

第五章：循环

胡兆龙

E-mail:huzhaolong@zjnu.edu.cn

基本框架

- while 循环
- 循环设计策略
- 利用哨兵值控制循环
- for 循环
- 嵌套循环
- 最小化数值误差
- break 和 continue

简介

打印字符串 **Programming is fun!** 100 次.

100 times {
 print("Programming is fun!")
 print("Programming is fun!")
 ...
 print("Programming is fun!")

```
count = 0
```

```
while count < 100:  
    print("Programming is fun!")  
    count = count + 1
```

条件控制循环，
一个表达式

```
for i in range(100):  
    print('Prgoramming is fun')
```

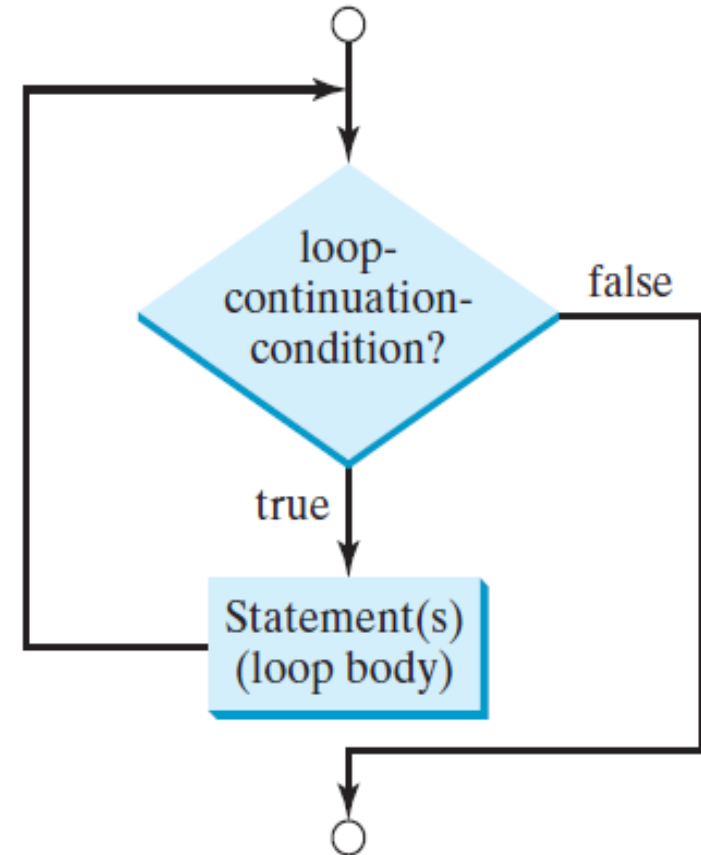
计数器控制循环，
一般知道迭代次数

while 循环

The syntax for the **while** loop is:

```
while loop-continuation-condition:  
    # Loop body  
    Statement(s)
```

推荐使用一个tab键
或者4个空格键



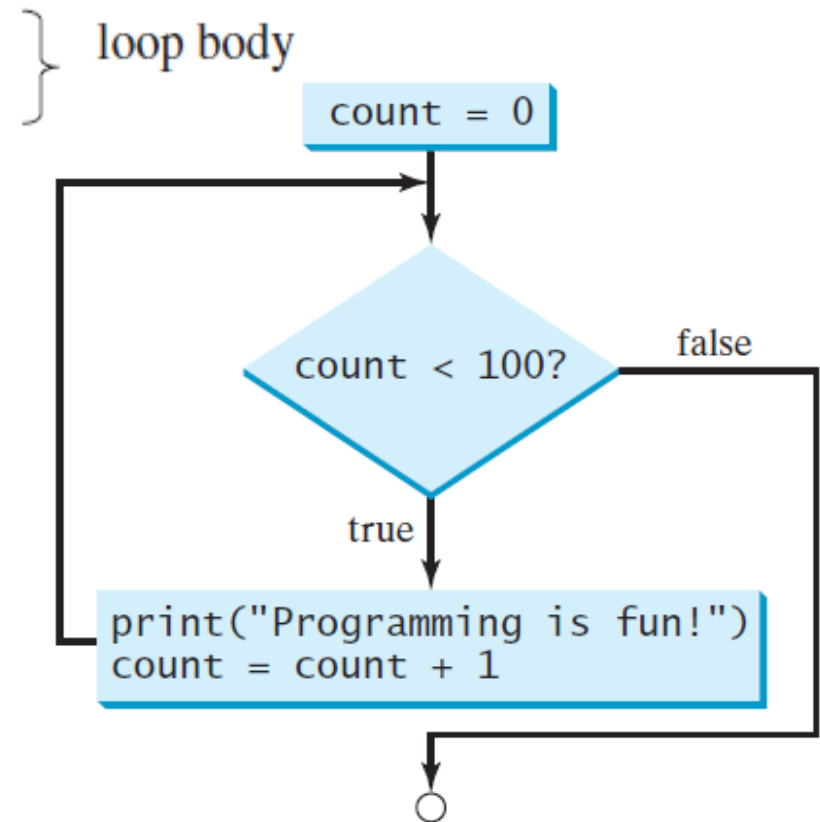
(a) A while loop

while 循环

```
count = 0
while count < 100:
    print("Programming is fun!")
    count = count + 1
```

loop-continuation-condition

} loop body



while 循环

```
sum = 0
i = 1
while i < 10:
    sum = sum + i
    i = i + 1
print("sum is", sum)
```

$i = 9$

$i = 10$

$sum = 1 + 2 + \dots + 9$

条件始终满足

```
sum = 0
i = 1
while i < 10:
    sum = sum + i
    i = i + 1
```

无限循环（死循环），
用 `ctrl + c` 跳出循环。

while 循环

```
count = 0
while count <= 100:
    print("Programming is fun!")
    count = count + 1
```

迭代了 101 次,被称为:
偏离 1 的误差。

结果是什么?

```
count = 0
while (count < 9):
    print('The count is:', count)
    count = count + 1
```

while 循环

```
i = 1
while i < 10:
    if i % 2 == 0:
        print(i)
```

(a) 死循环

```
i = 1
while i < 10:
    if i % 2 == 0:
        print(i)
    i += 1
```

(b) 死循环

这些循环体将会循环多少次？每个程序的结果是什么？

```
i = 1
while i < 10:
    if i % 2 == 0:
        print(i)
    i += 1
```

2
4
6
8

(c)

循环设计策略

Step 1: 找出需要被循环的语句

Step 2: 将循环语句写成如下形式:

while True:

 语句 (statements)

Step 3: 编写循环条件, 并给出控制循环的语句, 如

while 循环条件:

 语句 (statements)

 控制语句

例子：猜一个数

示例：

```
Guess a magic number between 0 and 100
Enter your guess: 50 ↵ Enter
Your guess is too high
Enter your guess: 25 ↵ Enter
Your guess is too low
Enter your guess: 42 ↵ Enter
Your guess is too high
Enter your guess: 39 ↵ Enter
Yes, the number is 39
```

例子：猜数

```
1 import random
4 number = random.randint(0, 100)
6 print("Guess a magic number between 0 and 100")
8 # Prompt the user to guess the number
9 guess = eval(input("Enter your guess: "))
```

```
while True:
```

```
    # Prompt the user to guess the number
    guess = eval(input("Enter your guess: "))
```

```
    if guess == number:
        print("Yes, the number is", number)
```

```
    elif guess > number:
        print("Your guess is too high")
```

```
    else:
        print("Your guess is too low")
```

例子：猜数

LISTING 5.3 GuessNumber.py

```
1  import random
4  number = random.randint(0, 100)
6  print("Guess a magic number between 0 and 100")
8  guess = -1
9  while guess != number:
10     # Prompt the user to guess the number
11     guess = eval(input("Enter your guess: "))
13     if guess == number:
14         print("Yes, the number is", number)
15     elif guess > number:
16         print("Your guess is too high")
17     else:
18         print("Your guess is too low")
```

例子： 多道减法题测试

Step 1: Generate two single-digit integers for **number1** and **number2**.

Step 2: If **number1** < **number2**, swap **number1** with **number2**.

Step 3: Prompt the student to answer, “What is $\text{number1} - \text{number2}$?”

Step 4: Check the student’s answer and display whether the answer is correct.

写一个程序：生成五道题，学生回答所有问题后，记录正确答案的个数。

例子：多道减法题测试

```
1  import random
2  import time
4  correctCount = 0 # Count the number of correct answers
5  count = 0 # Count the number of questions
6  NUMBER_OF_QUESTIONS = 5 # Constant
8  startTime = time.time() # Get start time
10 while count < NUMBER_OF_QUESTIONS:
11     # Generate two random single-digit integers
12     number1 = random.randint(0, 9)
13     number2 = random.randint(0, 9)
```

```
15     # If number1 < number2, swap number1 with
16     if number1 < number2:
17         number1, number2 = number2, number1
19     # Prompt the student to answer "What is number1 - number2"
20     answer = eval(input("What is " + str(number1) + " - " +
21                         str(number2) + "? "))
24     if number1 - number2 == answer:
25         print("You are correct!")
26         correctCount += 1
27     else:
28         print("Your answer is wrong.\n", number1, "-",
29               number2, "is", number1 - number2)
30
31     # Increase the count
32     count += 1
34 endTime = time.time() # Get end time
35 testTime = int(endTime - startTime) # Get test time
36 print("Correct count is", correctCount, "out of",
37       NUMBER_OF_QUESTIONS, "\nTest time is", testTime, "seconds")
```

What is $1 - 1$? 0

You are correct!

What is $7 - 2$? 5

You are correct!

What is $9 - 3$? 4

Your answer is wrong.

$9 - 3$ is 6

What is $6 - 6$? 0

You are correct!

What is $9 - 6$? 2

Your answer is wrong.

$9 - 6$ is 3

Correct count is 3 out of 5

Test time is 10 seconds

利用哨兵值控制循环

LISTING 5.5 SentinelValue.py

```
1 data = eval(input("Enter an integer (the input ends " +
2     "if it is 0): "))
3
4 # Keep reading data until the input is 0
5 sum = 0
6 while data != 0:
7     sum += data
8
9     data = eval(input("Enter an integer (the input ends " +
10         "if it is 0): "))
11
12 print("The sum is", sum)
```

步哨式控制循环

哨兵值: `data == 0`

```
Enter an integer (the input ends if it is 0): 4 ↵Enter
Enter an integer (the input ends if it is 0): 0 ↵Enter
```

利用哨兵值控制循环

注意

在循环控制条件中不要利用浮点值来比较相等，因为浮点值只是近似值，不精确，存在计算误差。

下面为一个计算 $1 + 0.9 + 0.8 + \dots + 0.1$ 的程序：

```
item = 1  
sum = 0
```

```
while item != 0:  
    sum += item  
    item -= 0.1
```

死循环

```
print(sum)
```

for 循环

通常, for 循环语句如下:

for **var** **in** sequence:

Loop body

statements



for i **in** range(initialValue, endValue):

Loop body

i = initialValue

while i < endValue:

Loop body

i += 1

Range 函数

函数 `range(a, b)` 返回一个**整数序列**：`a, a + 1, ..., b - 2, b - 1`. 默认 `a` 的值为 0.

`randrange(a, b)`
in random module

```
>>> for v in range(4, 8):  
...     print(v)  
...  
4  
5  
6  
7
```

`range(a, b, k)`,
其中 **k** 代表步长.

```
>>> for v in range(3, 9, 2):  
...     print(v)  
...  
3  
5  
7
```

```
for i in range(10):  
    if i % 2 == 0:  
        i = 1  
    print(i)
```

结果是什么？

1
1
1
3
1
5
1
7
1
9

while 循环和 for 循环之间的转换

```
sum = 0  
for i in range(1001):  
    sum = sum + i
```



```
sum = 0  
i = 0  
while i < 1001:  
    i = i + 1  
    sum = sum + i
```

嵌套循环

for iterating_var in sequence:

for iterating_var in sequence:
statements(s)

statements(s)

内循环
外循环

while expression:

while expression:

statements(s)

statements(s)

```
for i in range(5):  
    for j in range(i+1,5):  
        print(i,j)
```

0 1

0 2

0 3

0 4

1 2

1 3

1 4

2 3

2 4

3 4

注意: while 循环和 for 循环可以相互嵌套。

例子：乘法口诀表

Multiplication Table

1	2	3	4	5	6	7	8	9
---	---	---	---	---	---	---	---	---

一个 for
循环

1		1	2	3	4	5	6	7	8	9
2		2	4	6	8	10	12	14	16	18
3		3	6	9	12	15	18	21	24	27
4		4	8	12	16	20	24	28	32	36
5		5	10	15	20	25	30	35	40	45
6		6	12	18	24	30	36	42	48	54
7		7	14	21	28	35	42	49	56	63
8		8	16	24	32	40	48	56	64	72
9		9	18	27	36	45	54	63	72	81

嵌套循环

例子：乘法口诀表

```
1 print("          Multiplication Table")
2 # Display the number title
3 print(" |", end = '') ✕
4 for j in range(1, 10):
5     print(" ", j, end = '')
6 print() # Jump to the new line
7 print("-----")
8
9 # Display table body
10 for i in range(1, 10):
11     print(i, "|", end = '')
12     for j in range(1, 10):
13         # Display the product and align properly
14         print(format(i * j, "4d"), end = '')
15     print() # Jump to the new line
```

例子：乘法口诀表

```
print(' '*12,'Multiplication Table')
print(' '*4, end = '')
for i in range(1,10):
    print(format(i,'>4d'),end = '')
print()
print('-'*40)
for i in range(1,10):
    print(i,end = '|')
    for j in range(1,10):
        print(format(j * i,'>4d'), end = '')
    print()
```

嵌套循环

给出下面程序的结果

```
for i in range(1, 5):  
    j = 0  
    while j < i:  
        print(j, end = " ")  
        j += 1
```

```
i = 5  
while i >= 1:  
    num = 1  
    for j in range(1, i + 1):  
        print(num, end = "xxx")  
        num *= 2  
    print()  
    i -= 1
```

嵌套循环

Question: 用嵌套循环编写出如下表的程序

								1						
								1	2	1				
							1	2	4	2	1			
					1	2	4	8	4	2	1			
			1	2	4	8	16	8	4	2	1			
		1	2	4	8	16	32	16	8	4	2	1		
	1	2	4	8	16	32	64	32	16	8	4	2	1	
1	2	4	8	16	32	64	128	64	32	16	8	4	2	1

找规律：1，确定多少行；2，空格数，数值获取方法

								1						
							1	2	1					
					1	2	4	2	1					
			1	2	4	8	4	2	1					
		1	2	4	8	16	8	4	2	1				
	1	2	4	8	16	32	16	8	4	2	1			
1	2	4	8	16	32	64	128	64	32	16	8	4	2	1

```

for i in range(1,9):
    for j in range(9-1-i,0,-1): #get the spaces
        print(' '*4, end = '')
    for j in range(0,i):
        print(format(2**j,'>4d'),end = '') #the left side
    if i > 1:
        for j in range(i-1,0,-1):
            print(format(2**(j-1),'>4d'),end = '') #the right side
    print('\n') # a newline

```

							1							
						1	2	1						
				1	2	4	2	1						
			1	2	4	8	4	2	1					
		1	2	4	8	16	8	4	2	1				
	1	2	4	8	16	32	16	8	4	2	1			
1	2	4	8	16	32	64	128	64	32	16	8	4	2	1

```


for i in range(1, 9):
    print(' ' * (8-i), end = '')
    for j in range(0, i):
        print(format(2 ** j, '4d'), end = '')
    for j in range(1, i):
        print(format(2 ** (i-j-1), '4d'), end = '')
    print()

```

最小化数值误差

LISTING 5.7 TestSum.py

```
1  # Initialize sum
2  sum = 0
3
4  # Add 0.01, 0.02, ..., 0.99, 1 to sum
5  i = 0.01
6  while i <= 1.0:
7      sum += i
8      i = i + 0.01
9
10 # Display result
11 print("The sum is", sum)
```

 $i \approx 1.000000000x$

The sum is 49.5

最小化数值误差

```
sum = 0

# Add 0.01, 0.02, ..., 0.99, 1 to sum
i = 0.01
for count in range(100):
    sum += i
    i = i + 0.01

# Display result
print("The sum is", sum)
```

After this loop, **sum** is **50.5**.

例子：找出最大公约数

比如：16 和 24 的最大公约数是 8。

假设两个数分别为 **n1** 和 **n2**。

```
1  # Prompt the user to enter two integers
2  n1 = eval(input("Enter first integer: "))
3  n2 = eval(input("Enter second integer: "))
4
5  gcd = 1
6  k = 2
7  while k <= n1 and k <= n2:
8      if n1 % k == 0 and n2 % k == 0:
9          gcd = k
10         k += 1
11
12  print("The greatest common divisor for",
13        n1, "and", n2, "is", gcd)
```


$k \leq \min(n1, n2)$

例子：找出最大公约数

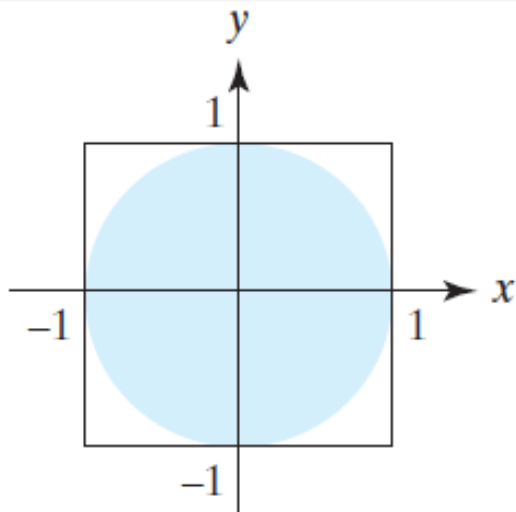
比如：16 和 24 的最大公约数是 8。

假设两个数分别为 **n1** 和 **n2**。

```
n1,n2 = eval(input('please enter two interges: '))
for i in range(1,max(n1 + 1,n2 + 1)):
    if n1 % i == 0 and n2 % i == 0:
        a = i
print('the Greatest Common Divisor is',a)
```



例子：利用蒙特卡洛方法计算pi



假设圆的半径为1，那么圆的面积为 π ，正方形的面积则为4，因为一个点随机撒在这个圆内的概率为：

$$\text{circleArea} / \text{squareArea} = \pi / 4.$$

因此我们可以通过该方程计算 π 。

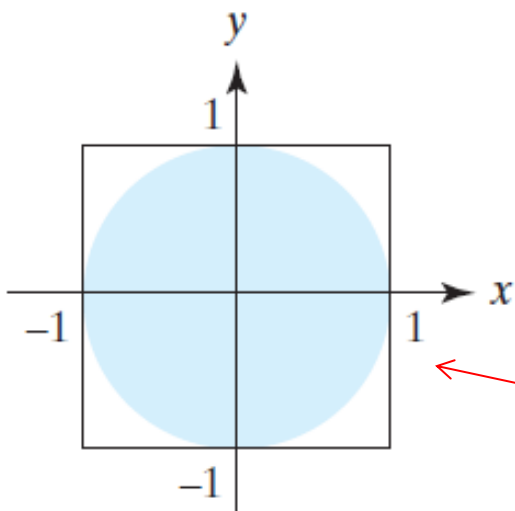
Step 1: 确定撒点次数

Step 2: 确定 x 和 y 的坐标

Step 3: 统计在圆内的点数

Step 4: 计算 $\pi = 4 * \text{圆内点数} / \text{总的撒点次数}$

例子：利用蒙特卡洛方法计算pi




```
1 import random
2
3 NUMBER_OF_TRIALS = 1000000 # Constant
4 numberOfHits = 0
5
6 for i in range(NUMBER_OF_TRIALS):
7     x = random.random() * 2 - 1
8     y = random.random() * 2 - 1
9
10    if x * x + y * y <= 1:
11        numberOfHits += 1
12
13 pi = 4 * numberOfHits / NUMBER_OF_TRIALS
14
15 print("PI is", pi)
```

break 和 continue

循环体中的关键字 **break** 帮助退出整个循环。

LISTING 5.11 TestBreak.py

```
1    sum = 0
2    number = 0
3
4    while number < 20:
5        number += 1
6        sum += number
7        if sum >= 100:
8            break
9
10   print("The number is", number)
11   print("The sum is", sum)
```



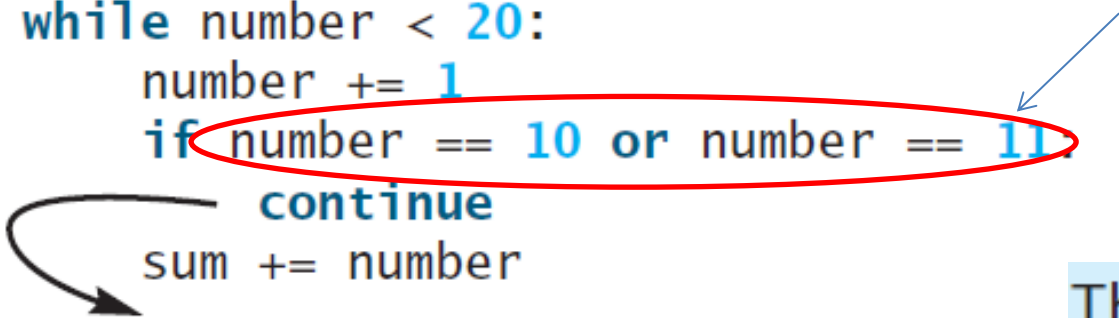
```
The number is 14
The sum is 105
```

break 和 continue

循环体中的关键字 **continue** 帮助退出或跳过当前的迭代。

LISTING 5.12 TestContinue.py

```
1  sum = 0
2  number = 0
3
4  while number < 20:
5      number += 1
6      if number == 10 or number == 11:
7          continue
8      sum += number
9
10 print("The sum is", sum)
```



10 和 11 并没加进来.

The sum is 189

break 和 continue

给出下面程序的结果

```
balance = 1000
while True:
    if balance < 9:
        break
    balance = balance - 9
print("Balance is", balance)
```

Balance is 1

```
balance = 1000
while True:
    if balance < 9:
        continue
    balance = balance - 9
print("Balance is", balance)
```

死循环

break 和 continue

给出下面程序的结果

```
for i in range(1, 4):  
    for j in range(1, 4):  
        if i * j > 2:  
            break  
  
        print(i * j)  
  
    print(i)
```

```
for i in range(1, 4):  
    for j in range(1, 4):  
        if i * j > 2:  
            continue  
  
        print(i * j)  
  
    print(i)
```


例子：显示下面表中的素数

素数：大于 2，且只能被自己和 1 整除的数。如 2, 3, 5, 7 都为素数，但 4, 6, 8, 和 9 都不是。

Question: 写一个程序，给出前 50 个素数，每行包含 10 个素数。

The first 50 prime numbers are

2	3	5	7	11	13	17	19	23	29
31	37	41	43	47	53	59	61	67	71
73	79	83	89	97	101	103	107	109	113
127	131	137	139	149	151	157	163	167	173
179	181	191	193	197	199	211	223	227	229

例子：显示下面表中的素数

这个问题可以被分成以下几个任务。

- 决定一个特定的数是否为素数。
- 对于 $\text{number}=2, 3, 4, 5, 6, \dots$ ，测试这个数字是否为素数。
- 统计所有素数的个数。
- 显示每个素数，每行显示 10 个。

(1) `NUMBER_OF_PRIMES = 50`

(2) 利用变量 `count` 追踪素数的个数，初始时 `count = 0`

(3) 因为素数是从大于1的整数开始，我们初始时设为 **2**

例子：显示下面表中的素数

```
while count < NUMBER_OF_PRIMES:
```

```
    Test if number is prime
```

```
    if number is prime:
```

```
        Display the prime number and increase count
```

```
    Increment number by 1
```

Use a Boolean variable `isPrime` to denote whether the number is prime; Set `isPrime` to `True` initially

```
for divisor in range(2, number / 2 + 1):
```

```
    if number % divisor == 0:
```

```
        Set isPrime to False
```

```
        Exit the loop
```

例子：显示下面表中的素数

```
1  NUMBER_OF_PRIMES = 50 # Number of primes to display
2  NUMBER_OF_PRIMES_PER_LINE = 10 # Display 10 per line
3  count = 0 # Count the number of prime numbers
4  number = 2 # A number to be tested for primeness
6  print("The first 50 prime numbers are")
9  while count < NUMBER_OF_PRIMES:
10     # Assume the number is prime
11     isPrime = True # Is the current number prime?
14     divisor = 2
15     while divisor <= number / 2:
16         if number % divisor == 0:
17             # If true, the number is not prime
18             isPrime = False # Set isPrime to false
19             break # Exit the for loop
20     divisor += 1
```

例子：显示下面表中的素数

```
22     # Display the prime number and increase the cou
23     if isPrime:
24         count += 1 # Increase the count
25
26         print(format(number, "5d"), end = '')
27         if count % NUMBER_OF_PRIMES_PER_LINE == 0:
28             # Display the number and advance to the
29             print() # Jump to the new line
30
31     # Check if the next number is prime
32     number += 1
```

例子：显示下面表中的素数

```
count,lines,numberOfPrime = 0,10,50
number = 2
print('The first prime are')
print()
while count < numberOfPrime:
    for i in range(2,(number//2+1)):
        if number % i == 0:
            break
        else:
            count += 1
            print(format(number,'>5d'),end = '')
            if count % lines == 0:
                print()
    number += 1
```

这是可以的

Exercises

- P129 5.1
- P130 5.7
- P130 5.9, 5.13, 5.18
- P133 5.26