Midterm 2 Equations	PHSX519 Electron
$\nabla \cdot \mathbf{D} = \rho_f, \nabla \times \mathbf{E} = 0, \nabla \cdot \mathbf{B} = 0, \nabla > 0$	$\mathbf{G} \mathbf{H} = \mathbf{J}_f$ Maxwell's equations in matter
$\mathbf{E}(\mathbf{x}) = \frac{1}{4\pi\epsilon_0} \int \rho(\mathbf{x}') \frac{\mathbf{x} - \mathbf{x}'}{ \mathbf{x} - \mathbf{x}' ^3} d^3x'$	Coulomb's Law (1.5)
$\delta(f(x)) = \sum_{i} \frac{1}{\left \frac{\mathrm{d}f}{\mathrm{d}x}(x_{i})\right } \delta(x - x_{i})$	Delta function Rule 5
$\oint_{S} \mathbf{E} \cdot \mathbf{n} \ da = \frac{1}{\epsilon_{0}} \int_{V} \rho(\mathbf{x}) d^{3}x$	Gauss' Law (1.11)
	etric field in terms of scalar potential (1.16)
$\Phi(\mathbf{x}) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\mathbf{x}')}{ \mathbf{x} - \mathbf{x}' } d^3x'$ Scalar	r potential in terms of charge density (1.17)
$\nabla^2 \Phi = -\rho/\epsilon_0$	Poisson Equation (1.28)
$\Phi(\mathbf{x}) = \frac{1}{4\pi\epsilon_0} \int_V \rho(\mathbf{x}') G_D(\mathbf{x}, \mathbf{x}') d^3 x' = \frac{1}{4\pi} \oint_S$	$(\mathbf{x}')\frac{\partial G_D}{\partial n'}da'$ DBCs (1.44)
$\Phi(\mathbf{x}) = \langle \Phi \rangle_S + \frac{1}{4\pi\epsilon_0} \int_V \rho(\mathbf{x}') G_N(\mathbf{x}, \mathbf{x}') d^3x + \frac{1}{4\pi\epsilon_0} \int_V \rho(\mathbf{x}') G_N(\mathbf{x}') d^3x + \frac{1}{4\pi\epsilon_0} \int_V \rho(\mathbf{x}') G_N(\mathbf{x}') d^3x + \frac{1}{4\pi\epsilon_0} \int_V \rho(\mathbf{x}') G_N(\mathbf{x}') d^3x + \frac{1}{4\pi\epsilon_0} \int_V \rho(\mathbf{x}') d^3x + \frac{1}{4\pi\epsilon_0}$	$\frac{1}{4\pi} \oint_{S} \frac{\partial \Phi}{\partial n'} G_N da' \qquad \qquad \text{NBCs (1.46)}$
$\frac{1}{ \mathbf{x} - \mathbf{x'} } = 4\pi \sum_{\ell=0}^{\infty} \sum_{m=-\ell}^{\ell} \frac{1}{2\ell+1} \frac{r_{\ell}^{\ell}}{r_{\ell}^{\ell+1}} Y_{\ell m}^{*}(\boldsymbol{\theta'}, \boldsymbol{\theta'})$	$\phi')Y_{\ell m}(\theta,\phi)$ GFE: r,θ,ϕ (3.70)
$\frac{1}{ \mathbf{x} - \mathbf{x}' } = \frac{2}{\pi} \sum_{m=-\infty}^{\infty} \int_{0}^{\infty} dk e^{im(\phi - \phi')} \cos[k]$	$(z - z')]I_m(k\rho_{<})K_m(k\rho_{>})$ GFE (3.148)
Where $r_{<}(r_{>})$ [$\rho_{<}(\rho_{>})$] is the smaller (larger) of $ \mathbf{x} $ and $ \mathbf{x'} $
$\Phi(\mathbf{x}) = \frac{1}{4\pi\epsilon_0} \sum_{l=0}^{\infty} \sum_{m=-l}^{l} \frac{4\pi}{2l+1} q_{lm} \frac{Y_{lm}}{r^{l+1}}$	Potential outside spher of charge (4.1)
$q_{lm} = \int Y_{lm}^*(\boldsymbol{\theta}', \boldsymbol{\phi}') r'^l \rho(\mathbf{x}') \ d^3x'$	Multipole moments (4.3)
$q = \int \rho(\mathbf{x'}) \ d^3x'$	Monopole (4.4)
$\mathbf{p} = \int \mathbf{x}' \rho(\mathbf{x}') \ d^3 x'$	Dipole (4.8)
$Q_{ij} = \int (3x_i'x_j' - r'\delta_{ij})\rho(\mathbf{x}')d^3x' = 3M_{ij} - 7$	$\operatorname{Tr}(\mathbf{M}\delta_{ij})$ Quadrupole (4.9)
$M_{ij} = \int x_i' x_j' \rho(x') \ d^3x$	Dana definition
$\Phi(\mathbf{x}) = \frac{1}{4\pi\epsilon_0} \left[\frac{q}{r} + \frac{\mathbf{p} \cdot \mathbf{x}}{r^3} + \frac{1}{2} \sum_{i,j} Q_{ij} \frac{x_i x_j}{r^5} + . \right]$] Multipole Expansion (4.10)
$\mathbf{D} = \epsilon_0 \mathbf{E} + \mathbf{P}$ $\mathbf{P} = \epsilon_0 \chi_e \mathbf{E}$	Electric displacement (4.34) Induced polarization (4.36)
$\mathbf{P} = (\epsilon - \epsilon_0)\mathbf{E}$	Better expression for polarization
$\mathbf{D} = \epsilon \mathbf{E}$ $\epsilon = \epsilon_0 (1 + \chi_e)$	Electric displacement (4.37) Electric permittivity (4.38)
$\begin{split} & \sigma_b = \mathbf{P} \cdot \hat{\mathbf{n}}, \rho_b = - \nabla \cdot \mathbf{P} \\ & \begin{cases} (\mathbf{D}_2 - \mathbf{D}_1) \cdot \mathbf{n}_{21} = \sigma \\ (\mathbf{E}_2 - \mathbf{E}_1) \times \mathbf{n}_{21} = 0 \end{cases} \end{split}$	Electric bound charge density (G. 4.11) Boundary conditions (4.40)
$ \oint \Phi_{\rm in} = -\left(\frac{3}{\epsilon/\epsilon_0 + 2}\right) E_0 r \cos \theta $	Dielectric sphere in $\mathbf{E}=E_0\mathbf{\hat{z}}$ (4.54)
$\begin{cases} \Phi_{\text{out}} = -E_0 r \cos \theta + \left(\frac{\epsilon/\epsilon_0 - 1}{\epsilon/\epsilon_0 + 2}\right) E_0 \frac{a^3}{r^2} \cos \theta \\ W = \int \rho(\mathbf{x}) \Phi(\mathbf{x}) \ d^3 x = \frac{1}{r} \int \mathbf{E} \cdot \mathbf{D} \ d^3 x \end{cases}$	Energy to bring charges from ∞ (4.83,89)
$\Delta W = -\frac{1}{2} \int_{V_1} \mathbf{P} \cdot \mathbf{E}_0 \ d^3 x$	Dielectric placed in \mathbf{E}_0 (4.93)
$W = q\Phi(0) - \mathbf{p} \cdot \mathbf{E}(0) - \frac{1}{6} \sum_{i} \sum_{j} Q_{ij} \frac{\partial E_{j}}{\partial x_{i}}(0) +$	Work multipole expsn. (4.24)
$\mathbf{N} = \mathbf{p} imes \mathbf{E}$	Torque on electric dipole (G. 4.4)
$\mathbf{F} = (\mathbf{P} \cdot \mathbf{\nabla})\mathbf{E}$ $\begin{pmatrix} a^3 \end{pmatrix}$	Force on electric dipole (G. 4.5)
$\Phi = -E_0 \left(r - rac{a^3}{r^2} ight)$ Electric poten $E_T = rac{2p\cos\theta}{4\pi\epsilon_0}, E_\theta = rac{2p\sin\theta}{4\pi\epsilon_0}$	tial of conducting sphere in ${\bf E}=E_0{\bf \hat{z}}$ (2.14) Electric dipole at origin in ${\bf \hat{z}}$ (4.12)
$\mathbf{E}_{r} = \frac{1}{4\pi\epsilon_{0}}, \mathbf{E}_{\theta} = \frac{1}{4\pi\epsilon_{0}}$ $\mathbf{E}(\mathbf{x}) = \frac{3\mathbf{n}(\mathbf{p} \cdot \mathbf{n}) - \mathbf{p}}{4\pi\epsilon_{0} \mathbf{x} - \mathbf{x}_{0} ^{3}}$	E-field due to dipole p (4.13)
$N = m \times B$	Torque on magnetic dipole moment (5.1)
$\nabla \cdot \mathbf{J} = 0$ $d\mathbf{B} = kI \frac{d1 \times \mathbf{x}}{ \mathbf{x} ^3}$	Condition of magnetostatics (5.3) Biot-Savart Law (5.4)
$\oint_C \mathbf{B} \cdot d\mathbf{l} = \mu_0 I$	Ampère's law (5.25)
$\mathbf{B}(\mathbf{x}) = \nabla \times \mathbf{A}(\mathbf{x})$	Magnetic vector potential (5.27)
$\mathbf{A}(\mathbf{x}) = \frac{\mu_0}{4\pi} \int \frac{\mathbf{J}(\mathbf{x'})}{ \mathbf{x} - \mathbf{x'} } d^3 x'$ Magnetic ve	ector potential of current distribution (5.32)
$\mathbf{m} = \frac{1}{2} \int \mathbf{x}' \times \mathbf{J}(\mathbf{x}') \ d^3 x$	Magnetic moment definition (5.54)
$\mathbf{m} = \frac{I}{2} \oint \mathbf{x} \times d\mathbf{l}$ Mag	gnetic moment of closed circuit (J. pg. 186)
$ \mathbf{m} = I \times (\text{Area})$ $u_0 \ \mathbf{m} \times \mathbf{x}$	Magnetic moment of plane loop (5.57)
$\mathbf{A}(\mathbf{x}) = \frac{\mu_0}{4\pi} \frac{\mathbf{m} \times \mathbf{x}}{ \mathbf{x} ^3}$	Dipole vector potential (5.55)
$\mathbf{B}(\mathbf{x}) = \frac{\mu_0}{4\pi} \left[\frac{3\mathbf{n}(\mathbf{n} \cdot \mathbf{m}) - \mathbf{m}}{ \mathbf{x} ^3} \right]$	Dipole induction (5.56)
$\mathbf{F} = \mathbf{\nabla}(\mathbf{m} \cdot \mathbf{B})$	Force on dipole (5.69)

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Magnetic field (5.81)				$\mathbf{H} = \frac{1}{\mu_0} \mathbf{B} - \mathbf{M}$
ation in linear media (G. 6.29) Linear condition (5.84)	Magnetiza			$\mathbf{M} = (\mu/\mu_0 - 1)$ $\mathbf{B} = \mu\mathbf{H}$
Interface BC (5.86)			a = 0 $a = \mathbf{K} c$	$\begin{cases} (\mathbf{B}_2 - \mathbf{B}_1) \cdot \mathbf{n} \\ \mathbf{n} \times (\mathbf{H}_2 - \mathbf{H}_1) \end{cases}$
Iagnetic scalar potential (5.93) and current density (G. 6.13,14) gnetic charge density (5.96,99)	Bound		$\mathbf{K}_b = \mathbf{M} \times \mathbf{n}$	$\mathbf{H} = -\nabla \Phi_{M}$ $\mathbf{J}_{M} = \nabla \times \mathbf{M},$ $\mathbf{\rho}_{M} = -\nabla \cdot \mathbf{M},$
potential of dipole (J. pg. 196)	netic scalar p			$\Phi_M(\mathbf{x}) = \frac{\mathbf{m} \cdot \mathbf{x}}{4\pi r^3}$
magnetic moment (J. pg. 197)	Total r			$\mathbf{m} = \int \mathbf{M} d^3x$
gnetic vector potential (5.101)	terms of mag	oisson equation i	Poi	$\nabla^2 \mathbf{A} = -\mu_0 \mathbf{J}_M$
Discontinuous M (5.103)	$\frac{\mathbf{n'}}{\mathbf{x'}} da'$	$x^3 x + \frac{\mu_0}{4\pi} \oint_S \frac{\mathbf{M}(\mathbf{x})}{ \mathbf{x} }$	$\frac{\mathbf{\nabla}' \times \mathbf{M}(\mathbf{x}')}{ \mathbf{x} - \mathbf{x}' } \ d^3 \mathbf{x}$	$\mathbf{A}(\mathbf{x}) = \frac{\mu_0}{4\pi} \int_V \mathbf{x}$
$M_0\hat{\mathbf{z}} \ [(r_{<}, r_{>}), \ (r, a)] \ (5.104)$	e with M = N	Sph	$I_0 a^2 \frac{r_{<}}{r_{>}^2} \cos \theta$	$\Phi_M(r,\theta) = \frac{1}{3}M_0$
Form magnetic field ${f B}_0$ (5.115)	phere in unifo	Permeable		$\mathbf{M} = \frac{3}{\mu_0} \left(\frac{\mu - \mu}{\mu + 2} \right)$
Magnetic flux (5.133)			ı	$F = \int_{S} \mathbf{B} \cdot \mathbf{n} \ da$
Electromotive force (5.134)				$\mathscr{E} = \oint_C \mathbf{E}' \cdot d\mathbf{l}$
Faraday's Law (5.135)				$\mathscr{E} = -k \frac{\mathrm{d}F}{\mathrm{d}t}$
arrent from zero (4.83)::(5.149)	y to ramp cur	Ener	d^3x	$W = \frac{1}{2} \int \mathbf{J} \cdot \mathbf{A} \ d$
energy in fields (4.89)::(5.148)	Magnetic e			$W = \frac{1}{2} \int \mathbf{H} \cdot \mathbf{B}$
Power in magetic field (5.147)	I			$\frac{\mathrm{d}W}{\mathrm{d}t} = \int \mathbf{H} \cdot \frac{\mathrm{d}\mathbf{I}}{\mathrm{d}}$
ble object in B ₀ (4.93)::(5.150)	lace permeabl	Energy to	$\mathbf{I} \cdot \mathbf{B}_0 \ d^3 x$	$\Delta W = \frac{1}{2} \int_{V_1} \mathbf{M}$
Change in energy due to EMF				$\frac{\mathrm{d}W}{\mathrm{d}t} = -\int \mathbf{J} \cdot \mathbf{F}$
N ferromagnets (HW 8.2b)	$M_i(\mathbf{x}) d^3x$	$\sum_{1}^{N} \sum_{j=1}^{N} \int \Phi_{M_{j}}(\mathbf{x}) d\mathbf{x}$	$d^{3}x = \frac{\mu_{0}}{2} \sum_{i=1}^{N} \int_{0}^{1} d^{3}x = \frac{\mu_{0}}{2} \int_{0}^{1} d^{3}x = \frac{\mu_{0}}$	$W = \frac{\mu_0}{2} \int \mathbf{H} ^2$
Inductive energy (5.152)		$_{ij}I_{i}I_{j}$	$a_{i}^{2} + \sum_{i=1}^{N} \sum_{j>i}^{N} M_{ij}$	$W = \frac{1}{2} \sum_{i=1}^{N} L_i I_i^2$
Mutual inductance (5.156)				$M_{ij} = \frac{1}{I_j} F_{ij}$
		L	$(0,z) - \left(\frac{\rho^2}{4}\right) \left[\frac{\partial}{\partial z}\right]$	
φ−sym, near origin (J Pr. 5.4)			$\left(\frac{\rho}{2}\right)\frac{\partial B_z(0,z)}{\partial z} +$	` 2
$\int_0^\infty J_1(ka)J_1(k\rho) \ dk$ A of current ring (J. PR. 5.10)		$I_1(k\rho <)K_1(k\rho >$	$\frac{a}{-} \int_0^\infty \cos(kz) I_1$	$A_{\phi}(\rho, z) = \frac{\mu_0 I \alpha}{\pi}$
Field of dipole (G 5.87,88)	in $\theta \hat{\boldsymbol{\theta}})$	$\frac{\mu_0 m}{4\pi r^3} (2\cos\theta \hat{\mathbf{r}} +$	$\frac{\sin \theta}{2} \Rightarrow \mathbf{B}_{\text{dip}} = \frac{\mu}{4}$	$\mathbf{A}_{\text{dip}} = \frac{\mu_0}{4\pi} \frac{m \sin r^2}{r^2}$
Mechanical torque		17.7	$\mathbf{r} = \mathbf{r} \times \mathbf{F}$	$\tau = I\alpha = -\frac{\partial W}{\partial \theta}$
				$I = \int r^2 \rho(x, y, z)$
Moment of inertia			$\partial^2 W$	
	$\frac{a^2 W}{2a^2} < 0 \Rightarrow U$	$= 0 \Rightarrow Saddle,$	able, $\frac{\partial}{\partial a^2} = 0$	$\frac{\partial^2 W}{\partial a^2} > 0 \Rightarrow Sta$
	- 1		table, $\frac{\partial}{\partial q^2} = 0$ $+ na^{n-1}x + \frac{n(r)}{r}$	~ 1
Unstable	=	$\frac{a(n-1)}{2!}a^{n-2}x^2$	~ 1	$(a+x)^n = a^n +$
Unstable Binomial Expansion Taylor Series $\sin \theta \sin \phi \cos \theta$ $\cos \theta \sin \phi -\sin \theta$ $\cos \phi 0$ $\begin{pmatrix} \hat{\mathbf{x}} \\ \hat{\mathbf{z}} \end{pmatrix}$	$ \begin{array}{l} \vdots \\ \vdots \\ \sin \theta \cos \phi \\ \cos \theta \cos \phi \\ -\sin \phi \end{array} $	$\frac{a(n-1)}{2!}a^{n-2}x^{2}$ $\frac{f''(a)}{2!}(x-a)^{2}$ $\begin{vmatrix} \hat{\mathbf{x}} \\ \hat{\mathbf{y}} \\ \hat{\mathbf{z}} \end{vmatrix}, \begin{pmatrix} \hat{\mathbf{f}} \\ \hat{\boldsymbol{\theta}} \\ \hat{\boldsymbol{\phi}} \end{pmatrix} =$	$+ na^{n-1}x + \frac{n(\tau)}{\tau}$	$f(x) \approx f(a) + \frac{f}{f(x)}$ $f(x) \approx f(a) + \frac{f}{f(a)}$ $\begin{cases} \hat{p} \\ \hat{\phi} \\ \hat{z} \end{cases} = \begin{pmatrix} \cos \phi \\ -\sin \phi \\ 0 \end{pmatrix}$
Unstable Binomial Expansion Taylor Series	$ \begin{array}{l} \vdots \\ \vdots \\ \sin \theta \cos \phi \\ \cos \theta \cos \phi \\ -\sin \phi \end{array} $	$\frac{a(n-1)}{2!}a^{n-2}x^{2}$ $\frac{f''(a)}{2!}(x-a)^{2}$ $\begin{vmatrix} \hat{\mathbf{x}} \\ \hat{\mathbf{y}} \\ \hat{\mathbf{z}} \end{vmatrix}, \begin{pmatrix} \hat{\mathbf{f}} \\ \hat{\boldsymbol{\theta}} \\ \hat{\boldsymbol{\phi}} \end{pmatrix} =$	$+ na^{n-1}x + \frac{n(\tau)}{\tau}$	$f(x) \approx f(a) + \frac{f}{f(x)}$ $f(x) \approx f(a) + \frac{f}{f(a)}$ $\begin{cases} \hat{p} \\ \hat{\phi} \\ \hat{z} \end{cases} = \begin{pmatrix} \cos \phi \\ -\sin \phi \\ 0 \end{pmatrix}$
Unstable Binomial Expansion Taylor Series $\sin \theta \sin \phi \cos \theta$ $\cos \theta \sin \phi - \sin \theta$ $\cos \phi$ 0 $\begin{bmatrix} \hat{\mathbf{x}} \\ \hat{\mathbf{y}} \\ \hat{\mathbf{z}} \end{bmatrix}$ $\begin{bmatrix} z/\sqrt{\rho^2 + z^2} & 0 \\ 0 & 1 \\ -\rho/\sqrt{\rho^2 + z^2} & 0 \end{bmatrix}$ $\begin{bmatrix} \hat{\mathbf{r}} \\ \hat{\theta} \\ \hat{\phi} \end{bmatrix}$ Decaying	$\begin{array}{l} -1\\ -\dots =\\ \\ \dots\\ \left(\sin\theta\cos\phi\\ \cos\theta\cos\phi\\ -\sin\phi \right)\\ \left(\rho/\sqrt{\rho^2+z^2}\right)\\ 0\\ z/\sqrt{\rho^2+z^2} \end{array}$	$\frac{t(n-1)}{2!}a^{n-2}x^{2}$ $\frac{f''(a)}{2!}(x-a)^{2}$ $\begin{pmatrix} \hat{\mathbf{x}} \\ \hat{\mathbf{y}} \\ \hat{\mathbf{z}} \end{pmatrix}, \begin{pmatrix} \hat{\mathbf{f}} \\ \hat{\boldsymbol{\theta}} \\ \hat{\boldsymbol{\phi}} \end{pmatrix} =$ $\begin{pmatrix} \hat{\boldsymbol{\rho}} \\ \hat{\boldsymbol{\phi}} \\ \hat{\mathbf{z}} \end{pmatrix}, \begin{pmatrix} \hat{\boldsymbol{\rho}} \\ \hat{\boldsymbol{\phi}} \\ \hat{\boldsymbol{z}} \end{pmatrix} =$ dly	$+ na^{n-1}x + \frac{n(r)}{r}$ $\frac{f'(a)}{1!}(x-a) + \frac{f}{r}$ $\phi \sin \phi 0$ $\phi \cos \phi 0$ $0 -\sin \theta$ $1 0$ Wiggly	$f(a+x)^n = a^n + f(x) \approx f(a) + \frac{f}{\hat{\phi}}$ $\begin{pmatrix} \hat{\rho} \\ \hat{\phi} \\ \hat{z} \end{pmatrix} = \begin{pmatrix} \cos \phi \\ -\sin \phi \\ \hat{\phi} \\ \hat{\phi} \end{pmatrix} = \begin{pmatrix} \sin \theta \\ \cos \theta \\ 0 \end{pmatrix}$
Unstable Binomial Expansion Taylor Series $\sin \theta \sin \phi \cos \theta \cos \phi \sin \phi$ $\cos \phi \sin \phi$ $\cos \phi 0$ $z/\sqrt{\rho^2 + z^2} 0$ $0 1$ $-\rho/\sqrt{\rho^2 + z^2} 0$ Decaying $1 \cosh(k_n x) + B \sinh(k_n x)$	$\dots = \dots$ $(\sin \theta \cos \phi \cos \phi \cos \phi - \sin \phi)$ $(\rho/\sqrt{\rho^2 + z^2})$ $(\pi/\sqrt{\rho^2 + z^2})$ $(\pi/\sqrt{\rho^2 + z^2})$	$\frac{a(n-1)}{2!} a^{n-2} x^{2}$ $\frac{f''(a)}{2!} (x-a)^{2}$ $\begin{pmatrix} \hat{\mathbf{x}} \\ \hat{\mathbf{y}} \end{pmatrix}, \begin{pmatrix} \hat{\mathbf{p}} \\ \hat{\boldsymbol{\theta}} \\ \hat{\boldsymbol{\phi}} \end{pmatrix} =$ $\begin{pmatrix} \hat{\boldsymbol{p}} \\ \hat{\boldsymbol{\phi}} \end{pmatrix}, \begin{pmatrix} \hat{\boldsymbol{p}} \\ \hat{\boldsymbol{\theta}} \\ \hat{\boldsymbol{z}} \end{pmatrix} =$ $\frac{dy}{dx} + B \sin(k_{n}x)$	$+ na^{n-1}x + \frac{n(r)}{r}$ $+ na^{n-1}x + n(r$	$(a+x)^n = a^n + \frac{1}{2}$ $f(x) \approx f(a) + \frac{f}{2}$ $\begin{pmatrix} \hat{\rho} \\ \hat{\phi} \\ \hat{z} \end{pmatrix} = \begin{pmatrix} \cos \phi \\ -\sin \phi \\ 0 \end{pmatrix}$ $\begin{pmatrix} \hat{\mathbf{r}} \\ \hat{\phi} \\ \hat{\phi} \end{pmatrix} = \begin{pmatrix} \sin \theta \\ \cos \theta \\ 0 \end{pmatrix}$ $x, y, z \qquad e^{\pm ik}$
Unstable Binomial Expansion Taylor Series $\sin \theta \sin \phi \cos \theta \cos \phi \sin \phi$ $\cos \phi \sin \phi$ $\cos \phi 0$ $z/\sqrt{\rho^2 + z^2} 0$ $\frac{0}{1} -\rho/\sqrt{\rho^2 + z^2} 0$ Decaying $1 \cosh(k_n x) + B \sinh(k_n x)$ $(k_n \rho) + BK_m(k_n \rho)$	$\dots = \dots$ $(\sin \theta \cos \phi \cos \phi \cos \phi \cos \phi - \sin \phi)$ $(\rho/\sqrt{\rho^2 + z^2})$ $(z/\sqrt{\rho^2 + z^2})$ $e^{\pm k_n x}, A$ $AI_m($	$\frac{a(n-1)}{2!}a^{n-2}x^{2}$ $\frac{f''(a)}{2!}(x-a)^{2}$ $\begin{pmatrix} \hat{\mathbf{x}} \\ \hat{\mathbf{y}} \\ \hat{\mathbf{z}} \end{pmatrix}, \begin{pmatrix} \hat{\mathbf{f}} \\ \hat{\boldsymbol{\theta}} \\ \hat{\boldsymbol{\phi}} \end{pmatrix} =$ $\begin{pmatrix} \hat{\boldsymbol{\theta}} \\ \hat{\boldsymbol{\phi}} \\ \hat{\boldsymbol{z}} \end{pmatrix}, \begin{pmatrix} \hat{\boldsymbol{\theta}} \\ \hat{\boldsymbol{\phi}} \\ \hat{\boldsymbol{z}} \end{pmatrix} =$ $\frac{1}{2}dy$ $\frac{1}{2}dy + B\sin(k_{n}x)$ $\frac{1}{2}dy + B\sin(k_{n}x)$ $\frac{1}{2}dy + B\sin(k_{n}x)$	$+ na^{n-1}x + \frac{n(r)}{r}$ $\frac{f'(a)}{1!}(x-a) + \frac{f}{r}$ $\phi \sin \phi 0$ $\phi \cos \phi 0$ $0 -\sin \theta$ $1 0$ Wiggly	$(a+x)^n = a^n + \frac{1}{2}$ $f(x) \approx f(a) + \frac{f}{2}$ $\begin{pmatrix} \hat{p} \\ \hat{\phi} \\ \hat{\phi} \end{pmatrix} = \begin{pmatrix} \cos \phi \\ -\sin \phi \\ 0 \end{pmatrix}$ $\begin{pmatrix} \hat{\mathbf{r}} \\ \hat{\theta} \\ \hat{\phi} \end{pmatrix} = \begin{pmatrix} \sin \theta \\ \cos \theta \\ 0 \end{pmatrix}$ $\frac{x}{\rho}, \psi, z \qquad e^{\pm ik}$
Unstable Binomial Expansion Taylor Series $\sin \theta \sin \phi \cos \theta \cos \phi \sin \phi$ $\cos \phi \sin \phi$ $\cos \phi 0$ $z/\sqrt{\rho^2 + z^2} 0$ $0 1$ $-\rho/\sqrt{\rho^2 + z^2} 0$ Decaying $1 \cosh(k_n x) + B \sinh(k_n x)$	$\begin{array}{l} \dots \\ \dots \\ (\sin\theta\cos\phi \\ \cos\theta\cos\phi \\ -\sin\phi \\ (\rho/\sqrt{\rho^2+z^2} \\ 0 \\ z/\sqrt{\rho^2+z^2} \\ e^{\pm k_n x}, A_{Im}(A_0+B_0 \ln A_1) \end{array}$	$\frac{(n-1)}{2!}a^{n-2}x^{2}$ $\frac{f''(a)}{2!}(x-a)^{2}$ $\begin{pmatrix} \hat{\mathbf{g}} \\ \hat{\mathbf{y}} \\ \hat{\mathbf{g}} \end{pmatrix}, \begin{pmatrix} \hat{\mathbf{f}} \\ \hat{\boldsymbol{\phi}} \\ \hat{\boldsymbol{\phi}} \end{pmatrix} =$ $\begin{pmatrix} \hat{\boldsymbol{\rho}} \\ \hat{\boldsymbol{\phi}} \\ \hat{\boldsymbol{\phi}} \end{pmatrix}, \begin{pmatrix} \hat{\boldsymbol{\rho}} \\ \hat{\boldsymbol{\phi}} \\ \hat{\boldsymbol{\phi}} \end{pmatrix} =$ $\frac{(\mathbf{g})}{2} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g}$ $\frac{(\mathbf{g})}{2} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g}$ $\frac{(\mathbf{g})}{2} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g}$ $\frac{(\mathbf{g})}{2} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g}$ $\frac{(\mathbf{g})}{2} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g}$ $\frac{(\mathbf{g})}{2} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g}$ $\frac{(\mathbf{g})}{2} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g}$ $\frac{(\mathbf{g})}{2} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g}$ $\frac{(\mathbf{g})}{2} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g}$ $\frac{(\mathbf{g})}{2} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g}$ $\frac{(\mathbf{g})}{2} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g} \cdot \mathbf{g}$ $\frac{(\mathbf{g})}{2} \cdot \mathbf{g} \cdot \mathbf{g}$ $\frac{(\mathbf{g})}{2} \cdot \mathbf{g} \cdot \mathbf{g}$ $\frac{(\mathbf{g})}{2} \cdot \mathbf{g} \cdot $	$+ na^{n-1}x + \frac{n(r)}{r}$ $+ na^{n-1}x + n(r$	$(a+x)^n = a^n + \frac{1}{2}$ $f(x) \approx f(a) + \frac{f}{2}$ $\begin{pmatrix} \hat{\rho} \\ \hat{\phi} \\ \hat{z} \end{pmatrix} = \begin{pmatrix} \cos \phi \\ -\sin \phi \\ 0 \end{pmatrix}$ $\begin{pmatrix} \hat{\mathbf{r}} \\ \hat{\phi} \\ \hat{\phi} \end{pmatrix} = \begin{pmatrix} \sin \theta \\ \cos \theta \\ 0 \end{pmatrix}$ $x, y, z \qquad e^{\pm ik}$