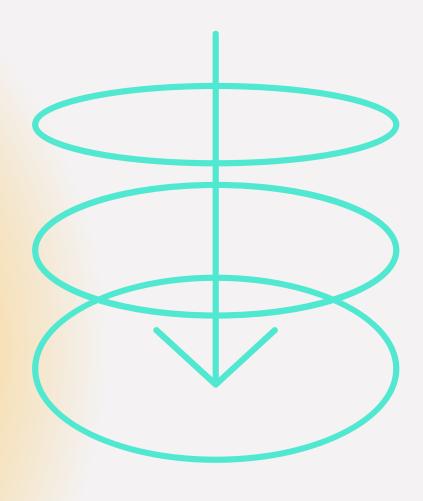
Introduction to



non-linear dimensionality reduction



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9°A

Team 5

01 - Definition

- Unsupervised dimensionality reduction technique.
- For data exploration and visualizing highdimensional data.
- It separate data that cannot be separate by a line.
- Easiest to use when features are numeric.



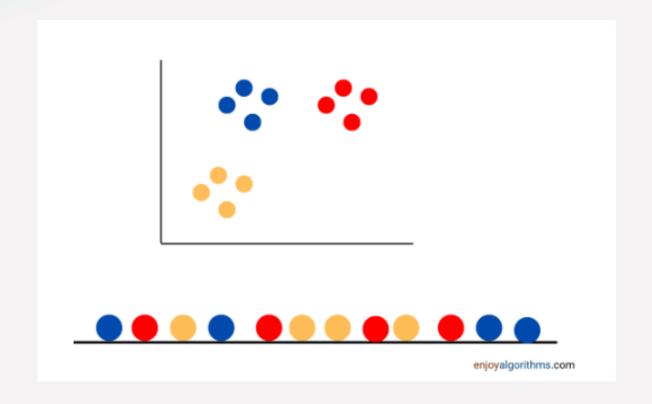




02 - How it works

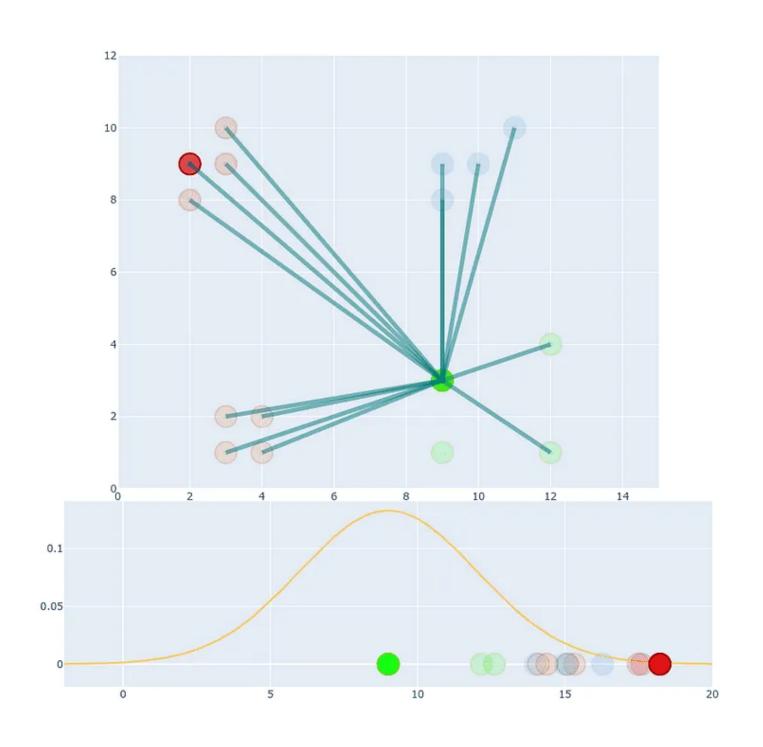
- 1. Similarity Measure
- 2. Mapping to Lower Dimension
- 3. Divergence Minimization
- 4. Cluster Formation





03 - Steps

- 1. Calculate joint probabilities (Gaussian).
- 2. Low dimension space.
- 3. Calculate joint probabilities (t-distribution).
- 4. Calculate divergence.
- 5. Optimize.

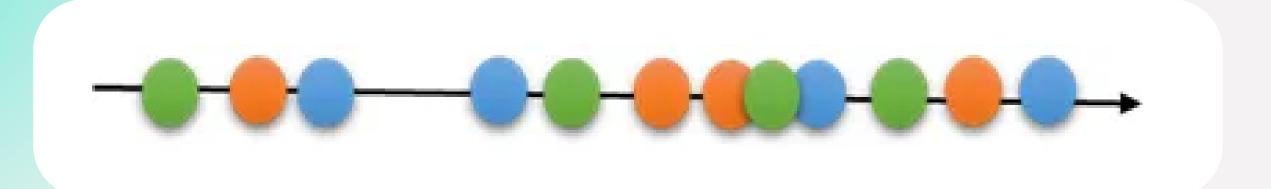


$$p_{j|i} = \frac{\exp(-||x_i - x_j||^2/2\sigma_i^2)}{\sum_{k \neq i} \exp(-||x_i - x_k||^2/2\sigma_i^2)},$$

$$p_{ij} = \frac{p_{j|i} + p_{i|j}}{2n}$$

Gaussian distribution

t distribution

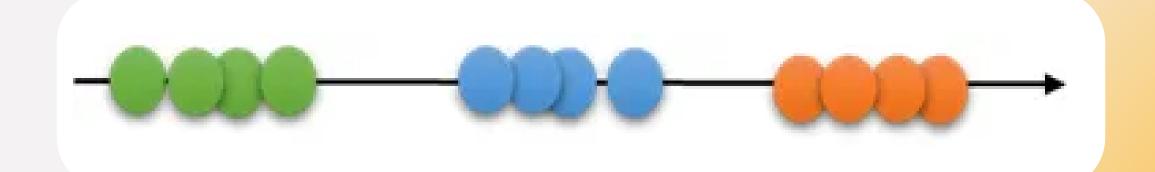


$$q_{ij} = \frac{\left(1 + \|y_i - y_j\|^2\right)^{-1}}{\sum_{k \neq l} \left(1 + \|y_k - y_l\|^2\right)^{-1}}$$

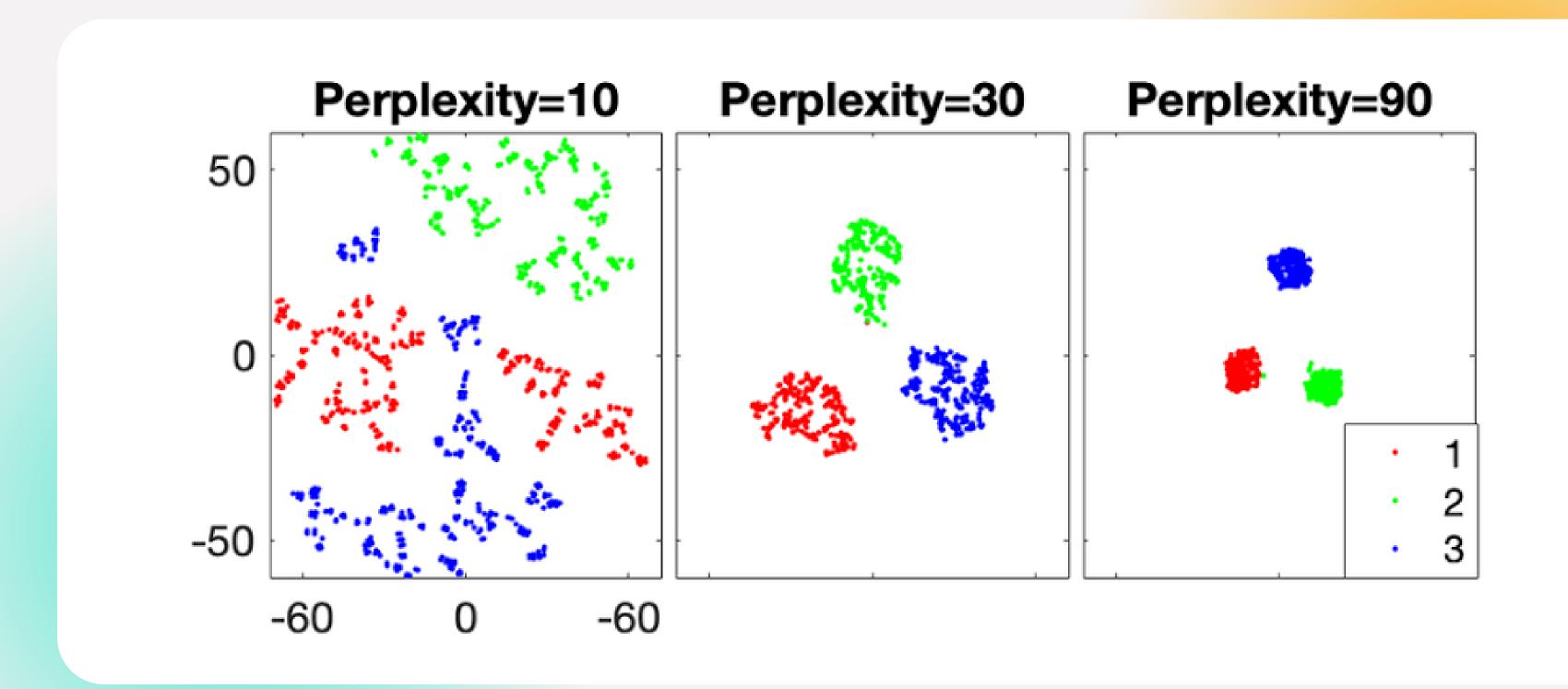
Kullback-Leiber divergence

$$C = D_{\mathrm{KL}}(P \parallel Q) = \sum_{x \in \mathcal{X}} P(x) \log \left(rac{P(x)}{Q(x)}
ight)$$

$$C = KL(P||Q) = \sum_{i} \sum_{j} p_{ij} \log \frac{p_{ij}}{q_{ij}}$$

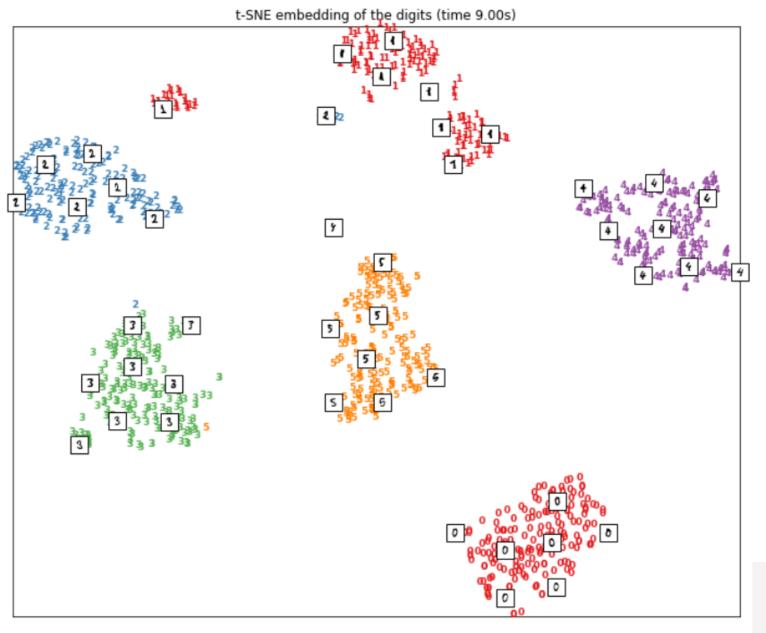


04 - t-SNE perplexity



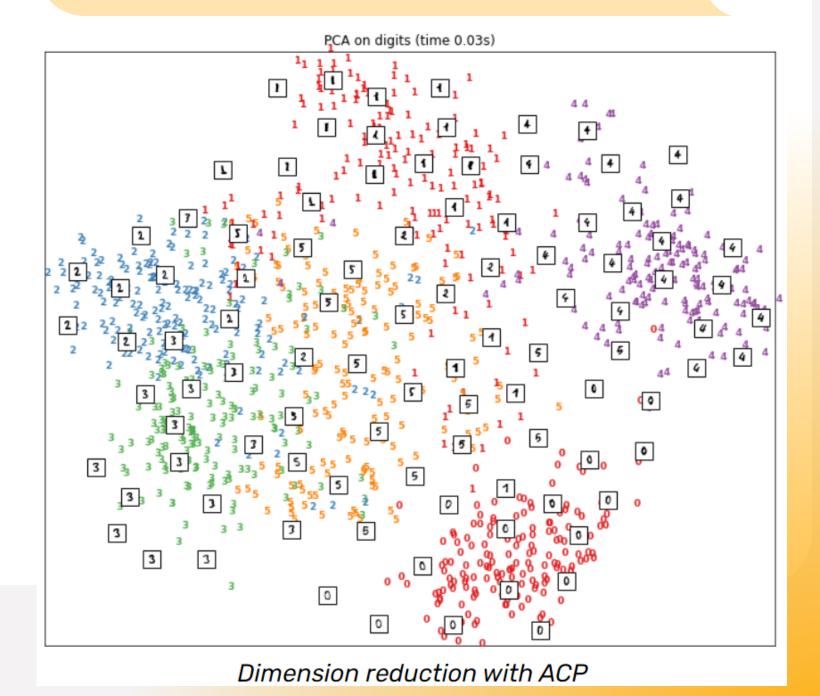
05 - TSN-E vs PCA

- Nonlinear technique.
- Lower dimensional space.



Dimension reduction with the t-SNE method

Preserving large pairwise distances.Maximize variance.



06 - Advantages and Disadvantages

Advantages

- 1. Handles Non-linear Data
- 2. Preserves Local Structure

Disadvantages

- 1. Computational Complexity
- 2. Non-Deterministic



07-References

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 September 2023, from https://www.enjoyalgorithms.com/blog/tsne-algorithm-in-ml
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THANKS!