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1

(ii) Hence, or otherwise, find
$$\int \frac{\cos 2x}{3 + \sin 2x} dx$$
.

2

(i)
$$\frac{d}{dx}[3 + \sin 2x] = 2 \cos 2x$$

(ii)
$$\int \frac{\cos 2x}{3 + \sin 2x} dx = \frac{1}{2} \int \frac{2\cos 2x}{3 + \sin 2x} dx$$

$$= \frac{1}{2} \log_e(3 + \sin 2x) + c \qquad \text{(using result in part (i))}$$
State Mean:
0.73
1.19

Board of Studies: Notes from the Marking Centre

- (i) Most candidates completed this part, correctly recognising that $2\cos 2x$ is the derivative of $\sin 2x$. Common problems were:
 - incorrectly adjusting the constant multiplier using $\frac{1}{2}$ or -2;
 - misinterpreting the question and differentiating using the product rule uv' + vu' with u = 3 and $v = \sin 2x$;
 - attempting to integrate instead of differentiating;
 - making errors when transcribing from line to line, for example sin 2x changing to sin x.
- (ii) In successful responses, candidates recognised that they were working with a log function, and showed the required adjustment to the numerator, linking their response from (i).

Common problems were:

• not recognising that the integral was in the form $\frac{f'(x)}{f(x)}$ and the primitive was a logarithmic

function;

- incorrect value of constant multiplier;
- incorrect use of brackets or no brackets at all;
- using the quotient rule and differentiating.

http://www.boardofstudies.nsw.edu.au/hsc_exams/2014/pdf_doc/2014-maths.pdf

^{*} These solutions have been provided by projectmaths and are not supplied or endorsed by BOSTES.