

SL Unit 4 – Problem Solving

Quiz 2

Question 1

Objectives:	4.1.18	Exam Reference:	May-14 11
-------------	--------	-----------------	-----------

Explain why an object is an example of abstraction.

[2]

Award up to [2 marks max].

An object hides the details;

Yet preserves the functionality;

OR

Objects combine abstractions of data and code;

While hiding away implementation of details;

Question 2

Objectives:	4.2.5	Exam Reference:	Nov-15 6
-------------	-------	-----------------	----------

A sub-program *all_even()* accepts a positive integer *N* and outputs *true* if all digits of *N* are even, otherwise it outputs *false*. For example, *all_even(246)* outputs *true* and *all_even(256)* outputs *false*.

The following algorithm is constructed for the sub-program *all_even(N)*.

```
EVEN = true
loop while (N > 0) and (EVEN = true)
    if (N mod 10) mod 2 = 1 then
        EVEN = false
    end if
end loop
output EVEN
```

(a) Explain why this algorithm does not obtain the correct result.

[2]

Award up to [2 max].

The value of *N* is never changed;

So the logical expression in the while loop always evaluates to true;

And loop repeats an infinite number of times;

- (b) Outline what should be changed in the algorithm to obtain the correct result. [3]

Statement $N = N \text{ div } 10$;
Should be written within the while loop;
After the if statement;

Question 3

Objectives:	4.2.1, 4.2.3, 4.2.6	Exam Reference:	Nov-15 9
-------------	---------------------	-----------------	----------

1. A candy company manufactures 20 different kinds of candy, each identified by a product ID. An array, *Product_ID*, is used to store the product IDs, and another array, *Unit_Price*, is used to store the price per unit of each type of candy. The unit price of the product identified by *Product_ID[N]* is equal to *Unit_Price[N]* for any index *N*.

Product_ID		Unit_Price
Mints-1A	[0]	15.20
Choco-1B	[1]	18.10
Jelly-1Q	[2]	16.30
	...	
Choco-2A	[19]	11.90

- (a) State the price of the candy identified by *Product_ID[2]*. [1]

16.30;

- (b) Explain the steps that would be needed in an algorithm to calculate the average unit price. [3]

Set a variable (sum) to zero;
Loop through the array *Unit_Price*;
Add each array element to variable sum;
Divide sum by 20;

- (c) Construct the algorithm that will output the price of a candy after its product ID is entered by the user. The algorithm should output an appropriate message if the product ID entered does not appear in the array *Product_ID*.

[6]

Award marks as follows up to [6].
Award [1] for the input.
Award [1] for introducing the Boolean variable.
Award [2] for the correct loop, [1] for a minor error.
Award [1] for the correct comparison in if statement.
Award [1] for correct assignment.
Award [1] for the output of the price after the loop.
Award [1] for 'does not appear' message.

Example answer:

```
NUM = ENTERED ID
K = 0
FOUND = false
loop while K<20 and NOT FOUND
  if NUM = Product_ID[K] then
    FOUND = true
    PRICE = Unit_Price[K]
  end if
  K=K+1
end loop
if FOUND then
  output "The price is ", PRICE
else
  output NUM, " does not appear on the list of product numbers"
end if
```

The company maintains two warehouses each of which stocks a selection of the 20 types of candy indicated above.

The first warehouse stocks 15 items and their IDs are stored in an array, *One*. The second warehouse stocks 10 items and their IDs are stored in an array, *Two*.

All product IDs common to both warehouses will be placed in an array, *Three*.

- (d) (i) State the maximum number of common product IDs which can be placed in *Three*.

[1]

- (ii) Construct the algorithm that will place all product IDs common to both warehouses in *Three*.

[4]

Award marks as follows up to [4].

Award [1] for variable(Z) that keeps track of current position in array Three.

Award [1] for the correct outer loop.

Award [1] for the correct inner loop.

Award [1] for the condition.

Award [1] for the correct assignment.

Example answer:

```
Z = 0
```

```
loop K from 0 to 14
```

```
  loop J from 0 to 9
```

```
    if One[K] = Two[J] then
```

```
      Three[Z] = One[K]
```

```
      Z=Z+1
```

```
    end if
```

```
  end loop
```

```
end loop
```

Question4

Objectives:	4.2.1, 4.2.6, 4.2.7	Exam Reference:	Nov-17 13
-------------	---------------------	-----------------	-----------

A character array *S* holds the word “PSEUDOCODE”.

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
P	S	E	U	D	O	C	O	D	E

- (a) State the index of character “U” in the array *S*.

3

- (b) Consider the following algorithm. The function *len()* returns the number of characters in an array (for example, *len(S)* is 10).

```

K = 0
CL = 0
loop while K < len(S)
    if S[K] = "E" then
        CL = CL + 1
    end if
    K = K + 1
end loop
output CL

```

For this algorithm, complete the following trace table.

[4]

K	CL	K < len(S)	S[K] = "E"	output
0	0	TRUE	FALSE	...
...

Award [1] for each correct column, other than column K.

K	CL	K < len(S)	S[K] = "E"	output
0	0	TRUE	FALSE	
1	"	"	"	
2	1	"	TRUE	
3	"	"	FALSE	
4	"	"	"	
5	"	"	"	
6	"	"	"	
7	"	"	"	
8	"	"	"	
9	2	"	TRUE	
10	"	FALSE		2

Note: The symbol " appearing in cells above means that the value in that cell is the same as the one in the cell just above it; unfilled cells means that no value must be present.

Remark: Accept drawings of tables where the values of the column CL are shifted downwards of one cell only, therefore showing the first value 2 when K = 10. Do not propagate by FT to the other columns, they are independent from the way CL has been filled.)

A simple method of encoding a message is to use substitutions to produce a cryptogram.

Given a positive integer N and the array *UPCASELETTERS* containing letters in alphabetical order, a new array *SUBSTITUTE* is created by shifting the entire contents of *UPCASELETTERS* to the left, N times. As an element moves off the left of the array, it moves back into the right side of the array.

For example, given the array *UPCASELETTERS*:

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]	[10]	[11]	[12]	[13]	[14]	[15]	[16]	[17]	[18]	[19]	[20]	[21]	[22]	[23]	[24]	[25]
A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z

When $N = 5$ the array *SUBSTITUTE* will be:

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]	[10]	[11]	[12]	[13]	[14]	[15]	[16]	[17]	[18]	[19]	[20]	[21]	[22]	[23]	[24]	[25]
F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E

- (c) Construct an algorithm which creates the array *SUBSTITUTE*. You may assume that a positive integer N and array *UPCASELETTERS* are given.

[5]

Example answer 1

Award marks as follows up to [5 max].

Award [1] for correct boundaries in first for-loop.

*Award [1] for correct assignment of array *SUBSTITUTE* in first loop.*

Award [1] for correct boundaries in second for-loop.

*Award [1] for correct assignment of array *SUBSTITUTE* in second loop.*

*Award [1] for incrementing *IND* in both loops.*

```

IND = 0
loop for K from N to len(UPCASELETTERS)-1
    // accept 'K from 0 to 25'
    SUBSTITUTE[IND] = UPCASELETTERS[K]
    IND = IND+1
end loop
loop for K from 0 to N-1
    SUBSTITUTE[IND] = UPCASELETTERS[K]
    IND = IND+1
end loop

```

This encoding method produces a cryptogram of a sentence by replacing each uppercase letter of the sentence with its substitute. Other characters in the sentence are not changed.

For example, using the arrays shown on page 6:

Input (sentence): ARS LONGA, VITA BREVIS.

Output (cryptogram): FWX QTSLF, ANYF GWJANX.

The following algorithm fragment inputs the characters, one by one, from the input sentence, and outputs its cryptogram using the method *encode()*.

```
loop while NOT end-of-input-sentence
    CH = input()
    CRYPTEDCH= encode(CH, UPCASELETTERS, SUBSTITUTE)
    output CRYPTEDCH
end loop
```

The method *encode()* accepts a character *CH* and two arrays *UPCASELETTERS* and *SUBSTITUTE*, as defined above, and returns the corresponding character *CRYPTEDCH* of the character *CH*.

(d) Explain the steps to construct an algorithm for the method *encode()*.

[5]

Award up to [5 max].

Search the array *UPCASELETTERS*;

Using a linear/sequential or binary search;

Search for the position/index of character *CH*;

If *CH* is found in *UPCASELETTER*;

Return the value stored in the array *SUBSTITUTE* at this position/index;

Otherwise return *CH*;