Introduction to Machine Learning

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Outline

The problems of Machine Learning (1 week) Introduction

Estimation

Answering a scientific problem Simple modelling

Validating models

Course summary

Course Contents Objective functions Pitfalls

Reading

The problems of Machine Learning (1 week) Introduction

Estimation

Validating models

Course summary

Reading

Machine Learning And Data Mining

The nuts and bolts

- ► Models
- ► Algorithms
- ► Theory
- Practice

Work flow

- Scientific question
- ► Formalisation of the problem
- Data collection
- Analysis and model selection

Types of machine learning / statistics problems

- ► Classification
- Regression
- Density estimation
- Clustering



Machine learning

Data Collection

- Downloading a clean dataset from a repository
- Performing a survey
- Scraping data from the web
- Deploying sensors, performing experiments, and obtaining measurements.

Modelling (what we focus on this course)

- ► Simple: the bias of a coin
- Complex: a language model.
- The model depends on the data and the problem

Algorithms and Decision Making

- ▶ We want to use models to make decisions.
- ▶ Decisions are made every step of the way.
- Decisions are automated algorithmically.



The main problems in machine learning and statistics

Prediction

- Will it rain tomorrow?
- How much will bitcoin be worth next year?

Inference

- Does my poker opponent have two aces?
- ▶ What is the mass of the moon?
- What is the law of gravitation?

Decision Making

- Should I go hiking tomorrow?
- Should I buy some bitcoins?
- ► Should I fold, call, or raise in my poker game?
- ▶ How can I get a spaceship to orbit the moon?

The need to learn from data

Problem definition

- What problem do we need to solve?
- ► How can we formalise it?
- What properties of the problem can we learn from data?

Data collection

- ► Why do we need data?
- ▶ What data do we need?
- How much data do we want?
- How will we collect the data?

Modelling and decision making

- ► How will we compute something useful?
- ► How can we use the model to make decisions?

Problem definition

► Health, weight and height

Health questions regarding height and weight

- ► What is a normal height and weight?
- How are they related to health?
- What variables affect height and weight?

Data collection

Think about which variables we need to collect to answer our research question.

Necessary variables

The variables we need to know about

- ► Weight
- ► Height
- ► Health issue:

Auxiliary variables

Factors related to height, weight and health

Possible confounders

Other factors that might affect health outcomes, unrelated to height and weight

Class data

The class enters their data into the excel file.

Mean estimation

- ▶ What is the average height/disease prevalence?
- What is the expected height/disease prevalence in the general population?

Supervised learning problems:

- Classification: Can we predict gender from height/weight?
- Regression: Can we predict weight from height and gender?
- In both cases we predict output variables from input variables

Input variables

Also called features, predictors, independent variables

Output variables

Also called response, or dependent variables.



Variables

The class data looks like this

First Name	Gender	Height	Weight	Age	Nationality	Smoking
Lee	М	170	80	20	Chinese	10
Fatemeh	F	150	65	25	Turkey	0
Ali	Male	174	82	19	Turkish	0
Joan	N	5'11	180	21	Brtish	4

► X: Everybody's data

 $\triangleright x_t$: The t-th person's data

 \triangleright $x_{t,k}$: The k-th feature of the \$t\$-th person.

 $ightharpoonup x_k$: Everybody's k-th feature

Raw versus neat data

▶ Neat data: $x_t \in \mathbb{R}^n$

Raw data: text, graphs, missing values, etc



Python pandas for data wrangling

Reading class data

```
import pandas as pd
X = pd.read_excel("data/class.xlsx")
X["First Name"]
```

- ► Array columns correspond to features
- Columns can be accessed through namesx

Summarising class data

```
X.hist()
import matplotlib.pyplot as plt
plt.show()
```

Pandas and DataFrames

- Data in pandas is stored in a DataFrame
- ► DataFrame is not the same as a numpy array.

Core libraries

```
import pandas as pd
import numpy as np
```

Series: A sequence of values

```
# From numpy array:
s = pd.Series(np.random.randn(3), index=["a", "b", "c"])
# From dict:
d = {"a": 1, "b": 0, "c": 2}
s = pd.Series(d)
# accessing elemets
s.iloc[2] #element 2
s.iloc[1:2] #elements 1,2
s.array # gets the array object
s.to_numpy() # gets the underlying numpy array
```

DataFrames

Constructing from a numpy array

```
data = np.random.uniform(size = [3,2])
df = pd.DataFrame(data, index=["John", "Ali", "Sumi"],
    columns=["X1", "X2"])
```

Constructing from a dictionary

Access

```
X["First Name"] # get a column
X.loc[2] # get a row
X.at[2, "First Name"] # row 2, column 'first name'
X.loc[2].at["First Name"] # row 2, element 'first name' of the s
X.iat[2,0] # row 2, column 0
```

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Means using python

Calculating the mean of a random variable

```
import numpy as np
X = np.random.gamma(170, 1, size=20)
X.mean()
np.mean(X)
```

Calculating the mean of our class data

```
X.mean() # gives the mean of all the variables through pandas.co
X["Height"].mean()
np.mean(X["Weight"])
```

One variable: expectations and distributions

Modelling the height

- ► Mean: models the expected value of the population
- ► Variance: models the variance of the population
- ▶ Empirical distribution: models the distribution of the population

The expected value and the mean

Assume $x_t: \Omega \to \mathbb{R}$, and $\omega \sim P$

- $\triangleright x_1, \ldots, x_t, \ldots, x_T$: random i.i.d. variables
- $ightharpoonup \Omega$: random outcome space
- ightharpoonup P: distribution of outcomes $\omega \in \Omega$
- \triangleright $\mathbb{E}_p[x]$: expectation of x under P

$$\mathbb{E}_{P}[x_{t}] = \sum_{\omega \in \Omega} x_{t}(\omega) P(\omega) \approx \frac{1}{T} \sum_{t=1}^{I} x_{t}$$

▶ The sample mean is $O(1/\sqrt{T})$ -close to the expected value.



Reminder: expectations of random variables

A gambling game

What are the expected winnings if you play this game?

- ► [a] With probability 1%, you win 100 CHF
- ▶ [b] With probability 40%, you win 20 CHF.
- ► [c] Otherwise, you win nothing

Solution

Reminder: expectations of random variables

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- ► [a] With probability 1%, you win 100 CHF
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Solution

- Let x be the amount won, then x(a) = 100, x(b) = 20, x(c) = 0.
- We need to calculate

$$\mathbb{E}_{P}(x) = \sum_{\omega \in \{a,b,c\}} x(\omega)P(\omega) = x(a)P(a) + x(b)P(b) + x(c)P(c)$$

$$ightharpoonup P(c)=59\%$$
, as $P(\Omega)=1$. Substituting,
$$\mathbb{E}_P(x)=1+8+0=9.$$

Populations, samples, and distributions

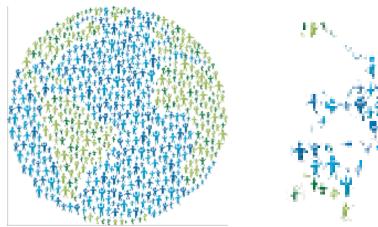


Figure: The world population

Figure: A sample

Two variables: conditional expectation

The height of different genders

Learning from data

Unsupervised learning

- ightharpoonup Given data x_1, \ldots, x_T .
- Learn about the data-generating process.
- Example: Estimation, compression, text/image generation

Supervised learning

- ightharpoonup Given data $(x_1, y_1), \ldots, (x_T, y_T)$
- ▶ Learn about the relationship between x_t and y_t .
- Example: Classification, Regression

Online learning

- ▶ Sequence prediction: At each step t, predict x_{t+1} from x_1, \ldots, x_t .
- Conditional prediction: At each step t, predict y_{t+1} from $x_1, y_1, \dots, x_t, y_t, x_{t+1}$

Reinforcement learning

Learn to act in an unknown world through interaction and rewards



Models

Models as summaries

- They summarise what we can see in the data
- ▶ The ultimate model of the data is the data

Models as predictors

- ► They make predictions about out of sample data
- This requires some assumptions about the data distribution.

Example models

- A numerical mean
- A linear classifier
- A linear regressor
- A deep neural network
- ► A Gaussian process
- A large language model



Validating models

Training data

- ► Calculations, optimisation
- ► Data exploration

Validation data

- ► Fine-tuning
- ► Model selection

Test data

Performance comparison

Simulation

- ► Interactive performance comparison
- White box testing

Real-world testing

► Actual performance measurement



The simplest model: A mean

Robust models of the mean

Model selection

- ► Train/Test/Validate
- ► Cross-validation
- ► Simulation

Course Contents

Models

- k-Nearest Neighbours.
- Linear models and perceptrons.
- Multi-layer perceptrons (aka deep neural networks).
- Bayesian Networks

Algorithms

- ► (Stochastic) Gradient Descent.
- ► Bayesian inference.

Supervised learning

The general goal is learning a function $f: X \to Y$.

Classification

- ▶ Input data $x_t \in \mathbb{R}$, $y_t \in [m] = \{1, 2, ..., m\}$
- Learn a mapping f so that $f(x_t) = y_t$ for unseen data

Regression

- ightharpoonup Input data x_t, y_t
- lackbox Learn a mapping f so that $f(x_t) = \mathbb{E}[y_t]$ for unseen data

Unsupervised learning

The general goal is learning the data distribution.

Compression

- Learn two mappings c, d
- ightharpoonup c(x) compresses an image x to a small representation z.
- ightharpoonup d(z) decompresses to an approximate image \hat{x} .

Density estimation

- lnput data x_1, \ldots, x_T from distribution with density p
- Problem: Estimate p.

Clustering

- ightharpoonup Input data x_1, \ldots, x_T
- ▶ Assign each data x_t . to cluster label c_t .

Supervised learning objectives

- ▶ Data (x_t, y_t) , $x_t \in X$, $y_t \in Y$, $t \in [T]$.
- ▶ i.i.d assumption: $(x_t, y_t) \sim P$ for all t.
- ▶ Supervised decision rule $\pi(a_t|x_t)$

Classification

- Predict the labels correctly, i.e. $a_t = y_t$.
- Have an appropriate confidence level

Regression

- Predict the mean correctly
- Have an appropriate variance around the mean

Unsupervised learning objectives

- ► Reconstruct the data well
- ► Be able to generate data

Reinforcement learning objectives

► Maximise total reward

Pitfalls

Reproducibility

- Modelling assumptions
- Distribution shift
- Interactions and feedback

Fairness

- Implicit biases in training data
- ► Fair decision rules and meritocracy

Privacy

- Accidental data disclosure
- Re-identification risk

ISLP Chapter 1