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INFLUENCE
OF FINAL-STATE INTERACTION
ON CORRELATIONS OF TWO PARTICLES
WITH NEARLY EQUAL MOMENTA

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1. In terms of the model independent point-like one-particle sources emitting unpolarized particles with spin j , the density of emission probability of two identical particles with 4-momenta p_1 and p_2 in space-time points $x_1=(\vec{r}_1, t_1)$ and $x_2=(\vec{r}_2, t_2)$ is given by

$$W(p_1, p_2) \approx 1 + b(p_1, p_2), \quad (1)$$

$$b(p_1, p_2) = g_0 \cos(qx). \quad (2)$$

Here $q = p_1 - p_2$, $x = x_1 - x_2$, $qx = q_0 t - \vec{q} \vec{r}$ and $g_0 = (-1)^{2j} / N(j) ; N(j)$ is the number of spin states: $N(j) = 2j+1$ if the particle mass $m \neq 0$; $N(j) = 2$ if $m=0$ and $j > 0$ (e.g., for photons). Eq. (2) reflects the influence of Bose- or Fermi-statistics on identical particle correlations. It allows one to estimate space-time dimensions of multiparticle emission region. The corresponding method, generalizing the idea of the well-known Brown-Twiss interferometer in astrophysics^{/1/}, has been elaborated by Kopylov and Podgoretsky^{/2-4/} and also by Cocconi^{/5/} and is successfully applied in a number of experimental papers.

However, eq. (2) does not allow for the effect of final-state interaction of identical particles. In general aspect, the final-state interaction was first discussed by Watson^{/6/} and Migdal^{/7/}. Later on various manifestations of this effect have been considered by many authors. A consistent method allowing for the final-state interaction was developed by Baldin^{/8,9/} in a study of the near threshold pion photoproduction on deuterium. It is important that, as in the case of Bose- or Fermi-statistics effect, the final-state interaction depends on space-time dimensions of particle emission region*.

The final-state interaction is absent for photons. Simple estimates show that its contribution is small for π^+ - or π^- -correlations, but it dominates in nucleon ones. Below we present analytical expressions for the correlation function $b(p_1, p_2)$ of arbitrary particles with $m \neq 0$ (like or unlike, charged or neutral) allowing for their final-state interaction.

* A dependence of such a kind was already pointed out by Baldin and Lebedev^{/10/} in the case of slow pion photoproduction on nuclei.

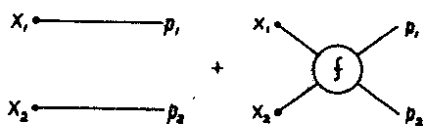


Fig. 1.

Following refs.^{/1-3/} we assume the particles emitted by independent one-particle point-like sources (presumably, it is a reasonable approximation in the case of multiparticle processes). The influence of final-state interaction in

terms of such a model was discussed previously by Kopylov^{/11/} for pions (he allowed only for real intermediate states in the diagram of Fig. 1) and by Koonin^{/12/} for nonrelativistic protons.

For a moment we assume that the production mechanism, as well as the particle interaction, is spin-independent. The function $b(p_1, p_2)$ can be then expressed through non-symmetrized Bethe-Salpeter amplitude $\psi_{p_1 p_2}(x_1, x_2)$, corresponding to a given interaction potential (see, e.g.,^{/13/})

$$b(p_1, p_2) = \left\{ \frac{j+1}{2(2j+1)} |\psi_{p_1 p_2}^*(x_1, x_2) + (-1)^{2j} \psi_{p_2 p_1}^*(x_1, x_2)|^2 + \right. \\ \left. + \frac{j}{2(2j+1)} |\psi_{p_1 p_2}^*(x_1, x_2) - (-1)^{2j} \psi_{p_2 p_1}^*(x_1, x_2)|^2 \right\} - 1, \quad (3)$$

where $(j+1)/(2j+1)$ is the fraction of two-particle states with even and $j/(2j+1)$ with odd summary spin for integer j or the opposite for half-integer j . At equal emission times t_1^* and t_2^* in the two-particle rest frame the amplitude $\psi_{p_1 p_2}^*(x_1, x_2)$, considered as a function of x_1 and x_2 coincides with the usual wave function of two interacting particles having the asymptotics corresponding to the superposition of plane and converging spherical wave^{/14/}. In fact, the approximation $t_1^* = t_2^*$ was used by Koonin when calculating the correlation function of two nonrelativistic protons^{/12/}. Later on we require no special limitations on the emission times t_1^* and t_2^* and also on particle pair velocity in the rest frame of particle sources.

For noninteracting particles the amplitude is given by the product of plane waves: $\psi_{p_1 p_2}^*(x_1, x_2) = e^{-ip_1 x_1} e^{-ip_2 x_2} = e^{-ip(x_1+x_2)} e^{-iqx/2}$, where $p = (p_1 + p_2)/2$. It is seen that in this case the formula (3) yields the correlation function (2). The emission amplitude for interacting particles (see Fig. 1) is given by

$$\psi_{p_1 p_2}(x_1, x_2) = e^{ip(x_1+x_2)} \{ e^{iqx/2} + \phi_{p_1 p_2}(x) \}, \quad (4)$$

$$\phi_{p_1 p_2}(x) = \frac{8\pi\sqrt{p^2}}{(2\pi)^4 i} e^{ipx} \int \frac{e^{-ikx} f(p_1, p_2, \kappa, 2p-\kappa)}{(\kappa^2 - m^2 + i0)((2p-\kappa)^2 + m^2 + i0)} d^4\kappa, \quad (5)$$

where $f(p_1, p_2, \kappa, 2p - \kappa)$ is the nonsymmetrized scattering amplitude analytically continued to the unphysical region. We consider such small relative particle momenta that the contribution of s-wave interaction is dominant. Provided that the intrinsic range d of the interaction potential is smaller than the distance r^* between the emission points in the two-particle rest frame, we can put $f(p_1, p_2, \kappa, 2p-\kappa) \approx f(k^*)$ (see also discussion of eq. (A.9) in Appendix) and take the amplitude f out of the integral in eq. (5):

$$\phi_{p_1 p_2}(x) = f(k^*) \Phi_{p_1 p_2}(x). \quad (6)$$

Here k^* is the momentum of one of the particles in their c.m.s.:

$$k^* = \sqrt{-q^2/2} = \sqrt{p^2 - m^2}, \quad p^2 = m_{12}^2/4; \quad f(k^*) = (e^{2i\delta_0(k^*)} - 1)/2ik^*$$

is the nonsymmetrized s-wave scattering amplitude* and $\Phi_{p_1 p_2}(x)$ is given by eq. (A.1) in Appendix. The integration in this formula can be performed in the approximation of small relative momenta of the particles in their c.m.s. ($k^* \ll m$). The result is given in (A.8).

From eqs. (3-6) it follows that the correlation function takes the form

$$b(p_1, p_2) = b_0(p_1, p_2) + b_i(p_1, p_2), \quad (7)$$

where

$$b_0(b_1, p_2) = g_0 \cos(qx) \quad (8)$$

is the contribution of Bose- or Fermi-statistics effect and $b_i(p_1, p_2)$ appears due to final state s-wave interaction:

$$b_i(p_1, p_2) = g_i \{ |f(k^*) \Phi_{p_1 p_2}(x)|^2 + 2 \operatorname{Re}[f(k^*) \Phi_{p_1 p_2}(x)] \cos(qx/2) \}, \quad (9)$$

$g_i = 1 + g_0$. When polarized (aligned) particles are emitted, the spin factors $g_0 = (-1)^{2j}/(2j+1)$ and g_i in eqs. (8-9) should be changed for $g_0 = \sum_{S=\text{even}} \rho_S - \sum_{S=\text{odd}} \rho_S$ and $g_i = 1 + g_0 = 2 \sum_{S=\text{even}} \rho_S$. Here $\rho_S = \sum_m \rho_{S m}^{S m}$ is the normalized emission probability of identical particles with nearly equal momenta $p_1 \approx p_2 \approx p$ in a state with summary spin S ; $\rho_{S m}^{S' m'}$ are the elements of the two-particle

* The corresponding scattering amplitude for identical particles in a state with summary spin S is equal to $[1 + (-1)^S] f(k^*)$. The cross sections of elastic scattering of two unpolarized identical particles is given by $\sigma = 4\pi(1 + g_0) |f(k^*)|^2$.

spin density matrix in the S, m -representation. If the particles are emitted independently with the same one-particle spin density matrix $\hat{\rho}_{(1)}$, then $\hat{\rho} = \hat{\rho}_{(1)} \otimes \hat{\rho}_{(1)}$ and $g_0 = (-1)^{2j} \text{Sp} \hat{\rho}_{(1)}^2$. In the case of practical interest, when nucleons with polarization P are produced, we have $\hat{\rho}_{(1)} = (1 + P\sigma)/2$ and $g_0 = -(1 + P^2)/2$, $g_i = (1 - P^2)/2$. We see that the contribution of s -wave interaction of two identical nucleons to the correlation function goes to zero at $P \rightarrow 1$ (identical nucleons with parallel spins cannot be in the s -wave state). When the final-state interaction is spin-dependent, the amplitudes $f(k^*)$ can be different in states with different summary spin. The generalization of eqs. (3-6) and (9) is quite transparent. In particular, the function b_i takes the form

$$b_i(p_1, p_2) = 2 \sum_{S=\text{even}} \rho_S \{ |f^S(k^*) \Phi_{p_1 p_2}(x)|^2 + 2 \text{Re}[f^S(k^*) \Phi_{p_1 p_2}(x)] \cos(qx/2) \}. \quad (10)$$

Note that $\rho_S = (2S+1)/(2j+1)^2$ if the production mechanism does not depend on spin projections.

2. The correlation function (7) should be averaged over a space-time distribution of particle sources. The result is denoted as follows:

$$B(q, p) = \langle b_0(p_1, p_2) \rangle + \langle b_i(p_1, p_2) \rangle = B_0(q, p) + B_i(q, p). \quad (11)$$

Below we consider in detail the correlations of two unpolarized neutrons. According to eq. (8), we have

$$B_0(q, p) = -\frac{1}{2} \langle \cos(qx) \rangle. \quad (12)$$

Using formula (6) also inside the range of the interaction potential, eq. (9) yields

$$B_i(q, p) = \frac{1}{2} \{ |f(k^*)|^2 \langle |\Phi_{p_1 p_2}(x)|^2 \rangle + 2 \text{Re}[f(k^*) \langle \Phi_{p_1 p_2}(x) \cos \frac{qx}{2} \rangle] \}. \quad (13)$$

The nn -interaction amplitude in the effective range approximation is of the form^{/14/}

$$f(k^*) = \left(\frac{1}{f_0} + \frac{1}{2} d_0 k^{*2} - ik^* \right)^{-1}. \quad (14)$$

According to the experimental data (see, e.g.,^{/15/}), the scattering length f_0 and the effective radius d_0 are equal to 17 fm^{*} and 2.7 fm, respectively.

The neutron emission points are assumed to be independent and distributed according to the Gaussian law

* The data on neutron-proton scattering yield the singlet scattering length equal to 23.7 fm^{/14/}. Such a violation of isotopic invariance is not yet completely clarified.

$$W(x_1, x_2) = \frac{1}{(2\pi)^4 r_0^6 \tau_0^2} \exp[-(r_1^2 + r_2^2)/2r_0^2 - (t_1^2 + t_2^2)/2\tau_0^2]. \quad (15)$$

The distribution of $x = x_1 - x_2$ is given by

$$W(x) = \frac{1}{(4\pi)^2 r_0^3 \tau_0} \exp\left(-\frac{r^2}{4r_0^2} - \frac{t^2}{4\tau_0^2}\right). \quad (16)$$

Eqs. (15-16) should be considered only as a convenient way to introduce space-time parameters of the particle production region. The mean-square radius and emission time are equal to $\sqrt{3}r_0$ and τ_0 , respectively (the mean-square space and time distance between the emission points are $\sqrt{2}$ times larger). Note that the parameters $2r_0, \tau_0$ in refs. ^{3,5/} and $\sqrt{2}r_0, \sqrt{2}\tau_0$ in ref. ^{12/} have been used as space-time characteristics of particle production. The averaging in (12) according to the distribution (16) yields the familiar Gaussian transform

$$B_0(q, p) = -\frac{1}{2} \exp(-r_0^2 q^2 - \tau_0^2 p^2). \quad (17)$$

Using the azimuthal symmetry of the functions $W(x)$ in (16) and $\Phi_{p_1 p_2}(x)$ with respect to the particle pair velocity \vec{v} the integration over the azimuthal angle in eq. (13) can be performed:

$$B_1(q, p) = \frac{1}{2} \int 2\pi r_T dr_T dt_L W(x) \{|f(k^*) \Phi_{p_1 p_2}(x)|^2 + \\ + 2\text{Re}[f(k^*) \Phi_{p_1 p_2}(x)] J_0\left(\frac{1}{2} q_T r_T\right) \cos[q_0(r_T - vt)/2v]\}, \quad (18)$$

where L and T denote the vector components parallel and perpendicular to the direction of the velocity \vec{v} ; J_0 is the Bessel function.

We note that in the case of spherically symmetrical distribution of the emission points the correlation function $B(q, p)$ depends only on three variables q_T, q_0 and v (the variables q_L and k^* are given by $q_L = q_0/v$ and $4k^{*2} = -q^2 = q_T^2 + q_0^2/v^2 v^2$; $\gamma = (1 - v^2)^{-1/2}$ is the particle pair Lorentz factor). In the general case it also depends on the directions of the vectors \vec{v} and \vec{q}_T which, in principle, can be used to determine the form of the particle production region ^{3,5/}. If this region moves with beforehand unknown velocity \vec{v}_0 , this parameter will enter into eqs. (17-18) through the Lorentz transformation of 4-momenta q and p into the rest frame of particle sources.

Analysis of eqs. (18) and (A.8) shows and calculations confirm it that for small enough k^* ($k^* \ll m$ and $k^* \ll m r_0/r_0$) the function $\Phi_{p_1 p_2}(x)$ can be approximated by formula (A.5) provided that the condition $\gamma p r_0/r_0 \gg m^{-1}$ is fulfilled; here

$\rho = (r_0^2 + v^2 r_0^2)^{1/2}$. In fact, this condition is fulfilled in many realistic cases of neutron production due to the small reverse neutron mass ($m^{-1} = 0.2$ fm). Inserting (A.5) into eq. (18) and integrating over t^* (see (A.2)), we obtain

$$B_i(q, p) = \frac{1}{4\sqrt{\pi} r_0^2 \gamma \rho} \int r_T dr_T dr_L^* \exp(-r_T^2/4r_0^2 - r_L^{*2}/4\gamma^2 \rho^2) \cdot x \times \left[\frac{|f|^2}{2r^{*2}} + \operatorname{Re}(f) \frac{e^{ik^*r^*}}{r^*} \right] J_0\left(\frac{1}{2} q_T r_T\right) \cos(q_0 r_L^*/2\gamma v) \quad (19)$$

where $r^* = (r_T^2 + r_L^{*2})^{1/2}$.

Eqs. (18-19) yield upper estimates of the function B_i as the relation (6), together with (A.8), or (A.5), overestimates $|\phi_{p_1 p_2}(x)| \approx |\phi_{k^*}(r^*)|$ for $r^* < d$. It is interesting that the correction to eq. (19) can be found without knowledge of the explicit form of $\phi_{k^*}(r^*)$ inside the range of nuclear forces (a similar method has been used by Baldin^{8,9/} to calculate matrix elements for the near threshold pion photoproduction on deuterium). Using the simple relation which follows from the effective radius theory^{16-18/}

$$\frac{1}{4\pi} \int |f| \frac{e^{ik^*r^*}}{r^*} + \cos(k^*r^*)|^2 - |\phi_{k^*}(r^*) + \cos(k^*r^*)|^2 d^3 r^* =$$

$$= |f|^2 \frac{1}{2k^*} \frac{d}{dk^*} \left[\operatorname{Re}\left(\frac{1}{f}\right) \right] \approx \frac{1}{2} |f|^2 d_0, \quad (20)$$

we obtain in the first order of d_0/r_0

$$B_i(q, p) = [\text{expres. (19)}] - \frac{1}{8\sqrt{\pi}} |f|^2 d_0 / \gamma \rho r_0^2. \quad (21)$$

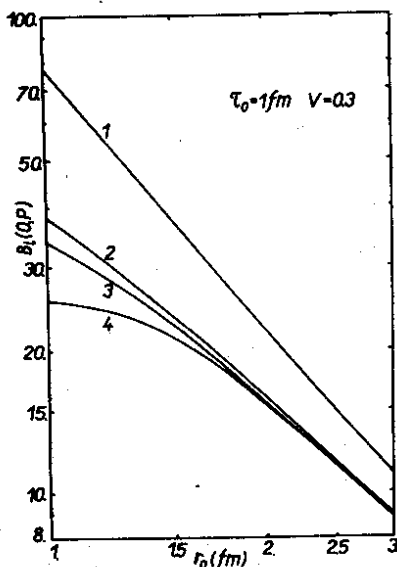
Actually, formula (21) underestimates the function B_i . However, for $r_0 \geq 1.5$ fm the relative error is quite small and rapidly decreases with increasing r_0 (see fig. 2)*. Formula (21) is unreliable for $r_0 \leq 1$ fm when the function B_i is almost entirely determined by the behaviour of the neutron wave function inside the range of the interaction potential and is sensitive to the potential form.

At $k^* = 0$ the integration in (19) can be performed and eq. (21) yields

$$B_i(0, p) = \frac{1}{\gamma \rho} \left[\frac{1}{4} \frac{|f|^2}{r_0} \left(1 - \frac{1}{2\sqrt{\pi}} \frac{d_0}{r_0} \right) A + \frac{1}{\sqrt{\pi}} \operatorname{Re} C \right]. \quad (22)$$

* For the square well potential the correction to eq. (21) can be approximated as $\Delta B_i(q, p) \approx (d_0/8.6 r_0)^3 |f|^2 / \gamma \rho r_0$. For $r_0 \geq 1.5$ fm $\Delta B_i/B_i < 5\%$.

Fig. 2. The function $B_i^{nn}(0, p)$. Curves 1 and 4 have been calculated according to eqs. (19) and (22), respectively. Curves 2 and 3 correspond to the exponential and square well potentials, respectively. The scattering length is equal to 17 fm and the effective radius 2.7 fm.



Here

$$A = \frac{1}{u} \arcsin(u), \quad (23)$$

$$C = \frac{1}{2u} \ln \frac{1+u}{1-u}, \quad u = \frac{v}{\rho} \sqrt{r^2 + r_0^2}.$$

$$A=C=1 \text{ at } v \rightarrow 0, \quad A = \frac{\pi}{2}, \quad C = \ln(2\gamma \sqrt{1 + \frac{r_0^2}{r^2}})$$

for $\gamma \gg 1$ and $A = \pi/2$, $C = \ln(2\gamma v r_0 / r_0)$ if $v r_0 \gg r_0$.

We note that for small particle velocities, when $\gamma p \approx r_0$, the function $B(q, p)$ becomes insensitive to the parameter r_0 (see figs. 3, 4). In this case

$$B_0(q, p) = -\frac{1}{2} \exp(-4k^* r_0^2), \quad (24)$$

$$B_i(q, p) = \frac{1}{4} \frac{|f|^2}{r_0^2} \left(1 - \frac{1}{2\sqrt{\pi}} \frac{d_0}{r_0}\right) + \frac{\text{Re} f}{\sqrt{\pi} r_0} F_1(2k^* r_0) - \frac{\text{Im} f}{2r_0} F_2(2k^* r_0),$$

where $F_1(z) = \frac{1}{z} e^{-z^2} \int_0^z e^{x^2} dx = 1 - \frac{2z^2}{3} + \frac{(2z^2)^2}{3.5} - \dots$, $F_2(z) = \frac{1}{z} (1 - e^{-z^2})$.

For two neutrons with $2k^* r_0 \leq 1$ the function B_i in (24) can be approximated by

$$B_i(q, p) = B_i(0, p) \left| \frac{f(k^*)}{f(0)} \right|^2 \exp(-4k^* r_0^2), \quad (25)$$

$$r_e^2 = r_0^2 \left[1 - \frac{4}{3\sqrt{\pi}} \frac{r_0}{f_0} \left(1 + \frac{4}{\sqrt{\pi}} \frac{r_0}{f_0} - \frac{1}{2\sqrt{\pi}} \frac{d_0}{r_0} \right) \right].$$

We see that for small particle velocities the correlation function $B(q, p)$ depends only on the momentum $k^* = \frac{1}{2} \sqrt{-q^2}$ and this dependence is determined by the scattering amplitude and the parameter r_0 .

It should be pointed out that the effect of final-state interaction becomes stronger with decreasing space-time dimensions of the production region. For r_0 and r_0 of about 2-3 fm the contribution of final-state interaction to the neut-

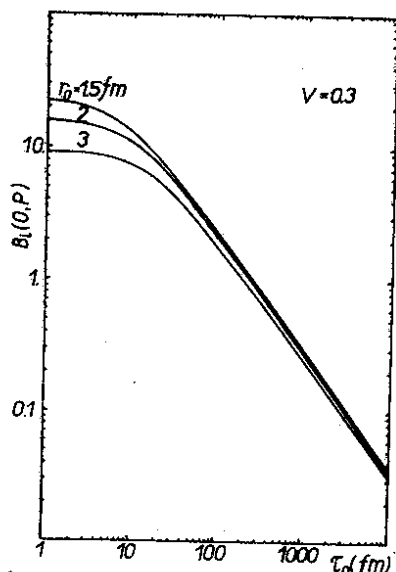


Fig. 3. The function $B_i^{nn}(0, p)$ calculated according to eq. (22); $f_0 = 17$ fm, $d_0 = 2.7$ fm.

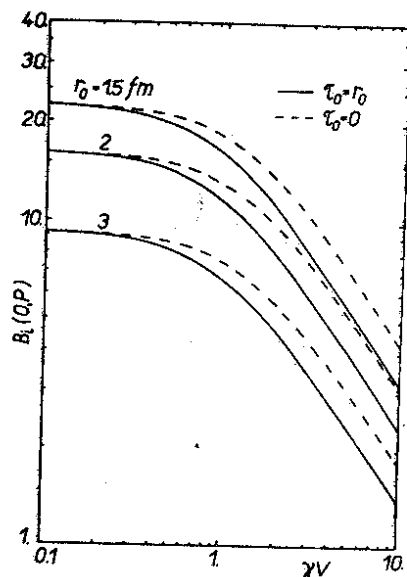


Fig. 4. The energy dependence of the function $B_i^{nn}(0, p)$; $\gamma v = p/m$.

ron correlation function at small $|q|$ is several tens as large as the contribution of Fermi-statistics effect; see the curves in figs. 3-6 calculated according to formulae (21-22). The final-state interaction is unessential in the case of large distances between particle sources or large emission time, e.g., in the case of neutron evaporation by excited heavy nuclei 19 (if $r_0 \sim 3$ fm and $v_0 \sim 10^4$ fm, the ratio B_i/B_0 is about 2% at $q=0$). Note that the role of final-state interaction becomes less important also with increasing neutron energy (fig. 4); in the ultrarelativistic case $B_i(0, p) \sim 1/\gamma$.

As can be seen from fig. 5, the q -dependence of the function $B_i(q, p)$ at small $|q|$ is mainly determined by the neutron scattering amplitude (due to the large neutron scattering length). Besides, even at $v=0.3$ the k^{*2} -dependence of the ratio $B_i(q, p)/|f(k^*)|^2$ is approximated by the exponential in eq. (25) (dashed line in fig. 5) with a relative error smaller than 10% for $2k^*r_0 \leq 1$ (note that $q_T^2 = 4k^{*2}$ at $q_0 = 0$).

It should be noted that for polarized neutrons the peak of the correlation function at $q=0$ can diminish or even turn into a dip. We recall that in the case of independent neutron emission with polarization \vec{P} the functions B_0 and B_i in eqs (17) and (18) should be multiplied by $(1+\vec{P}^2)$ and $(1-\vec{P}^2)$, respectively.

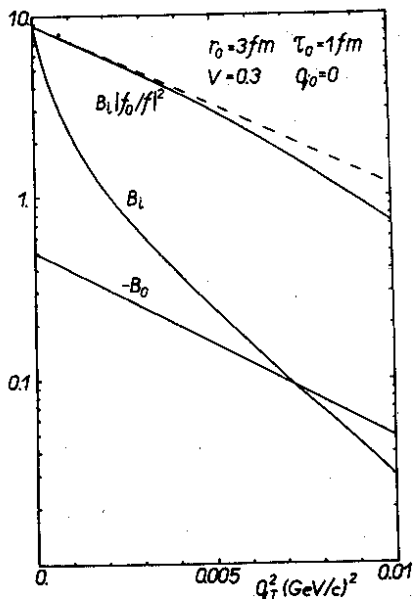


Fig. 5. The functions $B_i^{nn}(q, p)$ and $-B_0^{nn}(q, p)$ calculated according to eqs. (21) and (17). The dashed line corresponds to the approximate formula (25).

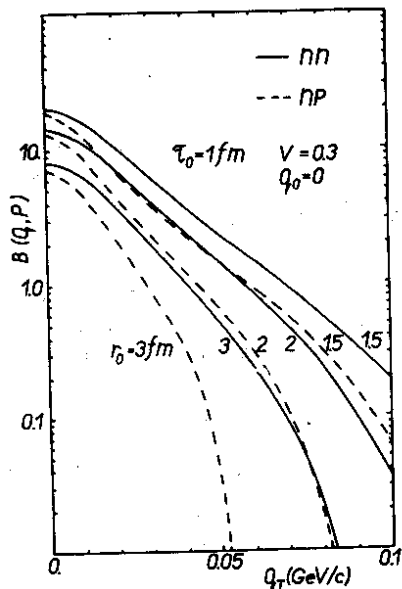


Fig. 6. The neutron-neutron and neutron-proton correlation functions.

We thus see that two-neutron correlations can be used to determine space-time dimensions of their production region only if the final-state interaction is correctly taken into account; the formulae of refs.^{2-5/} cannot be directly applied here.

3. The final-state interaction turns out to be essential also for the correlations of two neutral kaons (the experimental data and theoretical discussion of the latter see in refs.^{20,21/}). Provided that K^0 - and \bar{K}^0 -mesons are emitted by independent point-like sources, the correlation function $B_{s^0 s^0}^{K^0 K^0}$ of two K^0 -mesons differs from the neutron one only by the spin factors (see (8-9)). Thus, $B_{s^0 s^0}^{K^0 K^0} = \langle \cos(qx) \rangle$ describes the effect of Bose-statistics for spin-zero particles^{21/}, and $B_{s^0 s^0}^{K^0 K^0}$ is given by eqs. (13) or (18-19) multiplied by 4 with the scattering amplitude approximated by

$$f^{K^0 \bar{K}^0}(k^*) \approx \frac{i}{2} [f^{(0)} / (1 + k^* f^{(0)}) + f^{(1)} / (1 + k^* f^{(1)})].$$

Here $f^{(0)} = 1.7$ fm corresponds to the S^* -contribution with isospin $T=0$ and $f^{(1)} = 0.84$ fm - to the δ -contribution with $T=1$ (see /22/). The correction term in eq. (21) is small as

$\text{Ref} \approx 0$; see eq. (20). According to (22), $B_i^{K_s^0 K_s^0}(0, p) = A|f|^2 / \gamma \rho r_0$, where $|f| = 1.27$ fm and $1 \leq A \leq \frac{\pi}{2}$. We see that for

$\rho \sim 1$ fm and not too large γ -factors the contributions of final-state interaction and Bose-statistics effect to the correlation function become comparable.

The correlation functions for other identical spin-zero particles have a similar structure, in particular, for two neutral or charged pions (provided that the Coulomb interaction can be neglected, i.e., for $k^* > \pi m_\pi / 137 \approx 3$ MeV/c; see Section 5). Experimental data and theoretical calculations give the $\pi^+ \pi^+(\pi^0 \pi^0)$ -scattering length equal to $\sim -0.03(01)$ fm^{23/}. According to formula (22) multiplied by 4, the contribution of final-state interaction to the $\pi^+ \pi^+(\pi^0 \pi^0)$ -correlation function is smaller than 7%(23%) for $r_0 = 1$ fm*. Therefore it is possible to determine space-time dimensions of charged pion production region taking into account only the Bose-statistics effect (see refs. /2-5/) provided that $\gamma \rho \geq 1$ fm.

4. Final-state interaction has an influence also on the correlations of nonidentical particles. In this case it is convenient to consider the symmetrized correlation function

$b = \frac{1}{2} [b(p_1, p_2) + b(p_2, p_1)]$. Then for the spin-independent interaction

$$b = |f\Phi_{p_1 p_2}(x)|^2 + 2\text{Re}[f\Phi_{p_1 p_2}(x)] \cos(qx/2), \quad (26)$$

* Formulae (19), (21-22) are reliable under the condition $\gamma \rho r_0 / r_0 \gg m_\pi^{-1}$. As $m_\pi^{-1} = 1.4$ fm, this condition is not always fulfilled for space-time dimensions of ~ 1 fm in contrast to the case of nucleons or kaons. E.g., at $r_0 = r_0 = 1$ fm and $v = 0.3$ formula (22) leads to a $\sim 20\%$ overestimation of the function $B_i^{\pi\pi}(0, p)$. Note that in the realistic cases the terms in eqs. (21-22) proportional to $|f^{\pi\pi}|^2$ are very small (the effective radius of the two-pion interaction is determined by the ρ -meson mass: $d_0 = 2m_\rho^{-1} = 0.5$ fm).

i.e., the correlation function is entirely determined by the function $b_1(b_0=0)$. In the general case, when the s-wave final-state interaction of particles with spins j_1 and j_2 depends on their summary spin, and the particles are produced with normalized probability ρ_S in a state with summary spin S

$$b = \sum_S \rho_S \{ |f^{S\Phi}_{p_1 p_2}(x)|^2 + 2 \operatorname{Re}[f^{S\Phi}_{p_1 p_2}(x)] \cos(qx/2) \}. \quad (27)$$

If the production process does not depend on the particle spin projections, $\rho_S = (2S+1)/(2j_1+1)(2j_2+1)$. In particular, the proton-neutron correlation function averaged over the distribution of the sources of unpolarized nucleons is of the form

$$B^{np}(q, p) = \frac{1}{2} [B^{(0)}(q, p) + 3B^{(1)}(q, p)], \quad (28)$$

where the functions $B^{(S)}(q, p)$, $S=0, 1$ corresponding to the contributions of singlet and triplet spin states are given by eqs. (13), (18) or (19), (21-22). The np-scattering length and the effective radius of np-interactions in the singlet (triplet) state appearing in eq. (14) are equal to 23.7 fm and 2.7 fm (-5.4 fm and 1.7 fm), respectively^{/14/}. As is seen from fig. 6, the neutron-proton correlations are slightly weaker than the ones of two neutrons.

Note that in the case of independent neutron and proton production with polarizations \vec{P}_n and \vec{P}_p , the functions $B^{(0)}$ and $B^{(1)}$ in (28) should be multiplied by $(1 - \vec{P}_n \vec{P}_p)$ and $(1 + \frac{1}{3} \vec{P}_n \vec{P}_p)$, respectively.

According to eq. (26), the $\pi^+\pi^-$ -correlation function is given by (18) or (19), (21-22) multiplied by 2 with the $\pi^+\pi^-$ -scattering amplitude equal to $f_0^{\pi^+\pi^-} = \frac{2}{3}f_0^{(T=0)} + \frac{1}{3}f_0^{(T=2)} \approx 0.2$ fm

at $q=0$ ^{/23/}. For slow $\pi^+\pi^-$ -pairs ($p \leq m$) and $r_0 \sim 1$ fm we have $B^{\pi^+\pi^-}(0, p) \sim 0.25$. Thus, $\pi^+\pi^-$ -pairs can be used as a background in a study of charged-like pion correlations^{/2-5/} provided that the dimensions of the pion production region are large enough ($\gamma p \gtrsim 1-2$ fm).

5. It is well-known that the contribution of Coulomb interaction is determined by the factor^{/14/}

$$A_c^{(\pm)}(k^*) = \pm \frac{2\pi}{k^* a_c} [\exp(\pm \frac{2\pi}{k^* a_c}) - 1]^{-1}, \quad (29)$$

where a_c is the Bohr radius and the sign $+(-)$ corresponds to repulsion (attraction). The factor $A_c(k^*)$ is essentially different from 1 only for $k^* a_c / 2\pi < 1$. For particles with unit charges and equal masses $a_c = 2\hbar^2 / me^2$; for protons $a_c = 57.5$ fm. We thus see that the higher is the particle mass the wider is the region of momenta k^* where the Coulomb interaction is important.

Assuming again that the intrinsic range of the strong interaction potential is smaller than the distance between the emission points in the particle c.m.s., we can find the explicit expression for the amplitude $\psi_{p_1 p_2}(x_1, x_2)$ in eq. (3)

allowing for both the Coulomb interaction and the s-wave short-range interaction of identical particles; see eqs. (4) and (A.9-11). For equal emission times in the two-particle rest frame this expression coincides with the solution of Schrodinger equation outside the range of strong interaction having the asymptotics corresponding to the superposition of plane and diverging spherical wave distorted by the Coulomb interaction (see eq. (A.13)).

In the realistic cases the distance between emission points is small as compared to the Bohr radius. In such an approximation the expression for the amplitude $\psi_{p_1 p_2}(x_1, x_2)$ is essentially simplified (see eq. (A.15)) and the correlation function takes the form

$$B(q, p) = A_c(k^*) [1 + B_0(q, p) + B_1(q, p)] - 1, \quad (30)$$

where the functions B_0 and B_1 should be calculated according to eqs. (8) and (10-11). The scattering amplitude for neutral particles should be replaced here by the effective amplitude $f_c(k^*)$ or $f_c^S(k^*)$, renormalized by Coulomb interaction, and the function $\Phi_{p_1 p_2}(x)$ by

$$\Phi_{p_1 p_2}^c(x) = \Phi_{p_1 p_2}(x) + i(A_c^{(+)}(k^*) - 1) \text{sink}^* r^* / r^*. \quad (31)$$

In the case of two protons the functions $B_0(q, p)$ and $B_1(q, p)$ are given by eqs. (12) and (13) with the effective amplitude

$$f_c(k^*) = \left[\frac{1}{f_0} + \frac{1}{2} d_0 k^{*2} - \frac{2}{a_c} h(k^* a_c) - i k^* A_c^{(+)}(k^*) \right]^{-1}, \quad (32)$$

where $f_0 = 7.77$ fm, $d_0 = 2.77$ fm and the function $h(x)$ takes the form ^{/14/}

$$h(x) = \frac{1}{x^2} \sum_{n=1}^{\infty} \frac{1}{n(n^2 + x^2)} - C + \ln x, \quad C = 0.5772 \dots \quad (33)$$

If the emission points are distributed according to the Gauss law (see (16)), the function B_0 is given by eq. (17) and the function B_1 , under the conditions $mypr_0/r_0 \gg 1$, $k^* \ll m$, $k^* \ll mr_0/r_0$, by eqs. (19), (21) modified by $f(k^*) \rightarrow f_c(k^*)$ and $\Phi_{p_1 p_2}(x) \rightarrow \Phi_{p_1 p_2}^c(x)$. As is shown in Appendix (see

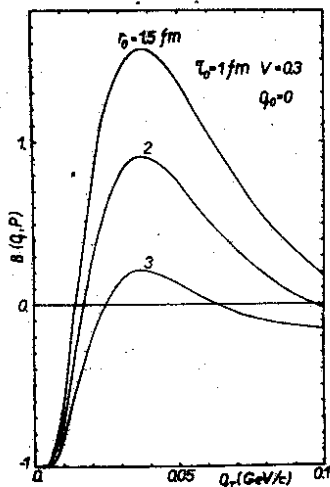
(A.16)), the correction term, proportional to the effective radius d_0 , connected with the behaviour of the wave function inside the range of the strong interaction potential is correctly taken into account by modified eqs. (19), (21).

It is clear from eq. (30) that the correlation function tends to the value $B=-1$ when $q \rightarrow 0$ (due to Coulomb repulsion). The joint effect of Coulomb and short-range forces leads to a peak in the correlation function, which, in contrast to the case of neutral particles, is shifted to $q \neq 0$ ($k^* \approx 2\pi/a_c = 21.6$ MeV/c, see fig. 7).

Eq. (30), together with (12-13) and (A.8), represents the analytical solution of the problem taking account of relativistic effects and nonequal emission times in the two-particle c.m.s. (if they appear to be essential). Previously the corresponding calculations for nonrelativistic protons have been done by Koonin^{/12/} (see also experimental papers^{/24,25/}). Our calculations at $v_{r0}=0$, $r_0=1.4-2.8$ fm yield the cross section ($\sigma \sim 1+B$) in the peak smaller by $\sim 20\%$ than that in ref.^{/12/}. It should be noted that the use of the approximation $r^* \ll a_c$ (see (A.14)) lowers the peak cross-section by about 10(20)% for $r_0=2(3)$ fm. Nevertheless, our approach makes it possible to look over, with enough accuracy, the analytical dependence of two-proton correlation function on the space-time parameters and does not require a large computer time.

In conclusion we note that the s-wave approximation for the strong final-state interaction is quite reliable for $k^* \lesssim 50$ MeV/c; the contribution of higher orbital angular momenta to the two-nucleon cross sections is less than 1%.

Fig. 7: The proton-proton correlation functions calculated according to formulae (29)-(33); $f_0^{pp} = 7.77$ fm, $d_0^{pp} = 2.77$ fm.



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APPENDIX

According to eq. (5), the function $\Phi_{p_1 p_2}(x)$ introduced in eq. (6) is of the form

$$\Phi_{p_1 p_2}(x) = \frac{8\pi\sqrt{k^{*2}+m^2}}{i(2\pi)^4} \int \frac{\exp[i(\sqrt{k^{*2}+m^2}t^* - \kappa_0^* t^* + \vec{\kappa}^* \vec{r}^*)] d^3\vec{\kappa}^* d\kappa_0^*}{(\kappa_0^* - \vec{\kappa}^* \cdot \vec{r}_L - m^2 + i0)[(2\sqrt{k^{*2}+m^2} - \kappa_0^*)^2 - \vec{\kappa}^{*2} - m^2 + i0]} \quad (A.1)$$

Here \vec{r}^* and t^* are the space and time components of the 4-vector $x = \{x, t\}$ in the two-particle rest frame. They are related to \vec{r} and t in the rest frame of the particle sources by the Lorentz transformation

$$\vec{r}_T^* = \vec{r}_T, \quad r_L^* = \gamma(r_L - vt), \quad t^* = \gamma(t - vr_L). \quad (A.2)$$

Here $\vec{v} = \vec{p}/p_0$ is the particle pair velocity, $\gamma = (1-v^2)^{-1/2}$ is the Lorentz factor, $r_L(r_T)$ is the component of the vector \vec{r} longitudinal (transverse) to \vec{v} . After integrating over the energy variable κ_0^* and over the angles of the vector $\vec{\kappa}^*$, we get

$$\Phi_{p_1 p_2}(x) = \frac{1}{2\pi r^*} \int_{-\infty}^{\infty} \frac{\kappa \sin \kappa r^*}{\kappa^2 - k^{*2} - i0} \left\{ \left(1 + \sqrt{\frac{k^{*2}+m^2}{\kappa^2+m^2}}\right) \exp[-i(\sqrt{\kappa^2+m^2} - \sqrt{k^{*2}+m^2})|t^*|] - \right. \\ \left. - \left(1 - \sqrt{\frac{k^{*2}+m^2}{\kappa^2+m^2}}\right) \exp[-i(\sqrt{\kappa^2+m^2} + \sqrt{k^{*2}+m^2})|t^*|] \right\} d\kappa, \quad (A.3)$$

where $r^* = (r_T^2 + r_L^{*2})^{1/2}$ and $\kappa = |\vec{\kappa}^*|$. For $k^* \ll m$ the formula (A.3) yields

$$\Phi_{p_1 p_2}(x) = \frac{1}{\pi r^*} \int_{-\infty}^{\infty} \frac{\kappa \sin \kappa r^*}{\kappa^2 - k^{*2} - i0} \exp(-i \frac{\kappa^2 - k^{*2}}{2m} |t^*|) d\kappa. \quad (A.4)$$

For equal emission times in the c.m.s. of particles ($t^* = 0$, $t = vr_L$) $\Phi_{p_1 p_2}(x)$ coincides with the diverging spherical wave:

$$\Phi_{p_1 p_2}(x) = e^{ik^* r^*} / r^*. \quad (A.5)$$

In the case of arbitrary t^* it is convenient to transform (A.4) into the form

$$\Phi_{p_1 p_2}(x) = \frac{e^{ik^* r^*}}{r^*} \int_{-\infty}^{r^*} e^{-ik^* r'} f(r', |t^*|) dr' - \\ - \frac{e^{-ik^* r^*}}{r^*} \int_{r^*}^{\infty} e^{ik^* r'} f(r', |t^*|) dr', \quad (A.6)$$

where

$$f(r', |t^*|) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{i\kappa r'} \exp(-i \frac{\kappa^2 - k^{*2}}{2m} |t^*|) d\kappa =$$

$$= \frac{1}{2} \sqrt{\frac{m}{\pi |t^*|}} (1-i) \exp[i(\frac{k^{*2} |t^*|}{2m} + \frac{r'^2 m}{2|t^*|})]. \quad (A.7)$$

From here

$$\Phi_{p_1 p_2}(x) = i \frac{\sin k^* r^*}{r^*} + \frac{1}{2r^*} (1-i) \{ e^{ik^* r'} [C_1(z_-) + iS_1(z_-)] +$$

$$+ e^{-ik^* r'} [C_1(z_+) + iS_1(z_+)] \}, \quad (A.8)$$

where $z_{\pm} = \sqrt{\frac{m}{2|t^*|}} (r^* \pm \frac{k^* |t^*|}{m})$ and $C_1(z)$, $S_1(z)$ are the Fresnel integrals: $C_1(z) + iS_1(z) = \sqrt{\frac{2}{\pi}} \int_0^z e^{iy^2} dy$. If $z_- \gg 1$, $S_1 = C_1 = 1/2$ and (A.8) is reduced to the spherical wave (A.5). If $\sqrt{\frac{m}{2|t^*|}} r^* \ll 1$, the function $\Phi_{p_1 p_2}(x)$ is close to zero for arbitrary k^* -values.

We can present the function (5) also in the form of 3-dimensional integral

$$\phi_{p_1 p_2}(x) = \int \phi_{k^*}(\vec{r}) g(\vec{r}^* - \vec{r}, |t^*|) d^3 \vec{r}, \quad (A.9)$$

where $e^{-ik^* \vec{r}} + \phi_{k^*}(\vec{r})$ satisfies the corresponding Schroedinger equation, $\phi_{k^*}(\vec{r}) = f(k^*) e^{ik^* r}/r$ outside the range of strong interaction. The function $g(\vec{r}', |t^*|)$ represents a 3-dimensional analog of the function $f(r', |t^*|)$ in eq. (A.7):

$$g(r', |t^*|) = \frac{1}{(2\pi)^3} \int e^{i\vec{\kappa} \cdot \vec{r}'} \exp(-i \frac{\kappa^2 - k^{*2}}{2m} |t^*|) d^3 \vec{\kappa} =$$

$$= \frac{1}{8} (\frac{m}{\pi |t^*|})^{3/2} (1-i)^3 \exp[i(\frac{k^{*2} |t^*|}{2m} + \frac{r'^2 m}{2|t^*|})], \quad (A.10)$$

$g(r', 0) = \delta^3(r')$. In the s-wave approximation the formulae (A.9)-(A.10) yield the previous result (6)-(A.8) neglecting the deviation of the function $\phi_{k^*}(\vec{r})$ from the diverging wave at $r < d$. It is clear that for $r^* < d$ the function $\phi_{p_1 p_2}(x)$ at arbitrary t^* -values is determined by the behaviour of $\phi_{k^*}(\vec{r})$ inside the range of strong interaction. To estimate the corresponding correction to the function B_1 in (18), we can use the square well potential and put for $r < d$

$$\phi_{k^*}(\vec{r}) = \frac{1}{\sin Kd} [f(k^*) e^{ik^* d} \frac{\sin Kr}{r} + \frac{1}{k^* r} (\sin k^* d \cdot \sin Kr - \sin Kd \cdot \sin k^* r)]$$

where $K = (K_0^2 + k^{*2})^{1/2}$ and $K_0 \approx \pi/2d$, $d \approx d_0$ (for neutrons $K_0 = 110.4$ MeV and $d = 0.983 d_0^{1/26}$). Presumably, such a correction is only weakly dependent on the potential form if $d/r_0 \leq 2$; see fig. 2 and eqs. (20)–(21) corresponding to the approximation $t^* = 0$.

For two charged particles with $k^* < 2\pi/a_c$ the scattering amplitude cannot be taken out of the integral in eq. (5). In this case it is convenient to use the representation (A.9)–(A.10). Outside the range of the strong interaction the function $\phi_{k^*}(\vec{r})$ is determined by the well-known Coulomb wave functions; for particles with equal charges (see, e.g., refs. /8,9/).

$$\phi_{k^*}(\vec{r}) = \sqrt{A_c^{(+)}} e^{i\delta_0^c} [e^{-ik^*\vec{r}} F(-\frac{i}{k^*a_c}, 1, i(k^*\vec{r} + k^*r)) + \frac{e^{2i\delta_0} - 1}{2ik^*} \cdot \frac{\tilde{G}}{A_c^{(+)} r}] - e^{-ik^*\vec{r}} \quad (A.11)$$

Here $\delta_0^c = \arg\Gamma(1 + i/k^*a_c)$ is the Coulomb phase corresponding to zero orbital angular momentum, δ_0 is the additional s-wave phase shift due to short range forces, F is the confluent hypergeometric function and \tilde{G} is the combination of confluent hypergeometric functions:

$$\tilde{G} = \sqrt{A_c^{(+)}} e^{i(k^*r - \frac{1}{k^*a_c} \ln 2k^*r + \delta_0^c)} G(1 + \frac{i}{k^*a_c}, \frac{i}{k^*a_c}, 2ik^*r).$$

The function $G(\alpha, \beta, z)$ is defined in §d of ref. /14/; see also ref. /27/. For $k^*r \gg 1$ $G=1$. The phase shift $\delta_0(k^*)$ is determined by the equation /14/

$$\frac{e^{2i\delta_0} - 1}{2ik^*} = \{ [\frac{1}{f_0} + \frac{1}{2} d_0 k^{*2} - h(k^*a_c)] / A_c^{(+)} - ik^* \}^{-1}, \quad (A.12)$$

where $A_c^{(+)}(k^*)$ and $h(k^*a_c)$ are given by (29) and (32), respectively.

In the approximation of equal emission times in the two-particle rest frame (at $|t^*| \ll m r^{*2}$) $\phi_{p_1 p_2}(x) = \phi_{k^*}(\vec{r}^*)$. In this case the amplitude $\psi_{p_1 p_2}$ is given by $\psi_{p_1 p_2}(x_1, x_2) =$

$= e^{ip(x_1 + x_2)} [e^{-ik^*\vec{r}^*} + \phi_{k^*}(\vec{r}^*)]$ and at $k^*r^* \gg 1$ has the asymptotics

$$\psi_{p_1 p_2}(x_1, x_2) = e^{ip(x_1 + x_2)} \{ e^{-ik^*\vec{r}^* + \frac{i}{k^*a_c} \ln(k^*\vec{r}^* + k^*r^*)} \times \quad (A.13)$$

$$\times \left[1 + \frac{1}{ik^* a_c^2 (\vec{k}^* \vec{r}^* + k^* r^*)} \right] + \\ + \left\{ \tilde{f}_c(\pi - \theta) + \frac{e^{2i\delta_0} - 1}{2ik^*} e^{2i\delta_0^c} \right\} \frac{e^{ik^* r^* - \frac{1}{k^* a_c} \ln 2k^* r^*}}{r^*} \}.$$

Here $\tilde{f}_c(\pi - \theta)$ is the amplitude of Coulomb scattering, θ is the angle between \vec{k}^* and \vec{r}^* .

The expression for the amplitude $\psi_{p_1 p_2}(x_1, x_2)$ is essentially simplified when $r^*/a_c \ll 1$. In this case

$$F = 1, \quad \tilde{G} = \cos k^* r^* + i A_c^{(+)} \sin k^* r^* \quad (\text{A.14})$$

and eqs. (4), (A.9)-(A.11) yield

$$\psi_{p_1 p_2}(x_1, x_2) = \sqrt{A_c^{(+)}} e^{i\delta_0^c} e^{ip(x_1 + x_2)} [e^{iqx/2} + f_c(k^*) \Phi_{p_1 p_2}^c(x)], \quad (\text{A.15})$$

$$\text{where } f_c(k^*) = \frac{e^{2i\delta_0} - 1}{2ik^*} \cdot \frac{1}{A_c^{(+)}(k^*)} \quad \text{coincides with eq. (32)}$$

and $\Phi_{p_1 p_2}^c(x)$ is given by eq. (31). Eq. (30) immediately follows from (A.15) and the definition (3) of the correlation function.

The correction to the correlation function connected with the deviation of the "true" wave function $e^{-ik^* \vec{r}} + \phi_{\vec{k}^*}(\vec{r})$ inside the range of strong interaction from the Coulomb one $e^{-ik^* \vec{r}} + \tilde{\phi}_{\vec{k}^*}(\vec{r})$, given by eq. (A.11), can be taken into account in a similar way as in the case of two neutral particles. According to the effective radius theory^{/16-18/}, there is the integral relation analogous to eq. (20):

$$\frac{1}{4\pi} \int [|\phi_{\vec{k}^*}(\vec{r}) + e^{-ik^* \vec{r}}|^2 - |\phi_{\vec{k}^*}(\vec{r}) + e^{-ik^* \vec{r}}|^2] d^3 \vec{r} = \\ = A_c^{(+)}(k^*) |f_c(k^*)|^2 d_0/2. \quad (\text{A.16})$$

From (A.16) it follows that the function $B_i(q, p)$ in eq. (30) includes the correction term proportional to the effective radius (see eq. (21)).

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в конечном состоянии на парные корреляции частиц с малыми отно-
сительными импульсами

В рамках модели независимых одночастичных источников исследуется влияние s -волнового взаимодействия в конечном состоянии на корреляции двух частиц с близкими импульсами. Вклад взаимодействия в конечном состоянии в корреляционную функцию определяется амплитудой рассеяния и пространственно-временными размерами области генерации. Подробно обсуждается случай двух нейтронов. Показано, что при размерах масштаба 2-3 ферми эффект взаимодействия в конечном состоянии для нейтронов существенно превышает интерференционные корреляции невзаимодействующих тождественных частиц со спином $1/2$. Обсуждается характер корреляций пар $K_s^0 K_s^0$, $\pi^+ \pi^+ (\pi^- \pi^-)$, np , $\pi^+ \pi^-$. Получены формулы, учитывающие совместный вклад кулоновских и короткодействующих сил. Рассмотрено влияние кулоновского взаимодействия на корреляции двух протонов.

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State Interaction on Correlations of Two Particles with Nearly
Equal Momenta

The influence of s -wave final-state interaction on correlations of two particles with nearly equal momenta is studied in terms of the model of independent point-like one-particle sources. The contribution of final-state interaction to the correlation function is determined by the scattering amplitude and the space-time dimensions of the particle emission region. Two-neutron correlations are considered in some detail. It is shown that for space-time dimensions of 2-3 fm the effect of neutron interactions dominates over the interference correlations of two noninteracting identical spin- $1/2$ particles. The $K_s^0 K_s^0$ -, two-neutral (charged) pion- and np -correlations are also discussed. The formulae taking into account the joint contribution of Coulomb and short-range forces to the correlations of charged particles have been obtained and applied in the case of two protons.

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