

CSCI104: Written Homework #1

1. Problem 1: Runtime Analysis

a. Part A: $f(n) = \Theta(\log(n))$

- i. In the loop, the loop runs until 'i' is greater than or equal to n
- ii. In each iteration, the variable 'i' is squared, which makes the number of iterations equivalent to $\log(n)$
- iii. Therefore, the runtime is $\Theta(\log(n))$

b. Part B: $f(n) = \Theta(n)$

- i. The outer loop runs until 'i' is greater than n, which runs for n times.
- ii. If 'i' is the multiple of a square root of n, an inner loop iterates until 'k' is greater than i^3 , which runs for i^3 times.
- iii. The outer loop runs n times + the inner loop for i^3 times
- iv. Therefore, the runtime is $\Theta(n)$

c. Part C: $f(n) = \Theta(n^2 * \log(n))$

- i. The first loop runs until 'i' is greater than n, which runs for n times.
- ii. The second loop runs until 'k' is greater than n, which runs for n times as well.
- iii. If $A[k]$ is equivalent to i, start another loop until 'm' is greater than n, where m doubles every iteration.
 1. Therefore, this loop iterates $\log(n)$ times
- iv. The first loop runs for n times, the second loop for n times, plus the final inner loop runs for $\log(n)$ times
- v. Therefore, the runtime is $\Theta(n^2 * \log(n))$

d. Part D: $f(n) = \Theta(n)$

- i. The first loop runs until 'i' is greater than or equal to n
- ii. If 'i' reaches the current array size, resize the array, which would take $\Theta(\text{size})$ time.
- iii. Therefore, it would iterate n times for the loop plus 'size' times for the resizing; $\Theta(n + \text{size})$, which is $\Theta(n)$

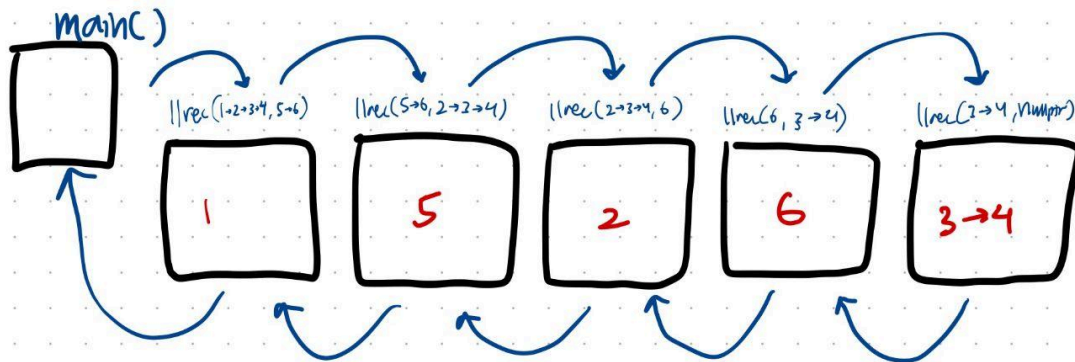
2. Problem 2: Linked List Recursion Tracing:

- a. Question a: What linked list is returned if llrec is called with the input linked lists $\text{in1} = 1,2,3,4$ and $\text{in2} = 5,6$?

- b. Question b: What linked list is return if llrec is called with the input linked lists
 $in1 = \text{nullptr}$ and $in2 = 2$?

Homework 1:

Question a: $in1 = 1 \rightarrow 2 \rightarrow 3 \rightarrow 4$, $in2 = 5 \rightarrow 6$



$\therefore \text{return}$

$in1 = 1 \rightarrow 5 \rightarrow 2 \rightarrow 6 \rightarrow 3 \rightarrow 4$

$llrec(\overset{in1}{1 \rightarrow 2 \rightarrow 3 \rightarrow 4}, \overset{in2}{5 \rightarrow 6})$

$1 \rightarrow in1 \rightarrow next : llrec(\overset{in1}{5 \rightarrow 6}, \overset{in2}{2 \rightarrow 3 \rightarrow 4})$

$5 \rightarrow in1 \rightarrow next : llrec(\overset{in1}{2 \rightarrow 3 \rightarrow 4}, \overset{in2}{6})$

$2 \rightarrow in1 \rightarrow next : llrec(\overset{in1}{6}, \overset{in2}{3 \rightarrow 4})$

$6 \rightarrow in1 \rightarrow next : llrec(\overset{in1}{3 \rightarrow 4}, \text{nullptr})$

if ($in2 = \text{null}$), return $in1$ ($3 \rightarrow 4$)

Question b: $in1 = \text{nullptr}$, $in2 = 2$

Since if $in1 == \text{nullptr}$ return $in2$,
 then it will return 2 since $in2 = 2$.