

Math 221  
Class Exercise: Mar. 28

$$\text{Let } U = \text{Span} \left\{ \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \right\} \text{ and } W = \text{Span} \left\{ \begin{bmatrix} 2 \\ 1 \\ 1 \end{bmatrix}, \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} \right\}$$

Find a matrix  $P$  so that  $Px$  is the projection of  $x$  onto  $U$  along  $W$ .

1. Check that  $P^2 = P$ .
2. Check that  $Px$  is in  $U$  for any  $x \in \mathbb{R}^3$ .
3. Check that  $Pw = 0$  for any  $w \in W$ .