

$$\text{Breezy}(\bar{z}) \Rightarrow \text{Pit}(\bar{z}+\hat{x}) \vee \text{Pit}(\bar{z}-\hat{x}) \vee \text{Pit}(\bar{z}+\hat{y}) \vee \text{Pit}(\bar{z}-\hat{y})$$

$$\neg \text{Breezy}(\bar{z}) \Rightarrow \neg \text{Pit}(\bar{z}+\hat{x}) \wedge \neg \text{Pit}(\bar{z}-\hat{x}) \wedge \neg \text{Pit}(\bar{z}+\hat{y}) \wedge \neg \text{Pit}(\bar{z}-\hat{y})$$

$$\text{Safe}(\bar{z}) \Rightarrow \neg \text{Pit}(\bar{z})$$

$$\text{Breezy}(\bar{a})$$

Knowledge base:

-Pervasive rules: (CNF)

$$\text{At}(\text{agent}, \bar{z}) \Rightarrow$$

Store in 3D array

1<sup>st</sup> dim: Clauses

2<sup>nd</sup> dim: literals

3<sup>rd</sup> dim: Negation, type, value.

$$\text{E.g. } (\text{P}(x) \vee x) \wedge (\neg x \vee a)$$

$$\Rightarrow \{\text{P}(x) \vee x, \neg x \vee a\}$$

$$\Rightarrow \begin{pmatrix} \text{P}(x), & x \\ \neg x, & a \end{pmatrix}$$

$$\Rightarrow \begin{pmatrix} 0 \\ \text{func} \\ *x \end{pmatrix}, \begin{pmatrix} 0 \\ \text{var} \\ *x \end{pmatrix}$$

$$\Rightarrow \begin{pmatrix} 1 \\ \text{var} \\ *x \end{pmatrix}, \begin{pmatrix} 0 \\ \text{const} \\ a \end{pmatrix}$$

-World rules

Store in 3D array of booleans.

1<sup>st</sup>, 2<sup>nd</sup> dim = x, y coordinate

3<sup>rd</sup> dim (bitwise) predicate - 64 predicates to work with

Then the knowledge can be in

1<sup>st</sup> dim: clause

2<sup>nd</sup> dim: literals.

3<sup>rd</sup> dim: x, y, z coordinate of storage area.

Convert above rules to CNF

$$[\neg \text{Breezy}(\bar{z}) \vee \text{Pit}(\bar{z}+\hat{x}) \vee \text{Pit}(\bar{z}-\hat{x}) \vee \text{Pit}(\bar{z}+\hat{y}) \vee \text{Pit}(\bar{z}-\hat{y})]$$

$$[\text{Breezy}(\bar{z}) \vee \neg \text{Pit}(\bar{z}-\hat{x})]$$

$$[\text{Breezy}(\bar{z}) \vee \neg \text{Pit}(\bar{z}+\hat{x})]$$

$$[\text{Breezy}(\bar{z}) \vee \neg \text{Pit}(\bar{z}-\hat{y})]$$

$$[\text{Breezy}(\bar{z}) \vee \neg \text{Pit}(\bar{z}+\hat{y})]$$

$$[\neg \text{Safe}(\bar{z}) \vee \neg \text{Pit}(\bar{z})] \quad \text{Safe}(\bar{z}) \Rightarrow \neg \text{Pit}(\bar{z})$$

Static Rules

$$\begin{aligned} & \neg \text{Breezy}(\tilde{s}) \vee \neg \text{Pit}(\tilde{s} + \hat{y}) \\ & [\neg \text{Safe}(\tilde{s}) \vee \neg \text{Pit}(\tilde{s})] \quad \text{Safe}(\tilde{s}) \Rightarrow \neg \text{Pit}(\tilde{s}) \\ & [\text{Safe}(\tilde{s}) \vee \text{Pit}(\tilde{s})] \quad \neg \text{Safe}(\tilde{s}) \Rightarrow \text{Pit}(\tilde{s}) \end{aligned}$$

Dynamic Rewrites

$$\neg \text{Breezy}(\tilde{a})$$

$$\text{Prove: } \neg \text{Safe}(\tilde{a} + \hat{x}) \quad \text{Safe}(\tilde{s}) \vee \text{Pit}(\tilde{s})$$

$$\theta = \{\tilde{s} / \tilde{a} + \hat{x}\}$$

$$\text{Pit}(\tilde{a} + \hat{x}) \quad \text{Breezy}(\tilde{s}) \vee \neg \text{Pit}(\text{East}(\tilde{s}))$$

$$\theta = \{\text{East}(\tilde{s}) / \tilde{a} + \hat{x}\}$$

$$\text{Breezy}(\tilde{a}) \quad \Rightarrow \tilde{s} = \text{West}(\tilde{a} + \hat{x})$$



$$\text{North}(\tilde{r}, \tilde{s}) \Rightarrow \tilde{r} = \tilde{s} + \hat{y}$$

$$\text{Breezy}(\tilde{a} + \hat{x})$$

Replace, using NSEW predicates

In CNF form

$$[\neg \text{Breezy}(\tilde{s}) \vee \text{East}(\tilde{s}, \tilde{r}) \vee \text{North}(\tilde{s}, \tilde{r}) \vee \text{South}(\tilde{s}, \tilde{r}) \vee \text{West}(\tilde{s}, \tilde{r})]$$

$$[\neg \text{Breezy}(\tilde{s}) \vee \text{Pit}(\tilde{r})]$$

$$[\text{Breezy}(\tilde{s}) \vee \neg \text{East}(\tilde{s}, \tilde{r}) \vee \neg \text{North}(\tilde{s}, \tilde{r}) \vee \neg \text{South}(\tilde{s}, \tilde{r}) \vee \neg \text{West}(\tilde{s}, \tilde{r}) \vee \neg \text{Pit}(\tilde{r})]$$

$$[\neg \text{Pit}(\tilde{s}) \vee \neg \text{Safe}(\tilde{s})]$$

$$[\text{Pit}(\tilde{s}) \vee \text{Safe}(\tilde{s})]$$

$$\neg \text{Breezy}(\tilde{a})$$

Literal  
class atom { type, val }

↑  
const/var/ hopefully not function.

$$\text{Prove: Safe}(\tilde{a} + \hat{x})$$

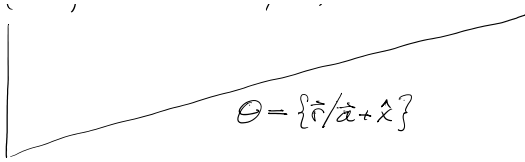
$$\neg \text{Safe}(\tilde{a} + \hat{x})$$

$$\text{Pit}(\tilde{s}) \vee \text{Safe}(\tilde{s})$$

$$\theta = \{\tilde{s} / \tilde{a} + \hat{x}\}$$

$$\text{Pit}(\tilde{a} + \hat{x})$$

$$\text{Breezy}(\tilde{s}) \vee \neg \text{East}(\tilde{s}, \tilde{r}) \vee \neg \text{North}(\tilde{s}, \tilde{r}) \vee \neg \text{South}(\tilde{s}, \tilde{r}) \vee \neg \text{West}(\tilde{s}, \tilde{r}) \vee \neg \text{Pit}(\tilde{r})$$



$$Breezy(\hat{s}) \vee \neg East(\hat{s}, \hat{a} + \hat{x}) \vee \neg North(\hat{s}, \hat{a} + \hat{x}) \vee \neg South(\hat{s}, \hat{a} + \hat{x}) \vee \neg West(\hat{s}, \hat{a} + \hat{x})$$

How about a function for NEW

$$\neg Breezy(\hat{s}) \vee Pit(East(\hat{s})) \vee Pit(North(\hat{s})) \vee Pit(South(\hat{s})) \vee Pit(West(\hat{s}))$$

$$Breezy(\hat{s}) \vee \neg Pit(East(\hat{s}))$$

$$Breezy(\hat{s}) \vee \neg Pit(North(\hat{s}))$$

$$Breezy(\hat{s}) \vee \neg Pit(South(\hat{s}))$$

$$Breezy(\hat{s}) \vee \neg Pit(West(\hat{s}))$$

$$\neg Pit(\hat{s}) \vee \neg Safe(\hat{s})$$

$$Pit(\hat{s}) \vee Safe(\hat{s}) \quad Breezy$$

$$Breezy(\hat{a})$$

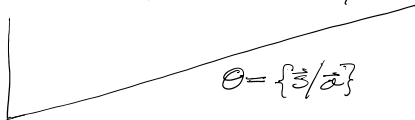
Data structure

Prove Safe(North( $\hat{a}$ ))

$$\Rightarrow \neg Safe(North(\hat{a})) \quad Pit(\hat{s}) \vee Safe(\hat{s})$$



$$Pit(North(\hat{a})) \quad Breezy(\hat{s}) \vee \neg Pit(North(\hat{s}))$$



$$Breezy(\hat{a})$$

$$\neg Pit(East(\hat{s})) \quad Pit(\hat{s})$$

$$\begin{pmatrix} \neg Pit \\ East(\hat{s}) \end{pmatrix} \quad \begin{pmatrix} Pit \\ lin \\ \hat{s} \end{pmatrix}$$

$$Pred(func1(\hat{s}_1, \hat{s}_2), func2(\hat{s}_1, \hat{s}_2))$$

$$kb[i, j] == tuple(int, vectuple(int, vec<int>))$$

$$\begin{array}{ccc} \uparrow & \uparrow & \uparrow \\ Pred/neg & funct & var/const. \end{array}$$

$$\{Pred1, [(func1, "var1, var2, \dots"), (func2, "var1, var2, \dots"), \dots]\}, \{Pred2, [(func1, "var1, var2, \dots"), (func2, "var1, var2, \dots"), \dots]\} \setminus n$$

## Wumpus Rules

$$\text{Stinky}(\tilde{s}, t) \Rightarrow \text{Wumpus}(\text{North}(\tilde{s}), t) \vee \text{Wumpus}(\text{South}(\tilde{s}), t) \vee \text{Wumpus}(\text{East}(\tilde{s}), t) \vee \text{Wumpus}(\text{West}(\tilde{s}), t)$$

$$\neg \text{Stinky}(\tilde{s}, t) \Rightarrow \neg \text{Wumpus}(\text{North}(\tilde{s}), t) \wedge \neg \text{Wumpus}(\text{South}(\tilde{s}), t) \wedge \neg \text{Wumpus}(\text{East}(\tilde{s}), t) \wedge \neg \text{Wumpus}(\text{West}(\tilde{s}), t)$$

$$\text{Scream}(\tilde{s}, t_1) \Rightarrow \neg \text{Wumpus}(\tilde{s}, t_2) \wedge \text{GreaterThan}(t_2, t_1)$$

$$\text{Wumpus}(\tilde{s}, t) \wedge \text{AgentAt}(\tilde{r}, t) \wedge [\text{SameX}(\tilde{r}, \tilde{s}) \vee \text{SameY}(\tilde{r}, \tilde{s})] \Rightarrow \text{Shoot}(\text{direction}(\tilde{r}, \tilde{s}))$$

We still need to determine how to incorporate walls!!

returns the direction of  $\tilde{r}$   
from  $\tilde{s}$ . Undefined if diagonal.

## Questions

- Is the current implementation "cheating" since resolution takes only one step?
- Can we ever locate pits/Wumpi exactly?
- Is it acceptable to chain inference engines?
- Does the scream predicate have an associated position?
- Does resolving the same clause twice ever give new information?