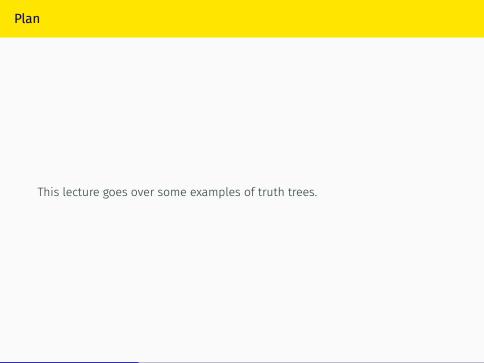
305 Lecture 22 - Examples of Truth Trees

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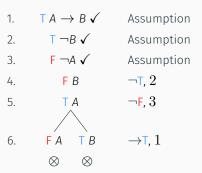


A Logical Truth

This is a tableau for showing $A \rightarrow (A \lor B)$ is a logical truth.

An Argument

Here is a tableau for showing that $A \to B$, $\neg B \vdash \neg A$ is valid.



An Open Tableau

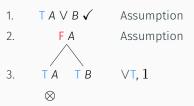
Here is a tableau for showing that $A \to B$, $\neg A \vdash \neg B$ is invalid.

1.
$$TA \rightarrow B \checkmark$$
 Assumption
2. $T \neg A \checkmark$ Assumption
3. $F \neg B \checkmark$ Assumption
4. FA $\neg T, 2$
5. TB $\neg F, 3$
6. FA TB $\rightarrow T, 1$

This one is over the top - since both branches are open. You only need one open branch.

Another Open Tableau

Here's one for the argument $A \lor B \vdash A$



The right hand branch is open, so the whole tableau is open.

