

$$\text{minimize: } \mathbf{x}^T \mathbf{W} \mathbf{x} / 2 + \mathbf{q}^T \mathbf{x} \quad (1)$$

$$\text{subject to: } \mathbf{A} \mathbf{x} = \mathbf{b} \quad (2)$$

$$\mathbf{C} \mathbf{x} \leq \mathbf{d} \quad (3)$$

$$\text{minimize: } \mathbf{x}^T \mathbf{W} \mathbf{x} / 2 + \mathbf{q}^T \mathbf{x} \quad (4)$$

$$\text{subject to: } \mathbf{A} \mathbf{x} = \mathbf{b} \quad (5)$$

$$\max^3 \{ \mathbf{0}, \mathbf{C} \mathbf{x} - \mathbf{d} \} \quad (6)$$

$$\begin{cases} \mathbf{W} \mathbf{x} + \mathbf{A}^T \boldsymbol{\lambda} + \mathbf{C}^T \boldsymbol{\mu} = \mathbf{0} & (7) \\ \mathbf{A} \mathbf{x} - \mathbf{b} = \mathbf{0} & (8) \\ \boldsymbol{\mu}^T (\mathbf{d} - \mathbf{C} \mathbf{x}) = 0, \boldsymbol{\mu} \geq \mathbf{0}, \mathbf{d} - \mathbf{C} \mathbf{x} \geq \mathbf{0} & (9) \end{cases}$$

$$\mathcal{L} = \mathbf{x}^T \mathbf{W} \mathbf{x} / 2 + \mathbf{q}^T \mathbf{x} + \boldsymbol{\lambda}^T (\mathbf{A} \mathbf{x} - \mathbf{b}) \quad (10)$$

$$+ \boldsymbol{\mu}^T \max^3 \{ \mathbf{0}, \mathbf{C} \mathbf{x} - \mathbf{d} \} \quad (11)$$

$$\begin{cases} \mathbf{W} \mathbf{x} + \mathbf{q} + \mathbf{A}^T \boldsymbol{\lambda} + 3\mathbf{C}^T (\max^2 \{ \mathbf{0}, \mathbf{C} \mathbf{x} - \mathbf{d} \} \circ \boldsymbol{\mu}) & (12) \\ \mathbf{A} \mathbf{x} - \mathbf{b} & (13) \\ \max^3 \{ \mathbf{0}, \mathbf{C} \mathbf{x} - \mathbf{d} \} & (14) \end{cases}$$

$$\boldsymbol{\eta} := \max \{ \mathbf{0}, \mathbf{C} \mathbf{x} - \mathbf{d} \}, \mathbf{D}_1 := \text{diag} \{ \boldsymbol{\mu} \}, \mathbf{D}_2 := \text{diag} \{ \boldsymbol{\eta} \}$$

$$\begin{cases} \mathbf{W} \mathbf{x} + \mathbf{q} + \mathbf{A}^T \boldsymbol{\lambda} + 3\mathbf{C}^T \mathbf{D}_2 \mathbf{D}_2 \boldsymbol{\mu} & (15) \\ \mathbf{A} \mathbf{x} - \mathbf{b} & (16) \\ \mathbf{D}_2 \mathbf{D}_2 \boldsymbol{\eta} & (17) \end{cases}$$

$$\dot{\mathbf{W}} \mathbf{x} + \mathbf{W} \dot{\mathbf{x}} + \dot{\mathbf{q}} + \dot{\mathbf{A}}^T \boldsymbol{\lambda} + \mathbf{A}^T \dot{\boldsymbol{\lambda}} + 3\dot{\mathbf{C}}^T \mathbf{D}_2 \mathbf{D}_2 \boldsymbol{\mu} \quad (18)$$

$$+ 3\mathbf{C}^T \mathbf{D}_2 \mathbf{D}_2 \dot{\boldsymbol{\mu}} + 6\mathbf{C}^T \mathbf{D}_1 \mathbf{D}_2 (\dot{\mathbf{C}} \mathbf{x} + \mathbf{C} \dot{\mathbf{x}} - \dot{\mathbf{d}}) \quad (19)$$

$$\dot{\mathbf{A}} \mathbf{x} + \mathbf{A} \dot{\mathbf{x}} - \dot{\mathbf{b}} \quad (20)$$

$$3\mathbf{D}_2 \mathbf{D}_2 (\dot{\mathbf{C}} \mathbf{x} + \mathbf{C} \dot{\mathbf{x}} - \dot{\mathbf{d}}) \quad (21)$$

$$\mathbf{M} = \begin{bmatrix} \mathbf{W} + 6\mathbf{C}^T \mathbf{D}_1 \mathbf{D}_2 \mathbf{C} & \mathbf{A}^T & 3\mathbf{C}^T \mathbf{D}_2 \mathbf{D}_2 \\ \mathbf{A} & \mathbf{0} & \mathbf{0} \\ 3\mathbf{D}_2 \mathbf{D}_2 \mathbf{C} & \mathbf{0} & \mathbf{0} \end{bmatrix}, \quad (22)$$

$$\mathbf{P} = \begin{bmatrix} \dot{\mathbf{W}} + 6\mathbf{C}^T \mathbf{D}_1 \mathbf{D}_2 \dot{\mathbf{C}} & \dot{\mathbf{A}}^T & 3\dot{\mathbf{C}}^T \mathbf{D}_2 \mathbf{D}_2 \\ \dot{\mathbf{A}} & \mathbf{0} & \mathbf{0} \\ 3\mathbf{D}_2 \mathbf{D}_2 \dot{\mathbf{C}} & \mathbf{0} & \mathbf{0} \end{bmatrix}, \quad (23)$$

$$\mathbf{v} = \begin{bmatrix} \dot{\mathbf{q}} - 6\mathbf{C}^T \mathbf{D}_1 \mathbf{D}_2 \dot{\mathbf{d}} \\ -\dot{\mathbf{b}} \\ -3\mathbf{D}_2 \mathbf{D}_2 \dot{\mathbf{d}} \end{bmatrix}, \quad (24)$$