

## Hierarchical Structure in Social Networks

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### Abstract

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### 1. Introduction

Hierarchy is an important feature of many organizations, such as firms, social clubs, and military units. Formally, we can define a hierarchy as a system where people or groups are ranked according to status or authority. Yet it is difficult to operationalize this definition for measurement and comparison. There has been a great deal of research on power and status in groups and organizations, but most of this research relies on measurements defined over domain specific rankings, such as job titles. At the same time, networks scholars have defined a number of broadly applicable hierarchy metrics based on network structure, but these metrics are not necessarily grounded in meaningful sociological concepts of status and authority. Contrastingly, social theorists like Michael Mann have noted the messiness of society and that a network-oriented perspective of the “socio-spatial and organizational model [of a network]” can explicate the “sources of social power,” [?] but they have generally not delved into the methodologies through which to fully explore such power dynamics. In this paper, we seek to bring together these two areas of research, and to develop a framework for measuring hierarchy in social networks that is both generally applicable and exhibits a high degree of construct validity.

Without statistical models/mathematical measurements for hierarchy which are theoretically based, and vice versa; theory that can be statistical/mathematically quantified and verified, the conceptual idea of hierarchy cannot be fully understood. We do not suggest that this project will achieve an overreaching theory and methods, but we strive to take the first step. At the very least, we will try to demonstrate the need for a united theory and corresponding methods. As an interdisciplinary team, we are in the unique position to accomplish our goals.

### 2. Sociological Theories of Hierarchy

We are still working through evaluating a few different datasets to best suit our purposes. However, at present, this is a little difficult because we really want our measure to be theoretically-grounded, but we haven’t yet developed a solid theoretical conception for hierarchy. Thus far, theory-wise, the Mann (1986) definition seems closest to the

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Liu-Driver measures discussed in the Mones et al. (2012) article: i.e., hierarchical networks are those in which the actions of a few nodes are needed to take control of the graph. Another potential definition, also implied, is hierarchy means the mechanisms of collective actions (i.e., the ability of different nodes to connect with one another) hinges on a small number.

### 3. Measuring Hierarchy

A number of analytical measures of hierarchy have been proposed for directed networks. Most proposed measures return a scalar value that is meant to capture the “hierarchical-ness” of a given network [1, 2? ? , 3? , 4]. This theoretically facilitates comparison between measures calculated on the same network, as well as comparison on the same measure across multiple networks. However some approaches to measuring hierarchy only provide a local measure of importance or position in the hierarchy for each node in the network [? ]. For these measures, one can calculate a Gini coefficient [? ] from the individual level scores and use these coefficients as a proxy for a global measure.

In this section, we introduce and describe ten candidate measures of network hierarchy that have been previously used in the networks literature. It is important to note that most of the measures we consider are only defined for directed networks, and thus for the remainder of this paper we assume all networks under consideration are directed. We begin by introducing some terminology that will be common across all measures. For a given network  $G = (V, E)$ , let  $V = \{v_i\}_{i=1}^N$  be the set of  $N$  vertices (nodes) associated with  $G$ , and  $E = \{e_j\}_{j=1}^M$  be the set of  $M$  edges associated with  $G$ . Furthermore, for a given edge  $e_j$ , let  $e_j^{(s)} \in 1 : N$  be the index of the sender of the edge and  $e_j^{(r)} \in 1 : N$  be the index of the recipient.

One other important point is that most measures of network hierarchy are meant to be applied to networks where the edge sets capture relations other than “has power over”. In this special case, it is theoretically easier to construct a measure of network hierarchy since the network must be directed and acyclic (preventing circular chains of command). However, obtaining such information is usually impossible in most cases (with military personnel networks being an obvious exception). Furthermore, if the researcher has collected such an edge-set, then the need for summary measures of the “hierarchical-ness” of the network is likely obviated, as deeper insights could be gained from applying inferential network analysis tools to the raw network. Therefore, we focus our attention on the measurement of hierarchy on networks where edges are not explicitly power relations.

#### 3.1. Analytical Measures of Hierarchy

The most basic measures of hierarchy or differential importance of a nodes in a network can all be derived from basic node-level measures of network centrality [5]. To aggregate from the node-level measures up to a single measure on a network, one can calculate  $C$ , the centralization of the network. Centralization captures the degree of inequality in the distribution of a given centrality measure over the network. In general, we should then expect that networks that are more centralized are also likely to be more hierarchical. However, this measure attains its maximal value for any centrality measure when one node has a maximal value of the given centrality measure and all the rest of the nodes have the minimal possible value. This will tend to give star networks maximal centralization scores. This implicit assumption in measurement is important to consider when evaluating the validity of centralization based measures of hierarchy. The four centrality measures we consider are: degree centrality, closeness centrality, betweenness centrality, and eigenvector centrality.

The **degree centrality** of node  $v_i$  is simply the number of outgoing or incoming edges incident to it. Formally, this can be calculated as:

$$\text{in-degree centrality}_i = \text{In}_i = \sum_{j=1}^M \mathbb{1}(e_j^{(r)} = i) \quad (1)$$

$$\text{out-degree centrality}_i = \text{Out}_i = \sum_{j=1}^M \mathbb{1}(e_j^{(s)} = i) \quad (2)$$

Degree centrality captures the number of friends or connections a node has, and intuitively, we should expect more powerful nodes will have more incoming and outgoing connections. However, degree centrality does not account for the identity of a node's alters. This can lead to difficulties when it is used to assess a node's position in a social hierarchy. For example, in a large company, we might expect that an administrative assistant may have a higher degree centrality than the CEO of a company if the edges being measured are work-related interaction. Furthermore, if there are many administrative assistants at the bottom of the power structure in an organization we might qualitatively consider to be extremely hierarchically structured, the degree centralization of the interaction network might be lower than in a comparably sized "organizationally flat" organization where a handful of people serve as coordinators. Thus we must take great care in interpreting this statistic, depending on the type of edges it is defined over. For given node-level in-degree or out-degree centrality measures  $\mathbf{c} = \{c_i\}_{i=1}^N$ , the corresponding in-degree or out-degree centralization measure is defined as:

$$\text{Degree Centralization} = \frac{\sum_{i=1}^N (\max\{c_i\} - c_i)}{(N-1)(N-2)} \quad (3)$$

where  $(N-1)(N-2)$  normalizes the measure for the size of the network.

The **betweenness centrality** of node  $v_i$  is a measure of the amount of influence a node has on the information transversed through it [? ]. Define  $D_{i,j}$  as the number of shortest paths in  $G$  between  $v_i$  and  $v_j$ , and  $D_{i,j}(k)$  as the number of these shortest paths that pass through  $v_k$ , then the betweenness centrality of node  $k$  is:

$$\text{betweenness centrality}_i = \sum_{i \neq k \neq j} \left( \frac{D_{i,j}(k)}{D_{i,j}} \right) \quad (4)$$

Betweenness centrality captures how in-the-middle-of-things a node is and when edges involve sharing information, how important the node is to information flowing quickly across the network. Intuitively, we should expect the nodes with higher betweenness centrality will be more powerful, and that greater inequality on this measure should signal a greater degree of hierarchical structure in a network. For given node-level betweenness centrality measures  $\mathbf{c} = \{c_i\}_{i=1}^N$ , the betweenness centralization measure is defined as:

$$\text{Betweenness Centralization} = \frac{\sum_{i=1}^N (\max\{c_i\} - c_i)}{(N-1)^2(N-2)} \quad (5)$$

where  $(N-1)^2(N-2)$  normalizes the measure for the size of the network. Similarly, the **closeness centrality** of node  $v_i$  is a measure of how few intermediate edges a given node must traverse to reach all other nodes in the network. Define  $d(i, j)$  as the length of the shortest path between  $v_i$  and  $v_j$ , then closeness centrality of node  $i$  is:

$$\text{closeness centrality}_i = \sum_{i \neq j} \left( \frac{1}{d(i, j)} \right) \quad (6)$$

Again, intuitively, powerful members of a hierarchy will tend to be able to reach others in the network more easily, and inequality in this measure (as captured by the closeness centralization of the network) should theoretically signal the degree of hierarchy in the network. For given node-level closeness centrality measures  $\mathbf{c} = \{c_i\}_{i=1}^N$ , the closeness centralization measure is defined as:

$$\text{Closeness Centralization} = \frac{\sum_{i=1}^N (\max\{c_i\} - c_i)}{\frac{(N-1)(N-2)}{(2N-3)}} \quad (7)$$

where  $\frac{(N-1)(N-2)}{(2N-3)}$  normalizes the measure for the size of the network.

The last of the classical centrality based measures is **eigenvector centrality**, which is meant to capture the degree to which a node is connected to other well connected nodes [? ]. Let the adjacency matrix of the network be defined as  $\mathbf{A}$  and the vector of local eigenvector centrality scores for each node be defined as  $\mathbf{w} = \{w(v_1), \dots, w(v_V)\}$ . Then to

calculate the eigenvalue centralities  $\mathbf{w}$ , one must solve the following eigenvector equation:

$$\mathbf{A}\mathbf{w} = \lambda\mathbf{w} \quad (8)$$

where  $\lambda$  is a vector of positive eigenvalues. The challenge is to find the *dominant eigenvector*, as only the largest eigenvalue results in the desired centrality measure for each node. Intuitively, higher eigenvector centrality should be associated with greater social or organizational importance. For given node-level eigenvector centrality measures  $\mathbf{c} = \{c_i\}_{i=1}^N$ , the eigenvector centralization measure is defined as:

$$\text{Eigenvector Centralization} = \frac{\sum_{i=1}^N (\max\{c_i\} - c_i)}{(N - 1)} \quad (9)$$

where  $(N - 1)$  normalizes the measure for the size of the network. Interestingly, the eigenvector centralization of a network can still be large even if there are a relatively large proportion of higher degree nodes, as long as the edges are organized such that only a few nodes are connected to all of these higher degree nodes.

**Landau's  $h$**  and **Kendall's  $K$**  are two closely related measures of hierarchy that operate on a *dominance* network – a transformation of the weighted sociomatrix of a given network [? ]. Intuitively, this *dominance* network is meant to capture dominance-subordination relationships (between animals). The  $[i, j]$  entry of the corresponding sociomatrix is coded as 1 if  $i$  is dominant over  $j$ , 0.5 if  $i$  and  $j$  are equals, and 0 if  $j$  is dominant over  $i$ . If the underlying network does not capture dominance relationships, then an weighted network can be transformed into a *dominance* network by assigning a value of 1 in the  $[i, j]$  entry of of the corresponding sociomatrix if the  $[i, j]$  entry of the original sociomatrix is greater than the  $[j, i]$  entry of the original sociomatrix, 0.5 in the  $[i, j]$  entry of of the corresponding sociomatrix if the  $[i, j]$  entry of the original sociomatrix is equal to the  $[j, i]$  entry of the original sociomatrix, and zero otherwise.

**Landau's  $h$**  is used to compare a directed network to a perfect linear hierarchy (a strict dominance-ordering of nodes) [? 2]. This measure is defined as follows:

$$h = \frac{12}{N^3 - N} \sum_{i=1}^N \left[ \text{Out}_i - \frac{N-1}{2} \right]^2 \quad (10)$$

where  $h \in [0, 1]$ . Note that Landau's  $h$  does not provide an individual level metric of importance or relative power. This measure was specifically designed to operate on networks of “has power over” edges, and thus may be difficult to interpret when the network is not explicitly defined on power relations. Because of a preference for chain-like structures, this measure will likely provide poor performance when edges measure social relations. **Kendall's  $K$**  is also designed to compare a directed network to a perfect linear hierarchy [3]. As noted in [2], it often gives an identical value to Landau's  $h$ , but is theoretically distinct. Begin by defining the number of *cyclic triads* ( $CyT$ ) in the network as:

$$CyT = \frac{N(N-1)(2N-1)}{12} - \frac{1}{2} \sum \text{Out}_i^2 \quad (11)$$

Then we can define Kendal's  $K$  as

$$K = 1 - \frac{d}{d_{max}} \quad (12)$$

where the value  $d_{max}$  is defined as follows:

$$d_{max} = \begin{cases} \frac{1}{24}(N^3 - N) & \text{if } N \text{ is odd} \\ \frac{1}{24}(N^3 - 4N) & \text{if } N \text{ is even} \end{cases} \quad (13)$$

Kendal's  $K \in [0, 1]$  is also only defined as a global measure, and no individual level analogue exists. It was also specifically designed to operate on networks of “has power over” edges, and is therefore likely a poor choice for networks defined over social interactions.

**M-reach degree** was developed to identify ‘key’ players in a network [? ]. It is defined as a measure for each

node  $v_i$  as the number of alters that are reachable from  $v_i$ . If  $G$  is directed then the reachable alters must lie along an outgoing path from  $v_i$ . A closely related measure, **M-reach closeness** is defined as the M-reach degree of a node, but with the contribution of each alter  $j$  that is reachable, weighted by the inverse of the shortest path length between  $i$  and  $j$ . Both of these measures are only defined for individual nodes, so to calculate a global measure for a network, we take the Gini coefficient of the measures calculated for each node  $i$ . The Gini coefficient [?] is a measure of inequality originally developed to measure income inequality in a society. For a vector of values  $x : \{x_i\}_{i=1}^N$  the Gini coefficient  $G$  of that vector is:

$$G = \frac{\sum_i \sum_j |x_i - x_j|}{2 \sum_i \sum_j x_i} \quad (14)$$

In words, it is half of the *average absolute difference* of all pairs of entries in the vector, divided by the average, which acts as a normalizing constant. We take the Gini coefficient of the  $M$ -reach degree and  $M$ -reach closeness values for each node in the network and treat this as our global measure of network hierarchy. Intuitively, this measure is capturing the degree of inequality in access to other nodes in the network. We should expect that a higher degree of inequality in this metric would be associated with a more hierarchical network. One potential shortcoming of these measures is that they only account for out-degree, when incoming ties may be a better signal of power relations in many real-world social networks.

**Global reaching centrality (GRC)** is a generalization of  $M$ -reach degree centrality measure [1], and was designed specifically to measure on any network. When the network is unweighted and directed, let  $C_R(i)$  be the local  $M$ -reach degree centrality of node  $i$ , then the global reaching centrality of the network can be defined as:

$$GRC = \frac{\sum_{i=1}^N [\max(C_R) - C_R(i)]}{N - 1} \quad (15)$$

When the graph is weighted and directed, the authors in [1] propose an alternative formulation of  $C_R(i)$ :

$$C'_R(i) = \frac{1}{N - 1} \sum_{j: 0 < d_{i,j}^{out} < \infty} \left( \frac{\sum_{k=1}^{d_{i,j}^{out}} w_i^{(k)}(j)}{d_{i,j}^{out}} \right) \quad (16)$$

where  $d_{i,j}^{out}$  is the (directed) path length from node  $i$  to node  $j$ , and  $w_i^{(k)}$  is the weight of the  $k$ th edge along this path. This alternative formulation can then be plugged into equation 15 to calculate the GRC for a weighted, directed network. Finally, when the network is unweighted and undirected, the authors in [1] propose an additional alternative formulation of  $C_R(i)$ :

$$C''_R(i) = \frac{1}{N - 1} \sum_{j: 0 < d(i,j) < \infty} \frac{1}{d(i,j)} \quad (17)$$

where  $d_{i,j}$  is the (undirected) path length from node  $i$  to node  $j$ . The intuition of for the interpretation of GRC as a measure of network hierarchy is almost identical to the interpretation of the Gini coefficient of the  $M$ -reach degree and  $M$ -reach closeness values for a network, with only difference being the way the individual measures are aggregated, and its extension to weighted and undirected networks. Again, a potential major shortcoming is that this measure only makes theoretical sense when the outgoing edges in the network signal a power relation where the sender has power over the recipient.

The last measure we consider, **rooted depth** [4], is only defined for networks where a root (a node that has only incoming edges) exists. Let  $N_r$  be the number of node-root pairs in the network. Then the rooted depth of the network

can be defined as:

$$D = \frac{1}{N_r} \sum_{i=1}^{N_r} l_{ri} \quad (18)$$

where  $l$  is the length of the shortest path between root  $r$  and node  $i$ . This measure can only be calculated for the network as a whole. However, given  $R$  roots in a network, we can calculate a local root depth for each node that is equal to the average length of the shortest path between itself and all roots. One of the major problems with this measure is that it is undefined for networks without a root (a node with only incoming edges). This makes it very difficult to apply to most networks (we were only able to calculate it for a small fraction of networks in our sample). Furthermore, since this measure relies on finding nodes with no outgoing ties, it can be very sensitive to the way the network is measured. In general, we do not find rooted depth to be a useful measure in our empirical analysis.

### 3.2. Relationships Between Hierarchy Measures

To begin to understand how these measures are related, we each of these ten measures on a total of 136 social, organizational, and information networks described in greater detail in Section 4. All of these networks are directed, and for almost all of them, we were not able to calculate the rooted depth of the network, and we therefore exclude it from our further analysis. Figure 1 illustrates the correlation coefficients between the nine hierarchy measures we were able to calculate on these networks. As we can see, Landau's  $h$  and Kendal's  $K$  are essentially perfectly correlated and thus largely redundant. These measures are also significantly correlated with the simple degree centralization of the network. We can also see that  $M$ -reach degree and  $M$ -reach closeness Gini coefficients are highly correlated, with both also being significantly correlated with GRC, as expected.

Perhaps surprisingly, the rest of the correlations depicted in Figure 1 are quite small and statistically insignificant, indicating that if all of these measures are valid, they are capturing different dimensions of hierarchy in a network. This finding suggests that either there are multiple dimensions to hierarchy in a network [6], some of these measures do not measure hierarchy, or some combination of both. To investigate this finding further, we perform several statistical and qualitative comparisons between these measures in Section 5.

## 4. Data

We refer to three main sources for our data. The first set of networks, County Managers, contains information on email communications between 17 county managers and their staff. They are categorized as communication networks. Our second set of networks contains information on 17 bills in congress and are classified as co-sponsorship networks. Our final source of data contains all networks found within UCINET. After removing 11 networks that were undirected, two-mode, or extreme outliers, we were left with a total of 136 networks. Of the 102 UCINET datasets included in our analysis, 33 did not have a classification. Since there are no clear guidelines on how UCINET defined types for each dataset, the accurate categorization of these 33 networks did not appear viable. These datasets are classified as unknown networks. Descriptive statistics for each of the nine types of networks we consider in this study are provided in Table 1.

Before fitting any of the hierarchy measures on these real datasets, we want to make sure that the measures are invariant to the size of the network. We simulate 7500 Barabasi-Albert (BA), 6000 Tree-Structured (TR), and 4500 Erdos-Renyi (ER) datasets, where one third of each type has 50 nodes, a third has 200, and the last third has 500. We are also curious to see how the hierarchy measures perform while altering the parameters of these datasets. For the BA datasets, we set the preferential treatment parameter to  $p = 0.5, 1, 2, 5, 10$ . We set the number of children parameter in the TR datasets to be  $c = 2, 5, 10, 50$ , and the probability of forming an edge in the ER datasets to  $d = 0.05, 0.1, 0.2$ . Figures can be found in Appendix C, which illustrate our findings. For the BA networks, we notice that Kendall and Landau's measures do not change as  $p$  increases. We note that all other measures except for degree and closeness decrease as  $p$  increases. For TR networks,

Figure 1. Pearson correlation coefficients between nine measures of network hierarchy. A black **X** in a cell indicates that there was not a significant correlation between measures at the  $\alpha = 0.05$  level of significance. Note that the correlation between Landau's  $h$  and Kendall's  $K$  was  $\approx 0.9996$  but was not exactly 1.

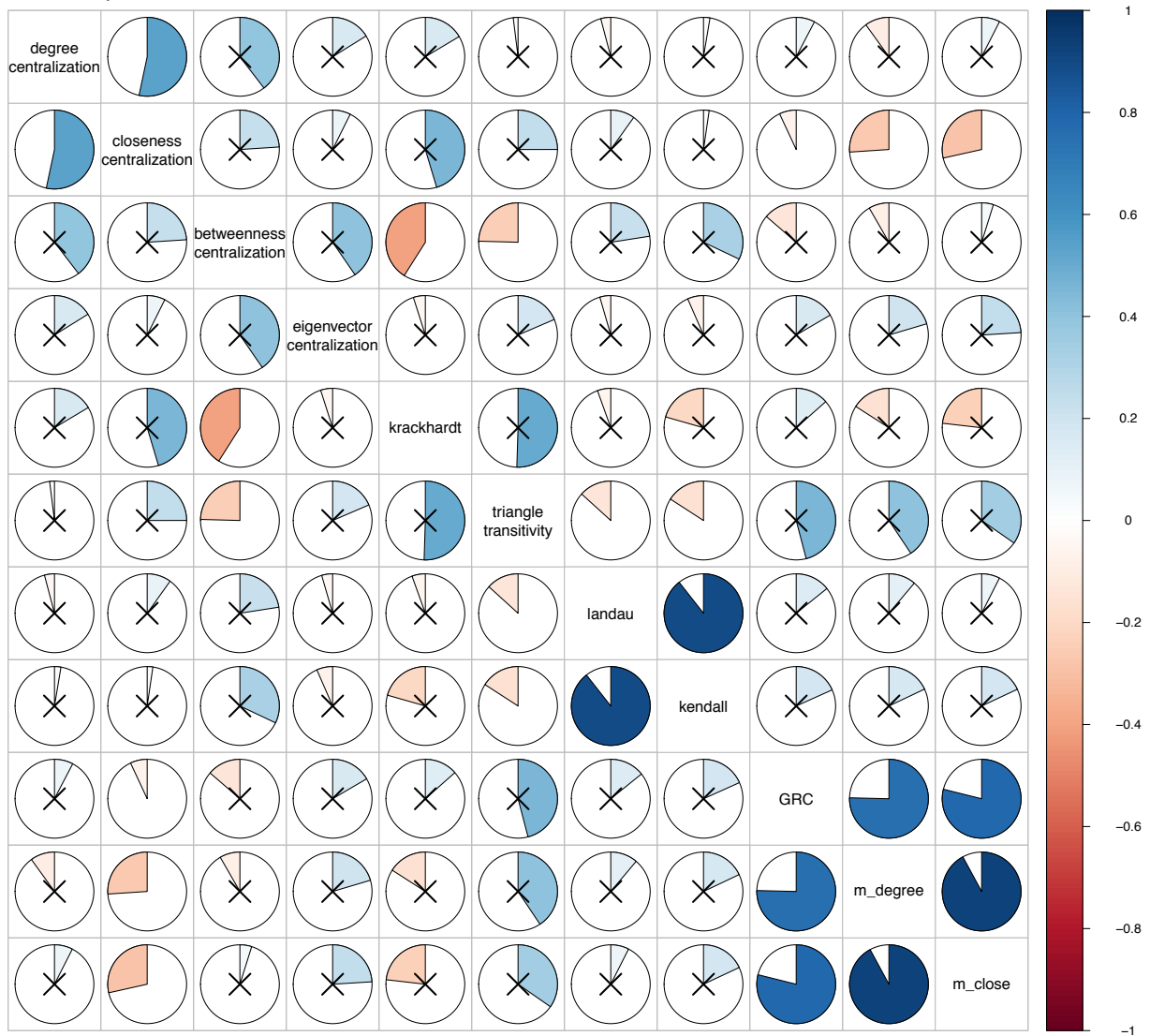
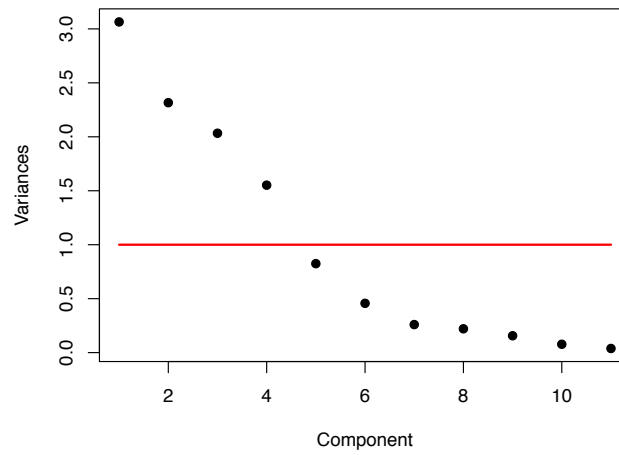


Table 1. Network Descriptive statistics for all 136 networks in our sample, aggregated by the network type. All columns are averages over networks of that type.

Type	# of Networks	Nodes	Edges	Density	Clustering Coefficient
<i>communication</i>	20	25.40	1764.25	2.87	0.55
<i>cosponsorship</i>	18	101.22	13358.89	1.32	0.79
<i>co-membership</i>	2	21.50	22.50	0.05	0.07
<i>interaction</i>	40	23.07	1944.95	1.99	0.59
<i>unknown</i>	33	38.70	445.36	0.38	0.43
<i>friendship</i>	6	29.83	92.00	0.12	0.35
<i>affect</i>	11	17.64	95.18	0.32	0.33
<i>terrorism</i>	1	63.00	308.00	0.08	0.36
<i>trade</i>	5	24.00	285.60	0.52	0.73

Figure 2. Eigenvalues for 9 largest principle components in our analysis indicate that we should examine the first three components, which all have eigenvalues greater than one.



## 5. Analysis

### 5.1. Principle Components Analysis

PCA component eigenvalues are illustrated in Figure 2. A graphical comparison of components one and two is provided in 3. A graphical comparison of components one and three is provided in 4. A graphical comparison of components two and three is provided in 5.

### 5.2. Simulation Study

### 5.3. Ground Truth Rankings

## 6. Conclusions

test



Figure 3. Principle components plot for components one and two.

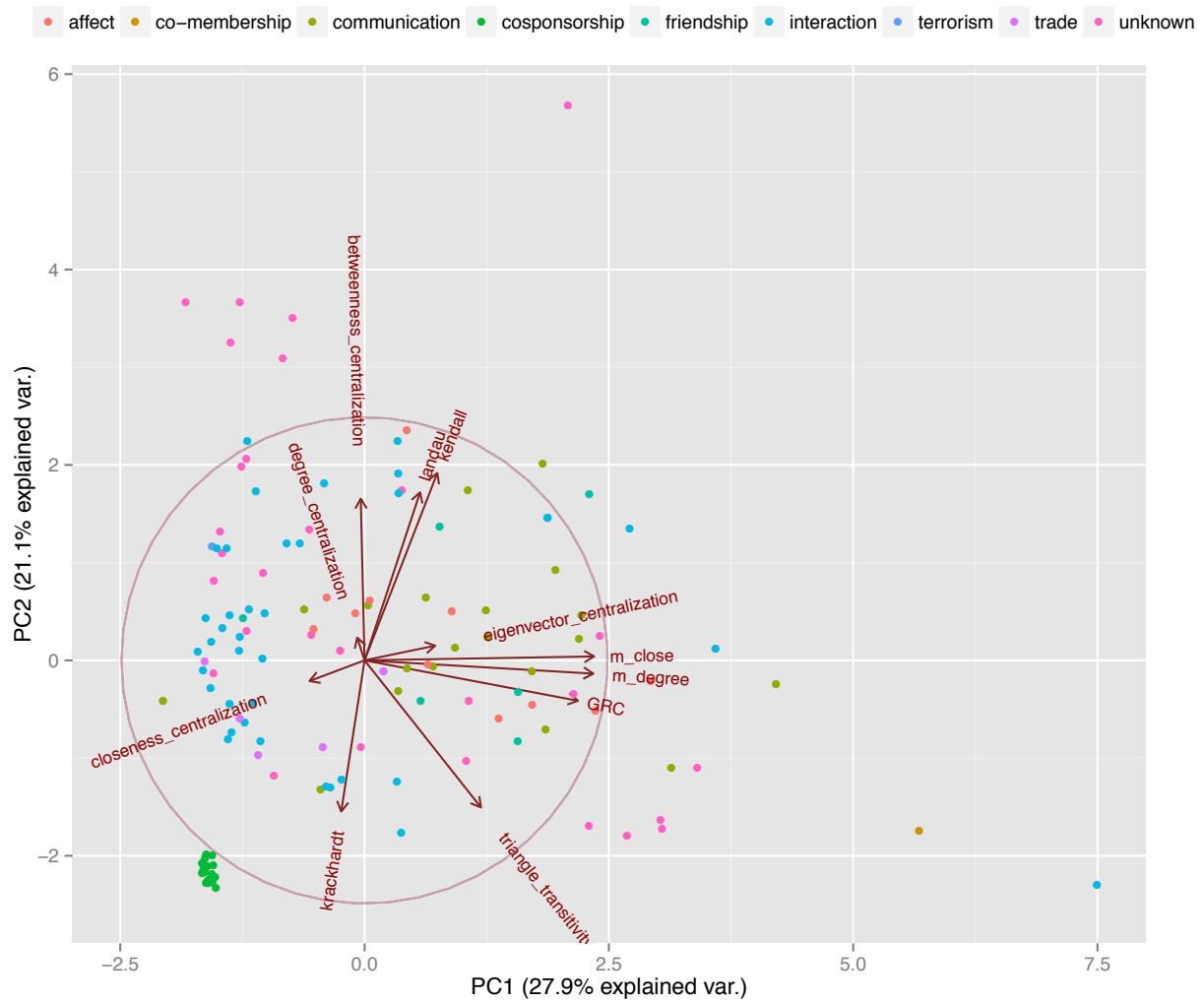


Figure 4. Principle components plot for components one and three.

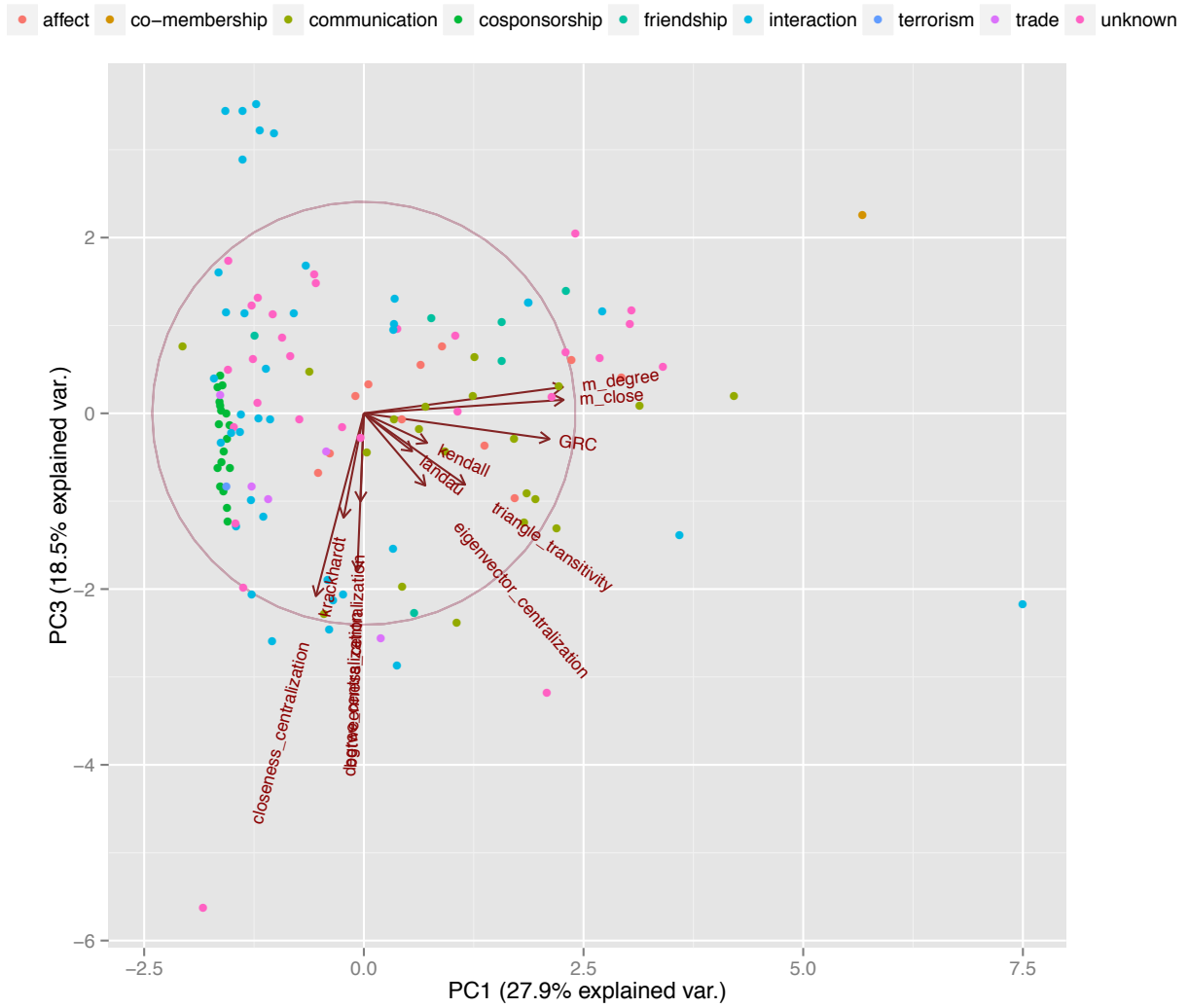


Figure 5. Principle components plot for components two and three.

● affect 
 ● co-membership 
 ● communication 
 ● cosponsorship 
 ● friendship 
 ● interaction 
 ● terrorism 
 ● trade 
 ● unknown

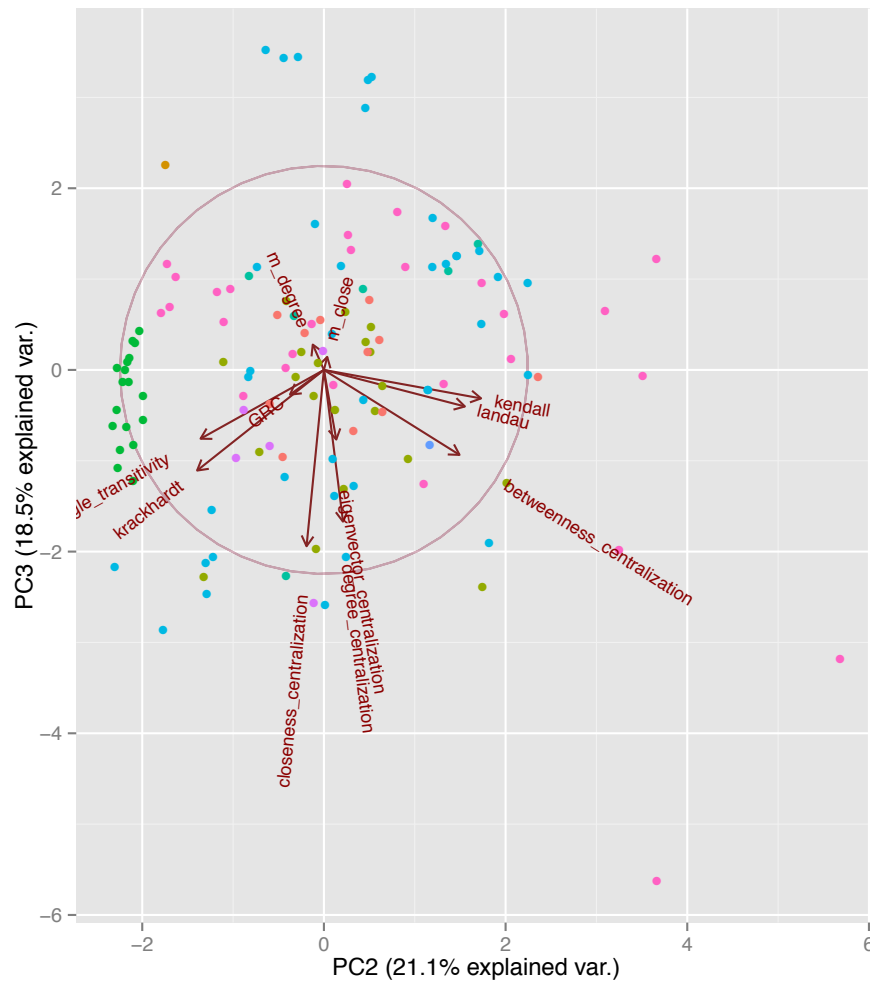


Figure 6. All figures show the average normalized global measure (denoted by the symbol in the bottom right key) by parameter value. The top left plot is for BA networks. The top right is for TR networks. The bottom left is for ER networks.

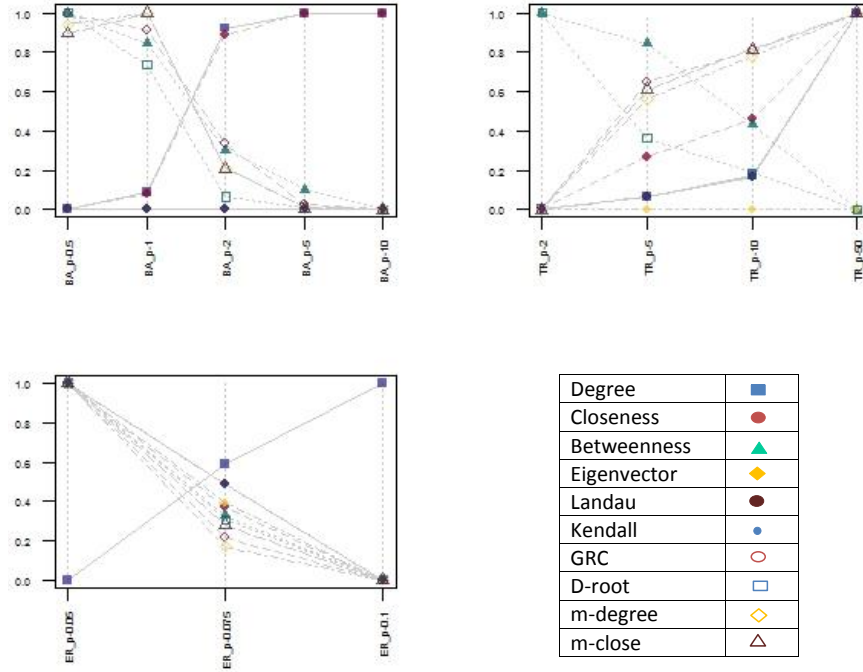
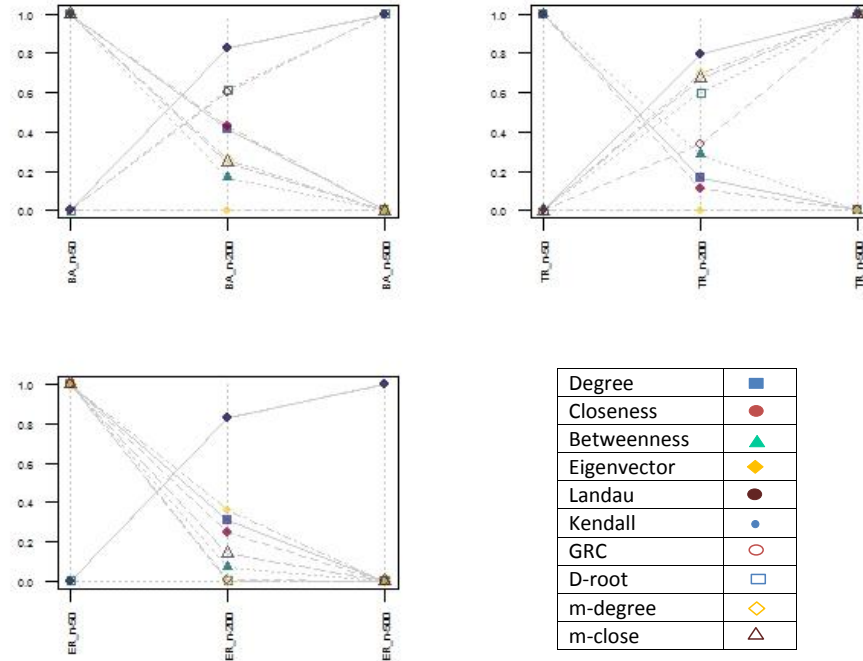


Figure 7. All figures show the average normalized global measure (denoted by the symbol in the bottom right key) by number of nodes. The top left plot is for BA networks. The top right is for TR networks. The bottom left is for ER networks.



	average_rank
degree centrality	0.75
closeness centrality	0.82
betweenness centrality	0.78
eigenvector centrality	0.78
m_degree	0.81
m_close	0.63
GRC	0.36
D_root	0.86

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## Appendix A. Dataset References

1. Adolescent Health: survey asked students to list 5 male and female friends. [? ]
2. Residence Hall: friendships between 217 students in Australian National University. [? ]
3. Taro Exchange: gift-giving relationships between households in a Papaun village. [? ]
4. Highschool: friendship relationship between boys at a small Indiana high school in 1957-1958. [? ]
5. Dutch College: friendships between 32 university freshmen. [? ]
6. Monks: preference ratings between monks in a cloister during a crisis. [? ]
7. Physicians: innovation spread between 246 physicians in Illinois. [? ]
8. Seventh graders: activity specific proximity rankings for 29 middle school students in Victoria [? ].
9. Prosper loans: loans between users of prosper.com [? ].
10. Libimseti.cz: likes between users on a Czech dataing site [? ].
11. Digg: friendships on Digg [? ].
12. Youtube: connections between Youtube users [? ].
13. Epinions: who-trusts-whom between users of epinions [? ].
14. EU emails: emails for 18 months from a major European research institution [? ].
15. Facebook: friends lists from FAcbook, generated through a Facebook app survey [? ].
16. Google Plus: friends between users who selected to “share circles” on Google Plus [? ].
17. Linx kernel mailing list: communication network for the linux kernel mailing list, where each edge is a reply from a user to another [? ].
18. Livejournal: map of an online community friendships of Livejournal users [? ].
19. Manufacturing: communication network between employess of a mid-size manufacturing firm [? ].
20. Pokec: Friendship networks in the Pokec online social network, popular in Slovakia [? ].
21. Slashdot: tagging between users in slashdot for 2008 and 2009 [? ].
22. Twitter: circles between twitter users [? ].
23. UC Irvine: messages sent between students on an online community at UC Irvine [? ].
24. U. Rovira i Virgili: email communication network from University Rovira i Virgili in Tarragona [? ].