

departamento de matemática



universidade de aveiro

1. Indique o conjunto solução das seguintes inequações.

(a) $8(1 - x) \leq 4(3x - 5)$

(b) $3x - (2x + 1) > 5(1 - x)$

(c) $2(x - 1) < 2(x + 4)$

(d) $1 - (2x + 5) \geq 7 - (8 - 5x)$

(e) $5(x - 5) < 3(1 - 2x)$

(f) $\frac{x}{3} \leq 7(x + 5)$

(g) $-(1 + 3x) \leq -\frac{5}{2}$

(h) $\frac{5x - 3}{2} > 7x$

(i) $\frac{1 - (2x - 1)}{2} \leq 0$

(j) $1 - 5x \geq 2 - \frac{x + 1}{3}$

(k) $\frac{1 - \frac{x}{2}}{3} < 2$

(l) $x - \frac{4x - 1}{2} < 1$

(m) $\frac{x + 10}{4} > 5 - x$

(n) $3\left(\frac{x}{2} + 1\right) \leq x - 2(1 - x)$

(o) $4 - \frac{10x + 1}{6} < 4x - \frac{16x + 3}{4}$

(p) $\frac{2(x + 1)}{3} - \frac{x + 2}{4} > 2x$

(q) $4x^2 - 3x \geq 0$

(r) $-x^2 + 12x - 27 \geq 0$

(s) $4x^2 + x + 7 > 0$

(t) $x^2 - 10x + 25 \leq 0$

(u) $x \leq x^2$

(v) $x^2 - x < 2x - 3$

(w) $\left(x - \frac{1}{2}\right)(3 - x) < 0$

(x) $\frac{1}{2}(7 - 3x)(5 - x) \geq 0$

(y) $(x - 4)^2 - 3(x - 2)^2 > 0$

(z) $\frac{x^2 - 4}{12} + \frac{x^2 + 4}{8} > 1$

(aa) $x^4 - 6x^2 + x^3 \geq x + x^2 - 6$

(ab) $2x^3 + 6x^2 < x^2 + 4x + 3$

(ac) $7x^2 + 29x - 30 < 2x(x^2 + 2x)$

(ad) $2x^2 + 3x + 2 \leq x^4$

(ae) $\frac{x - 3}{4 - x} \leq 1$

(af) $\frac{1}{x - 2} - \frac{3}{x + 1} \geq 0$

(ag) $\frac{x(x-1)}{x(x+2)} \geq -3$

(ah) $\frac{x-1}{x+4} \leq \frac{x-5}{x-1}$

(ai) $\frac{x+2}{x+8} > \frac{x-2}{x+3}$

(aj) $\frac{x+3}{3} - \frac{4}{x+2} < \frac{x}{3}$

(ak) $\frac{4x+3}{2x-5} - \frac{3x+8}{3x-7} \geq 1$

(al) $\frac{1}{x-2} + \frac{x}{3x+6} < \frac{4}{x^2-4}$

(am) $\frac{x}{x+12} \geq \frac{x+1}{20}$

(an) $\frac{x^2+1}{x^2} \leq 0$

(ao) $\frac{x^2-2x}{x^2+1} < 0$

(ap) $\frac{-x^2+4x+5}{x^2+2x+6} \geq 0$

(aq) $\frac{x^2+6x-45}{x^2-9} > 5$

(ar) $\frac{x-5}{x+8} \leq \frac{x-1}{x-2}$

(as) $\frac{-x^3+3x^2+x-3}{x+2} \leq 0$

(at) $\frac{2x^3+7x^2+2x-3}{x^3-6x^2+3x+10} < 0$

2. Indique o conjunto solução das seguintes inequações com módulos:

(a) $|x-3| < 6$

(b) $|2x-5| > 1$

(c) $|3x-3| \leq 2x+2$

(d) $|x-4| \geq 3x-6$

(e) $|2x-6| < x+4$

(f) $|x^2-5x| < 3x-6$

(g) $2x^2-2|x| > 8$

(h) $(x-6)^2-4|x-6|-5 \leq 0$

(i) $\left| \frac{x+3}{x-5} \right| > 1$

(j) $\left| \frac{x-1}{2-x} \right| \leq 3$

(k) $\left| \frac{1-x}{x+1} \right| \leq x$

(l) $\left| \frac{x^2+2}{x+3} \right| > x-1$

1. (a) $[\frac{7}{5}, +\infty[$; (b) $]1, +\infty[$; (c) \mathbb{R} ; (d) $] -\infty, -\frac{3}{7}[$; (e) $] -\infty, \frac{28}{11}[$; (f) $[-\frac{21}{4}, +\infty[$;
 (g) $[\frac{1}{2}, +\infty[$; (h) $] -\infty, -\frac{1}{3}[$; (i) $]1, +\infty[$; (j) $] -\infty, -\frac{1}{7}[$; (k) $] -10, +\infty[$;
 (l) $] -\frac{1}{2}, +\infty[$; (m) $]2, +\infty[$; (n) $[\frac{10}{3}, +\infty[$; (o) $] \frac{11}{4}, +\infty[$; (p) $] -\infty, \frac{2}{19}[$;
 (q) $] -\infty, 0] \cup [\frac{3}{4}, +\infty[$; (r) $[3, 9]$; (s) \mathbb{R} ; (t) $\{5\}$; (u) $] -\infty, 0] \cup [1, +\infty[$;
 (v) \emptyset ; (w) $] -\infty, \frac{1}{2}[\cup]3, +\infty[$; (x) $] -\infty, \frac{7}{3}] \cup [5, +\infty[$; (y) $]1 - \frac{\sqrt{48}}{4}, 1 + \frac{\sqrt{48}}{4}[$;
 (z) $] -\infty, -2[\cup]2, +\infty[$; (aa) $] -\infty, -3] \cup [-1, 1] \cup [2, +\infty[$; (ab) $] -\infty, -3[\cup] -\frac{1}{2}, 1[$;
 (ac) $] \frac{-1+\sqrt{241}}{-4}, 1[\cup] \frac{-1-\sqrt{241}}{-4}, +\infty[$; (ad) $] -\infty, -1] \cup [2, +\infty[$; (ae) $] -\infty, \frac{7}{2}] \cup [4, +\infty[$;
 (af) $] -\infty, -1[\cup]2, \frac{7}{2}[$; (ag) $] -\infty, -2[\cup] -\frac{5}{4}, +\infty[\setminus \{0\}$; (ah) $] -4, 1[\cup [21, +\infty[$;
 (ai) $] -\infty, -8[\cup] -3, 22[$; (aj) $] -2, 2[$; (ak) $[\frac{16}{9}, \frac{7}{3}[\cup] \frac{5}{2}, +\infty[$; (al) $] -3, -2[$;
 (am) $] -\infty, -12[\cup [3, 4]$; (an) \emptyset ; (ao) $]0, 2[$; (ap) $[-1, 5]$; (aq) $] -3, 0[\cup] \frac{3}{2}, 3[$;
 (ar) $] -8, \frac{9}{7}] \cup]2, +\infty[$; (as) $] -\infty, -2[\cup [-1, 1] \cup [3, +\infty[$;
 (at) $] -3, -1[\cup] -1, \frac{1}{2}[\cup]2, 5[$.
2. (a) $] -3, 9[$; (b) $] -\infty, 2[\cup]3, +\infty[$; (c) $[\frac{1}{5}, 5]$; (d) $] -\infty, \frac{5}{2}[$; (e) $] \frac{2}{3}, 10[$;
 (f) $] \frac{2+\sqrt{28}}{2}, \frac{8+\sqrt{40}}{2}[$; (g) $] -\infty, \frac{-1-\sqrt{17}}{2}[\cup] \frac{1+\sqrt{17}}{2}, +\infty[$; (h) $[1, 11]$; (i) $]1, +\infty[\setminus \{5\}$;
 (j) $] -\infty, \frac{7}{4}] \cup] \frac{5}{2}, +\infty[$; (k) $[-1 + \frac{\sqrt{8}}{2}, +\infty[$; (l) $] -\infty, \frac{5}{2}[$.