

Having a BLAST with SLAM

Meeting 4, CSCI 5535, Fall 2013



Announcements

- Homework 0 due Sat
 - Questions?
- Move Tue office hours to 4-5pm

Software Model Checking via Counterexample Guided Abstraction Refinement

There are easily dozens of papers.

We will skim.

SLAM Overview/Review

- Input:

Specification — property to check : “no deadlocks”
“program uses lock correctly”
Not “I am webserver”

Program ((programs, device drivers))

- Output:

✓ verified = program has no deadlocks

✗ counterexample = path that may result in error
that violates the spec

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SLAM Overview

- Input: Program and Specification
 - Standard C Program (pointers, procedures)
 - Specification = Partial Correctness
 - Given as a finite state machine (typestate)
 - "I use locks correctly", **not** "I am a webserver"
- Output: Verified or Counterexample
 - Verified = program does not violate spec
 - Can come with proof!
 - Counterexample = concrete bug instance
 - A path through the program that violates the spec

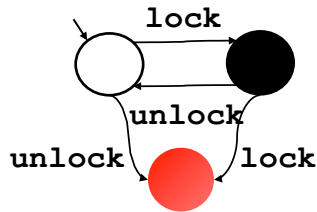
5

Take-Home Message

- **SLAM** is a **software model checker**. It **abstracts** C programs to **boolean programs** and model-checks the boolean programs.
- No errors in the boolean program implies no errors in the original.
- An error in the boolean program **may** be a real bug. Or SLAM may **refine** the abstraction and start again.

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Property 1: Double Locking

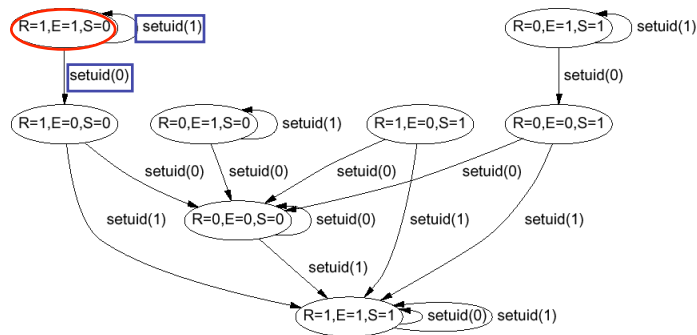


"An attempt to re-acquire an acquired lock or release a released lock will cause a **deadlock**."

Calls to **lock** and **unlock** must **alternate**.

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Property 2: Drop Root Privilege



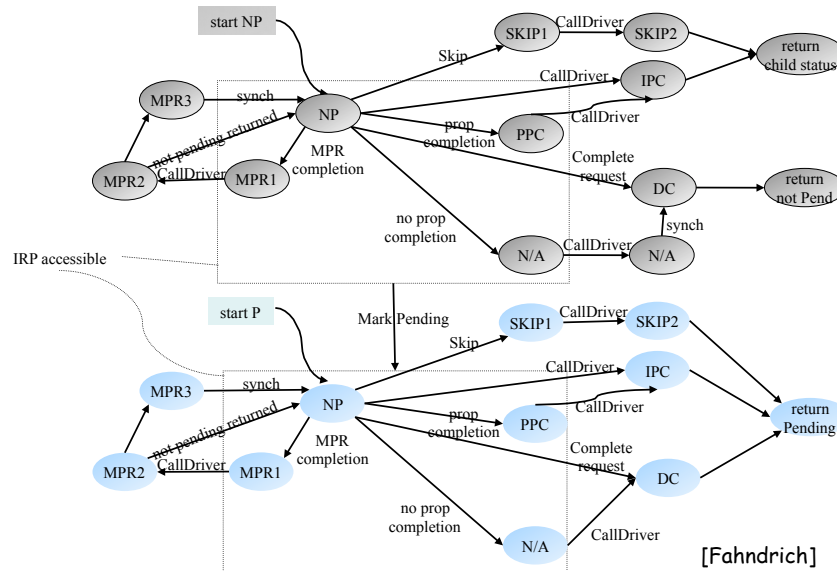
[Chen-Wagner-Dean '02]

"User applications must not run with root privilege"

When **execv** is called, must have **suid** \neq 0

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Property 3 : IRP Handler



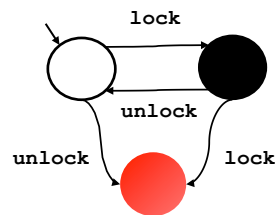
[Fahndrich] 9

Example SLAM Input

```

Example ( ) {
1: do{
    lock();
    old = new;
    q = q->next;
2:   if (q != NULL){
3:     q->data = new;
    unlock();
    new ++;
  }
4: } while(new != old);
5: unlock();
  return;
}

```



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SLAM in a Nutshell

```

SLAM(Program p, Spec s) =
  Program q = incorporate_spec(p,s);           // slic
  PredicateSet abs = { };
  while true do
    BooleanProgram b = abstract(q,abs);        // c2bp
    match model_check(b) with                  // bebop
    | No_Error  $\Rightarrow$  print("no bug"); exit(0)
    | Counterexample(c)  $\Leftrightarrow$ 
      if is_valid_path(c, p) then              // newton
        print("real bug"); exit(1)
      else
        abs  $\Leftarrow$  abs  $\cup$  new_preds(c)        // newton
  done
  
```

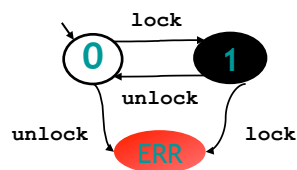
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Incorporating Specs

```

Example ( ) {
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    old = new;
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5: unlock();
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```

Ideas?



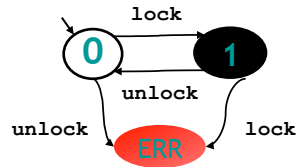
#12

Incorporating Specs

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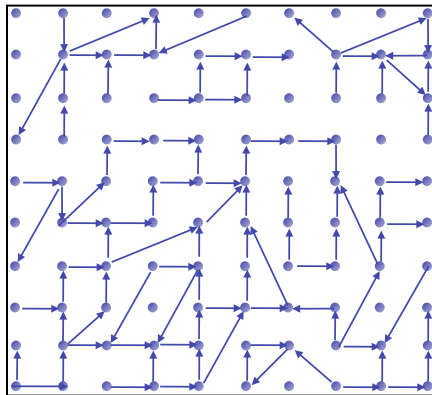
```

Example ( ) {
1: do{
    if L=1 goto ERR;
    else L=1;
    old = new;
    q = q->next;
2:   if (q != NULL){
3:     q->data = new;
        if L=0 goto ERR;
        else L=0;
        new ++;
    }
4: } while(new != old);
5: if L=0 goto ERR;
   else L=0;
   return;
ERR: abort();
}

```

Original program
violates spec iff
new program
reaches ERR

Program As Labeled Transition System



State

Transition

$pc \mapsto 3$
 $lock \mapsto \bullet$
 $old \mapsto 5$
 $new \mapsto 5$
 $q \mapsto 0x133a$

```

3: unlock();
   new++;
4: } ...

```

$pc \mapsto 4$
 $lock \mapsto \circ$
 $old \mapsto 5$
 $new \mapsto 6$
 $q \mapsto 0x133a$

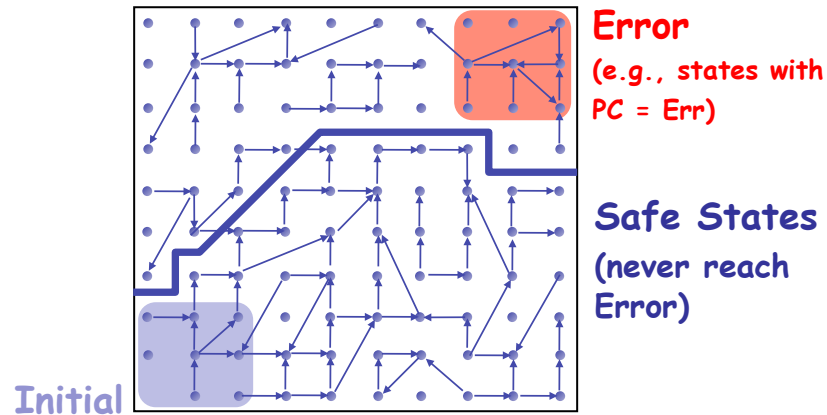
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```

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The Safety Verification Problem



Is there a **path** from an **initial** to an **error** state ?

Problem? Infinite state graph (old=1, old=2, old=...)

Solution? Set of states \simeq logical formula

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Representing [Sets of States] as Formulas

$[F]$ states satisfying F $\{s \mid s \models F\}$	F FO formula over program vars
$[F_1] \cap [F_2]$	$F_1 \wedge F_2$
$[F_1] \cup [F_2]$	$F_1 \vee F_2$
$\overline{[F]}$	$\neg F$
$[F_1] \subseteq [F_2]$	

i.e. $F_1 \wedge \neg F_2$ unsatisfiable

Representing [Sets of States] as Formulas

$[F]$

states satisfying F $\{s \mid s \models F\}$

F

FO formula over program vars

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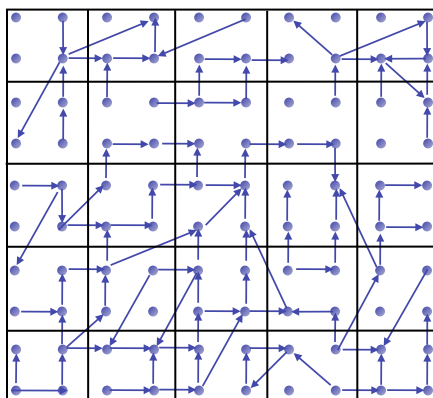
$\neg F$

$[F_1] \subseteq [F_2]$

$F_1 \Rightarrow F_2$

i.e. $F_1 \wedge \neg F_2$ unsatisfiable

Idea 1: Predicate Abstraction



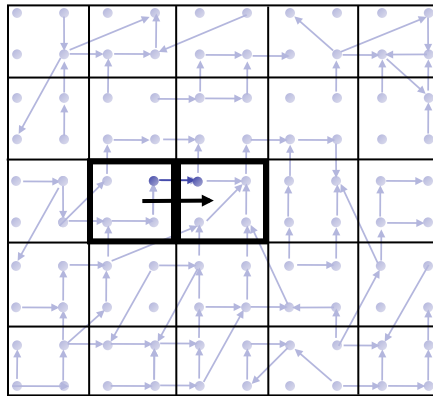
- **Predicates** on program state:
 $\text{old} \neq \text{new}$ lock (i.e., $\text{lock} = \text{true}$)
 $\text{old} = \text{new}$

- States satisfying **same** predicates are **equivalent**
 - Merged into one **abstract state**

Why?

- Num of abstract states is **finite**
 - Thus **model-checking the abstraction will be feasible!**

Abstract States and Transitions



State



Transition



pc \mapsto 3
lock \mapsto ●
old \mapsto 5
new \mapsto 5
q \mapsto 0x133a

```
3: unlock();
   new++;
4: } ...
```

pc \mapsto 4
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new \mapsto 6
q \mapsto 0x133a



Theorem Prover

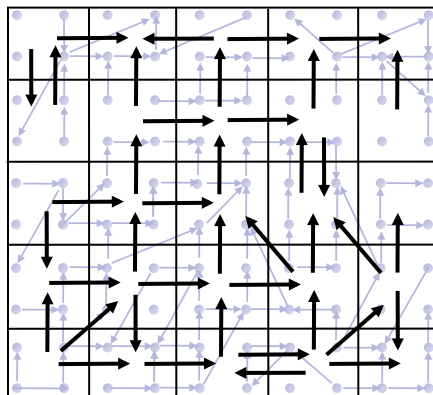


lock
old=new

\neg lock
 \neg old=new

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Abstraction



State



Transition



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lock \mapsto ●
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Theorem Prover



lock
old=new

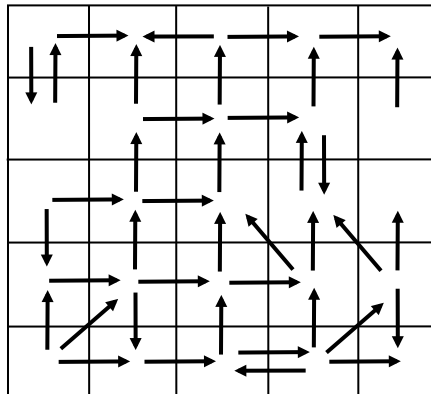
\neg lock
 \neg old=new

Existential Lifting

(i.e., $A_1 \xrightarrow{\exists} A_2$ iff $\exists c_1 \in A_1. \exists c_2 \in A_2. c_1 \rightarrow c_2$)

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Abstraction



State



Transition



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 $lock \mapsto \bullet$
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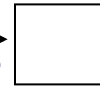
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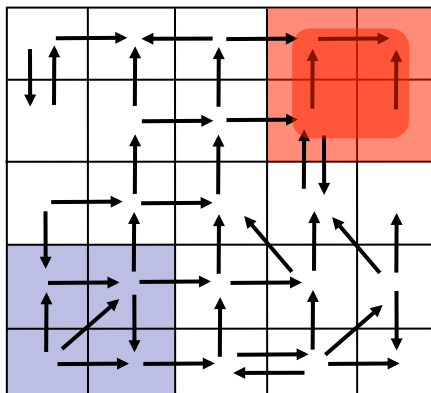


$lock$
 $old=new$

$\neg lock$
 $\neg old=new$

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Analyze Abstraction



Analyze finite graph

Over Approximate

Safe \Rightarrow System Safe

No **false negatives**

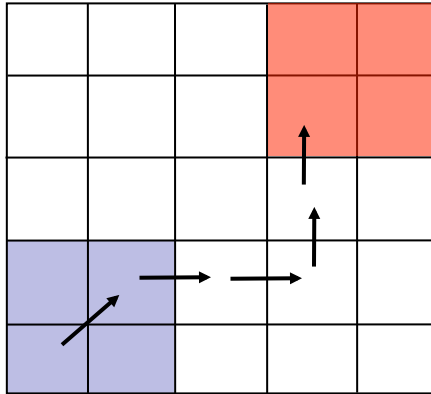
Problem

Spurious **counterexamples**

false positives

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Idea 2: Counterexample-Guided Refinement

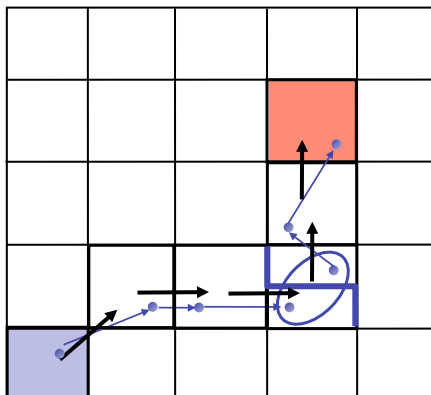


Solution

Use spurious **counterexamples** to **refine** abstraction!

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Idea 2: Counterexample-Guided Refinement



Solution

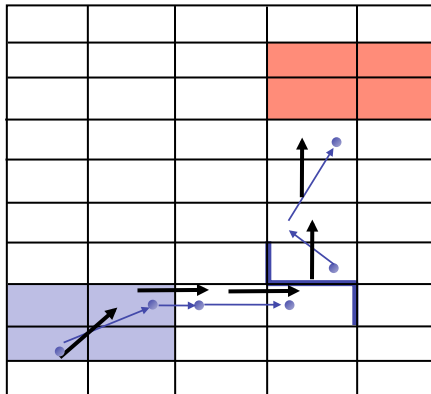
Use spurious **counterexamples** to **refine** abstraction!

1. **Add predicates** to distinguish states across **cut**
2. Build **refined** abstraction

Imprecision due to **merge**

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Iterative Abstraction-Refinement



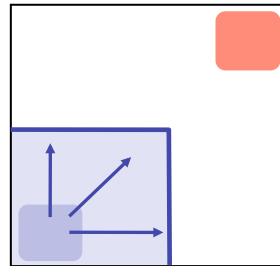
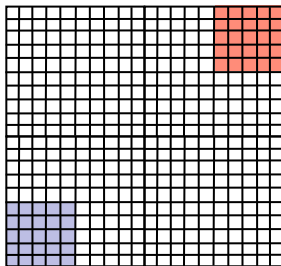
[Kurshan et al 93] [Clarke et al 00]
[Ball-Rajamani 01]

Solution

Use spurious **counterexamples** to **refine** abstraction!

1. **Add predicates** to distinguish states across **cut**
2. Build **refined** abstraction
 - eliminates counterexample
3. **Repeat** search until real counterexample or system proved safe ²⁵

Problem: Abstraction is Expensive Why?



Reachable

Problem

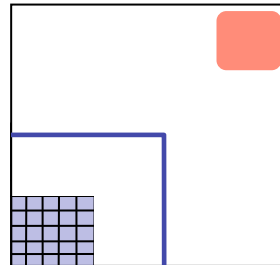
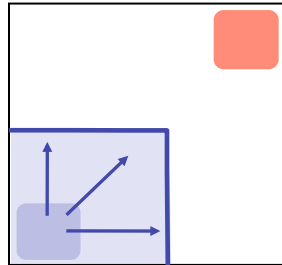
#abstract states = $2^{\text{\#predicates}}$
Exponential Thm. Prover queries

Observe

Fraction of state space reachable
#Preds ~ 100's, #States ~ 2^{100} ,
#Reach ~ 1000's

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Solution1: Only Abstract Reachable States



Safe

Problem

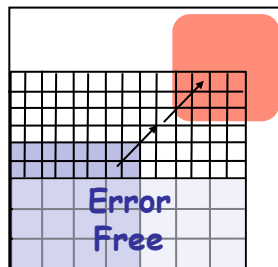
#abstract states = $2^{\text{\#predicates}}$
Exponential Thm. Prover queries

Solution

Build abstraction **during** search

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Solution2: Don't Refine Error-Free Regions



Problem

#abstract states = $2^{\text{\#predicates}}$
Exponential Thm. Prover queries

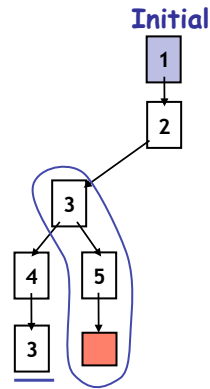
Solution

Don't refine error-free regions

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Key Idea for Solutions?

Key Idea: Reachability Tree



Unroll Abstraction

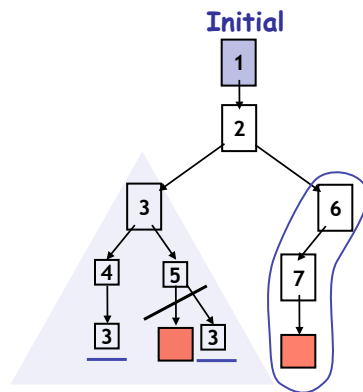
1. Pick tree-node (=abs. state)
2. Add children (=abs. successors)
3. On **re-visiting** abs. state, **cut-off**

Find min infeasible suffix

- Learn new predicates
- Rebuild subtree with new preds.

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Key Idea: Reachability Tree



Error Free

Unroll Abstraction

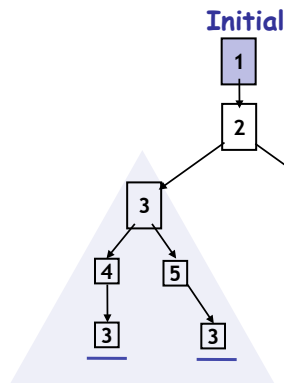
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32

Key Idea: Reachability Tree



Unroll Abstraction

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Find min infeasible suffix

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Error Free

SAFE

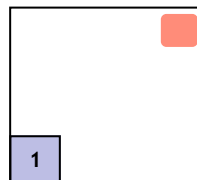
S1: Only Abstract Reachable States

S2: Don't refine error-free regions 33

Build-and-Search

```
Example ( ) {
1: do{
    lock();
    old = new;
    q = q->next;
2:   if (q != NULL){
3:     q->data = new;
    unlock();
    new ++;
  }
4: }while(new != old);
5: unlock();
}
```

1 \neg LOCK



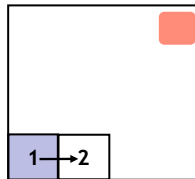
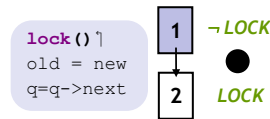
Predicates: LOCK

Reachability Tree 34

Build-and-Search

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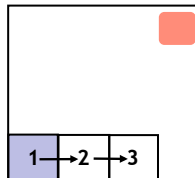
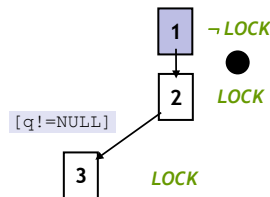
Predicates: **LOCK**

Reachability Tree 35

Build-and-Search

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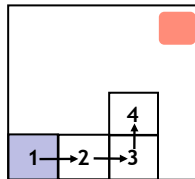
Predicates: **LOCK**

Reachability Tree 36

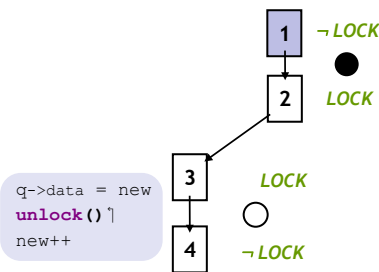
Build-and-Search

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Predicates: LOCK

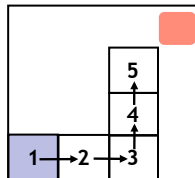


Reachability Tree 37

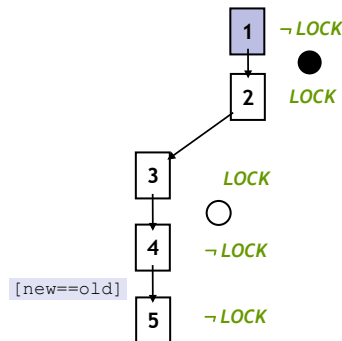
Build-and-Search

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Predicates: LOCK

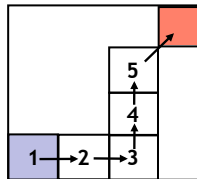


Reachability Tree 38

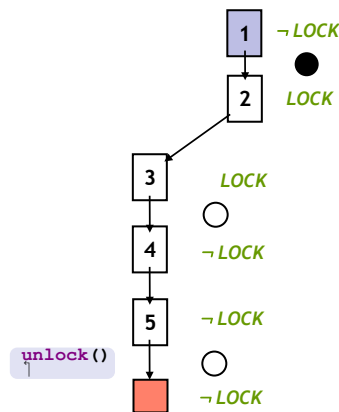
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Predicates: **LOCK**

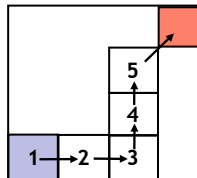


Reachability Tree 39

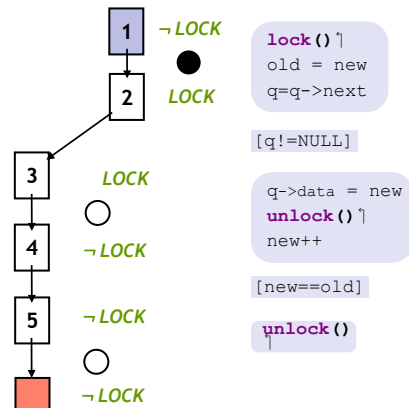
Analyze Counterexample

```

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Predicates: **LOCK**

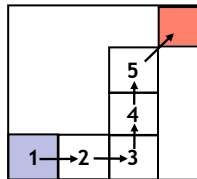


Reachability Tree 40

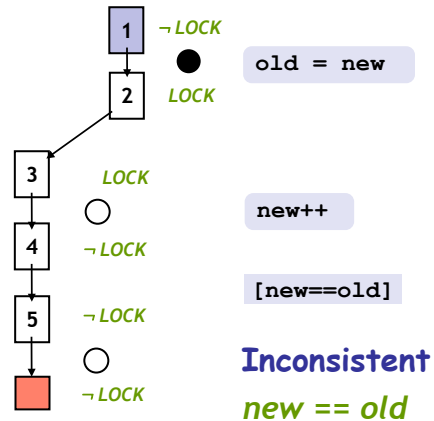
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Predicates: **LOCK**

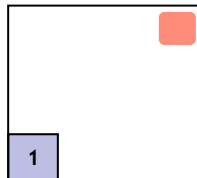


Reachability Tree 41

Repeat Build-and-Search

```

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```



Predicates: **LOCK, new == old**

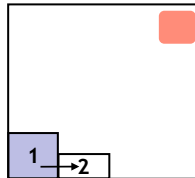
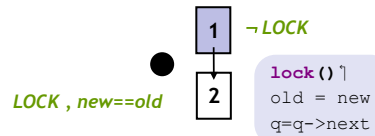


Reachability Tree 42

Repeat Build-and-Search

```

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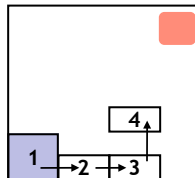
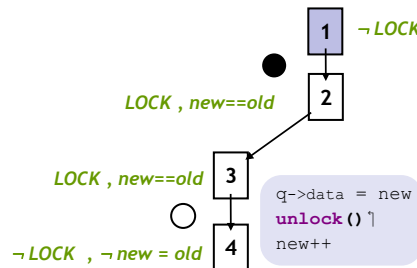
Predicates: $LOCK, new == old$

Reachability Tree 43

Repeat Build-and-Search

```

Example ( ) {
1: do{
    lock();
    old = new;
    q = q->next;
2:   if (q != NULL){
3:     q->data = new;
    unlock();
    new ++;
    }
4: }while (new != old);
5: unlock();
}
    
```



Predicates: $LOCK, new == old$

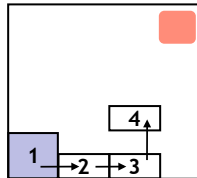
Reachability Tree 44

Repeat Build-and-Search

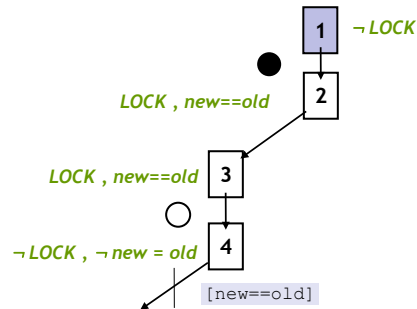
```

Example ( ) {
1: do{
    lock();
    old = new;
    q = q->next;
2:   if (q != NULL){
3:     q->data = new;
    unlock();
    new ++;
  }
4: }while(new != old);
5: unlock();
}

```



Predicates: $LOCK, new == old$



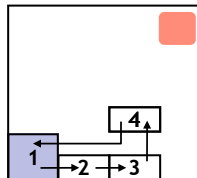
Reachability Tree 45

Repeat Build-and-Search

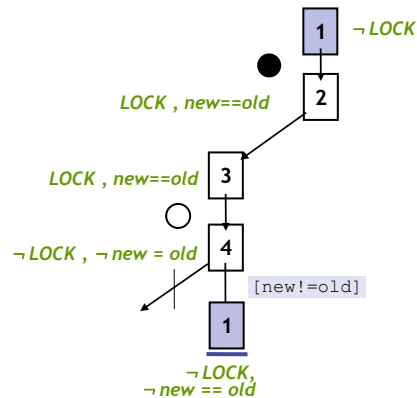
```

Example ( ) {
1: do{
    lock();
    old = new;
    q = q->next;
2:   if (q != NULL){
3:     q->data = new;
    unlock();
    new ++;
  }
4: }while(new != old);
5: unlock();
}

```



Predicates: $LOCK, new == old$



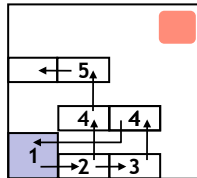
Reachability Tree 46

Repeat Build-and-Search

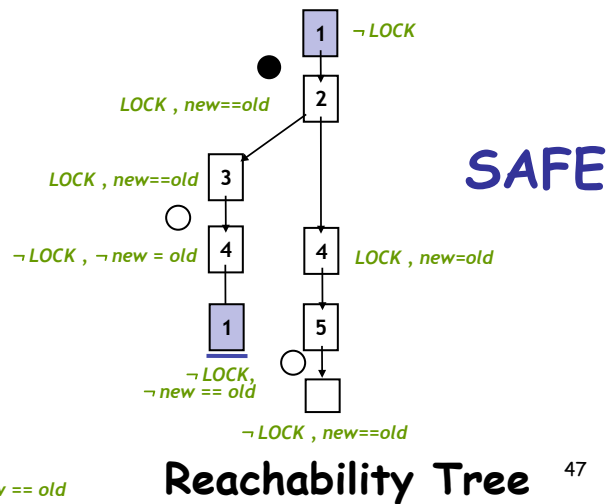
```

Example ( ) {
1: do{
    lock();
    old = new;
    q = q->next;
2:   if (q != NULL){
3:     q->data = new;
    unlock();
    new ++;
    }
4: }while(new != old);
5: unlock();
}

```

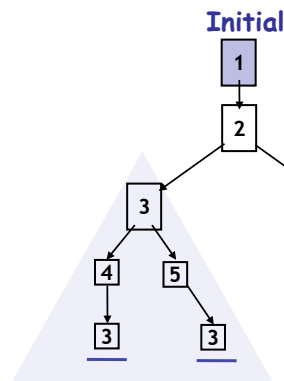


Predicates: $LOCK, new == old$



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Key Idea: Reachability Tree



Error Free

SAFE

Unroll Abstraction

1. Pick tree-node (=abs. state)
2. Add children (=abs. successors)
3. On re-visiting abs. state, cut-off

Find min infeasible suffix

- Learn new predicates
- Rebuild subtree with new preds.

S1: Only Abstract Reachable States

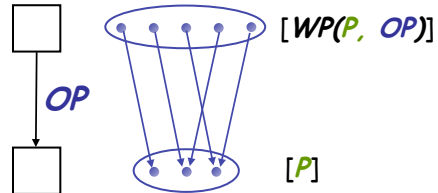
S2: Don't refine error-free regions

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Weakest Preconditions

$WP(P, OP)$

Weakest formula P' s.t.
if P' is true before OP
then P is true after OP



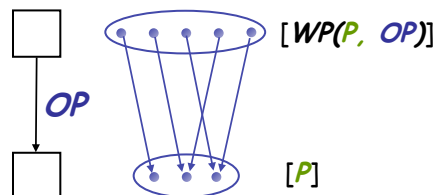
51

Weakest Preconditions

More on this later in the semester!

$WP(P, OP)$

Weakest formula P' s.t.
if P' is true before OP
then P is true after OP



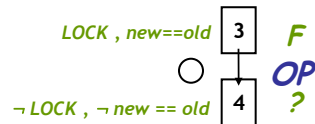
52

How to compute successor?

```

Example ( ) {
1: do{
    lock();
    old = new;
    q = q->next;
2:   if (q != NULL){
3:     q->data = new;
    unlock();
    new ++;
  }
4: }while(new != old);
5: unlock();
}

```



For each p

- Check if p is true (or false) after OP

Q: When is p true after OP ?

- If $WP(p, OP)$ is true before OP !
- We know F is true before OP
- Thm. Pvr. Query: $F \Rightarrow WP(p, OP)$

Predicates: $LOCK, new == old$

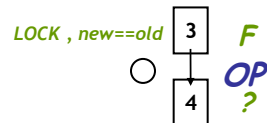
53

How to compute successor?

```

Example ( ) {
1: do{
    lock();
    old = new;
    q = q->next;
2:   if (q != NULL){
3:     q->data = new;
    unlock();
    new ++;
  }
4: }while(new != old);
5: unlock();
}

```



For each p

- Check if p is true (or false) after OP

Q: When is p false after OP ?

- If $WP(\neg p, OP)$ is true before OP !
- We know F is true before OP
- Thm. Pvr. Query: $F \Rightarrow WP(\neg p, OP)$

Predicates: $LOCK, new == old$

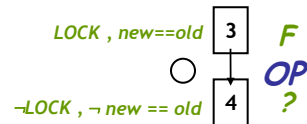
54

How to compute successor?

```

Example ( ) {
1: do{
    lock();
    old = new;
    q = q->next;
2:   if (q != NULL){
3:     q->data = new;
    unlock();
    new++;
  }
4: }while(new != old);
5: unlock();
}

```



For each p

- Check if p is true (or false) after OP

Q: When is p false after OP ?

- If $WP(\neg p, OP)$ is true before OP !
- We know F is true before OP
- Thm. Pvr. Query: $F \Rightarrow WP(\neg p, OP)$

Predicate: $new == old$

True? $(LOCK, new == old) \Rightarrow (new + 1 = old)$ **NO**

False? $(LOCK, new == old) \Rightarrow (new + 1 \neq old)$ **YES**

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Advanced SLAM/BLAST

Too Many Predicates

- Use Predicates Locally

Counter-Examples

- Craig Interpolants

Procedures

- Summaries

Concurrency

- Thread-Context Reasoning

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SLAM Summary

- 1) Instrument Program With Safety Policy
- 2) Predicates = { }
- 3) Abstract Program With Predicates
 - Use **Weakest Preconditions and Theorem Prover Calls**
- 4) Model-Check Resulting Boolean Program
 - Use **Symbolic Model Checking**
- 5) Error State Not Reachable?
 - Original Program Has **No Errors: Done!**
- 6) Check Counterexample Feasibility
 - Use **Symbolic Execution**
- 7) Counterexample Is Feasible?
 - Real **Bug: Done!**
- 8) Counterexample Is Not Feasible?
 - 1) Find New Predicates (Refine Abstraction)
 - 2) Goto Line 3

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Bonus: SLAM/BLAST Weakness

```

1: F() {
2:   int x=0;
3:   lock();
4:   x++;
5:   while (x ≠
      88);
6:   if (x < 77) {
7:     lock();
8:   }

```

- Preds = {}, Path = 234567
- [x=0, ¬x+1≠88, x+1<77]
- Preds = {x=0}, Path = 234567
- [x=0, ¬x+1≠88, x+1<77]
- Preds = {x=0, x+1=88}
- Path = 23454567
- [x=0, ¬x+2≠88, x+2<77]
- Preds = {x=0, x+1=88, x+2=88}
- Path = 2345454567
- ...
- Result: the predicates
"count" the loop iterations₅₈

For Next Time

- Post about today's class and reading