

$$a = \frac{k1}{\omega} (\alpha1 - \beta1) - \frac{k2}{\omega} \alpha2 == 0$$

$$b = \alpha1 + \beta1 == \alpha2$$

$$-\frac{k2 \alpha2}{\omega} + \frac{k1 (\alpha1 - \beta1)}{\omega} == 0$$

$$\alpha1 + \beta1 == \alpha2$$

Solve[a && b, {α2, β1}] // FullSimplify

$$\left\{ \left\{ \alpha2 \rightarrow \frac{2 k1 \alpha1}{k1 + k2}, \beta1 \rightarrow \frac{(k1 - k2) \alpha1}{k1 + k2} \right\} \right\}$$

$$R = \frac{1 - \sqrt{\epsilon / \epsilon_0 + I \sigma / \epsilon_0 \omega}}{1 + \sqrt{\epsilon / \epsilon_0 + I \sigma / \epsilon_0 \omega}}$$

$$\frac{1 - \sqrt{\frac{\epsilon}{\epsilon_0} + \frac{i \sigma \omega}{\epsilon_0}}}{1 + \sqrt{\frac{\epsilon}{\epsilon_0} + \frac{i \sigma \omega}{\epsilon_0}}}$$

A = ComplexExpand[Re[R]] // FullSimplify

$$-\frac{-1 + \sqrt{\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}}}{1 + 2 \cos\left[\frac{1}{2} \operatorname{Arg}\left[\frac{\epsilon + i \sigma \omega}{\epsilon_0}\right]\right] \left(\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}\right)^{1/4} + \sqrt{\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}}}$$

B = ComplexExpand[Im[R]] // FullSimplify

$$-\frac{2 \sin\left[\frac{1}{2} \operatorname{Arg}\left[\frac{\epsilon + i \sigma \omega}{\epsilon_0}\right]\right] \left(\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}\right)^{1/4}}{1 + 2 \cos\left[\frac{1}{2} \operatorname{Arg}\left[\frac{\epsilon + i \sigma \omega}{\epsilon_0}\right]\right] \left(\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}\right)^{1/4} + \sqrt{\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}}}$$

Amplitude = $\sqrt{A^2 + B^2}$ // Expand // FullSimplify

$$\sqrt{\frac{\epsilon^2 + \sigma^2 \omega^2 + \left(1 - 2 \cos\left[\operatorname{Arg}\left[\frac{\epsilon + i \sigma \omega}{\epsilon_0}\right]\right] \sqrt{\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}}\right) \epsilon_0^2}{\left(1 + 2 \cos\left[\frac{1}{2} \operatorname{Arg}\left[\frac{\epsilon + i \sigma \omega}{\epsilon_0}\right]\right] \left(\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}\right)^{1/4} + \sqrt{\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}}\right)^2 \epsilon_0^2}}$$

F = ComplexExpand[Abs[R]] // FullSimplify

$$\sqrt{\frac{1 - 2 \cos\left[\frac{1}{2} \operatorname{Arg}\left[\frac{\epsilon + i \sigma \omega}{\epsilon_0}\right]\right] \left(\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}\right)^{1/4} + \sqrt{\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}}}{1 + 2 \cos\left[\frac{1}{2} \operatorname{Arg}\left[\frac{\epsilon + i \sigma \omega}{\epsilon_0}\right]\right] \left(\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}\right)^{1/4} + \sqrt{\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}}}}$$

B / A // FullSimplify

$$\frac{2 \operatorname{Sin}\left[\frac{1}{2} \operatorname{Arg}\left[\frac{\epsilon + i \sigma \omega}{\epsilon_0}\right]\right] \left(\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}\right)^{1/4}}{-1 + \sqrt{\frac{\epsilon^2 + \sigma^2 \omega^2}{\epsilon_0^2}}}$$