

## 305 Lecture 17 - Building Complicated Truth Tables

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July 13, 2020

# Plan

This lecture is about how to build more complicated truth tables than we have looked at so far.

## Associated Reading

No new reading; we're just going to do a more complicated example than the book goes over.

## The Example

We are going to work out the truth table for this sentence:

$$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$$

## How Many Rows

- How many rows should there be in the truth table?

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- How many rows should there be in the truth table?
- There are three (3) atomic sentences, so there should be  $2^3 = 8$  rows.

## Laying Out the Rows

- The convention for these is a bit odd.
- Here's one way to think about it.
- For the left-most column you fill the first half of the rows with  $\mathbb{T}$  and then the second half of the rows with  $\mathbb{F}$ .

## First Column

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$
T			
T			
T			
T			
F			
F			
F			
F			



## Second Column

- Then the second column has one quarter  $\mathbb{T}$ , followed by one quarter  $\mathbb{F}$ , followed by one quarter  $\mathbb{T}$ , followed by one quarter  $\mathbb{F}$ .
- In this case that means we alternate every two rows.

## Second Column

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$
T	T		
T	T		
T	F		
T	F		
F	T		
F	T		
F	F		
F	F		

## Third Column

- From now on you do half as many rows between changes.
- In this table we did 4 rows with one value then 4 of another for column 1, 2 with one value then 2 with another for column 2, and now alternate every row for column 3.
- It's helpful to know the full algorithm in case you ever have to do this with 5 or more variables.
- But I won't do that in this course.

## Third Column

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$
T	T	T	
T	T	F	
T	F	T	
T	F	F	
F	T	T	
F	T	F	
F	F	T	
F	F	F	

## Parsing the Sentence

Now we need to go back to our sentence.

$$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$$

What is its **main connective**?

## Parsing the Sentence

Now we need to go back to our sentence.

$$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$$

What is its **main connective**?

- It's the first  $\rightarrow$ . The sentence is of the form  $D \rightarrow E$ , where  $D$  is  $(A \vee \neg B)$  and  $E$  is  $(B \rightarrow (A \wedge C))$

So eventually, we will have the truth value for the whole sentence under the first  $\rightarrow$ .

- But that's some distance away.
- While that's where we want to get to, we have to build from the inside out.
- The first thing to do is to repeat the values for the atomic sentences.

# Atomic Replicator

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$			
T	T	T	T	T	T	T
T	T	F	T	T	T	F
T	F	T	T	F	F	T
T	F	F	T	F	F	F
F	T	T	F	T	T	T
F	T	F	F	T	T	F
F	F	T	F	F	F	T
F	F	F	F	F	F	F

What can we fill in immediately?



## Next Steps

- We have enough on the table to include the values for  $\neg B$ .
- And we have enough on the table to include the values for the  $A \wedge C$  on the far right.
- We'll do these in order.

# Negation

Everywhere  $B$  is  $\mathbb{T}$ ,  $\neg B$  is  $\mathbb{F}$ , so let's include all of those.

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$				
$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$
$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$
$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$		$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$
$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$		$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$
$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$
$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$
$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$		$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$
$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$		$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$

## Negation (cont)

Everywhere  $B$  is  $\mathbb{F}$ ,  $\neg B$  is  $\mathbb{T}$ , so let's include all of those.

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$				
T	T	T	T	F	T	T	T
T	T	F	T	F	T	T	F
T	F	T	T	T	F	F	T
T	F	F	T	T	F	F	F
F	T	T	F	F	T	T	F
F	T	F	F	F	T	T	F
F	F	T	F	T	F	F	T
F	F	F	F	T	F	F	F

# Conjunction

If  $A, C$  are both  $\text{T}$ , so is  $A \wedge C$ . So let's include those.

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$					
T	T	T	T	F	T	T	T	T
T	T	F	T	F	T	T		F
T	F	T	T	T	F	F	T	T
T	F	F	T	T	F	F	T	F
F	T	T	F	F	T	T	F	T
F	T	F	F	F	T	T	F	F
F	F	T	F	T	F	F	F	T
F	F	F	F	T	F	F	F	F

## Conjunction (cont)

And  $A \wedge C$  is false everywhere else.

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$					
T	T	T	T	F	T	T	T	T
T	T	F	T	F	T	T	F	F
T	F	T	T	T	F	F	T	T
T	F	F	T	T	F	F	F	F
F	T	T	F	F	T	T	F	T
F	T	F	F	F	T	T	F	F
F	F	T	F	T	F	F	F	T
F	F	F	F	T	F	F	F	F

## Complex Disjunction

- The next step is combining the values of  $A$  and  $\neg B$  to get the value of  $A \vee \neg B$ .
- The main thing to remember here is what your inputs are.
- In this case it's not too confusing; it's the values immediately to either side of the  $\vee$ .
- But that won't be the general case.

# Disjunction

When  $A$  is  $\mathbb{T}$ , so is  $A \vee \neg B$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$					
T	T	T	T	T	F	T	T	T
T	T	F	T	T	F	T	T	F
T	F	T	T	T	T	F	T	T
T	F	F	T	T	T	F	T	F
F	T	T	F	F	T	T	F	T
F	T	F	F	F	T	T	F	F
F	F	T	F	T	F	F	F	T
F	F	F	F	T	F	F	F	F

## Disjunction (cont)

And when  $\neg B$  is  $\mathbb{T}$ , so is  $A \vee \neg B$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$					
T	T	T	T	T	F	T	T	T
T	T	F	T	T	F	T	T	F
T	F	T	T	T	T	F	T	T
T	F	F	T	T	T	F	T	F
F	T	T	F		F	T	F	T
F	T	F	F		F	T	F	F
F	F	T	F	T	T	F	F	T
F	F	F	F	T	T	F	F	F



## Disjunction (part III)

Otherwise,  $A \vee \neg B$  is  $\mathbb{F}$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$						
T	T	T	T	T	F	T	T	T	T
T	T	F	T	T	F	T	T	F	F
T	F	T	T	T	T	F	F	T	T
T	F	F	T	T	T	F	F	F	F
F	T	T	F	F	F	T	F	F	T
F	T	F	F	F	F	T	F	F	F
F	F	T	F	T	T	F	F	F	T
F	F	F	F	T	T	F	F	F	F

# Conditional

- Now we have to do  $B \rightarrow (A \wedge C)$ .
- We have to remember the table for  $\rightarrow$  - TFTT.
- And we have to remember that what's on the right-hand side of this conditional is a complex sentence:  $A \wedge C$ .

## Conditional Terminology

- It's helpful to recall our distinctive terminology for conditionals
- We'll often call the left-hand side of a conditional the **antecedent**. ('Ante' for before, if that helps.)

## Conditional Terminology

- It's helpful to recall our distinctive terminology for conditionals
- We'll often call the left-hand side of a conditional the **antecedent**. ('Ante' for before, if that helps.)
- And we'll call the right-hand side the **consequent** (i.e., what comes after).
- We won't have fancy distinct terminology for the left-hand and right-hand sides of other sentences, because they are symmetric.

## Row 1

$B$  is  $\mathbb{T}$ ,  $A \wedge C$  is  $\mathbb{T}$ , so this is  $\mathbb{T} \rightarrow \mathbb{T}$ , i.e.,  $\mathbb{T}$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$								
T	T	T	T	T	F	T	T	T	T	T	
T	T	F	T	T	F	T	T	F	F	F	
T	F	T	T	T	T	F	F	T	T	T	
T	F	F	T	T	T	F	F	T	F	F	
F	T	T	F	F	F	T	T	F	F	T	
F	T	F	F	F	F	T	T	F	F	F	
F	F	T	F	T	T	F	F	F	F	T	
F	F	F	F	T	T	F	F	F	F	F	

## Row 2

$B$  is  $\mathbb{T}$ ,  $A \wedge C$  is  $\mathbb{F}$ , so this is  $\mathbb{T} \rightarrow \mathbb{F}$ , i.e.,  $\mathbb{F}$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$								
T	T	T	T	T	F	T	T	T	T	T	
T	T	F	T	T	F	T	T	F	F	F	
T	F	T	T	T	T	F	F	T	T	T	
T	F	F	T	T	T	F	F	T	F	F	
F	T	T	F	F	F	T	T	F	F	T	
F	T	F	F	F	F	T	T	F	F	F	
F	F	T	F	T	T	F	F	F	F	T	
F	F	F	F	T	T	F	F	F	F	F	

# Row 3

$B$  is  $\mathbb{F}$ ,  $A \wedge C$  is  $\mathbb{T}$ , so this is  $\mathbb{F} \rightarrow \mathbb{T}$ , i.e.,  $\mathbb{T}$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$								
T	T	T	T	T	F	T	T	T	T	T	T
T	T	F	T	T	F	T	T	F	T	F	F
T	F	T	T	T	T	F	F	T	T	T	T
T	F	F	T	T	T	F	F	T	F	F	F
F	T	T	F	F	F	T	T	F	F	T	T
F	T	F	F	F	F	T	T	F	F	F	F
F	F	T	F	T	T	F	F	F	F	T	T
F	F	F	F	T	T	F	F	F	F	F	F

## Row 4

$B$  is  $\mathbb{F}$ ,  $A \wedge C$  is  $\mathbb{F}$ , so this is  $\mathbb{F} \rightarrow \mathbb{F}$ , i.e.,  $\mathbb{T}$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$								
T	T	T	T	T	F	T	T	T	T	T	T
T	T	F	T	T	F	T	T	F	T	F	F
T	F	T	T	T	T	F	F	T	T	T	T
T	F	F	T	T	T	F	F	T	T	F	F
F	T	T	F	F	F	T	T	F	F	T	T
F	T	F	F	F	F	T	T	F	F	F	F
F	F	T	F	T	T	F	F	F	F	T	T
F	F	F	F	T	T	F	F	F	F	F	F



## Row 5

$B$  is  $\mathbb{T}$ ,  $A \wedge C$  is  $\mathbb{F}$ , so this is  $\mathbb{T} \rightarrow \mathbb{F}$ , i.e.,  $\mathbb{F}$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$								
$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$
$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$
$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$
$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$
$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$
$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$
$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$
$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$

## Row 6

$B$  is  $\mathbb{T}$ ,  $A \wedge C$  is  $\mathbb{F}$ , so this is  $\mathbb{T} \rightarrow \mathbb{F}$ , i.e.,  $\mathbb{F}$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$								
$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$
$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$
$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$
$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$
$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$
$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$
$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$		$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$
$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$		$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$

## Rows 7 and 8

$B$  is  $\mathbb{F}$ ,  $A \wedge C$  is  $\mathbb{F}$ , so this is  $\mathbb{F} \rightarrow \mathbb{F}$ , i.e.,  $\mathbb{F}$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$							
T	T	T	T	T	F	T	T	T	T	T
T	T	F	T	T	F	T	T	F	F	F
T	F	T	T	T	T	F	F	T	T	T
T	F	F	T	T	T	F	F	T	F	F
F	T	T	F	F	F	T	T	F	F	T
F	T	F	F	F	F	T	T	F	F	F
F	F	T	F	T	T	F	F	T	F	T
F	F	F	F	T	T	F	F	T	F	F

## Almost Done

- Now we just need to put the two parts together.
- We have a conditional whose left-hand side, the antecedent, is  $A \vee \neg B$ .
- And the right-hand side, the consequent, is  $B \rightarrow (A \wedge C)$ .
- In each row we've computed the truth values for the antecedent and consequent.
- Now it's a matter of just looking up how they combine.
- Remember that the truth table for  $\rightarrow$  is TFFT.
- To help, I've started by putting in blue the columns for the antecedent and consequent.

## Getting There

Bolding the two relevant columns.

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$								
T	T	T	T	<b>T</b>	F	T	T	<b>T</b>	T	T	T
T	T	F	T	<b>T</b>	F	T	T	<b>F</b>	T	F	F
T	F	T	T	<b>T</b>	T	F	F	<b>T</b>	T	T	T
T	F	F	T	<b>T</b>	T	F	F	<b>T</b>	T	F	F
F	T	T	F	<b>F</b>	F	T	T	<b>F</b>	F	F	T
F	T	F	F	<b>F</b>	F	T	T	<b>F</b>	F	F	F
F	F	T	F	<b>F</b>	T	F	F	<b>T</b>	F	F	T
F	F	F	F	<b>F</b>	T	F	F	<b>T</b>	F	F	F

## Row 1

That's  $\mathbb{T} \rightarrow \mathbb{T}$ , i.e.,  $\mathbb{T}$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$								
T	T	T	T	T	F	T	T	T	T	T	T
T	T	F	T	T	F	T	T	F	T	F	F
T	F	T	T	T	T	F	F	T	T	T	T
T	F	F	T	T	T	F	F	T	T	F	F
F	T	T	F	F	F	T	T	F	F	F	T
F	T	F	F	F	F	T	T	F	F	F	F
F	F	T	F	F	T	F	F	T	F	F	T
F	F	F	F	F	T	F	F	T	F	F	F

## Row 2

That's  $\mathbb{T} \rightarrow \mathbb{F}$ , i.e.,  $\mathbb{F}$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$								
T	T	T	T	T	F	T	T	T	T	T	T
T	T	F	T	T	F	T	F	T	F	F	F
T	F	T	T	T	T	F	F	T	T	T	T
T	F	F	T	T	T	F	F	T	F	F	F
F	T	T	F	F	F	T	T	F	F	T	T
F	T	F	F	F	F	T	T	F	F	F	F
F	F	T	F	F	T	F	F	T	F	F	T
F	F	F	F	F	T	F	F	T	F	F	F

## Row 3

That's  $\mathbb{T} \rightarrow \mathbb{T}$ , i.e.,  $\mathbb{T}$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$								
T	T	T	T	T	F	T	T	T	T	T	T
T	T	F	T	T	F	T	F	T	F	F	F
T	F	T	T	T	T	F	F	T	T	T	T
T	F	F	T	T	T	F	F	T	F	F	F
F	T	T	F	F	F	T	T	F	F	F	T
F	T	F	F	F	F	T	T	F	F	F	F
F	F	T	F	F	T	F	F	T	F	F	T
F	F	F	F	F	T	F	F	T	F	F	F



## Row 4

That's also  $\mathbb{T} \rightarrow \mathbb{T}$ , i.e.,  $\mathbb{T}$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$								
T	T	T	T	T	F	T	T	T	T	T	T
T	T	F	T	T	F	T	F	T	F	F	F
T	F	T	T	T	T	F	F	T	T	T	T
T	F	F	T	T	T	F	F	T	F	F	F
F	T	T	F	F	F	T	T	F	F	F	T
F	T	F	F	F	F	T	T	F	F	F	F
F	F	T	F	F	T	F	F	T	F	F	T
F	F	F	F	F	T	F	F	T	F	F	F

## Rows 5 and 6

That's  $\mathbb{F} \rightarrow \mathbb{F}$ , i.e.,  $\mathbb{T}$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$								
T	T	T	T	T	F	T	T	T	T	T	T
T	T	F	T	T	F	T	F	T	F	F	F
T	F	T	T	T	T	F	F	T	T	T	T
T	F	F	T	T	T	F	F	T	F	F	F
F	T	T	F	F	F	T	T	F	F	F	T
F	T	F	F	F	F	T	T	F	F	F	F
F	F	T	F	F	T	F	F	T	F	F	T
F	F	F	F	F	T	F	F	T	F	F	F

## Rows 7 and 8

That's  $F \rightarrow T$ , i.e.,  $T$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$								
T	T	T	T	T	F	T	T	T	T	T	T
T	T	F	T	T	F	T	F	T	F	F	F
T	F	T	T	T	T	F	F	T	T	T	T
T	F	F	T	T	T	F	F	T	F	F	F
F	T	T	F	F	F	T	T	F	F	F	T
F	T	F	F	F	F	T	T	F	F	F	F
F	F	T	F	F	T	F	F	T	F	F	T
F	F	F	F	F	T	F	F	T	F	F	F

## Summing Up

It's true everywhere except when  $A, B$  are both  $\mathbb{T}$ , and  $C$  is  $\mathbb{F}$ .

A	B	C	$(A \vee \neg B) \rightarrow (B \rightarrow (A \wedge C))$								
$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$
$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$
$\mathbb{T}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$
$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$
$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$
$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$
$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$
$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{T}$	$\mathbb{F}$	$\mathbb{F}$	$\mathbb{F}$

## For Next Time

We'll finish our discussion of truth tables with discussion of what we can do with truth tables.