

2013 11bEvaluate $\lim_{x \rightarrow 2} \frac{x^3 - 8}{x^2 - 4}$.**2**

$$\begin{aligned}\lim_{x \rightarrow 2} \frac{x^3 - 8}{x^2 - 4} &= \lim_{x \rightarrow 2} \frac{(x - 2)(x^2 + 2x + 4)}{(x - 2)(x + 2)} \\ &= \lim_{x \rightarrow 2} \frac{x^2 + 2x + 4}{x + 2} \\ &= \frac{2^2 + 2(2) + 4}{2 + 2} \\ &= 3\end{aligned}$$

State Mean:
0.93

* These solutions have been provided by [projectmaths](#) and are not supplied or endorsed by BOSTES.

Board of Studies: Notes from the Marking Centre

Many candidates had difficulty with this question.

Common problems were:

- substituting '2' into the function and giving an answer of '0' or 'undefined'
- not factorising $x^3 - 8$ or $x^2 - 4$ correctly; some factorised the difference of 2 cubes, then incorrectly factorised $x^2 + 2x + 4$ so they could cancel
- thinking that finding the limit as $x \rightarrow \infty$ was required
- confusing the limit with differentiation by first principles or the quotient rule.

Source: http://www.boardofstudies.nsw.edu.au/hsc_exams/