Compositional Analysis of Catch Curve Data

Model

$$S_a = e^{-Z(a-k)}; \qquad a = k, \dots, B \tag{1}$$

$$\beta_a(\beta_k, \alpha) = \begin{cases} 1 - (1 - \beta_k) \left(\frac{b_0 - a}{b_0 - k}\right)^{\alpha}; & a = k, \dots, b_0 - 1\\ 1; & a = b_0, \dots, B \end{cases}$$
 (2)

$$R_a(\rho_1, \dots, \rho_m, \tau) = 1 + \sum_{h=1}^m \rho_h \exp\left[-\frac{1}{2} \left(\frac{a - b_h}{\tau}\right)^2\right]; \qquad a = k, \dots, B$$
 (3)

$$p_a = \frac{S_a \beta_a R_a}{\sum_{a=k}^B S_a \beta_a R_a}; \qquad a = k, \dots, B$$

$$\tag{4}$$

$$p_A = \sum_{a=A}^{B} p_a \tag{5}$$

Amalgamation into groups

$$p_i = \sum_{a=a, i+1}^{a_i} p_a; \qquad i = 1, \dots, g$$
 (6)

Parameters

Z = total mortality

 $\alpha, \beta_k = \text{selectivity parameters}$

 $\rho_h = \text{recruitment anomaly } (h = 1, \dots, m)$

 $\tau = \text{anomaly 'width'}$