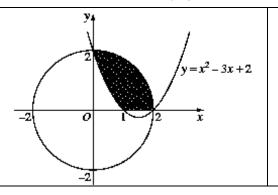
05

The shaded region in the diagram is bounded by the circle of radius 2 centred at the origin, the parabola  $y = x^2 - 3x + 2$ , and the x-axis.

By considering the difference of two areas, find the area of the shaded region.



Area = Area of quadrant with radius 2 units **minus** area under  $y = x^2 - 3x + 2$ , from x = 0 to x = 1  $= \frac{1}{4} \times \pi \times 2^2 - \int_{2}^{1} x^2 - 3x + 2 \ dx$ 

$$= \pi - \left[\frac{x^3}{3} - \frac{3x^2}{2} + 2x\right]_0^1$$
$$= \pi - \left[\frac{1}{3} - \frac{3}{2} + 2 - 0\right]$$

$$= \pi - \frac{5}{6}$$
 : area of  $(\pi - \frac{5}{6})$  unit<sup>2</sup>

## **Board of Studies: Notes from the Marking Centre**

Better responses to this part recognised that the area of a quadrant of a circle could be found by using the formula for the area of a circle. Common errors in this part were made in writing the equation of the circle, for example  $y = \sqrt{4 - x^2} = 2 - x$ , and determining an integral expression that represented the shaded region.

Source: http://www.boardofstudies.nsw.edu.au/hsc\_exams/

<sup>\*</sup> These solutions have been provided by projectmaths and are not supplied or endorsed by the Board of Studies