

$$[Fe/H] = 0.040 \text{ (TRAPPIST-1, Gillon et al. 2017)}$$

$$\Rightarrow [Mg/Fe] = 0.12 \text{ (Fig 1, Griffith et al. 2020)}$$

$$[Mg/Fe] = \log \left(\frac{Mg/Fe}{(Mg/Fe)_\odot} \right)$$

$$Fe/Mg = 0.9 \Rightarrow Mg/Fe = 1.11$$

↑ from Exoplanet

$$[Mg/Fe] = \log \left(\frac{Mg/Fe}{1.11} \right)$$

$$\log \left(\frac{Mg/Fe}{1.11} \right) = 0.12$$

$$10^{\log \left(\frac{Mg/Fe}{1.11} \right)} = 10^{0.12}$$

$$\frac{Mg/Fe}{1.11} = 10^{0.12}$$

$$\frac{Mg}{Fe} = (1.11) 10^{0.12} \approx 1.46$$

↓

$$\frac{Fe}{Mg} = 0.683$$

$$[Fe/Mg] = \log \left(\frac{Fe/Mg}{(Fe/Mg)_\odot} \right)$$

$$= \log \left(\frac{0.683}{0.9} \right)$$

$$= -0.12$$

use table 2,
closest value to ours is

$$[Fe/Mg] = -0.134$$

ours is likely off due to estimation

$$\text{so, adopt } [Fe/Mg] \approx -0.134$$

$$\text{gives } [Mg/H] = 0.445$$

Table 1 gives:

$$[Si/Mg] = -0.017 \quad \text{for } [Mg/H] = 0.445$$

$$\text{Eq. } \frac{N}{M} = \frac{N_0}{M_0} \cdot 10^{[N/M]}$$

$$Si/Mg_{\odot} = 0.9 \quad (\text{Exoplanet})$$

$$\frac{Si}{Mg} = \left(\frac{Si}{Mg} \right)_{\odot} \cdot 10^{[Si/Mg]}$$

$$= 0.9 \cdot 10^{-0.017}$$

$$= 0.86 \quad \text{or} \quad 0.87$$

Density of planet (assuming uniform density)

$$\text{Density} = \frac{\text{Mass}}{\text{Volume}}$$

$$\text{Volume} = \frac{4}{3} \pi R^3$$

$$\begin{aligned} \text{Radius} &= 0.943 R_E, \quad \text{mass} = 0.772 M_E \\ R_E &= 6378 \text{ km} \quad M_E = 5.974 \times 10^{24} \text{ kg} \\ \rightarrow &= 0.943 (6378 \text{ km}) = 6014.45 \end{aligned}$$

$$\text{Volume} = \frac{4}{3} \pi (6014.45)^3 = 9.113 \times 10^{11} \text{ km}^3$$

$$\text{Density} = \frac{\text{Mass}}{\text{Volume}} = \frac{0.772 (5.974 \times 10^{24} \text{ kg})}{9.113 \times 10^{11} \text{ km}^3}$$

$$= 5.061 \times 10^{12} \text{ kg / km}^3$$

$$1 \text{ g/cm}^3 = 1 \times 10^{-12} \text{ kg / km}^3$$

$$5.061 \times 10^{12} \text{ kg/cm}^3 \times \frac{1 \text{ g/cm}^3}{1 \times 10^{12} \text{ kg/cm}^3}$$

$$= 5.06 \text{ g/cm}^3$$

↑
approx. density