

Name: Peter RauscherDate: 09/17/2001

Pledge: I pledge my honor that I have abided by the Stevens Honor System.

Give the complexity of the following functions. Choose the most appropriate notation from among  $O$ ,  $\theta$ , and  $\Omega$ .

```
1. void function1(int n) {
    for (int i = 1; i <= n; i++) {
        for (int j = i; j <= n; j += 2) {
            cout << "*";
        }
    }
}
```

Answer:  $\theta(n^2)$ 

```
2. void function2(int n) {
    int count = 0;
    for (int i = 1; i * i * i <= n; i++) {
        count++;
    }
    cout << count;
}
```

Answer:  $\theta(\log_3 n)$ 

```
3. void function3(int n) {
    int count = 0;
    for (int i = 1; i * i <= n; i++) { //log3n
        for (int j = 1; j + n/2 <= n; j++) { // n/2
            for (int k = 1; k <= n; k *= 2) { // logn
                count++;
            }
        }
    }
    cout << count;
}
//
```

Answer:  $\theta(n \cdot \log n \cdot \log_3 n)$ 

```
4. void function4(int n) {
    int count = 0;
    for (int i = n/2; i <= n; i++) { // n/2
        for (int j = 1; j <= n; j *= 2) { // logn
            for (int k = 1; k <= n; k *= 2) { //logn
                count++;
            }
        }
    }
    cout << count;
}
```

Answer:  $\theta(n \log n)$

```
5. void function5(int n) {
    if (n % 2 == 0) {
        return;
    }
    for (int i = 1; i <= n; i++) {
        for (int j = 1; j <= n; j++) {
            cout << "*";
            break;
        }
    }
}
```

Answer:  $O(n^2)$

```
6. void function6(int n) {
    int count = 0;
    for (int i = 1; i <= n/2; i++) {
        for (int j = 1; j <= n/3; j++) {
            for (int k = 1; k <= n/4; k++) {
                count++;
            }
        }
    }
    cout << count;
}
```

Answer:  $\theta(n^3)$

```
7. void function7(int n) {
    for (int i = 1; i <= n; i++) {
        for (int j = 1; j <= n; j += i) {
            cout << "*";
        }
    }
}
```

Answer:  $\theta(n \log n)$

```
8. void function8(int n) {
    int i = 1, s = 1;
    while (s <= n) {
        i++;
        s += i;
        cout << "*";
    }
}
```

Answer:  $\theta(\log n)$

#### 9. Processing Arrays

- a. Suppose you have an unsorted array of integers of length  $n$  and want to sum all the elements inside it. What is the running time of your algorithm?  $\theta(n)$

- b. Suppose you have an unsorted array of integers of length  $n$  and want to determine if all the values inside are positive. What is the running time of your algorithm?  $\theta(\mathbf{n})$
- c. Suppose you have a sorted array of integers of length  $n$  and want to determine the median value. What is the running time of your algorithm?  $\theta(\mathbf{n})$

10. **I** T / F  $f(n) = 5n^2 + 4n + 8 \in \theta(n^2)$

If true, prove it by giving *integral* values for the required constants  $c_1$ ,  $c_2$ , and  $n_0$ . Choose the tightest values possible for the  $c_1$  and  $c_2$  constants. If false, show the contradiction.

$$c_1 n^2 \leq 5n^2 + 4n + 8 \leq c_2 n^2$$

$$c_1 \leq 5 + 4/n + 8/n^2 \leq c_2$$

$$c_1 =$$

$$c_2 =$$

$$n_0 =$$