

Math 201, Assignment 5

Due at the beginning of class on July 29, 2015

Illegible or disorganized solutions will receive no credit! Please, for the sake of our marker, be neat!

- 1) Solve the following IVP:

$$y'' + 6y' + 5y = \delta(t - 2), \quad y(0) = 0, \quad y'(0) = 0$$

- 2) Find the Laplace Transform of the periodic triangular wave, given by:

$$f(t) = 2t, \quad 0 \leq t < 2 \text{ and } f(t + 2) = f(t)$$

- 3) Solve the integral equation:

$$y(t) = t + \int_0^t y(x)dx + \int_0^t (t - x)y(x)dx$$

- 4) Use the convolution theorem to find

$$\mathcal{L}^{-1} \left\{ \frac{s^2}{(s^2 + 1)^2} \right\}$$

- 5) Use a power series about the point $x = 0$ to solve the following differential equation:

$$y'' - xy' - y = 0$$

Obtain a recursion formula for the coefficients and write the first 3 nonzero terms of the power series of each of the two linearly independent solutions. Include the interval of convergence of the power series.