

The Data

This week we'll be working with measurements of body dimensions. This data set contains measurements from 247 men and 260 women, most of whom were considered healthy young adults.

```
#bdims <- read.csv("C:/CUNY/Courses/CUNY-repository/606/Week3-09_Sep2016/Lab3/more/Body.csv", header=TRUE)
load("C:/CUNY/Courses/CUNY-repository/606/Week3-09_Sep2016/Lab3/more/bdims.RData")
```

Let's take a quick peek at the first few rows of the data.

```
head(bdims)
```

```
##   bia.di bii.di bit.di che.de che.di elb.di wri.di kne.di ank.di sho.di
## 1  42.9  26.0  31.5  17.7  28.0  13.1  10.4  18.8  14.1 106.2
## 2  43.7  28.5  33.5  16.9  30.8  14.0  11.8  20.6  15.1 110.5
## 3  40.1  28.2  33.3  20.9  31.7  13.9  10.9  19.7  14.1 115.1
## 4  44.3  29.9  34.0  18.4  28.2  13.9  11.2  20.9  15.0 104.5
## 5  42.5  29.9  34.0  21.5  29.4  15.2  11.6  20.7  14.9 107.5
## 6  43.3  27.0  31.5  19.6  31.3  14.0  11.5  18.8  13.9 119.8
##   che.di wai.di nav.di hip.di thi.di bic.di for.di kne.di cal.di ank.di
## 1  89.5  71.5  74.5  93.5  51.5  32.5  26.0  34.5  36.5  23.5
## 2  97.0  79.0  86.5  94.8  51.5  34.4  28.0  36.5  37.5  24.5
## 3  97.5  83.2  82.9  95.0  57.3  33.4  28.8  37.0  37.3  21.9
## 4  97.0  77.8  78.8  94.0  53.0  31.0  26.2  37.0  34.8  23.0
## 5  97.5  80.0  82.5  98.5  55.4  32.0  28.4  37.7  38.6  24.4
## 6  99.9  82.5  80.1  95.3  57.5  33.0  28.0  36.6  36.1  23.5
##   wri.di age  wgt  hgt sex
## 1  16.5  21 65.6 174.0  1
## 2  17.0  23 71.8 175.3  1
## 3  16.9  28 80.7 193.5  1
## 4  16.6  23 72.6 186.5  1
## 5  18.0  22 78.8 187.2  1
## 6  16.9  21 74.8 181.5  1
```

You'll see that for every observation we have 25 measurements, many of which are either diameters or girths. A key to the variable names can be found at <http://www.openintro.org/stat/data/bdims.php>, but we'll be focusing on just three columns to get started: weight in kg (**wgt**), height in cm (**hgt**), and **sex** (1 indicates male, 0 indicates female).

Since males and females tend to have different body dimensions, it will be useful to create two additional data sets: one with only men and another with only women.

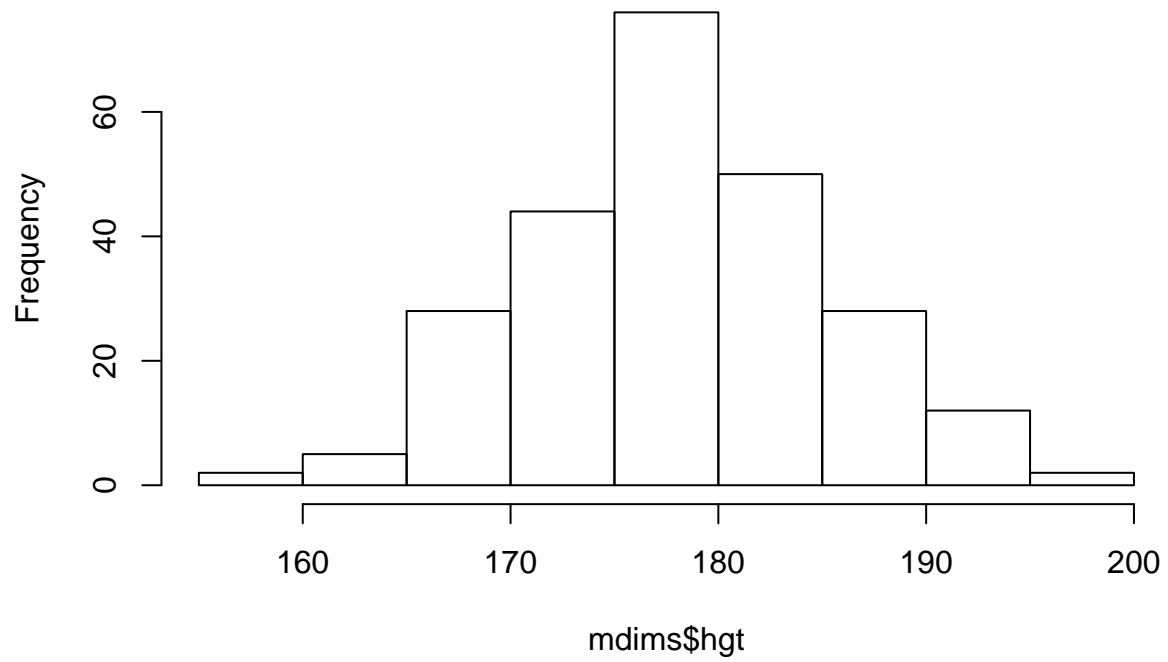
```
mdims <- subset(bdims, sex == 1)
fdims <- subset(bdims, sex == 0)
```

1. Make a histogram of men's heights and a histogram of women's heights. How would you compare the various aspects of the two distributions?

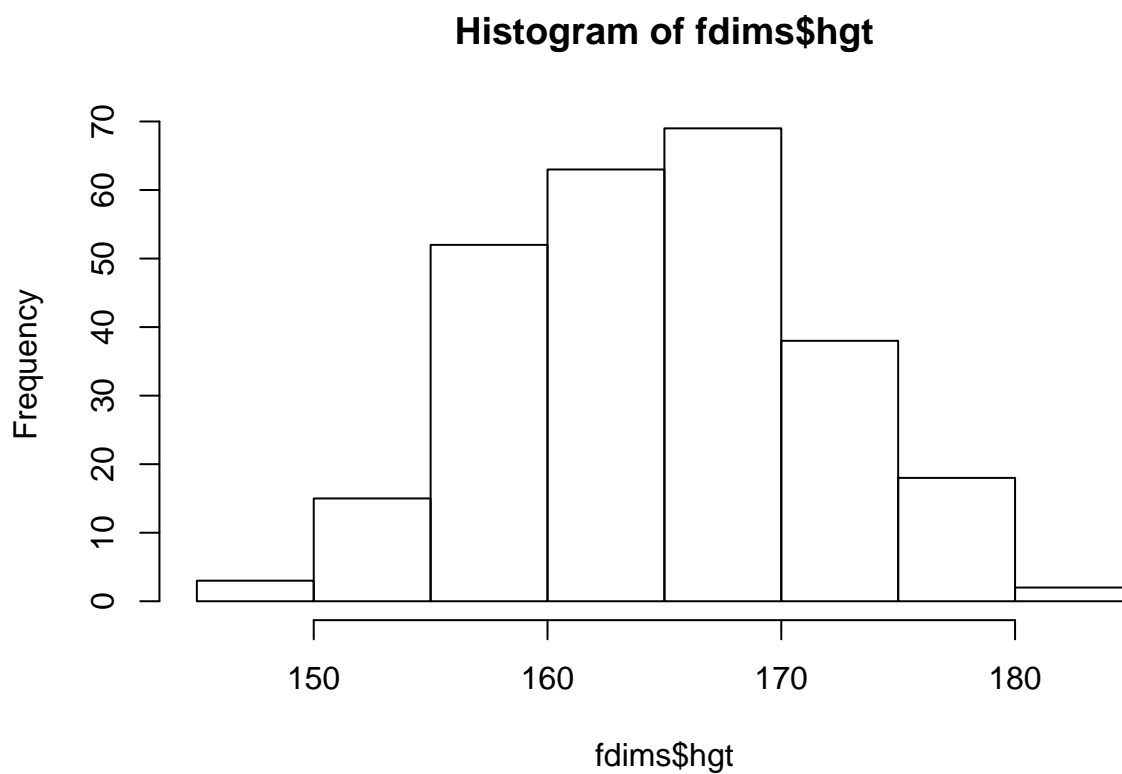
Answer

```
hist(mdims$hgt)
```

Histogram of mdims\$hgt



```
hist(fdims$hgt)
```

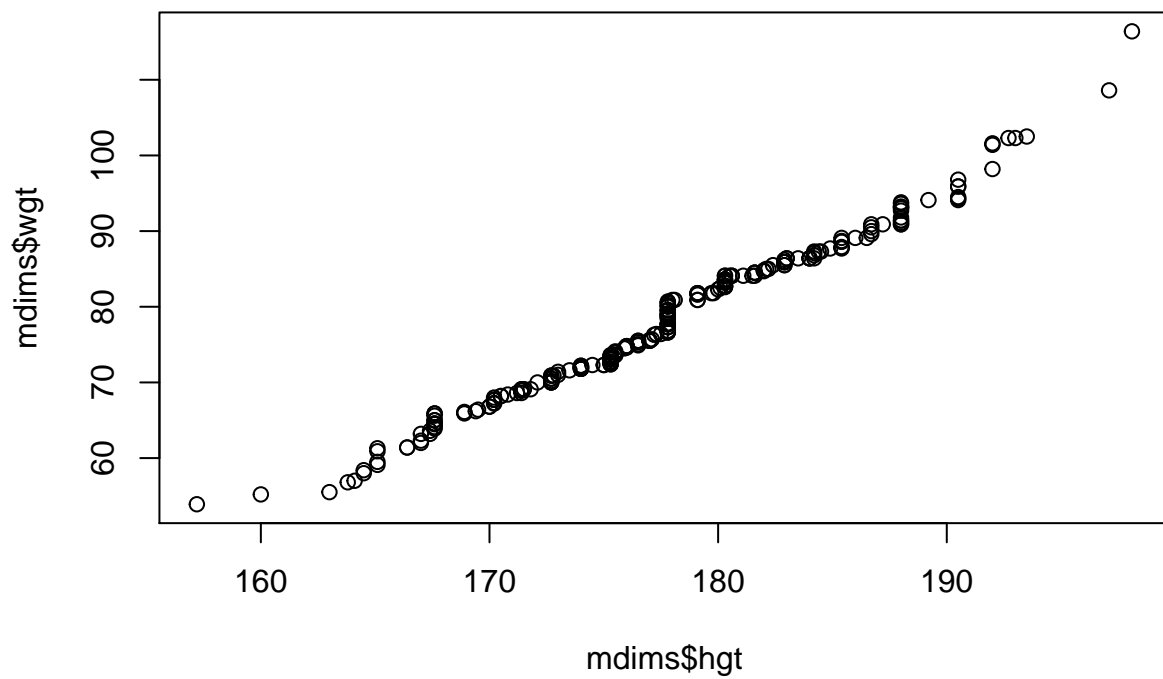


Men hights are an perfect unimodel symmetric normal distribution. The mean is centered around 178.

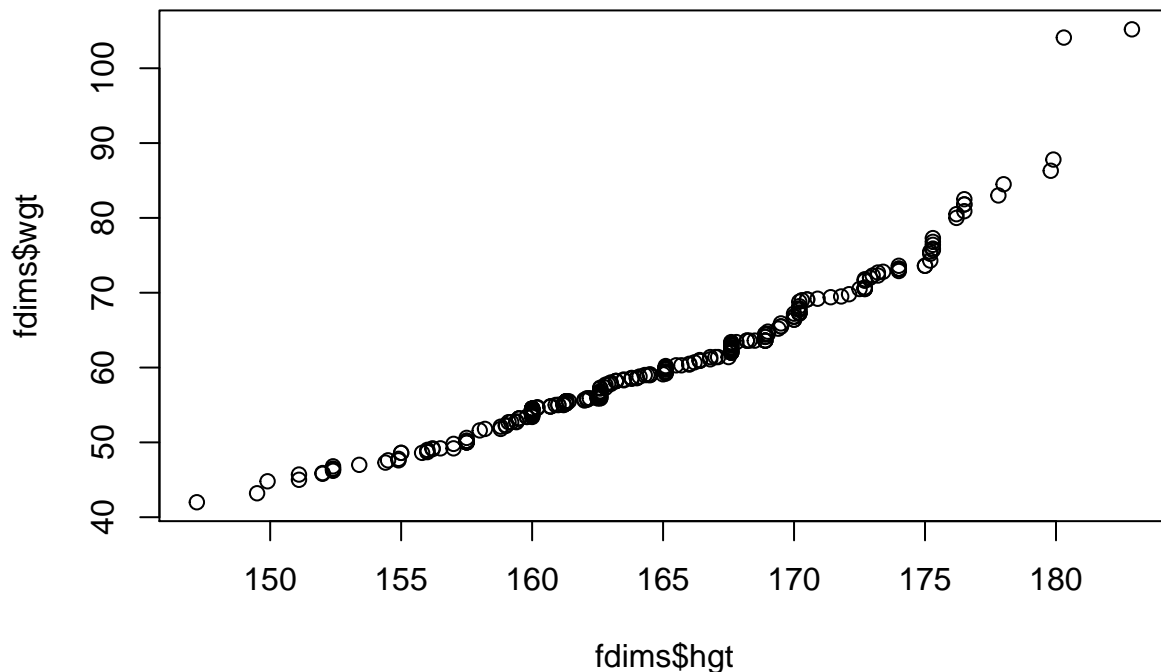
Female hights are an unimodel symmetric normal distribution. The mean is centered around 168.

Below are the qqplot of height and weight.

```
qqplot(mdims$hgt,mdims$wgt)
```



```
qqplot(fdims$hgt,fdims$wgt)
```



The normal distribution

In your description of the distributions, did you use words like *bell-shaped* or *normal*? It's tempting to say so when faced with a unimodal symmetric distribution.

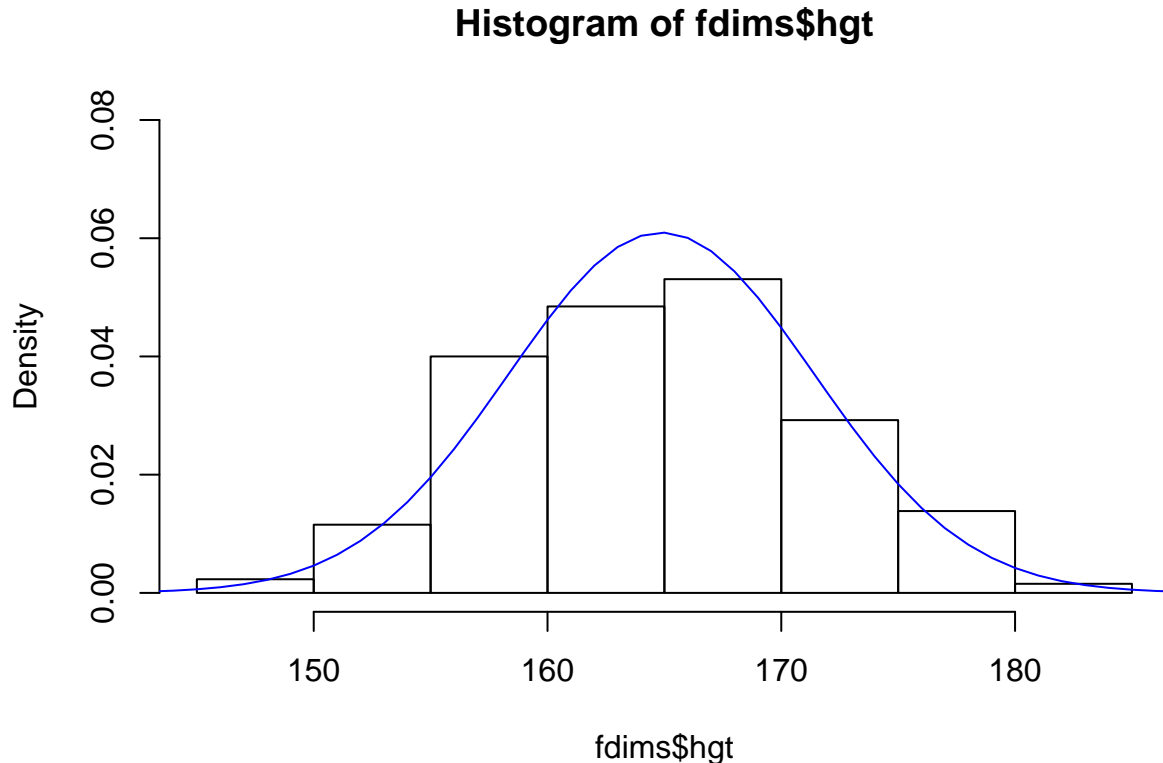
To see how accurate that description is, we can plot a normal distribution curve on top of a histogram to see how closely the data follow a normal distribution. This normal curve should have the same mean and standard deviation as the data. We'll be working with women's heights, so let's store them as a separate object and then calculate some statistics that will be referenced later.

```
fhgtmean <- mean(fdims$hgt)
fhgtsd   <- sd(fdims$hgt)
```

Next we make a density histogram to use as the backdrop and use the `lines` function to overlay a normal probability curve. The difference between a frequency histogram and a density histogram is that while in a frequency histogram the *heights* of the bars add up to the total number of observations, in a density histogram the *areas* of the bars add up to 1. The area of each bar can be calculated as simply the height *times* the width of the bar. Using a density histogram allows us to properly overlay a normal distribution curve over the histogram since the curve is a normal probability density function. Frequency and density histograms both display the same exact shape; they only differ in their y-axis. You can verify this by comparing the frequency histogram you constructed earlier and the density histogram created by the commands below.

```
hist(fdims$hgt, probability = TRUE, ylim = c(0, 0.08))
x <- 140:190
```

```
y <- dnorm(x = x, mean = fhgtmean, sd = fhgtstd)
lines(x = x, y = y, col = "blue")
```



After plotting the density histogram with the first command, we create the x- and y-coordinates for the normal curve. We chose the x range as 140 to 190 in order to span the entire range of `fheight`. To create `y`, we use `dnorm` to calculate the density of each of those x-values in a distribution that is normal with mean `fhgtmean` and standard deviation `fhgtstd`. The final command draws a curve on the existing plot (the density histogram) by connecting each of the points specified by `x` and `y`. The argument `col` simply sets the color for the line to be drawn. If we left it out, the line would be drawn in black.

The top of the curve is cut off because the limits of the x- and y-axes are set to best fit the histogram. To adjust the y-axis you can add a third argument to the histogram function: `ylim = c(0, 0.06)`.

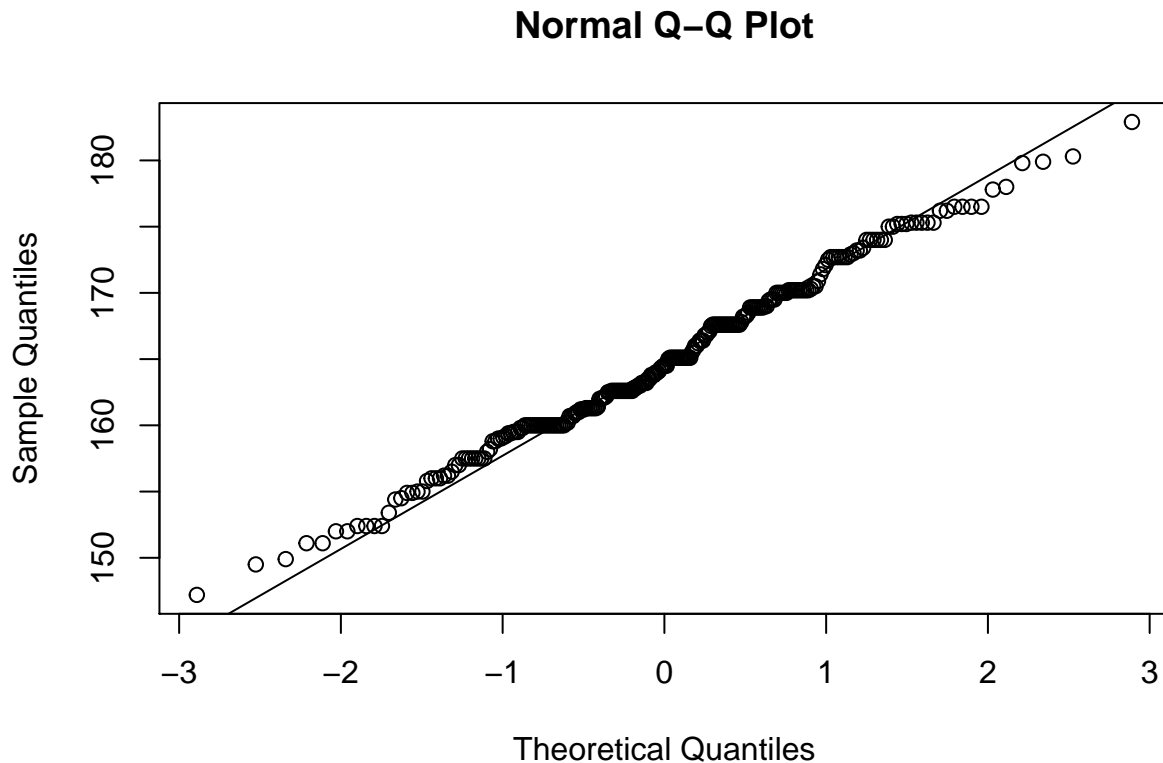
2. Based on the this plot, does it appear that the data follow a nearly normal distribution?

Answer Yes. The data are nearly falling into an noraml distribution

Evaluating the normal distribution

Eyeballing the shape of the histogram is one way to determine if the data appear to be nearly normally distributed, but it can be frustrating to decide just how close the histogram is to the curve. An alternative approach involves constructing a normal probability plot, also called a normal Q-Q plot for “quantile-quantile”.

```
qqnorm(fdims$hgt)
qqline(fdims$hgt)
```



A data set that is nearly normal will result in a probability plot where the points closely follow the line. Any deviations from normality leads to deviations of these points from the line. The plot for female heights shows points that tend to follow the line but with some errant points towards the tails. We're left with the same problem that we encountered with the histogram above: how close is close enough?

A useful way to address this question is to rephrase it as: what do probability plots look like for data that I *know* came from a normal distribution? We can answer this by simulating data from a normal distribution using `rnorm`.

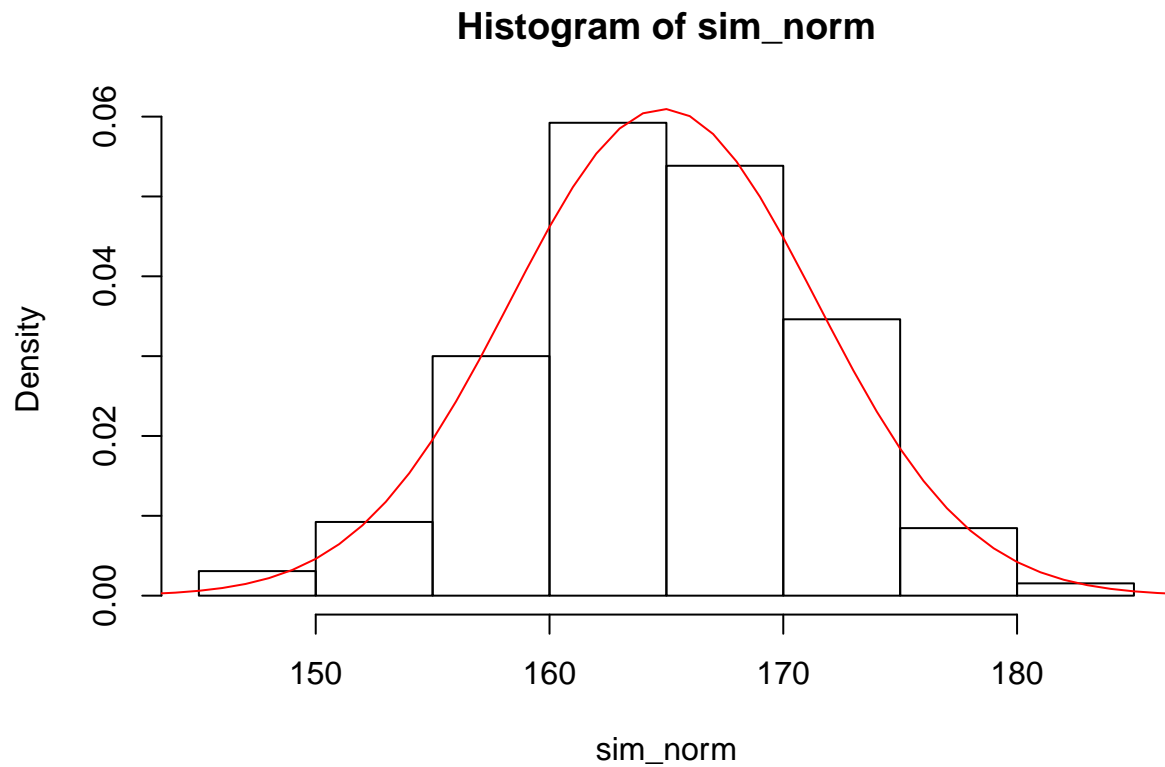
```
sim_norm <- rnorm(n = length(fdims$hgt), mean = fhgtmean, sd = fhgtstd)
```

The first argument indicates how many numbers you'd like to generate, which we specify to be the same number of heights in the `fdims` data set using the `length` function. The last two arguments determine the mean and standard deviation of the normal distribution from which the simulated sample will be generated. We can take a look at the shape of our simulated data set, `sim_norm`, as well as its normal probability plot.

**** 3. Make a normal probability plot of `sim_norm`. Do all of the points fall on the line? How does this plot compare to the probability plot for the real data? ****

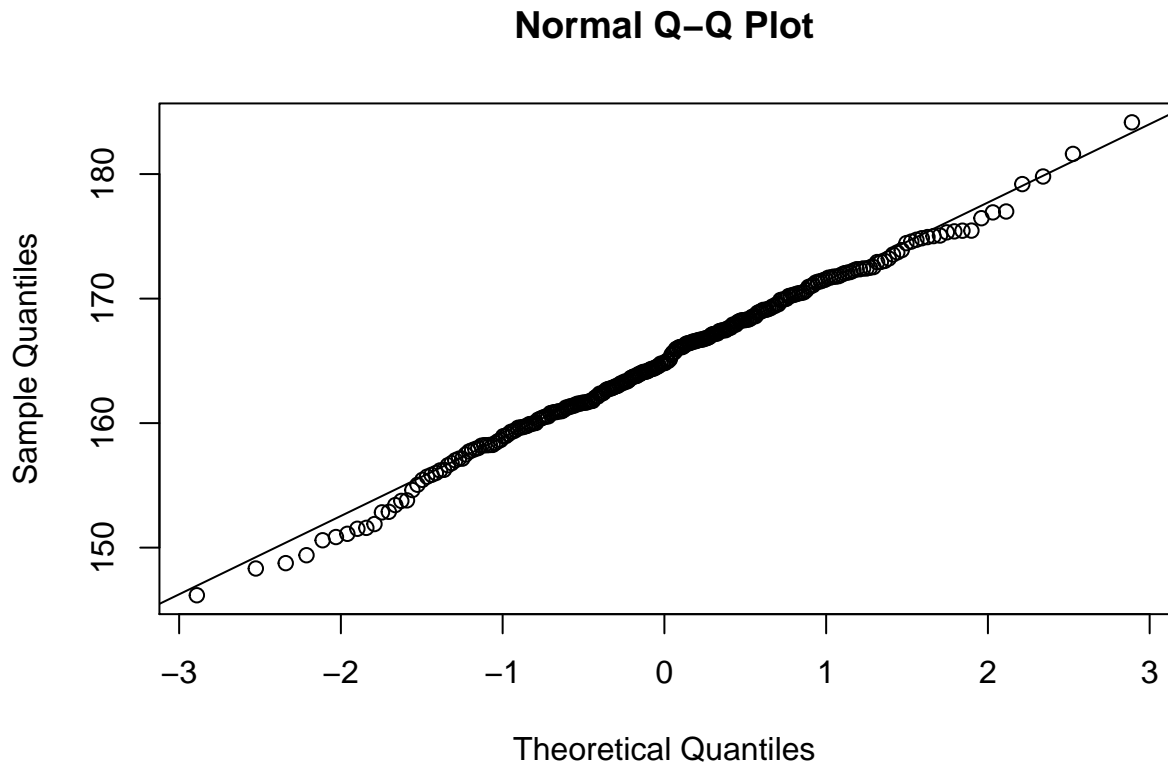
Below is the histogram plot of `sim_norm`. Most of the point bins fall under normal distribution curve. But this might vary depends on the `rnorm`.

```
hist(sim_norm,probability = TRUE)
simx <- 140:190
simy <- dnorm(simx,mean = fhgtmean,sd=fhgtsd)
lines(simx,simy,col="red")
```



Below is the QQ plot of `sim_norm`. Most of the points fall under a straight line. But this might vary depends on the `rnrm`.

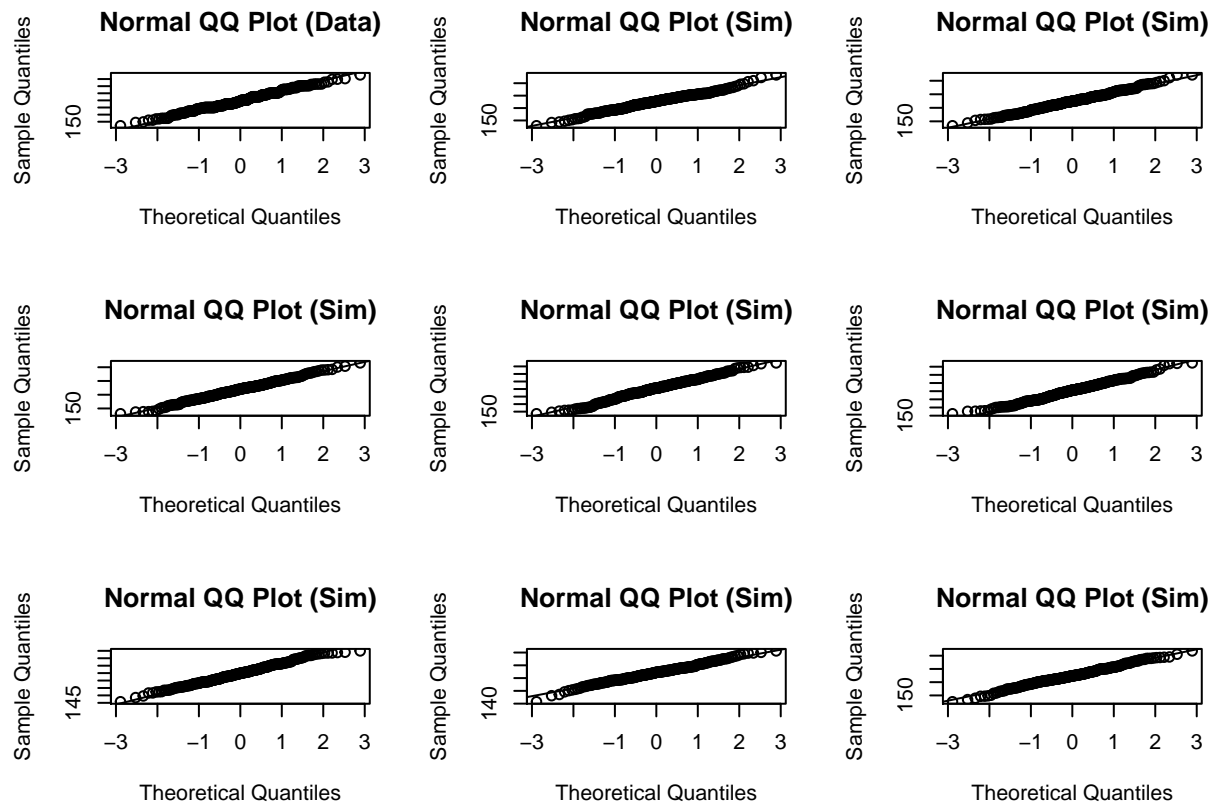
```
qqnorm(sim_norm)
qqline(sim_norm)
```

`sim_norm` plot is more symmetrical and normally distributed compared to the real data.

Even better than comparing the original plot to a single plot generated from a normal distribution is to compare it to many more plots using the following function. It may be helpful to click the zoom button in the plot window.

```
qqnormsim(fdims$hgt)
```



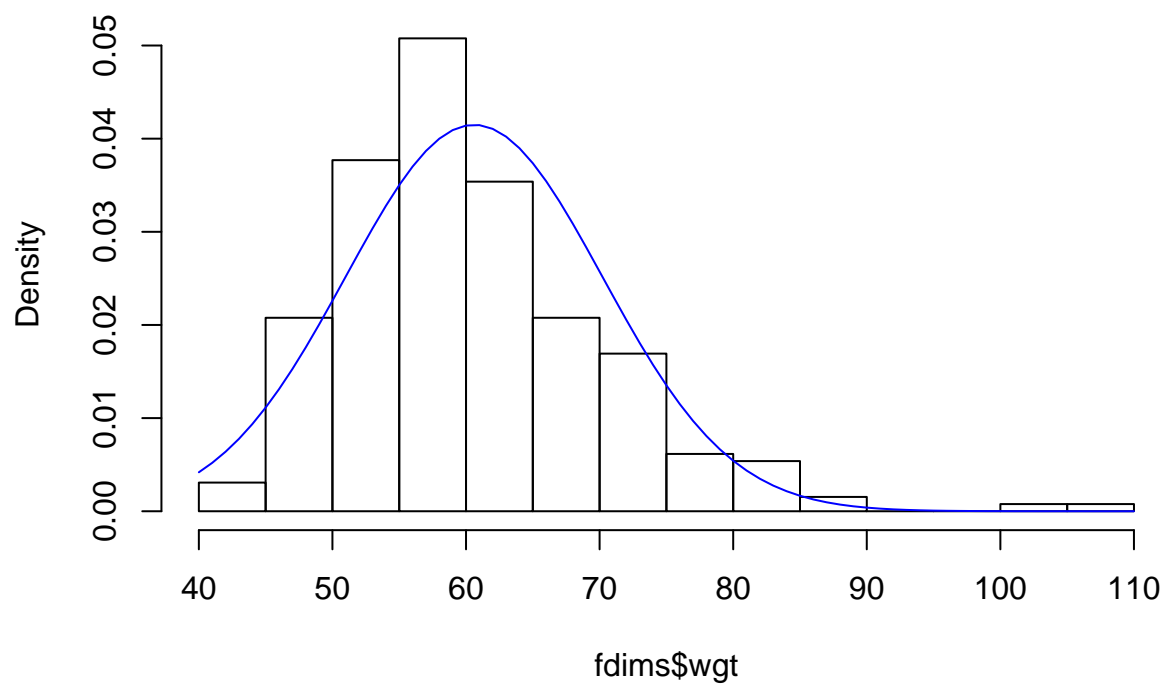
4. Does the normal probability plot for `fdims$ht` look similar to the plots created for the simulated data? That is, do plots provide evidence that the female heights are nearly normal?

Yes. `fdims$ht` look similar to the plots created for simulated data. The plots provide that the female heights are nearly normal

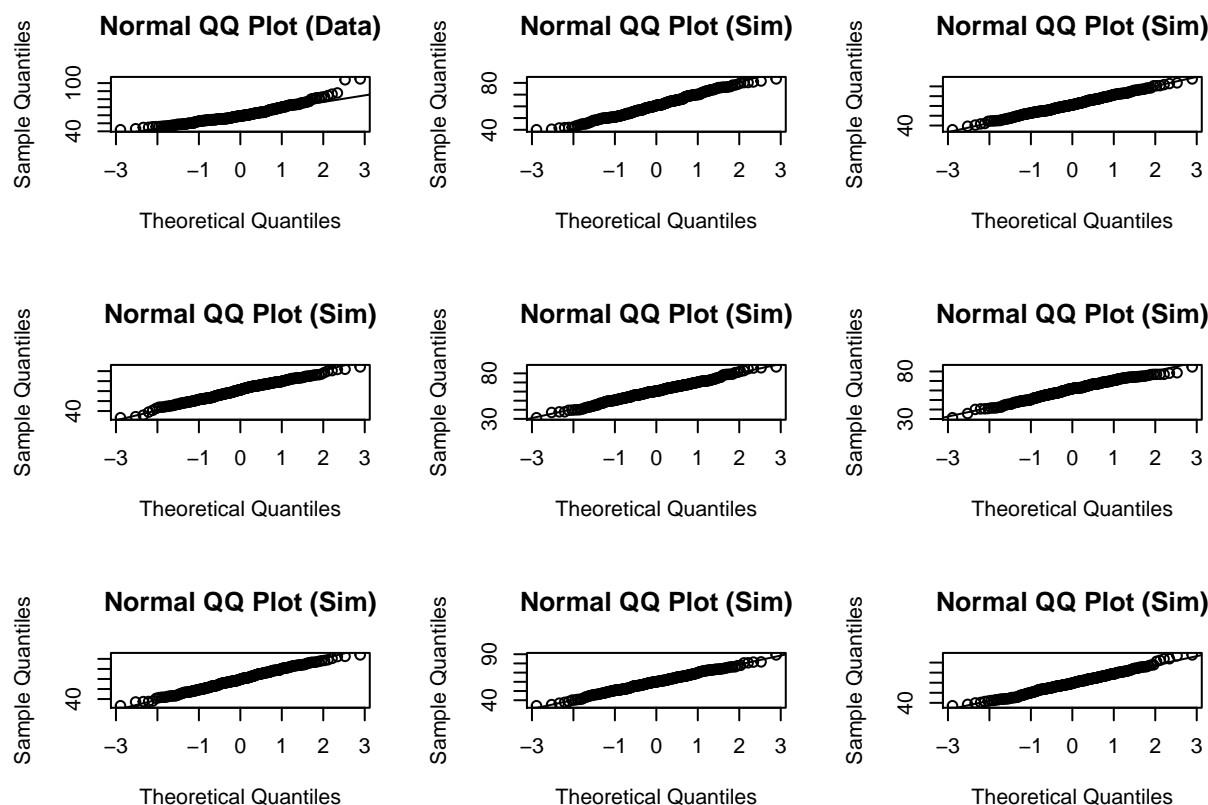
5. Using the same technique, determine whether or not female weights appear to come from a normal distribution.

```
hist(fdims$wgt, probability = TRUE)
x <- 40:110
y <- dnorm(x = x, mean = mean(fdims$wgt), sd = sd(fdims$wgt))
lines(x = x, y = y, col = "blue")
```

Histogram of fdims\$wgt



```
qqnormsim(fdims$wgt)
```



** This distribution is skewed to its right. And there were some outliers, `fdims$wgt` look similar to the plots created for simulated data. The plots provide that the female weights are nearly normal**

Normal probabilities

Okay, so now you have a slew of tools to judge whether or not a variable is normally distributed. Why should we care?

It turns out that statisticians know a lot about the normal distribution. Once we decide that a random variable is approximately normal, we can answer all sorts of questions about that variable related to probability. Take, for example, the question of, “What is the probability that a randomly chosen young adult female is taller than 6 feet (about 182 cm)?” (The study that published this data set is clear to point out that the sample was not random and therefore inference to a general population is not suggested. We do so here only as an exercise.)

If we assume that female heights are normally distributed (a very close approximation is also okay), we can find this probability by calculating a Z score and consulting a Z table (also called a normal probability table). In R, this is done in one step with the function `pnorm`.

```
1 - pnorm(q = 182, mean = fhgtmean, sd = fhgtsd)
```

```
## [1] 0.004434387
```

Note that the function `pnorm` gives the area under the normal curve below a given value, `q`, with a given mean and standard deviation. Since we’re interested in the probability that someone is taller than 182 cm, we have to take one minus that probability.

Assuming a normal distribution has allowed us to calculate a theoretical probability. If we want to calculate the probability empirically, we simply need to determine how many observations fall above 182 then divide this number by the total sample size.

```
sum(fdims$hgt > 182) / length(fdims$hgt)
```

```
## [1] 0.003846154
```

Although the probabilities are not exactly the same, they are reasonably close. The closer that your distribution is to being normal, the more accurate the theoretical probabilities will be.

6. Write out two probability questions that you would like to answer; one regarding female heights and one regarding female weights. Calculate the those probabilities using both the theoretical normal distribution as well as the empirical distribution (four probabilities in all). Which variable, height or weight, had a closer agreement between the two methods?

Probability of a random female picked is above height 165?

```
1-pnorm(165, mean=mean(fdims$hgt),sd=sd(fdims$hgt))
```

```
## [1] 0.4922167
```

Probability of a random female picked is below weight 20?

```
pnorm(20, mean=mean(fdims$wgt),sd=sd(fdims$wgt))
```

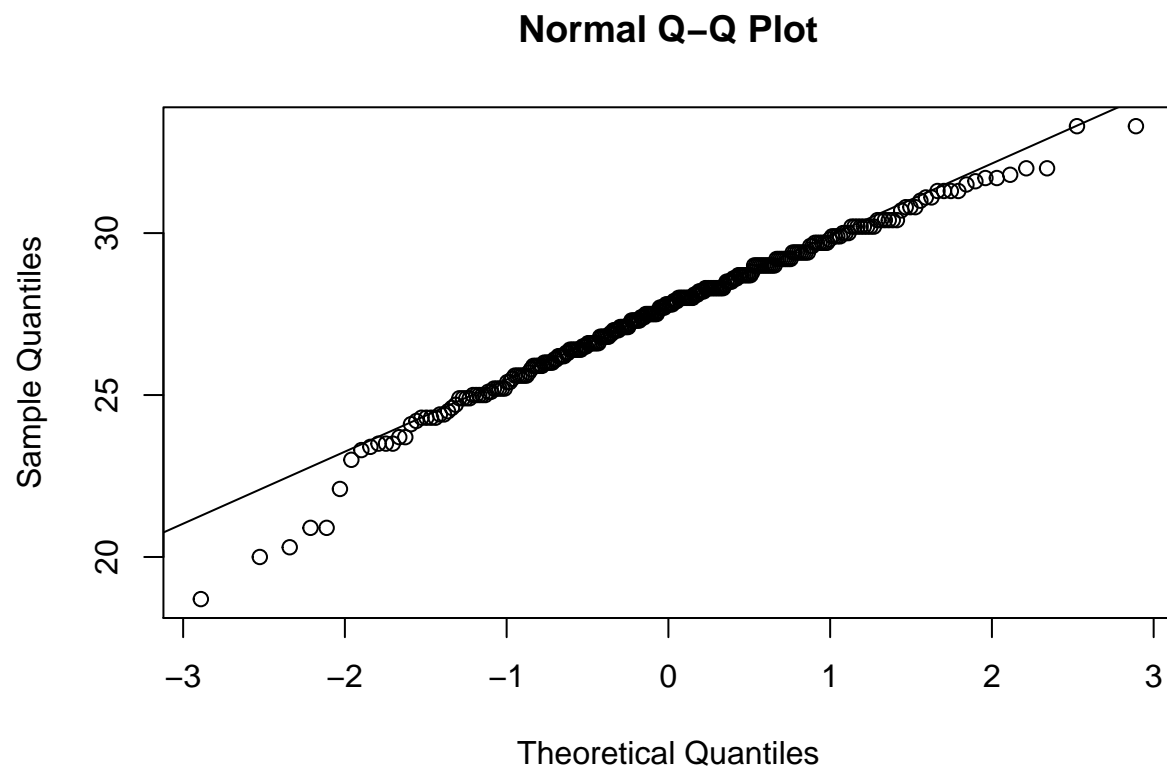
```
## [1] 1.209098e-05
```

It seems the probability of picking a woman under 20 is almost 0.

On Your Own

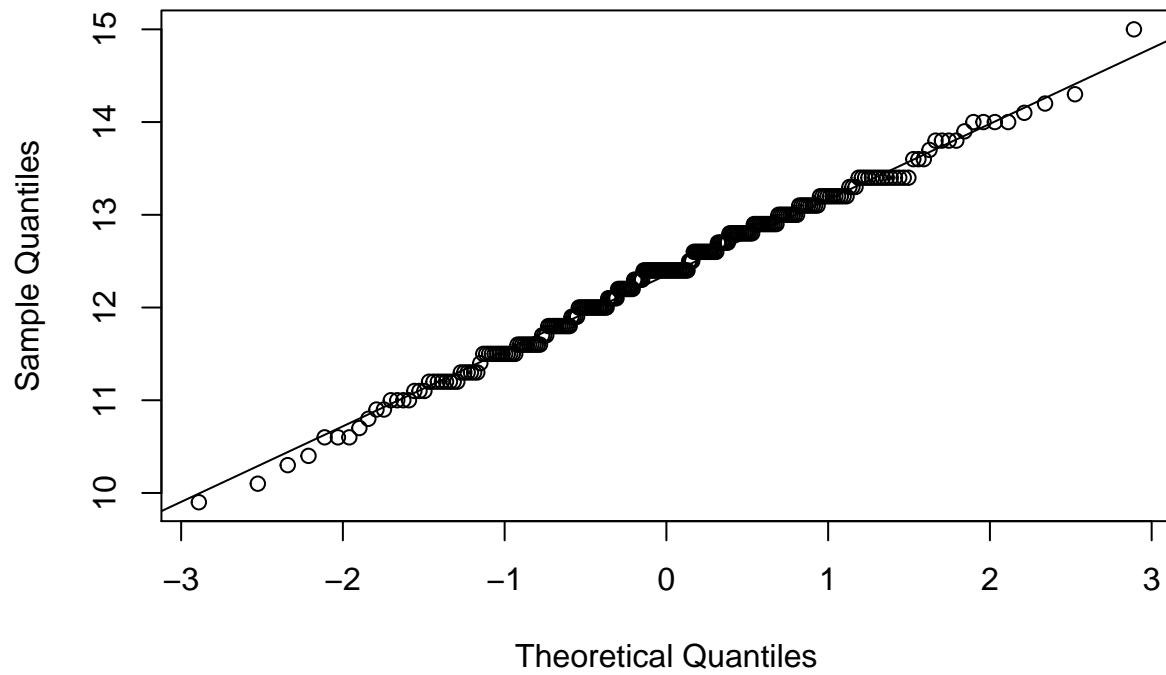
- Now let's consider some of the other variables in the body dimensions data set. Using the figures at the end of the exercises, match the histogram to its normal probability plot. All of the variables have been standardized (first subtract the mean, then divide by the standard deviation), so the units won't be of any help. If you are uncertain based on these figures, generate the plots in R to check.
 - a. The histogram for female biliac (pelvic) diameter (**bii.di**) belongs to normal probability plot letter **Normal Q-Q Plot B**.
 - b. The histogram for female elbow diameter (**elb.di**) belongs to normal probability plot letter **Normal Q-Q Plot C**.
 - c. The histogram for general age (**age**) belongs to normal probability plot letter **Normal Q-Q Plot D**.
 - d. The histogram for female chest depth (**che.de**) belongs to normal probability plot letter **Normal Q-Q Plot A**.

```
#cross validation  
qqnorm(fdims$bii.di)  
qqline(fdims$bii.di)
```



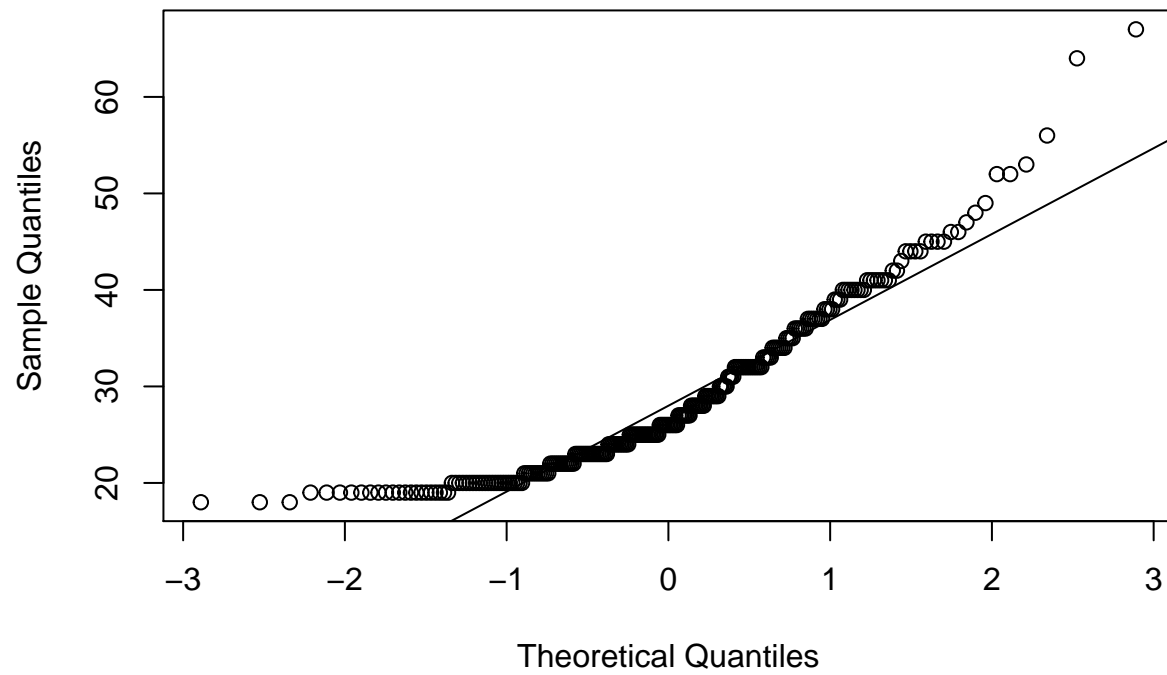
```
qqnorm(fdims$elb.di)  
qqline(fdims$elb.di)
```

Normal Q-Q Plot



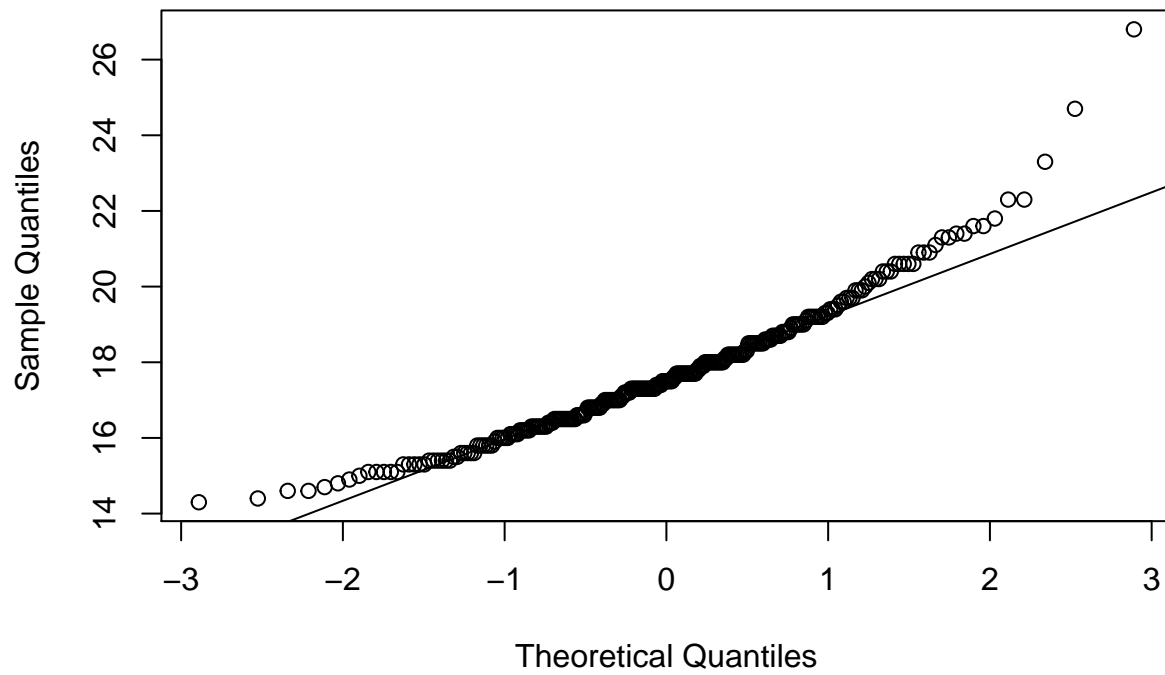
```
qqnorm(fdims$age)  
qqline(fdims$age)
```

Normal Q-Q Plot



```
qqnorm(fdims$che.de)  
qqline(fdims$che.de)
```

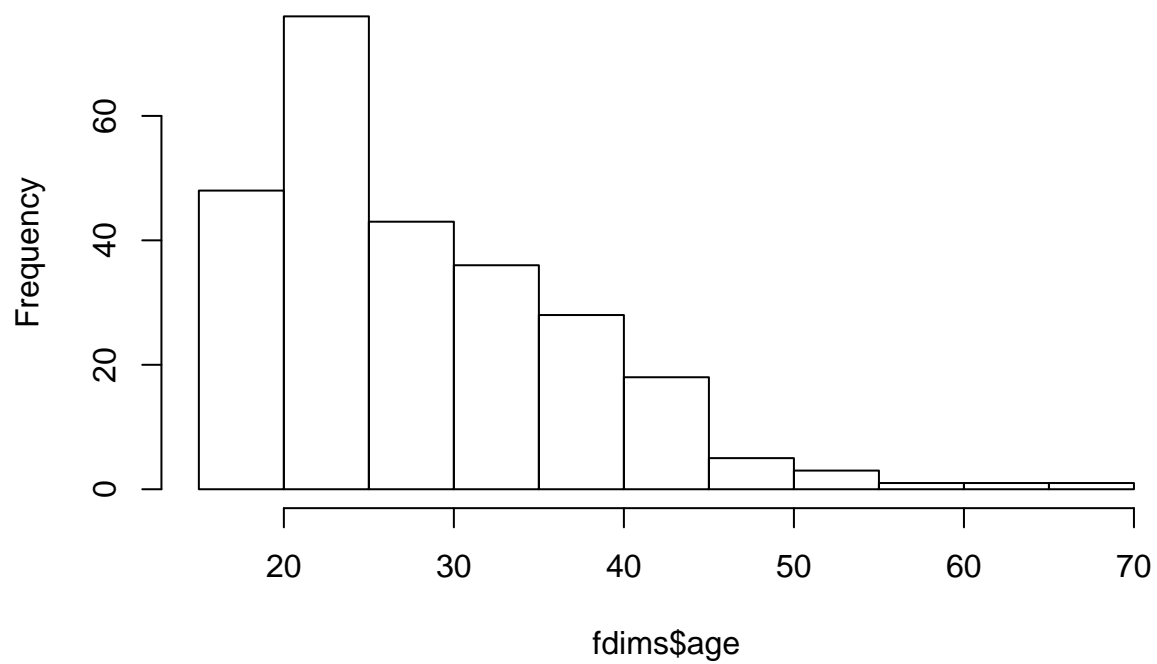

Normal Q-Q Plot



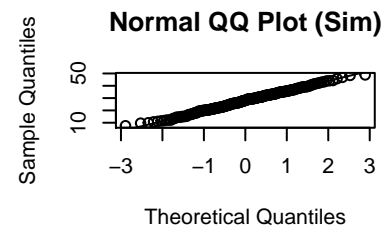
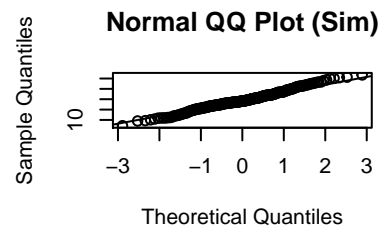
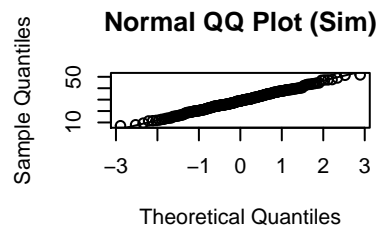
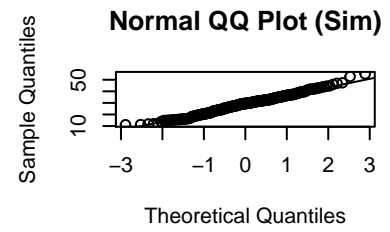
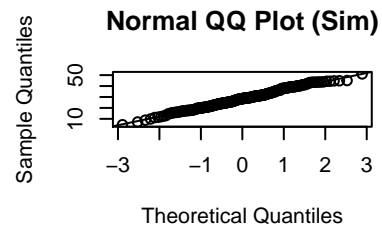
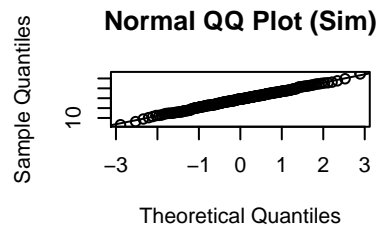
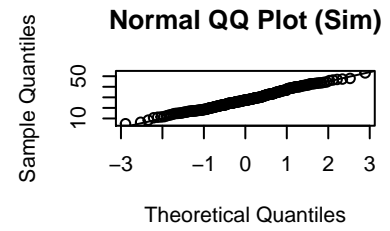
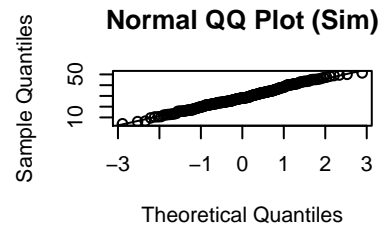
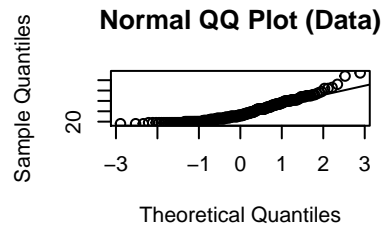
- Note that normal probability plots C and D have a slight stepwise pattern. Why do you think this is the case?

```
hist(fdims$age)
```

Histogram of fdims\$age

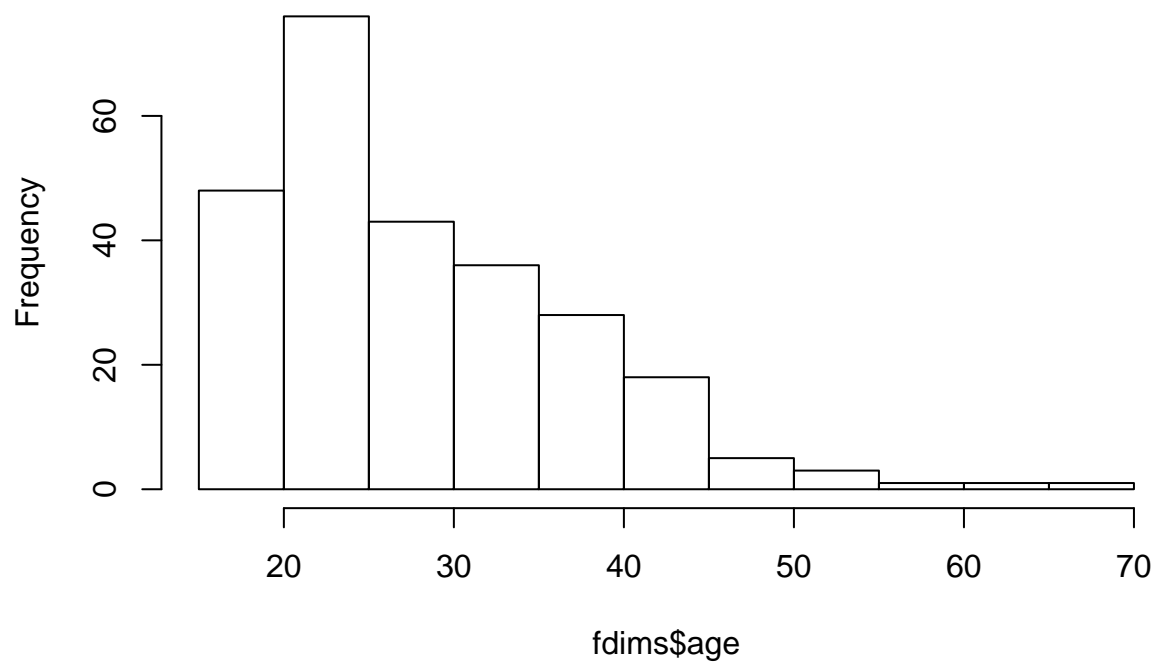


```
qqnormsim(fdims$age)
```

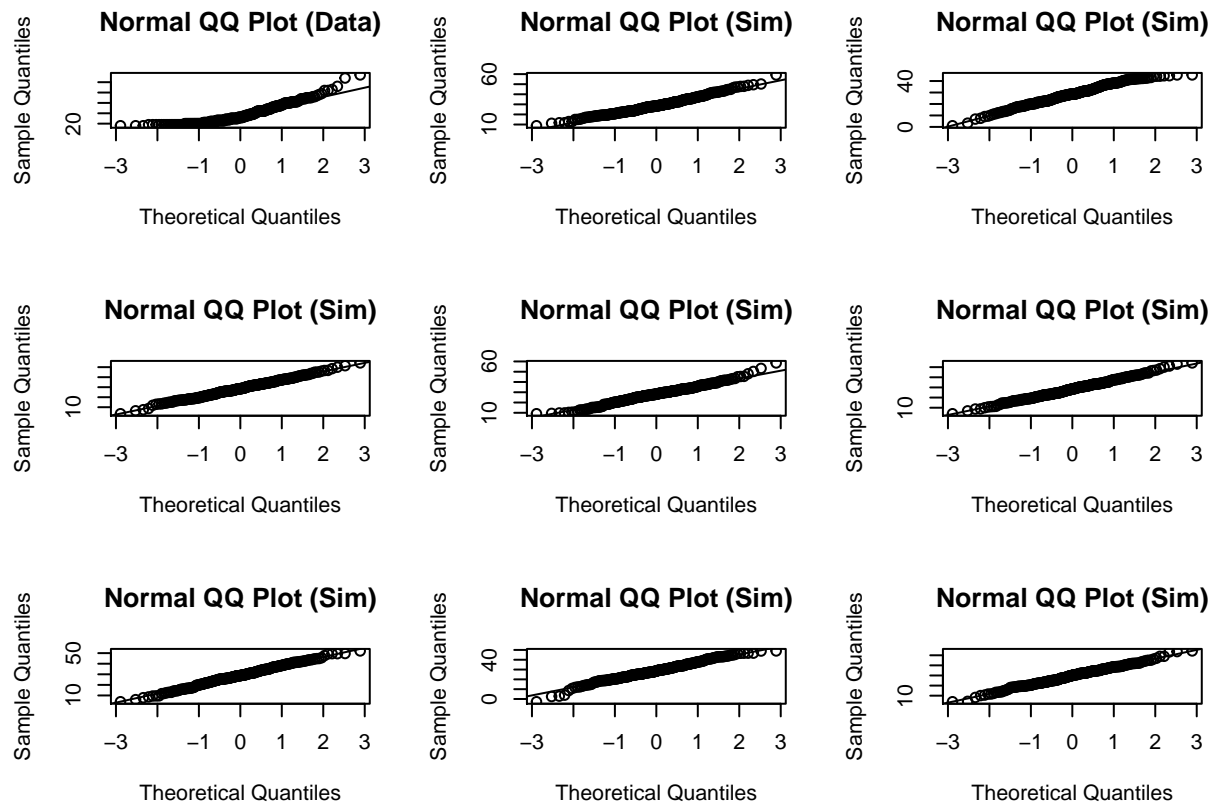


```
hist(fdims$age)
```

Histogram of fdims\$age



```
qqnormsim(fdims$age)
```



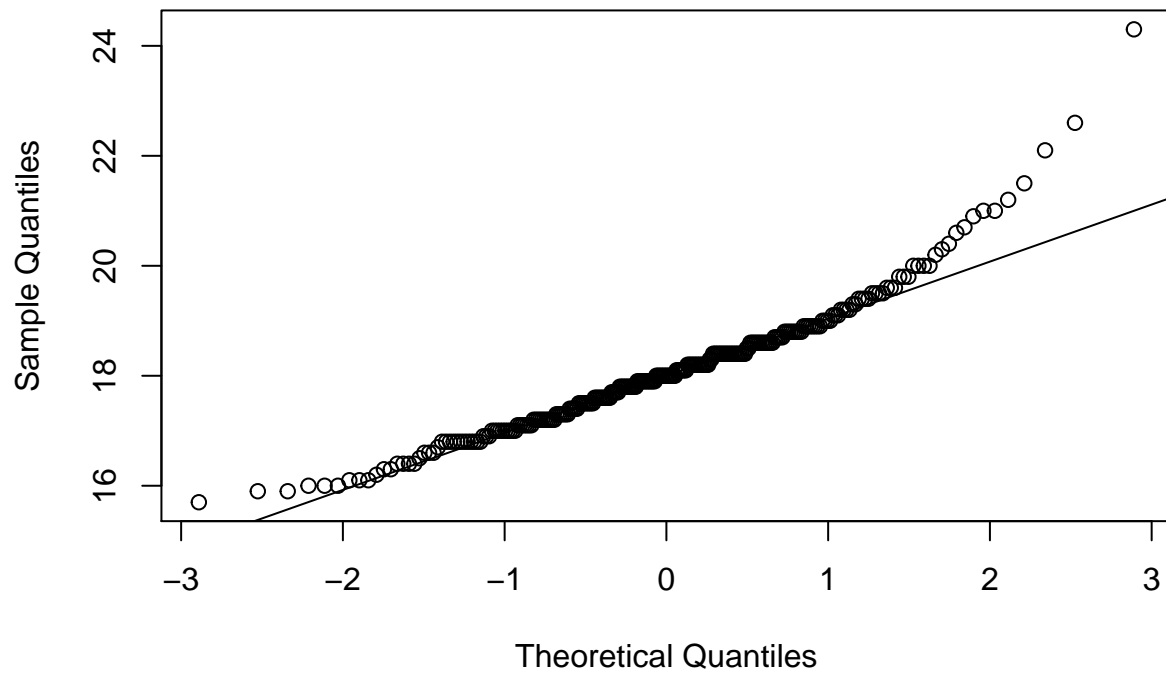
C and D has age and height. These were mentioned in rounded number. It is not continuous. So it is shown in steps.

- As you can see, normal probability plots can be used both to assess normality and visualize skewness. Make a normal probability plot for female knee diameter (`kne.di`). Based on this normal probability plot, is this variable left skewed, symmetric, or right skewed? Use a histogram to confirm your findings.

** Yes. Normal probability plots can be used both to access normality and to visualize skewness.

```
qqnorm(fdims$kne.di)
qqline(fdims$kne.di)
```

Normal Q-Q Plot



```
qqnormsim(fdims$kne.di)
```

