2

State Mean:

1.60/2

0.58/1

12 Rectangles of the same height are cut from a strip and arranged in a row. The first rectangle has width 10 cm. The width of each subsequent rectangle is 96% of the width of the previous rectangle.

NOT TO SCALE

- (i) Find the length of the strip required to make the first ten rectangles.
- (ii) Explain why a strip of length 3 m is sufficient to make any number of rectangles.

10, 9.6, ...

(i)
$$a = 10, r = 0.96, n = 10$$

$$S_n = \frac{a(1 - r^n)}{1 - r}$$

$$= \frac{10(1 - 0.96^{10})}{1 - 0.96}$$

$$= 83.791841 \dots$$

The strip would be 83.79 m

= 83.79 (2 dec pl)

(ii)
$$\lim \text{sum} = \frac{a}{1-r}$$

= $\frac{10}{1-0.96}$
= 250

As limiting sum is 250, then the strip has a maximum length of 250 cm, or 2.5 m, which means that 3 m is sufficient.

Board of Studies: Notes from the Marking Centre

- (i) Responses that correctly identified the geometric progression usually obtained full marks. Simple addition of 10 terms in geometric progression was a successful technique, although this frequently led to rounding errors and took extra time. A common error was to find the tenth term rather than the sum of the first ten terms.
- (ii) Candidates who correctly interpreted the need for a limiting sum were usually successful. In some responses, candidates did not realise that when an explanation is required, they need to supply some justification. Some candidates offered only a response with no calculations and did not come up with a limiting sum.

Source: http://www.boardofstudies.nsw.edu.au/hsc_exams/

^{*} These solutions have been provided by *projectmaths* and are not supplied or endorsed by the Board of Studies