

$$\mathbf{E}(\mathbf{x}) = \frac{1}{4\pi\epsilon_0} \int \rho(\mathbf{x}') \frac{\mathbf{x} - \mathbf{x}'}{|\mathbf{x} - \mathbf{x}'|^3} d^3x' \quad \text{Coulomb's Law (1.5)}$$

$$\delta(f(x)) = \sum_i \frac{1}{\left| \frac{df}{dx}(x_i) \right|} \delta(x - x_i) \quad \text{Delta function Rule 5}$$

$$\oint_S \mathbf{E} \cdot \mathbf{n} da = \frac{1}{\epsilon_0} \int_V \rho(\mathbf{x}) d^3x \quad \text{Gauss' Law (1.11)}$$

$$\nabla \times \mathbf{E} = 0 \quad \text{Curl of electric field (1.14)}$$

$$\mathbf{E} = -\nabla\Phi \quad \text{Electric field in terms of scalar potential (1.16)}$$

$$\Phi(\mathbf{x}) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\mathbf{x}')}{|\mathbf{x} - \mathbf{x}'|} d^3x' \quad \text{Scalar potential in terms of charge density (1.17)}$$

$$(\mathbf{E}_2 - \mathbf{E}_1) \cdot \mathbf{n} = \sigma/\epsilon_0 \quad \text{Electric field of a surface distribution (1.22)}$$

$$\nabla^2\Phi = -\rho/\epsilon_0 \quad \text{Poisson Equation (1.28)}$$

$$\nabla^2\Phi = 0 \quad \text{Laplace Equation (1.29)}$$

$$\nabla^2 \left( \frac{1}{|\mathbf{x} - \mathbf{x}'|} \right) = -4\pi\delta(\mathbf{x} - \mathbf{x}') \quad \text{Laplace's equation for a point charge (1.31)}$$

$$G(\mathbf{x}, \mathbf{x}') = \frac{1}{|\mathbf{x} - \mathbf{x}'|} + F(\mathbf{x}, \mathbf{x}') \quad \text{Green's function for Poisson's equation (1.40)}$$

$$\Phi(\mathbf{x}) = \frac{1}{4\pi\epsilon_0} \int_V \rho(\mathbf{x}') G_D(\mathbf{x}, \mathbf{x}') d^3x' = \frac{1}{4\pi} \oint_S (\mathbf{x}') \frac{\partial G_D}{\partial n'} da' \quad \text{Green's function potential Dirichlet B.C.s (1.44)}$$

$$\Phi(\mathbf{x}) = \langle \Phi \rangle_S + \frac{1}{4\pi\epsilon_0} \int_V \rho(\mathbf{x}') G_N(\mathbf{x}, \mathbf{x}') d^3x' + \frac{1}{4\pi} \oint_S \frac{\partial \Phi}{\partial n'} G_N da' \quad \text{Green's function potential Neumann B.C.s (1.46)}$$

$$W = \frac{\epsilon_0}{2} \int |\nabla\Phi|^2 d^3x = \frac{\epsilon_0}{2} \int |\mathbf{E}|^2 d^3x \quad \text{Energy stored in electric field (1.54)}$$

$$V_i = \sum_{j=1}^n p_{ij} q_j, \quad (i = 1, 2, \dots, n) \quad Q_i = \sum_{j=1}^n C_{ij} V_j, \quad (i = 1, 2, \dots, n) \quad \text{Capactiance matrix (1.62)}$$

$$W = \frac{1}{2} \sum_{i=1}^n Q_i V_i = \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n C_{ij} V_i V_j \quad \text{Potential energy of conductor system (1.62)}$$

$$q' = -\frac{a}{y} q, \quad y' = \frac{a^2}{y} \quad \text{Magnitude and position of image charge on sphere (2.4)}$$

$$\Phi = -E_0 \left( r - \frac{a^3}{r^2} \right) \quad \text{Scalar potential of conducting sphere in uniform Electric field (2.14)}$$

$$\frac{1}{|\mathbf{x} - \mathbf{x}'|} = 4\pi \sum_{\ell=0}^{\infty} \sum_{m=-\ell}^{\ell} \frac{1}{2\ell+1} \frac{r_{<}^{\ell}}{r_{>}^{\ell+1}} Y_{\ell m}^*(\theta', \phi') Y_{\ell m}(\theta, \phi) \quad \text{Green's function expansion in spherical coordinates (3.70)}$$

Where  $r_{<}$  ( $r_{>}$ ) is the smaller (larger) of  $|\mathbf{x}|$  and  $|\mathbf{x}'|$

	Wiggly	Decaying
Cartesian	$e^{\pm i k_n x}, A \cos(k_n x) + B \sin(k_n x)$	$e^{\pm k_n x}, A \cosh(k_n x) + B \sinh(k_n x)$
Cylindrical (3D)	$e^{im\phi}, A J_m(k_n \rho) + B Y_m(k_n \rho)$	$A I_m(k_n \rho) + B K_m(k_n \rho)$
Cylindrical (2D)	$e^{im\phi}$	$A_0 + B_0 \ln \rho + \sum A_m \rho^m + B_m \rho^{-m}$
Spherical ( $\phi$ symmetry)	$P_{\ell}(\cos \theta)$	$A \left( \frac{r}{a} \right)^{\ell} + B \left( \frac{r}{a} \right)^{-(\ell+1)}$
Spherical (No $\phi$ symmetry)	$Y_{\ell m}(\theta, \phi)$	$A \left( \frac{r}{a} \right)^{\ell} + B \left( \frac{r}{a} \right)^{-(\ell+1)}$

$$\int_0^L \sin\left(\frac{n\pi x}{L}\right) \sin\left(\frac{m\pi x}{L}\right) dx = \frac{L}{2} \delta_{nm} \quad \int_0^L \sin\left(\frac{n\pi x}{L}\right) \cos\left(\frac{m\pi x}{L}\right) dx = \frac{Ln[1 + \cos(n\pi)]}{\pi(n^2 - 1)}$$

$$\int_0^{2\pi} d\phi \int_0^L dz e^{i(m-m')\phi} e^{i\frac{2\pi}{L}(n-n')z} = 2\pi L \delta_{m'm} \delta_{n'n}$$

$$J_m(k\rho) \propto (k\rho)^m \quad Y_m(k\rho) \propto (k\rho)^{-m} \quad I_m(k\rho) \propto (k\rho)^m \quad K_m(k\rho) \propto (k\rho)^{-m} \quad \text{As their argument approaches zero}$$