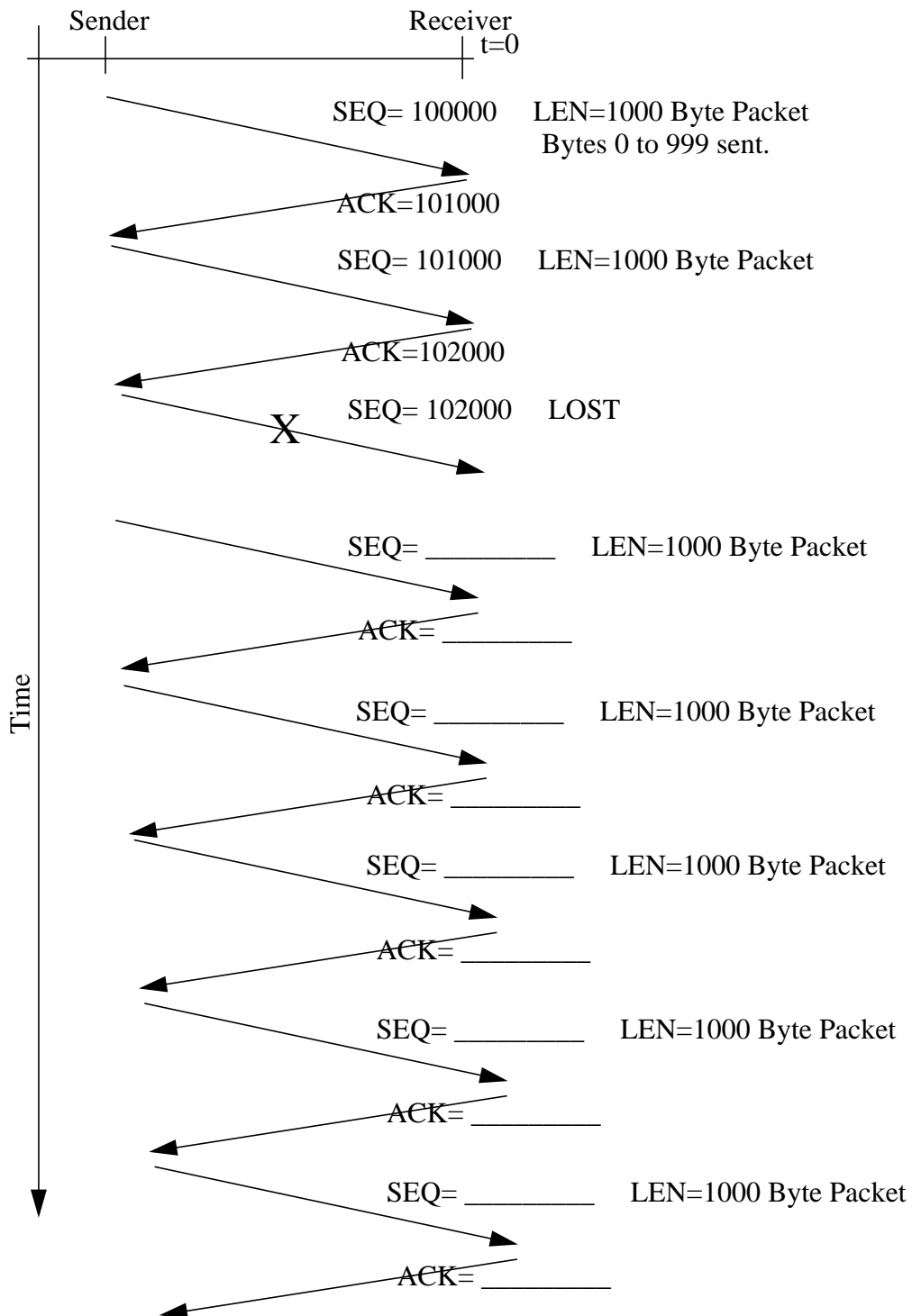
Part i) Slow Start: Congestion Threshold set at 16K Bytes. Advertised window set at 16K Bytes. MSS set at 1K Bytes. Congestion window initially set at 1K Bytes. RTT 100ms.

The transmission starts with the sender sending 1 1KB packet (8000 bits) on a 100Mbps network.

Sketch the Transmission Sequence Chart: Indicate the sender window size. (Error free mode)



4 Part ii) Fast Retransmission. Assume sender window >32K. Timeout = 10 RTT. Maximum number of Duplicate ACKs is 3.





5) CRC Fun with polynomial division. Value 20.

**Sender side:** Consider a frame of data consisting of Data = 1 0 0 1 0 1 1, or  $D(x) = x^6 + x^3 + x + 1$

The CRC polynomial is  $P(x) = x^3 + x + 1$ . Degree of the CRC is 3.

For the data calculate:  $D'(x) = x^3 D(x)$ , this is ordinary polynomial multiplication.  
What is  $D'(x)$ ?

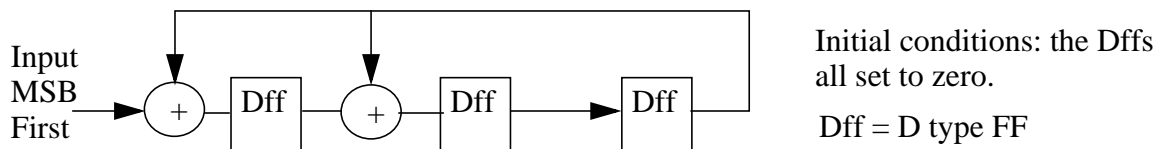
CRC Remainder Generation: Divide  $D'(x)$  by the CRC polynomial.

Methods to use:

1) Either use long division of polynomials in GF(2). Multiplication is ordinary multiplication,  $1 \times 1 = 1$ ,  $1 \times 0 = 0$ , addition and subtraction are the exor operation,  $1 + 1 = 0$ ,  $1 + 0 = 1$ ,  $1 - 1 = 0$ ,  $0 - 1 = 1$ . e.g.

$$\begin{array}{r}
 \phantom{x^2 + 1} \overline{x^2 + x} \\
 x^2 + 1 \overline{) x^4 + x^3 + x^2 + 1} \\
 \underline{x^4 \phantom{+ x^3} + x^2} \phantom{+ 1} \\
 \phantom{x^4 + } x^3 + \phantom{x^2} 1 \\
 \underline{\phantom{x^4 + } x^3 + \phantom{x^2} x} \\
 \phantom{x^4 + x^3 + } x + 1 \text{ (Remainder)}
 \end{array}
 \qquad
 \frac{x^4 + x^3 + x^2 + 1}{x^2 + 1} = x^2 + x + R(x + 1)$$

or 2) CRC Circuit analysis.



Operation after clocking in all the data  $D'(x)$ , the CRC remainder  $R(x)$  is in the Dffs.

Add  $R(x)$  to  $D'(x)$  to obtain  $D''(x)$ . What is  $D''(x)$ ?

Send  $D''(x)$  to the receiver.

**Receiver Side:** After receiving  $D''(x)$ , check it for errors using the CRC.

That is, Divide  $D''(x)$  by  $P(x)$  (the CRC polynomial). Either method described above can be used.

What is the CRC signature or remainder?

If the  $D(x)$  were corrupted during transit such that the original data  $x^6 + x^3 + x + 1$  were changed to  $x^6 + x^3 + x$ . What is the CRC that the receiver would calculate?

If the corrupted frame was associated with a wired Ethernet MAC, what would happen.

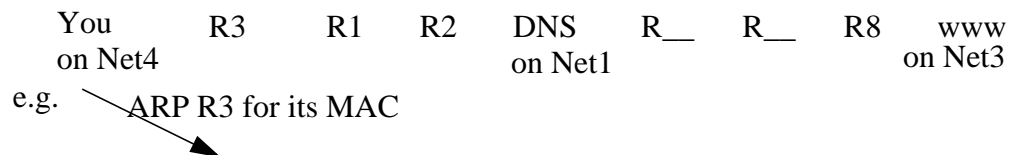
If the corrupted frame was associated with a wireless 802.11 MAC, what would happen?

6) Packet Sequence Events: Use the network of Question1. Value 10.

You are the lone host on Net4, the DNS server is on Net1, [www.beerafterexam tastesgreat.com](http://www.beerafterexam tastesgreat.com) is on Net3.

Draw the packet sequence chart for initially contacting [www.beerafterexam tastesgreat.com](http://www.beerafterexam tastesgreat.com) from your browser. (Include TCP connection handshake SYN and ACK flag settings)

The Network Routing Tables and ARP tables are up to date. Host ARP tables are not. That is routers know next router hop and the next router's MAC address.



7) Confidence Boosters: Value 5

- a) The IP header checksum, checks the IP header only. True or False?
- b) The TCP checksum, checks the TCP header plus the data payload. True or False?
- c) An IP network is packet switched. True or False?
- d) This test was pretty hard. True or False?
- e) All the answers in this section are True. True or False?

Appendix: Helpful hints

$a \bmod b + c \bmod b = (a+c) \bmod b$   
 $a \bmod b \times c \bmod b = (ac) \bmod b$