

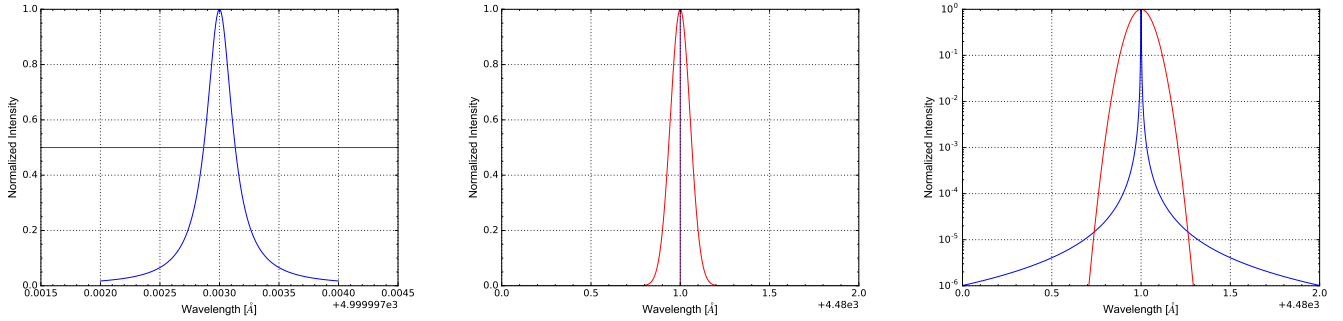
## HW 04: LINE BROADENING

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### 1. NATURAL BROADENING

The equation used to generate the Lorentz profile is provided in equation 1. The profile is shown in figure 1 (left), with a green line to indicate the half maximum intensity. Based on the figure, the full width at half maximum is approximately  $2.5 \times 10^{-4} \text{ \AA}$ , which agrees with  $\Gamma/2\pi$ .

$$\phi_\nu = \frac{\Gamma/4\pi^2}{(\nu - \nu_0)^2 + (\Gamma/4\pi)^2} \quad (1)$$



**Figure 1.** Profiles for Lorentz (left), Doppler (middle), and a combination of the two (right).

### 2. DOPPLER BROADENING

The equation used to generate the Doppler broadening is provided in equation 2. The profile is shown in figure 1 (middle). The  $V_{th}$  and the  $\Delta\lambda_D^2$  found for the Mg II line at 4481 Å were 2.6322 km/s and 0.0787 Å, respectively. The normalized intensity when inputting  $\lambda = \lambda_0 + \Delta\lambda_D^2$  in equation 2, was 0.3679. When both the Lorentz and Doppler profiles are compared, figure 1 (right), the wavelength at which the Lorentz profile is greater than the Doppler is at approximately 4481.27 Å.

$$\exp\left(-\frac{(\lambda - \lambda_0)^2}{\Delta\lambda_D^2}\right) \quad (2)$$

### 3. ROTATION

The stellar parameters in table 1, used for this section were found at the Caltech "Encyclopedia of Astronomy and Astrophysics" (<http://www.astro.caltech.edu/~george/ay20/ea-stellarmasses.pdf>). The highest escape velocities were from spectral class O, and in general, the higher spectral classes. Rotational velocities of the main sequence objects were found in the "Allen-Astrophysical Quantities" reference, and consisted of the  $v_{sin(i)}$  parameters. The maximum rotational broadening were found using the  $v_{sin(i)}$  parameters against the speed of light. For a B-type star, the maximum rotational broadening is approximately 6004 Å.

It cannot be an H-line because of pressure broadening (Stark). The Stark broadening in particular is not sensitive to rotational broadening, therefore it must be a metal line or else Stark broadening dominates the profile.

**Table 1.** Stellar Parameters.

| Spectral Class | Mass<br>[ $M_{\odot}$ ] | Radius<br>[ $R_{\odot}$ ] | Escape Velocity<br>[km/s] | $v_e \sin(i)$<br>[km/s] | Max Rotational Broadening<br>[Å] |
|----------------|-------------------------|---------------------------|---------------------------|-------------------------|----------------------------------|
| O4 V           | 60                      | 10                        | 1513.187402               | 140                     | 4669.897333                      |
| B5 V           | 5                       | 2.7                       | 840.6596678               | 180                     | 6004.153714                      |
| A2 III         | 2.5                     | 3.8                       | 501.0664191               | 160                     | 5337.025523                      |
| F5 V           | 1.25                    | 1.2                       | 630.4947509               | 60                      | 2001.384571                      |
| G8 V           | 1                       | 1.2                       | 563.931649                | 20                      | 667.1281904                      |

NOTE—Stellar parameters found from derivations and catalogs.