

# 444 Lecture 12

## Signals

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2/16/23

# Day Plan

Beer and Quiche

Going to College

Honest Signaling

# The Beer-Quiche Game

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- He quickly realises this is a rougher bar than he expected, and the patrons are all staring at him.

# The Beer-Quiche Game

- Sender is smart, and he quickly realises that the patrons are both bullies and cowards. They're bullies, so they are looking for a fight, but cowards, so they won't fight a Tough Guy. And they think it's about 60% likely that he's a Tough Guy.

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- Sender really wants to avoid a fight (whether or not he's a Tough Guy).
- He knows that if he just tries to leave, they will conclude that he too is a Wimp, so he better order something

# The Beer-Quiche Game

- His choices are beer or quiche.



# The Beer-Quiche Game

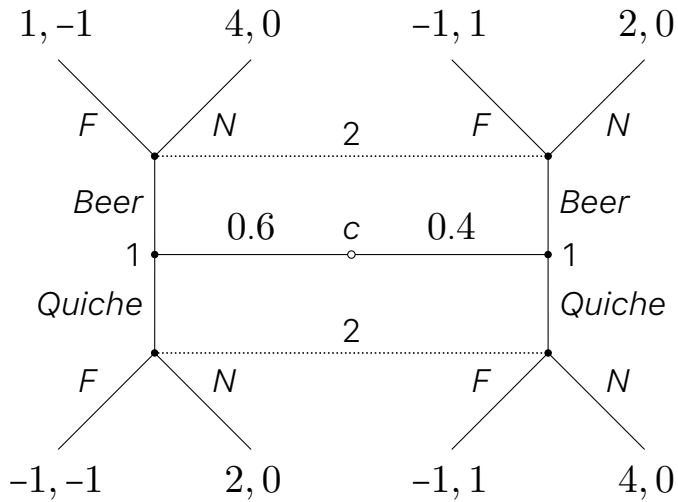
- His choices are beer or quiche.
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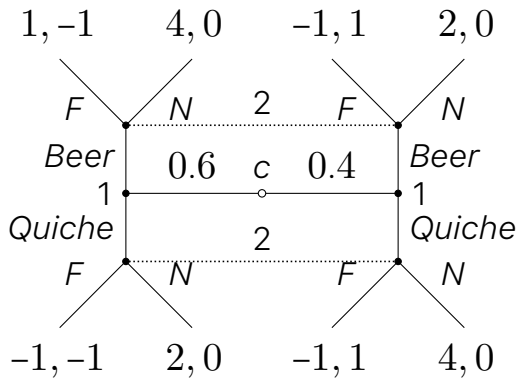
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- And while they can't read his character, they can hear his order.

# The Beer-Quiche Game

- His choices are beer or quiche.
- He knows that the patrons believe, correctly, that if he's a Tough Guy, he'd prefer beer, and if he's a Wimp, he'd prefer quiche.
- And while they can't read his character, they can hear his order.
- But he would also prefer not to get in a fight either way. Even Tough Guys have better things to do at 8 in the morning.



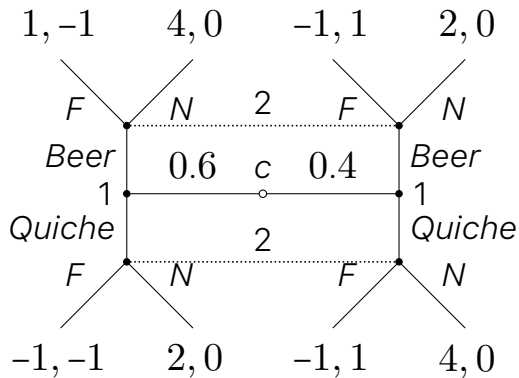


Sender gets (a) 3 points for avoiding fight; plus (b) +1 for liked order, -1 for disliked order.



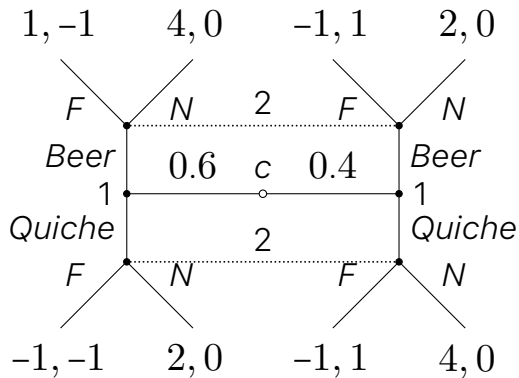
## Obvious Equilibrium

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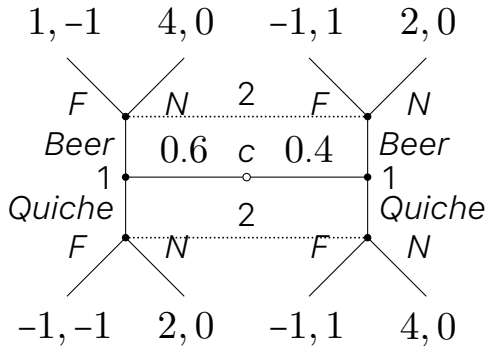
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- Hearer doesn't fight if Beer, fights if Quiche.

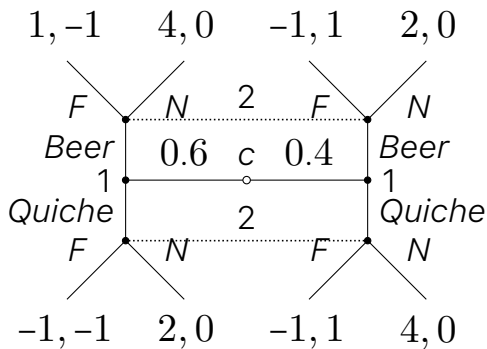




## Non-Obvious Equilibrium

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- The initial statement of the puzzle, and an idea for a solution, is in Cho and Kreps, *Signaling Games and Stable Equilibrium*, QJE 1987.
- If you like puzzles in this area, I highly recommend that paper.

# Our Lessons

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- Nature may provide something like a 'character', or what Harsanyi called a 'type', to Sender.
- You don't have to think of this as some random event that occurs at a particular time, like the whimsical assignment of characters to the pre-infants in *Soul*.



## Our Lessons (cont.)

- All that matters is that there is some feature of Sender that Sender knows and Hearer doesn't.

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- Well, and that Hearer's probability distribution over the possible types of Sender is common knowledge; this game gets nasty if the initial probability for Tough Guy is under 0.5.

## Our Lessons (cont)

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- This is also a good example of a non-cooperative, but positive-sum, signaling game.
- And that's the kind of game that we're going to spend more time looking at in future lectures.

# Day Plan

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Going to College

Honest Signaling

# The College Game

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- There are two attributes of Sender that we're going to be interested in.
- They are either a High Value or Low Value employee.
- They will either Like or Dislike college.
- Let's assume that these attributes are perfectly correlated: all and only the High Value employees Like college.

# Features of College in this Game

- College does not change anyone's value to employers - High Value employees are high value whether or not they go to college, and Low Value employees are low value either way.
- College is fun for people who Like it (i.e., the High Values), but it's not so much fun to be actually worth the expense. But it's a relatively minor overpay for the people who Like it, and both unbearable and exorbitantly expensive for those who Dislike it.
- I am *not* saying either of these are true, though I don't entirely disagree with the second.

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- Unfortunately, they have literally no way of telling who is High Value and who is Low Value.
- All they know is that only 40% of people are High Value.

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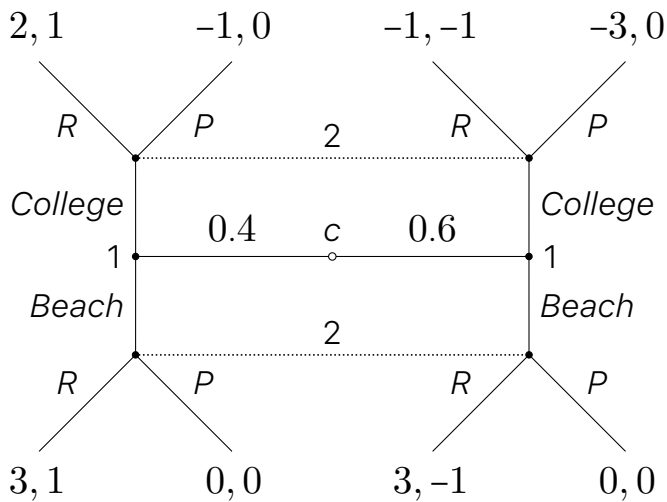
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- They lose 1 point if they Recruit a Low Value Sender.



## Some Notes

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- In the original Spence game, Sender gets to choose how much to spend on education from a range. They have infinitely many choices, not just the binary College/Beach choice. This doesn't really affect the analysis.
- What is crucial is that education is more costly for Low Value employees.

## Some Notes

- There are a lot of equilibria to this game, but the most natural is the separating equilibria, where Like/High go to college, and Dislike/Low go to the Beach.



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- There are a lot of equilibria to this game, but the most natural is the separating equilibria, where Like/High go to college, and Dislike/Low go to the Beach.
- For reasons I don't know (but can guess about), the wikipedia page on signaling games is dire. This is odd because most of the game theory pages are really very good.

# Plausibility

Here are some ways in which the model (or at least the separating equilibrium of the model) does seem to look a bit like the real world.

- College grads get paid a lot more than non-grads.

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- It isn't immediately obvious how what we do here explains the higher pay.

# Plausibility

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- Yet there is a ton of demand for places in college (at least pre-pandemic), and obviously a lot of demand for college grads.

# Plausibility

Here are some ways in which the model (or at least the separating equilibrium of the model) does seem to look a bit like the real world.

- College is more fun, i.e., less costly, for people with certain skills (perseverance, curiosity, writing/mathematical aptitude) that are independently valuable to employers.

# Implausibility

But there are several ways in which the model does not seem particularly plausible.

- At least after a few weeks/months/years in the job, employers have some ability to tell who is High Value, so if education was purely a signal, it should wear off after a little while.

# Implausibility

But there are several ways in which the model does not seem particularly plausible.

- The correlation between High Value and Liking college is a long way from perfect. At least in my day, the people who *really* liked college were not at all what I'd think of as High Value employees for most businesses.

# Implausibility

But there are several ways in which the model does not seem particularly plausible.

- Even if the people who Dislike college really really hate calculus class, it's a little hard to see how they could hate it so much to turn down the college wage premium.



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- In the extreme case, one type of Sender has two options, the other has one.
- In this case, Sender doing the thing that only their type can do is called **honest signaling** or **indexical signaling**.

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- Maybe Hearer is a mugger, or maybe they are a cheetah and Sender is a springbok.
- Sender is either Strong or Weak.
- If they are Strong, they have the option of Jumping in the air before running away.
- This will slow them down, but will display their type to Hearer.

# Payoffs

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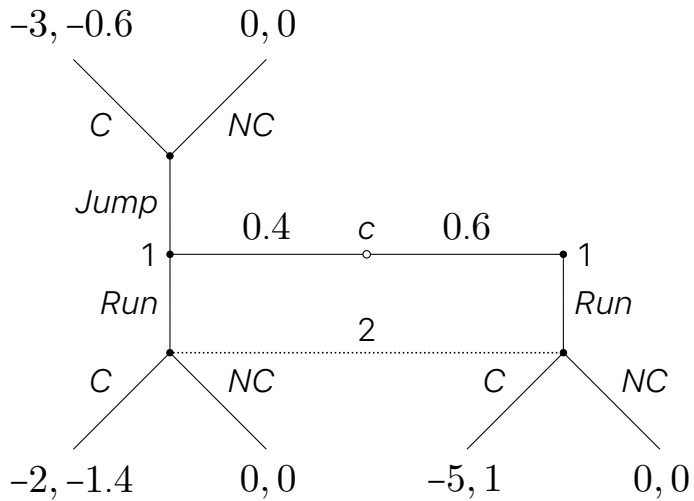
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- Fast sender has a 20% chance of being caught if they don't Jump, and a 30% chance of being caught if they Jump.
- Slow sender can't jump, and has a 50% chance of being caught.



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- If everyone does the same thing, i.e., Run, then Hearer's expected utility from Chasing is positive, so they will Chase everyone.
- But Fast Senders don't want this; they would prefer Jump plus No Chase to Run plus Chase.
- And if they Jump, Hearer will know it isn't worth Chasing.
- So the only sensible equilibrium is that Fast Senders Jump, and Hearer chases all and only Senders who Run (rather than Jumping).

# College

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- Could there be an honest signaling explanation of why there is a college wage premium?
- Maybe; it seems relevant that some people aren't admitted to college and others could not complete it.
- But I don't know what such an explanation could look like.

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# Can't/Won't

- In real life the boundary between a game where signaling is costly for one type and where it is impossible can be hard to draw.
- Especially for non-human animals, what exactly does it mean to say they could do something but choose not to because it is too expensive, rather than say that they can't.
- And for humans, we don't even consider some things to be viable options because they are prohibitively expensive.

# Can't/Won't

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# Can't/Won't

- Are these cases where something is not an option, or where it is rationally not chosen for expense.
- It isn't clear that much could, or should, turn on this.

## For Next Time

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