

# Applied Related Rates

## Recitation Questions

**Problem 1** Find the mistake in the solution to the given problem. Then solve the problem correctly.

Two boats leave from the same dock, but at slightly different times. One boat is traveling east at 30mph while the other boat is traveling north at 15mph. At an instant in time when the boat traveling east is 15 miles from the dock and the boat traveling north is 10 miles away from the dock, at what rate is the distance between the boats changing?

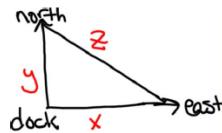
• We want to find  $\frac{dz}{dt}$  so  
 $x^2 + y^2 = z^2$

• We know  $x=15, y=10,$   
 $\frac{dx}{dt} = 30, \frac{dy}{dt} = 15$

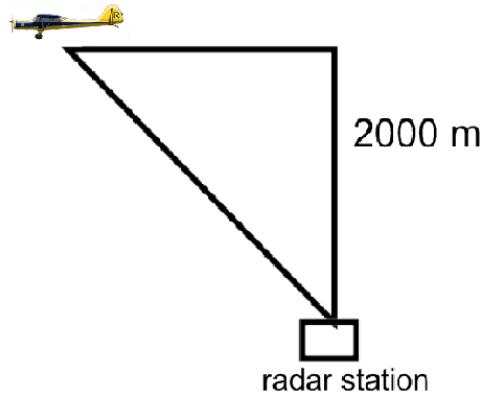
• Substituting  $x=15$  and  $y=10:$   
 $15^2 + 10^2 = z^2$  or  $325 = z^2$

• Take the derivative:  
 $0 = 2z \frac{dz}{dt}$

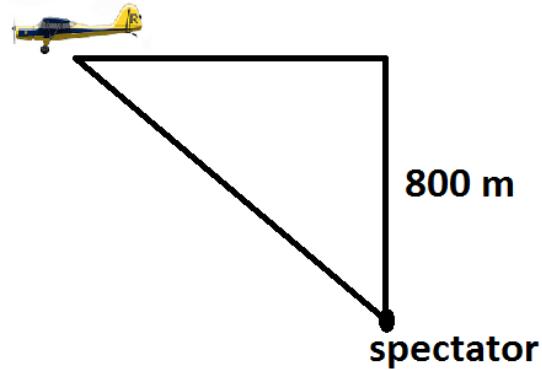
• So  $\frac{dz}{dt} = 0$



**Problem 2** A plane flying horizontally at an altitude of 2000 m and a speed of 200 m/sec passes directly over a radar station. (See figure below.) Find the rate at which the distance from the plane to the station is increasing 5 seconds after the plane passed directly over the radar station. Make sure to label the figure.

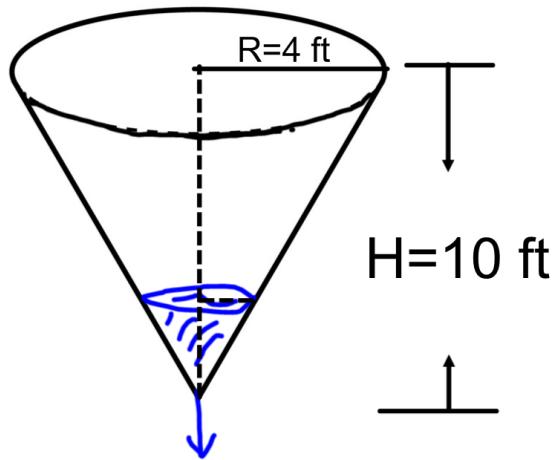


**Problem 3** A plane flying horizontally at an altitude of 800m and speed of 200 m/sec passes directly over a spectator at an air show. (See figure below.) Find the rate at which the angle of elevation,  $\theta$ , is changing 4 seconds later. Make sure to label the figure. ( $\theta$  = angle between the ground and the line from the spectator to the plane)



**Problem 4** A cylindrical swimming pool with a radius of 10 feet and height of 5 feet is being filled with water. How fast is the water being pumped into the pool (in  $\text{ft}^3/\text{min}$ ) if the water level is increasing at a rate of 6 in./minute? Make sure to draw a picture to represent the situation.

**Problem 5** A conical water tank of height 10 feet and radius 4 feet is being drained through a hole in the bottom (See figure below).



- (a) Let  $r$  be the radius of the water at depth  $h$ . In the figure above, label  $r$  and  $h$ .
- (b) Find an expression for  $r$  in terms of  $h$ .
- (c) The water in the tank is being drained at a rate of 2 feet<sup>3</sup> per minute. What is the rate of change of the water depth when the water depth is 3 feet?