Differentiate with respect to x: (ii) $\frac{x^2}{x-1}$

Using quotient rule:
$$f'(x) = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$$
, where $u = x^2$ $v = x - 1$

$$\frac{du}{dx} = 2x$$

$$\frac{dv}{dx} = 1$$

$$= \frac{(x-1) \cdot 2x - x^2 \cdot 1}{(x-1)^2}$$

$$= \frac{2x^2 - 2x - x^2}{(x-1)^2}$$

$$= \frac{x^2 - 2x}{(x-1)^2}$$

$$= \frac{x(x-2)}{(x-1)^2}$$

Board of Studies: Notes from the Marking Centre

Very few candidates attempted to rewrite the question in the form of the product rule, with most candidates using the quotient rule. Many responses contained significant errors in simplifying, such as incorrect cancelling.

Source: http://www.boardofstudies.nsw.edu.au/hsc_exams/

^{*} These solutions have been provided by projectmaths and are not supplied or endorsed by the Board of Studies