

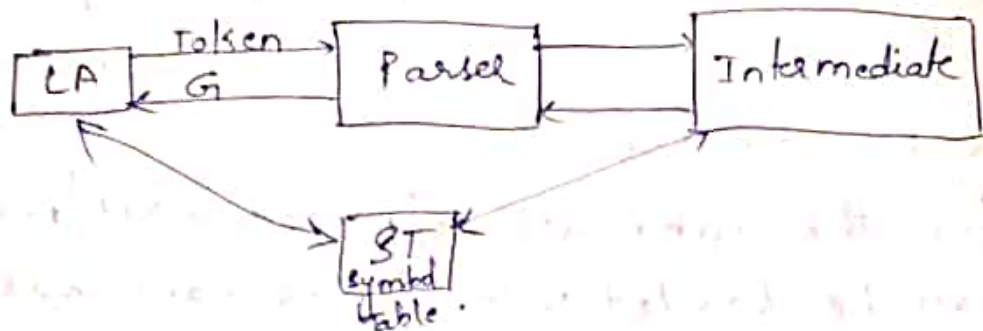
14-3-2022

UNIT - 2

Syntax Analysis.

Role of Parser :-

→ To check syntactic errors.



Any recursive structure of any programming lang can be ~~for~~ represented by Context Free grammar

CFG = (VTPS)

starting symbol.
set of Terminals.
set of NonTerminals.
Production Rules

For $A \rightarrow \alpha$ sentinal form?

Parse Tree :-

A tree which is having derivations is called a 'parse tree'.

$\alpha A \beta$ can be written as $\alpha \gamma \beta$ if there is a production rule $A \rightarrow \gamma$ in our grammar. This is called as derivation.

Derivations are of 2 types :- (i) Left Most derivation
(ii) Right Most derivation

$E \rightarrow E + E \mid E - E \mid E * E \mid E / E \mid - E$

$E \rightarrow (E)$

$E \rightarrow id$

LMD:-

$E \rightarrow E + E$

$E \rightarrow E - E + E$

$\rightarrow id - E + E$

$\rightarrow id - id + E$

$\rightarrow id - id + id$

RMD:-

$E \rightarrow E - E$

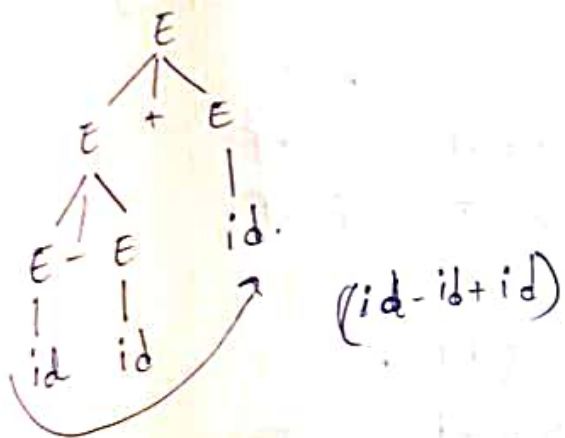
$\rightarrow E - E + E$

$\rightarrow E - E + id$

$\rightarrow E - id + id$

$\rightarrow id - id + id$

Parse Tree \rightarrow Internal nodes \rightarrow Non Terminals
Leaf nodes \rightarrow terminals



Ambiguity:- If any grammar produces more than one parse tree, that grammar is ambiguous grammar & that parse tree is ambiguous parse tree

Eg:- LMD

$E \rightarrow E + E$

$\rightarrow id + E$

$\rightarrow id + E * E$

$\rightarrow id + id * id$

LMD

$E \rightarrow E * E$

$\rightarrow E + E * E$

$\rightarrow id + id * id$

(2 Parse Trees)

LR(0) items :-

$$E \rightarrow E + T / T$$

$$T \rightarrow T * F / F$$

$$F \rightarrow F \wedge G / G$$

$$G \rightarrow (E) / id$$

15/3/2022

→ Topdown Parser cannot handle Left Recursion.

Eliminating Left Recursion :-

If any production is of the form $A \rightarrow A\alpha / \beta$, then it is said to be in LR.

→ It is eliminated by the following rule :-

$$\boxed{A \rightarrow A\alpha / \beta} \text{ is turned into } \boxed{A \rightarrow \beta A'}$$

$$\boxed{A' \rightarrow \alpha A' / \epsilon}$$

Eg:- production rules :-

$$\left. \begin{array}{l} E \rightarrow E + T / T \\ T \rightarrow T * F / F \\ F \rightarrow (E) / id \end{array} \right\} \text{ LR}$$

$$\begin{array}{l|l} A = E & A = T \\ \alpha = +T & \alpha = *F \\ \beta = T & \beta = F \end{array}$$

$$E \rightarrow E + T / T$$

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' / \epsilon$$

$$T \rightarrow T * F / F$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' / \epsilon$$

After eliminating LR, the production rules :-

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' / \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' / \epsilon$$

$$F \rightarrow (E) / id$$

If there are multiple production rules in LR,

Eg: $A \rightarrow A\alpha_1 / A\alpha_2 / A\alpha_3 \dots A\alpha_n / \beta_1 / \beta_2 \dots \beta_n$
then after elimination of LR,

$$A \rightarrow \beta_1 A' / \beta_2 A' \dots$$

$$A' \rightarrow \alpha_1 A' / \alpha_2 A' \dots / \epsilon$$

Eg: $S \rightarrow Aa/b$
 $A \rightarrow Ac / Sd / \epsilon$

$$A \rightarrow Ac / Aad / bd / \epsilon$$

$$A \rightarrow bdA' / \epsilon A'$$

$$A' \rightarrow cA' / adA' / \epsilon$$

Final production rules after eliminating LR: -

$$S \rightarrow Aa/b$$

$$A \rightarrow bdA' / A'$$

$$A' \rightarrow cA' / adA' / \epsilon$$

Elimination of Left Factoring: - Because decision taking is difficult.

If we have $A \rightarrow \alpha\beta_1 / \alpha\beta_2$

starting with same symbols in the same production rule.

The idea is that when it is not clear which of 2 alternative productions are used to expand a non-terminal A. so, we may be able to rewrite A production to take a decision.

If $A \rightarrow \alpha\beta_1 / \alpha\beta_2$ are 2 productions &

if begins with a non-empty string derived α , we do not know which A should be either $\alpha\beta_1$ or $\alpha\beta_2$. Then, rewrite it as:

$$A \rightarrow \alpha A'$$

$$A' \rightarrow \beta_1 / \beta_2$$

Eg:- $S \rightarrow iEtS / iEtSeS / a$
 $E \rightarrow b$

$$\alpha = iEtS$$

$$\beta_1 = \epsilon$$

$$\beta_2 = eS$$

$$S \rightarrow iEtS S' / a$$

$$S' \rightarrow \epsilon / eS$$

$$E \rightarrow b$$

After
elimination
Left
Factoring

Left Recursion Problems :- Left Factoring

① $A \rightarrow ABd / Aa / a$

$B \rightarrow Bc / b$

① $A \rightarrow aAB / aBc / aC$

② $S \rightarrow bSSaaS / bSSc$
 $/ bSb / a$

② $E \rightarrow E+E / E^*E / a$

③ $S \rightarrow (L) / a$
 $L \rightarrow L, S / S$

④ $S \rightarrow S_0 S_1 S / 01$

③ $S \rightarrow a / ab / abc / ac$

Left Recursions :-

$$① A \rightarrow ABd / Aa / a$$

$$A \rightarrow aA' / A'$$

$$A' \rightarrow BdA' / \epsilon / aA'$$

$$⑤ S \rightarrow (L) / a$$

$$L \rightarrow L, S / S$$

$$L \rightarrow SL'$$

$$L' \rightarrow \epsilon, SL' / \epsilon$$

$$S \rightarrow (L) / a$$

$$② E \rightarrow E, E / E * E / a$$

$$E \rightarrow \epsilon a E' / E'$$

$$E' \rightarrow +EE' / *EE' / \epsilon$$

$$④ S \rightarrow S_0 S, S / 01$$

$$S \rightarrow 01 S'$$

$$S' \rightarrow 0 S, S S' / \epsilon$$

Left Factoring :-

$$① A \rightarrow aAB / aBC / aAC$$

$$A \rightarrow aA'$$

$$A' \rightarrow AB / BC / AC$$

$$② S \rightarrow bSSa / bSSaSt / bSb / a$$

$$A \rightarrow bSA' / a$$

$$A' \rightarrow Saas / SaSb / b$$

$$A' \rightarrow SaA'' / b$$

$$A'' \rightarrow aS / Sb$$

Final Production rules:

$$A \rightarrow bSA' / a$$

$$A' \rightarrow SaA'' / b$$

$$A'' \rightarrow aS / Sb$$

$$③ S \rightarrow a / ab / abc / abcd$$

$$S \rightarrow aS'$$

$$S' \rightarrow \epsilon / b / bc / bcd$$

$$S' \rightarrow \epsilon / bS''$$

$$S'' \rightarrow \epsilon / c / cd$$

$$S'' \rightarrow \epsilon / cS'''$$

$$S''' \rightarrow \epsilon / d$$

Final rules :-

$S \rightarrow as'$

$S' \rightarrow \epsilon / bS''$

$S'' \rightarrow \epsilon / cS'''$

$S''' \rightarrow \epsilon / d$

17/3/2022

Top down Parsing

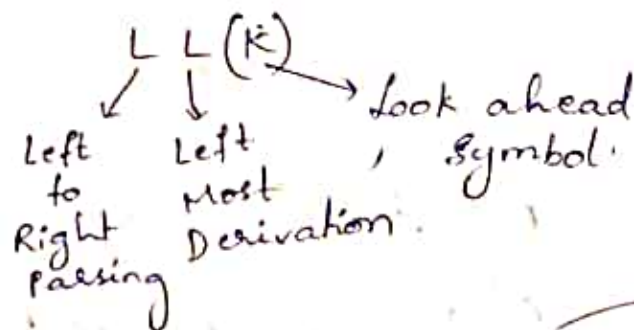
YACC is a parser generator for bottom-up Parsing

JAVACC is a parser used for top-down Parsing

Approaches:-

① Recursive Descent parsing technique:-

→ It is also called as $LL(K)$ parsing technique.



Now it is Non-Recursive Descent parsing technique.

→ Also called as $LL(1)$ parser.

used to create a Predictive Parser.

Because only 1 look ahead symbol is used.

→ To generate a parse table, we need to know FIRST and FOLLOW.

→ This parse table is used to build a parse tree.

→ There are 3 rules to find out FIRST and 3 rules to find FOLLOW.

FIRST :-

1. If X is a terminal, $FIRST(X) = \{X\}$
2. If X is a non-terminal & $X \rightarrow \epsilon$ is a production, $FIRST(X) = \{\epsilon\}$
3. If X is a non-terminal & $X \rightarrow y_1 y_2 \dots y_k$
 $FIRST(X) = FIRST(y_1)$
if $y_1 \rightarrow \epsilon$, $FIRST(X) = FIRST(y_2)$
 $y_2 \rightarrow \epsilon$, $FIRST(X) = FIRST(y_3)$
 \vdots
 $y_k \rightarrow \epsilon$, $FIRST(X) = \{\epsilon\}$.

Q1) Find out the $FIRST(S)$, $FIRST(A)$, $FIRST(B)$, $FIRST(D)$, $FIRST(E)$.

$S \rightarrow ABCDE$

$A \rightarrow a/\epsilon$

$B \rightarrow b/\epsilon$

$C \rightarrow c$

$D \rightarrow d/\epsilon$

$E \rightarrow e/\epsilon$

$FIRST(S) = \{a, b, c\}$

$FIRST(A) = \{a, \epsilon\}$

$FIRST(B) = \{b, \epsilon\}$

$FIRST(C) = \{c\}$

$FIRST(D) = \{d, \epsilon\}$

$FIRST(E) = \{e, \epsilon\}$

$$② S \rightarrow ACB/CbB/Ba.$$

$$A \rightarrow da/BC$$

$$B \rightarrow g/\epsilon$$

$$C \rightarrow h/\epsilon$$

$$\text{FIRST}(S) = \{d, g, h, \epsilon, b, a\}$$

$$\text{FIRST}(A) = \{d, g, h, \epsilon\}$$

$$\text{FIRST}(B) = \{g, \epsilon\}$$

$$\text{FIRST}(C) = \{h, \epsilon\}$$

FOLLOW :-

1. $\text{FOLLOW}(S) = \{\$ \}$, If S is start symbol

2. If $A \rightarrow \alpha B \beta$, then $\text{FOLLOW}(B) = \text{FIRST}(\beta)$ except ϵ

3. If $A \rightarrow \alpha \beta$ or $A \rightarrow \alpha B \beta$, when

$\text{FIRST}(\beta)$ contains ϵ

$\text{FOLLOW}(B) = \text{FOLLOW}(A)$

Q1) $S \rightarrow ABCDE$

$A \rightarrow a/\epsilon$

$B \rightarrow b/\epsilon$

$C \rightarrow c$

$D \rightarrow d/\epsilon$

$E \rightarrow e/\epsilon$

$\text{Follow}(S) = \{\$, \}$

$\text{Follow}(A) = \{b, c\}$

$\text{Follow}(B) = \{c\}$

$\text{Follow}(C) = \{d, e, \$\}$

$\text{Follow}(D) = \{e, \$\}$

$\text{Follow}(E) = \{\$, \}$

$\text{FIRST}(S) = \{a, b, c\}$

$\text{FIRST}(A) = \{a, \epsilon\}$

$\text{FIRST}(B) = \{b, \epsilon\}$

$\text{FIRST}(C) = \{c\}$

$\text{FIRST}(D) = \{d, \epsilon\}$

$\text{FIRST}(E) = \{e, \epsilon\}$

Q2) $S \rightarrow ACB \mid cbB \mid Ba$
 $A \rightarrow da \mid Bc$
 $B \rightarrow g \mid \epsilon$
 $C \rightarrow h \mid \epsilon$

$\text{Follow}(S) = \{\$, \}$

$\text{Follow}(A) = \{h, g, \$, b\}$

$\text{Follow}(C) = \{g, \$, b\}$

$\text{Follow}(B) = \{a, b, \$, g\}$

22/3/2022

* Steps for constructing predictive parser :-

1. Eliminate Left Recursion.
2. Eliminate Left Factoring.
3. Find FIRST & FOLLOW
4. Construct predictive parse table / parse table
5. Parse the i/p statement.

$$P) \quad E \rightarrow E + T / T$$

$$T \rightarrow T * F / F$$

$$F \rightarrow (E) / id$$

① eliminate LR

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' / \epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' / \epsilon$$

$$F \rightarrow (E) / id$$

② eliminate LF

No Left Factoring

③

$$FIRST(E) = \{id, (\}$$

$$FIRST(E') = \{+, \epsilon\}$$

$$FIRST(T) = \{id, (\}$$

$$FIRST(T') = \{*, \epsilon\}$$

$$FIRST(F) = \{ (, id \}$$

$$Follow(E) = \{ \$,) \}$$

$$Follow(E') = \{ \$,) \}$$

$$Follow(T) = \{ +, \$,) \}$$

$$Follow(T') = \{ *, \$,) \}$$

$$Follow(F) = \{ *, +, \$,) \}$$

? WTF

24/3/2022

Parse table using FIRST and FOLLOW:-

Rows - Non-Terminals
columns - Terminals

	+	*	()	id	\$
E			$E \rightarrow TE'$		$E \rightarrow TE'$	
E'	$E' \rightarrow TE'$			$E' \rightarrow \epsilon$		$E' \rightarrow \epsilon$
T			$T \rightarrow FT'$		$T \rightarrow FT'$	
T'	$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$		$T' \rightarrow \epsilon$
F			$F \rightarrow (\epsilon)$		$F \rightarrow id$	

Rules to fill the parse table:-

~~1. If the production does not contain ϵ , then find first(-~~

① $M[A, a] = A \rightarrow \alpha$
a is FIRST(α)

② $M[A, b] = A \rightarrow \alpha$

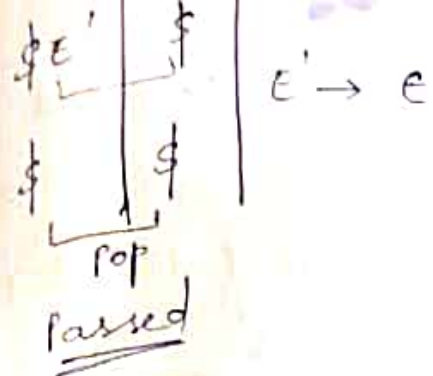
If ϵ is in FIRST(α), then consider Follow

Parsing any input string:-

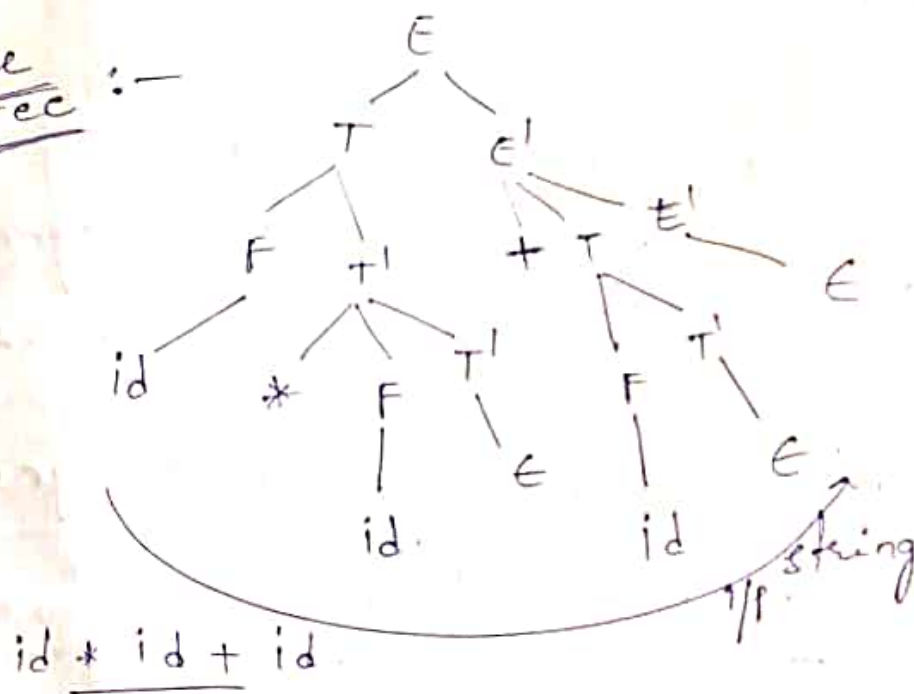
$$W = id * id + id$$

Here we use the concept of stack.

stack	i/p	o/p
\$E	id * id + id \$	
\$E'T	id * id + id \$	$E \rightarrow TE'$
\$E'T'F	id * id + id \$	$T \rightarrow FT'$
\$E'T'id	id * id + id \$	$F \rightarrow id$
\$E'T'	* id + id \$	$T' \rightarrow *FT'$
\$E'T'F*	* id + id \$	
\$E'T'F	id + id \$	$F \rightarrow id$
\$E'T'id	id + id \$	$F \rightarrow id$
\$E'T'	+ id \$	
\$E'	+ id \$	$T' \rightarrow E$
\$E'T+	+ id \$	$E' \rightarrow +TE'$
\$E'T	id \$	
\$E'T'F	id \$	$T \rightarrow FT'$
\$E'T'id	id \$	$F \rightarrow id$
\$E'T'	\$	
\$E'	\$	$T' \rightarrow E$



Parse Tree :-



31/3/2022

Error recovery in Predictive parsing :-
when errors occur :-

1. when multiple entries in parsing table create an error
2. when top of the stack doesn't match i/p
3. when top of stack matches, but i/p is empty in parsing table

Error Recovery :- (Panic Mode)

Panic Mode Rules :-

Place all symbols in Follow(A) into sync

1. If parser looks ^{up} an entry, $M[A, a]$ and finds it blank, then the i/p symbol a is

skipped.

2. If the entry is sync bit, then non-terminal on top of stack is popped.
3. If the token not matches the top of the stack, then pop the token in the stack.

	+	*	()	id	\$
E			$E \rightarrow TE'$	sync	$E \rightarrow TE'$	sync
E'	$E' \rightarrow TE'$			$E' \rightarrow E$		$E' \rightarrow E$
T	sync		$T \rightarrow FT'$	sync	$T \rightarrow FT'$	sync
T'	$T' \rightarrow E$	$T' \rightarrow FT'$		$T' \rightarrow E$		$T' \rightarrow E$
F	sync	sync	$F \rightarrow (E)$	sync	$F \rightarrow id$	sync

I/P =) id * + id \$

stack	i/p	o/p
\$E	id * + id \$	sync,
\$E'T	id * + id \$	$E \rightarrow TE'$
\$E'T'F	id * + id \$	$T \rightarrow FT'$
\$E'T'id	id * + id \$	$F \rightarrow id$
\$E'T'	* + id \$	
\$E'T'F*	* + id \$	$T \rightarrow * F$ <u>error</u>
\$E'T'F	+ id \$	
\$E'T'	+ id \$	$T' \rightarrow E$

\$ E' .	+ id \$
\$ E' T +	+ id \$
\$ E' T	id \$
\$ E' T' F	id \$
\$ E' T' id .	id \$
\$ E' T'	\$
\$	\$

$E' \rightarrow F T E'$

$T \rightarrow F T'$