VFQ 25 - Example

Installing smartPROM

If you are using smartPROM for the first time, install it from the github repo. We need the devtools library to install libraries from github.

```
library(devtools)
install_github("byet/smartPROM")
```

Analysis

```
library(smartPROM)

##
## Attaching package: 'smartPROM'

## The following object is masked from 'package:base':
##
## cat
Read the dataset
```

Discretize the states

In this example, we will discretize the vfq overall score into two states: H = above 75, L = below 75.

df <- read.csv("./data/Cleaned_and_scored_VFQ25.csv")</pre>

You can discretize into more than two intervals by providing a vector to cutoff. Note that, number of states should be one more than number of cutoffs. e.g. 'discretize(df\$OverallScore, cutoff=C(25,75), states = c('L','M','H'))

```
intv <- discretize(df$OverallScore, cutoff=75, states = c('L','H'))</pre>
```

We also have a function that ensures disretised intervals are larger than MCID and have about the same size. But this'd be an overkill for this example.

```
intv <- mipm_intervals(df$OverallScore, threshold=75, MCID= 15, states = c('L','H'), n_interval = 2, Lo
```

Measured and Target variables.

We will use questions 1-14, 18-25 as our measured variables. These will be potential inputs that will be asked in our evaluations. We ignored the questions about driving in this example as they had many missing values (non-drivers).

Our target variable is the discretized score we created above. We name it lf in our analysis.

```
measured <- paste0("vfq", c(1,2,3,4,5,6,7,8,9,10,11,12,13,14,18,19,20,21,22,23,24,25))
target <- "lf"
n_measured <- length(measured)

# Dataset composed of just inputs and target variable.
dfq <- df[measured]
dfq[target] <- intv</pre>
```

Learn BN

We use a Naive BN structure in this example. We could have used BN structure built by experts or data-driven structure learning algorithms.

```
naive_bn_dfq <- naivebn_arcs(target, measured)
bn <- learn_bn(dfq, arc_set= naive_bn_dfq, na_omit = TRUE)</pre>
```

Computerized Adaptive Testing with BNs

cat_iterations iteratively asks questions from measured by using the CAT algorithm. For, every question selected by CAT, we enter the data regarding this question to the BN and get the posterior probability of target after entering the data.

Below, we run cat_iterations for the first row of our dataset.

```
res\_iter <- \ cat\_iterations (bn, \ data = dfq[1,], \ target=target, \ query = measured, \ num\_iter = n\_measured \ ,
```

Results

 $distance_{to_all_queries}$ compares the probability distribution of target variables when we enter the responses of first x questions entered with CAT to when we enter the responses for all the questions.

```
1.014484e-02
                   2.478380e-03
                                   7.252465e-04
                                                  2.891743e-05
                                                                 8.610211e-06
##
##
               lf
                              lf
                                              1f
                                                             lf
                                                                            lf
##
    2.934647e-06
                   5.769667e-07
                                   1.438398e-07
                                                  1.585806e-08
                                                                 3.477396e-09
##
               lf
                              1f
                                              lf
                                                             ٦f
                                                                            1f
##
    3.081990e-10
                   9.663592e-12
                                   3.323775e-12
                                                  4.292030e-13
                                                                 1.509818e-13
##
                              lf
                                              1f
                                                             1f
                                                                            ٦f
               lf
    7.681942e-14
                                   2.214861e-15
                                                  2.184704e-16 -1.754270e-18
##
                   2.214861e-15
##
               lf
                              1f
##
    0.000000e+00
                   0.00000e+00
```

Below we use errorAllQuestion to compare the accuracy of predicting target variables when different number of inputs are entered with CAT. This is for only the first row of data.

```
errorAllQuestions(res_iter$bns, dfq[1,], measured,numericStates = FALSE)
```

```
##
                              [,2]
                                                    [,4]
                                                               [,5]
                                                                          [,6]
                                                                                     [,7]
                   [,1]
                                         [,3]
## Accuracy 0.8181818 0.8181818 0.8181818 0.8181818 0.8181818 0.8181818 0.8181818
                     NA
                               NA
                                           NA
                                                      NA
                                                                 NA
                                                                            NA
                                                                                       NA
                   [,8]
                              [,9]
                                        [,10]
                                                   [,11]
                                                                         [,13]
                                                                                    [,14]
##
                                                              [,12]
   Accuracy 0.8181818 0.8181818 0.8181818 0.8181818 0.8181818 0.8181818 0.8181818
##
##
   MAE
                     NA
                               NA
                                           NA
                                                                            NA
                                                                                       NA
                                                      NA
                                                                 NA
                                                                         [,20]
                  [,15]
                             [,16]
                                        [,17]
                                                   [,18]
                                                              [,19]
                                                                                    [,21]
## Accuracy 0.8181818 0.8181818 0.8181818 0.8181818 0.8181818 0.8636364 0.9090909
## MAE
                     NA
                                NA
                                           NA
                                                      NA
                                                                 NA
                                                                            NA
                                                                                       NA
##
                  [,22]
## Accuracy 0.9090909
```

Below we use errorAllQuestion to compare the accuracy of predicting responses to unanswered questions when different number of inputs are entered with CAT. This is for only the first row of data.

```
errorAllQuestions(res_iter$bns, dfq[1,], target, numericStates = FALSE)
             [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13]
##
## Accuracy
                                      1
                                            1
                                                       1
                                                                                1
                                                                                      1
                                                           {\tt NA}
## MAE
               NA
                    NA
                          NA
                               NA
                                     NA
                                          NA
                                                NA
                                                     NA
                                                                 NA
                                                                        NA
                                                                               NA
                                                                                     NA
##
             [,14]
                   [,15] [,16] [,17] [,18]
                                              [,19] [,20] [,21] [,22]
## Accuracy
                        1
                              1
                                     1
                                            1
                                                  1
                                                         1
                                                               1
                 1
## MAE
                             NA
                                    NA
                NA
                       NA
                                          NA
                                                 NA
```

To get the error for all data, we need to compute this for all rows of data and get the average.

Running cat for all the data

Below we run CAT for all rows of data.

Below we compute the area under the curve for target variable prediction when different number of questions are selected with CAT.

```
perf <- performance(res, dfq, targetVars = target)
perf</pre>
```

```
##
             lf
     0.9029526
## 1
## 2
     0.9358327
## 3
     0.9447682
## 4
     0.9759000
## 5
     0.9761461
## 6
     0.9782699
## 7
     0.9834758
## 8 0.9843564
## 9 0.9868816
## 10 0.9867392
## 11 0.9869593
## 12 0.9881896
## 13 0.9883061
## 14 0.9875939
## 15 0.9871018
## 16 0.9870500
## 17 0.9873608
## 18 0.9879565
## 19 0.9881637
## 20 0.9881896
## 21 0.9873867
## 22 0.9874385
```