

Detailed description

For using z3 follow <https://rise4fun.com/z3/tutorial>

Exercise 1

1. The precondition is that n has to be an integer and $n > 1$

The postcondition is that m integer, $m > n$, $m \% i == 0 \ \&\& \ n \% i == 0$

2. The program implementation in c is in src and the implementation in maude in maude/Exercise1.maude

```
in pl-builtins.maude
in cink-syntax.maude
in tableaux.maude

mod Exercise1 is including CINK-SYNTAX .

ops primality : -> DeclId .
ops exercise1 : -> Stmt .

eq exercise1 =
  int primality ( int n )
  {
    if ( n > 1 ) {
      int m ;
      m = n + 1 ;
      int i ;
      i = 2 ;

      while ( m % i != 0 || n % i != 0 ) {
        if ( i > m / 2 ) { m = m + 1 ; i = 2 ; } else { i = i +
1 ; }
      }
      return m ;
    }
    return -1 ;
  }

void main () {
  int m ;
  m = primality ( 5 );
  printf("%d;", m) ;
}

.

endm
```

To execute it run: `maude Exercise1.maude`

3. The tableaux code for our program is in tableaux.maude.

To execute it run: `maude Exercise.maude`

4. Use v3 to verify the program

The implications are :

1. $i > m / 2 \rightarrow [2 / i][m + 1 / m]$
2. $n \leq m \ \&\& \ (n \% i == 0 \ \&\& \ m \% i == 0)$

Exercise 2

1. We added Exercise2.maude which is a module that contains 3 examples of problems and operations with arrays.

In cink-syntax.maude we added the following operations:

```
- op int_[] : Exp Id -> DeclId [prec 40] .
- op int[] : Exp -> DeclId [prec 40] .
- op _[]=_ : Exp Id Exp -> Exp [ prec 40 ] .
- _=_[] : Exp Exp Id -> Exp [ prec 40 ] .
- op _[]=_[] : Exp Id Exp Id -> Exp [ prec 40 ] .
- op _[]=_[] : Exp Stmt Exp Stmt -> Exp [ prec 40 ] .
- op printf("%d;",_[]) : Exp Id -> Exp .
```

2. In Exercise2 we added 3 examples of operations with arrays.

```
in pl-builtins.maude
in cink-syntax.maude

mod Exercise2 is including CINK-SYNTAX .

ops example1 : -> Stmt .
ops example2 : -> Stmt .
ops example3 : -> Stmt .

eq example1 =

    int a[5];
    int i ;
```

```

        i = 2 ;
        a[1] = 7 ;
        a[i * 2] = 5 + a[i + 1] ;
        .

eq example2 =

    int a[5];
    int b[3] ;
    b = a ;
    printf("%d;", b[1]) ;
    .

eq example3 =

    int i ;
    i = 0 ;
    int a[5] ;

    while(i < 5){
        a[i] = i + 1 ;
        i = i + 1 ;
        printf("%d;", a[i]) ;
    }

    int b[] = a[5] ;

    i = 0 ;
    while(i < 5){
        b[i] = i * 2 + a[i] ;

        i = i + 1 ;

        a[i] = b[i - 1] ;
    }
    .

endm

```

Exercise 3

- 1.
2. Exercise 3 solution implemented with the cink changes to support arrays

```

in pl-builtins.maude
in cink-syntax.maude

mod Exercise3 is including CINK-SYNTAX .
  ops contains0 : -> DeclId .
  ops example1 : -> Stmt .

```

```

eq example1 =
  int contains0 ( int a[], int j ){
    int i = 0 ;

    while(i < j){
      if(a[i] == 0){
        printf("%d;", i) ;
        return 0 ;
      }

      i = i + 1 ;
    }

    return -1 ;
  }

  void main(){
    int a[4] = {1, 2, 6, 4, 0} ;
    int i ;
    i = contains0(a, 4) ;

    printf("%d;", i) ;
  }
  .
endm

```

The changes to support this were the addition of dynamic allocation operation:

```

op _[_]={_} : Exp Id List{Exp} -> Exp [prec 0 ] .

```