

## EXERCISES 2(b)

Simplify the following expressions by collecting like terms.

- $3x + 5 + 7x + 10$
- $4a + b - a - 4b$
- $3xy + 2xy - yx$
- $3a^2b - 3ab^2 + 2a^2b$
- $2x^2y + 3x^2y^2 - x^2y + 3x^2y^2$
- $3p^2q - 5pq - 2p^2q$
- $x^2 - 3x + 2x + 4x^2$
- $2x^2 + 5y^2 - 4x^2$
- $7x - 3 + 3x - 2$
- $6ab + 3ab + 5a + 4a$
- $mn + 8mn - 3nm$
- $5xy^2 + 3xy^2 - 2xy$
- $3abc + 5bca - 2cba$
- $12mn + 3m - 6mn - m$
- $a^2 + 5a^2 - 3a - 5a$
- $9x^2 - 3xy + 5yx - 6x^2$

Simplify the following expressions by removing the brackets and collecting like terms.

- $5a - 3(a + b)$
- $8m - 5(2m - 3n)$
- $5(2x + 3) - 5(x + 7)$
- $7(2k + 1) - 3(k + 2)$
- $5x(x - 2y) + 3x(2x - y)$
- $2a + 3b - (a - b)$
- $3x(x - y) + 2x(x - y)$
- $m(3m - 5n) + 3m(2m - n)$
- $2(x^2 - x - 6) - 3(x^2 + 2x)$
- $3(x^2 + 5x - 1) - (2x^2 + x - 2)$
- $a(a + 1) - 3(2a + 1)$
- $4(2x - y) - 6x$
- $3(2x + 5y) + 4(x - y)$
- $6(2a + 3b) + 3(a - b)$
- $5a(a + 2) - 3a(a + 1)$
- $4a(2a + b) - a(a + 2b)$
- $x + 5y - (3x + 2y)$
- $5x(2x + 1) - (x^2 + x)$
- $15(x - 2) + 4(3x - 3)$
- $3x(x - 2) - 4(x - 1)$
- $(5x + 2y - 3) - (x - 7y + 9)$
- $3(m^2 - m) - 2(m^2 + 2m + 5)$

## EXERCISES 2(f)

Factorize

- $2a + 2b$
- $2x^2 - 6xy$
- $5a^3 + 10a^2b$
- $px - py - pz$
- $8a^2b - 3a^2b^2$
- $9a^2b - 6ab^2$
- $mp + m^2p - mp^2$
- $20x - 5y$
- $m^2n + mn^2$
- $-15x - 10x^2$
- $5a^2b^3 - 18a^3b^2$
- $9m^3n^2 - 5m^2n^3$
- $54x^2y^2 - 54x^3y^3$
- $5a^2b - 5a^2b^2 - 5a^2b^3$
- $ab + ac + ad$
- $3a^2b + 6a^2b^2 + 9abc$
- $8p^2r^2q + 3p^2r^2q$
- $4a^2 + 4b^2 - 4c^2$

- $a + a^2$
- $r^2 - 2rs$

## EXERCISES 2(d)

Write down the expansion of:

- $(x + 5)(x + 1)$
- $(x + 2)(x + 4)$
- $(x - 2)(x - 3)$
- $(a - 3)(a + 4)$
- $(a + 5)(a - 4)$
- $(p - 7)(p - 3)$
- $(c + 4)(c - 5)$
- $(x - 6)(x + 1)$
- $(t + 5)(t - 1)$
- $(x + 4)(x + 8)$
- $(x + 4)(x - 8)$
- $(x - 3)(x + 9)$
- $(p - 5)^2$
- $(x - 1)^2$
- $(y + 7)^2$
- $(2x + 3)(x + 5)$
- $(3x - 4)(x - 2)$
- $(3m + 7)(2m - 1)$
- $(3y - 2)(4y + 3)$
- $(6x - 7)(x - 4)$
- $(5x - 3)(7x + 2)$
- $(2m - 11)(3m - 4)$
- $(y + 5)(3y - 2)$
- $(5z - 14)(2z + 5)$
- $(x - 14)(6x - 1)$
- $(2p - 1)(4p + 3)$
- $(3x + 2)(3x + 2)$
- $(2p - 9)(2p + 9)$
- $(3x + 2)(2x + 3)$
- $(x + 1)(2x - 1)$
- $(4p - 5)^2$
- $(3x + 4)^2$
- $(2a - 5)^2$
- $(5y - 3)^2$
- $(4y + 9)^2$
- $(2x - 3)^2$
- $(5p - 1)^2$
- $(3p + 7)^2$
- $(2z + 6)^2$

Further extended.

## EXERCISES 2(g)

Factorize each of the following and check your result by expanding your answer.

- $a(x + 2) + b(x + 2)$
- $x(p - 1) - 4(p - 1)$
- $5a(p - 6) - 3(p - 6)$
- $c(a - 3b) + d(a - 3b)$
- $4x(x - y) + 5(x - y)$
- $3a(2b - 3c) - m(2b - 3c)$
- $p(a + b) + q(a + b) - r(a + b)$
- $x(y + z) - y(y + z) - z(y + z)$
- $x^2(2x - 1) + 4(2x - 1)$
- $a(x + 2y) - b(x + 2y)$
- $ax + 4a + bx + 4b$

- $x^2 - xy + xz - yz$
- $10y - 25y^2 + 4x - 10xy$
- $a^2 - ab - ac + bc$
- $ac - 2bc - 2ad + 4bd$
- $a^3 + 3a^2b + ab^2 + 3b^3$
- $3xy - 6y + 7x - 14$
- $ab + ax - 3b - 3x$
- $a^3 - a^2b - ab + b^2$
- $x^2 - 2xy - xz + 2yz$
- $2mn + 2mp + pn^2 + p^2n$
- $x^3 + 3x^2 + 4x + 12$
- $2ax + 6bx - 6a - 9b$
- $3a - 3b + 2a^2 - 2ab$
- $m^2p + m^2 + np + n$
- $ay - 2a + y^2 - 2y$
- $2axc + 2c - axd - d$
- $p^2q - pq^2 + 5p - 5q$
- $2a^3 - a^2 + 2a - 1$
- $ax^2 - axy + bxy - by^2$
- $x^2y + x^2 + y + 1$
- $2xy - xz - 8y + 4z$
- $2x - 6y - xy + 3y^2$
- $ab - 3a - 4b + 12$
- $3m^2 - 3mn - m + n$
- $a^3 + 3a^2b + ab^2 + 3b^3$
- $2x^3 - 2x^2 + 2x - 2$
- $xw - yw + xy - y^2$

## EXERCISES 2(h)

Factorize

1.  $p^2 - q^2$
4.  $64 - m^2$
7.  $a^2b^2 - c^2$
10.  $\frac{a^2}{25} - 1$
13.  $(x + 1)^2 - 9$
16.  $\frac{x^2}{4} - \frac{1}{9}$
19.  $99^2 - 1$
22.  $12a^3 - 3ab^2$
25.  $24x^2 - 54y^2$
28.  $a^2 - (a - b)^2$
31.  $x^3 - x^2y - 9x + 9y$
34.  $a^2x - x$
37.  $3x^2y^2 - 12y^2$
40.  $5 - 5x^2$
43.  $(p + 2)^2 - (p - 2)^2$
46.  $x^3 - 3x^2 - 9x + 27$
2.  $m^2 - 1$
5.  $9a^2 - 25$
8.  $p^2q^2 - r^2$
11.  $p^2 - \frac{1}{4}$
14.  $x^2 - y^2z^2$
17.  $(a + 2)^2 - 4$
20.  $523^2 - 477^2$
23.  $3x^2y - 27y$
26.  $8a^2 - 2b^2$
29.  $a^3 - ab^2$
32.  $x^3 + 3x^2 - 4x - 12$
35.  $48a^2 - 75b^2$
38.  $(1 + h)^2 - 1$
41.  $\frac{a^2}{b^2} - \frac{b^2}{a^2}$
44.  $64 - (9x)^2$
47.  $8a^2x^2 - 18a^2y^2$
3.  $x^2 - 16$
6.  $x^2 - 0.36$
9.  $9x^2 - 4y^2$
12.  $36c^2 - 49d^2$
15.  $(2a)^2 - (3b)^2$
18.  $x^2 - (y + z)^2$
21.  $a^3b - ab^3$
24.  $45a^2x - 20x$
27.  $(x + y)^2 - 4$
30.  $2x^2 - 0.08$
33.  $p^2q - p^2 - 16q + 16$
36.  $\frac{x^2}{25} - y^2$
39.  $z^3 - z$
42.  $m^2n - n^3$
45.  $2m^2n^2 - 18n^4$
48.  $a^3 + 2a^2 - ab^2 - 2b^2$

## EXERCISES 2(j)

Factorize the following quadratic trinomials.

1.  $x^2 + 4x + 3$
4.  $x^2 + 6x + 5$
7.  $m^2 + 9m + 20$
10.  $p^2 + 19p + 18$
13.  $x^2 + 8x + 12$
16.  $x^2 - 8x + 12$
19.  $m^2 - 21m + 20$
22.  $p^2 - 2p - 15$
25.  $x^2 - 2x - 35$
28.  $a^2 - 4a - 12$
31.  $x^2 + 6x - 72$
34.  $x^2 - x - 42$
37.  $x^2 - 11x - 42$
40.  $y^2 - 6y - 55$
2.  $x^2 + 10x + 21$
5.  $a^2 + 7a + 6$
8.  $p^2 + 9p + 18$
11.  $x^2 + 7x + 12$
14.  $x^2 - 7x + 12$
17.  $m^2 - 9m + 20$
20.  $x^2 - 14x + 13$
23.  $p^2 + 14p - 15$
26.  $x^2 - 3x - 10$
29.  $x^2 - 7x + 6$
32.  $x^2 - 21x - 72$
35.  $x^2 - 19x - 42$
38.  $x^2 + 6x - 7$
41.  $x^2 + 14x + 33$
3.  $x^2 + 11x + 24$
6.  $a^2 + 12a + 32$
9.  $p^2 + 11p + 18$
12.  $x^2 + 13x + 12$
15.  $x^2 - 13x + 12$
18.  $m^2 - 12m + 20$
21.  $p^2 + 2p - 15$
24.  $p^2 - 14p - 15$
27.  $x^2 + 17x + 72$
30.  $x^2 - x - 72$
33.  $a^2 + 13a + 30$
36.  $x^2 + 19x - 42$
39.  $y^2 + 6y - 55$
42.  $x^2 - 14x + 33$

## EXERCISES 2(k)

Factorize

1.  $2x^2 + 3x + 1$
4.  $4a^2 + 13a + 3$
7.  $8x^2 - 14x + 3$
10.  $8x^2 + 14x + 5$
13.  $3x^2 - 17x + 10$
16.  $10x^2 - 11x - 8$
19.  $9x^2 - 12x + 4$
22.  $15m^2 + 17m - 18$
25.  $12y^2 + 14y - 6$
28.  $6x^2 - 19x + 14$
31.  $6p^2 + 25p + 21$
34.  $24x^2 - 59x + 36$
37.  $9x^2 + 9x - 10$
40.  $5x^2 - 2x - 3$
43.  $4x^2 + 12x + 9$
2.  $3x^2 + 11x - 4$
5.  $4x^2 + 5x + 1$
8.  $2x^2 - 9x - 5$
11.  $6x^2 + 17x + 12$
14.  $6a^2 - 13a - 63$
17.  $2x^2 + 3x - 2$
20.  $2x^2 - 9x + 10$
23.  $10a^2 - 41a - 18$
26.  $6x^2 - 25x + 14$
29.  $6x^2 - 20x + 14$
32.  $10a^2 - 11a - 6$
35.  $15x^2 - 19x + 6$
38.  $2x^2 - 9x + 4$
41.  $3p^2 - 7p + 2$
44.  $9x^2 + 30x + 25$
3.  $2x^2 + 7x + 6$
6.  $3a^2 - 5a + 2$
9.  $13c^2 - 7c - 6$
12.  $3x^2 - 13x + 4$
15.  $3x^2 - 11x - 4$
18.  $4x^2 - 12x + 9$
21.  $6x^2 - 85x + 14$
24.  $2y^2 - 4y - 6$
27.  $6x^2 - 29x + 28$
30.  $8x^2 + 2x - 3$
33.  $12y^2 + 28y - 5$
36.  $3x^2 - 2x - 1$
39.  $10p^2 + 11p + 3$
42.  $8x^2 - 6x - 9$
45.  $4x^2 - 28x + 49$

To factorize the expressions in the next set of exercises, it will be necessary to use *one or more* of the techniques we have studied:

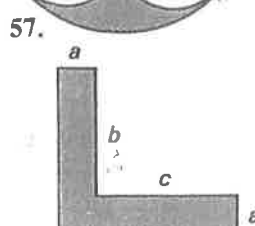
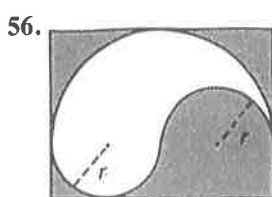
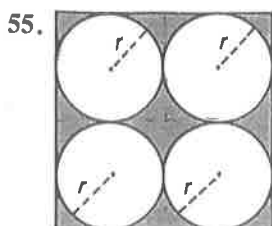
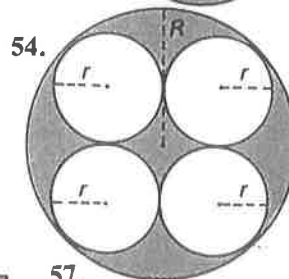
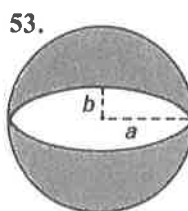
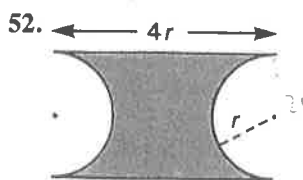
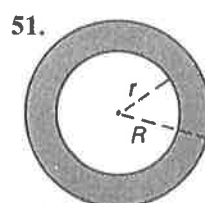
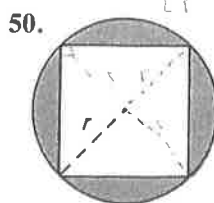
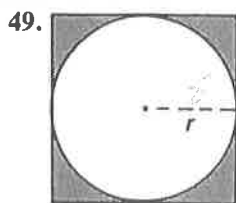
- (i) something common in each term,
- (ii) grouping and using the Distributive Law in reverse,
- (iii) difference of two squares,
- (iv) ~~sum and difference of two cubes,~~
- (v) quadratic trinomials

## EXERCISES 2(I)

Factorize completely

1.  $x^2 - 3x$
3.  $3x^2 + 9x$
5.  $x^2 - 9$
7.  $3x^2y - 12y^3$
9.  $1 - (b - c)^2$
11.  $(a + b)^2 - b^2$
13.  $a^2 - a - 42$
15.  $2x^3 + 14x^2 - 16x$
17.  $(x + 2y)^2 - 4$
- ✗ 19.  $a^3 - 1$
21.  $x^2 - 36y^2$
23.  $x^2 + x - 12$
25.  $4x^2 - 28x - 480$
27.  $6y^3 + 3y^2 - 3y$
29.  $15a^2 - 60$
31.  $5a^2x - 125x$
33.  $5t^3 + 5t^2 - 360t$
35.  $5 - 125a^2$
37.  $m^2 - mn + 6m - 6n$
39.  $x^2(x + 3) - 4(x + 3)$
41.  $4 - (x + 1)^2$
43.  $x^2 - 2x + ax - 2a$
45.  $2axc - axd + 2c - d$
- ✗ 47.  $\frac{a^3}{8} - 1$
2.  $2a^3 - 8a$
4.  $x^2 - 8x$
6.  $x^2 - 8x - 9$
8.  $5x^3y - 20xy^3$
10.  $10x^2 + 9x - 1$
- ✗ 12.  $6x^3 - 48$
14.  $a(m + n) - b(m + n)$
16.  $3a^3 + 24a^2 + 21a$
18.  $x^2 - 3x - 10$
20.  $ab^2 + abc + abd$
22.  $x^2 + x$
24.  $x(y - z) + y(y - z)$
26.  $bx^2 - 14bxy + 49by^2$
28.  $6y^3 + 26y^2 + 8y$
30.  $9mn - 25m^3n^3$
32.  $(x + y)^2 - (x - y)^2$
34.  $x^2 - 12xy + 20y^2$
36.  $ax + bx + ay + by$
38.  $(x + 3y)(x - 3y) - 3z(x + 3y)$
40.  $mx^2 - xy + ly - mlx$
42.  $6x^3 - 34x^2 - 56x$
44.  $x^2 - 10x - 144$
- ✗ 46.  $p^3 + 125$
- ✗ 48.  $(x + h)^3 + 1$

Write an algebraic expression in factorized form for the shaded area in each of the figures in questions 49. to 57.



# EXERCISES 2(o)

Express each of the following as a single fraction.

$$\begin{aligned} 17. & \frac{1}{a-b} + \frac{1}{a+b} \\ 19. & \frac{x}{x-y} + \frac{y}{x-y} \\ 21. & \frac{3a-b}{a^2-b^2} + \frac{1}{a-b} \\ 23. & \frac{x}{x^2-y^2} - \frac{y}{x^2-y^2} \\ 25. & \frac{x^2-4x+3}{x^2-1} - \frac{1}{x^2-1} \\ 27. & \frac{1}{x+y} - \frac{1}{x-y} \\ 29. & \frac{1}{x-5} - \frac{1}{x+5} + \frac{x+10}{x^2-25} \end{aligned}$$

$$\begin{aligned} 18. & \frac{3}{x-y} - \frac{2}{x+y} \\ 20. & \frac{x}{x-y} + \frac{y}{x+y} \\ 22. & \frac{1}{x^2-4} - \frac{1}{x+2} \\ 24. & \frac{3}{(x-2)^2} + \frac{2}{x-2} \\ 26. & \frac{3}{x-2} + \frac{1}{x+3} \\ 28. & \frac{5}{2a+6} + \frac{a}{a^2-9} \\ 30. & \frac{6}{3x-2} - \frac{8}{4x+1} \end{aligned}$$

$$\begin{aligned} 31. & \frac{7a}{3a-4} - \frac{5a}{2a-3} \\ 33. & \frac{1}{x+4} + \frac{x}{x^2-16} \\ 35. & \frac{1}{a+3} + \frac{a^2+5a+6}{a+4} \\ 37. & \frac{x+1}{x-1} - \frac{x-1}{x+1} \\ 39. & \frac{5}{x-2} + \frac{3}{x^2-4} \\ 41. & \frac{3x}{x^2-16} - \frac{2}{x+4} \end{aligned}$$

$$\begin{aligned} 32. & \frac{y}{x^2-xy} + \frac{1}{x} \\ 34. & \frac{1}{x+2} + \frac{1}{x-2} + \frac{4}{x^2-4} \\ 36. & \frac{3}{x^2-4} - \frac{2}{x^2-3x+2} \\ 38. & \frac{3a+1}{3a-1} - \frac{3a+1}{3a+1} \\ 40. & \frac{5}{x+1} - \frac{3}{x-2} \\ 42. & \frac{5}{3x} - \frac{2}{x^2-5x} \end{aligned}$$

# EXERCISES 2(m)

Simplify

$$\begin{aligned} 1. & \frac{8a-4b}{4} \\ 4. & \frac{8x^2-4xy}{8xy} \\ 7. & \frac{3a-5b}{3a^2-5ab} \\ 10. & \frac{p^2q-pq^2}{pq} \\ 13. & \frac{x^2-y^2}{(x+y)^2} \\ 16. & \frac{15a^2-5ab}{3ab-b^2} \\ 19. & \frac{a^2+ab}{ab+b^2} \\ 22. & \frac{x^2-6x+8}{x^2-x-2} \\ 25. & \frac{x^2+4x+4}{x^2-3x-10} \\ 28. & \frac{3x^2-xy}{xy} \times \frac{x^2y}{3xy-y^2} \\ 2. & \frac{15x+10y}{15} \\ 5. & \frac{12ab-6b^2}{9ab} \\ 8. & \frac{m+m^2}{m} \\ 11. & \frac{x^2+xy}{2x} \\ 14. & \frac{k^2+k}{k+1} \\ 17. & \frac{4x^2-4xy}{x^2-y^2} \\ 20. & \frac{a^2-b^2}{a^2+ab} \\ 23. & \frac{x^2+3x+2}{x^2-4} \\ 26. & \frac{4x^3y-16xy}{x^2+2x-8} \\ 3. & \frac{14x-7y}{2x-y} \\ 6. & \frac{8x+2}{4x+1} \\ 9. & \frac{mn-n^2}{n} \\ 12. & \frac{2rs-12r}{r^2+rs} \\ 15. & \frac{x^2-9}{x^2+3x} \\ 18. & \frac{x^2-7x+6}{x^2-36} \\ 21. & \frac{x^2-1}{x^2-5x+4} \\ 24. & \frac{x^2-5x+6}{x^2+x-12} \\ 27. & \frac{m^2+m-2}{m^2-m} \\ 29. & \frac{12a+9}{15} \times \frac{5}{4a+3} \end{aligned}$$

$$\begin{aligned} 30. & \frac{2a^2-3ab}{ab-b^2} \times \frac{2a^2-2ab}{4a-6b} \\ 32. & \frac{12x^2-4x}{3x^2-x} \div \frac{10x^2y}{5x^2y^2} \\ 34. & \frac{(a+2b)(a-b)}{a^2-4b^2} \times \frac{a^2-3ab+2b^2}{ab-b^2} \\ 36. & \frac{x^3+y^3}{x^2-y^2} \\ 38. & \frac{2x+2y}{x^3-y^3} \times \frac{x^2-2xy+y^2}{x^2-y^2} \\ 40. & \frac{x^3-(x-y)^3}{x^2-(x-y)^2} \\ 31. & \frac{15x^2-5xy}{10xy} \div \frac{3x-y}{2y} \\ 33. & \frac{x^2-2x-3}{x^2-4x-5} \times \frac{x^2-25}{(x-3)(x+5)} \\ 35. & \frac{m^2-9}{m^2-m-12} \div \frac{m^2-3m}{m^2-9m+20} \\ 37. & \frac{8x^2+4x+2}{8x^3-1} \\ 39. & \frac{(x+h)^3-x^3}{h} \end{aligned}$$

# EXERCISES 2(n)

Express each of the following as a single fraction.

$$\begin{aligned} 1. & \frac{x}{5} - \frac{x}{6} \\ 4. & \frac{y}{2} + \frac{2y}{3} - \frac{y}{4} \\ 7. & \frac{3x+2}{6} - \frac{x+1}{4} \\ 10. & \frac{a-2b}{6} - \frac{2a+b}{9} \\ 3. & \frac{a}{3} + \frac{4a}{5} - \frac{a}{6} \\ 6. & \frac{2x-y}{3} - \frac{x-3y}{6} \\ 9. & \frac{x}{2} + \frac{y}{4} - \frac{x+y}{3} \\ 12. & \frac{1}{x} - \frac{2}{3x} \\ 15. & \frac{m}{n} - \frac{n}{m} \\ 18. & \frac{1}{ab} + \frac{a}{bc} \\ 21. & \frac{1}{x} + \frac{2}{x} - \frac{1}{x^2} \\ 2. & \frac{3x}{8} + \frac{x}{2} \\ 5. & \frac{a+2}{5} - \frac{a-1}{3} \\ 8. & \frac{3m-2n}{5} + \frac{m+n}{10} \\ 11. & \frac{3(a+b)}{4} - \frac{a-b}{6} \\ 14. & \frac{1}{ab} - \frac{2}{b} \\ 17. & \frac{5}{a^2b} - \frac{2}{ab^2} \\ 20. & \frac{1}{x+1} + \frac{2}{3} \end{aligned}$$

## EXERCISES 21(b)

Solutions

1.  $10x + 15$
4.  $9ab + 9a$
7.  $5a^2b - 3ab^2$
10.  $6abc$
13.  $5x^2 - x$
16.  $3x^2 + 2xy$
19.  $15n - 2m$
22.  $15a + 15b$
25.  $11x^2 - 13xy$
29.  $5x^2 - 5xy$
33.  $-x^2 - 8x - 12$
37.  $a^2 - 5a - 3$
2.  $10x - 5$
5.  $4xy$
8.  $8xy^2 - 2xy$
11.  $p^2q - 5pq$
14.  $6a^2 - 8a$
17.  $2a - 3b$
20.  $10x + 11y$
23.  $11k + 1$
26.  $7a^2 + 2ab$
30.  $9x^2 + 4x$
34.  $3x^2 - 10x + 4$
38.  $m^2 - 7m - 10$
3.  $3a - 3b$
6.  $6mn$
9.  $x^2y + 6x^2y^2$
12.  $6mn + 2m$
15.  $5y^2 - 2x^2$
18.  $2x - 4y$
21.  $5x - 20$
24.  $2a^2 + 7a$
27.  $a + 4b$
31.  $9m^2 - 8mn$
35.  $x^2 + 14x - 1$
28.  $3y - 2x$
32.  $27x - 42$
36.  $4x + 9y - 12$

## EXERCISES 21(d)

1.  $x^2 + 6x + 5$
4.  $a^2 + a - 12$
7.  $c^2 - c - 20$
10.  $x^2 + 12x + 32$
13.  $p^2 - 10p + 25$
16.  $2x^2 + 13x + 15$
19.  $12y^2 + y - 6$
22.  $6m^2 - 41m + 44$
25.  $6x^2 - 85x + 14$
28.  $4p^2 - 81$
31.  $16p^2 - 40p + 25$
34.  $25y^2 - 30y + 9$
37.  $25p^2 - 10p + 1$
2.  $x^2 + 6x + 8$
5.  $a^2 + a - 20$
8.  $x^2 - 5x - 6$
11.  $x^2 - 4x - 32$
14.  $x^2 - 2x + 1$
17.  $3x^2 - 10x + 8$
20.  $6x^2 - 31x + 28$
23.  $3y^2 - 13y - 10$
26.  $8p^2 + 2p - 3$
29.  $6x^2 + 13x + 6$
32.  $9x^2 + 24x + 16$
35.  $16y^2 + 72y + 81$
38.  $9p^2 + 42p + 49$
3.  $x^2 - 5x + 6$
6.  $p^2 - 10p + 21$
9.  $t^2 + 4t - 5$
12.  $x^2 + 6x - 27$
15.  $y^2 + 14y + 49$
18.  $6m^2 + 11m - 7$
21.  $35x^2 - 11x - 6$
24.  $10z^2 - 3z - 70$
27.  $9x^2 + 12x + 4$
30.  $2x^2 + x - 1$
33.  $4a^2 - 20a + 25$
36.  $4x^2 - 12x + 9$
39.  $4z^2 + 24z + 36$

## EXERCISES 21(f)

1.  $2(a + b)$
5.  $mn(m + n)$
9.  $a(b + c + d)$
13.  $a^2b(8 - 3b)$
17.  $54x^2y^2(1 - xy)$
2.  $5(4x - y)$
6.  $r(r - 2s)$
10.  $p(x - y - z)$
14.  $m^2n^2(9m - 5n)$
18.  $4(a^2 + b^2 - c^2)$
3.  $a(1 + a)$
7.  $5a^2(a + 2b)$
11.  $a^2b^2(5b - 18a)$
15.  $p^2q(8r + 3)$
19.  $mnp(1 + m - p)$
4.  $2x(x - 3y)$
8.  $-5x(3 + 2x)$
12.  $3ab(a + 2ab + 3c)$
16.  $3ab(3a - 2b)$
20.  $5a^2b(1 - b - b^2)$

## EXERCISES 21(g)

1.  $(a + b)(x + 2)$
4.  $(c + d)(a - 3b)$
7.  $(p + q - r)(a + b)$
10.  $(a - b)(x + 2y)$
13.  $(x + z)(x - y)$
16.  $(5y + 2x)(2 - 5y)$
19.  $(a - 3)(b + x)$
22.  $(a^2 - b)(a - b)$
25.  $(a + y)(y - 2)$
28.  $(2x - 3)(2a + 3b)$
31.  $(ax + by)(x - y)$
34.  $(x^2 + 1)(y + 1)$
37.  $(a^2 + b^2)(a + 3b)$
40.  $2(x^2 + 1)(x - 1)$
2.  $(x - 4)(p - 1)$
5.  $(4x + 5)(x - y)$
8.  $(x - y - z)(y + z)$
11.  $(a + b)(x + y)$
14.  $(2x + 1)(y + z)$
17.  $(a^2 + b^2)(a + 3b)$
20.  $(3y + 7)(x - 2)$
23.  $(3 + 2a)(a - b)$
26.  $(x^2 + 4)(x + 3)$
29.  $(pq + 5)(p - q)$
32.  $(a^2 + 1)(2a - 1)$
35.  $(a - 4)(b - 3)$
38.  $(3m - 1)(m - n)$
3.  $(5a - 3)(p - 6)$
6.  $(3a - m)(2b - 3c)$
9.  $(x^2 + 4)(2x - 1)$
12.  $(a + b)(x + 4)$
15.  $(a - c)(a - b)$
18.  $(c - 2d)(a - 2b)$
21.  $(x - z)(x - 2y)$
24.  $(2m + pn)(n + p)$
27.  $(2c - d)(ax + 1)$
30.  $(m^2 + n)(p + 1)$
33.  $(x - 4)(2y - z)$
36.  $(2 - y)(x - 3y)$
39.  $(w + y)(x - y)$

## EXERCISES 21(h)

1.  $(p - q)(p + q)$
4.  $(8 - m)(8 + m)$
7.  $(ab - c)(ab + c)$
10.  $\left(\frac{a}{5} - 1\right)\left(\frac{a}{5} + 1\right)$
13.  $(x - 2)(x + 4)$
16.  $\left(\frac{x}{2} - \frac{1}{3}\right)\left(\frac{x}{2} + \frac{1}{3}\right)$
19. 9800
22.  $3a(2a - b)(2a + b)$
25.  $6(2x - 3y)(2x + 3y)$
28.  $b(2a - b)$
31.  $(x - 3)(x + 3)(x - y)$
34.  $x(a - 1)(a + 1)$
37.  $3y^2(x - 2)(x + 2)$
40.  $5(1 - x)(1 + x)$
43.  $8p$
46.  $(x - 3)(x + 3)(x - 3)$
2.  $(m - 1)(m + 1)$
5.  $(3a - 5)(3a + 5)$
8.  $(pq - r)(pq + r)$
11.  $\left(p - \frac{1}{2}\right)\left(p + \frac{1}{2}\right)$
14.  $(x - yz)(x + yz)$
17.  $a(a + 4)$
20. 46000
23.  $3y(x - 3)(x + 3)$
26.  $2(2a - b)(2a + b)$
29.  $a(a - b)(a + b)$
32.  $(x - 2)(x + 2)(x + 3)$
35.  $3(4a - 5b)(4a + 5b)$
38.  $h(2 + h)$
41.  $\left(\frac{a}{b} - \frac{b}{a}\right)\left(\frac{a}{b} + \frac{b}{a}\right)$
44.  $(8 - 9x)(8 + 9x)$
47.  $2a^2(2x - 3y)(2x + 3y)$
3.  $(x - 4)(x + 4)$
6.  $(x - 0.6)(x + 0.6)$
9.  $(3x - 2y)(3x + 2y)$
12.  $(6c - 7d)(6c + 7d)$
15.  $(2a - 3b)(2a + 3b)$
18.  $(x - y - z)(x + y + z)$
21.  $ab(a - b)(a + b)$
24.  $5x(3a - 2)(3a + 2)$
27.  $(x + y - 2)(x + y + 2)$
30.  $2(x - 0.2)(x + 0.2)$
33.  $(p - 4)(p + 4)(q - 1)$
36.  $\left(\frac{x}{5} - y\right)\left(\frac{x}{5} + y\right)$
39.  $z(z - 1)(z + 1)$
42.  $n(m - n)(m + n)$
45.  $2n^2(m - 3n)(m + 3n)$
48.  $(a - b)(a + b)(a + 2)$

## EXERCISES 2(1)

1.  $(x + 1)(x + 3)$
2.  $(x + 3)(x + 7)$
3.  $(x + 3)(x + 8)$
4.  $(x + 5)(x + 1)$
5.  $(a + 6)(a + 1)$
6.  $(a + 4)(a + 8)$
7.  $(m + 5)(m + 4)$
8.  $(p + 6)(p + 3)$
9.  $(p + 2)(p + 9)$
10.  $(p + 1)(p + 18)$
11.  $(x + 4)(x + 3)$
12.  $(x + 1)(x + 12)$
13.  $(x + 6)(x + 2)$
14.  $(x - 3)(x - 4)$
15.  $(x - 12)(x - 1)$
16.  $(x - 2)(x - 6)$
17.  $(m - 5)(m - 4)$
18.  $(m - 10)(m - 2)$
19.  $(m - 20)(m - 1)$
20.  $(x - 13)(x - 1)$
21.  $(p + 5)(p - 3)$
22.  $(p - 5)(p + 3)$
24.  $(p - 15)(p + 1)$
23.  $(p + 15)(p - 1)$
25.  $(x - 7)(x + 5)$
26.  $(x - 5)(x + 2)$
27.  $(x + 9)(x + 8)$
28.  $(a - 6)(a + 2)$
29.  $(x - 6)(x - 1)$
30.  $(x - 9)(x + 8)$
31.  $(x + 12)(x - 6)$
32.  $(x - 24)(x + 3)$
33.  $(a + 10)(a + 3)$
34.  $(x - 7)(x + 6)$
35.  $(x - 21)(x + 2)$
36.  $(x + 21)(x - 2)$
37.  $(x - 14)(x + 3)$
38.  $(x + 7)(x - 1)$
39.  $(v + 11)(v - 5)$
40.  $(v - 11)(v + 5)$
41.  $(x + 3)(x + 11)$
42.  $(x - 3)(x - 11)$

1.  $(2x + 1)(x + 1)$
2.  $(3x - 1)(x + 4)$
3.  $(2x + 3)(x + 2)$
4.  $(4a + 1)(a + 3)$
5.  $(4x + 1)(x + 1)$
6.  $(3a - 2)(a - 1)$
7.  $(4x - 1)(2x - 3)$
8.  $(2x + 1)(x - 5)$
9.  $(13c + 6)(c - 1)$
10.  $(4x + 5)(2x + 1)$
11.  $(3x + 4)(2x + 3)$
12.  $(3x - 1)(x - 4)$
13.  $(3x - 2)(x - 5)$
14.  $(3a + 7)(2a - 9)$
15.  $(3x + 1)(x - 4)$
16.  $(5x - 8)(2x + 1)$
17.  $(2x - 1)(x + 2)$
18.  $(2x - 1)(2x - 3)$
19.  $(3x - 2)(3x - 2)$
20.  $(x - 2)(2x - 5)$
21.  $(6x - 1)(x - 14)$
22.  $(5m + 9)(3m - 2)$
23.  $(5a + 2)(2a - 9)$
24.  $2(y - 3)(y + 1)$
25.  $2(3y - 1)(2y + 3)$
26.  $(3x - 2)(2x - 7)$
27.  $(3x - 4)(2x - 7)$
28.  $(6x - 7)(x - 2)$
29.  $2(3x - 7)(x - 1)$
30.  $(4x + 3)(2x - 1)$
31.  $(p + 3)(6p + 7)$
32.  $(5a + 2)(2a - 3)$
33.  $(6y - 1)(2y + 5)$
34.  $(8x - 9)(3x - 4)$
35.  $(5x - 3)(3x - 2)$
36.  $(3x + 1)(x - 1)$
37.  $(3x + 5)(3x - 2)$
38.  $(2x - 1)(x - 4)$
39.  $(5p + 3)(2p + 1)$
40.  $(5x + 3)(x - 1)$
41.  $(3p - 1)(p - 2)$
42.  $(4x + 3)(2x - 3)$
43.  $(2x + 3)^2$
44.  $(3x + 5)^2$
45.  $(2x - 7)^2$

1.  $x(x - 3)$
2.  $2a(a - 2)(a + 2)$
3.  $3x(x + 3)$
4.  $x(x - 8)$
5.  $(x - 3)(x + 3)$
6.  $(x - 9)(x + 1)$
7.  $3y(x - 2y)(x + 2y)$
8.  $5xy(x - 2y)(x + 2y)$
9.  $(1 - b + c)(1 + b - c)$
10.  $(10x - 1)(x + 1)$
11.  $a(a + 2b)$
12.  $6(x - 2)(x^2 + 2x + 4)$
13.  $(a - 7)(a + 6)$
15.  $2x(x + 8)(x - 1)$
16.  $3a(a + 7)(a + 1)$
17.  $(x + 2y - 2)(x + 2y + 2)$
18.  $(x - 5)(x + 2)$
21.  $(x - 6y)(x + 6y)$
24.  $(x + y)(y - z)$
19.  $(a - 1)(a^2 + a + 1)$
20.  $ab(b + c + d)$
27.  $3y(2y - 1)(y + 1)$
22.  $x(x + 1)$
23.  $(x + 4)(x - 3)$
24.  $(x + y)(y - z)$
25.  $4(x - 15)(x + 8)$
26.  $b(x - 7y)^2$
27.  $3y(2y - 1)(y + 1)$
28.  $2y(3y + 1)(y + 4)$
29.  $15(a - 2)(a + 2)$
30.  $mn(3 - 5mn)(3 + 5mn)$
31.  $5x(a - 5)(a + 5)$
32.  $4xy$
33.  $5(t + 9)(t - 8)$
34.  $(x - 2y)(x - 10y)$
35.  $5(1 - 5a)(1 + 5a)$
36.  $(x + y)(a + b)$
37.  $(m + 6)(m - n)$
38.  $(x + 3y)(x - 3y - 3z)$
39.  $(x - 2)(x + 2)(x + 3)$
40.  $(x - l)(mx - y)$
41.  $(1 - x)(3 + x)$
42.  $2x(3x + 4)(x - 7)$
43.  $(x + a)(x - 2)$
44.  $(x - 18)(x + 8)$
45.  $(ax + 1)(2c - d)$

46.  $(p + 5)(p^2 - 5p + 25)$
47.  $\left(\frac{a}{2} - 1\right)\left(a^2 + \frac{a}{2} + 1\right)$
48.  $(x + h + 1)(x^2 + 2xh + h^2 - x - h + 1)$
49.  $(4 - \pi)r^2$
50.  $(\pi - 2)r^2$
52.  $(8 - \pi)r^2$
53.  $\pi a(a - b)$
55.  $4(4 - \pi)r^2$
56.  $2(6 - \pi)r^2$
51.  $\pi(R - r)(R + r)$
54.  $\pi(R - 2r)(R + 2r)$
57.  $a(a + b + c)$

1.  $2a - b$
2.  $\frac{3x + 2y}{3}$
3. 7
4.  $\frac{2x - y}{2y}$
5.  $\frac{2(2a - b)}{3a}$
6. 2
7.  $\frac{1}{a}$
8.  $1 + m$
9.  $m - n$
10.  $p - q$
11.  $\frac{x + y}{2}$
12.  $\frac{2(s - 6)}{r + s}$
13.  $\frac{x - y}{x + y}$
14.  $k$
15.  $\frac{x - 3}{x}$
16.  $\frac{5a}{b}$
17.  $\frac{4x}{x + y}$
18.  $\frac{x - \frac{1}{6}}{x + \frac{1}{6}}$
19.  $\frac{a}{b}$
20.  $\frac{a - b}{a}$
21.  $\frac{x + 1}{x - 4}$
22.  $\frac{x - 4}{x + 1}$
23.  $\frac{x + 1}{x - 2}$
24.  $\frac{x - 2}{x + 4}$
25.  $\frac{x + 2}{x - 5}$
26.  $\frac{4xy(x + 2)}{x + 4}$
27.  $\frac{m + 2}{m}$
28.  $\frac{x^2}{y}$
29. 1
30.  $\frac{a^2}{b}$
31. 1
32.  $2y$
33. 1
34.  $\frac{a - b}{b}$
35.  $\frac{m - 5}{m}$
36.  $\frac{x^2 - xy + y^2}{x - y}$
37.  $\frac{2}{2x - 1}$
38.  $\frac{2}{x^2 + xy + y^2}$
39.  $3x^2 + 3xh + h^2$
40.  $\frac{3x^2 - 3xy + y^2}{2x - y}$

# EXERCISES 2(n)

1.  $\frac{x}{30}$
2.  $\frac{7x}{8}$
3.  $\frac{29a}{30}$
4.  $\frac{11y}{12}$
5.  $\frac{-2a+11}{15}$
6.  $\frac{3x+y}{6}$
7.  $\frac{3x+1}{12}$
8.  $\frac{7m-3n}{10}$
9.  $\frac{2x-y}{12}$
10.  $\frac{-a-8b}{18}$
11.  $\frac{7a+11b}{12}$
12.  $\frac{1}{3x}$
13.  $\frac{3a+1}{a^2}$
14.  $\frac{1-2a}{ab}$
15.  $\frac{m^2-n^2}{mn}$
16.  $\frac{4z+3x}{xyz}$
17.  $\frac{5b-2a}{a^2b^2}$
18.  $\frac{c+a^2}{abc}$
19.  $\frac{4a-11}{6a}$
20.  $\frac{2x+5}{3(x+1)}$
21.  $\frac{3x-1}{x^2}$

## EXERCISES 2(o)

1.  $(x-3)(x+3)$
2.  $x^2-25$
3.  $x(x-2)$
4.  $6(x-2)$
5.  $x^2-4x$
6.  $x(x-4)(x+4)$
7.  $x^2-1$
8.  $2(x-3)(x+3)$
9.  $x^2+4x+4$
10.  $x^2-y^2$
11.  $(x-2)(x+2)(x+1)$
12.  $xy(x^2-y^2)$
13.  $x(x-2)^2$
14.  $x(x-3)(x+3)$
15.  $x^2-25$
16.  $xy(x^2-y^2)$
17.  $\frac{2a}{(a-b)(a+b)}$
18.  $\frac{x+5y}{(x-y)(x+y)}$
19.  $\frac{x+y}{x-y}$
20.  $\frac{x^2+2xy-y^2}{(x-y)(x+y)}$
21.  $\frac{4a}{a^2-b^2}$
22.  $\frac{3-x}{x^2-4}$
23.  $\frac{1}{x+y}$
24.  $\frac{2x-1}{(x-2)^2}$
25.  $\frac{4}{(x-1)(x-3)(x+1)}$
26.  $\frac{4x+7}{(x-2)(x+3)}$
27.  $\frac{-2y}{(x+y)(x-y)}$
28.  $\frac{7a-15}{2(a^2-9)}$
29.  $\frac{x+20}{(x-5)(x+5)}$
30.  $\frac{22}{(3x-2)(4x+1)}$
31.  $\frac{-a^2-a}{(3a-4)(2a-3)}$
32.  $\frac{1}{x-y}$
33.  $\frac{2x-4}{x^2-16}$
34.  $\frac{2}{x-2}$
35.  $\frac{2}{a+2}$
36.  $\frac{x-7}{(x-2)(x+2)(x-1)}$
37.  $\frac{4x}{(x-1)(x+1)}$
38.  $\frac{12a}{(3a-1)(3a+1)}$
39.  $\frac{5x+13}{(x-2)(x+2)}$
40.  $\frac{2x-13}{(x+1)(x-2)}$
41.  $\frac{x+8}{(x-4)(x+4)}$
42.  $\frac{5x-31}{3x(x-5)}$