

Cryptography Assignment - 9

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Question 1:

Suppose a RSA public key is: $n =$

12595317567839835157014997776421103567942015693842958685000057996
17750548880147110509521944049285041602433244172023804646590835427
723055191592144638318476432867385429617360121

$e = 65537$

(a) What is the cipher text if you encrypt your student ID number using the textbook RSA algorithm?

Program:

$n =$

12595317567839835157014997776421103567942015693842958685000057996
17750548880147110509521944049285041602433244172023804646590835427
723055191592144638318476432867385429617360121

$e = 65537$

$id = 113436879$

$R = \text{Integers}(n)$

$result = R(id^e)$

`print("Cipher text is : "+str(result))`

Output:

Cipher text is :

40723575884404770497912623117423434653429728303935981668152316790
52714319812425851310017433832707198823924805011664028991904874893
42100169940025619756518725913337499705913185

```
n = 1259531756783983515701499777642110356794201569384295868500005799617750548880147110509521944049285041602433244172023
e = 65537
id = 113436879
R = Integers(n)
result = R(id^e)
print("Cipher text is : "+str(result))
```

Cipher text is : 4072357588440477049791262311742343465342972830393598166815231679052714319812425851310017433832707198
82392480501166402899190487489342100169940025619756518725913337499705913185

(b) Explain why the textbook RSA is not safe for encrypting student ID numbers. Is the attack cipher text only, known plaintext, chosen plaintext, or chosen cipher text? How can you improve the security of the textbook RSA?

For short messages m we might have $m_e < n$ where m_e is the cipher text and n is the product of p & q , making it possible to decrypt it as e^{th} root extraction which leads to the finding of the plain text for the given cipher text also Chinese remainder theorem can be implemented for breaking the algorithm. Thus, for making the decryption difficult we need to have the messages longer as a result of which the logarithm operation is difficult, for making the message length longer we can follow a technique called padding which adds random digits to the message. Attack is cipher text and known plaintext.

Question 2:

Examine the certificates of your browser, and find the RSA public key, n and e (in decimal) for <https://www.google.com>

Public key (Hexadecimal number):

9c 2a 04 77 5c d8 50 91 3a 06 a3 82 e0 d8 50 48 bc 89 3f f1 19 70 1a 88 46 7e e0
8f c5 f1 89 ce 21 ee 5a fe 61 0d b7 32 44 89 a0 74 0b 53 4f 55 a4 ce 82 62 95 ee eb
59 5f c6 e1 05 80 12 c4 5e 94 3f bc 5b 48 38 f4 53 f7 24 e6 fb 91 e9 15 c4 cf f4 53
0d f4 4a fc 9f 54 de 7d be a0 6b 6f 87 c0 d0 50 1f 28 30 03 40 da 08 73 51 6c 7f ff
3a 3c a7 37 06 8e bd 4b 11 04 eb 7d 24 de e6 f9 fc 31 71 fb 94 d5 60 f3 2e 4a af 42
d2 cb ea c4 6a 1a b2 cc 53 dd 15 4b 8b 1f c8 19 61 1f cd 9d a8 3e 63 2b 84 35 69
65 84 c8 19 c5 46 22 f8 53 95 be e3 80 4a 10 c6 2a ec ba 97 20 11 c7 39 99 10 04
a0 f0 61 7a 95 25 8c 4e 52 75 e2 b6 ed 08 ca 14 fc ce 22 6a b3 4e cf 46 03 97 97 03
7e c0 b1 de 7b af 45 33 cf ba 3e 71 b7 de f4 25 25 c2 0d 35 89 9d 9d fb 0e 11 79
89 1e 37 c5 af 8e 72 69

n (2048 bits) =

19713895149719550196537065661910573762693934593220985668782860735
42706088914079388591906373777830354872491625325260656490417749176
25332956169846177093787397837481001468825436125658259067992821335
10087546060971220666055151463898734279731009956582933624646298029
26583812704620053849659131445894093708218502984561227458484587528
62570572475984749255657759898663106366337682555017481724034308764

60228793912189332026189491067186811703150477068536877439284697584
04186023748939509940265888774558861314239120902426326584230184486
81931804770311659363324209847963477313873639149508954913329761777
15889375379088870580457661428329

e (24 bits) = 65537

Program screenshot:

```
s = "9c 2a 04 77 5c d8 50 91 3a 06 a3 82 e0 d8 50 48 bc 89 3f f1 19 70 1a 88 46 7e e0 8f c5 f1 89 ce 21 ee 5a fe 61 0d 1  
s = s.replace(' ', '')  
p = int(s, 16)  
print(p)
```

197138951497195501965370656619105737626939345932209856687828607354270608891407938859190637377783035487249162532526065
649041774917625332956169846177093787397837481001468825436125658259067992821335100875460609712206660551514638987342797
310099565829336246462980292658381270462005384965913144589409370821850298456122745848458752862570572475984749255657759
898663106366337682555017481724034308764602287939121893320261894910671868117031504770685368774392846975840418602374893
950994026588877455886131423912090242632658423018448681931804770311659363324209847963477313873639149508954913329761777
15889375379088870580457661428329