

CSCI104: Written Homework #1

1. Problem 1: Runtime Analysis

a. Part A: $f(n) = \Theta(\log(n))$

- i. In the loop, the loop runs until 'i' is greater than or equal to n
- ii. In each iteration, the variable 'i' is squared, which makes the number of iterations equivalent to $\log(n)$
- iii. Therefore, the runtime is $\Theta(\log(n))$

b. Part B: $f(n) = \Theta(n)$

- i. The outer loop runs until 'i' is greater than n, which runs for n times.
- ii. If 'i' is the multiple of a square root of n, an inner loop iterates until 'k' is greater than i^3 , which runs for i^3 times.
- iii. The outer loop runs n times + the inner loop for i^3 times
- iv. Therefore, the runtime is $\Theta(n)$

c. Part C: $f(n) = \Theta(n^2 * \log(n))$

- i. The first loop runs until 'i' is greater than n, which runs for n times.
- ii. The second loop runs until 'k' is greater than n, which runs for n times as well.
- iii. If $A[k]$ is equivalent to i, start another loop until 'm' is greater than n, where m doubles every iteration.
 - 1. Therefore, this loop iterates $\log(n)$ times
- iv. The first loop runs for n times, the second loop for n times, plus the final inner loop runs for $\log(n)$ times
- v. Therefore, the runtime is $\Theta(n^2 * \log(n))$

d. Part D: $f(n) = \Theta(n)$

- i. The first loop runs until 'i' is greater than or equal to n
- ii. If 'i' reaches the current array size, resize the array, which would take $\Theta(\text{size})$ time.
- iii. Therefore, it would iterate n times for the loop plus 'size' times for the resizing; $\Theta(n + \text{size})$, which is $\Theta(n)$

2. Problem 2: Linked List Recursion Tracing:

- a. Question a: What linked list is returned if llrec is called with the input linked lists $\text{in1} = 1,2,3,4$ and $\text{in2} = 5,6$?

- b. Question b: What linked list is return if llrec is called with the input linked lists
in1 = nullptr and in2 = 2?

Homework 1:

Question a: in1 = 1 → 2 → 3 → 4 , in2 = 5 → 6

llrec(ⁱⁿ¹1 → 2 → 3 → 4, ⁱⁿ²5 → 6)

1 → in1 → next : llrec(ⁱⁿ¹5 → 6, ⁱⁿ²2 → 3 → 4)

5 → in1 → next : llrec(ⁱⁿ¹2 → 3 → 4, ⁱⁿ²6)

2 → in1 → next : llrec(ⁱⁿ¹6, ⁱⁿ²3 → 4)

6 → in1 → next : llrec(ⁱⁿ¹3 → 4, nullptr)

if in2 = null, return in1 (3 → 4)

∴ return

in1 = 1 → 5 → 2 → 6 → 3 → 4

Question b: in1 = nullptr , in2 = 2

Since if in1 == nullptr return in2,

then it will return 2 when in2 = 2.