

# Math 111

## Exponential functions

(DEFINITION) A function  $f$  is **exponential** if it can be written as:

(EXAMPLE)

$$f(x) = 2^x$$

(NOTES) about  $f(x) = a^x$

(DEFINITION) The **natural exponential function** has base:

## Logarithmic functions

(DEFINITION) The **logarithmic function** of base  $a$  is the *inverse* of the exponential function with base  $a$ .

(EXAMPLES)

1.  $f(x) = \log_2 x$

2.  $f(x) = \ln x$       (**natural logarithmic function**)

3.  $g(x) = \ln(2x - 1)$

(APPLICATIONS)

Suppose that  $S(t) = 100e^{0.1t}$  represents the population of a growing colony of bacteria, with  $t$  measured in hours.

1. At what time is  $S$  twice its starting value?
2. At what time is  $S$  four times its starting value?

## Trigonometric functions

(DEFINITIONS)

Two basic **trigonometric functions**,  $\sin x$  and  $\cos x$ , are defined by:

(NOTES)

(OTHER EXAMPLES)