Part A

Aim:

- Design algorithms for following problems.
 Euclid Algorithm, Matrix Multiplication, Matrix addition
- 2. Find time and space complexity of algorithms.
- 3. Implement the algorithms in any programming language.

Prerequisite: Any programming language

Outcome: Algorithms and their implementation

Theory:

Procedure:

- 1. Design algorithm and find complexity
- 2. Implement algorithms in any programming language.
- 3. Paste output

Practice Exercise:

S.no	Query statement
1	Design and analysis Euclid algorithm for finding GCD of two numbers.
2	Design and analysis algorithm for matrix addition.
3	Design and analysis algorithm for matrix multiplication.

Instructions:

end

- 1. Design, analysis and implement the algorithms.
- 2. Paste the snapshot of the output in input & output section.

Part B

1)Design and analysis Euclid algorithm for finding GCD of two numbers.

```
ALGORITHM: Euclid algorithm for finding gcd of 2 numbers a,b
INPUT: Two integers a,b
OUTPUT: Largest integer that divides both the input numbers a,b (i.e gcd of a,b)
begin
gcd_euclid(a,b)
begin while(b%a!=0)
rem=b%a
b=a
a=rem
end while
return a
```

Amortized Analysis: (How much resource(time and space) our algorithm takes to execute)

Time Analysis:

In at most O(log a)+O(log b) steps, this will be reduced to the simple cases. Which yield an O(log n) algorithm, where n is the lower limit of a and b.

Time complexity of the above algorithm would in order of O(log(min(a,b))).

Space Analysis:

No of variables used here are 3, i.e. a,b,rem where each variable takes a space of O(1) (so, 1+1+1=3 which is a constant).

Therefore, space complexity will become O(1)

```
Code:
```

```
import java.util.*;
class euclid{
    public static int gcd_euclid(int a,int b)
    {
        int rem;
        while(b%a!=0)
        {
            rem=b%a;
            b=a;
            a=rem;
        }
        return a;
    }
    public static void main(String args[])
    {
        int a,b;
        Scanner sc=new Scanner(System.in);
        a=sc.nextInt();
        b=sc.nextInt();
        sc.close();
        System.out.println(gcd_euclid(a,b)+" is the gcd of "+a+" and "+b);
    }
}
```

Input and Output:

```
Options

12
21
3 is the gcd of 12 and 21
```

2) Design and analysis algorithm for matrix addition.

```
ALGORITHM: Addition of 2 matrices
Input: 2 matrices arr1 and arr2 of order n1*m1 and n2*m2
Output: Equivalent sum of matrices obtained of order n1*m1
     begin
     Matrix addition(arr1[],arr2[])
        define addm matrix as (n1 * m1)
        if row size and column size of arr1==arr2:
             for(i=0;i<n1;i++)
                 for(j=0;j<m1;j++)
                     addm[i][j]=arr1[i][j]+arr2[i][j];
                     System.out.print(addm[i][j]+" ");
                 System.out.println();
             return ;
        else
            System.out.println("Can't add the 2 matrices");
            return ;
     end
Amortized Analysis: (How much resource(time and space ) our algorithm takes to execute )
Time analysis:
Here in this algorithm we have 2 for loops where each loop if of O(n1),O(m1)
and the loops are nested. So the time complexity becomes O(n1*m1) . For a
square matrix where n1=m1 the order becomes O(n1^2) \Rightarrow O(n^2)
Space Analysis:
Here in this algorithm we used 4 variables(n1,m1,i,j) 3 matrices data
structures of order n1*m1 n1*m1 and n1*m2 . So the space complexity will be
(n1*m1) + (n1*m1) + (n1*m1) + 4 i.e. O((n1*m1) + (n1*m1) + (n1*m1) + 4) which
is equal to O((n1*m1) + (n1*m1) + (n1*m1)).
If n1=m1 then space complexity will be in O(n^2)
Code:
import java.util.*;
class Matrix add{
    public static void main(String args[])
        int n1,m1,n2,m2,i,j;
        Scanner sc=new Scanner(System.in);
        System.out.println("Enter row size and column size of 2 matrices");
        n1=sc.nextInt();
        m1=sc.nextInt();
        n2=sc.nextInt();
        m2=sc.nextInt();
```

```
if(n1!=n2 && m1!=m2){
             System.out.println("Can't add the 2 matrices");
             return ;
        }
        int arr1[][]=new int[n1][m1];
        int arr2[][]=new int[n2][m2];
        int addm[][]=new int[n1][n2];
        System.out.println("Enter elements of matrix 1");
        for(i=0;i<n1;i++){</pre>
             {
                 for(j=0;j<m1;j++){</pre>
                     arr1[i][j]=sc.nextInt();
                 }
             }
        }
        System.out.println("Enter elements of matrix 2");
        for(i=0;i<n1;i++){</pre>
             {
                 for(j=0;j<m1;j++){</pre>
                     arr2[i][j]=sc.nextInt();
                 }
             }
        }
        sc.close();
        System.out.println("Sum of both the matrices is ");
        for(i=0;i<n1;i++){</pre>
            {
                 for(j=0;j<m1;j++){</pre>
                     addm[i][j]=arr1[i][j]+arr2[i][j];
                 System.out.print(addm[i][j]+" ");
                 System.out.println();
            }
        }
    }
}
```

Input & Output:

```
Enter row size and column size of 2 matrices
3 3
3 Tenter elements of matrix 1
1 2 3
4 5 6
7 8 9
Enter elements of matrix 2
9 8 7
6 5 4
3 2 1
Sum of both the matrices is
10 10 10
10 10 10
10 10 10
```

3) Design and analysis algorithm for matrix multiplication.

Algorithm: Multiplication of matrices

Input: 2 matrices arr1 and arr2 of order n1*m1 and n2*m2 **Output:** Equivalent product of matrices obtained of order n1*m2

```
begin
Matrix multiplication( arr1[ ],arr2[ ])
   define addm matrix as (n1 * m2)
   if m1==n2:
        for(i=0;i<n1;i++)</pre>
            for(j=0;j<m2;j++)
                mul[i][j]=0;
                for(k=0;k<m1;k++)
                     mul[i][j]+=arr1[i][k]*arr2[k][j];
                System.out.print(mul[i][j]+" ");
            System.out.println();
        return ;
   else
       System.out.println("Can't multiply the 2 matrices");
       return ;
end
```

Amortized Analysis: (How much resource(time and space) our algorithm takes to execute)

Time analysis:

```
Here in this algorithm we have 3 for loops where each loop if of O(n1),O(m2),O(m1) and the loops are nested. So the time complexity becomes O(n1*m2*m1). For a square matrix where n1=m2=m1 the order becomes O(n1^3) = 3
```

```
0(n^3)
Space Analysis:
Here in this algorithm we used 7 variables(n1,m1,n2,m2,i,j,k) 3 matrices data
structures of order n1*m1 n2*m2 and n1*m2 . So the space complexity will be
(n1*m1) + (n2*m2) + (n1*m2) + 7 i.e. O((n1*m1) + (n2*m2) + (n1*m2) + 6) which
is equal to O((n1*m1) + (n2*m2) + (n1*m2)).
If n1=n2=m2 then space complexity will be in O(n^2)
CODE:
import java.util.*;
class Matrix mul{
    public static void main(String args[])
        int n1,m1,n2,m2,i,j,k;
        Scanner sc=new Scanner(System.in);
        System.out.println("Enter row size and column size of 2 matrices");
        n1=sc.nextInt();
        m1=sc.nextInt();
        n2=sc.nextInt();
        m2=sc.nextInt();
        if(m1!=n2){
            System.out.println("Can't multiply the 2 matrices");
            return ;
        }
        int arr1[][]=new int[n1][m1];
        int arr2[][]=new int[n2][m2];
        int mul[][]=new int[n1][n2];
        System.out.println("Enter elements of matrix 1");
        for(i=0;i<n1;i++){</pre>
            {
                for(j=0;j<m1;j++){</pre>
                    arr1[i][j]=sc.nextInt();
                }
            }
        }
        System.out.println("Enter elements of matrix 2");
        for(i=0;i<n2;i++){</pre>
            {
                for(j=0;j<m2;j++){</pre>
                    arr2[i][j]=sc.nextInt();
                }
            }
        }
```

```
sc.close();
        System.out.println("product of both the matrices is ");
        for(i=0;i<n1;i++){</pre>
             {
                 for(j=0;j<m2;j++){</pre>
                      mul[i][j]=0;
                      for(k=0;k<m1;k++)</pre>
                      {
                          mul[i][j]+=arr1[i][k]*arr2[k][j];
                      }
                 System.out.print(mul[i][j]+" ");
                 System.out.println();
             }
        }
    }
}
```

Input and output:

```
Enter row size and column size of 2 matrices
2 3
3 2
Enter elements of matrix 1
1 2 3
4 5 6
Enter elements of matrix 2
1 2
3 4
5 6
product of both the matrices is
22 28
49 64
```

Observation & Learning:

Learned about Amortized Analysis of an algorithm and found the time, space complexities of Euclid Algorithm, Matrix Multiplication, Matrix addition.

Implemented the algorithms in java programming language.

Conclusion:

Wrote algorithms for the 3 problem statements and executed them in Java programming language successfully

Questions:

- 1. What is the goodness criteria for algorithms?
- 2. How will two algorithms that solve the same problem be compared?

Answers:

- 1. Goodness of an algorithm is determined by:
 - **a.** Characteristics of that algorithm (Should have 0/more inputs and at least 1 output, finiteness, definiteness, effectiveness)
 - **b.** Growth of the algorithm
 - **c.** Time and space complexity of algorithm (The one with less time and space complexity is good)
- 2. They can be compared by finding time and space complexities of algorithms.