

18/11/2022

# POWER ELECTRONICS

## AND DRIVES

### INTRODUCTION.

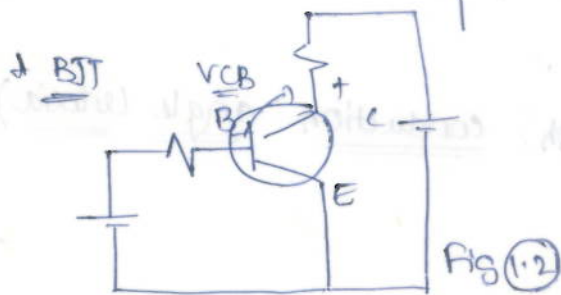
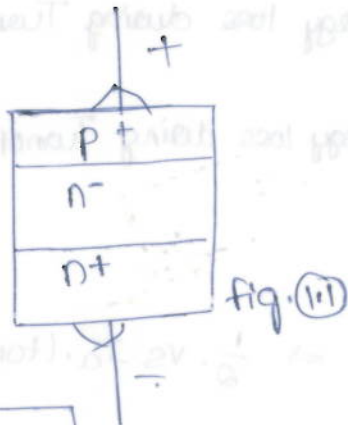
(P.S.BIMBRA)

( )

(N.P.T.E.L)

\* RCT and Traic only do reverse conducting,

\* Power diode :-



over drive the Base current.

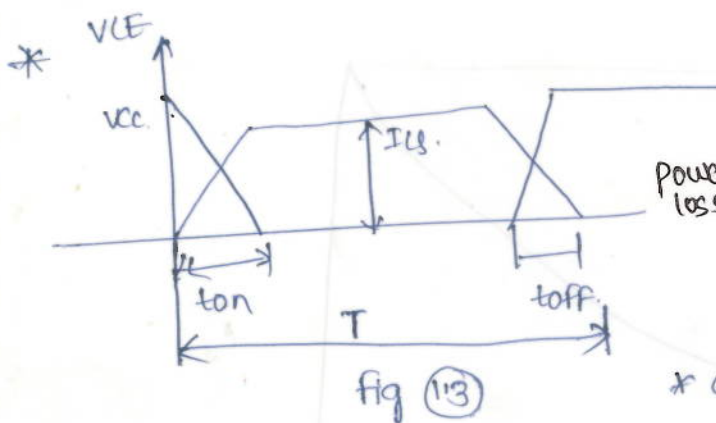
$$I_C = \frac{V_{CC} - V_{CE}}{R_C}$$

$$\beta = I_C / I_B$$

$$I_{C(sat)} = \frac{V_{CC} - V_{CE(s)}}{R_C}$$

$$I_B(sat) = I_{C(sat)} / \beta$$

$$\text{over drive factor} = \frac{I_B}{I_{B(sat)}}$$



\* Switch on energy loss  $\Rightarrow \frac{V_{CC} \times I_{Cs}}{6} \times t_{on}$

Power loss = average value of switch on loss  $\Rightarrow \left( \frac{V_{CC} \times I_{Cs}}{6} \times t_{on} \right) \times f$

\* Switch off energy loss  $\Rightarrow \left( \frac{V_{CC} \times I_{Cs}}{6} \times t_{off} \right) \times f$

\* average value of switch off loss  $\Rightarrow \frac{V_{CC} \times I_{Cs}}{6} \times t_{off} \times f$

\* Peak value of instantaneous power loss  $\Rightarrow$

during switch on  $\Rightarrow \frac{V_{CC} \times I_{Cs}}{4}$

during switch off  $\Rightarrow \frac{V_{CC} \times I_{Cs}}{4}$

Both are same

18/11/2021

ELECTRONICS

AND  
DRIVES

INTRODUCTION.

(P.2.BINBA)

( )

power diode etc

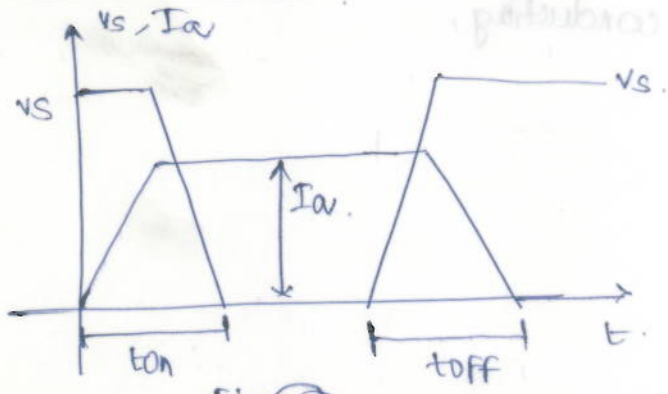


fig (14)

\* Energy loss during Turnon  $\Rightarrow \frac{1}{2} \cdot V_s \cdot I_a \cdot (t_{on})$

\* Energy loss during Turnoff  $\Rightarrow \frac{1}{2} \cdot V_s \cdot I_a \cdot (t_{off})$

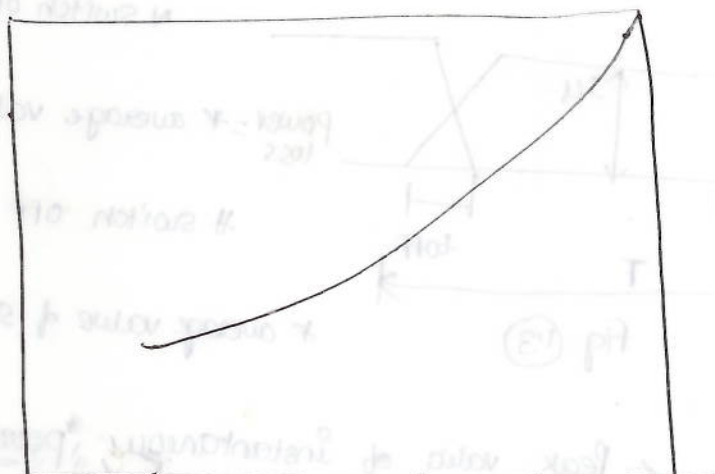
\* Average Energy loss  $\Rightarrow \frac{1}{2} \cdot V_s \cdot I_a \cdot (t_{on} + t_{off}) \cdot f$

form - factor and onstate current (through conduction angle criteria)

(next page

Fig 3.3 onwards.

$I(T_{avg})$



30° 60° 90° 120° 150°

concl. angle

## Diode - rectifiers

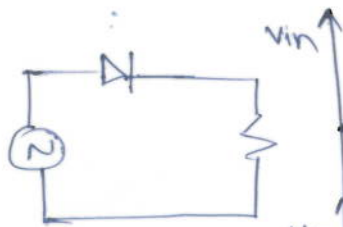


fig 2.1

$$V_D = \frac{V_m}{\pi}$$

$$V_{or} = \frac{V_m}{2}$$

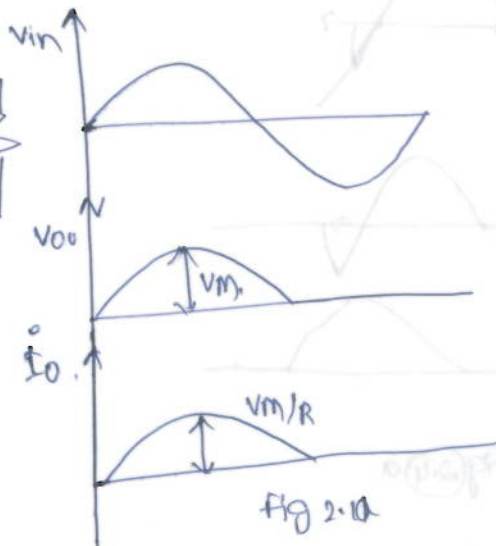


fig 2.1a

$$V_{or} = \left[ \frac{1}{2\pi} \int_0^\pi V_m \sin^2 \omega t \, d\omega t \right]$$

$$V_m \left[ \frac{1}{2\pi} \int_0^\pi \sin^2 \omega t \, d\omega t \right] = \frac{V_m}{2}$$

PF  $\Rightarrow$   $\neq$  unity (if TIF coupled)  
else unity.

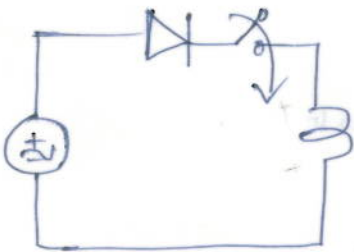


fig 2.2

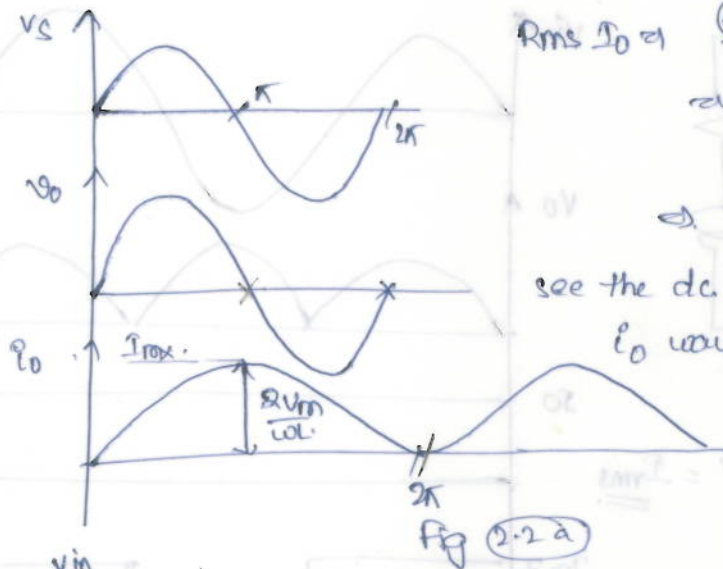


fig 2.2a

Rms  $I_o = \sqrt{\frac{1}{2\pi} \int_0^\pi I_o^2 \sin^2 \omega t \, d\omega t}$

$$= \sqrt{\frac{I_o^2}{2}}$$

$$\Rightarrow \sqrt{2} I_o = 1.225 I_o$$

see the dc component in  $i_o$  waveform equation,

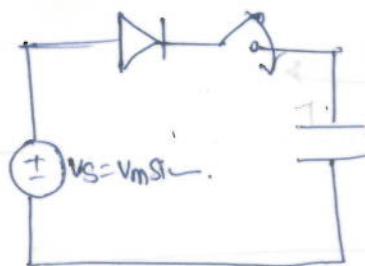


fig 2.3

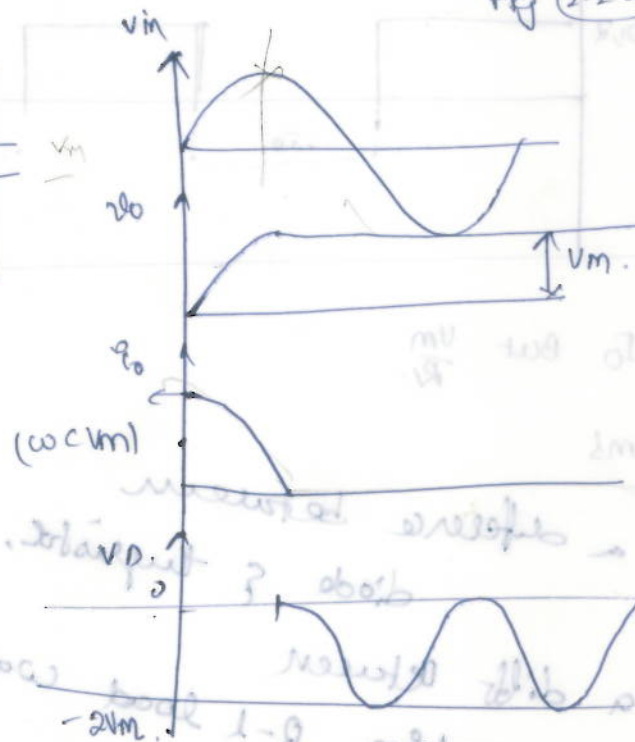
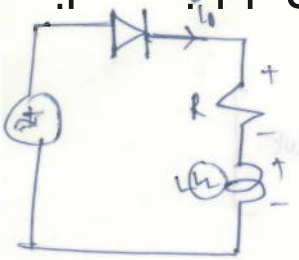


fig 2.3a

$$V_D = V_m (1 - \cos \omega t)$$

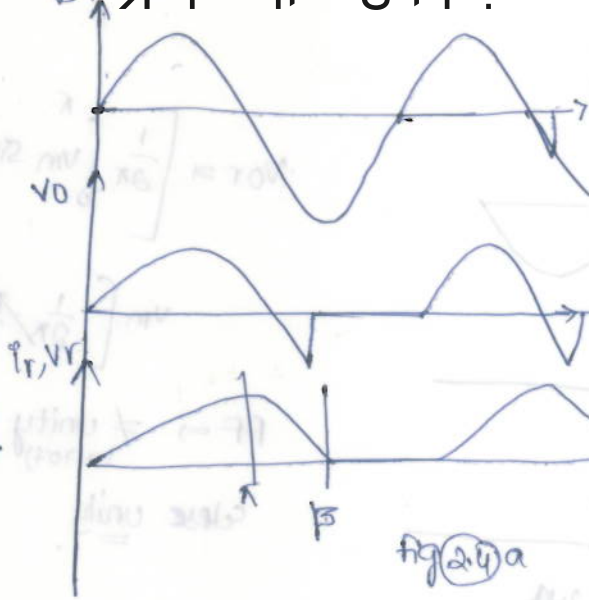
$$= 1.225 V_m$$





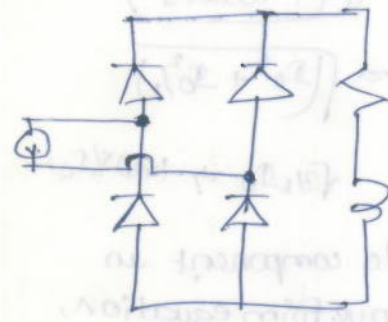
fig(2.4)

$$V_0 \Rightarrow \frac{V_m}{2\pi} [1 - \cos\beta]$$



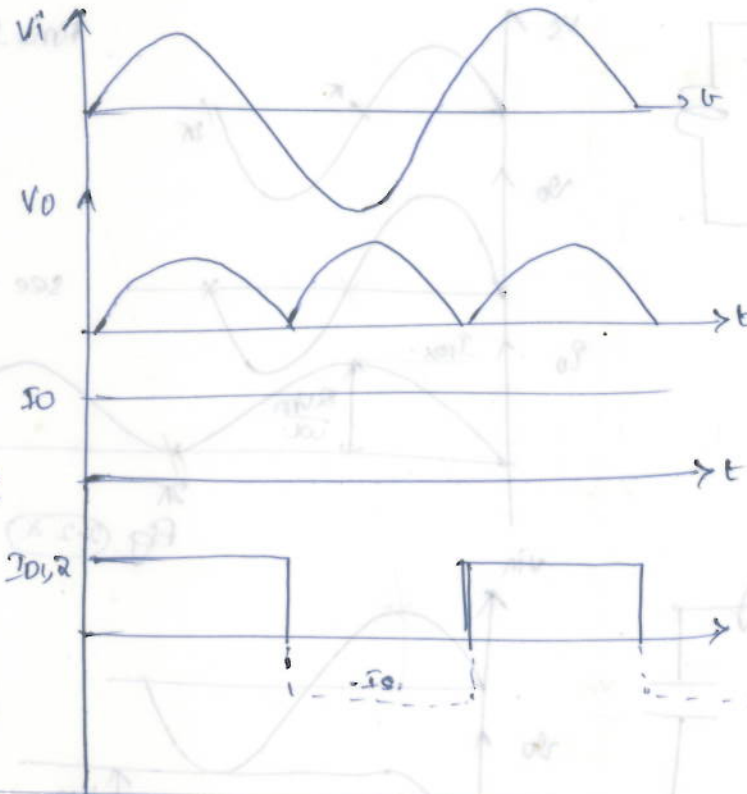
fig(2.4a)

Full bridge - diode -  $I_0$  const. - (RL).



$$\text{Avg. } I_0 \approx \frac{V_0}{R} \approx \frac{2V_m}{\pi R} = I_{rms}$$

$$I_{max} \approx I_0$$



but for R-load

$$I_{max} \neq I_0 \text{ But } \frac{V_m}{R}$$

$$I_0 \neq I_{rms}$$

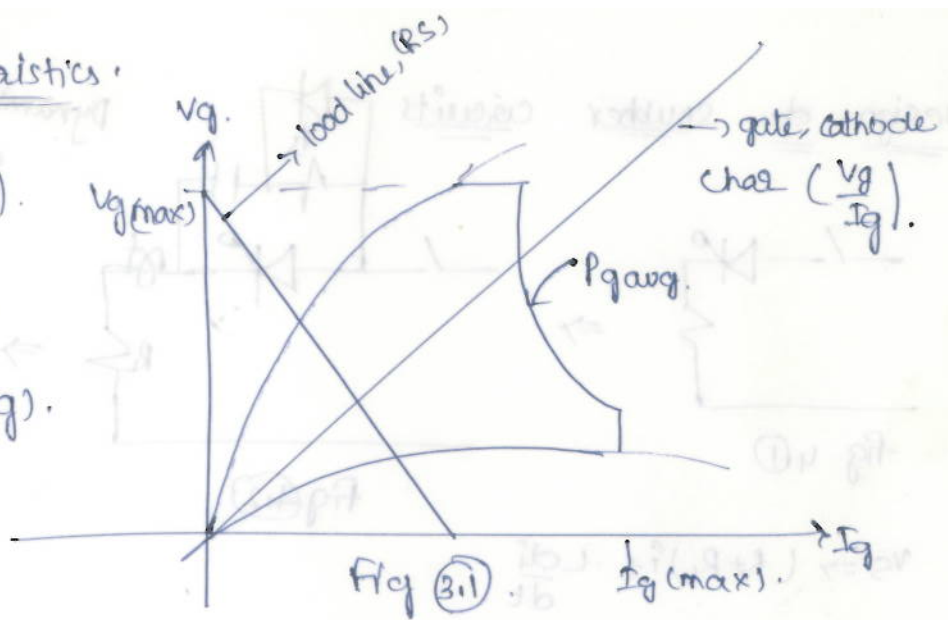
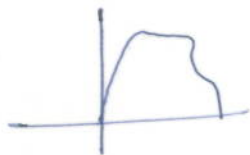
always there is a difference between diode & thyristor,  
and there is a diff between R-load waveform, R-L load waveform in uncontrolled & controlled.

# Thyristor gate characteristics.

$$\frac{1}{T} \int_0^T P_{g(max)} = P_g (avg)$$

$$\frac{T_1}{T} (P_{g(max)}) = P_g (avg)$$

$$\rightarrow dP_{g(max)} = P_g (avg)$$

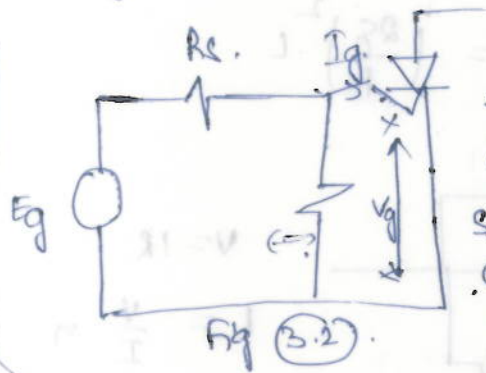


\* gate cathode characteristics means  $\frac{V_g}{I_g}$ ; (usually given trcl.)

Load line slope  $\Rightarrow R_s \Rightarrow$  (usually given -ve)

## \* SCR - derating phenomenon (HUF-wave only)

Every manufacturer specifies the maximum (RMS) current handled by SCR. (fixed value)



\* parallel R across gate-cath,  $\Rightarrow$  for suppression of leakage currents and thermal stability.

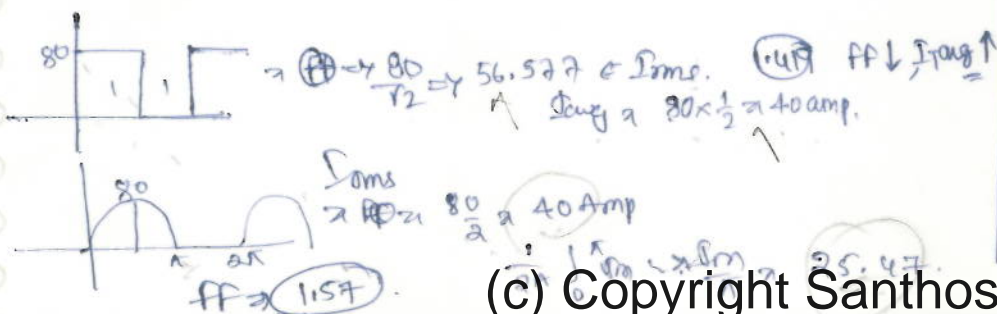
Rms Because, (current) heat produced depends on rms, But not  $I_{avg}$

$$\text{so, } F.F. = \frac{I_{rms}}{I_{avg}}$$

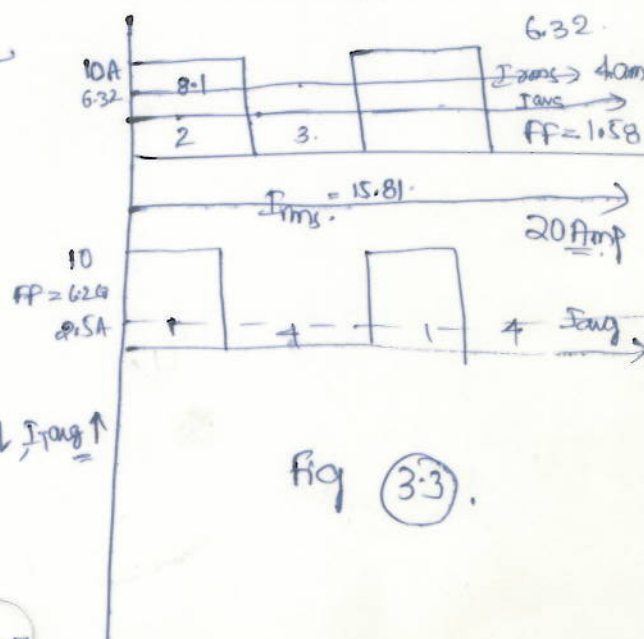
$$\text{form factor} = \frac{\left[ \frac{1}{2\pi} \int_0^{2\pi} I_m^2 \sin^2 \theta \right]^{1/2}}{\frac{I_m}{2\pi} [1 + \cos \theta]}$$

\* do prefer max conduction angle.

\* prefer sine wave, not sq. wave.



## visualization



# Design of snubber circuits

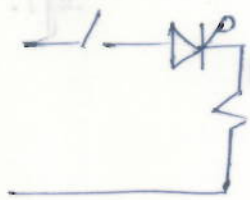


fig 4.1

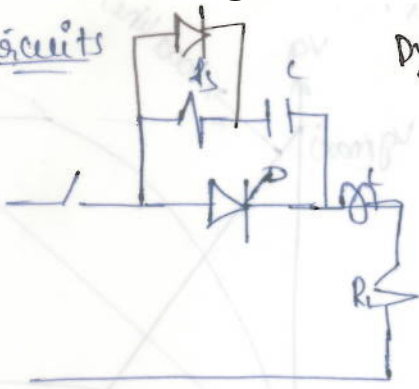


fig 4.2

Dynamic equalizing circuit

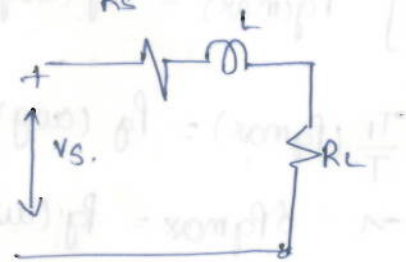


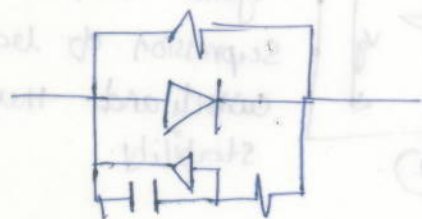
Fig. 4.3

$$V_s \Rightarrow (R_s + R_L) i + L \frac{di}{dt}$$

$$\textcircled{1} L = \frac{V_s}{(di/dt)} \Rightarrow 4.8 \text{ mH}$$

② next decide (R) Based on current carrying capacity of

$$\textcircled{3} C = \left( \frac{2V_s}{R} \right)^2 \cdot L$$



$$V = IR$$

$$R = \frac{V}{I} \approx \frac{NV_{bm} - V_s}{(n-1) \Delta I_b}$$

$$Q = CV \Rightarrow C = \frac{Q}{V} \approx \frac{\Delta Q (n-1)}{NV_{bm} - V_s}$$

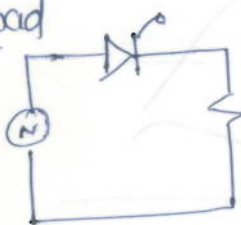


Fig 3.3



# phase controlled rectifiers (Half wave).

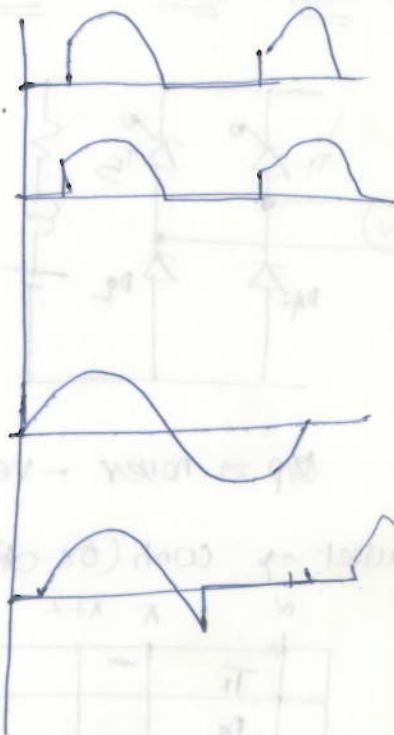
R-load



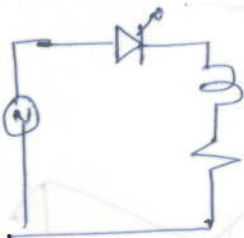
$$V_O \rightarrow \frac{1}{2\pi} \int_0^\pi V_m \sin \omega t \, d\omega \Rightarrow \frac{V_m}{2\pi} [1 + \cos \alpha]$$

$$V_{OR} \propto \left[ \frac{V_m^2}{2\pi} [(\pi - \alpha) + \frac{1}{2} \sin 2\alpha] \right]^{1/2}$$

$$PF \propto \frac{V_{OR}}{V_S}$$



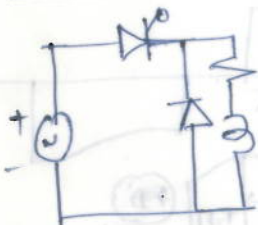
R-L load



$$V_O = \frac{V_m}{2\pi} [\cos \alpha - \cos \beta]$$

$$V_{OR} = \left[ \frac{V_m^2}{2\pi} (\beta - \alpha) + \frac{1}{2} (\sin 2\alpha - \sin 2\beta) \right]^{1/2}$$

R-L - F-Diode

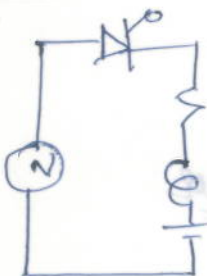


$\Rightarrow$  o/p looks like  $\textcircled{R}$  load,

$\Rightarrow$  current can be continuous / di's continuous,

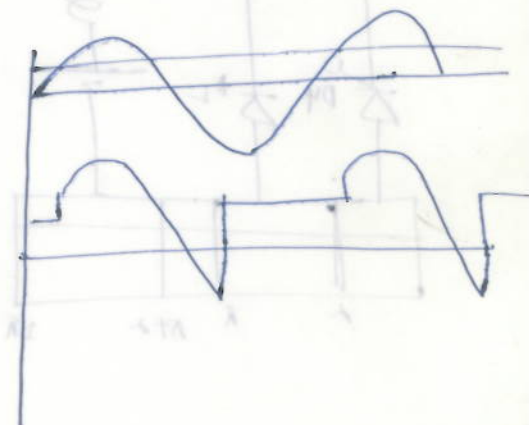
$\Rightarrow$  p.f. unimproved.

R-L - E load

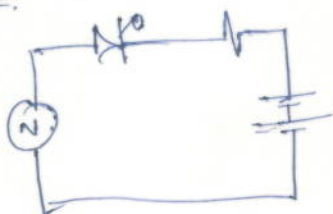


$\Rightarrow$  P.V  $\Rightarrow (E + V_m)$

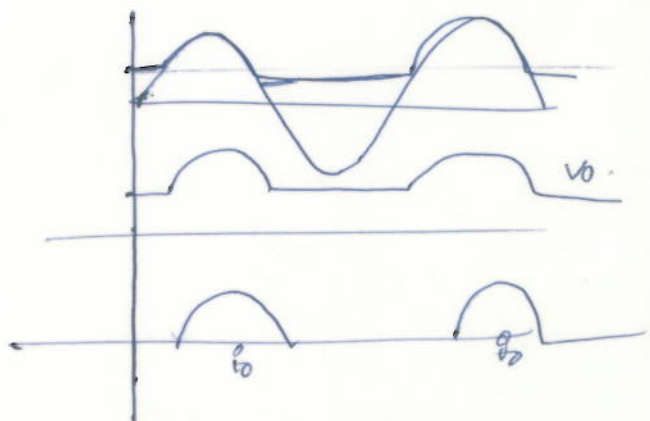
$$I_O \propto \frac{1}{2\pi} [V_m (\cos \alpha - \cos \beta) - E (\beta - \alpha)]$$



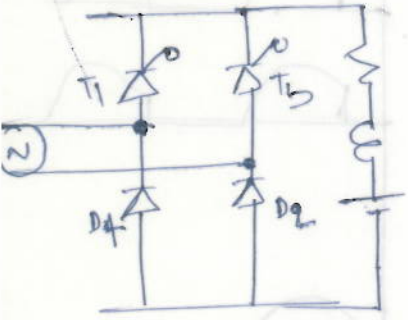
R-E load



$$i_O \propto \frac{V_m \sin \omega t - E}{R}$$

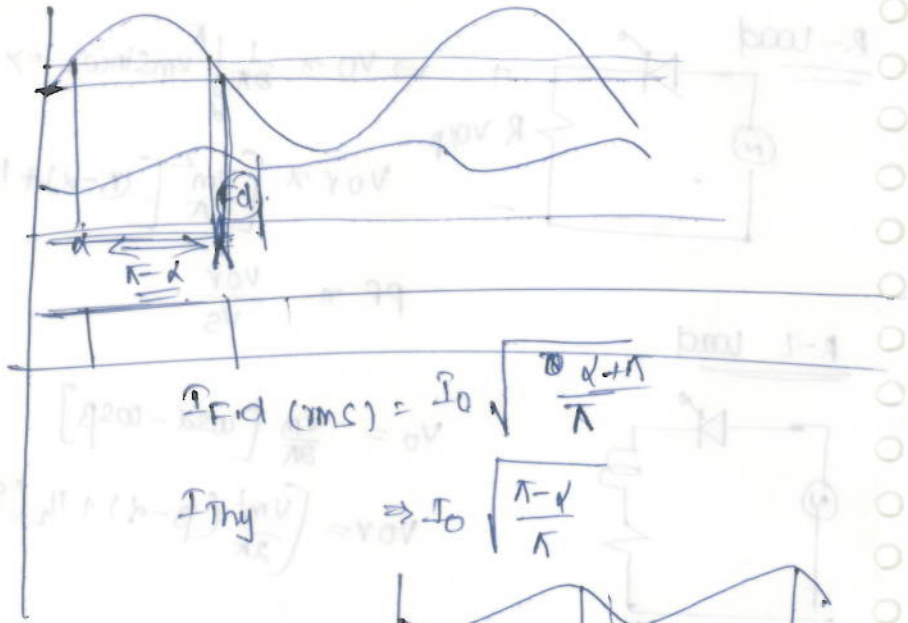
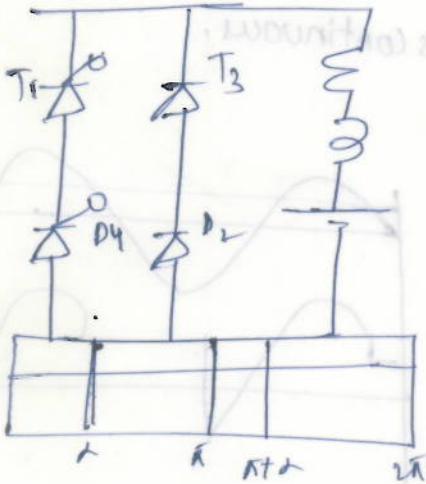
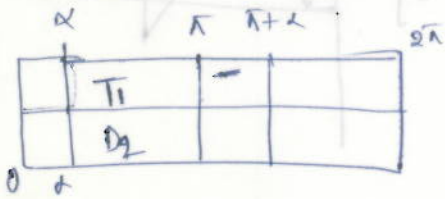


full wave rectifiers  $\Rightarrow$  Half controlled



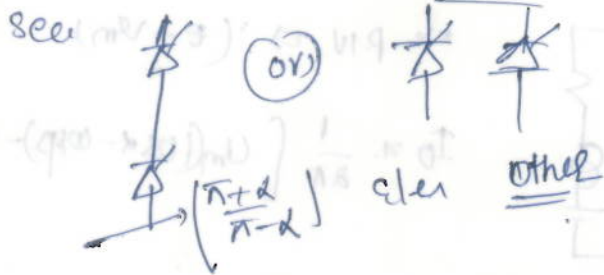
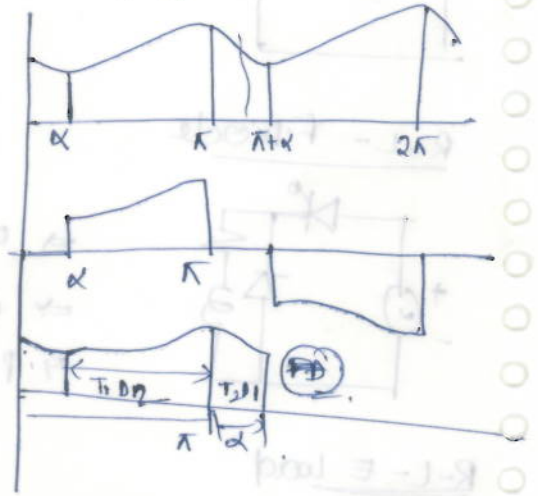
o/p  $\neq$  never -ve,

u/sset  $\Rightarrow$  conti (or) dis - cont



$$I_{Fid} (rms) = I_0 \sqrt{\frac{\pi - \alpha}{\pi}}$$

$$I_{Thy} \Rightarrow I_0 \sqrt{\frac{\pi - \alpha}{\pi}}$$



$$I_{Fid} (rms) = I_0 \sqrt{\frac{\pi - \alpha}{\pi}}$$





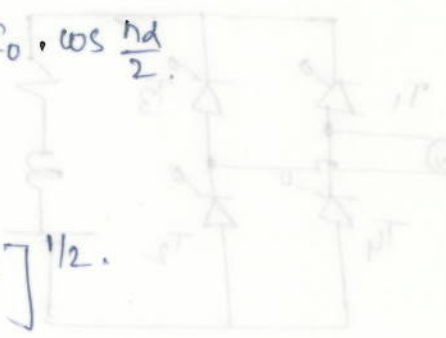
1d semi

11/11/19

Rms value of  $n$ th harmonic current,  $\frac{2\sqrt{2}}{n\pi} I_0 \cos \frac{n\alpha}{2}$

Rms fundamental  $\Rightarrow \frac{2\sqrt{2} I_0}{\pi} \cos \alpha/2$

Rms value of total input current,  $I_0 \left[ \frac{\pi - \alpha}{\pi} \right]^{1/2}$



displacement factor  $\Rightarrow \cos \alpha/2$

power factor  $\Rightarrow (1 + \cos \alpha) \cdot \sqrt{\frac{2}{\pi(\pi - \alpha)}}$

power input  $\Rightarrow V_0 I_0$

Reactive Power  $\Rightarrow V_0 I_0 \tan \alpha/2$



$$\frac{2\sqrt{2}}{\pi} I_0 \cos \alpha/2$$

$$\frac{2\sqrt{2}}{n\pi} I_0 \cos(n\alpha/2)$$

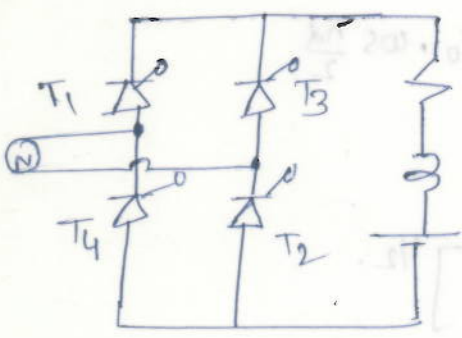
PF

$$(1 + \cos \alpha) \cdot \sqrt{\frac{2}{\pi(\pi - \alpha)}}$$

$$V_0 I_0, \quad R \approx V_0 I_0 \tan \alpha/2$$

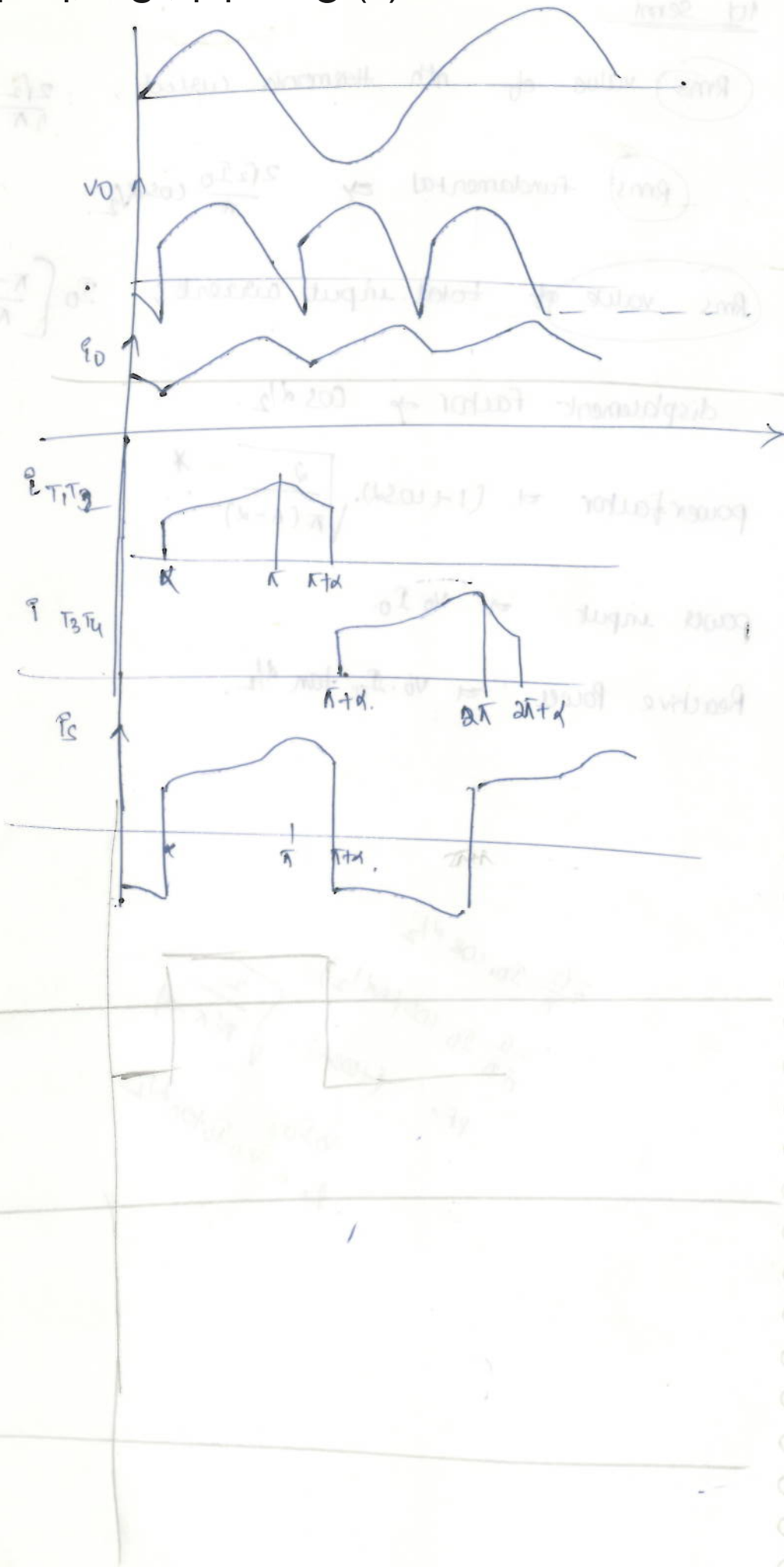
$$I_0 \sqrt{\frac{\pi - \alpha}{\pi}}$$

full controlled



$$\frac{2V_m}{\pi} \cos \alpha$$

$$V_{or} = V_s$$



# 1 $\phi$ full - fourier analysis

(rms) value of  $n$ th harmonic  $\Rightarrow \frac{2\sqrt{2}}{n\pi} I_0$

(rms) value of fund. comp  $\Rightarrow \frac{2\sqrt{2}}{\pi} I_0 \Rightarrow 0.90032 I_0$

(rms) value of total ip current  $\Rightarrow \left[ \frac{2\sqrt{2} \times \pi}{\pi} \right] \Rightarrow I_0$

displacement factor  $\Rightarrow \cos \alpha$

power factor  $\Rightarrow \cos \alpha \cdot \frac{\sqrt{2} \cdot 2}{\pi}$

Active Power input  $\Rightarrow V_0 \cdot I_0$

Reactive Power input  $\Rightarrow V_0 \cdot I_0 \cdot \tan \alpha$

$\frac{2\sqrt{2}}{n\pi} I_0$

$\frac{2\sqrt{2}}{\pi} I_0$

$I_0 = I_{rms}$

$\cos \alpha$

$\frac{2\sqrt{2}}{\pi} \cos \alpha$

$V_0 I_0$

$V_0 I_0 \tan \alpha$



fig 1

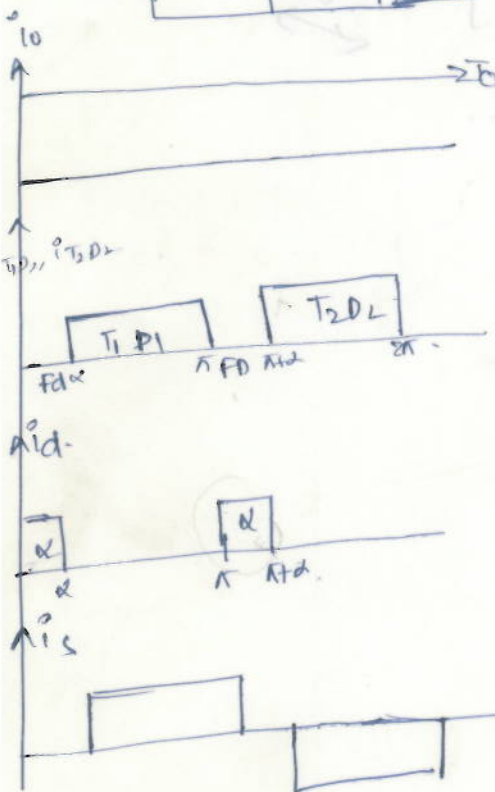
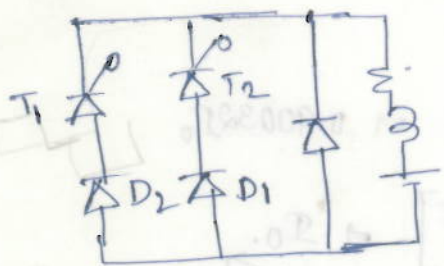


fig 2

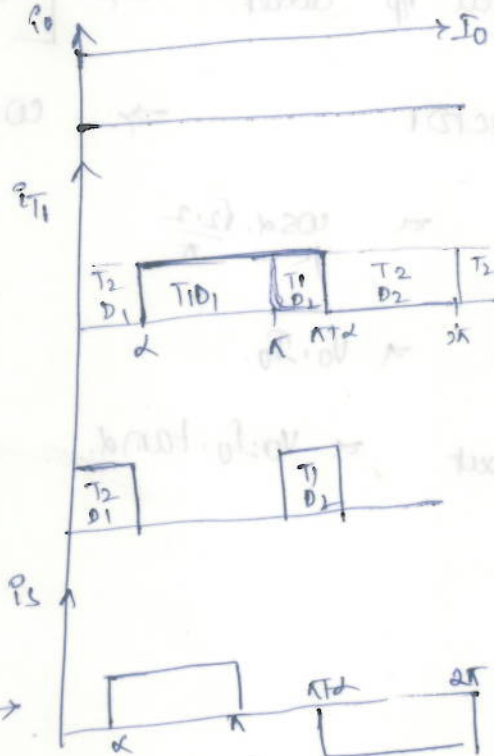
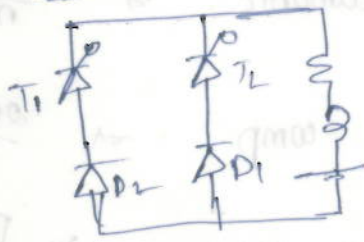
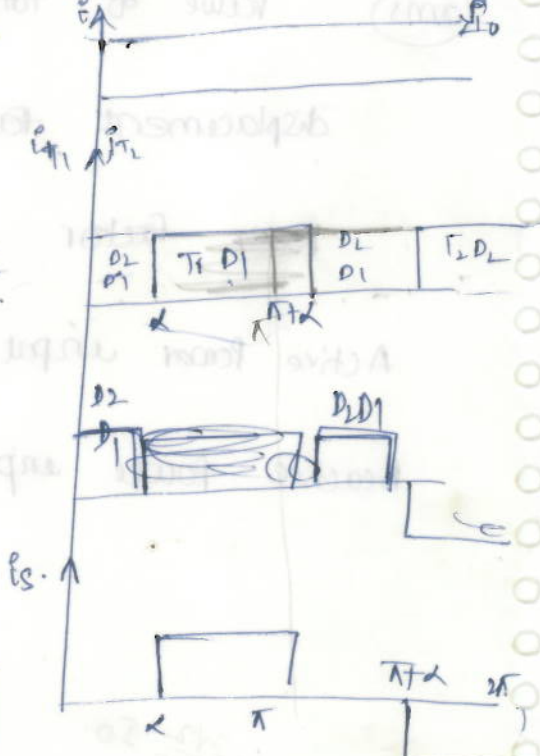
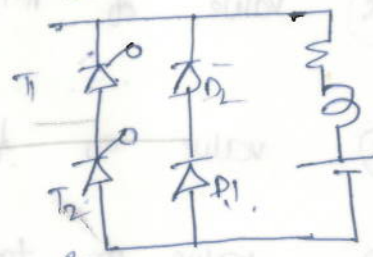


fig 3



### 3d - Rectifier circuits

(quantitative Analysis only)

3d - Half wave controlled,  $\frac{3\sqrt{6}V_{ph}}{2\pi} \cos \alpha$

Avg. curre. rating of SCR  $\approx I_o/3$ .

rms. curre. rating of SCR  $\approx I_o/\sqrt{3}$ .

### 3d - Full converters:-

rms value of source current,  $I_o \cdot \sqrt{2/3}$ . ( $120^\circ$  &  $180^\circ$ ).

rms value of thyrist. curre.,  $I_o \cdot \sqrt{1/3}$  ( $120^\circ$  &  $360^\circ$ ).

### Analysis:-

Q

RMS Value of  $n$ th har. curre.  $\sim \frac{2I_o}{n\pi} \cdot \sin\left(\frac{n\pi}{3}\right)$

RMS value of fund. com. of  $i$   $\approx \frac{\sqrt{6}}{\pi} I_o$ .

RMS. value of source current  $\approx I_o \cdot \sqrt{2/3}$

Distortion factor  $\Rightarrow \cos \alpha$ .

power factor  $\approx 3/\pi \cos \alpha$ .

Active Power input  $\approx V_o \cdot I_o$ .

Reactive Power input  $\approx V_o I_o \tan \alpha$ .

Source  
 $I_o \sqrt{2/3}$ ,  $I_o \sqrt{1/3}$

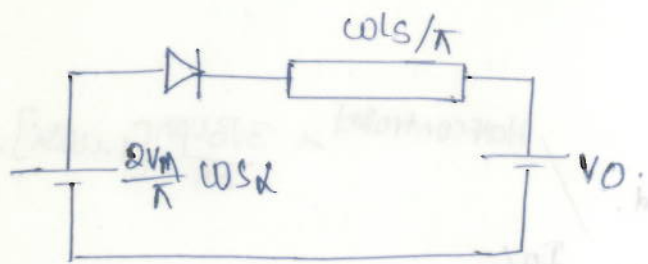
$\sqrt{\frac{180-\alpha}{180}}$ ;  $\sqrt{\frac{180-\alpha}{360}}$

$226^\circ$

$276^\circ$

$\sqrt{\frac{\pi-\alpha}{\pi}} \times I_{\text{source}}$

$\sqrt{\frac{\pi-\alpha}{2\pi}}$



$$I_0 = \frac{V_m}{\omega L_s} [\cos \alpha - \cos(\alpha + \pi)]$$

$$V_{or} = \frac{V_m}{\pi} [\cos \alpha + \cos(\alpha + \pi)]$$

$$\cos(\alpha + \pi) = \left( -\frac{I_0 \cdot \omega L_s}{V_m} \right) + \cos(\alpha)$$

$$\text{Inductive voltage regulation} = \left[ 1 - \frac{\cos \alpha}{2} \right]$$

3 $\phi$  full converter.

$$V_0 = \frac{3 \cdot V_{mL}}{\pi} \cos \alpha \quad \text{for } 0 < \alpha < \pi/3.$$

$$= \frac{3 V_{mL}}{\pi} [1 + \cos(\alpha + \pi)] \quad \text{for } \pi/3 < \alpha < \frac{2\pi}{3};$$

3 $\phi$  semi-converter.

$$V_0 = \frac{3 V_{mL}}{2\pi} [1 + \cos \alpha].$$

3 $\phi$  mid point:-

$$V_0 = \frac{3 V_m}{2\pi} \cos \alpha:$$



# Dual converters

without circulating inductor  $\Rightarrow$  only 1 at a time in operation, another ideal,

with circulating inductor  $\Rightarrow$  Both are simultaneously operated,  $(\alpha_1 + \alpha_2 = 180^\circ)$

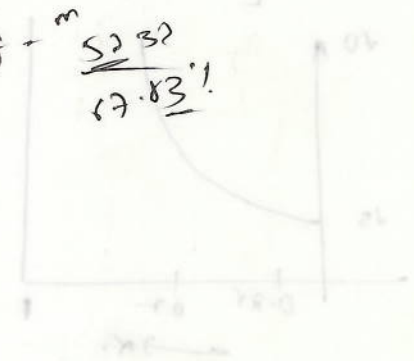
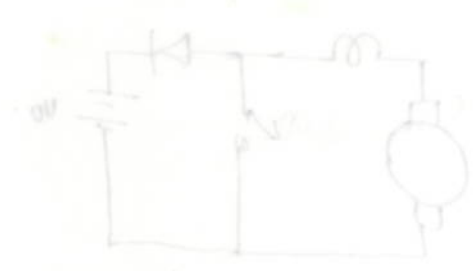
1st phase

$$\frac{V_m}{\omega L} [1 - \sin \alpha_1]$$

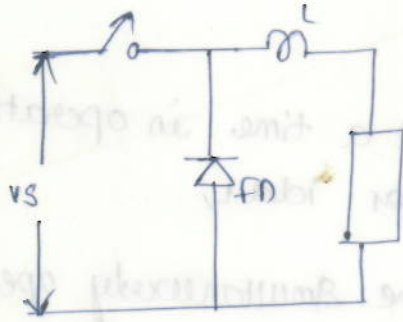
$$\frac{\sqrt{2} V_m}{\omega L} [1 - \sin \alpha_1]$$

peak  $\Rightarrow \frac{V_m}{\omega L}$

Peak  $\frac{\sqrt{2} V_m}{\omega L}$



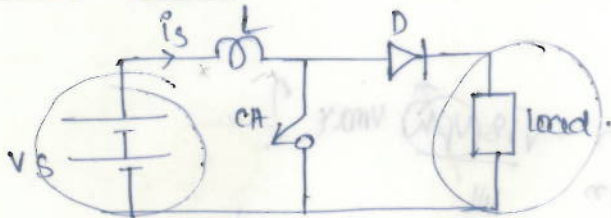
## BASIC



$$V_O = \alpha V_S$$

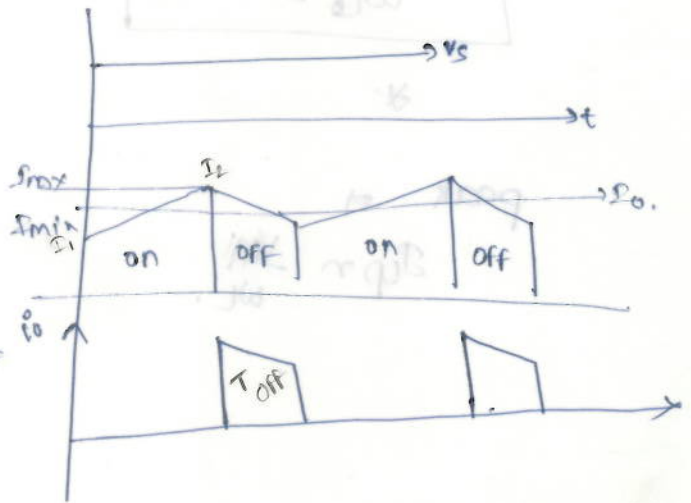
\* P.W.M technique fail if  $T_{ON} \approx 0$  (commutation badly fail).

## step-up chopper

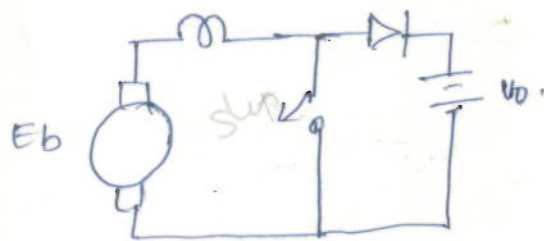


$$V_S \left( \frac{I_L + I_L}{2} \right) T_{ON} = (V_O - V_S) \left( \frac{I_L + I_L}{2} \right) T_{OFF}$$

$$[V_O = V_S / (1 - \alpha)]$$



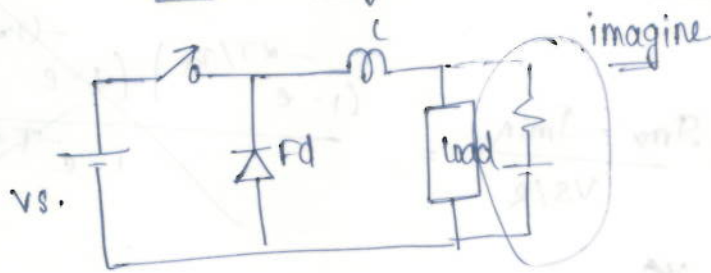
## Regenerative Braking using step-up



$$do \cdot \left( \frac{E_b}{1 - \alpha} > V_O \right)$$

Type (d)  $V_O = V_S \left( \frac{T_{ON} - T_{OFF}}{T_{ON} + T_{OFF}} \right)$

## Stepdown chopper Analysis



\* average o/p voltage =  $\alpha V_s$

\* average "output current" =  $\frac{\alpha V_s}{R}$

\* R.M.S. value of o/p voltage =  $\frac{\sqrt{\alpha} \cdot V_s}{R}$

\* R.M.S. value of o/p current =  $\frac{\sqrt{\alpha} \cdot V_s}{R}$

\* R.M.S. thyristor current =  $\frac{\sqrt{\alpha} (V_s - E)}{R}$

\* average thyristor current =  $\frac{\alpha (V_s - E)}{R}$

\* Eff. Resistance Ref =  $\frac{R}{\alpha}$

## \* Critical Inductance

$$V = L \frac{di}{dt}$$

$$L = \frac{V \times t}{I}$$

$$\frac{(V_s - V_o) \cdot T_{on}}{2 I_o}$$

(or)

$$\frac{(V_s - V_o) \cdot V_o^2}{2 f \cdot V_s \cdot P_o}$$

$$\alpha V_s$$

$$\alpha V_s / R$$

$$\frac{\sqrt{\alpha} V_s}{\frac{\alpha V_s}{R}}$$

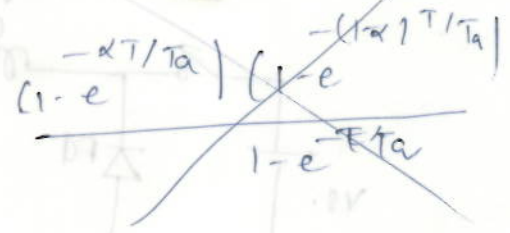
$$\frac{\sqrt{\alpha} (V_s - E)}{R}$$

$$\frac{\alpha (V_s - E)}{R}$$

$\frac{R}{2}$  eff. step down =

$$(1 - \alpha) V_s \sqrt{(1 - \alpha) I_o}$$



Analysis of Type-A chopper

\* per unit ripple  $\rightarrow \frac{I_{mx} - I_{min}}{V_s/R} =$

$$\Rightarrow \frac{\frac{V_s}{4fL}}{\frac{V_s}{R}}$$

\*  $\delta$  dependent  
per unit ripple  $\approx \frac{1}{4RfL}$  [max when  $\alpha = 0.5$ ]

\* ripple  $\approx I_{mx} - I_{min} = \frac{V_s}{4fL}$   
 $\delta$  independent

$$n\alpha \pi$$

$$n\alpha = 1$$

\* rms value of fund. voltage  $\approx \frac{0.45 V_s}{n} (\text{or}) \frac{2V_s}{\pi \sqrt{2}} \cdot \sin(n\alpha)$

\*  $R_F = \sqrt{\frac{1}{\alpha} - 1}$

$$\alpha = 1$$

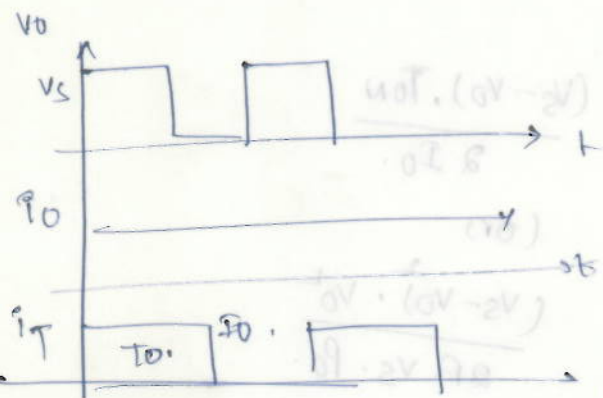
to eliminate  $n^{\text{th}}$  Harmonic

\* TYPE-A  $\rightarrow$  RLIS  $\Rightarrow$

$$I_{T(av)} = \frac{\alpha(V_s - E)}{R}$$

$$= \frac{L}{RT} (I_{mx} - I_{min})$$

↑  
increase ripple present



$$I_T \Rightarrow I_o \times \frac{T_o}{T_b} \Rightarrow \alpha \left( \frac{2V_s - E}{R} \right) \approx \frac{2V_s - E}{R}$$

$$d = \frac{E}{2V_s}$$

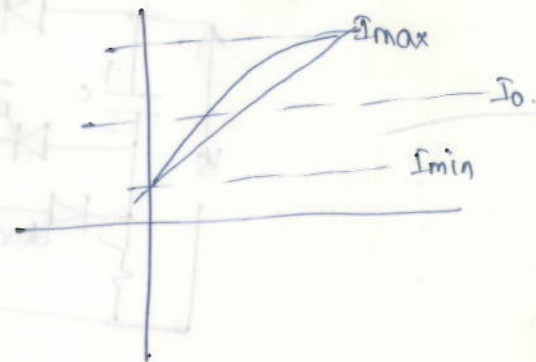
$$I_{T(max)} \approx \frac{E^2}{4V_s R}$$

Process To find  $I_{max}$ ,  $I_{min}$  in a chopper:-

find  $I_0 \approx \frac{V_s - E}{R_L}$  (RLE)

find  $\Delta I \approx I_{max} - I_{min} = \frac{V_s}{L f_L}$

$I_0 \approx \frac{I_{max} + I_{min}}{2} = \frac{V_s}{L f_L}$



$I_{max} + I_{min} = 2 I_0$

$I_{max} - I_{min} = \frac{V_s}{L f_L}$

$2 I_{max} = ( )$

A stepdown (Type-A)  $\approx$  Inductance  $\propto \alpha(1-\alpha)$

$\alpha = \text{duty cycle}$

$\frac{2V_s}{\pi f_L} \sin(\alpha \delta)$

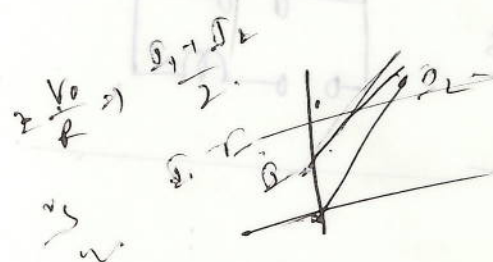
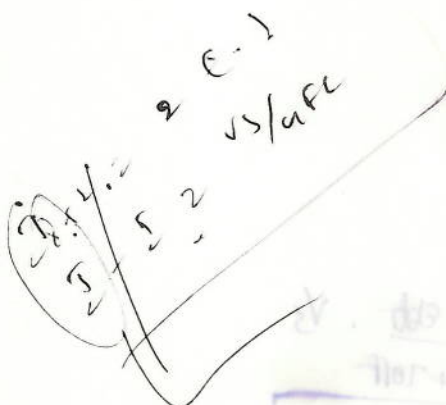
$\frac{2V_s}{\pi f_L} \sin(\alpha \delta)$

chopper RLE load:-

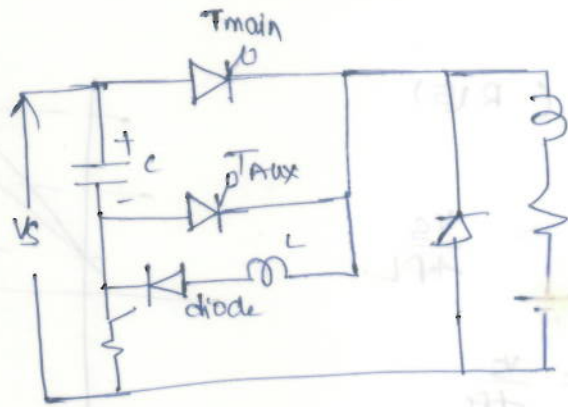
$\frac{E}{V_s} \geq 0$

yes  $\rightarrow$  Conti

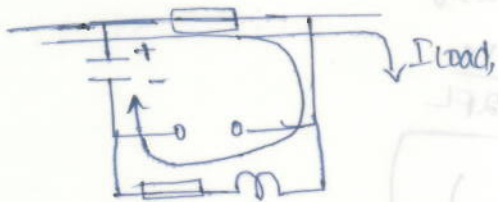
No  $\rightarrow$  Disc.



# Voltage commutated chopper



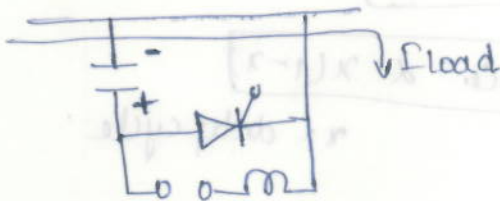
mode (1)



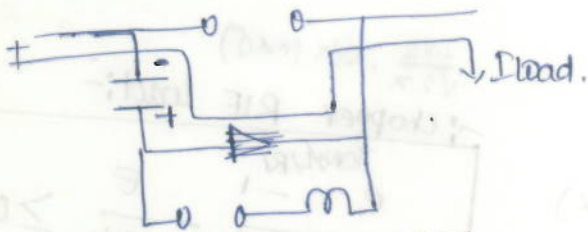
more current handled, by main thyristor

$$I_{total} \approx I_{load} + V_s \sqrt{C/L}$$

mode (2)

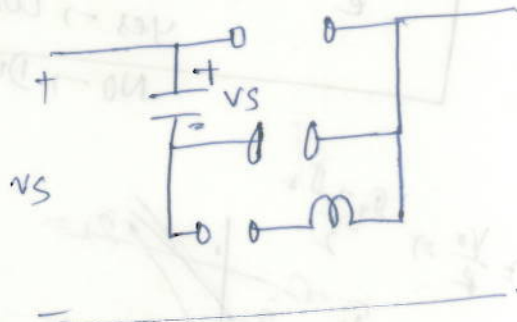


mode (3)



voltage across load  $\approx \underline{2V_s}$

mode (4)



no-load operation fails.

$$T_{eff} = T_{ON} + \frac{2V_s \cdot C}{I_0} ; \Rightarrow$$

max.

$$V_o = \frac{T_{ON} \cdot T_{eff}}{T_{ON} + T_{off}} \cdot V_s$$

$$V_o \approx T_{ON} \cdot T_{eff} \cdot V_s \cdot F$$



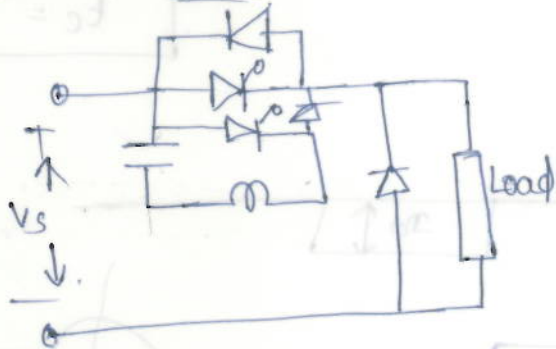
$$t_c = R_c \ln(2)$$

$$T_{on} + \frac{2V_{s.c}}{I_o}$$

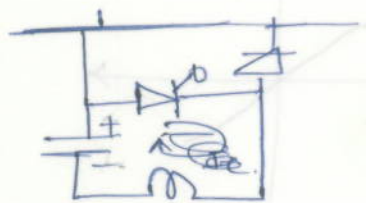
The diagrams show two types of simple machines. The first is a pulley, consisting of a wheel with a rope passing over it. The second is a lever, consisting of a rigid bar pivoted on a point, with a fulcrum in the middle and a load on one end and an effort on the other.

<b>NOVEMBER</b> 30 31 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 1995	<b>DECEMBER</b> 31 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 1995	<b>JANUARY</b> 31 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 1995	<b>FEBRUARY</b> 28 29 30 31 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 1995	<b>MARCH</b> 31 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 1995	<b>APRIL</b> 30 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 1995	<b>MAY</b> 31 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 1995	<b>JUNE</b> 30 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 1995	<b>JULY</b> 31 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 1995	<b>AUGUST</b> 31 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 1995	<b>SEPTEMBER</b> 30 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 1995	<b>OCTOBER</b> 31 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 1995	<b>NOVEMBER</b> 30 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 1995	<b>DECEMBER</b> 31 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 1995
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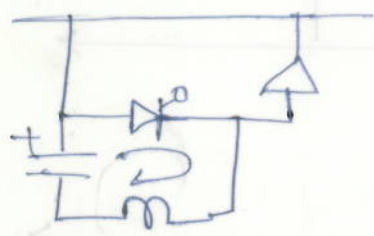
nger from  
like the



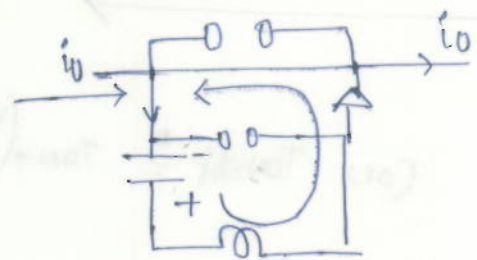
mode ①



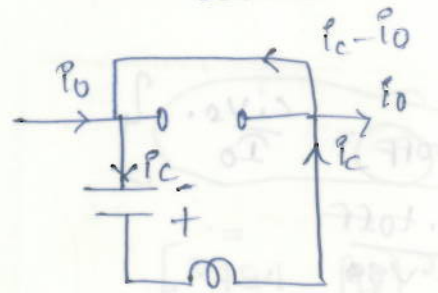
mode ②



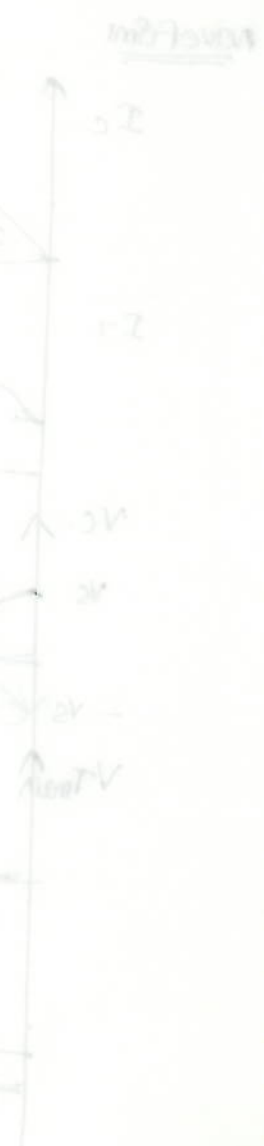
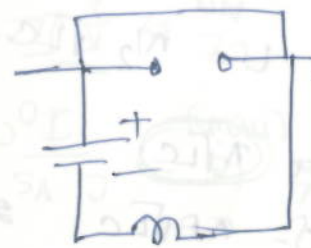
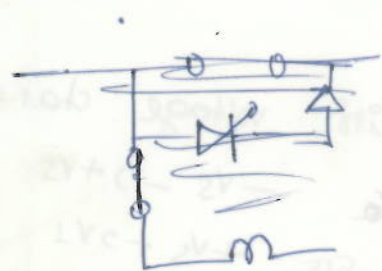
mode ③



mode ④



mode ④



Tough waveforms

$$\gamma = \frac{I_{CP}}{I_0} \approx \frac{V_s \sqrt{C/L}}{I_0}$$

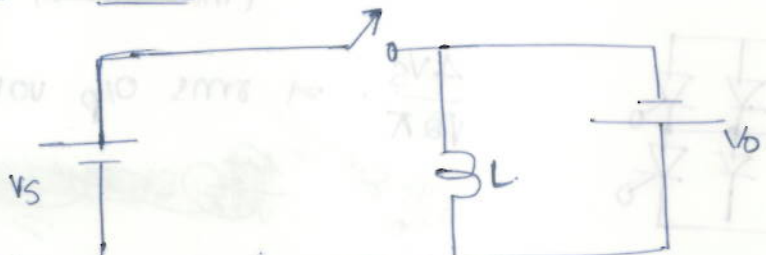
$$T_{main} = \left[ \pi - 2 \sin^{-1}(1/\gamma) \right] / \omega_0 \approx \left[ \pi - 2 \sin^{-1}(1/\gamma) \right] \sqrt{LC}$$

$$C = \left[ \frac{\gamma I_0 \cdot t_c}{V_s \left[ \pi - 2 \sin^{-1}(1/\gamma) \right]} \right]$$

Peak cap voltage  $\rightarrow V_s + I_0 \sqrt{L/C}$

$$T_{AUX} \approx \left[ \pi - \sin^{-1}(1/\gamma) \right] \sqrt{LC}$$

BUCK - BOOST CHOPPER



during  $T_{on}$



$$V = L \frac{di}{dt}$$

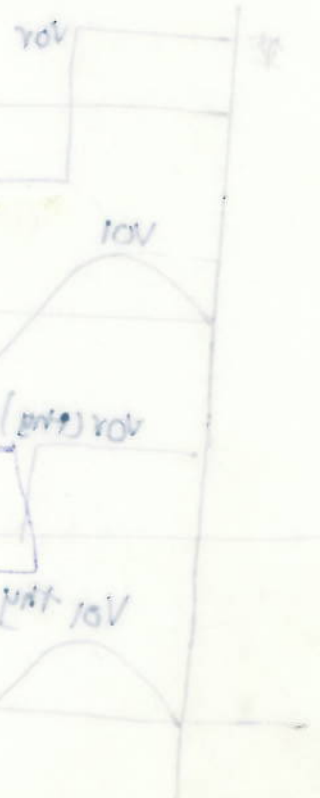
$$V_{in} = L \cdot \frac{\Delta I}{T_{ON}}$$

$$L \cdot \Delta I = V_s T_{ON}$$

$$L \cdot \Delta I = V_o T_{OFF}$$

$$(V_s T_{ON} = V_o T_{OFF})$$

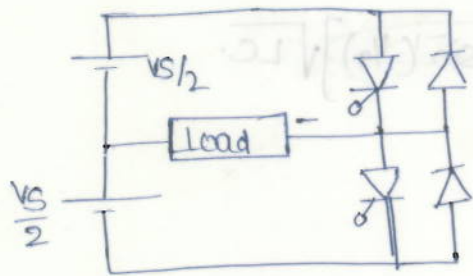
$$V_o = \frac{V_s d}{1-d}$$





# Inverters

\* dc  $\rightarrow$  ac converters.



Half Bridge

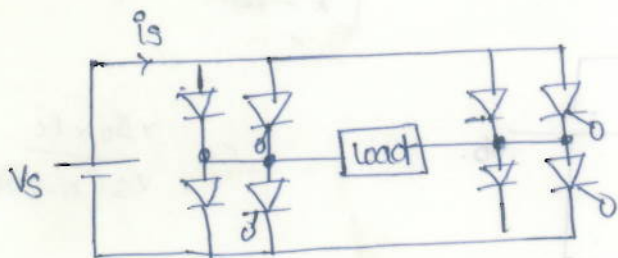
$$\frac{2V_s}{\sqrt{2}\pi} \Rightarrow \text{rms. o/p voltage.}$$

$$\frac{2V_s}{\sqrt{2}\pi} \sin(\omega t)$$

\* prefer R-L-C - under damped loads,

$$\frac{1}{\omega R} \left( \frac{\omega L - \frac{1}{\omega C}}{R} \right) = 0 \Rightarrow \omega L > \frac{1}{\omega C} \Rightarrow \text{under damp.} \Rightarrow \text{Load comm. (Cap-nature)}$$

$$\omega L < \frac{1}{\omega C} \Rightarrow \text{overdamp} \Rightarrow \text{Forced comm (ind-nature).}$$



$$\frac{4V_s}{\sqrt{2}\pi} \Rightarrow \text{rms o/p voltage.}$$

$$\frac{4V_s}{\sqrt{2}\pi} \sin(\omega t)$$

Important things to remember (Full Bridge).

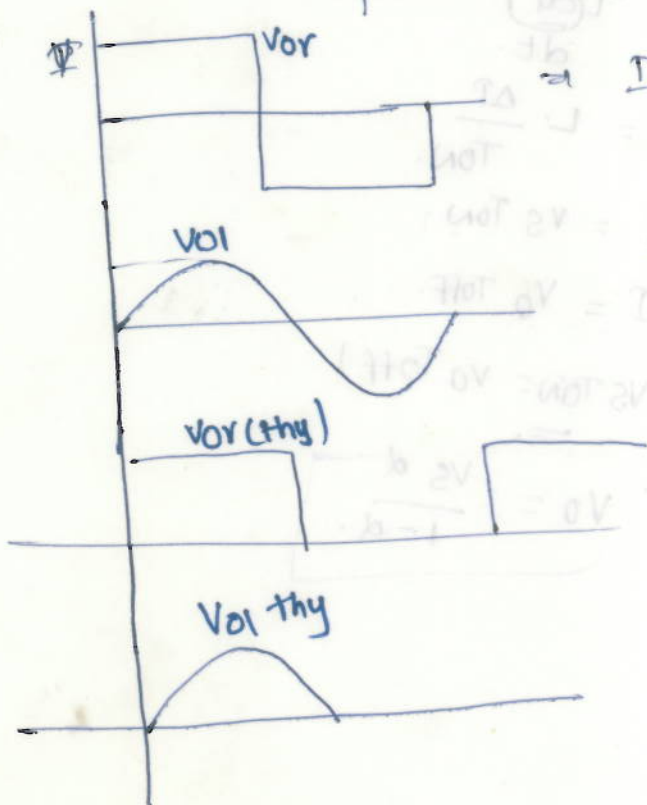
$$I_{rms} = I_o \text{ (avg)}$$

$$I_{avg} = \frac{1}{\pi} \int_0^{\pi} I_m \sin \omega t \Rightarrow \frac{2I_m}{\pi}$$

$$I_{rms} = I_o \sqrt{\frac{1}{2}}$$

$$I_{rms} \Rightarrow \left[ \frac{I_m}{\sqrt{2}} \right] = \frac{I_m}{\sqrt{2}}$$

$$I_{avg} = \frac{I_m}{\pi}$$



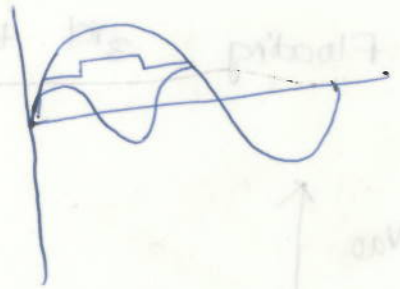
\* mc-murray

(235)

$$v = \frac{L di}{dt}$$

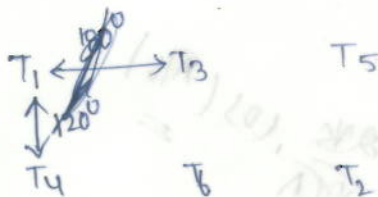
$$L = \frac{V_s t_r \times (2.35)}{I_{om}}$$

$$C = \frac{I_{om} \times t_r \times (2.35)}{V_s}$$



### Three phase Inverters

180° mode



$T_1 \xrightarrow{120^\circ} T_3$

$$\begin{matrix} T_1 \\ \downarrow 180^\circ \\ T_4 \end{matrix} \quad V_{ao} = \frac{2V_s}{\sqrt{2}\pi} \quad (\text{phax})$$

$$(\text{fund}) \quad V_{ab} \approx \frac{4V_s}{\sqrt{2}\pi} \cos(30^\circ) = 2.578 V_s$$

$$V_{ab} \approx \frac{4V_s}{\sqrt{2}\pi} \cos 30^\circ = 0.7800 V_s$$

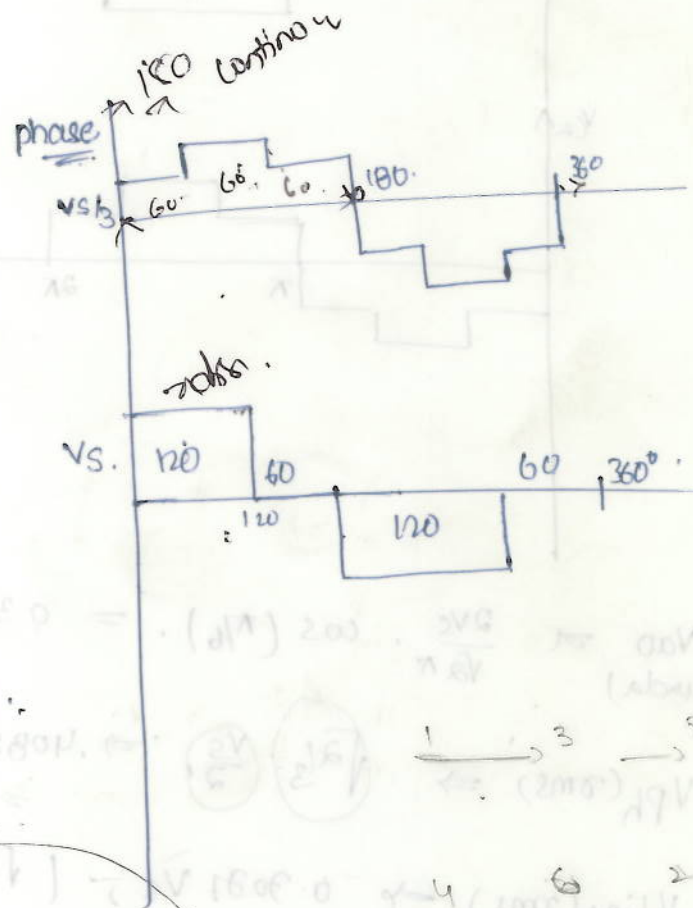
$$V_{ab}(\text{rms}) = \frac{0.7800 V_s}{\sqrt{3}} = 0.4503 V_s$$

$$V_{ao}(\text{fund}) = \frac{0.4503 V_s}{\sqrt{3}} = \frac{V_{ab}(\text{fund})}{\sqrt{3}}$$

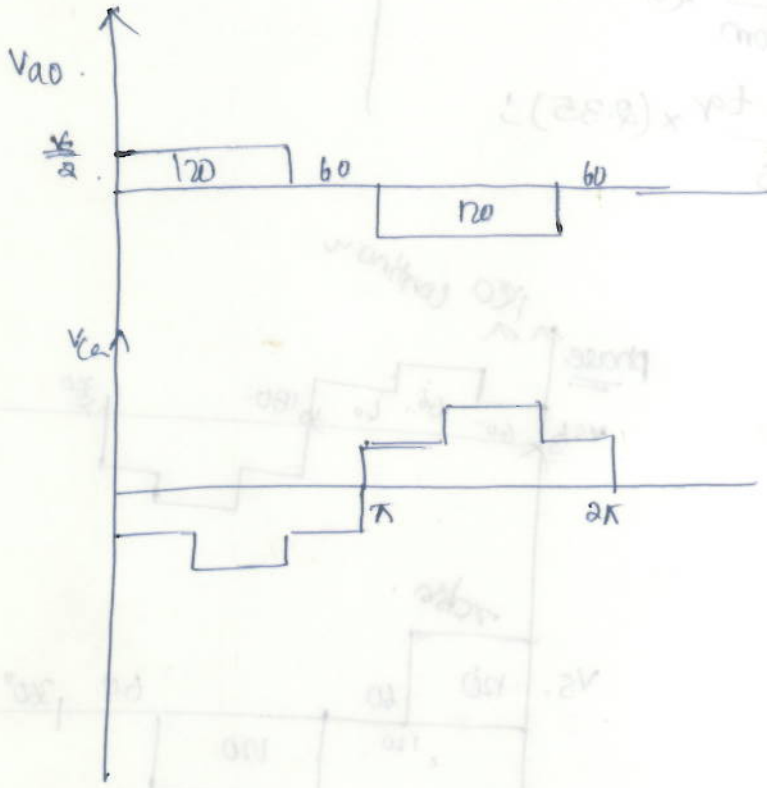
$$V_{ao}(\text{rms}) = \frac{V_{ab}(\text{rms})}{\sqrt{3}} = 0.4714 V_s$$

\* Three thyristors conduct at any time;

\*  $V_{s13}$



\* Floating 3rd terminal (Potentially Balanced for (R) load, unbalanced for Remaining)



$$\frac{V_s}{2} \times \sqrt{\frac{120}{180}} = \frac{V_s}{2}$$

$$\frac{2V_s}{\sqrt{2}} \cos(\pi/6) = \frac{2V_s}{\sqrt{2}} \cdot \frac{\sqrt{3}}{2} = \frac{V_s \sqrt{3}}{\sqrt{2}}$$

$$\frac{V_s}{2} \times \sqrt{\frac{2}{3}} = \frac{V_s}{2}$$

$V_{ao} \approx \frac{2V_s}{\sqrt{2}} \cos(\pi/6) = 0.3898V_s$   
(Fund)

$V_{ph}(rms) \Rightarrow \sqrt{\frac{2}{3}} \left( \frac{V_s}{2} \right) = 0.4082V_s$

$V_{line}(rms) \Rightarrow 0.7071V_s ; \left( \sqrt{\frac{2}{3}} \right) \times \frac{V_s}{2} \cdot \sqrt{3} = 0.7071V_s$

Find  $\frac{V_s}{2} \sqrt{\frac{120}{180}}$ ; gives load current for load.  
then  $\frac{V_s}{2} \sqrt{\frac{120}{360}}$  gives hypotenuse current.



# PULSE WIDTH MODULATION

\* ~~total~~ less components needed,

\* lower harmonics in op eliminated, higher order can be filtered out. (LC filter)

## Single pulse modulation

$$V_{or} = V_s \sqrt{\frac{2d}{\pi}}$$

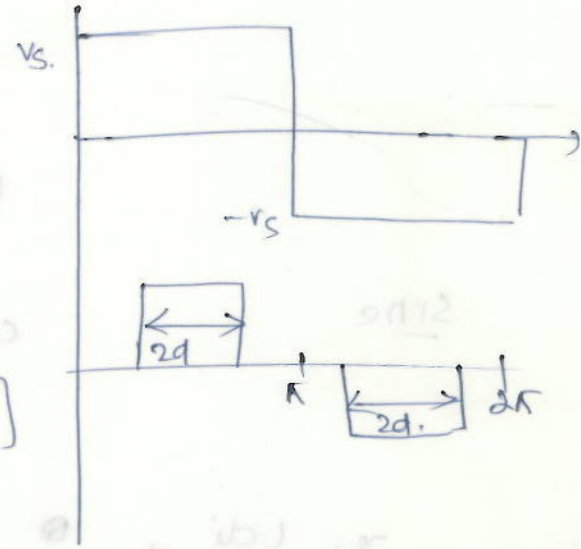
$$V_o \approx \frac{4V_s}{\pi} \cdot \sin\left(\frac{n\pi}{2}\right) \cdot \sin(nd) \quad (\text{max})$$

$\uparrow$  Both (sines)

$$V_{orm} \Rightarrow \frac{4V_s}{\pi} \dots \rightarrow \left[ \text{if } 2d = \pi \right]$$

$$\Rightarrow \left[ \frac{4V_s}{\pi} \sin nd \right] \text{ if } d \neq \pi/2$$

To Eliminate  $n^{\text{th}}$  harmonic make  $2d = \frac{2\pi}{n}$



$$2d = 2\pi = 360^\circ$$

$$\frac{V_{orm}}{V_{orm}} = \frac{\sin nd}{n} \quad \left. \begin{array}{l} \text{increase} \\ [d = \pi/2] \end{array} \right\}$$

## MULTIPLE PULSE MODULATION

$$\left[ d = \frac{2\pi}{n} \right]$$

$$V_{or} = V_s \sqrt{\frac{2d}{\pi}}$$

$$\frac{4V_s}{\pi} \sin(nd) \sin\left(\frac{n\pi}{2}\right)$$

$$2d = \pi \Rightarrow \pi/n \Rightarrow 2d = \frac{2\pi}{n}$$

width  $\propto \frac{2\pi}{n}$

To eliminate  $n^{\text{th}}$  harmonic  $\Rightarrow 2d = \frac{2\pi}{n}$  (single pulse!)

$$d = \frac{\pi}{n} \quad (\text{multi})$$

Current Source Inverters\* no feedback diodes,

\* only SCR's/GTO's

SQ. wave output,

$$f_{max} = \frac{1}{10RC}$$

$$C = \frac{t_{qr}}{0.69R}$$

$$f_{max} = \frac{0.069}{t_{qr}}$$

$$C \geq \frac{0.106}{R f_{min}}$$

$$v = L \frac{di}{dt}$$

$$T = 1/f = \pi \frac{1}{50}$$

$$\frac{di}{dt} = \frac{0.5}{T} \Rightarrow 25$$

$$V_s = L \frac{di}{dt}$$

$$L = \frac{V_s}{di/dt} = \left( \frac{1}{25} \right)$$

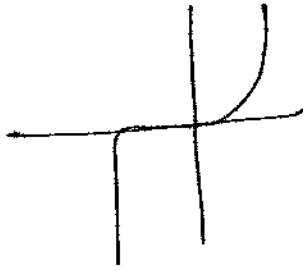
$$t_c = R_c \ln(2)$$

H/03/14

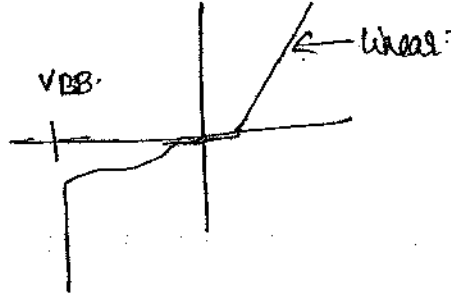
# IES MADE EASY POWER ELECTRONICS :

Santhosh

signal diode



power diode



\* The thickness of depletion region governs reverse blocking voltage.

general purpose

fast recovery

no recovery → [short E]

• nano seconds

$t_{on} = 5 \mu s$

→  $t_{on} = 25 \mu s$

→ Amps → 1 to 1000 A

→  $I = 1 A$  to  $100 A$

→ Limited to 300 A

→  $V_{rating} \Rightarrow 50 V$  to  $5 K V$

→  $V_{rating} \Rightarrow 50 V$  to  $3 K V$

→  $V_{rating} 100 V$

→ gold, platinum doping

→ conduction due to majority carrier

→ very high switch freq

\* In SCR:  $I_{latch} = 214 I_{hold}$

\* Temperature Ⓢ Power Avg analogy:-

↓  $I_{avg}$  on  $\theta$  → Junction, casing, Sink, Ambient





single pulse  $\Rightarrow 180^\circ/360^\circ$  ;

Two pulse  $\Rightarrow \frac{2\pi}{2} \Rightarrow 180^\circ$  & every  $180^\circ$  ;

Three pulse  $\Rightarrow \frac{2\pi}{3} \Rightarrow 120^\circ$  (each) ;

Six Pulse  $\Rightarrow \frac{2\pi}{6} \Rightarrow 60^\circ$  (each envelope)

