#### Hierartical Structure in Social Networks

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SODA502: Final Project

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#### Theorizing Hierarchy in Networks - Prior Work

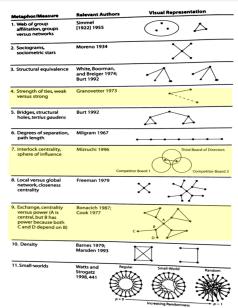


FIGURE 1. Social network conceptual toolkit. Note: Figure courtesy of Nature, vol. 363.

#### Theorizing Hierarchy in Networks - Mann

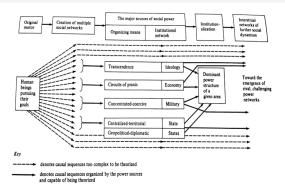


Figure 1.2. Causal IEMP model of organized power

#### Societies as organized power networks

	Authoritative
Intensive	Army command structure
Extensive	Militaristic empire

Figure 1.1. Forms of organizational reach

Diffused
A general strike
Market exchange

## Hierarchy in networks–Measures

Measure	Undirected	Weighted	Global	Local
Landau's h		X	X	
Kendall's K	X	X		X
Reach Degree	X	X		X
Reach Closeness	X	X		X
GRC	X	X	X	X
Rooted Depth			X	
Degree	X	X	X	X
Closeness	X	X	X	X
Betweenness	X	X	X	X
Eigenvector	X	X	X	X

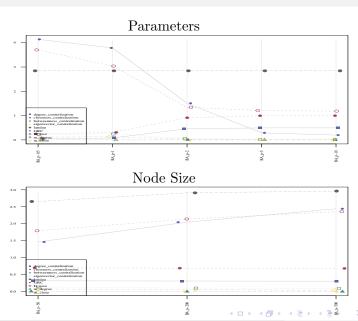
#### Hierarchy in Networks-Simulated Datasets

- 7500 Barabasi-Albert (BA) Datasets with node size 50, 200, or 500 and preferential attachment parameter 0.5, 1, 2, 5, or 10.
- 6000 Tree-Structured (TR) Datasets with node size 50, 200, or 500 and children parameter 2, 5, 10, or 50.
- 4500 Erdos-Renyi (ER) Datasets with node size 50, 200, or 500 and parameter size 0.05, 0.1, or 0.2.

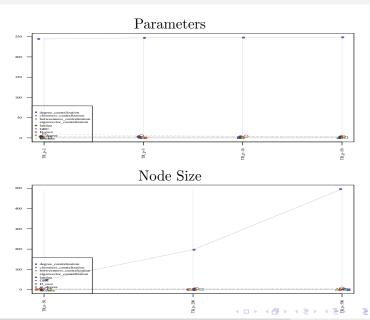
BA and TR	Node	Edge	Density
	50	49	0.02
	200	199	0.005
	500	499	0.002

$_{\rm ER}$	Node	Parameter	Edge	Density	Cluster Coefficient
	50	0.05	122.524	0.050	0.0956
	50	0.1	244.768	0.100	0.188
	50	0.2	490.050	0.200	0.359
	200	0.05	1989.242	0.050	0.098
	200	0.1	3980.776	0.100	0.190
	200	0.2	7952.138	0.120	0.360
	500	0.05	12473.270	0.050	0.097
	500	0.1	24932.824	0.100	0.190
	500	0.2	49892.784	0.200	0.360

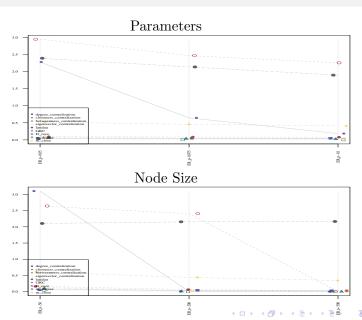
## Average Global Hierarchy–BA Networks



# Average Global Hierarchy–TR Networks



## Average Global Hierarchy–ER Networks



#### Hierarchy in Networks–Results

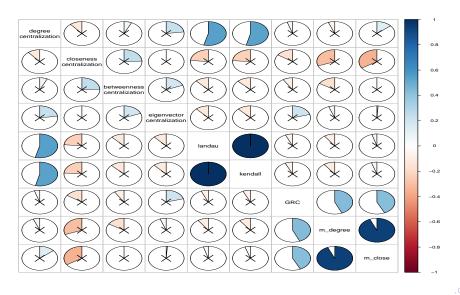
- GRC and D Root are not robust to changes in node size.
  - GRC increases with node size for both BA and TR networks
  - GRC decreases with node size for ER networks.
  - D Root increases with node size for BA networks.

#### Hierarchy in Networks–Datasets

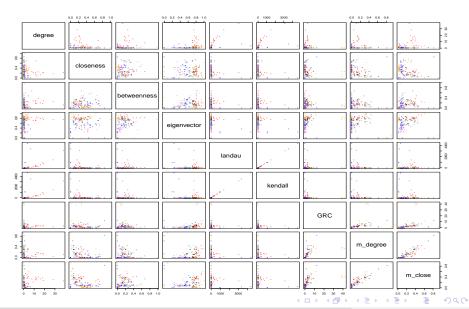
• 141 datasets from UCINET, organizational emails, and Congress

Type	Nodes	Edges	Density	Cluster Coeff.
Communication	25.714	2419	3.483	0.558
Cosponsorship	101.222	13358.889	1.317	0.788
Co-membership	22	9267.333	18.318	0.377
Interaction	23.075	1944.95	1.985	0.589
Unknown	76.833	4688.25	0.360	NaN
Friendship	29.833	92	0.122	0.348
Affect	17.636	95.182	0.319	0.329
Terrorism	63	308	0.079	0.361
Trade	24	285.6	0.5170	0.734

#### Hierarchy in Networks – Global Measures

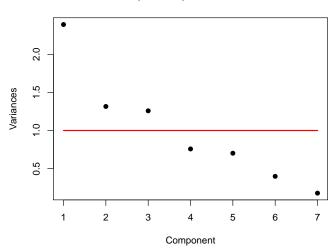


#### Hierarchy in Networks – Global Measures



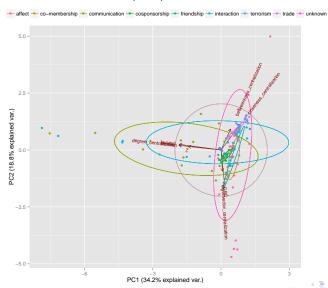
## Hiearchy in Networks – PCA

#### **Principle Component Variances**



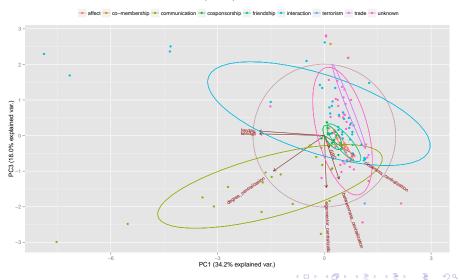
## Hierarchy in Networks – PCA

#### Principal Components: 1 and 2

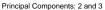


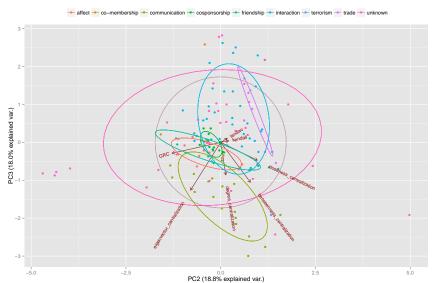
### Hierarchy in Networks – PCA





### Hierarchy in Networks – PCA





#### Hierarchy in Networks–Results

- Need first three principle components to explain the variation.
- Both trade and co-membership stay grouped and towards the center.
- Both Landau and Kendall stay in same direction.
- From the first PCA plot (PC1 PC2), we notice that there are three clear groupings of measures.
- PC3 tries to separate the grouping of Betweenness from Landau and Kendall.

#### Hierarchy in Networks – Local Measures

