Assignment Week 6

Philosophy 305

Due February 11, 2022, 5pm

Proofs

Provide proofs of each of the following arguments. You should enter these in http://carnap.io, and make a note in Canvas when you are done.

1.
$$A \rightarrow B, A \rightarrow C \vdash A \rightarrow (B \land C)$$

2.
$$A \rightarrow (B \rightarrow C) \vdash (A \land B) \rightarrow C$$

3.
$$A \lor C, A \rightarrow C, B \rightarrow D \vdash C \lor D$$

4.
$$A \lor (B \land C) \vdash (A \lor B) \land (A \lor C)$$

5.
$$(A \rightarrow C) \land (B \rightarrow C) \vdash (A \lor B) \rightarrow C$$

6.
$$\neg A \rightarrow \neg B \vdash B \rightarrow A$$

Challenge questions (to get full marks, you just need to complete any one of these, but you are welcome to try all of them)

7.
$$\neg(A \land B) \vdash \neg A \lor \neg B$$

8.
$$A \rightarrow (B \lor C) \vdash (A \rightarrow B) \lor (A \rightarrow C)$$

9.
$$\vdash (A \rightarrow B) \lor (B \rightarrow A)$$

10.
$$(A \rightarrow B) \rightarrow A \vdash A$$