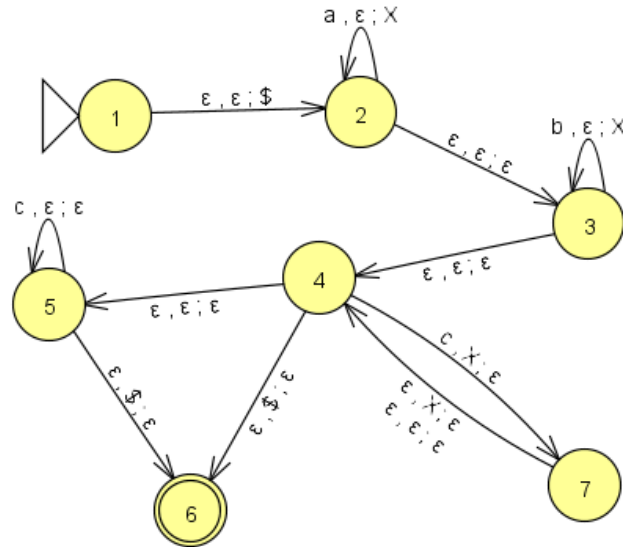


CS 361 – Homework 5

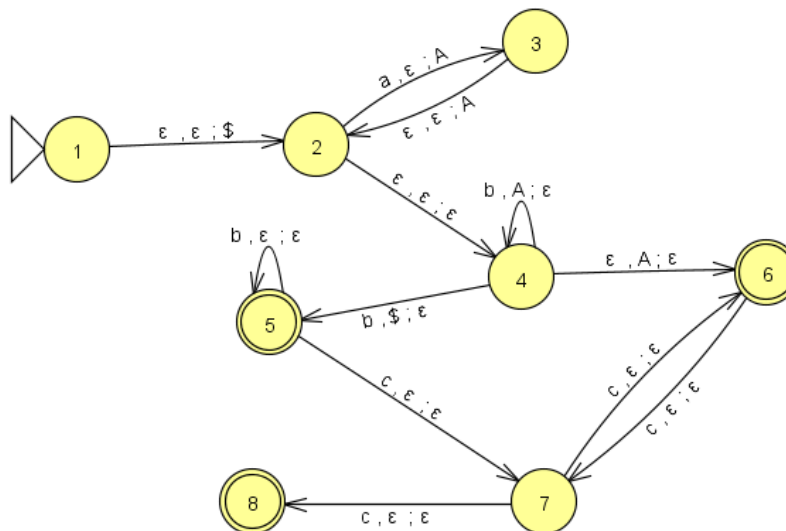
Total possible points: 60

1. (15 points) Construct a **pushdown automaton** for $A = \{a^n b^m c^i \mid 0 \leq n+m \leq 2i\}$

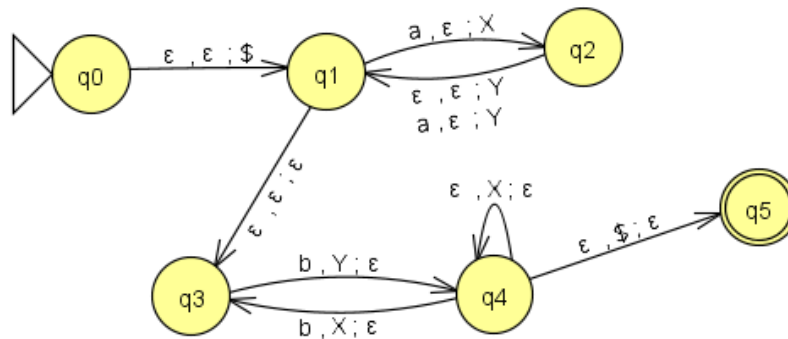
ϵ



2. (15 points) Design a **pushdown automaton** recognizing $B = \{a^n b^m c^i \mid i, n, m > 0, n \neq 2m, i \text{ is even}\}$.



3. (15 points) Design a **pushdown automaton** recognizing $C = \{ a^m b^n \mid m \geq 0, 2m \geq n \geq m \}$



4. (15 points) Consider the following grammar G:

$S \rightarrow 01Sba \mid A$
 $A \rightarrow abA10 \mid \epsilon \mid B$
 $B \rightarrow ccB \mid \epsilon$

- What are the variables of G?
: $V = \{S, A, B\}$
- What are the terminals of G?
: $\Sigma = \{0, 1, a, b, c\}$
- What is the start variable of G?
: start variable = S
- Give 2 strings that are in $L(G)$
: ϵ, cc
- Give 2 strings over the alphabet of G that are not in $L(G)$
: 0110, aaa
- True or False: $R \Rightarrow^* 01abcc10ba$
: True
- True or False: $R \Rightarrow^* 01baccab10$
: False

h. True or False: $R \Rightarrow^* 01ccba$

: True

i. True or False: $R \Rightarrow^* \epsilon$

: True

j. Describe $L(G)$ using set notation, i.e., which types of strings are generated using G

: $L(G) = \{ (01)^a (ab)^b \mid a, b \text{ is greater than } 0 \}$