# HOMEWORK 2B LINEAR ALGEBRA: VECTOR SPACES \*

#### 10-606 MATHEMATICAL FOUNDATIONS FOR MACHINE LEARNING

#### **START HERE: Instructions**

- Collaboration Policy: Please read the collaboration policy in the syllabus.
- Late Submission Policy: See the late submission policy in the syllabus.
- Submitting your work: You will use Gradescope to submit answers to all questions.
  - Written: For written problems such as short answer, multiple choice, derivations, proofs, or plots, please use the provided template. Submissions can be handwritten onto the template, but should be labeled and clearly legible. If your writing is not legible, you will not be awarded marks. Alternatively, submissions can be written in LaTeX. Each derivation/proof should be completed in the boxes provided. To receive full credit, you are responsible for ensuring that your submission contains exactly the same number of pages and the same alignment as our PDF template.

- Latex Template: https://www.overleaf.com/read/wzyymkmvyjzj

| Question      | Points |
|---------------|--------|
| Vector Spaces | 8      |
| Total:        | 8      |

<sup>\*</sup>Compiled on Friday 1st September, 2023 at 18:35

## **Instructions for Specific Problem Types**

For "Select One" questions, please fill in the appropriate bubble completely:

**Select One:** Who taught this course?

- Matt Gormley
- Noam Chomsky

If you need to change your answer, you may cross out the previous answer and bubble in the new answer:

**Select One:** Who taught this course?

- Henry Chai
- Noam Chomsky

For "Select all that apply" questions, please fill in all appropriate squares completely:

**Select all that apply:** Which are scientists?

- Stephen Hawking
- Albert Einstein
- Isaac Newton
- □ I don't know

Again, if you need to change your answer, you may cross out the previous answer(s) and bubble in the new answer(s):

**Select all that apply:** Which are scientists?

- Stephen Hawking
- Albert Einstein
- Isaac Newton
- □ I don't know

For questions where you must fill in a blank, please make sure your final answer is fully included in the given space. You may cross out answers or parts of answers, but the final answer must still be within the given space.

**Fill in the blank:** What is the course number?

10-606

10-6067

## 1 Vector Spaces (8 points)

| 1. | (1 point) sion.            | <b>Select one:</b> For any finite-dimensional vector space, the size of its basis is equal to its dimen- |
|----|----------------------------|--|
|    | $\bigcirc$                 | True   |
|    | $\bigcirc$                 | False  |
| 2. | (1 point)                  | Select one: For any finite-dimensional vector space, there is always a unique basis.                     |
|    | $\bigcirc$                 | True   |
|    | $\bigcirc$                 | False  |
| 3. | (1 point)                  | Select one: Every vector space contains a zero vector.   |
|    | $\bigcirc$                 | True   |
|    | $\bigcirc$                 | False  |
| 4. | (1 point)                  | Select one: A vector space can have more than one zero vector.   |
|    | $\bigcirc$                 | True   |
|    | $\bigcirc$                 | False  |
| 5. | (1 point) $\mathbb{R}^n$ . | Select one: Matrices can be used to represent any translation or rotation on the vector space            |
|    | $\bigcirc$                 | True   |
|    | $\bigcirc$                 | False  |
| 6. | (1 point)                  | Select one: Every square matrix is invertible.   |
|    | $\bigcirc$                 | True   |
|    | $\bigcirc$                 | False  |
| 7. | (1 point)                  | Select one: Every symmetric matrix is invertible.  |
|    | $\bigcirc$                 | True   |
|    | $\bigcirc$                 | False  |
| 8. | (1 point)                  | Select one: Matrix multiplication is associative and commutative.  |
|    | $\circ$                    | True   |
|    | $\bigcirc$                 | False  |

### **2** Collaboration Questions

After you have completed all other components of this assignment, report your answers to these questions regarding the collaboration policy. Details of the policy can be found in the syllabus.

- 1. Did you receive any help whatsoever from anyone in solving this assignment? If so, include full details.
- 2. Did you give any help whatsoever to anyone in solving this assignment? If so, include full details.
- 3. Did you find or come across code that implements any part of this assignment? If so, include full details.

| Your Answer |  |
|-------------|--|
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