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2015 13 (i) Find the domain and range for the function $f(x) = \sqrt{9-x^2}$.

2 2

b (ii) On a number plane, shade the region where the points (x, y) satisfy both of the inequalities $y \le \sqrt{9 - x^2}$ and $y \ge x$.

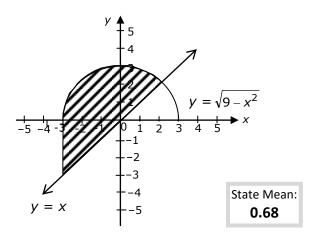
(ii)

(i) Domain: $-3 \le x \le 3$

Range: $0 \le f(x) \le 3$

State Mean:

1.11



^{*} These solutions have been provided by projectmaths and are not supplied or endorsed by BOSTES.

Board of Studies: Notes from the Marking Centre

(b)(i) This part was challenging. Candidates who sketched $y = \sqrt{9 - x^2}$ were generally more successful in finding the correct domain and range.

Common problems were:

- incorrectly stating their solution as $x \ge -3$, $x \le 3$ instead of $-3 \le x \le 3$
- not recognising the function as a semicircle and using the same values for the domain and range
- having the inequality signs reversed or using < instead of ≤
- only stating the domain
- giving the range as $y \ge 0$ since a square root is always positive.

(b)(ii) This part was challenging. Many candidates correctly graphed the semicircle but were less successful adding the graph of y = x and correctly shading the required region. Candidates are reminded to draw neat, clear diagrams, use a ruler to draw lines and show a scale on each axis. The size of each diagram should be at least one-third of a page.

Common problems were:

- not drawing the vertical boundaries of |x| = 3 for the semicircular region
- not shading any region at all or not continuing the region below the x-axis between the lines x = -3 and y = x
- sketching the semicircle only and not the line y = x
- drawing an incorrect semicircle, for example $y = -\sqrt{9 x^2}$
- graphing the solution as an inequality on a number line.