
CS 361 – Homework 6

Total possible points: 60

1. (15 points) Use a **set notation** to **define** the language generated by the following grammar

$$R \rightarrow TT|U$$

$$T \rightarrow 0T|T0|\#$$

$$U \rightarrow 0U00|\#$$

Consider the following strings. If they are in $L(G)$, derive them.

- a) 00#0000
 - b) ϵ
2. (15 points) Let $A = \{0^n 1^m 0^n 1^m \mid m, n > 0 \text{ and } m \neq n\}$. If A is a context free language, then build the corresponding PDA or CFG. If not, prove that A is not a context-free language using the pumping lemma.
3. (15 points) Let $B = \{a\#b\#c \mid a, b, c \text{ are sequences of } 1\text{'s}; |c| = |a| + |b|; |a| \geq 0; \text{ and } |b| > 0\}$. If B is a context free language, then build the corresponding CFG. If not, use the pumping lemma to show that B is not a context-free language.
4. (15 points) Let $C = \{a^n b^m c^{2n} \mid m, n > 0\}$. If C is a context free language, then build the corresponding PDA. If not, use the pumping lemma to show that C is not a context-free language.

Note that for full credit you need to provide a complete proof, *considering all the possibilities*, as discussed in class.