

**NOTE:** Problems are graded at 10 pts. each, unless indicated otherwise.

- 31 [Jackson Prob. (14.2)]. Using the Larmor formulas for the nonrelativistic motion of a point charge  $q$ , find the time-averaged quantities:  $\langle dP/d\Omega \rangle$  = power radiated per unit solid angle, and  $\langle P \rangle$  = total power radiated, when  $q$  moves as follows...
- (A)... along the  $z$ -axis with instantaneous position:  $z(t) = R \cos \omega_0 t$  ( $R$  &  $\omega_0$  = const);
- (B)... in a circle of radius  $R$  in the  $xy$  plane, at frequency  $\omega_0$  ( $R$  &  $\omega_0$  = const).
- In each case, sketch the angular distribution of the radiation. Is there a significant difference in  $\langle P \rangle$  for the linear motion vs. the circular motion?

- 32 [Jackson Prob. (14.3)]. A nonrelativistic particle of mass  $m$ , charge  $Ze$ , and initial kinetic energy  $K$  collides head-on with a fixed central force field. The interaction is repulsive, and is specified by a potential  $V(r)$ :  $V(r)$  increases as the separation  $r$  decreases, and  $V(r) > K$  for all  $r < r_0$  (so  $r_0$  = "closest distance of approach").

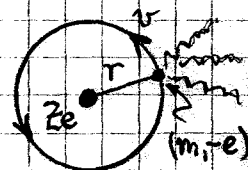
(A) Show that the total energy radiated by  $Ze$  during this encounter is ...

$$\Delta W = \frac{4}{3c} \left( \frac{Ze}{mc} \right)^2 \sqrt{\frac{m}{2}} \int_{r_0}^{\infty} \left| \frac{dV}{dr} \right|^2 \frac{dr}{\sqrt{V(r_0) - V(r)}}.$$

(B) Let the potential be Coulombic:  $V(r) = ZZe^2/r$ . If  $v_0$  is the velocity of  $Ze$  at infinity, show the radiated energy is:

$$\Delta W = \frac{16}{45} (Z/Z_0) (v_0/c)^3 K \ll K.$$

- 33 An electron (mass  $m$ , charge  $(-e)$ ), in a hydrogenlike atom (stationary nucleus of charge  $Ze$ ), moves in a circular orbit of radius  $r$ . Treat the system classically, and assume the electron velocity  $v \ll c$ .



- (A) Find an expression for the electron's total orbit energy  $E$  in terms of  $r$  alone.
- (B) Assume the electron radiates energy  $\Delta E \ll |E|$ , per orbit. Find the radiated power  $P$  in terms of  $r$  alone. Equate  $P$  to the rate of loss of orbital energy, to obtain a differential eqn for the decrease in orbit radius  $r$  due to radiation.
- (C) Calculate the elapsed time for the electron to spiral into the nucleus if it starts from  $r = a_0$ . Set  $Z=1$ ,  $a_0 = 0.53 \text{ \AA}$  (Bohr radius). Calculate a number for the collapse time.