Полиморфизм в Haskell и typeclasses Краткий ликбез и пример

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Слушатели

• Воспринимают густые слайды

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 - с последовательно вываливающимися элементами

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Слушатели

- Воспринимают густые слайды
 с последовательно вываливающимися элементами
- Легко читают код со слайдов
- Стремятся задать вопрос, когда непонятно

Algebraic data types

data $X = A \mid B \text{ Int } \mid C \text{ Int String}$

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• Применение функций

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• Базовые типы

Algebraic data types

data
$$X = A \mid B \text{ Int } \mid C \text{ Int String}$$

• Применение функций

• Базовые типы

Pattern matching

Algebraic data types

data
$$X = A \mid B \text{ Int } \mid C \text{ Int String}$$

• Применение функций

• Базовые типы

- Pattern matching
- Синтаксис списков

О чём доклад

- Параметрический и ad-hoc полиморфизм
- Тайпклассы и полиморфизм
- Возможности, которые даёт использование полиморфизма
 - ▶ Чужой код работает иначе
 - ▶ Наш код работает по-разному

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Доклад не подразумевает полноту изложения

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 - ▶ Наш код работает по-разному

Доклад не подразумевает полноту изложения ...и немного лукавит

```
prepend :: Int -> [Int] -> [Int]
prepend a xs = a:xs
```

```
prepend :: Int -> [Int] -> [Int]
prepend a xs = a:xs
append :: Int -> [Int] -> [Int]
append a [] = [a]
append a (x:xs) = x:(append a xs)
```

```
prepend :: Int -> [Int] -> [Int]
prepend a xs = a:xs

append :: Int -> [Int] -> [Int]
append a [] = [a]
append a (x:xs) = x:(append a xs)

zip' :: [Int] -> [Double] -> [(Int, Double)]
zip' [] = []
zip' [] = []
zip' (a:as) (b:bs) = (a, b):(zip' as bs)
```

```
prepend :: Int -> [Int] -> [Int]
prepend a xs = a:xs
append :: Int -> [Int] -> [Int]
append a [] = [a]
append a (x:xs) = x:(append a xs)
zip' :: [Int] -> [Double] -> [(Int, Double)]
zip' [] = []
zip' _ [] = []
zip'(a:as)(b:bs) = (a, b):(zip'as bs)
```

Важны ли конкретные типы Int и Double?

Что именно они делают, не зависит от этих типов

```
prepend :: a -> [a] -> [a]
prepend a xs = a:xs

append :: a -> [a] -> [a]
append a [] = [a]
append a (x:xs) = x:(append a xs)

zip' :: [a] -> [b] -> [(a, b)]
zip' [] = []
zip' _ [] = []
zip' (a:as) (b:bs) = (a, b):(zip' as bs)
```

```
prepend :: a -> [a] -> [a]
prepend a xs = a:xs
append :: a -> [a] -> [a]
append a [] = [a]
append a (x:xs) = x:(append a xs)
zip' :: [a] -> [b] -> [(a, b)]
zip' [] = []
zip' _ [] = []
zip'(a:as)(b:bs) = (a, b):(zip'as bs)
```

Type-level и value-level namespace'ы различны

Type-level и value-level namespace'ы различны

Только структура аргументов

```
head :: [a] -> Maybe a
head [] = Nothing
head (x:_) = Just x
```

```
head :: [a] -> Maybe a
head [] = Nothing
head (x:_) = Just x
```

Даже тар!

```
map :: (a -> b) -> [a] -> [b]
map _ [] = []
map f (x:xs) = (f x):(map xs)
```

maximum :: [a] -> Maybe a

```
maximum :: [a] -> Maybe a
maximumInt :: [Int] -> Maybe Int
maximumInt [] = Nothing
maximumInt (x:xs) = Just $ findMax xs x where
 findMax[] c = c
 findMax (x:xs) c = findMax xs $ if x < c then c else x
maximumDouble :: [Double] -> Maybe Double
maximumDouble [] = Nothing
maximumDouble (x:xs) = Just $ findMax xs x where
 findMax [] c = c
 findMax (x:xs) c = findMax xs $ if x < c then c else x
```

```
maximum :: [a] -> Maybe a
maximumInt :: [Int] -> Maybe Int
maximumInt [] = Nothing
maximumInt (x:xs) = Just $ findMax xs x where
 findMax[] c = c
 findMax (x:xs) c = findMax xs $ if x < c then c else x
maximumDouble :: [Double] -> Maybe Double
maximumDouble [] = Nothing
maximumDouble (x:xs) = Just $ findMax xs x where
 findMax [] c = c
 findMax (x:xs) c = findMax xs $ if x < c then c else x
```

Тела функций одинаковые

Но ведут функции себя немного по-разному

fold :: [a] -> Maybe a

```
fold :: [a] -> Maybe a

foldInt :: [Int] -> Maybe Int

foldInt [] = Nothing

foldInt (x:xs) = Just $ foldNE x xs where
   foldNE x xs = maybe x (x +) $ fold xs

foldString :: [String] -> String

foldString [] = Nothing

foldString (x:xs) = Just $ foldNE x xs where
   foldNE x xs = maybe x (x ++) $ fold xs
```

```
fold :: [a] -> Maybe a
foldInt :: [Int] -> Maybe Int
foldInt [] = Nothing
foldInt (x:xs) = Just $ foldNE x xs where
  foldNE x xs = maybe x (x +) $ fold xs
foldString :: [String] -> String
foldString [] = Nothing
foldString (x:xs) = Just $ foldNE x xs where
  foldNE x xs = maybe x (x ++) $ fold xs
Функции принципиально делают одно и то же
```

Но ведут себя по-разному в зависимости от типа

... от типа?

```
foldIntM :: [Int] -> Maybe Int
foldIntM [] = Nothing
foldIntM (x:xs) = Just $ foldNE x xs where
  foldNE x xs = maybe x (x +) $ fold xs

foldIntS :: [Int] -> Maybe Int
foldIntS [] = Nothing
foldIntS (x:xs) = Just $ foldNE x xs where
  foldNE x xs = maybe x (x *) $ fold xs
```

Два пути

• Оставаться в параметрическом полиморфизме

```
maximum :: forall a. (a->a->Bool) -> [a] -> Maybe a fold :: forall a. (a->a->a) -> [a] -> Maybe a
```

Два пути

• Оставаться в параметрическом полиморфизме

```
maximum :: forall a. (a->a-><mark>Bool</mark>) -> [a] -> Maybe a fold :: forall a. (a->a->a) -> [a] -> Maybe a или даже

data Ord a = MkOrd (a -> a -> Bool)
```

```
data Ord a = MkOrd (a -> a -> Bool)
maximum :: forall a. Ord a -> [a] -> Maybe a
```

Два пути

Оставаться в параметрическом полиморфизме

```
maximum :: forall a. (a->a->Bool) -> [a] -> Maybe a
fold :: forall a. (a->a->a) -> [a] -> Maybe a
или даже
data Ord a = MkOrd (a -> a -> Bool)
```

```
maximum :: forall a. Ord a -> [a] -> Maybe a
```

Ad-hoc полиморфизм

```
maximum :: forall a E ordered. [a] -> Maybe a
fold :: forall a E squashable. [a] -> Maybe a
↑ это не синтаксис Haskell ↑
```

```
data Ord a = MkOrd (a -> a -> Bool)
maximum :: Ord a -> [a] -> Maybe a

data Semi a = MkSemi (a -> a -> a)
fold :: Semi a -> [a] -> Maybe a
```

```
data Ord a = MkOrd (a -> a -> Bool)
maximum :: Ord a -> [a] -> Maybe a

data Semi a = MkSemi (a -> a -> a)
fold :: Semi a -> [a] -> Maybe a

maxes :: Ord a -> [[a]] -> [Maybe a]
maxes ord = map $ maximum ord
```

```
data Ord a = MkOrd (a -> a -> Bool)
maximum :: Ord a -> [a] -> Maybe a
data Semi a = MkSemi (a -> a -> a)
fold :: Semi a -> [a] -> Maybe a
maxes :: Ord a -> [[a]] -> [Maybe a]
maxes ord = map $ maximum ord
combMaxes :: Ord a -> Semi a -> [[a]] -> Maybe a
combMaxes o (MkSemi fs) = fold maybeSemi . maxes o
 where
   maybeSemi Nothing y = y
   mavbeSemi x Nothing = x
   maybeSemi (Just x) (Just y) = Just \$ fs x y
```

- Постоянно передавать
- Порядок важен
- Иерархия структур
- Переиспользование преобразований
- Полиморфизм на преобразованиях
- ..

```
maximum :: forall a ∈ ordered. [a] -> Maybe a

↑ это не синтаксис Haskell ↑
```

```
maximum :: forall a ∈ ordered. [a] -> Maybe a

↑ это не синтаксис Haskell ↑

class Ord a where
  (<) :: a -> a -> Bool

maximum :: forall a. Ord a => [a] -> Maybe a
```

```
maximum :: forall a E ordered. [a] -> Maybe a
↑ это не синтаксис Haskell ↑
class Ord a where
  (<) :: a -> a -> Bool
maximum :: forall a. Ord a => [a] -> Maybe a
maximum [] = Nothing
maximum (x:xs) = Just $ findMax xs x where
  findMax [] c = c
  findMax (x:xs) c = findMax xs $ if x < c then c else x
```

```
class Semigroup a where
  (<>) :: a -> a -> a

fold :: Semigroup a => [a] -> Maybe a
fold [] = Nothing
fold (x:xs) = Just $ foldNE x xs where
  foldNE x xs = maybe x (x <>) $ fold xs
```

Тайпклассы: инстансы

```
class Semigroup a where
  (<>) :: a -> a -> a

fold :: Semigroup a => [a] -> Maybe a
```

Тайпклассы: инстансы

```
class Semigroup a where
  (<>) :: a -> a -> a
fold :: Semigroup a => [a] -> Maybe a
instance Semigroup Int where
  (<>) = (+)
instance Semigroup String where
  (<>) = (++)
```

Тайпклассы: инстансы

```
class Semigroup a where
  (<>) :: a -> a -> a
fold :: Semigroup a => [a] -> Maybe a
instance Semigroup Int where
  (<>) = (+)
instance Semigroup String where
  (<>) = (++)
fold [1, 2, 3] -- gives Just 6
fold ["1", "2", "3"] -- gives Just "123"
```

Тайпклассы: условные инстансы

Жизнь налаживается

```
maxes :: Ord a => [[a]] -> [Maybe a]
maxes = map maximum
```

Жизнь налаживается

```
maxes :: Ord a => [[a]] -> [Maybe a]
maxes = map maximum

combMaxes :: (Ord a, Semigroup a) => [[a]] -> Maybe a
combMaxes = fold . maxes
```

Жизнь налаживается

```
maxes :: Ord a => [[a]] -> [Maybe a]
maxes = map maximum

combMaxes :: (Ord a, Semigroup a) => [[a]] -> Maybe a
combMaxes = fold . maxes
```

Но есть нюансы

- не так легко подставлять свои функции
- выбор тайпклассов должен быть удачным

```
newtype Last a = Last a
getLast :: Last a -> a
getLast (Last a) = a
newtype First a = First { getFirst :: a }
```

```
newtype Last a = Last a
getLast :: Last a -> a
getLast (Last a) = a

newtype First a = First { getFirst :: a }
instance Semigroup (Last a) where
   _ <> x = x
instance Semigroup (First a) where
   x <> _ = x
```

```
newtype Last a = Last a
getLast :: Last a -> a
qetLast (Last a) = a
newtype First a = First { getFirst :: a }
instance Semigroup (Last a) where
 <> X = X
instance Semigroup (First a) where
 X \ll X = X
head :: [a] -> Maybe a
head = fmap getFirst . fold . map First
last :: [a] -> Maybe a
last = fmap getLast . fold . map Last
```

Тайпклассы: функции по умолчанию

class Ord a where

- (<) :: a -> a -> Bool
- (>) :: a -> a -> Bool

$$a > b = b < a$$

Тайпклассы: функции по умолчанию

class Ord a where (<) :: a -> a -> Bool (>) :: a -> a -> Bool a > b = b < a (<=) :: a -> a -> Bool

Тайпклассы: функции по умолчанию

class Ord a where

```
(<) :: a -> a -> Bool
(>) :: a -> a -> Bool
a > b = b < a
(<=) :: a -> a -> Bool
(==) :: a -> a -> Bool
(/=) :: a -> a -> Bool
a <= b = a < b \mid \mid a == b
```

Иерархия тайпклассов

```
class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool
  a == b = not \$ a /= b
  a /= b = not \$ a == b
class Eq a => Ord a where
  (<) :: a -> a -> Bool
  (>) :: a -> a -> Bool
  (<=) :: a -> a -> Bool
  (>=) :: a -> a -> Bool
  a <= b = a < b | | a == b
```

Когерентность

```
class Semigroup a => Monoid a where
  mempty :: a

class Semigroup a => ReversibleSemigroup a where
  rev :: a -> a
```

Когерентность

```
class Semigroup a => Monoid a where
 mempty :: a
class Semigroup a => ReversibleSemigroup a where
  rev :: a -> a
f :: (Monoid a, ReversibleSemigroup a) =
  rev mempty <> mempty
 ↑ гарантируется, что <> одна и та же ↑
```

Когерентность

Из-за этого иерархия инстансов повторяет иерархию классов

```
instance Semigroup String where
  (<>) = (++)

instance Monoid String where
  mempty = ""
```

Поиск инстансов

Не "если есть это, то инстанс вот", а "вот инстанс, для него мне требуется"

При поиске инстансов рассматривается только часть правее "=>"

Поиск инстансов

class Impossible a where

Не "если есть это, то инстанс вот", а "вот инстанс, для него мне требуется"

При поиске инстансов рассматривается только часть правее "=>"

```
magic :: forall b. a -> b

instance Impossible a => Semigroup a where
  a <> _ = magic a
```

Поиск инстансов

Не "если есть это, то инстанс вот", а "вот инстанс, для него мне требуется"

При поиске инстансов рассматривается только часть правее "=>"

```
class Impossible a where
  magic :: forall b. a -> b
```

```
instance Impossible a => Semigroup a where
a <> = magic a
```

Такой инстанс полностью выключает любой поиск для Semigroup

kind *

Int, [Int], Maybe Int, Either String Int, Int -> String

kind *

Int, [Int], Maybe Int, Either String Int, Int -> String

class Semigroup a where

```
kind *
Int, [Int], Maybe Int, Either String Int, Int -> String
class Semigroup a where
  (<>) :: a -> a -> a
```

```
kind * -> *
```

Maybe, Either String, (->) Int

```
kind *
Int, [Int], Maybe Int, Either String Int, Int -> String

class Semigroup a where
  (<>) :: a -> a -> a

kind * -> *
Maybe, Either String, (->) Int
```

class Functor m where

fmap :: (a -> b) -> m a -> m b

О чём ещё можно продолжить

- instance resolution
 - overlapping instances
- много типов
 - multiparameter typeclasses
 - ▶ functional dependencies
 - type families
- вывод тайпклассов
 - derivable typeclasses
 - newtype deriving
 - deriving via
- ...

Пример: исходное состояние

```
putStrLn :: String -> IO ()
getLine :: IO String

program :: IO ()
program = do
   putStrLn "What is your name?"
   name <- getLine
   putStrLn ("Hi, " ++ name)</pre>
```

Пример: исходное состояние

```
putStrLn :: String -> IO ()
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program :: IO ()
program = do
   putStrLn "What is your name?"
   name <- getLine
   putStrLn ("Hi, " ++ name)</pre>
```

Как протестировать, что функция делает ровно то, что там надо?

Пример: выделили абстракцию

```
class ConsoleIO m where
  putStrLn :: String -> m ()
  getLine :: m String
```

Пример: выделили абстракцию

```
class ConsoleI0 m where
  putStrLn :: String -> m ()
  getLine :: m String

program :: (Monad m, ConsoleI0 m) => m ()
program = do
  putStrLn "What is your name?"
  name <- getLine
  putStrLn ("Hi, " ++ name)</pre>
```

Пример: выделили абстракцию

```
class Monad m => ConsoleIO m where
  putStrLn :: String -> m ()
  getLine :: m String

program :: ConsoleIO m => m ()
program = do
  putStrLn "What is your name?"
  name <- getLine
  putStrLn ("Hi, " ++ name)</pre>
```

```
instance ConsoleI0 IO where
  putStrLn = Prelude.putStrLn
  getLine = Prelude.getLine
```

class MonadIO m where
 liftIO :: IO a -> m a

```
class MonadIO m where
  liftIO :: IO a -> m a
```

```
instance MonadIO m => ConsoleIO m where
  putStrLn = liftIO . Prelude.putStrLn
  getLine = liftIO $ Prelude.getLine
```

```
class MonadIO m where
  liftIO :: IO a -> m a
```

```
instance MonadIO m => ConsoleIO m where
  putStrLn = liftIO . Prelude.putStrLn
  getLine = liftIO $ Prelude.getLine
```

Скомпилируется?

```
class MonadIO m where
  liftIO :: IO a -> m a
```

```
instance MonadIO m => ConsoleIO m where
  putStrLn = liftIO . Prelude.putStrLn
  getLine = liftIO $ Prelude.getLine
```

Скомпилируется?

Взлетит?

```
class MonadIO m where
  liftI0 :: I0 a -> m a
newtype RealConsoleT m a = RealConsoleT
                         { runRealConsole :: m a }
 deriving (Functor, Applicative, Monad, MonadIO)
instance MonadIO m => ConsoleIO (RealConsoleT m) where
  putStrLn = liftIO . putStrLn
  getLine = liftI0 $ getLine
```

```
class MonadIO m where
  liftI0 :: I0 a -> m a
newtype RealConsoleT m a = RealConsoleT
                         { runRealConsole :: m a }
 deriving (Functor, Applicative, Monad, MonadIO)
instance MonadIO m => ConsoleIO (RealConsoleT m) where
  putStrLn = liftIO . putStrLn
  getLine = liftI0 $ getLine
```

Скомпилируется?

```
class MonadIO m where
  liftI0 :: I0 a -> m a
newtype RealConsoleT m a = RealConsoleT
                         { runRealConsole :: m a }
 deriving (Functor, Applicative, Monad, MonadIO)
instance MonadIO m => ConsoleIO (RealConsoleT m) where
  putStrLn = liftIO . putStrLn
  getLine = liftI0 $ getLine
Скомпилируется?
```

Взлетит?

```
program :: ConsoleI0 m => m ()
instance ConsoleI0 IO where ...
instance MonadI0 m => ConsoleI0 (ReadConsoleT m) where .
instance Applicative m => ConsoleI0 (NoConsoleT m) where
```

```
program :: ConsoleI0 m => m ()
instance ConsoleI0 IO where ...
instance MonadI0 m => ConsoleI0 (ReadConsoleT m) where .
instance Applicative m => ConsoleI0 (NoConsoleT m) where
```

```
main = program
```

```
program :: ConsoleI0 m => m ()

instance ConsoleI0 I0 where ...
instance MonadI0 m => ConsoleI0 (ReadConsoleT m) where .
instance Applicative m => ConsoleI0 (NoConsoleT m) where
```

```
main = program
main = runRealConsole program
```

```
program :: ConsoleI0 m => m ()

instance ConsoleI0 I0 where ...
instance MonadI0 m => ConsoleI0 (ReadConsoleT m) where .
instance Applicative m => ConsoleI0 (NoConsoleT m) where
```

```
main = program
main = runRealConsole program
main = runNoConsole program
```

Пример: инстанс для тестирования

```
data ScenarioAction = ExpectPrinting String
                      ExpectReading String
newtype TestingConsoleT m a = TestingConsoleT
  (ExceptT String (StateT [ScenarioAction] m) a)
 deriving (Functor, Applicative, Monad,
    MonadState [ScenarioAction], MonadError String)
runTestingConsole :: [ScenarioAction]
                  -> TestingConsoleT m a
                  -> Either String a
instance Monad m => ConsoleIO (TestingConsoleT m) where
  . . .
```

Пример: инстанс для тестирования

```
instance Monad m => ConsoleIO (TestingConsoleT m) where
  putStrLn s = do
    sc <- get
    (curr, sc') <- case sc of
      [] -> throwError "Scenario ended, but putStrLn"
      (x:xs) \rightarrow pure(x, xs)
    put sc'
    case curr of
      ExpectPrinting exp ->
        when (s /= exp) $ throwError "Wrong is printed"
      ExpectReader -> throwError "Reading is expected"
  getLine = ...
```

Пример: запуск для тестирования

```
scenario =
  [ ExpectPrintlng "What is your name?"
  , ExpectReading "Denis"
  , ExpectPrinting "Hi, Denis" ]
runTestingConsole scenario program -- gives Right ()
```

Пример: запуск для тестирования

```
scenario =
  [ ExpectPrintlng "What is your name?"
  , ExpectReading "Denis"
  , ExpectPrinting "Hi, Denis" ]
runTestingConsole scenario program -- gives Right ()
В hpec можно это использовать так:
spec = describe "Hello program" do
         it "asks and responds" do
           testRun `shouldBe` Right ()
 where
    testRun = runTestingConsole scenario program
```

Спасибо