Math 221 Class Exercises: Mar. 16

1. Let x be a vector in \mathbb{R}^3 . Show that set of vectors orthogonal to x is a subspace of \mathbb{R}^3 .

2. Consider the vector space \mathbb{P}_2 with inner product $\langle p(x), q(x) \rangle = \int_{-1}^1 p(x)q(x) dx$. Carry out the orthogonalization process to produce an orthonormal basis from the basis $\alpha = \{1, x, x^2\}$.