

Solutions_Q_8

Question 8.1

The dependent variable would be an indicator of the families' enjoyment on our summer vacation. The independent variables would be average temperature, if we could get to the location easily on a scale (driving, train, airplane), how much money we had saved during the year indicating money would could spend, if other family members could come along (which could be negative for some and positive for others!)

Question 8.2

For a model with all variables...

The Multiple R-squared: is 0.8031 which indicates is RSS/TSS meaning about 80% of the variance is explained by regression overall variables.

I did not scale the data but did remove terms that had a $\Pr(>|t|)$ over 0.05 iteratively as they violated the null hypothesis that the particular coefficient was not zero.

Removing variables still leaves us with 76% R-squared. The final regression was

```
pred<-lm(Crime~M+Ed+Po1+U2+Ineq+Prob,data=dat)
```

```
dat=read.csv("~/o.csv", header=TRUE)
pred<-lm(Crime~M+So+Ed+Po1+Po2+LF+M.F+Pop+NW+U1+U2+Wealth+Ineq+Prob+Time,data=dat)
```

```
pred<-lm(Crime~M+Ed+Po1+Po2+LF+M.F+Pop+NW+U1+U2+Wealth+Ineq+Prob+Time,data=dat)
pred<-lm(Crime~M+Ed+Po1+Po2+LF+M.F+Pop+NW+U1+U2+Wealth+Ineq+Prob,data=dat)
pred<-lm(Crime~M+Ed+Po1+Po2+M.F+Pop+NW+U1+U2+Wealth+Ineq+Prob,data=dat)
pred<-lm(Crime~M+Ed+Po1+Po2+M.F+Pop+U1+U2+Wealth+Ineq+Prob,data=dat)
pred<-lm(Crime~M+Ed+Po1+M.F+Pop+U1+U2+Wealth+Ineq+Prob,data=dat)
pred<-lm(Crime~M+Ed+Po1+M.F+U1+U2+Wealth+Ineq+Prob,data=dat)
pred<-lm(Crime~M+Ed+Po1+M.F+U1+U2+Ineq+Prob,data=dat)
pred<-lm(Crime~M+Ed+Po1+U1+U2+Ineq+Prob,data=dat)
pred<-lm(Crime~M+Ed+Po1+U2+Ineq+Prob,data=dat)
```

```
summary(pred)
```

```
##
## Call:
## lm(formula = Crime ~ M + Ed + Po1 + U2 + Ineq + Prob, data = dat)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -470.68  -78.41  -19.68   133.12   556.23
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -5040.50     899.84  -5.602 1.72e-06 ***
## M             105.02      33.30   3.154 0.00305 **
## Ed            196.47      44.75   4.390 8.07e-05 ***
## Po1           115.02      13.75   8.363 2.56e-10 ***
## U2             89.37      40.91   2.185 0.03483 *
## Ineq           67.65      13.94   4.855 1.88e-05 ***
```

```
## Prob          -3801.84    1528.10  -2.488  0.01711 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 200.7 on 40 degrees of freedom
## Multiple R-squared:  0.7659, Adjusted R-squared:  0.7307
## F-statistic: 21.81 on 6 and 40 DF,  p-value: 3.418e-11
```

Doing PCA on the dataset

```
dat=read.csv("~/o.csv", header=TRUE)
pca_mine=prcomp(dat)
summary(pca_mine)
```

```
## Importance of components:
##
##          PC1      PC2      PC3      PC4      PC5      PC6
## Standard deviation  982.1164 341.1338 35.46689 7.41067 6.05210 2.266
## Proportion of Variance  0.8912  0.1075  0.00116 0.00005 0.00003 0.000
## Cumulative Proportion  0.8912  0.9987  0.99990 0.99996 0.99999 1.000
##
##          PC7      PC8      PC9      PC10     PC11     PC12     PC13
## Standard deviation  1.804 1.319 0.9088 0.7297 0.4199 0.2456 0.2059
## Proportion of Variance 0.000 0.000 0.0000 0.0000 0.0000 0.0000 0.0000
## Cumulative Proportion 1.000 1.000 1.0000 1.0000 1.0000 1.0000 1.0000
##
##          PC14      PC15      PC16
## Standard deviation  0.02361 0.01279 0.006995
## Proportion of Variance 0.00000 0.00000 0.000000
## Cumulative Proportion 1.00000 1.00000 1.000000
```

Indicates that almost 90% of the variance is in the first two components (0.9987).

Not PART OF 8.2 (Question for me to explore)

Two great examples for the reconstruction

<https://stats.stackexchange.com/questions/229092/how-to-reverse-pca-and-reconstruct-the-original-data>

<https://stats.stackexchange.com/questions/57467/how-to-perform-dimensionality-reduction>
57478#57478

Some of the variables that were pulled out do to the null hypothesis on the coefficient being zero are present and large in PC1

```
nComp = 2
mu=colMeans(dat)
X = pca_mine$x[,1:nComp] %*% t(pca_mine$rotation[,1:nComp])
X = scale(X, center = -mu, scale = FALSE)
h=X[1,]
```