# MATH 3341: Introduction to Scientific Computing Lab

Melissa Butler

University of Wyoming

October 11, 2021



Lab 08: MATLAB Interpolation Routines and Their Derivatives



#### Polynomial Interpolation Routines



#### polyfit and polyval

• p = polyfit(xdata, ydata, n): finds the coefficients of a polynomial p(x) of degree n, i.e.,  $p(x) = p_1 x^n + p_2 x^{n-1} + \cdots + p_n x + p_{n+1}$ , that fits the data xdata, ydata best in a least-squares sense. p is a row vector of length n + 1 containing the polynomial coefficients in

descending powers, p stores  $[p_1, p_2, \dots, p_n, p_{n+1}]$ .



#### polyfit and polyval

- p = polyfit(xdata, ydata, n): finds the coefficients of a polynomial p(x) of degree n, i.e.,  $p(x) = p_1 x^n + p_2 x^{n-1} + \cdots + p_n x + p_{n+1}$ , that fits the data xdata, ydata best in a least-squares sense. p is a row vector of length n + 1 containing the polynomial coefficients in descending powers, p stores  $[p_1, p_2, \dots, p_n, p_{n+1}]$ .
- y = polyval(p, x): returns the value of a polynomial p evaluated at x:  $y = p(x) = p_1 x^n + p_2 x^{n-1} + \cdots + p_n x + p_{n+1}$ .



## polyfit and polyval

- p = polyfit(xdata, ydata, n): finds the coefficients of a polynomial p(x) of degree n, i.e.,  $p(x) = p_1 x^n + p_2 x^{n-1} + \cdots + p_n x + p_{n+1}$ , that fits the data xdata, ydata best in a least-squares sense. p is a row vector of length n + 1 containing the polynomial coefficients in descending powers, p stores  $[p_1, p_2, \dots, p_n, p_{n+1}]$ .
- y = polyval(p, x): returns the value of a polynomial p evaluated at x:  $y = p(x) = p_1 x^n + p_2 x^{n-1} + \cdots + p_n x + p_{n+1}$ .



• pp = spline(xdata, ydata): Use cubic spline (piecewise cubic polynomial) to fit the data xdata and ydata. pp is a struct (structure) contains number of pieces of cubic polynomials (pp.pieces), coefficients matrix (pp.coefs) of which the ith row are the coeffcients for the ith piece cubic polynomial, break points (pp.breaks) which is a row vector contains the endpoints of the interval for each pieces.



- pp = spline(xdata, ydata): Use cubic spline (piecewise cubic polynomial) to fit the data xdata and ydata. pp is a struct (structure) contains number of pieces of cubic polynomials (pp.pieces), coefficients matrix (pp.coefs) of which the ith row are the coeffcients for the ith piece cubic polynomial, break points (pp.breaks) which is a row vector contains the endpoints of the interval for each pieces.
- pp = pchip(xdata, ydata): Use Piecewise Cubic Hermite Interpolating Polynomial to fit the data xdata and ydata. pp is same as above.



- pp = spline(xdata, ydata): Use cubic spline (piecewise cubic polynomial) to fit the data xdata and ydata. pp is a struct (structure) contains number of pieces of cubic polynomials (pp.pieces), coefficients matrix (pp.coefs) of which the ith row are the coeffcients for the ith piece cubic polynomial, break points (pp.breaks) which is a row vector contains the endpoints of the interval for each pieces.
- pp = pchip(xdata, ydata): Use Piecewise Cubic Hermite Interpolating Polynomial to fit the data xdata and ydata. pp is same as above.
- y = ppval(pp, x): determines which intervals x lies on and then evaluate the corresponding cubic polynomial at x.



- pp = spline(xdata, ydata): Use cubic spline (piecewise cubic polynomial) to fit the data xdata and ydata. pp is a struct (structure) contains number of pieces of cubic polynomials (pp.pieces), coefficients matrix (pp.coefs) of which the ith row are the coeffcients for the ith piece cubic polynomial, break points (pp.breaks) which is a row vector contains the endpoints of the interval for each pieces.
- pp = pchip(xdata, ydata): Use Piecewise Cubic Hermite Interpolating Polynomial to fit the data xdata and ydata. pp is same as above.
- y = ppval(pp, x): determines which intervals x lies on and then evaluate the corresponding cubic polynomial at x.
- y = spline(xdata, ydata, x): is the same as y = ppval(spline(xdata, ydata), x), thus providing, in y, the values of the interpolant at x.



#### Example:



Derivatives of Interpolation Polynomials



#### polyder: Differentiate polynomial

• dp = polyder(p): returns the derivative of the polynomial whose coefficients are the elements of vector p.



## polyder: Differentiate polynomial

- dp = polyder(p): returns the derivative of the polynomial whose coefficients are the elements of vector p.
- Example:

p = [4 3 2 1]  
dp = polyder(p) % dp = [12 6 2]  
That is, given a polynomial 
$$p(x) = 5x^3 + 3x^2 + 2x + 1$$
, the

derivative with respect to x is  $p'(x) = 3x^3 + 3x^2 + 2x + 1$ , the

