August Composition (Composition Composition Compositio

February 21, 2023

Day Plan

The Basic Game

Axelrod

Prisoners' Dilemma

Basic Challenge:

- Each player is better off defecting;
- The players are collectively better off if both cooperate.

Tragedy of the Commons

- In a two-player setting, we normally call this Prisoners' Dilemma, or PD.
- In a multi-player setting it's sometimes called the Tragedy of the Commons.

/39

Tragedy of the Commons

- The story (which is probably wildly ahistorical) is that everyone grazed their herds on the commons - which was a good thing to do or else the herd would die - but collectively this made the commons unusable.
- And in the standard story, private property was the solution to the tragedy.

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- How do we get to cooperation?
- First question is whether in this case we should want to get to cooperation.
- Second question is whether this really is PD.
- Let's assume that the answer in each case is yes, what do we do.

9

Change the Payouts

One possible social response is to change the payouts.

• Snitches get stiches is kind of a version of this response.

7/3

Change the Options

Another is to make it just impossible for everyone to do the defecting move.

- Enclosures are sort of like this.
- Just like with signaling games, the difference between making something expensive and making it impossible is a little vague, but it's useful conceptually to think of them as separate options.

8/39

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Iterate the Game

- But the simplest way to handle this kind of problem is to iterate the game.
- Arguably it is in everyone's interests to be cooperative if they will have to interact with the other players repeatedly.



Robert Axelrod

9/3

Evolution Cooperation

Axelrod's Famous 1984 Book

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Axelrod worked with this version of Prisoners' Dilemma (PD).

Indefinite Iteration

In the fancier version of the game, he didn't tell people how long the game would go.

- Instead he just said there was a probability of it ending after each round; if I recall 0.005.
- This was used to avoid backwards induction reasoning.
- It turned out not to really mater a ton; no one uses backward induction reasoning in practice. But it's theoretically useful.

The Tournament

- There are *n* strategies submitted.
- Strategies are not quite full strategies in our sense; they just say
 what to do given what the other player did. (They don't account
 for possible errors in their own performance.)
- Each will play k rounds of PD with each of the other n-1 strategies.
- Their payouts will add up over the k(n-1) rounds and the one
 with the highest total will win.

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Cooperative and Competitive

- This is not entirely a cooperative game; ultimately if I'm a strategy
 I want to win, and that means I want the other strategy I'm
 interaction with to lose.
- But in the short run there is much to be gained by improving our mutual position vs the other n – 2 strategies.
- So in the short run there is a benefit to cooperation, even if we're ultimately rivals.

The Basic Game

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Iterated Axelrod Game

- Axelrod famously ran a tournament just like the one described here.
- But we can iterate the whole tournament in an interesting way.
- Of course the Axelrod tournament involves iterating PD within each 'round'; the idea now is to play multiple rounds.

15/39

16/39

Iterated Axelrod Game

- \bullet Imagine at the start each strategy is $1/\!n$ of the overall 'population'.
- After playing all these games, where each strategy plays k(n-1) versions of PD, each strategy gets a score.
- In the next round, it's share of the population is a function of (a) its initial population, and (b) its score in this round.
- And in future rounds, one's score is a weighted average of how well one does in games against the other strategies, where the weights are given by their populations.

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Evolution of Cooperation

- This is a useful model for thinking about the phenomena in the title of Axelrod's book: The Evolution of Cooperation.
- We want strategies that do well not just when the world consists
 of random strategies, but when the world consists of strategies
 that themselves could have survived at least a little bit of
 evolution.

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- · Theoretically this could make a difference.
- Strategies that exploit dumb strategies could do well initially, but then fade away.
- Alternatively, some strategies could do badly against bad strategies, but if they survive initial rounds, do well when there are sophisticated strategies around.

Spatial Evolution

- To be even more realistic, you could imagine that each strategy lives 'somewhere' in a large grid.
- And at each round, each strategy plays with a weighted average of strategies that live nearby.
- This really does make a difference; some strategies that aren't great against the world in general are fairly immune to invasion, and can even expand their territory under a range of conditions.

39

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The Basic Game

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Overview

This lecture covers some of the lessons from the Iterated Prisoners' Dilemma tournaments that Michigan professor Robert Axelrod ran in the early 1980s.

21/35

Four Papers

- Effective Choice in the Prisoner's Dilemma, Journal of Conflict Resolution 24 (1980): 3-25.
- More Effective Choice in the Prisoner's Dilemma, Journal of Conflict Resolution 24 (1980): 379-403.
- The Emergence of Cooperation among Egoists, *The American Political Science Review* 75 (1981): 306-318.
- The Evolution of Cooperation with William Hamilton, Science 211 (1981): 1390-1396.

The First Tournament

- Axelrod advertised the first round of his tournament, and called for submissions.
- This was far from trivial in pre-internet days, and he only got 13 submissions.
- In the first tournament he said that *k* would be 100, but no one actually exploited that fact.

2

The Winner

Tit-for-Tat

Tit-for-Tat

Two rules.

- 1. Play C at round 1.
- 2. In all subsequent rounds, do whatever the other player just did.

25/39

26/39

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The Second Tournament

- So Axelrod wrote this up, including saying who won.
- He called for more submissions, and now got 66.
- Some of these were typed, some came to Ann Arbor on the huge magnetic disks that were used way back then.
- He ran the tournament again, this time with a random number of rounds.
- And Tit-for-Tat won again.

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Logic and Victory

- This doesn't mean Tit-for-Tat is the best strategy.
- Indeed, in each tournament it was easy in retrospect to describe strategies that would have beaten everyone, including TFT, if they had been entered.
- But still, it's pretty impressive.

28/3

Four Features

Tit-for-Tat has five striking characteristics, each of which was positively correlated with success in the tournaments.

- Nice
- Provocable
- Forgiving
- Not envious
- Simple

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Nice

The clearest distinction in the tournament was between strategies that were Nice and those that were Nasty.

- By definition, a strategy is Nice iff it is never the first to defect.
- You don't have to be very nice in the intuitive sense to count as Nice.

29/39

30/39

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Grim Trigger

Here is one nice strategy, one Axelrod calls Grim Trigger.

- 1. Cooperate on move 1.
- 2. If the other player ever defects, defect on every subsequent move

This strategy did really badly; it was the worst Nice strategy in round 2. But still many Nasty strategies did worse.

31/39

Nice Strategies

- In the evolutionary versions of the game, there can be a tendency for strategies to tend towards being Nice.
- Then evolution stops, because when two Nice strategies meet, the payout is inevitably 3k to each.
- Although the best strategies are all Nice, it is how they interact with Nasty strategies that determines who wins.

32/3

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Provocable

- It's bad to get pushed around.
- Nasty strategies are always looking for how much they can get away with.
- So you want to send a clear message that defections will not be tolerated.
- Obviously TFT does that.

Forgiving

- But you don't want to be Grim Trigger.
- It's bad to be pushed around, but it's not much better to end up in all defect land.
- You need a way back to all cooperate land.
- TFT has that, though notably it isn't perfect at this.
- TFT can get into CD-DC-CD-etc cycles with a bunch of strategies.

34/

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35/39

Not Envious

- In any interaction, TFT never does better than who it is playing with.
- Yet it comes out first overall.
- This is kind of amazing.
- It just does not care at all about winning against who it is facing off with.

Not Envious To a Fault

• Note that TFT doesn't always do that well in evolutionary games.

- This is because it might take this a bit too far.
- It doesn't look to exploit weaknesses in opponents.

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- Other strategies try to figure out what their rivals are doing.
- They normally get this wrong.
- Or they try and send complex signals.
- These are usually misinterpreted.
- TFT keeps things simple, and doesn't lose points messing around looking for any edges.

37/39

Rest of Day

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- I'm not going to do slides about Oyun.
- But the plan for the rest of the day is to go over the assignment, and talk about how the tournament software works.

39/39

Variant Games

- The most interesting variant to me is the one where a strategy only gets implemented with probability 0.99 on each move.
- Sometimes there are performance errors.
- TFT does terribly in this; it can't get out of randomly generated defection cycles.
- In this kind of game you need to be a bit more forgiving.
- But also you can try to get away with a bit more; if the other person will treat a defection as random, you can plan a few.

38/39