An in-context learning framework for control

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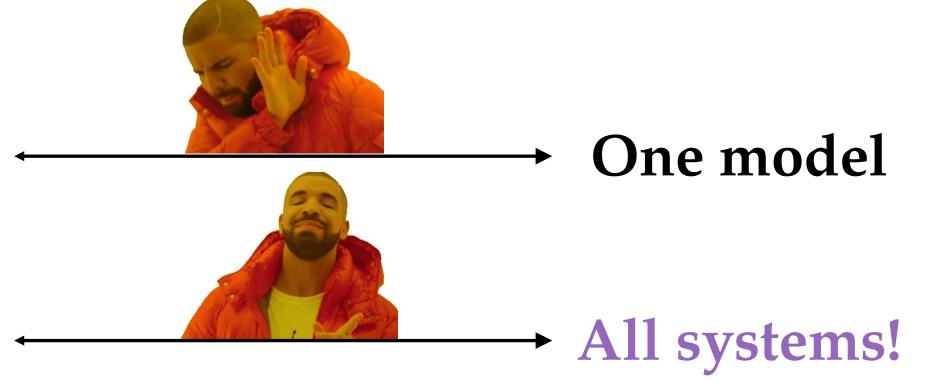
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In-context learning approach

- Design of a unified model, estimator or controller from data $\mathcal{D} = \left\{D^{(i)}\right\}_{i=1}^{M} \text{ of a class of } similar \text{ systems } \mathcal{S} = \bigcup_{i=1}^{M} S^{(i)}$
- Transformers are trained for the class, but can adapt to the specific system extrapolating the context from data

One system

One model

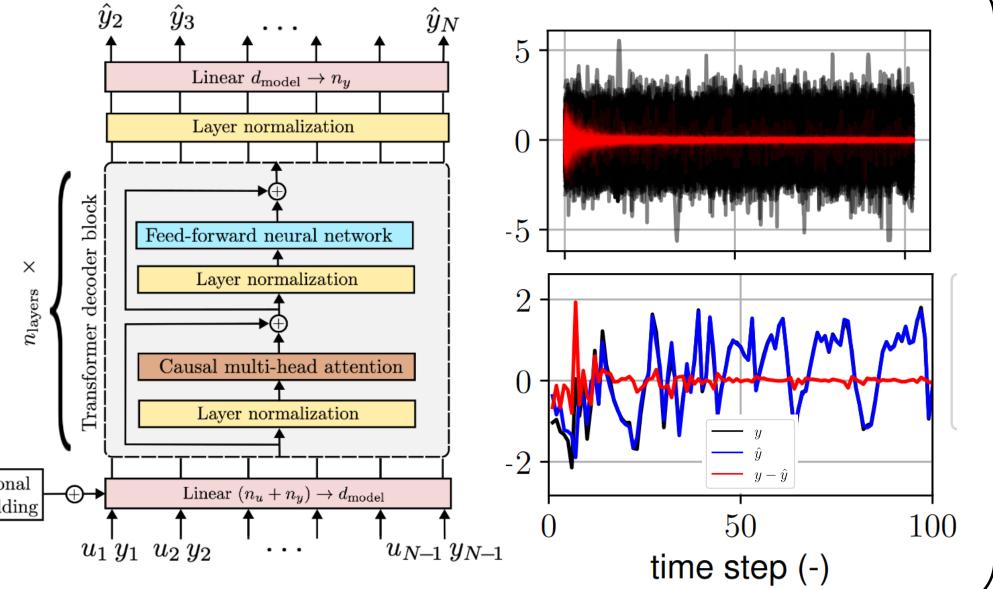




Paper link

System Identification

- Original work of Marco Forgione, Filippo Pura, and Dario Piga. "From system models to class models: An in-context learning paradigm." *IEEE Control Systems Letters* (2023).
- Goal: one-step prediction $\hat{y}_{k+1} = \mathcal{M}_{\phi}(u_{1:k}, y_{1:k}), \ \forall S \in \mathcal{S}$
- Context is understood from input/output data $D^{(i)} = (u_{1:N}^{(i)}, y_{1:N}^{(i)})$
- Learning from (potentially infinite) set of similar systems through a simulator
- Excellent performance on nonlinear systems (Class of WH systems)



Paper in preparation.. stay tuned

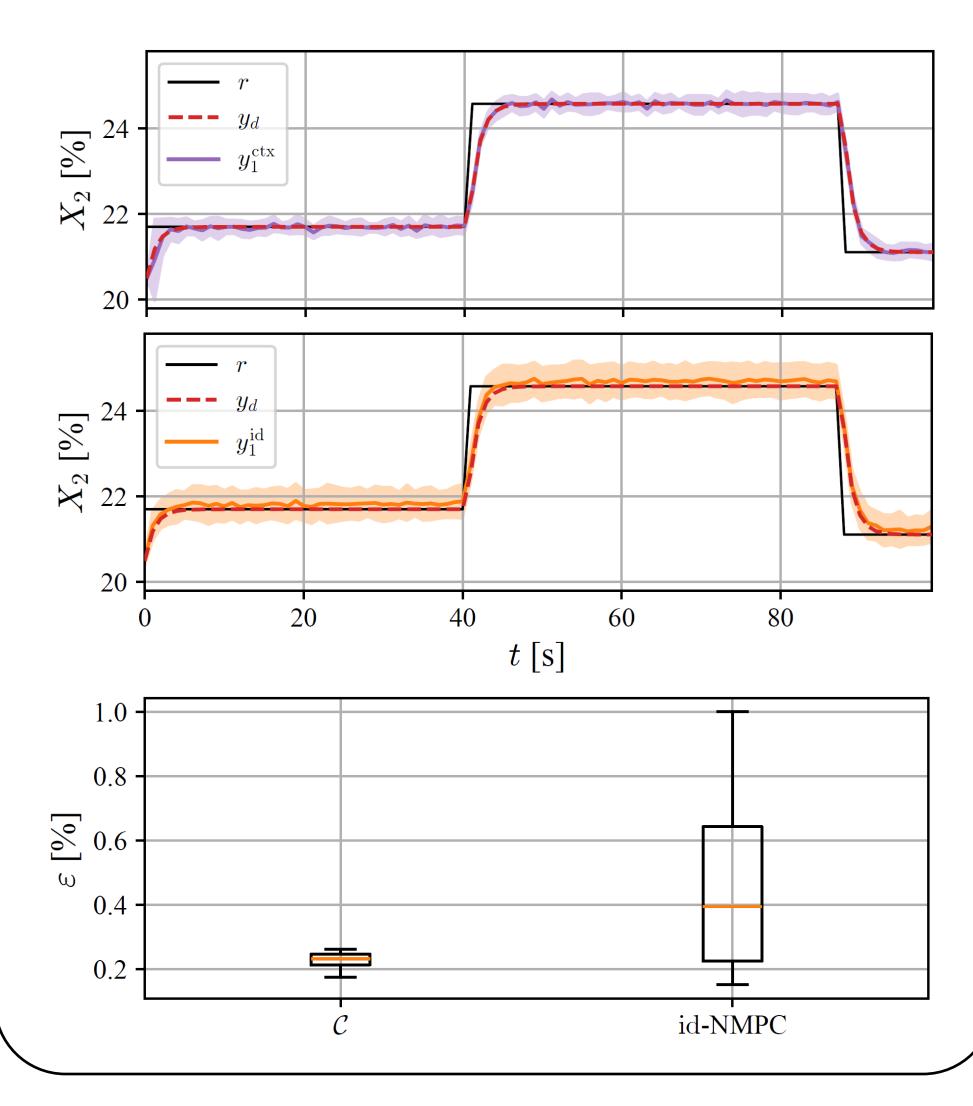
Control

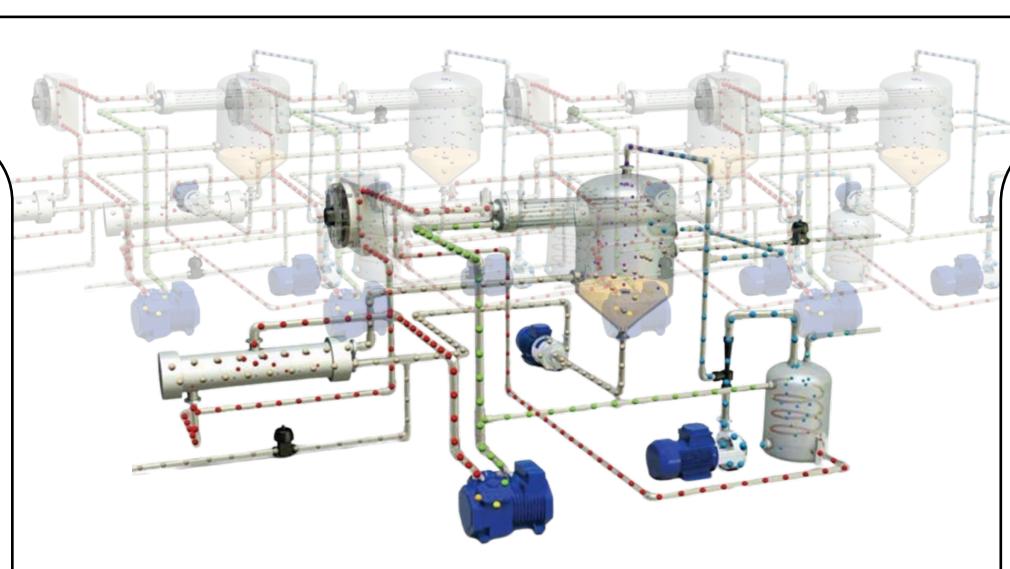
$$\hat{u}_k = \mathcal{C}_{\phi}(e_{1:k}, u_{0:k-1})$$

• Goal: model reference control

$$\min_{\phi} \mathbb{E}_{p(\mathcal{D})} \left[\sum_{k=1}^{N-1} \left\| u_k^{\star} - \mathcal{C}_{\phi}(e_{1:k}, u_{0:k-1}) \right\|_2^2 \right]$$

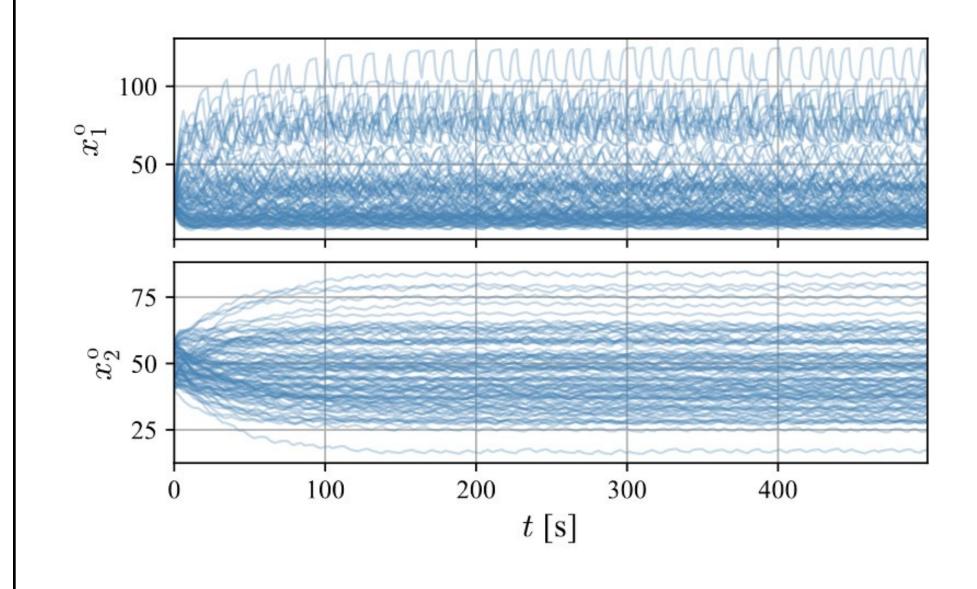
- Context is understood from errors $e_{1:k}$ and inputs $u_{0:k-1}$
- Matching error is reduced with respect to NMPC





Example: evaporation process

- Nonlinear benchmark
- Class *S* described by 19 parameters, each perturbed by 5-20%



Future works





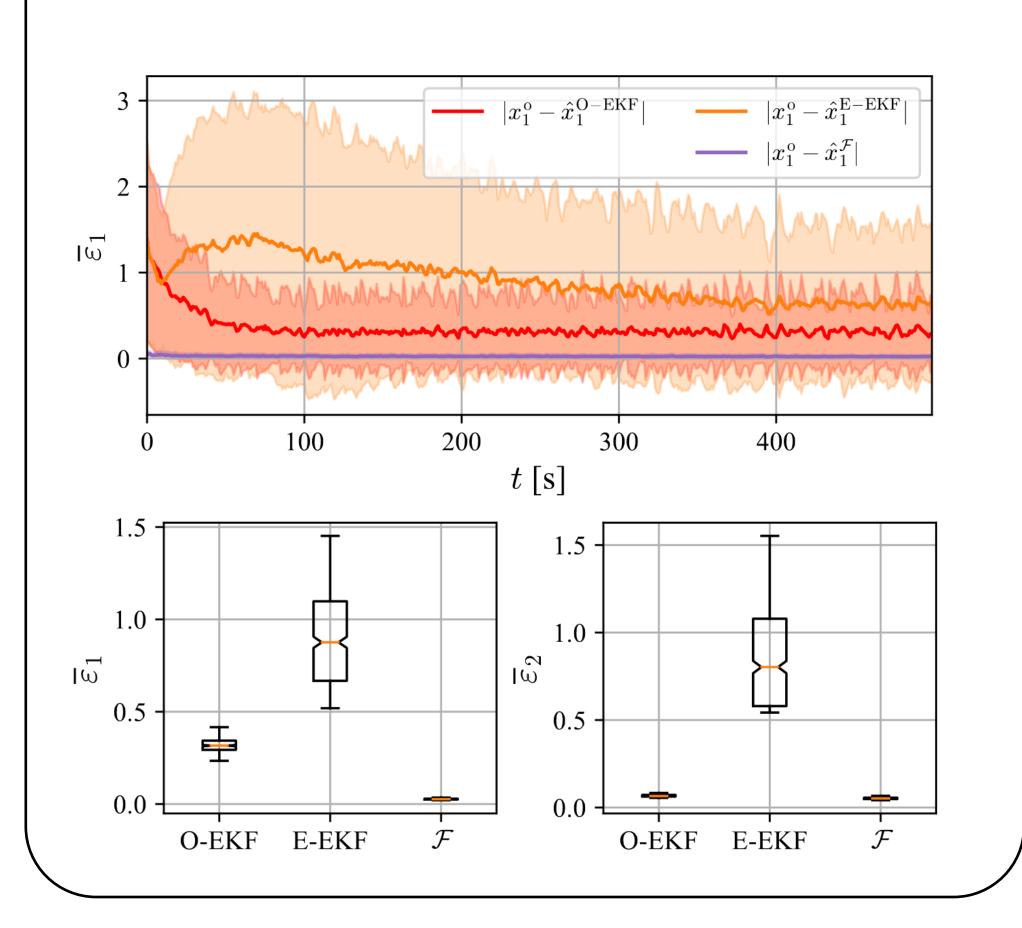
State Estimation

$$\widehat{x}_k = \mathcal{F}_{\phi}(u_{1:k}, y_{1:k}),$$

Goal: state estimation

$$\min_{\phi} \mathbb{E}_{p(\mathcal{D})} \left[\sum_{k=1}^{N-1} \left\| x_k^{o} - \mathcal{F}_{\phi}(u_{1:k}, y_{1:k}) \right\|_2^2 \right]$$

- Context is undestood from inputs $u_{1:k}$ and outputs $y_{1:k}$
- Estimation error is reduced with respect to EKF



- Experimental validation on applications
- Architectural modifications to speed up learning
- Formal results on properties of the approach (stability, effect of noise)