

# CSC421 Intro to Artificial Intelligence



## Chapter 3 Informed Searching

# Review

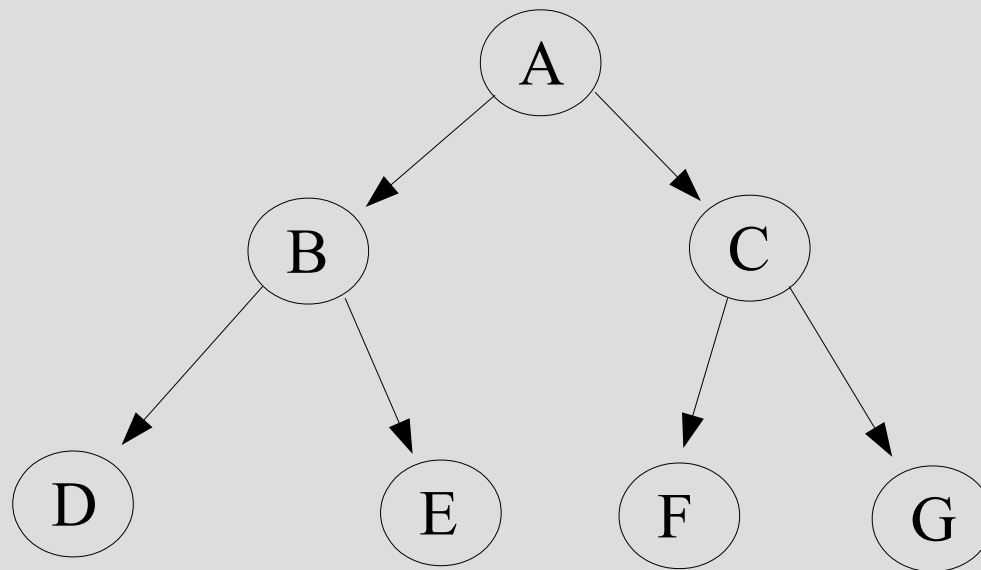


## Review

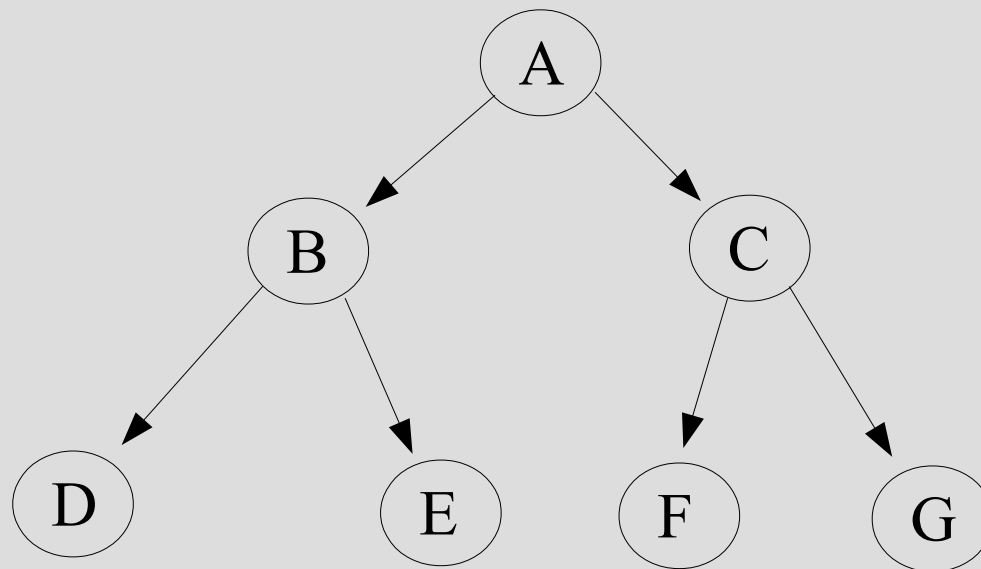
```
function TREE-SEARCH(problem, strategy) returns a solution, or failure
  initialize the search tree using the initial state of problem
  loop do
    if there are no candidates for expansion then return failure
    choose a leaf node for expansion according to strategy
    if the node contains a goal state then return the corresponding solution
    else expand the node and add the resulting nodes to the search tree
```

Strategy = picking the order of node expansion

# Mini-test



# Mini-test

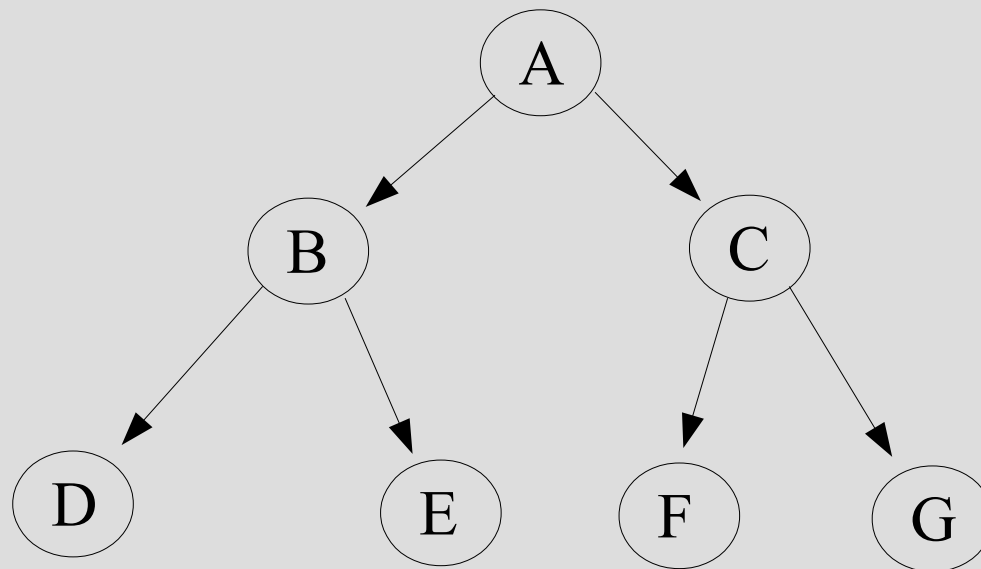


BFS: FIFO fringe =

[A]->[B,C]->[C,D,E]->[D,E,F,G]->...

Order of nodes visited: ABCDEFG

# Mini-test

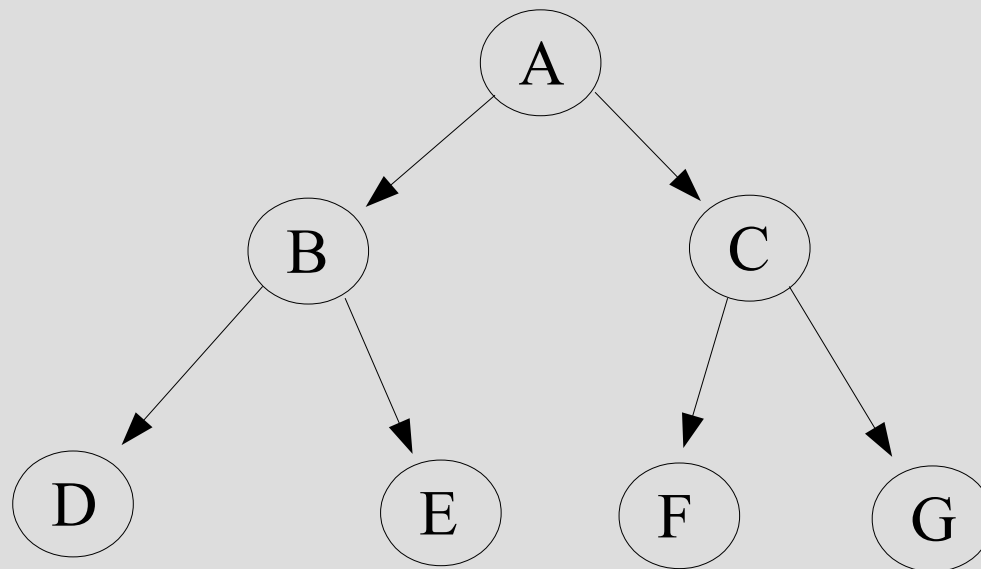


DFS: LIFO fringe =

$[A] \rightarrow [B, C] \rightarrow [D, E, C] \rightarrow [E, C] \rightarrow [C] \rightarrow [F, G]$

Order of nodes visited: ABDECFG

# Mini-test



A  
ABC  
ABDECFG

IDS: Multiple DFS up to depth  
Order of nodes visited:  
AABCABDECFG

# Best-first search



Idea: use an **evaluation function** for each node –  
estimate of “desirability”

Expand most desirable unexpanded node

Implementation:

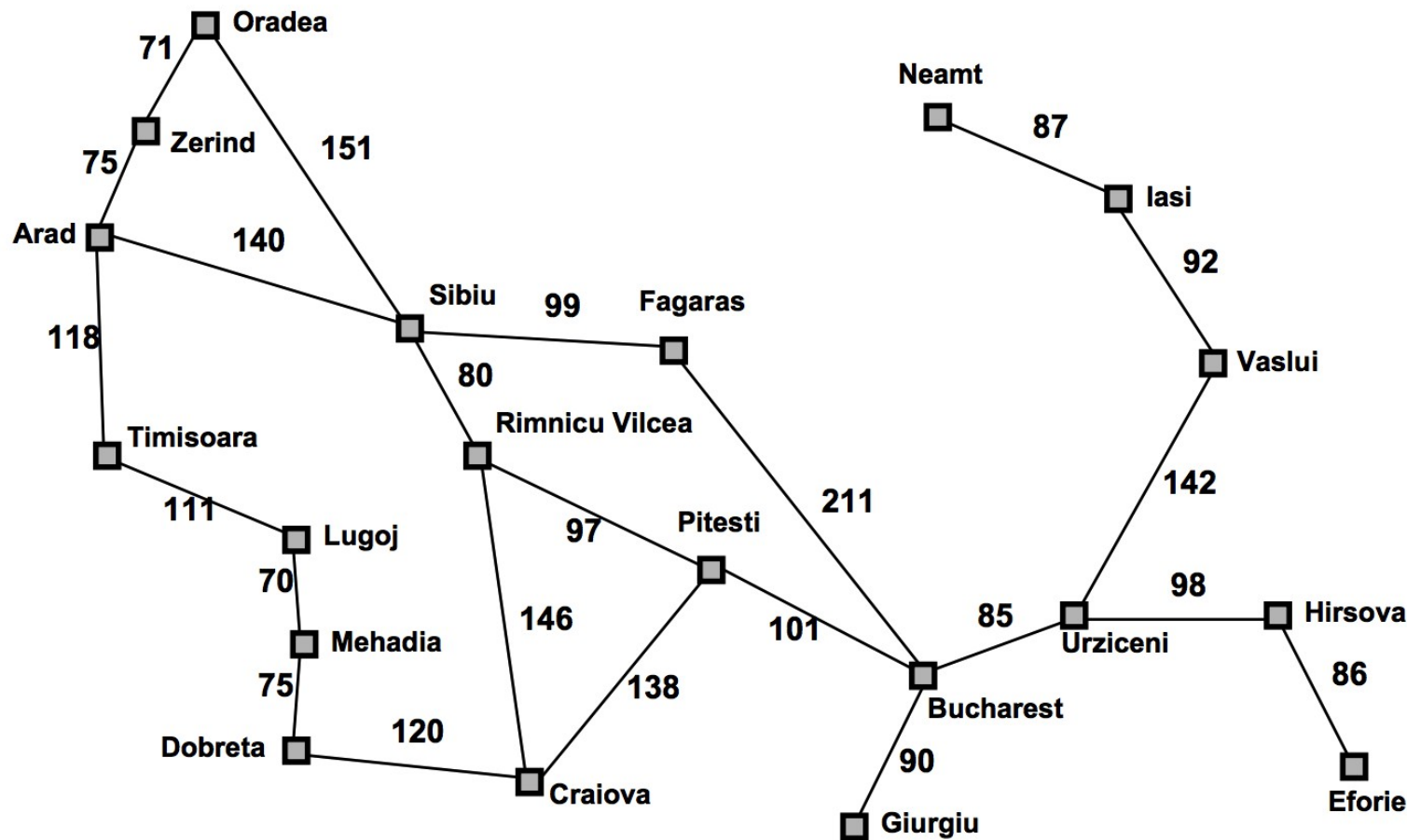
Fringe is a queue sorted in decreasing order of  
desirability

Special cases:

Greedy search

A\*-search

# Map with step costs and straight-line distances to goal



Straight-line distance  
to Bucharest

<b>Arad</b>	366
<b>Bucharest</b>	0
<b>Craiova</b>	160
<b>Dobreta</b>	242
<b>Eforie</b>	161
<b>Fagaras</b>	178
<b>Giurgiu</b>	77
<b>Hirsova</b>	151
<b>Iasi</b>	226
<b>Lugoj</b>	244
<b>Mehadia</b>	241
<b>Neamt</b>	234
<b>Oradea</b>	380
<b>Pitesti</b>	98
<b>Rimnicu Vilcea</b>	193
<b>Sibiu</b>	253
<b>Timisoara</b>	329
<b>Urziceni</b>	80
<b>Vaslui</b>	199
<b>Zerind</b>	374



# Greedy Search

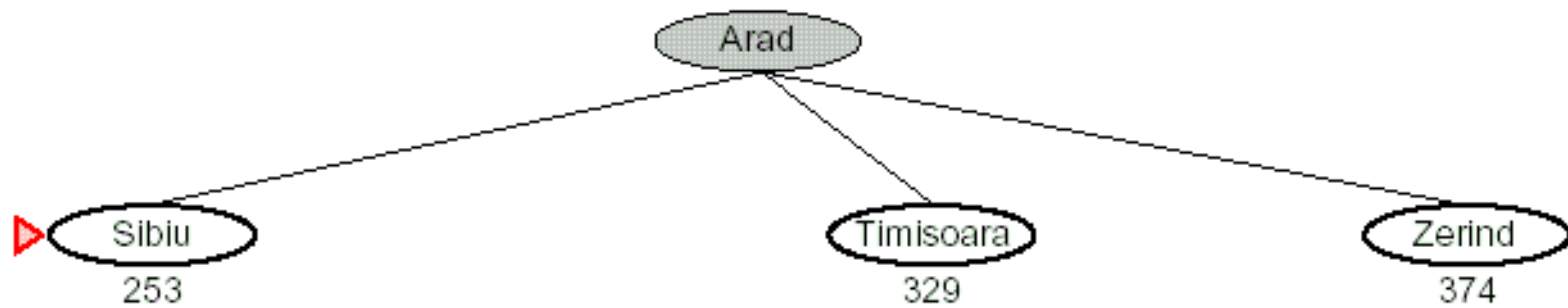


Evaluation function  $h(n)$  (heuristic) = estimate of cost from  $n$  to goal

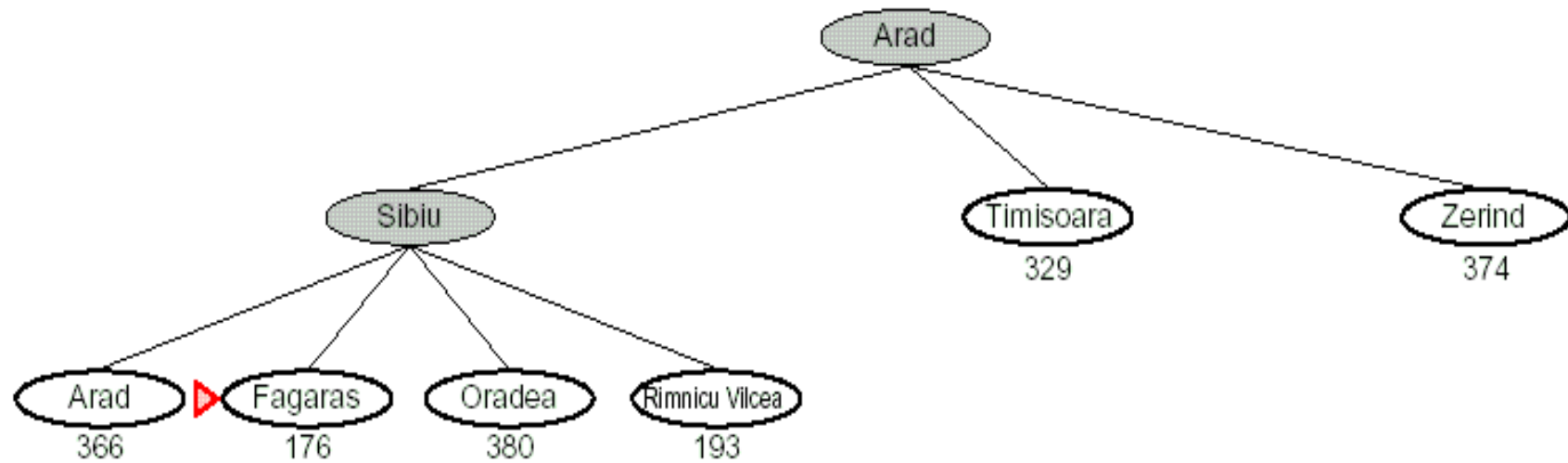
E.g.,  $h_{\text{SLD}}(n)$  = straight-line distance from  $n$  to  
Bucarest

Greedy search expands the node that **appears** to be closest to goal

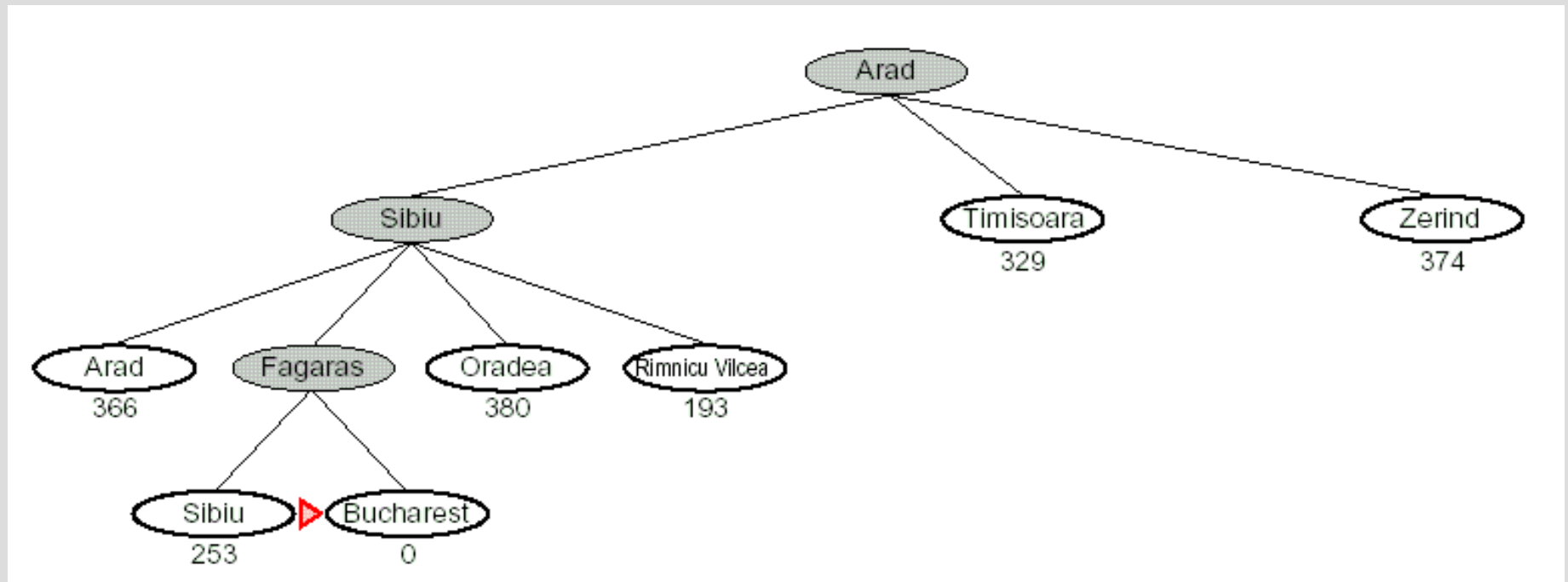
# Greedy Search Example



# Greedy Search Example



# Greedy Search Example



# Properties of Greedy Search



Complete: no it can get stuck in loops – however complete with repeated state checking

Time:  $O(b^m)$  but good heuristic can give dramatic improvements in many cases

Space:  $O(b^m)$

Optimal: No, why ?

# A-\* search



Idea: avoid expanding paths that are already expensive

Evaluation function  $f(n) = g(n) + h(n)$

$g(n)$  : cost so far to reach  $n$

$h(n)$  : estimated cost to goal from  $n$

$f(n)$  : estimated total cost of path through  $n$  to goal

A-\* search needs to use an **admissible** heuristic i.e always  
 $\leq$  true cost

For example  $h_{\text{SDL}}$  is always less than the true distance (at  
least in Euclidean geometry)

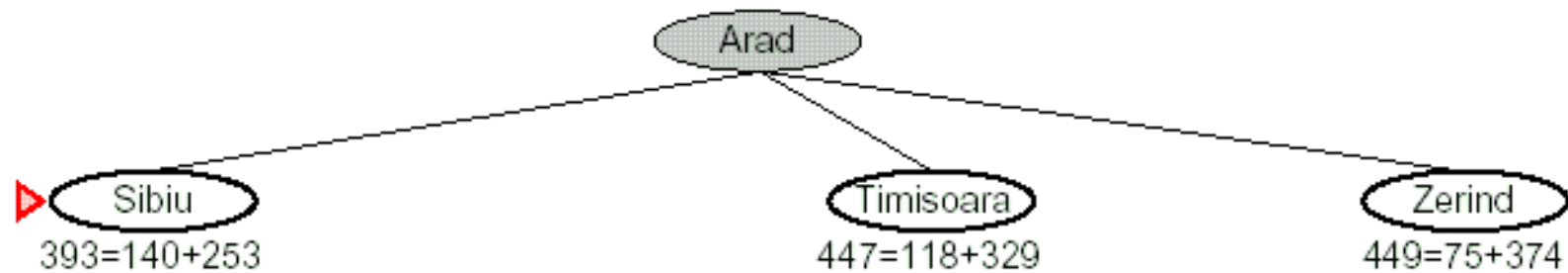
Theorem: A\* is **optimal**

# A\* example



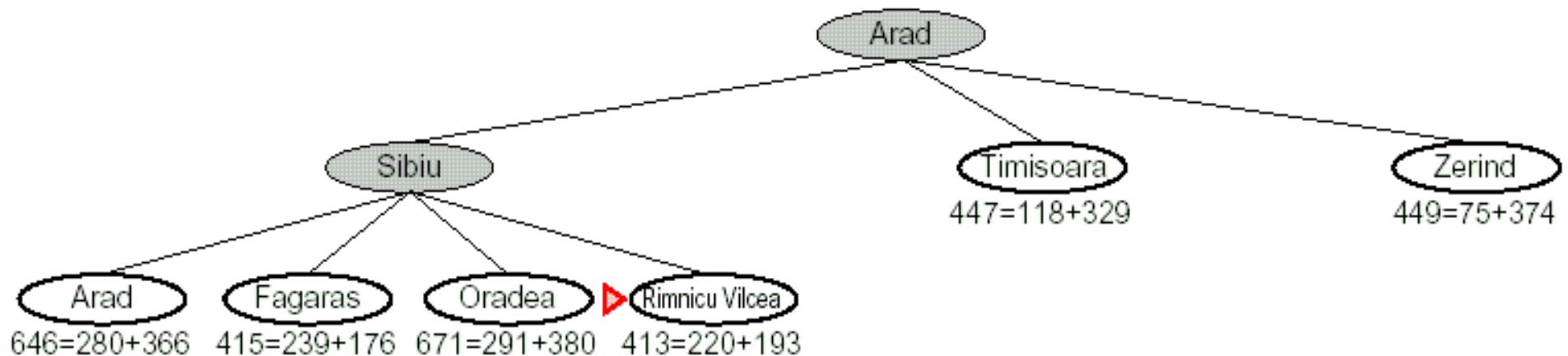
▶ Arad  
366=0+366

# A\* example





# A\* example



Gradually adds *f-contours* of nodes  
Nice easy optimality proof read the book

# A\* properties



Complete: Yes, unless there are infinitely many nodes with  $f \leq f(G)$

Time: exponential in [relative error in \* length of solution]

Memory: Keeps all nodes in memory

Optimality: yes

Problems

- Exponential growth for most optimal solution

- Sometimes good-enough ok (suboptimal)

- Memory-intensive (read book for some approaches to reducing memory load)

# Admissable Heuristic



e.g., for the 8-puzzle

$h_1(n)$  = number of misplaced tiles

$h_2(n)$  = total Manhattan distance (i.e #squares from desired location of each tile)

7	2	4
5		6
8	3	1

Start State

1	2	3
4	5	6
7	8	

Goal State

$$h_1(S) = ?$$

$$h_2(S) = ?$$

# Dominance



If  $h_2(n) \geq h_1(n)$  for all  $n$  (both admissible) then  $h_2$  dominates  $h_1$  is better for search

Typical search costs:

$D=14$

IDS 3,473,941 nodes

$A^*(h_1) = 539$  nodes

$A^*(h_2) = 113$  nodes

# Relaxed problems



Admissible heuristics can be derived from the exact solution cost of a relaxed version of the problem  
If the rules of the 8-puzzle are relaxed so that a tile can move anywhere then  $h_1$  gives the shortest solution

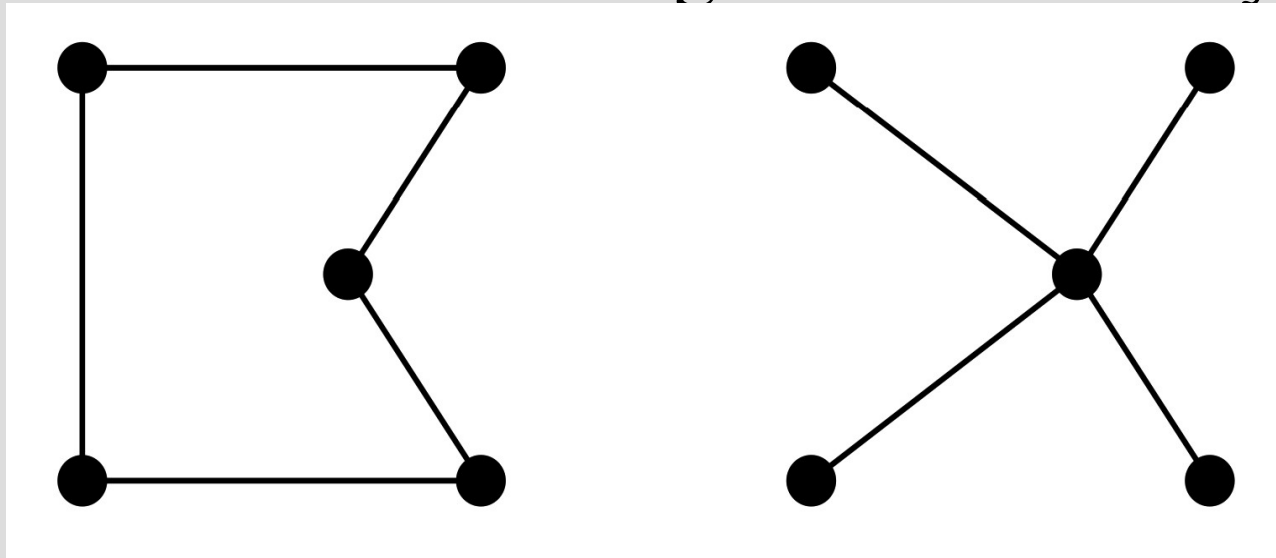
What about  $h_2$  ?

Key point: the optimal solution cost of a relaxed problem is no greater than the optimal solution of the real problem

# More relaxed problems



- Well known example: traveling salesman problem
- Find the shortest tour visiting all cities exactly once



Minimum spanning tree can be computed in  $O(n^2)$  and is a lower bound on the shortest (open) tour

# Summary



Heuristic functions estimate costs of shortest paths

Good heuristics can dramatically reduce search cost

Greedy best-first search expands lowest  $h$

- Incomplete, not always optimal

$A^*$  search expands lowest  $g + h$

- Complete and optimal

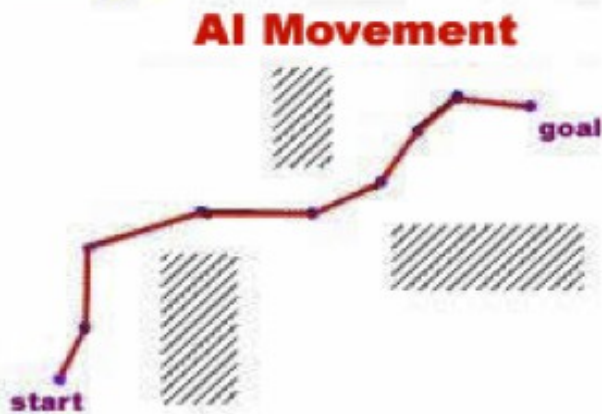
Admissable heuristics can be derived from the exact solution of relaxed problems

# Food for thought

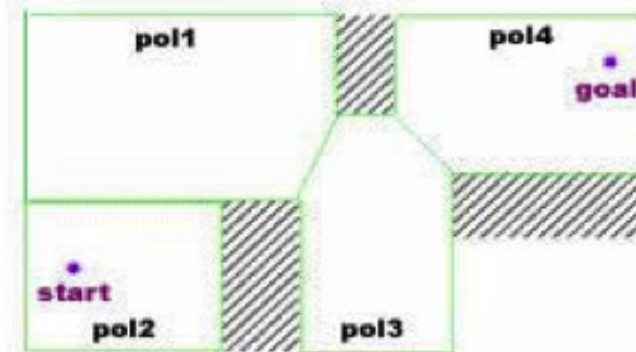


- A\* in modern computer games
- Simplifying search space without compromising solution
  - Hierarchical path finding
  - Waypoints
  - Navigation mesh
- Memory issues
  - Node bank
  - IDA\*
- Game examples
  - Age of empires
  - Civilization
  - World of Warcraft





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The diagram shows a 2D environment divided into four quadrants by a green cross. The quadrants are labeled **pol1** (top-left), **pol2** (bottom-left), **pol3** (bottom-right), and **pol4** (top-right). A red path starts at a purple dot labeled **start** in the **pol2** region, moves diagonally up and to the right, crosses the boundary into **pol1**, and then continues diagonally up and to the right into **pol4**, ending at a purple dot labeled **goal**. There are green hatched rectangular areas at the intersections of the boundaries: one at the top intersection, one at the bottom intersection, and one on the right side.

**(b)**

Fig. 3 Different representations of waypoint graph and NavMesh [7]

# Age of Empires

