State Mean:

1.67/3

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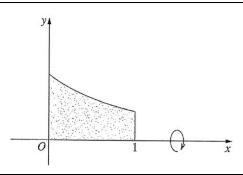
12 | 14b | The diagram shows the region

bounded by $y = \frac{3}{(x+2)^2}$, the x-axis,

the y-axis, and the line x = 1.

The region is rotated about the x-axis to form a solid.

Find the volume of the solid.



$$V = \pi \int_{0}^{1} y^{2} dx$$
$$= \pi \int_{0}^{1} \left(\frac{3}{x^{2}} \right)^{2} dx$$

$$= \pi \int_{0}^{1} \left(\frac{3}{(x+2)^{2}} \right)^{2} dx$$

$$= \pi \int_{0}^{1} \frac{9}{(x+2)^{4}} dx$$
$$= 9\pi \int_{0}^{1} (x+2)^{-4} dx$$

$$= 9\pi \left[\frac{(x+2)^{-3}}{-3} \right]_0^1$$

$$=-3\pi\left[\frac{1}{(x+2)^3}\right]_0^1$$

$$= -3\pi \left[\frac{1}{27} - \frac{1}{8} \right]$$

$$= -3\pi \left[\frac{-19}{216} \right]$$

$$= \frac{19\pi}{72}$$

 \therefore volume is $\frac{19\pi}{72}$ units³

Board of Studies: Notes from the Marking Centre

Many candidates correctly stated $V = \pi \int_0^1 \left\{ \frac{3}{(x+2)^2} \right\}^2 dx$, but most omitted the dx.

Omitting π was not a common error.

In many responses, candidates were unable to find the primitive. The most common error involved attempting to use logarithms in the primitive or to obtain a primitive involving $(x+5)^{-5}$.

Source: http://www.boardofstudies.nsw.edu.au/hsc_exams/

^{*} These solutions have been provided by projectmaths and are not supplied or endorsed by the Board of Studies