

CS3334 Data Structures (2022 Sem A)

Assignment: Hash Table

Name: xxx

SID: xxx

Overview

I have implemented a hash table that follows all the operations mentioned in the requirements document. Namely, for a hash table **T** it is possible to perform following operations:

- InsertKey(x): inserts the key/entry **x** to **T**;
- DeleteKey(x): removes the key/entry **x** from **T**;
- SearchKey(x): searches for the key/entry **x** in **T**: if it is found, returns “x was found”, otherwise, it returns “x does not exist”.

Details

Having stated the general functionality of a hash table, let's talk about the details of its implementation.

Entries

Overall, my version of hash table is basically an **Array** that contains pointers to Entries. In order to get a bigger picture of the hash table, let's first analyze the implementation of Entry:

```
class Entry {
public:
    int key;
    Entry* next;
    Entry() {
        this->key = NULL;
        this->next = NULL;
    }
    Entry(int k) {
        this->key = k;
    }
}
```

The Entry class is implemented in a similar way as a **node** for **linked list**: it has a key and the pointer to a next Entry object. Its default constructor sets both its key and next NULL. Second constructor which asks for (int k) assigns **this->key**.

The reason I have made Entry class this way is because I have decided to handle collisions with separate chaining using **linked lists**.

HashTable Array

The hash table itself is an array of pointers to Entries as mentioned above:

```
const int SIZE = 100000;
class HashTable {
private:
    Entry* array[SIZE];
    string hashFunc;
    double A = 0.543216789;
public:
    HashTable(string s) { //setting every entry NULL initially
        for (int i = 0; i < SIZE; i++) {
            array[i] = new Entry();
        }
        hashFunc = s;
    }
    int hashByDivision(int key) {
```

It has a fixed size of 100000. Its constructor takes a **string** and assigns it as a name to a hashing method **hashFunc**. So it is more convenient to choose which hashing method to try while initializing a hash table.

Hashing functions

The hashing in my hash table is implemented using **Division method** and **Multiplication method**.

```
int hashByDivision(int key) {
    return key % SIZE;
}

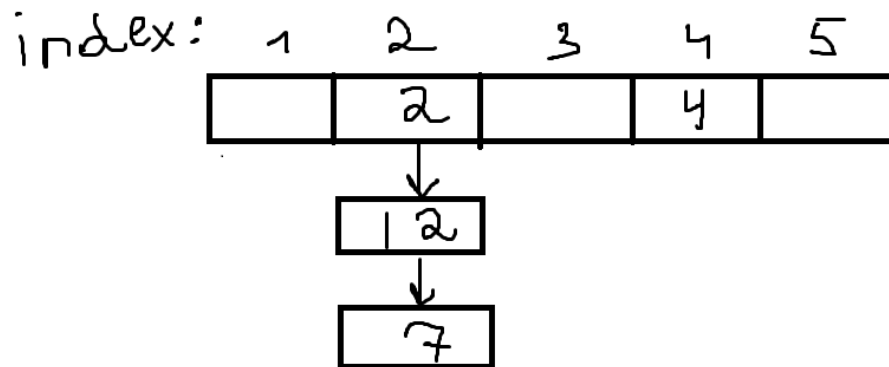
int hashByMultiplication(int key) {
    return floor(SIZE * (fmod(key * A, 1)));
}
```

Note: for a Multiplication method, I have used a **floor()** function from **<cmath>**.

Insert/Delete/Search operations and Collision handling

As mentioned above, I have used **linked lists** to avoid collisions, meaning for instance for a hash table of **size 5** with the following hash function, if **x** is inserted as **2** and then as **12**, then it would have a collision. This is because $2\%5 = 12\%5$. So, the linked list would solve our problem: every time we see a collision, we append a node to an Entry as shown below:

$$h(x) = x \% 5, \quad x = 2, 12, 7, 4$$



```

void insertKey(int k) {
    int h = getHashingMethod(k);

    if (array[h]->key != NULL && array[h]->key != k) {
        Entry* newNode = new Entry(k);
        array[h]->addNode(newNode);
    }
    else {
        array[h] = new Entry(k);
    }
}

```

Insert

```

void deleteKey(int k) {
    int h = getHashingMethod(k);

    if (array[h]->key != NULL) {
        if (array[h]->key != k) {
            array[h]->removeNode(k);
        }
        else {
            array[h] = new Entry();
        }
        printf("%d was deleted successfully\n", k);
    }
    else {
        printf("%d does not exist\n", k);
    }
}

```

Delete

```

void searchKey(int k) {
    int h = getHashingMethod(k);

    if (this->hasKey(k)) {
        printf("%d was found\n", k);
    }
    else {
        printf("%d does not exist\n", k);
    }
}

```

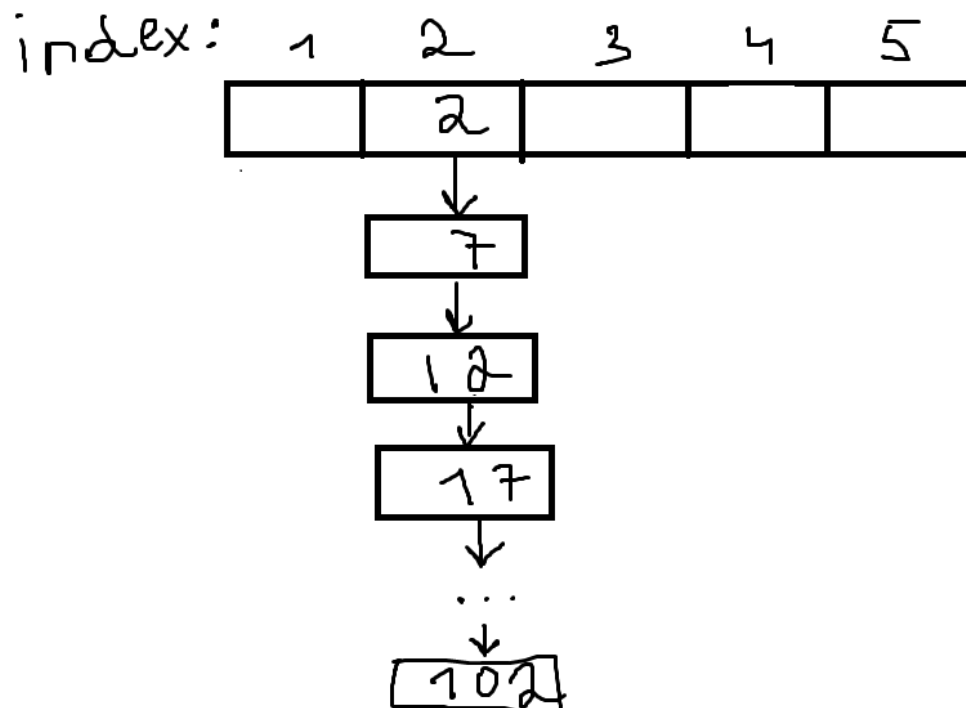
Search

Time complexity analysis

The **average time complexity** for all those 3 operations is **$O(1)$ – constant time**. This is because on average, we assume that no collision happens. Hence, looking up a key in an array takes constant time.

The **worst case scenario** for my hash table is when every insertion causes collision: meaning for instance for the previous example with $h(x)=x\%5$, if the keys were **2,7,12,17,22,...,102**, the hash table might look like this:

$$h(x) = x \% 5, \quad x = 2, 7, 12, \dots, 102$$



This would mean that every insertion/deletion/search operation would take $O(n)$ where n is the **number of keys/entries linked** together. This is because in order to search for a key, it should traverse **one-by-one** until it reaches the point. If we assume that the searched key is the **tail** of the linked list, it takes traversal of every key as well.

On the other hand, it is also worth noting that this method of separate chaining does not depend on the size of the array. Naturally, the type of hashing does not fully prevent collision and with linked list approach like this, we can see that it does not affect its performance. However, it should also be pointed that multiplication hashing method is more suitable for large size of array.

Testing

Here are short instructions on how to execute cpp files. Once you have downloaded the zip file, unpack it and then change the cmd directory to it using 'cd file_path' command. Then, if you type 'g++ .\sampleGenerator.cpp -o exec_file' or 'g++ .\Source.cpp -o exec_file', you will create an exec file ready for execution. The 'Source.cpp' file was for OJ system, while 'sampleGenerator' was given from the canvas, though, I have made some changes to its code (see SampleGenerator.cpp section below).

CityU CS ACM Programming Team Online Judge System

First, after the implementation of the hash table, I checked it in the OJ system. Both **Division** and **Multiplication** methods passed the testcases. The runtime for both were fairly the same. However, when I changed the hash table array size from 100000 to 10000, the difference between the two methods rocketed. In fact, the **Division** method implementation was the **6th** fastest in the OJ records:

Top 30 Solvers

Rank	ID	User	Run Time (sec.)	Memory (KB)	Submission Time
1	232271	kendall	0.004	1724	2022-11-29 00:03:54
2	231764	唐新荣	0.004	11456	2022-11-28 14:43:08
3	231473	57159984 - TSOI Tsz Chun	0.005	1472	2022-11-28 02:14:28
4	230702	Eklavya Agarwal	0.005	1820	2022-11-26 15:38:19
5	233116	haz	0.005	17568	2022-11-29 22:16:58
6	233864	loili	0.006	2444	2022-11-30 19:15:56
7	251747	simul	0.014	1764	2022-11-28 14:29:03

This also supports my statement that for less number of array size, **the Division** method is more suitable.

I have test my code with the C++ 11, flag: -static -std=c++0x compiler in the OJ.

SampleGenerator.cpp

Additionally, in order check the correctness of my implementation, I have used the **sampleGenerator.cpp** source code, which uses `<unordered_set>`. I have made little changes to a code, so that whenever the unordered set searches for a key and decides that it **exists** and my hash table, on the contrary, decides that it **does not**, I printed out those records (Also, vice-versa, when the unordered says it **does not exist**, while my hash table says it **does**).

Microsoft Visual Studio Debug Console

1.54251s

for Division method (SIZE= 10^5)

Microsoft Visual Studio Debug Console

1.54517s

for Multiplication method (SIZE= 10^5).

Here, we can see that both have the same performance time. However, if we set size of an array to **10000** now

Microsoft Visual Studio Debug Console

1.49716s

for Division method (SIZE= 10^4)

Microsoft Visual Studio Debug Console

1.55399s

for Multiplication method (SIZE= 10^4).

Now we can conclude that on practicality, the Division methods performs much faster than the Multiplication if the size of an array is less, which further confirms my statement mentioned above.