A ROOT Guide For Beginners

"Diving Into ROOT"

Contents

Abstract

ROOT is a software framework for data analysis and I/O: a powerful tool to cope with the demanding tasks typical of state of the art scientific data analysis. Among its prominent features are an advanced graphical user interface, ideal for interactive analysis, an interpreter for the C++ programming language, for rapid and efficient prototyping and a persistency mechanism for C++ objects, used also to write every year petabytes of data recorded by the Large Hadron Collider experiments. This introductory guide illustrates the main features of ROOT which are relevant for the typical problems of data analysis: input and plotting of data from measurements and fitting of analytical functions.

1 Motivation and Introduction

Welcome to data analysis!

Comparison of measurements to theoretical models is one of the standard tasks in experimental physics. In the most simple case, a "model" is just a function providing predictions of measured data. Very often, the model depends on parameters. Such a model may simply state "the current I is proportional to the voltage U", and the task of the experimentalist consists of determining the resistance, R, from a set of measurements.

As a first step, a visualisation of the data is needed. Next, some manipulations typically have to be applied, e.g. corrections or parameter transformations. Quite often, these manipulations are complex ones, and a powerful library of mathematical functions and procedures should be provided - think for example of an integral or peak-search or a Fourier transformation applied to an input spectrum to obtain the actual measurement described by the model.

One specialty of experimental physics are the inevitable uncertaintes affecting each measurement, and visualisation tools have to include these. In subsequent analysis, the statistical nature of the errors must be handled properly.

As the last step, measurements are compared to models, and free model parameters need to be determined in this process. Bellow you will find an example of a function (model) fit to data points. Several standard methods are available, and a data analysis tool should provide easy access to more than one of them. Means to quantify the level of agreement between measurements and model must also be available. Quite often, the data volume to be analyzed is large - think of fine-granular measurements accumulated with the aid of computers. A usable tool therefore must contain easy-to-use and efficient methods for storing and handling data.

In Quantum mechanics, models typically only predict the probability density function ("pdf") of measurements depending on a number of parameters, and the aim of the experimental analysis is to extract the parameters from the observed distribution of frequencies at which certain values of the measurement are observed. Measurements of this kind require means to generate and visualize frequency distributions, so-called histograms, and stringent statistical treatment to extract the model parameters from purely statistical distributions.

Simulation of expected data is another important aspect in data analysis. By repeated generation of "pseudo-data", which are analysed in the same manner as intended for the real data, analysis procedures can be validated or compared. In many cases, the distribution of the measurement errors is not precisely known, and simulation offers the possibility to test the effects of different assumptions.

A powerful software framework addressing all of the above requirements is ROOT, an open source project coordinated by the European Organisation for Nuclear Research, CERN in Geneva.

ROOT is very flexible and provides both a programming interface to use in own applications and a graphical user interface for interactive data analysis. The purpose of this document is to serve as a beginners guide and provides extendable examples for your own use cases, based on typical problems addressed in student labs. This guide will hopefully lay the ground for more complex applications in your future scientific work building on a modern, state-of the art tool for data analysis.

This guide in form of a tutorial is intended to introduce you quickly to the ROOT package. This goal will be accomplished using concrete examples, according to the "learning by doing" principle. Also because of this reason, this guide cannot cover all the complexity of the ROOT package. Nevertheless, once you feel confident with the concepts presented in the following chapters, you will be able to appreciate the ROOT Users Guide (The ROOT Users Guide 2015) and navigate through the Class Reference (The ROOT Reference Guide 2013) to find all the details you might be interested in. You can even look at the code itself, since ROOT is a free, open-source product. Use these documents in parallel to this tutorial!

The ROOT Data Analysis Framework itself is written in and heavily relies on the `C++` programming language: some knowledge about `C++` is required. Jus take advantage from the immense available literature about `C++` if you do not have any idea of what this language is about.

ROOT is available for many platforms (Linux, Mac OS X, Windows...), but in this guide we will implicitly assume that you are using Linux. The first thing you need to do with ROOT is install it, don't you ? Obtaining the latest ROOT version is straightforward. Just seek the "Pro" version on this webpage http://root.cern.ch/downloading-root. You will find precompiled versions for the different architectures, or the ROOT source code to compile yourself. Just pick up the flavour you need and follow the installation instructions.

Let's dive into ROOT!

2 ROOT Basics

Now that you have installed ROOT, what's this interactive shell thing you're running ? It's like this: ROOT leads a double life. It has an interpreter for macros Cling that you can run from the command line or like other applications. But it is also an interactive shell that can evaluate arbitrary statements and expressions. This is extremely useful for debugging, quick hacking and testing. Let us first have a look at some very simple examples.

2.1 ROOT as calculator

You can even use the ROOT interactive shell instead of a calculator! Launch the ROOT interactive shell with the command:

root

on your Linux box. The prompt should appear shortly.

```
1+1
(int) 2
2*(4+2)/12.
(double) 1.00000
sqrt(3.)
(double) 1.73205
1>2
(bool) false
TMath::Pi()
(Double_t) 3.14159
TMath::Erf(.2)
(Double_t) 0.222703
```

Not bad. You can see that ROOT offers you the possibility not only to type in C++ statements, but also advanced mathematical functions, which live in the TMath namespace.

Now let's do something more elaborated. A numerical example with the well known geometrical series:

```
double x=.5
```

```
(double) 0.500000

int N=30

(int) 30

double geom_series=0

(double) 0.00000

for (int i=0;i<N;++i)geom_series+=TMath::Power(x,i)

TMath::Abs(geom_series - (1-TMath::Power(x,N-1))/(1-x))

(Double_t) 1.86265e-09
```

Here we made a step forward. We even declared variables and used a for control structure. Note that there are some subtle differences between Cling and the standard C++ language. You do not need the ";" at the end of line in interactive mode – try the difference e.g. declare a different double like in the command above.

2.2 Learn C++ at the ROOT prompt

Behind the ROOT prompt there is an interpreter based on a real compiler toolkit: LLVM. It is therefore possible to exercise many features of C++ and the standard library. For example in the following snippet we define a lambda function, a vector and we sort it in different ways:

```cpp
using doubles = std::vector<double>;
auto pVec = [](const doubles& v){for (auto&& x:v) cout << x << endl;};
doubles v{0,3,5,4,1,2};
pVec(v);

0
3
5
4
1
2

std::sort(v.begin(),v.end());
pVec(v);

0
1
2
3
4
5
```

Or, if you prefer random number generation:

```cpp
std::default_random_engine generator;
std::normal_distribution<double> distribution(0.,1.);
distribution(generator);
std::cout << distribution(generator);

-0.407472

distribution(generator);
std::cout << distribution(generator);

0.399771

distribution(generator);
std::cout << distribution(generator);

0.0523187
```

2.3 ROOT as function plotter

Using one of ROOT's powerful classes, here TF1 will allow us to display a function of one variable, x. Try the following:

```
TCanvas canvas_2("c", "c");
TF1 f1("f1","sin(x)/x",0.,10.);
```

`f1` is an instance of a `TF1` class, the arguments are used in the constructor; the first one of type string is a name to be entered in the internal ROOT memory management system, the second string type parameter defines the function, here sin(x)/x, and the two parameters of type double define the range of the variable x. The Draw() method, here without any parameters, displays the function in a window which should pop up after you typed the above two lines.

```
f1.Draw();
canvas_2.Draw();
```
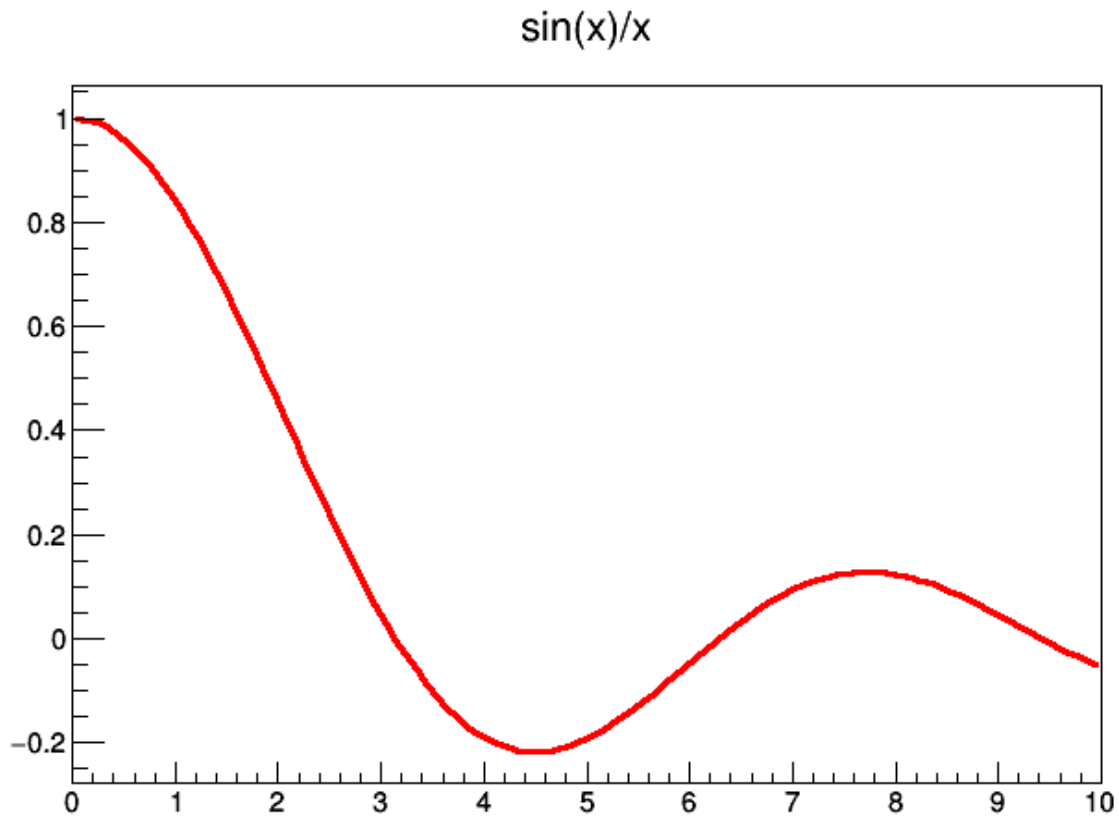

Figure 1: Simple sin graph

A slightly extended version of this example is the definition of a function with parameters, called [0], [1] and so on in the ROOT formula syntax. We now need a way to assign values to these parameters; this is achieved with the method SetParameter(,) of class TF1. Here is an example:

```
TF1 f2("f2","[0]*sin([1]*x)/x",0.,10.);
```

You can try to change the parameters of the input bellow and try the results.

```
f2.SetParameter(0,1);
f2.SetParameter(1,1);
f2.Draw();
canvas_2.Draw();
```

[0]*sin([1]*x)/x

Figure 2: Editing parameters of a sin graph

Of course, this version shows the same results as the initial one. Try playing with the parameters and plot the function again. The class TF1 has a large number of very useful methods, including integration and differentiation. To make full use of this and other ROOT classes, visit the documentation on the Internet under http://root.cern.ch/drupal/content/reference-guide. Formulae in ROOT are evaluated using the class TFormula, so also look up the relevant class documentation for examples, implemented functions and syntax.
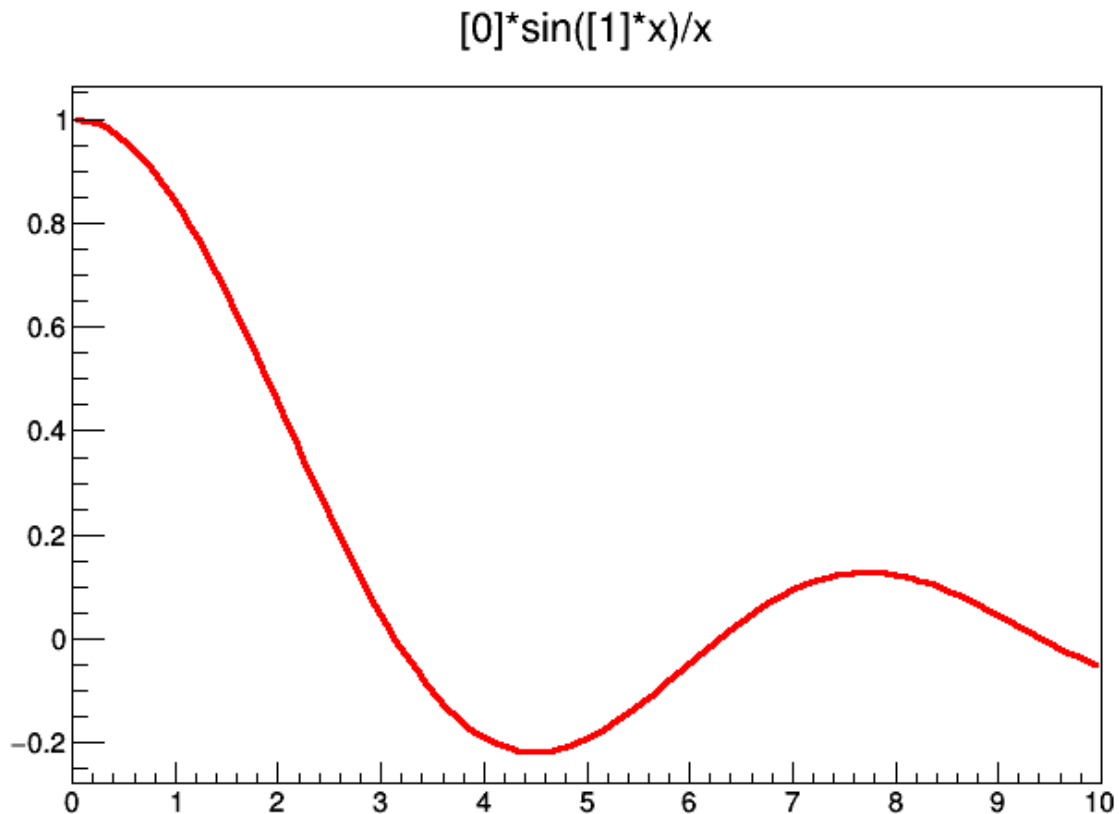
You should definitely download this guide to your own system to have it at you disposal whenever you need it.

To extend a little bit on the above example, consider a more complex function you would like to define. You can also do this using standard C or C++ code.

Consider the example below, which calculates and displays the interference pattern produced by light falling on a multiple slit. Please do not type in the example below at the ROOT command line, there is a much simpler way: Make sure you have the file slits.C on disk, and type root slits.C in the shell. This will start root and make it read the "macro" slits.C, i.e. all the lines in the file will be executed one after the other.

In this example drawing the interference pattern of light falling on a grid with n slits and ratio r of slit width over distance between slits.

```
%%cpp -d
```

As always in the notebook envirement we need to [.....................]. Something you will not need to do in your machine.

```
auto pi = TMath::Pi();
```

Bellow you can see the function code.

We define the necessary functions in C++ code, split into three separate functions, as suggested by the problem considered. The full interference pattern is given by the product of a function depending on the ratio of the width and distance of the slits, and a second one depending on the number of slits. More important for us

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here is the definition of the interface of these functions to make them usable for the ROOT class TF1: the first argument is the pointer to x, the second one points to the array of parameters.

```cpp
%%cpp -d
double single(double *x, double *par) {
  return pow(sin(pi*par[0]*x[0])/(pi*par[0]*x[0]),2);
}


double nslit0(double *x,double *par){
  return pow(sin(pi*par[1]*x[0])/sin(pi*x[0]),2);
}


double nslit(double *x, double *par){
  return single(x,par) * nslit0(x,par);
}
```

Here is how the main program should look like.

It starts with the definition of a function slits() of type void. After asking for user input, a ROOT function is defined using the C-type function given in the beginning. We can now use all methods of the TF1 class to control the behaviour of our function – nice, isn't it ?

```cpp
%%cpp -d
  void slits() {
  float r,ns;


  r = 1;
  ns=0.45;

  /* // request user input
  cout << "slit width / g ? ";
  scanf("%f",&r);
  cout << "# of slits? ";
  scanf("%f",&ns);
  cout <<"interference pattern for "<< ns
      <<" slits, width/distance: "<<r<<endl;
  */

  // define function and set options
  TF1 *Fnslit  = new TF1("Fnslit",nslit,-5.001,5.,2);
  Fnslit->SetNpx(500);

  // set parameters, as read in above
  Fnslit->SetParameter(0,r);
  Fnslit->SetParameter(1,ns);

  // draw the interference pattern for a grid with n slits
  Fnslit->Draw();
}
slits();
canvas_2.Draw();
```
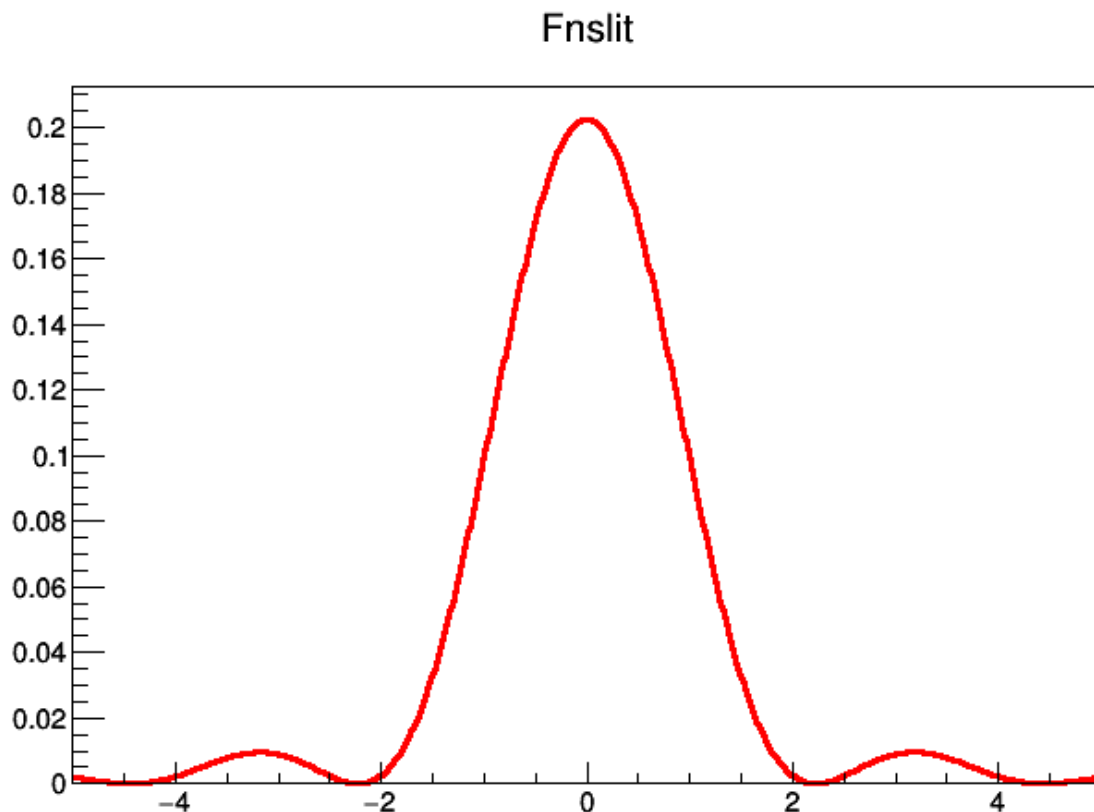
Figure 3: Slits graph

Output of slits.C with parameters 0.2 and 2.

In the commented out section the example asks for user input, namely the ratio of slit width over slit distance, and the number of slits. After entering this information, you should see the graphical output as above.

This is a more complicated example than the ones we have seen before, so spend some time analysing it carefully, you should have understood it before continuing.

If you like, you can easily extend the example to also plot the interference pattern of a single slit, using function double single, or of a grid with narrow slits, function double nslit0, in TF1 instances.

Here, we used a macro, some sort of lightweight program, that the interpreter distributed with ROOT, Cling, is able to execute. This is a rather extraordinary situation, since C++ is not natively an interpreted language! There is much more to say: chapter 3 is indeed dedicated to macros.

2.4 Controlling ROOT

One more remark at this point: as every command you type into ROOT is usually interpreted by Cling, an "escape character" is needed to pass commands to ROOT directly. This character is the dot at the beginning of a line:

```
root [1] .<command>
```

This is a selection of the most common commands. * **quit root**, simply type `.q`

- obtain a **list of commands**, use `.?`
- **access the shell** of the operating system, type `.!<OS_command>`; try, e.g. `.!ls` or `.!pwd`

- **execute a macro**, enter `.x <file_name>`; in the above example, you might have used `.x slits.C` at the ROOT prompt

- **load a macro**, type `.L <file_name>`; in the above example, you might instead have used the command `.L slits.C` followed by the function call `slits();`. Note that after loading a macro all functions and procedures defined therein are available at the ROOT prompt.

  - **compile a macro**, type `.L <file_name>+`; ROOT is able to manage for you the `C++` compiler behind the scenes and to produce machine code starting from your macro. One could decide to compile a macro in order to obtain better performance or to get nearer to the production environment.

Use `.help` at the prompt to inspect the full list.

2.5 Plotting Measurements

To display measurements in ROOT, including errors, there exists a powerful class `TGraphErrors` with different types of constructors. In the example here, we use data from the file `ExampleData.txt` in text format:

```
TCanvas canvas_2_5;
TGraphErrors gr("../data/ExampleData.txt");
gr.Draw("AP");
canvas_2_5.Draw();
```
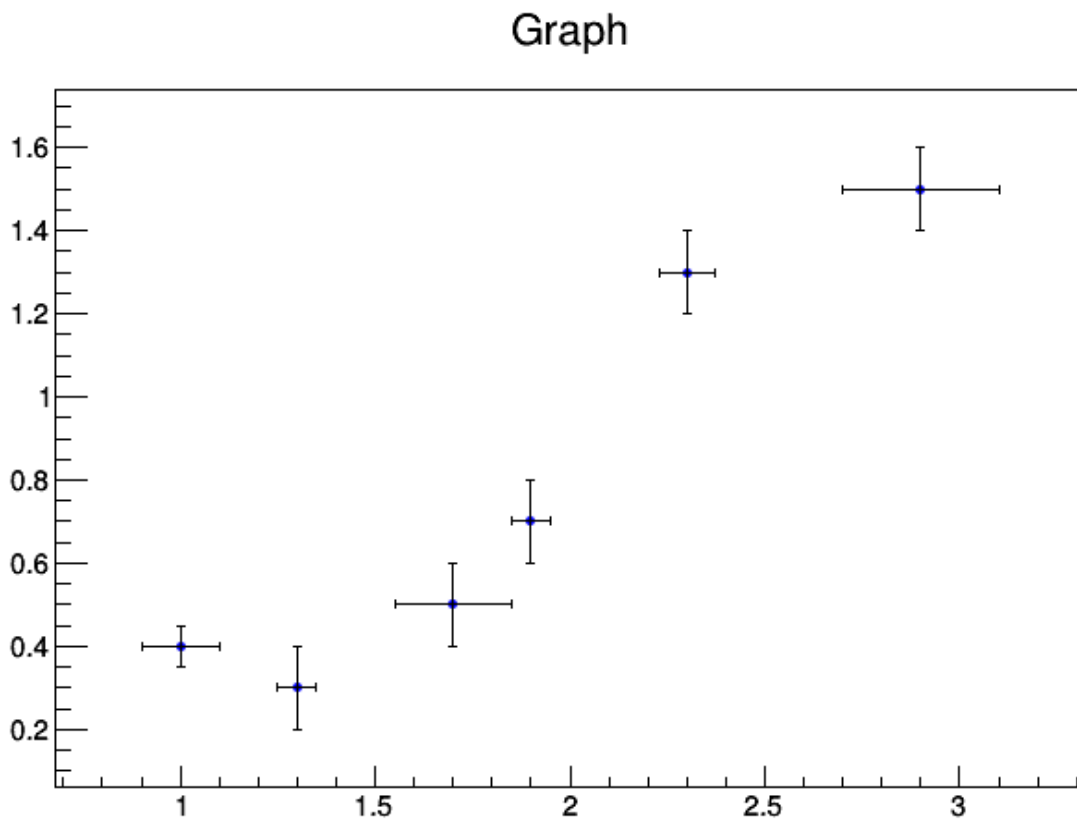

Figure 4: Displaying measurements with class TGraphErrors

Make sure the file `ExampleData.txt` is available in the directory from which you started ROOT. Inspect this file now with your favourite editor, or use the command `less ExampleData.txt` to inspect the file, you will see something like that:

```
# fake data to demonstrate the use of TGraphErrors
```

```
# x    y    ex    ey
 1.   0.4  0.1   0.05
 1.3  0.3  0.05  0.1
 1.7  0.5  0.15  0.1
 1.9  0.7  0.05  0.1
 2.3  1.3  0.07  0.1
 2.9  1.5  0.2   0.1
```

The format is very simple and easy to understand. Lines beginning with `#` are ignored. It is very convenient to add some comments about the type of data. The data itself consist of lines with four real numbers each, representing the x- and y- coordinates and their errors of each data point.

The argument of the method `Draw("AP")` is important here. Behind the scenes, it tells the TGraphPainter class to show the axes and to plot markers at the x and y positions of the specified data points. Note that this simple example relies on the default settings of ROOT, concerning the size of the canvas holding the plot, the marker type and the line colours and thickness used and so on. In a well-written, complete example, all this would need to be specified explicitly in order to obtain nice and well readable results. A full chapter on graphs will explain many more of the features of the class `TGraphErrors` and its relation to other ROOT classes in much more detail.

2.6 Histograms in ROOT

Frequency distributions in ROOT are handled by a set of classes derived from the histogram class `TH1`, in our case `TH1F`. The letter F stands for float, meaning that the data type `float` is used to store the entries in one histogram bin.

```
TCanvas canvas_2_6;
TF1 efunc("efunc","exp([0]+[1]*x)",0.,5.);
efunc.SetParameter(0,1);
efunc.SetParameter(1,-1);
```

The first lines of this example define a function, an exponential in this case, and set its parameters.

```
TH1F hist_2_6_1("histogram 2.6.1","example histogram",100,0.,5.);
```

In this line a histogram is instantiated, with a name, a title, a certain number of bins (100 of them, equidistant, equally sized) in the range from 0 to 5.

We use yet another new feature of ROOT to fill this histogram with data, namely pseudo-random numbers generated with the method `TF1::GetRandom`, which in turn uses an instance of the ROOT class `TRandom` created when ROOT is started.

```
for (int i=0;i<1000;i++) {hist_2_6_1.Fill(efunc.GetRandom());}
```

Data is entered in the histogram using the method `TH1F::Fill` in a loop construct. As a result, the histogram is filled with 1000 random numbers distributed according to the defined function.

```
hist_2_6_1.Draw();
canvas_2_6.Draw();
```
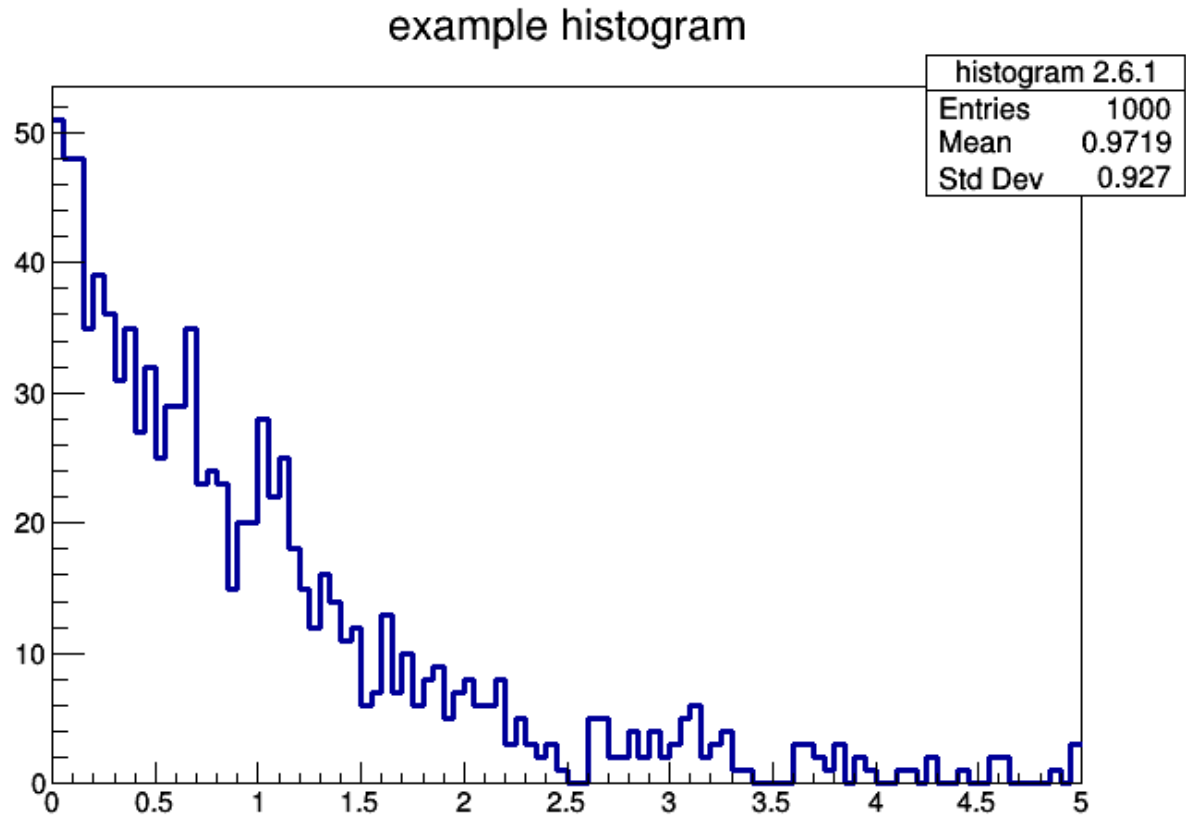
Figure 5: Filling a histogram with TH1F::Fill

The histogram is displayed using the method `TH1F::Draw()`. You may think of this example as repeated measurements of the life time of a quantum mechanical state, which are entered into the histogram, thus giving a visual impression of the probability density distribution. The plot is shown above.

Note that you will not obtain an identical plot when executing the lines above, depending on how the random number generator is initialised.

The class `TH1F` does not contain a convenient input format from plain text files. The following lines of `C++` code do the job. One number per line stored in the text file "expo.dat" is read in via an input stream and filled in the histogram until end of file is reached.

```
TH1F hist_2_6_2("histogram 2.6.2","example histogram",100,0.,5.);
ifstream inp;
inp.open("../data/expo.dat");
while (inp >> x) { hist_2_6_2.Fill(x); }
hist_2_6_2.Draw();
inp.close();
canvas_2_6.Draw();
```

Figure 6: Filling a histogram from plain text files

2.7 Interactive ROOT

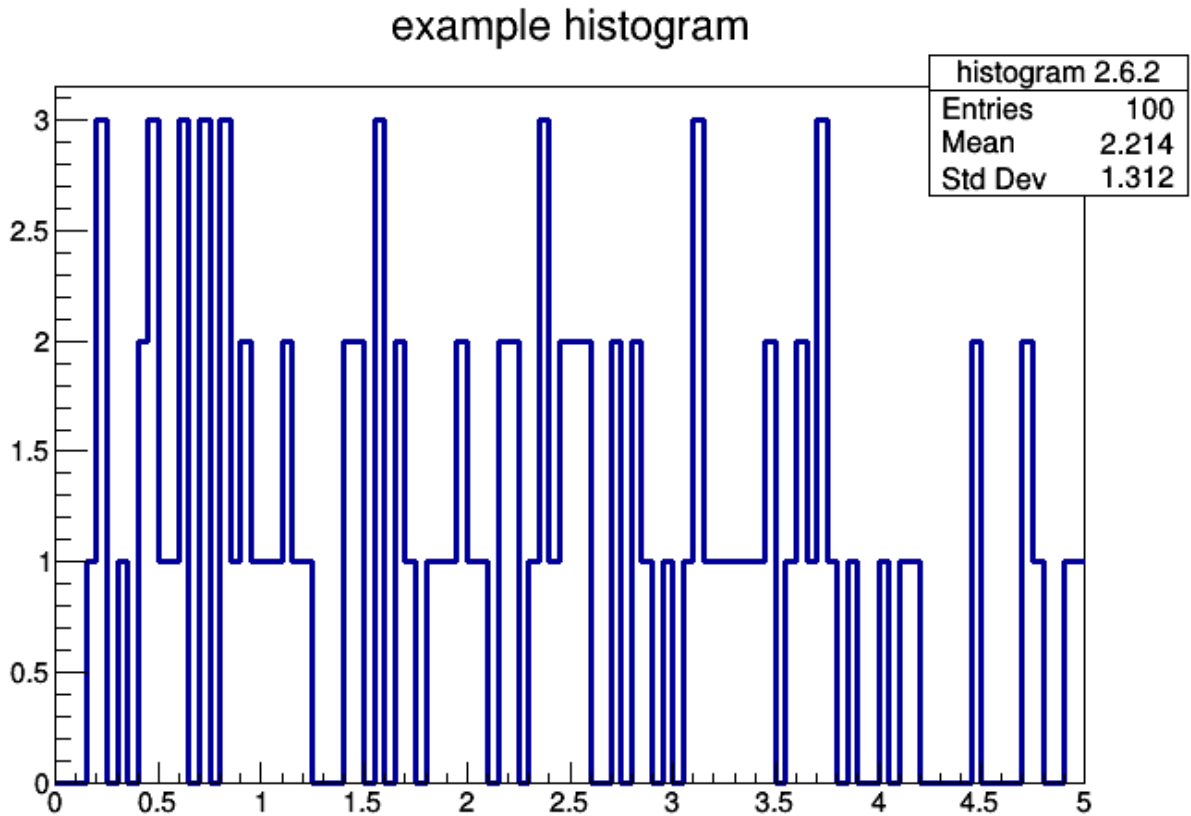Look at one of your plots again and move the mouse across. You will notice that this is much more than a static picture, as the mouse pointer changes its shape when touching objects on the plot. When the mouse is over an object, a right-click opens a pull-down menu displaying in the top line the name of the ROOT class you are dealing with, e.g. `TCanvas` for the display window itself, `TFrame` for the frame of the plot, `TAxis` for the axes, `TPaveText` for the plot name. Depending on which plot you are investigating, menus for the ROOT classes `TF1`, `TGraphErrors` or `TH1F` will show up when a right-click is performed on the respective graphical representations. The menu items allow direct access to the members of the various classes, and you can even modify them, e.g. change colour and size of the axis ticks or labels, the function lines, marker types and so on. Try it!

You will probably like the following: in the output produced by the example `slits.C`, right-click on the function line and select "SetLineAttributes", then left-click on "Set Parameters". This gives access to a panel allowing you to interactively change the parameters of the function, as shown in the figure above. Change the slit width, or go from one to two and then three or more slits, just as you like. When clicking on "Apply", the function plot is updated to reflect the actual value of the parameters you have set.

Another very useful interactive tool is the `FitPanel`, available for the classes `TGraphErrors` and `TH1F`. Predefined fit functions can be selected from a pull-down menu, including "`gaus`", "`expo`" and "`pol0`" - "`pol9`" for Gaussian and exponential functions or polynomials of degree 0 to 9, respectively. In addition, user-defined functions using the same syntax as for functions with parameters are possible.

After setting the initial parameters, a fit of the selected function to the data of a graph or histogram can be performed and the result displayed on the plot. The fit panel has a number of control options to select the fit method, fix or release individual parameters in the fit, to steer the level of output printed on the console, or to extract and display additional information like contour lines showing parameter correlations. As function fitting

is of prime importance in any kind of data analysis, this topic will again show up later.

If you are satisfied with your plot, you probably want to save it. Just close all selector boxes you opened previously and select the menu item `Save as...` from the menu line of the window. It will pop up a file selector box to allow you to choose the format, file name and target directory to store the image. There is one very noticeable feature here: you can store a plot as a root macro! In this macro, you find the C++ representation of all methods and classes involved in generating the plot. This is a valuable source of information for your own macros, which you will hopefully write after having worked through this tutorial.

Using ROOT's interactive capabilities is useful for a first exploration of possibilities. Other ROOT classes you will encounter in this tutorial have such graphical interfaces. We will not comment further on this, just be aware of the existence of ROOT's interactive features and use them if you find them convenient. Some trial-and-error is certainly necessary to find your way through the huge number of menus and parameter settings.

2.8 ROOT Beginners' FAQ

At this point of the guide, some basic questions could have already come to your mind. We will try to clarify some of them with further explanations in the following.

2.8.1 ROOT type declarations for basic data types

In the official ROOT documentation, you find special data types replacing the normal ones, e.g. `Double_t`, `Float_t` or `Int_t` replacing the standard `double`, `float` or `int` types. Using the ROOT types makes it easier to port code between platforms (64/32 bit) or operating systems (windows/Linux), as these types are mapped to suitable ones in the ROOT header files. If you want adaptive code of this type, use the ROOT type declarations. However, usually you do not need such adaptive code, and you can safely use the standard C type declarations for your private code, as we did and will do throughout this guide. If you intend to become a ROOT developer, however, you better stick to the official coding rules!

2.8.2 Configure ROOT at start-up

The behaviour of a ROOT session can be tailored with the options in the `.rootrc` file. Examples of the tunable parameters are the ones related to the operating and window system, to the fonts to be used, to the location of start-up files. At start-up, ROOT looks for a `.rootrc` file in the following order:

- `./.rootrc //local directory`
- `$HOME/.rootrc //user directory`
- `$ROOTSYS/etc/system.rootrc //global ROOT directory`

If more than one `.rootrc` files are found in the search paths above, the options are merged, with precedence local, user, global. The parsing and interpretation of this file is handled by the ROOT class TEnv. Have a look to its documentation if you need such rather advanced features. The file `.rootrc` defines the location of two rather important files inspected at start-up: `rootalias.C` and `rootlogon.C`. They can contain code that needs to be loaded and executed at ROOT startup. `rootalias.C` is only loaded and best used to define some often used functions. rootlogon.C contains code that will be executed at startup: this file is extremely useful for example to pre-load a custom style for the plots created with ROOT. This is done most easily by creating a new TStyle object with your preferred settings, as described in the class reference guide, and then use the command `gROOT->SetStyle("MyStyleName");` to make this new style definition the default one. As an example, have a look in the file rootlogon.C coming with this tutorial. Another relevant file is `rootlogoff.C` that it called when the session is finished.

2.8.3 ROOT command history

Every command typed at the ROOT prompt is stored in a file `.root_hist` in your home directory. ROOT uses this file to allow for navigation in the command history with the up-arrow and down-arrow keys. It is also convenient to extract successful ROOT commands with the help of a text editor for use in your own macros.

2.8.4 ROOT Global Pointers

All global pointers in ROOT begin with a small "g". Some of them were already implicitly introduced (for example in the section Configure ROOT at start-up). The most important among them are presented in the following:

- **gROOT:** the `gROOT` variable is the entry point to the `ROOT` system. Technically it is an instance of the `TROOT` class. Using the gROOT pointer one has access to basically every object created in a ROOT based program. The `TROOT` object is essentially a container of several lists pointing to the main `ROOT` objects.

- **gStyle:** By default ROOT creates a default style that can be accessed via the `gStyle` pointer. This class includes functions to set some of the following object attributes.

- Canvas

- Pad

- Histogram axis

- Lines

- Fill areas

- Text

- Markers

- Functions

- Histogram Statistics and Titles

- etc . . .

- **gSystem:** An instance of a base class defining a generic interface to the underlying Operating System, in our case `TUnixSystem`.

- **gInterpreter:** The entry point for the ROOT interpreter. Technically an abstraction level over a singleton instance of `TCling`.

At this point you have already learnt quite a bit about some basic features of ROOT.

Please move on to become an expert!

3 ROOT Macros

You know how other books go on and on about programming fundamentals and finally work up to building a complete, working program? Let's skip all that. In this guide, we will describe macros executed by the ROOT C++ interpreter Cling.

It is relatively easy to compile a macro, either as a pre-compiled library to load into ROOT, or as a stand-alone application, by adding some include statements for header file or some "dressing code" to any macro.

3.1 General Remarks on ROOT macros

If you have a number of lines which you were able to execute at the ROOT prompt, they can be turned into a ROOT macro by giving them a name which corresponds to the file name without extension. The general structure for a macro stored in file `MacroName.C` is:

```
void MacroName() {
        <           ...
          your lines of C++ code
                ...              >
}
```

The macro is executed by typing:

```
> root MacroName.C
```

at the system prompt, or executed using `Bash .x` at the ROOT prompt.

```
> root
root [0] .x MacroName.C
```

Or it can be loaded into a ROOT session and then be executed by typing:

```
root [0].L MacroName.C
root [1] MacroName();
```

at the ROOT prompt.Note that more than one macro can be loaded this way, as each macro has a unique name in the ROOT name space. A small set of options can help making your plot nicer.

```
gROOT->SetStyle("Plain");     // set plain TStyle
gStyle->SetOptStat(111111);   // draw statistics on plots,
                              // (0) for no output
gStyle->SetOptFit(1111);      // draw fit results on plot,
                              // (0) for no ouput
gStyle->SetPalette(57);       // set color map
gStyle->SetOptTitle(0);       // suppress title box
```

Next, you should create a canvas for graphical output, with size, subdivisions and format suitable to your needs, see documentation of class `TCanvas`:

```
TCanvas canvas_3_1("31Canvas","Title",0,0,900,400);
canvas_3_1.Divide(2,1);
canvas_3_1.cd(1);
```

These parts of a well-written macro are pretty standard, and you should remember to include pieces of code like in the examples above to make sure your plots always look as you had intended.

Below, in section Interpretation and Compilation, some more code fragments will be shown, allowing you to use the system compiler to compile macros for more efficient execution, or turn macros into stand-alone applications linked against the ROOT libraries.

3.2 A more complete example

Let us now look at a rather complete example of a typical task in data analysis, a macro that constructs a graph with errors, fits a (linear) model to it and saves it as an image. To run this macro, simply type in the shell:

```
> root macro1.C
```

The code is built around the ROOT class `TGraphErrors`, which was already introduced previously. Have a look at it in the class reference guide, where you will also find further examples. The macro shown below uses additional classes, `TF1` to define a function, TCanvas to define size and properties of the window used for our plot, and `TLegend` to add a nice legend. For the moment, ignore the commented include statements for header files, they will only become important at the end in section Interpretation and Compilation.

```
%%cpp -d

// Builds a graph with errors, displays it and saves it as
// image. First, include some header files
// (not necessary for Cling)

#include "TCanvas.h"
#include "TROOT.h"
#include "TGraphErrors.h"
#include "TF1.h"
#include "TLegend.h"
#include "TArrow.h"
#include "TLatex.h"
```

```cpp
void macro3_2_1(){    //#1
    // The values and the errors on the Y axis
    const int n_points=10;
    double x_vals[n_points]=
            {1,2,3,4,5,6,7,8,9,10};
    double y_vals[n_points]=
            {6,12,14,20,22,24,35,45,44,53};
    double y_errs[n_points]=
            {5,5,4.7,4.5,4.2,5.1,2.9,4.1,4.8,5.43};

    // Instance of the graph
    //#2
    TGraphErrors graph(n_points,x_vals,y_vals,nullptr,y_errs);
    graph.SetTitle("Measurement XYZ;lenght in cm;Arb Units");

    // Make the plot estetically better
    //#3
    graph.SetMarkerStyle(kOpenCircle);
    graph.SetMarkerColor(kBlue);
    graph.SetLineColor(kBlue);

    // The canvas on which we'll draw the graph
    //#4
    auto  Canvas_3_2_1 = new TCanvas();

    // Draw the graph !
    //#5
    graph.DrawClone("APE");

    // Define a linear function
    //#6
    TF1 function_3_2_1("Linear law","[0]+x*[1]",.5,10.5);
    // Let's make the funcion line nicer
    //#7
    function_3_2_1.SetLineColor(kRed);   function_3_2_1.SetLineStyle(2);
    // Fit it to the graph and draw it
    //#8
    graph.Fit(&function_3_2_1);
    function_3_2_1.DrawClone("Same");

    // Build and Draw a legend
    //#9
    TLegend leg(.1,.7,.3,.9,"Lab. Lesson 1");
    leg.SetFillColor(0);
    graph.SetFillColor(0);
    leg.AddEntry(&graph,"Exp. Points");
    leg.AddEntry(&function_3_2_1,"Th. Law");
    leg.DrawClone("Same");

    // Draw an arrow on the canvas
    //#10
    TArrow arrow(8,8,6.2,23,0.02,"|>");
    arrow.SetLineWidth(2);
    arrow.DrawClone();

    // Add some text to the plot
    //#11
```

```
    TLatex text(8.2,7.5,"#splitline{Maximum}{Deviation}");
    text.DrawClone();

    /*this command will create a pdf file with the graph in the same folder.
    If you want to use it you can uncoment it and comment the Draw command bellow.*/
    //#12

//    mycanvas->Print("graph_with_law.pdf");
    Canvas_3_2_1->Draw();
}
```

Let's give a look to the obtained plot. Beautiful outcome for such a small bunch of lines, isn't it ?

Your first plot with data points, a fit of an analytical function, a legend and some additional information in the form of graphics primitives and text. A well formatted plot, clear for the reader is crucial to communicate the relevance of your results to the reader.

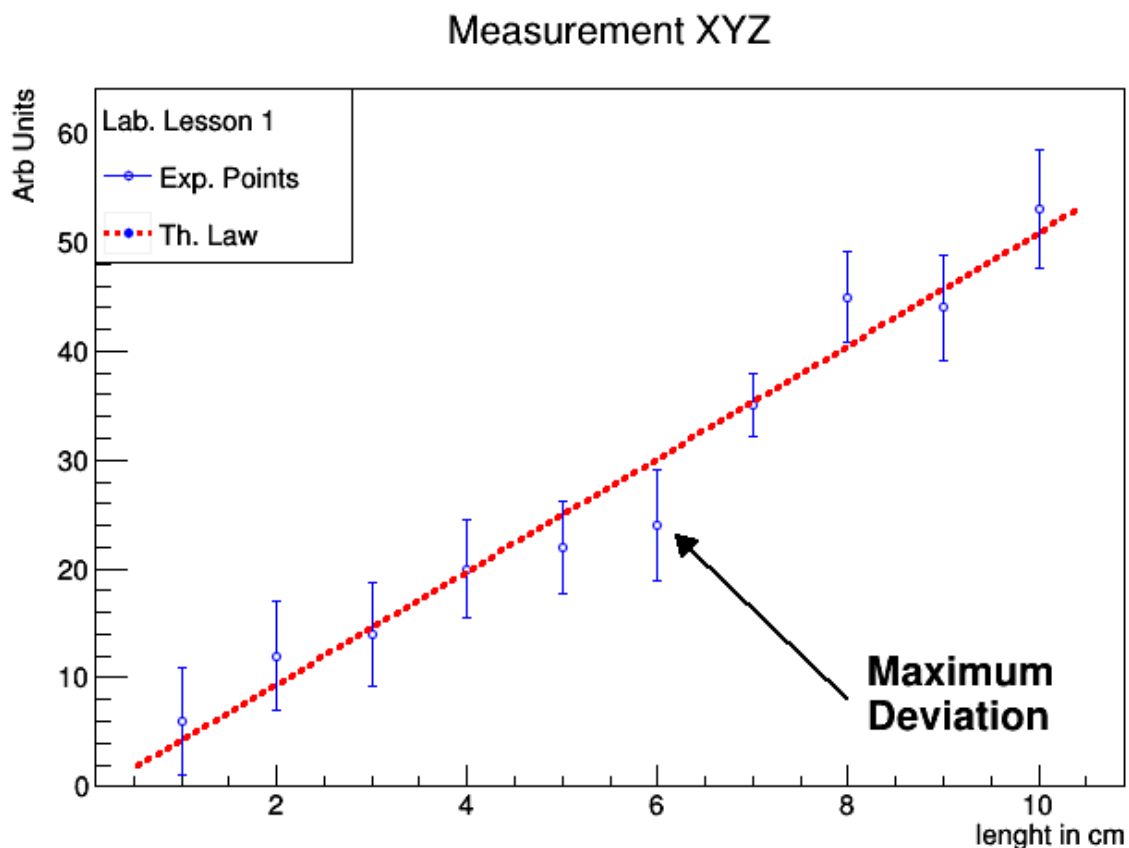`macro3_2_1();`

Figure 7: Your first plot with data points

```
 FCN=3.84883 FROM MIGRAD    STATUS=CONVERGED     31 CALLS        32 TOTAL
                    EDM=5.96982e-22    STRATEGY= 1     ERROR MATRIX ACCURATE
  EXT PARAMETER                                STEP        FIRST
  NO.   NAME      VALUE          ERROR        SIZE      DERIVATIVE
   1  p0          -1.01604e+00   3.33409e+00  1.48321e-03  -8.98235e-12
   2  p1           5.18756e+00   5.30717e-01  2.36095e-04   9.40487e-12
```

Let's comment it in detail:

- **Point #1:** the name of the principal function (it plays the role of the "main" function in compiled programs) in the macro file. It has to be the same as the file name without extension.

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- **Point #2:** instance of the TGraphErrors class. The constructor takes the number of points and the pointers to the arrays of x values, y values, x errors (in this case none, represented by the NULL pointer) and y errors. The second line defines in one shot the title of the graph and the titles of the two axes, separated by a ";".

- **Point #3:** These three lines are rather intuitive right ? To understand better the enumerators for colours and styles see the reference for the TColor and TMarker classes.

- **Point #4:** the canvas object that will host the drawn objects. The "memory leak" is intentional, to make the object existing also out of the macro1 scope.

- **Point #5:** the method DrawClone draws a clone of the object on the canvas. It has to be a clone, to survive after the scope of macro1, and be displayed on screen after the end of the macro execution. The string option "APE" stands for:

- A imposes the drawing of the Axes.

- P imposes the drawing of the graph's markers.

- E imposes the drawing of the graph's error bars.

- **Point #6:** define a mathematical function. There are several ways to accomplish this, but in this case the constructor accepts the name of the function, the formula, and the function range.

- **Point #7:** maquillage. Try to give a look to the line styles at your disposal visiting the documentation of the TLine class.

- **Point #8:** fits the f function to the graph, observe that the pointer is passed. It is more interesting to look at the output on the screen to see the parameters values and other crucial information that we will learn to read at the end of this guide. The DrawClone comand tha follows draws the clone of the object on the canvas again. The "Same" option avoids the cancellation of the already drawn objects, in our case, the graph. The function f will be drawn using the same axis system defined by the previously drawn graph.

- **Point #9:** completes the plot with a legend, represented by a TLegend instance. The constructor takes as parameters the lower left and upper right corners coordinates with respect to the total size of the canvas, assumed to be 1, and the legend header string. You can add to the legend the objects, previously drawn or not drawn, through the addEntry method. Observe how the legend is drawn at the end: looks familiar now, right ?

- **Point #10:** defines an arrow with a triangle on the right hand side, a thickness of 2 and draws it.

- **Point #11:** interpret a Latex string which hast its lower left corner located in the specified coordinate. The #splitline{}{} construct allows to store multiple lines in the same TLatex object.

- **Point #12:** save the canvas as image. The format is automatically inferred from the file extension (it could have been eps, gif, . . .).

3.3 Summary of Visual effects

3.3.1 Colours and Graph Markers

We have seen that to specify a colour, some identifiers like kWhite, kRed or kBlue can be specified for markers, lines, arrows etc. The complete summary of colours is represented by the ROOT "colour wheel". To know more about the full story, refer to the online documentation of `TColor`.

ROOT provides several graphics markers types. Select the most suited symbols for your plot among dots, triangles, crosses or stars. An alternative set of names for the markers is available.

3.3.2 Arrows and Lines

The macro line 55 shows how to define an arrow and draw it. The class representing arrows is `TArrow`, which inherits from `TLine`. The constructors of lines and arrows always contain the coordinates of the endpoints. Arrows also foresee parameters to specify their shapes. Do not underestimate the role of lines and arrows in your plots. Since each plot should contain a message, it is convenient to stress it with additional graphics primitives.

3.3.3 Text

Also text plays a fundamental role in making the plots self-explanatory. A possibility to add text in your plot is provided by the TLatex class. The objects of this class are constructed with the coordinates of the bottom-left corner of the text and a string which contains the text itself. The real twist is that ordinary Latex mathematical symbols are automatically interpreted, you just need to replace the "" by a "#".

If "" is used as control character , then the TMathText interface is invoked. It provides the plain TeX syntax and allow to access character's set like Russian and Japenese.

3.4 Interpretation and Compilation

As you observed, up to now we heavily exploited the capabilities of ROOT for interpreting our code, more than compiling and then executing. This is sufficient for a wide range of applications, but you might have already asked yourself "how can this code be compiled ?". There are two answers.

3.4.1 Compile a Macro with ACLiC

ACLiC will create for you a compiled dynamic library for your macro, without any effort from your side, except the insertion of the appropriate header files at the top of the code. In this example, they are already included. To generate an object library from the macro code, from inside the interpreter type (please note the "+"):

```
root [1] .L macro1.C+
```

Once this operation is accomplished, the macro symbols will be available in memory and you will be able to execute it simply by calling from inside the interpreter:

```
root [2] macro1()
```

3.4.2 Compile a Macro with the Compiler

A plethora of excellent compilers are available, both free and commercial. We will refer to the `GCC` compiler in the following. In this case, you have to include the appropriate headers in the code and then exploit the root-config tool for the automatic settings of all the compiler flags. root-config is a script that comes with ROOT; it prints all flags and libraries needed to compile code and link it with the ROOT libraries. In order to make the code executable stand-alone, an entry point for the operating system is needed, in C++ this is the procedure `int main();`. The easiest way to turn a ROOT macro code into a stand-alone application is to add the following "dressing code" at the end of the macro file. This defines the procedure main, the only purpose of which is to call your macro:

```
int main() {
  ExampleMacro();
  return 0;
}
```

To create a stand-alone program from a macro called `ExampleMacro.C`, simply type

```
> g++ -o ExampleMacro ExampleMacro.C 'root-config --cflags --libs'
```

and execute it by typing:

```
> ./ExampleMacro
```

This procedure will, however, not give access to the ROOT graphics, as neither control of mouse or keyboard events nor access to the graphics windows of ROOT is available. If you want your stand-alone application have display graphics output and respond to mouse and keyboard, a slightly more complex piece of code can be used. In the example below, a macro `ExampleMacro_GUI` is executed by the ROOT class `TApplication`. As a additional feature, this code example offers access to parameters eventually passed to the program when started from the command line. Here is the code fragment:

```cpp
%%cpp -d
/*
 This piece of code demonstrates how a root macro is used as a standalone
    application with full acces the grapical user interface (GUI) of ROOT   */

//     ==>>  put the code of your macro here
void ExampleMacro_GUI() {
  // Create a histogram, fill it with random gaussian numbers
  TH1F *histogram_3_4 = new TH1F ("histogram_3_1", "example histogram", 100, -5.,5.);
  histogram_3_4->FillRandom("gaus",1000);

  auto  canvas_3_4 = new TCanvas();
  // draw the histogram
  histogram_3_4->DrawClone();

/* - Create a new ROOT file for output
   - Note that this file may contain any kind of ROOT objects, histograms,
     pictures, graphics objects etc.
   - the new file is now becoming the current directory */
  TFile *file_3_4 = new TFile("../data/ExampleMacro.root","RECREATE","ExampleMacro");

  // write Histogram to current directory (i.e. the file just opened)
  histogram_3_4->Write();

  // Close the file.
  //   (You may inspect your histogram in the file using the TBrowser class)
  file_3_4->Close();

  canvas_3_4->Draw();
}


void StandaloneApplication() {
  // ==>> this application calls the ROOT macro
  ExampleMacro_GUI();
}

StandaloneApplication();
```
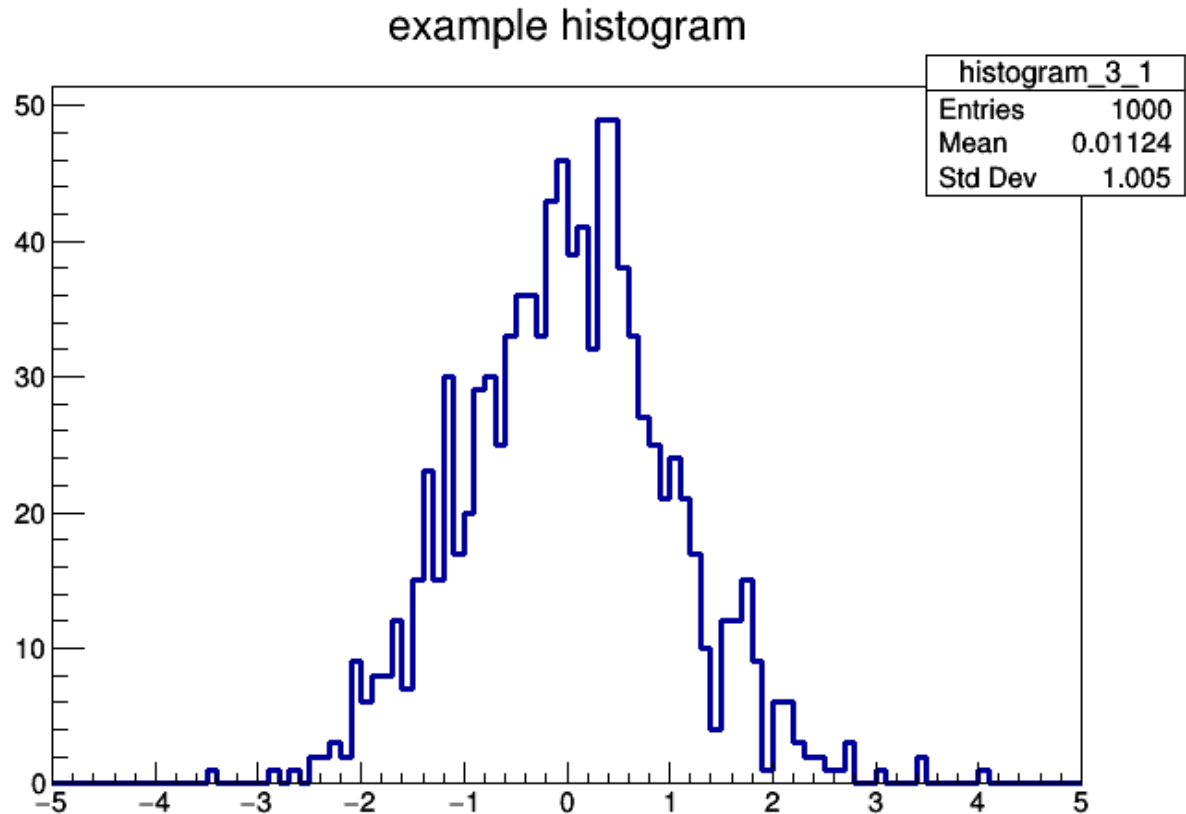
Figure 8: Creating a stand-alone program from a macro

Compile the code with:

`g++ -o ExampleMacro_GUI ExampleMacro_GUI 'root-config --cflags --libs'`

and execute the program with

`> ./ExampleMacro_GUI`

4 Graphs

In this Chapter we will learn how to exploit some of the functionalities ROOT provides to display data exploiting the class `TGraphErrors`, which you already got to know previously.

4.1 Read Graph Points from File

The fastest way in which you can fill a graph with experimental data is to use the constructor which reads data points and their errors from an ASCII file (i.e. standard text) format:

`TGraphErrors(const char *filename, const char *format="%lg %lg %lg %lg", Option_t *option="");`

The format string can be:

- "%lg %lg" read only 2 first columns into X,Y

- "%lg %lg %lg" read only 3 first columns into X,Y and EY

- "%lg %lg %lg %lg" read only 4 first columns into X,Y,EX,EY

This approach has the nice feature of allowing the user to reuse the macro for many different data sets. Here is an example of an input file. The nice graphic result shown is produced by the macro below, which reads two such input files and uses different options to display the data points.

"' # Measurement of Friday 26 March # Experiment 2 Physics Lab

1 6 5 2 12 5 3 14 4.7 4 20 4.5 5 22 4.2 6 24 5.1 7 35 2.9 8 45 4.1 9 44 4.8 10 53 5.43 "'

```cpp
%%cpp -d
// Reads the points from a file and produces a simple graph.
int macro_4_1(){
    auto canvas_4_1=new TCanvas();
    canvas_4_1->SetGrid();

    TGraphErrors graph_expected("../data/macro4_1_input_expected.txt", "%lg %lg %lg");
    graph_expected.SetTitle(
        "Measurement XYZ and Expectation;"
        "lenght [cm];"
        "Arb.Units");
    graph_expected.SetFillColor(kYellow);
    graph_expected.DrawClone("E3AL"); // E3 draws the band

    TGraphErrors graph("../data/macro4_1_input.txt","%lg %lg %lg");
    graph.SetMarkerStyle(kCircle);
    graph.SetFillColor(0);
    graph.DrawClone("PESame");

    // Draw the Legend
    TLegend leg(.1,.7,.3,.9,"Lab. Lesson 2");
    leg.SetFillColor(0);
    leg.AddEntry(&graph_expected,"Expected Points");
    leg.AddEntry(&graph,"Measured Points");
    leg.DrawClone("Same");

    graph.Print();
    canvas_4_1->Draw();
    return 0;
}
macro_4_1();
```
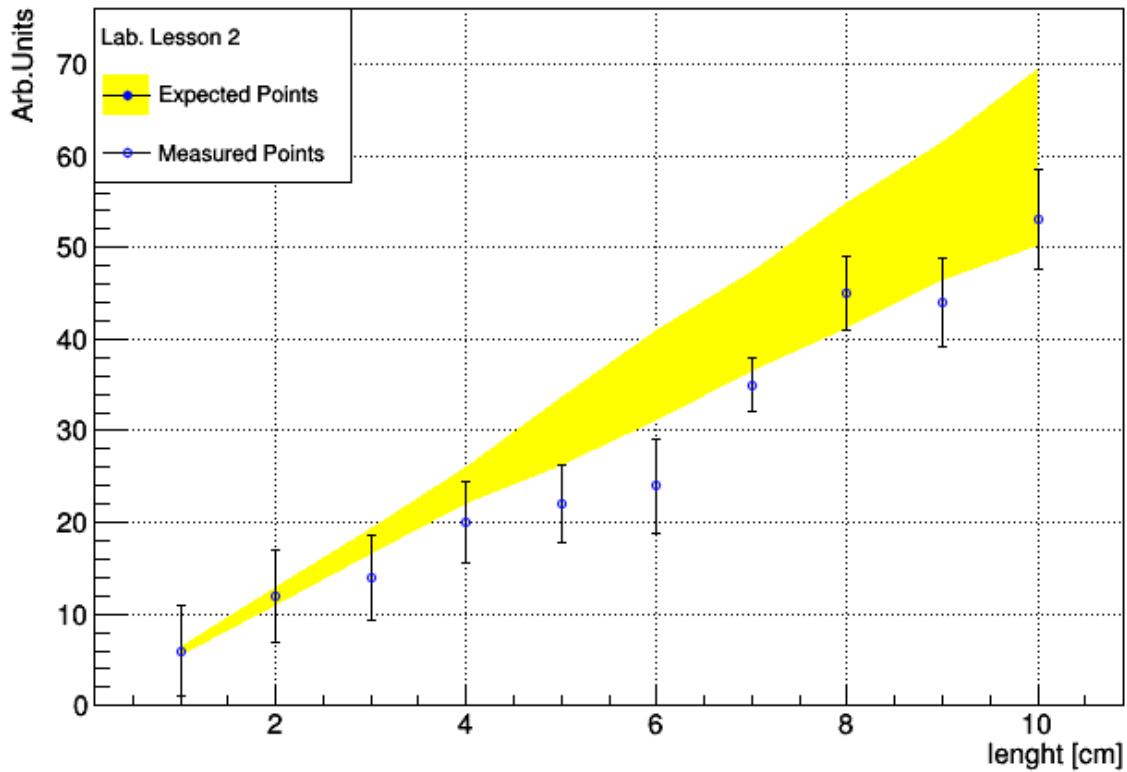
Figure 9: Filling a graph with experimental data

```
x[0]=1, y[0]=6, ex[0]=0, ey[0]=5
x[1]=2, y[1]=12, ex[1]=0, ey[1]=5
x[2]=3, y[2]=14, ex[2]=0, ey[2]=4.7
x[3]=4, y[3]=20, ex[3]=0, ey[3]=4.5
x[4]=5, y[4]=22, ex[4]=0, ey[4]=4.2
x[5]=6, y[5]=24, ex[5]=0, ey[5]=5.1
x[6]=7, y[6]=35, ex[6]=0, ey[6]=2.9
x[7]=8, y[7]=45, ex[7]=0, ey[7]=4.1
x[8]=9, y[8]=44, ex[8]=0, ey[8]=4.8
x[9]=10, y[9]=53, ex[9]=0, ey[9]=5.43
```

In addition to the inspection of the plot, you can check the actual contents of the graph with the `TGraph::Print()` method at any time, obtaining a printout of the coordinates of data points on screen. The macro also shows us how to print a coloured band around a graph instead of error bars, quite useful for example to represent the errors of a theoretical prediction.

4.2 Polar Graphs

With ROOT you can profit from rather advanced plotting routines, like the ones implemented in the `TPolarGraph`, a class to draw graphs in polar coordinates. You can see the example macro in the following:

```
auto canvas_4_2 = new TCanvas("myCanvas","myCanvas",600,600);
Double_t rmin=0.;
Double_t rmax=TMath::Pi()*6.;
const Int_t npoints=1000;
Double_t r[npoints];
Double_t theta[npoints];
```

```
for (Int_t ipt = 0; ipt < npoints; ipt++) {
    r[ipt] = ipt*(rmax-rmin)/npoints+rmin;
    theta[ipt] = TMath::Sin(r[ipt]);
}
TGraphPolar grP1 (npoints,r,theta);
grP1.SetTitle("A Fan");
grP1.SetLineWidth(3);
grP1.SetLineColor(2);
grP1.DrawClone("L");
canvas_4_2->Draw();
```
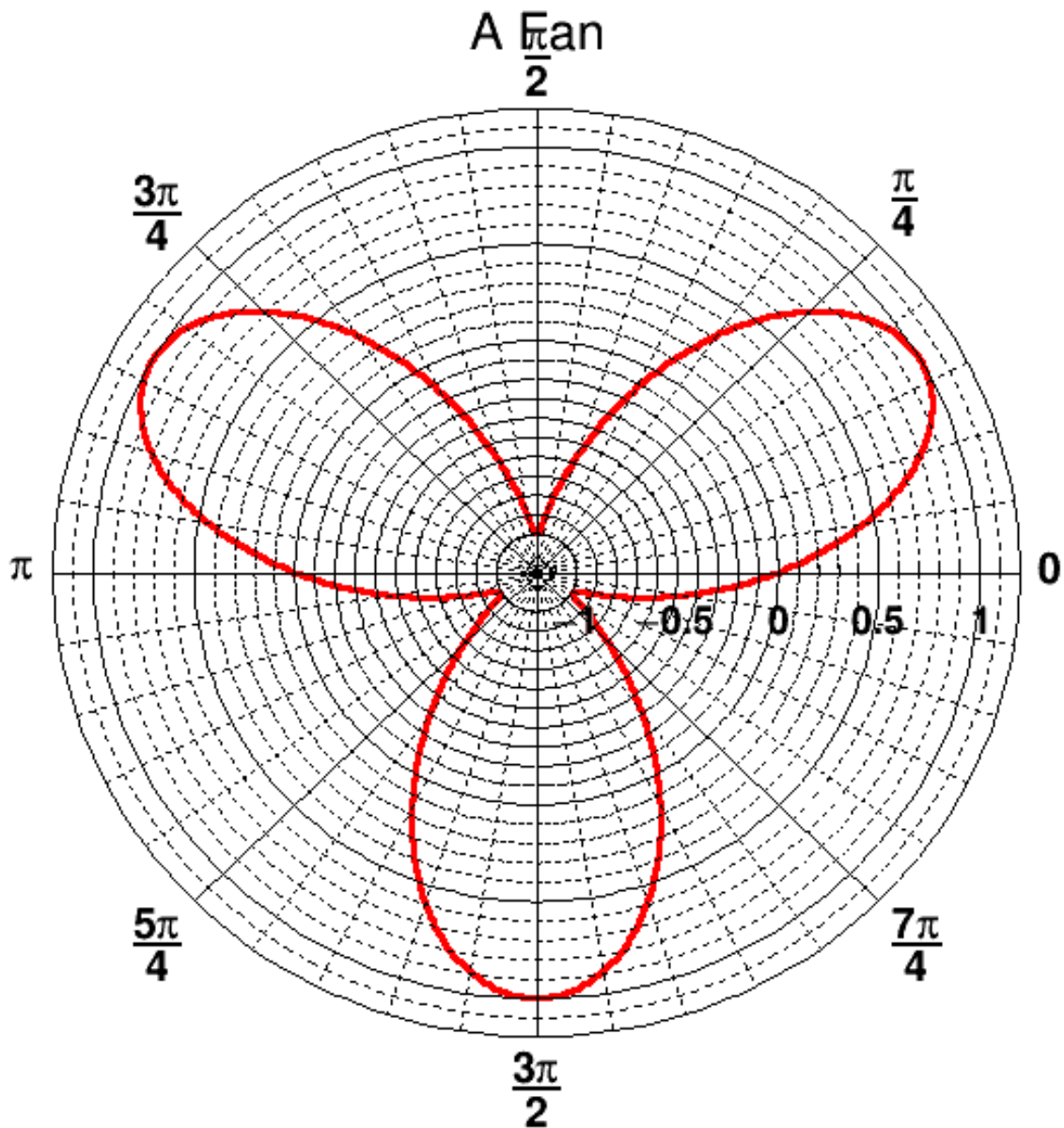

Figure 10: Drawing graphs in polar coordinates using TPolarGraph

A new element was added on the canvas declaration, the size of the canvas: it is sometimes optically better to show plots in specific canvas sizes.

4.3 2D Graphs

Under specific circumstances, it might be useful to plot some quantities versus two variables, therefore creating a bi-dimensional graph. Of course ROOT can help you in this task, with the **TGraph2DErrors** class. The following macro produces a bi-dimensional graph representing a hypothetical measurement, fits a bi-dimensional function to it and draws it together with its x and y projections. Some points of the code will be explained in detail. This time, the graph is populated with data points using random numbers, introducing a new and very important ingredient, the ROOT `TRandom3` random number generator using the Mersenne Twister algorithm (Matsumoto 1997).

Let's go through the code, step by step to understand what is going on:

- The instance of the random generator. You can then draw out of this instance random numbers distributed according to different probability density functions, like the Uniform one at point 2. See the on-line documentation to appreciate the full power of this ROOT feature.

```
//#1
TRandom3 my_random_generator;
```

- You are already familiar with the TF1 class. This is its two-dimensional version. At line 16 two random numbers distributed according to the TF2 formula are drawn with the method TF2::GetRandom2(double& a, double&b).

```
//#2
TF2 function_4_3("f2","1000*(([0]*sin(x)/x)*([1]*sin(y)/y))+2000",-6,6,-6,6);
function_4_3.SetParameters(1,1);
TGraph2DErrors dte(500);
// Fill the 2D graph
double rnd, x, y, z, ex, ey, ez;
for (Int_t i=0; i<500; i++) {
    function_4_3.GetRandom2(x,y);
    // A random number in [-e,e]
    rnd = my_random_generator.Uniform(-0.3,0.3);
    z = function_4_3.Eval(x,y)*(1+rnd);
    dte.SetPoint(i,x,y,z);
    ex = 0.05*my_random_generator.Uniform();
    ey = 0.05*my_random_generator.Uniform();
    ez = fabs(z*rnd);
    dte.SetPointError(i,ex,ey,ez);
}
```

- Fitting a 2-dimensional function just works like in the one-dimensional case, i.e. initialisation of parameters and calling of the Fit() method.

```
//#4
// Fit function to generated data
function_4_3.SetParameters(0.7,1.5);  // set initial values for fit
function_4_3.SetTitle("Fitted 2D function");
dte.Fit(&function_4_3);
// Plot the result
auto canvas_4_3_1 = new TCanvas();
function_4_3.SetLineWidth(1);
function_4_3.SetLineColor(kBlue-5);
```

```
 FCN=550.868 FROM HESSE     STATUS=NOT POSDEF     14 CALLS          48 TOTAL
                  EDM=9.72579e-13     STRATEGY= 1      ERR MATRIX NOT POS-DEF
  EXT PARAMETER                  APPROXIMATE      STEP         FIRST
  NO.   NAME        VALUE            ERROR        SIZE      DERIVATIVE
   1   p0         6.83686e-01   1.49858e-01   4.34655e-06  -3.65525e-05
   2   p1         1.46504e+00   3.21126e-01   9.31404e-06  -1.28163e-05
```

- The Surf1 option draws the TF2 objects (but also bi-dimensional histograms) as coloured surfaces with a wire-frame on three-dimensional canvases.

```
//#5
TF2   *function_4_3_c = (TF2*)function_4_3.DrawClone("Surf1");
```

- Retrieve the axis pointer and define the axis titles.

```
//#6
TAxis *Xaxis = function_4_3_c->GetXaxis();
TAxis *Yaxis = function_4_3_c->GetYaxis();
TAxis *Zaxis = function_4_3_c->GetZaxis();
Xaxis->SetTitle("X Title"); Xaxis->SetTitleOffset(1.5);
Yaxis->SetTitle("Y Title"); Yaxis->SetTitleOffset(1.5);
Zaxis->SetTitle("Z Title"); Zaxis->SetTitleOffset(1.5);
```

- Draw the cloud of points on top of the coloured surface.

```
//#7
dte.DrawClone("P0 Same");
// Make the x and y projections
```

- Here you learn how to create a canvas, partition it in two sub-pads and access them. It is very handy to show multiple plots in the same window or image.

```
//#8
auto canvas_4_3_2= new TCanvas("ProjCan","The Projections",1000,400);
canvas_4_3_2->Divide(2,1);
canvas_4_3_2->cd(1);
dte.Project("x")->Draw();
canvas_4_3_2->cd(2);
dte.Project("y")->Draw();

canvas_4_3_2 ->Draw();
```
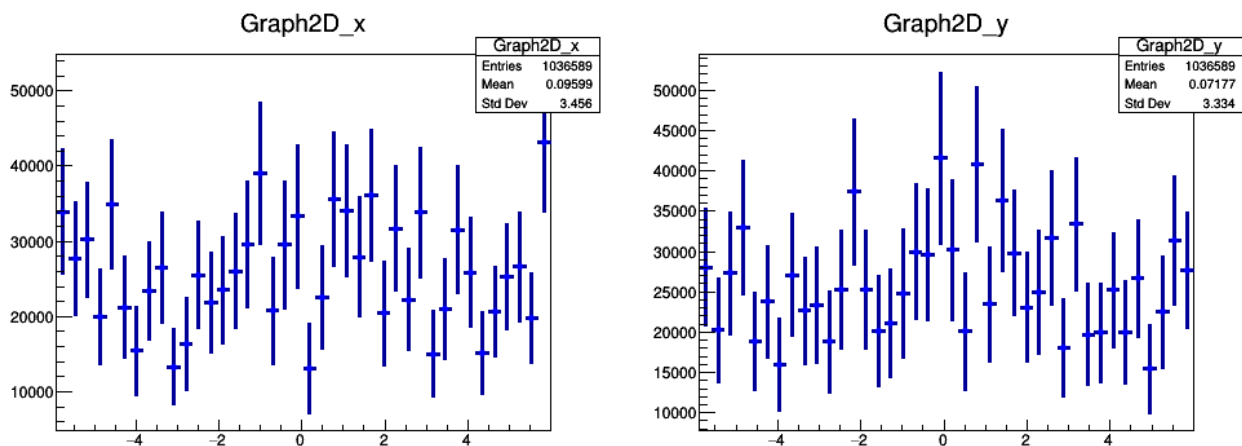

Figure 11: Canvas partitioned it in two sub-pads

4.4 Multiple graphs

The class `TMultigraph` allows to manipulate a set of graphs as a single entity. It is a collection of TGraph (or derived) objects. When drawn, the X and Y axis ranges are automatically computed such as all the graphs will be visible.

```
TCanvas *canvas_4_4 = new TCanvas("canvas_4_4","multigraph",700,500);
canvas_4_4->SetGrid();
```

Here we create the multigraph.

```
TMultiGraph *multigraph_4_4 = new TMultiGraph();

// create first graph
const Int_t n1 = 10;
Double_t px1[] = {-0.1, 0.05, 0.25, 0.35, 0.5, 0.61,0.7,0.85,0.89,0.95};
Double_t py1[] = {-1,2.9,5.6,7.4,9,9.6,8.7,6.3,4.5,1};
Double_t ex1[] = {.05,.1,.07,.07,.04,.05,.06,.07,.08,.05};
Double_t ey1[] = {.8,.7,.6,.5,.4,.4,.5,.6,.7,.8};
TGraphErrors *error_graph_1 = new TGraphErrors(n1,px1,py1,ex1,ey1);
error_graph_1->SetMarkerColor(kBlue);
error_graph_1->SetMarkerStyle(21);
multigraph_4_4->Add(error_graph_1);
```

Here we create two graphs with errors and add them in the multigraph.

```
// create second graph
const Int_t n2 = 10;
Float_t x2[]  = {-0.28, 0.005, 0.19, 0.29, 0.45, 0.56,0.65,0.80,0.90,1.01};
Float_t y2[]  = {2.1,3.86,7,9,10,10.55,9.64,7.26,5.42,2};
Float_t ex2[] = {.04,.12,.08,.06,.05,.04,.07,.06,.08,.04};
Float_t ey2[] = {.6,.8,.7,.4,.3,.3,.4,.5,.6,.7};
TGraphErrors *error_graph_2 = new TGraphErrors(n2,x2,y2,ex2,ey2);
error_graph_1->SetMarkerColor(kRed);
error_graph_1->SetMarkerStyle(20);
multigraph_4_4->Add(error_graph_1);

multigraph_4_4->Draw("apl");
```

Here we draw the multigraph. The axis limits are computed automatically to make sure all the graphs' points will be in range.

```
multigraph_4_4->GetXaxis()->SetTitle("X values");
multigraph_4_4->GetYaxis()->SetTitle("Y values");

gPad->Update();
gPad->Modified();
canvas_4_4->Draw();
```
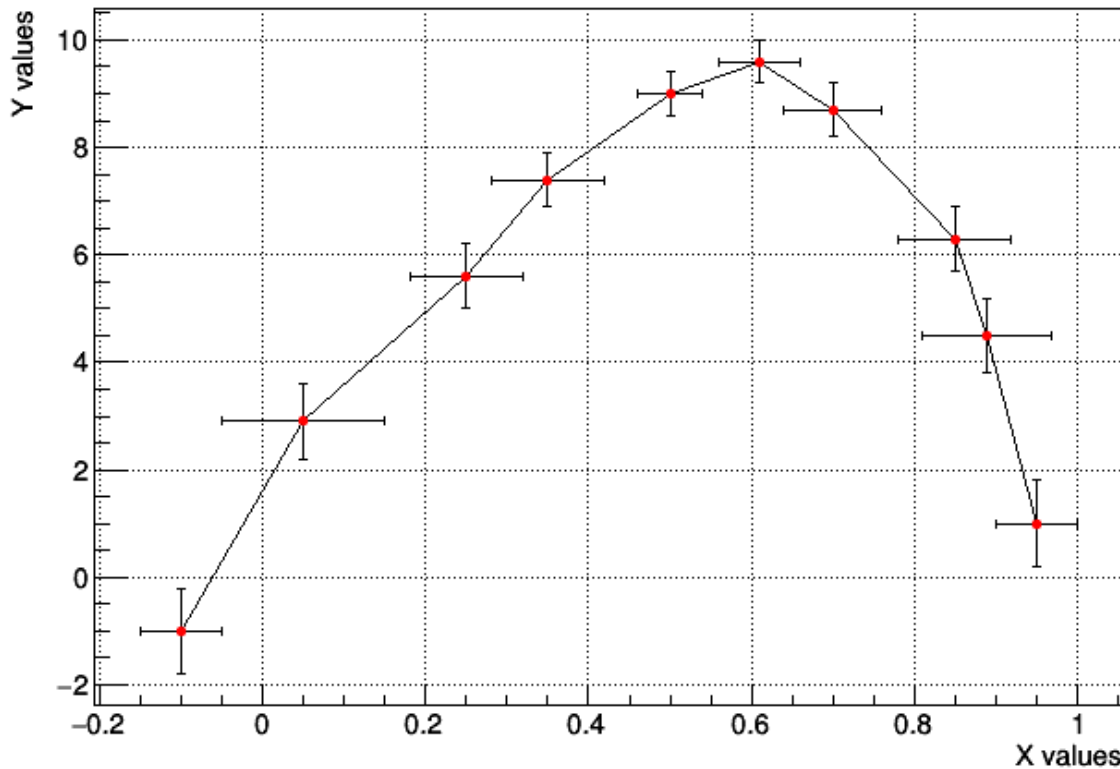
Figure 12: Drawing a multigraph

5 Histograms

Histograms play a fundamental role in any type of physics analysis, not only to visualise measurements but being a powerful form of data reduction. ROOT offers many classes that represent histograms, all inheriting from the `TH1` class. We will focus in this chapter on uni- and bi- dimensional histograms the bin contents of which are represented by floating point numbers the `TH1F` and `TH2F` classes respectively. To optimise the memory usage you might go for one byte (`TH1C`), short (`TH1S`), integer (`TH1I`) or double-precision (`TH1D`) bin-content.

5.1 Your First Histogram

Let's suppose you want to measure the counts of a Geiger detector located in proximity of a radioactive source in a given time interval. This would give you an idea of the activity of your source. The count distribution in this case is a Poisson distribution. Let's see how operatively you can fill and draw a histogram with the following example macro.

The result of a counting (pseudo) experiment. Only bins corresponding to integer values are filled given the discrete nature of the poissonian distribution.

Using histograms is rather simple. The main differences with respect to graphs that emerge from the example are:

- In the begining the histograms have a name and a title right from the start, no predefined number of entries but a number of bins and a lower-upper range.

```cpp
auto cnt_r_h=new TH1F("count_rate",
            "Count Rate;N_{Counts};# occurencies",
```

```
                  100, // Number of Bins
                  -0.5, // Lower X Boundary
                  15.5); // Upper X Boundary

   auto mean_count=3.6f;
   TRandom3 rndgen_5_1;
   // simulate the measurements
```

- During each loop of the following for an entry is stored in the histogram through the TH1F::Fill method.

```
   for (int imeas=0;imeas<400;imeas++)
       cnt_r_h->Fill(rndgen_5_1.Poisson(mean_count));

   auto canvas_5_1= new TCanvas();
   cnt_r_h->Draw();

   auto canvas_5_2= new TCanvas();
```

- The histogram can be drawn also normalised, ROOT automatically takes cares of the necessary rescaling.

```
   cnt_r_h->DrawNormalized();
```

- This small snippet shows how easy it is to access the moments and associated errors of a histogram.

```
// Print summary
cout << "Moments of Distribution:\n"
     << " - Mean     = " << cnt_r_h->GetMean() << " +- "
                         << cnt_r_h->GetMeanError() << "\n"
     << " - Std Dev  = " << cnt_r_h->GetStdDev() << " +- "
                         << cnt_r_h->GetStdDevError() << "\n"
     << " - Skewness = " << cnt_r_h->GetSkewness() << "\n"
     << " - Kurtosis = " << cnt_r_h->GetKurtosis() << "\n";
canvas_5_1->Draw();
```
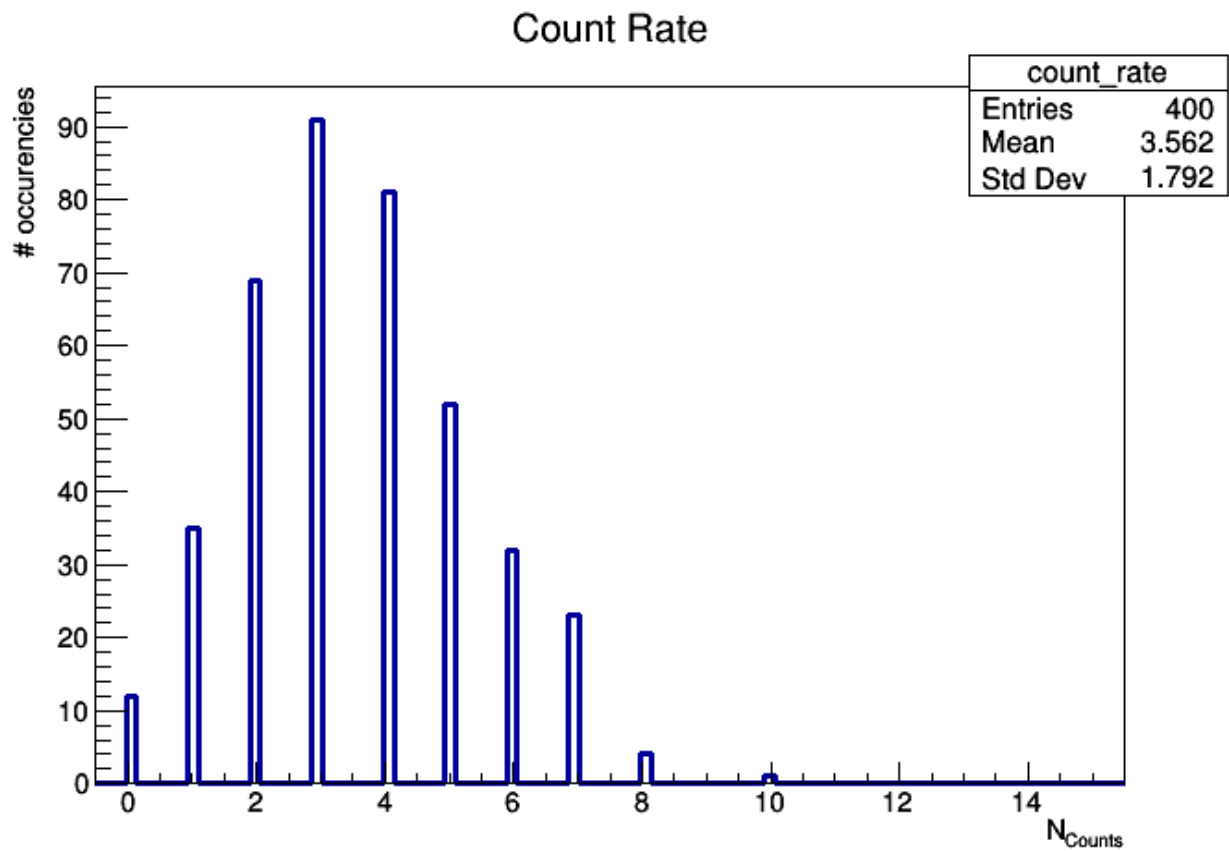
Figure 13: Creating a Histogram: example 1

```
Moments of Distribution:
 - Mean     = 3.5625 +- 0.0895976
 - Std Dev  = 1.79195 +- 0.0633551
 - Skewness = 0.326374
 - Kurtosis = -0.242483

   canvas_5_2->Draw();
```
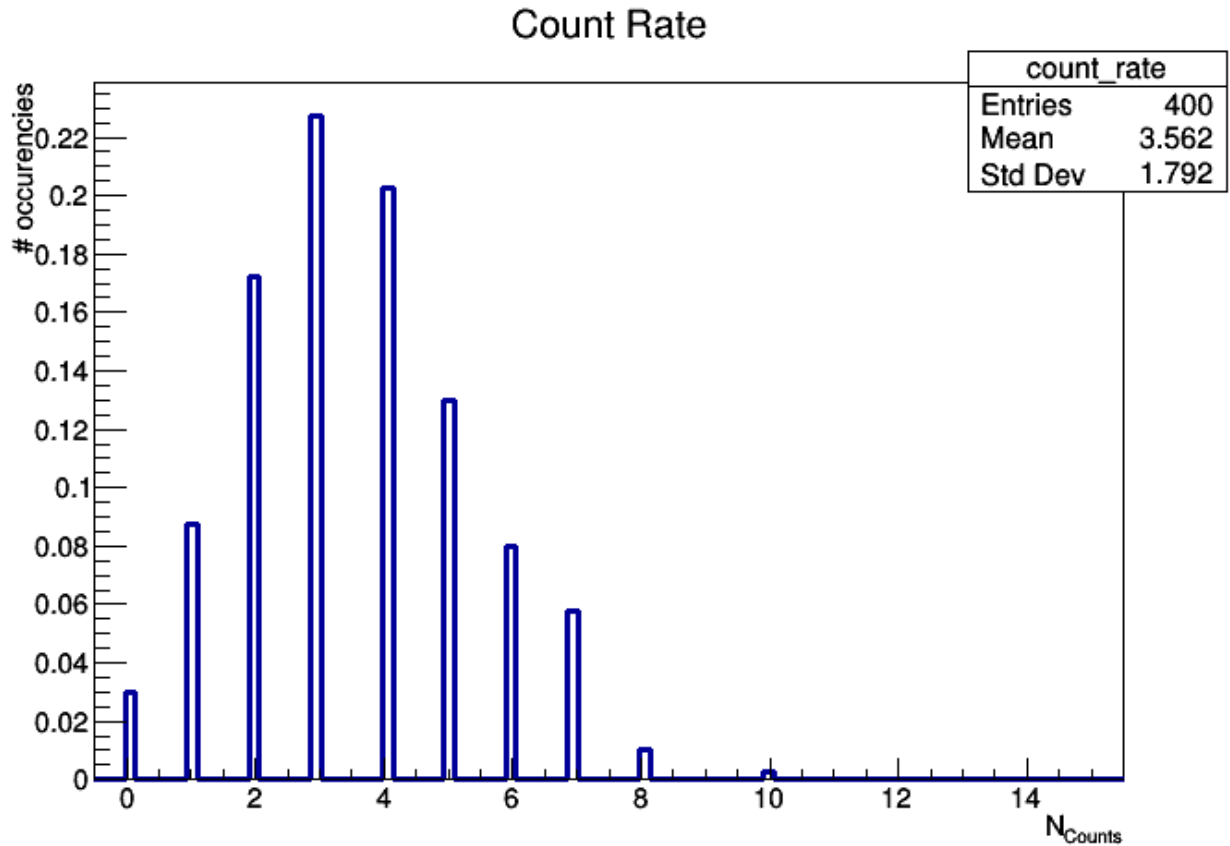
Figure 14: Creating a Histogram: example 2

5.2 Add and Divide Histograms

Quite a large number of operations can be carried out with histograms. The most useful are addition and division. In the following macro we will learn how to manage these procedures within ROOT.

Some lines now need a bit of clarification:

- Cling, as we know, is also able to interpret more than one function per file. In this case the format_h function simply sets up some parameters to conveniently set the line of histograms.

```
%%cpp -d
// Divide and add 1D Histograms

void format_h(TH1F* h, int linecolor){
    h->SetLineWidth(3);
    h->SetLineColor(linecolor);
    }

    auto sig_h=new TH1F("sig_h","Signal Histo",50,0,10);
    auto gaus_h1=new TH1F("gaus_h1","Gauss Histo 1",30,0,10);
    auto gaus_h2=new TH1F("gaus_h2","Gauss Histo 2",30,0,10);
    auto bkg_h=new TH1F("exp_h","Exponential Histo",50,0,10);

    // simulate the measurements
    TRandom3 rndgen_5_2;
```

- Here some C++ syntax for conditional statements is used to fill the histograms with different numbers of entries inside the loop.

```cpp
for (int imeas=0; imeas<4000; imeas++){
    bkg_h->Fill(rndgen_5_2.Exp(4));
    if (imeas%4==0) gaus_h1->Fill(rndgen_5_2.Gaus(5,2));
    if (imeas%4==0) gaus_h2->Fill(rndgen_5_2.Gaus(5,2));
    if (imeas%10==0)sig_h->Fill(rndgen_5_2.Gaus(5,.5));}

// Format Histograms
int i=0;
for (auto hist : {sig_h,bkg_h,gaus_h1,gaus_h2})
    format_h(hist,1+i++);

// Sum
auto sum_h= new TH1F(*bkg_h);
```

- Here the sum of two histograms. A weight, which can be negative, can be assigned to the added histogram.

```cpp
sum_h->Add(sig_h,1.);
sum_h->SetTitle("Exponential + Gaussian;X variable;Y variable");
format_h(sum_h,kBlue);

auto canvas_5_2_sum= new TCanvas();
sum_h->Draw("hist");
bkg_h->Draw("SameHist");
sig_h->Draw("SameHist");
```

- The division of two histograms is rather straightforward.

```cpp
// Divide
auto dividend=new TH1F(*gaus_h1);
dividend->Divide(gaus_h2);
```

- When you draw two quantities and their ratios, it is much better if all the information is condensed in one single plot. These lines provide a skeleton to perform this operation.

```cpp
// Graphical Maquillage
dividend->SetTitle(";X axis;Gaus Histogram 1 / Gaus Histogram 2");
format_h(dividend,kOrange);
gaus_h1->SetTitle(";;Gaus Histo 1 and Gaus Histo 2");
gStyle->SetOptStat(0);

TCanvas* canvas_5_2_divide= new TCanvas();
canvas_5_2_divide->Divide(1,2,0,0);
canvas_5_2_divide->cd(1);
canvas_5_2_divide->GetPad(1)->SetRightMargin(.01);
gaus_h1->DrawNormalized("Hist");
gaus_h2->DrawNormalized("HistSame");

canvas_5_2_divide->cd(2);
dividend->GetYaxis()->SetRangeUser(0,2.49);
canvas_5_2_divide->GetPad(2)->SetGridy();
canvas_5_2_divide->GetPad(2)->SetRightMargin(.01);
dividend->Draw();

canvas_5_2_sum->Draw();
canvas_5_2_divide->Draw();
```
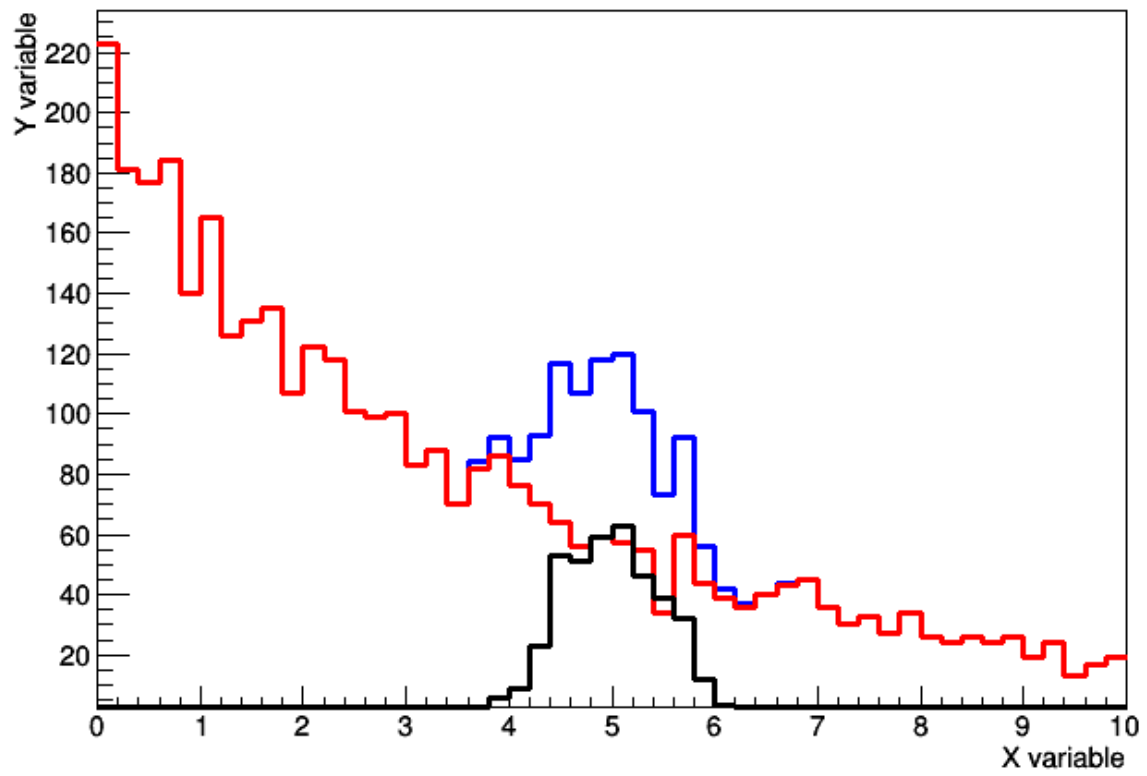
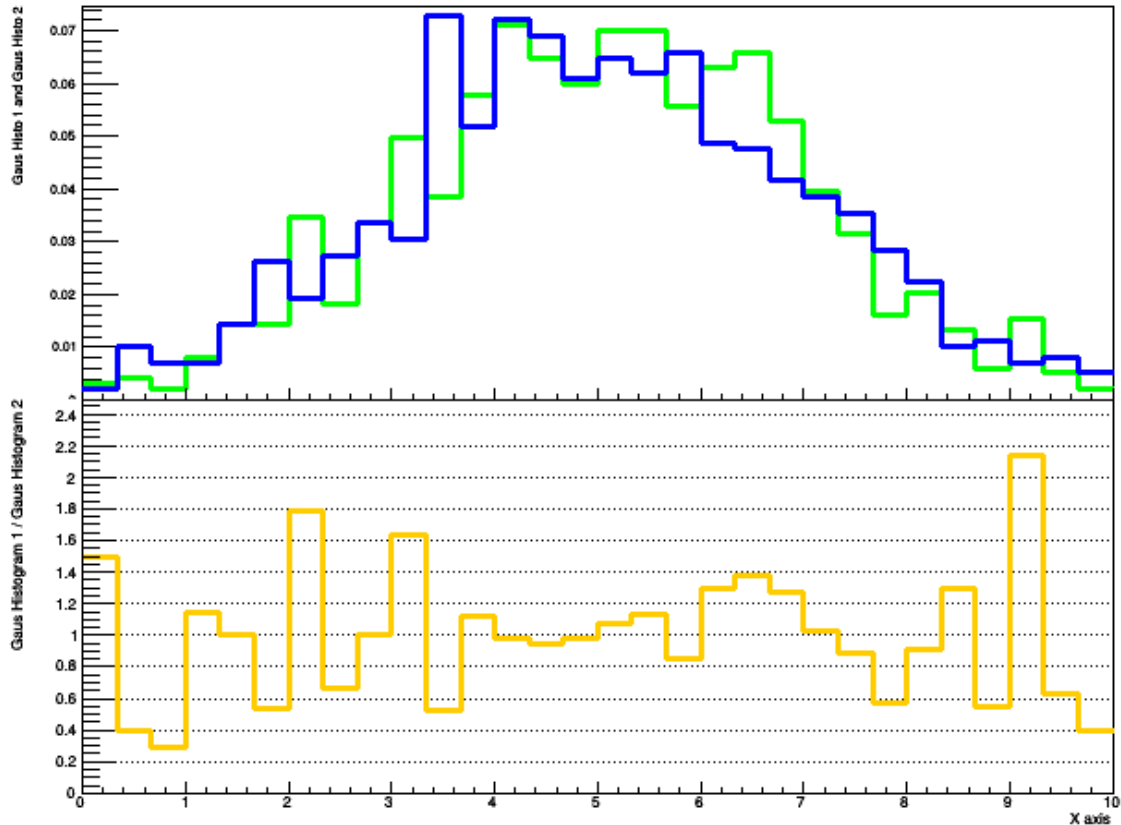Figure 15: Adding and dividing Histograms

Figure 16: Adding and dividing Histograms

5.3 Two-dimensional Histograms

Two-dimensional histograms are a very useful tool, for example to inspect correlations between variables. You can exploit the bi-dimensional histogram classes provided by ROOT in a simple way. Let's see how in this code:

```
%jsroot off

// Draw a Bidimensional Histogram in many ways
// together with its profiles and projections

gStyle->SetPalette(kBird);
gStyle->SetOptStat(0);
gStyle->SetOptTitle(0);

TH2F bidi_h("bidi_h","2D Histo;Gaussian Vals;Exp. Vals",
            30,-5,5,  // X axis
            30,0,10); // Y axis

TRandom3 rgen_5_3;
for (int i=0;i<500000;i++)
    bidi_h.Fill(rgen_5_3.Gaus(0,2),10-rgen_5_3.Exp(4),.1);

auto canvas_5_3_1=new TCanvas("canvas_5_3_1","canvas_5_3_1",800,800);
canvas_5_3_1->Divide(2,2);
canvas_5_3_1->cd(1);bidi_h.Draw("Cont1");
canvas_5_3_1->cd(2);bidi_h.Draw("Colz");
canvas_5_3_1->cd(3);bidi_h.Draw("lego");
```

```
canvas_5_3_1->cd(4);bidi_h.Draw("surf3");
    // Profiles and Projections
canvas_5_3_1->Draw();
```
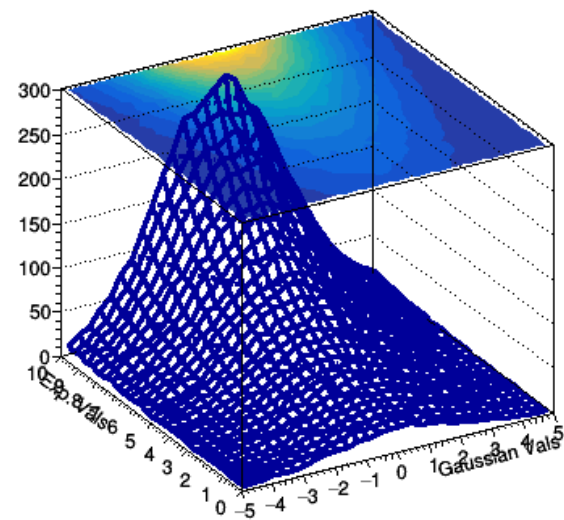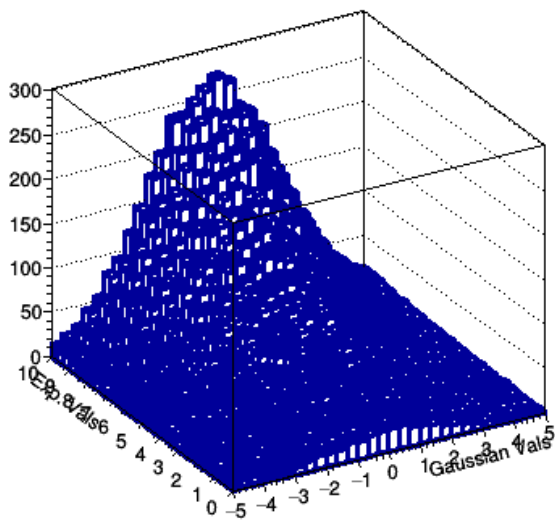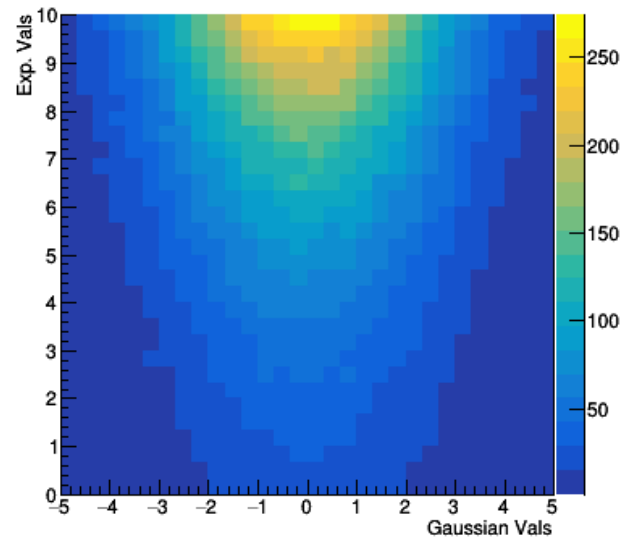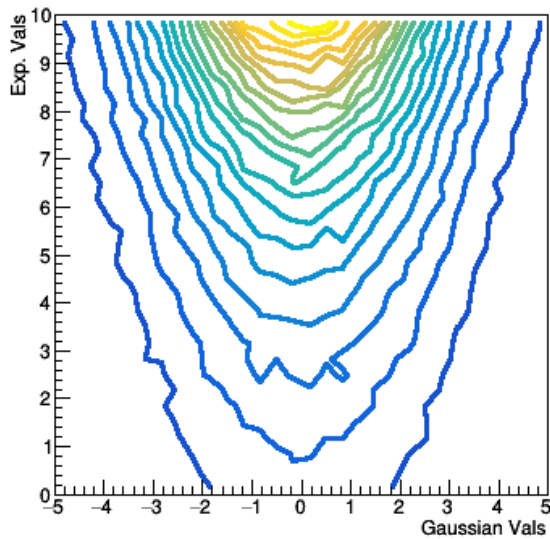

Figure 17: 2D Histograms example1

```
auto canvas_5_3_2=new TCanvas("canvas_5_3_2","canvas_5_3_2",800,800);
canvas_5_3_2->Divide(2,2);
canvas_5_3_2->cd(1);bidi_h.ProjectionX()->DrawClone();
canvas_5_3_2->cd(2);bidi_h.ProjectionY()->DrawClone();
canvas_5_3_2->cd(3);bidi_h.ProfileX()->DrawClone();
canvas_5_3_2->cd(4);bidi_h.ProfileY()->DrawClone();

canvas_5_3_2->Draw();
```
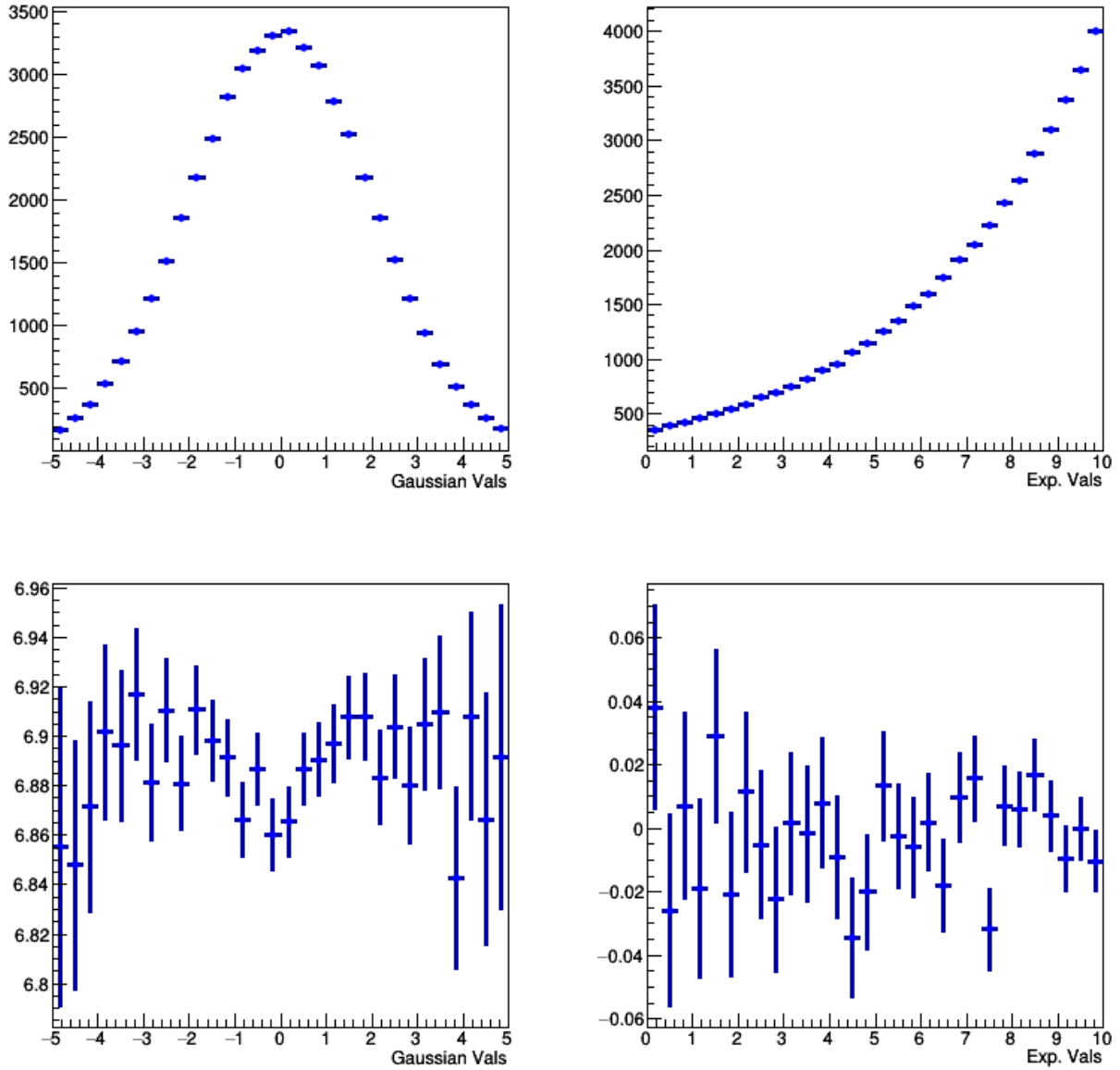
Figure 18: 2D Histograms example2

Two kinds of plots are provided within the code, the first one containing three-dimensional representations and the second one projections and profiles of the bi-dimensional histogram.

The projections and profiles of bi-dimensional histograms.

When a projection is performed along the x (y) direction, for every bin along the x (y) axis, all bin contents along the y (x) axis are summed up. When a profile is performed along the x (y) direction, for every bin along the x (y) axis, the average of all the bin contents along the y (x) is calculated together with their RMS and displayed as a symbol with error bar.

Correlations between the variables are quantified by the methods `Double_t GetCovariance()` and `Double_t GetCorrelationFactor()`.

5.4 Multiple histograms

The class `THStack` allows to manipulate a set of histograms as a single entity. It is a collection of `TH1` (or derived) objects. When drawn, the X and Y axis ranges are automatically computed such as all the histograms will be visible. Several drawing option are available for both 1D and 2D histograms. The next macros shows how it looks for 2D histograms:

```
%jsroot off
```

```
// Example of stacked histograms using the class THStack
auto canvas_5_4=new TCanvas("canvas_5_4","canvas_5_4", 900, 700);
```

- Here we create the stack.

```
THStack *stHistogram_5_4 = new THStack("stHistogram_5_4","Stacked 2D histograms");
```

- Here we create two histograms to be added in the stack.

```
TF2 *f1 = new TF2("f1","xygaus + xygaus(5) + xylandau(10)",-4,4,-4,4);
Double_t params1[] = {130,-1.4,1.8,1.5,1, 150,2,0.5,-2,0.5, 3600,-2,0.7,-3,0.3};
f1->SetParameters(params1);
TH2F *histogram_5_4_1 = new TH2F("histogram_5_4_1","histogram_5_4_1",20,-4,4,20,-4,4);
histogram_5_4_1->SetFillColor(38);
histogram_5_4_1->FillRandom("f1",4000);
TF2 *f2 = new TF2("f2","xygaus + xygaus(5)",-4,4,-4,4);
Double_t params2[] = {100,-1.4,1.9,1.1,2, 80,2,0.7,-2,0.5};
f2->SetParameters(params2);
TH2F *histogram_5_4_2 = new TH2F("histogram_5_4_2","histogram_5_4_2",20,-4,4,20,-4,4);
histogram_5_4_2->SetFillColor(46);
histogram_5_4_2->FillRandom("f2",3000);
```

- Here we add the histograms in the stack.

```
stHistogram_5_4->Add(histogram_5_4_1);
stHistogram_5_4->Add(histogram_5_4_2);
```

- Finally we draw the stack as a lego plot. In which the colour distinguish the two histograms.

```
stHistogram_5_4->DrawClone();
canvas_5_4->Draw();
```
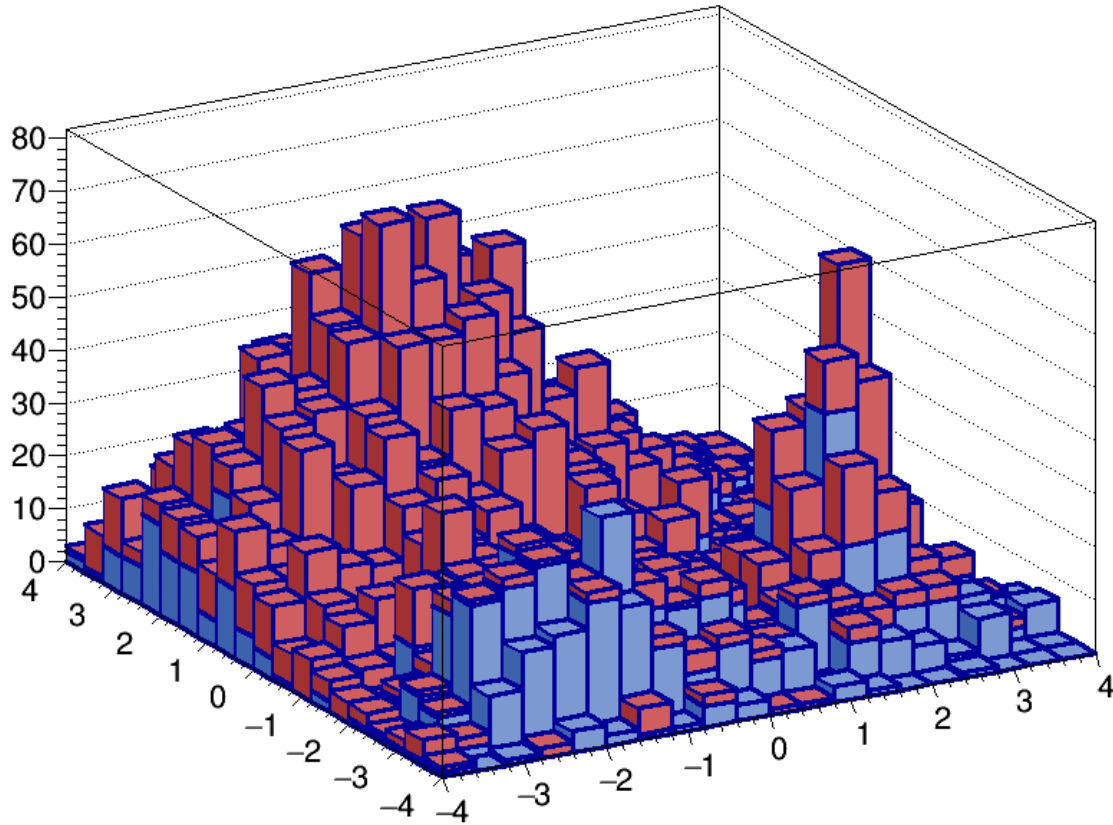
Figure 19: 2D stacked Histograms example

6 Functions and Parameter Estimation

6.1 Fitting Functions to Pseudo Data

In the example below, a pseudo-data set is produced and a model fitted to it.

ROOT offers various minimisation algorithms to minimise a χ^{2} or a negative log-likelihood function. The default minimiser is MINUIT, a package originally implemented in the FORTRAN programming language. A C++ version is also available, MINUIT2, as well as Fumili (Silin 1983) an algorithm optimised for fitting. The minimisation algorithms can be selected using the static functions of the `ROOT::Math::MinimizerOptions` class. Steering options for the minimiser, such as the convergence tolerance or the maximum number of function calls, can also be set using the methods of this class. All currently implemented minimisers are documented in the reference documentation of ROOT: have a look for example to the `ROOT::Math::Minimizer` class documentation. The complication level of the code below is intentionally a little higher than in the previous examples.

Let's go through the code, step by step to understand what is going on:

- First we create a simple function to ease the make-up of lines. Remember that the class TF1 inherits from TAttLine.

```
// %jsroot on

%%cpp -d
void format_line(TAttLine* line,int col,int sty){
```

```
line->SetLineWidth(5); line->SetLineColor(col);
line->SetLineStyle(sty);}
```

- Here we creat a definition of a customised function, namely a Gaussian (the "signal") plus a parabolic function, the "background".

```
%%cpp -d
double the_gausppar(double* vars, double* pars){
return pars[0]*TMath::Gaus(vars[0],pars[1],pars[2])+pars[3]+pars[4]*vars[0]+pars[5]*vars[0]*vars[0];}
```

- Some make-up for the Canvas. In particular we want that the parameters of the fit appear very clearly and nicely on the plot.

```
auto canvas_6_1=new TCanvas("canvas_6_1","canvas_6_1");
gStyle->SetOptTitle(0); gStyle->SetOptStat(0);
gStyle->SetOptFit(1111); gStyle->SetStatBorderSize(0);
gStyle->SetStatX(.89); gStyle->SetStatY(.89);

TF1 parabola("parabola","[0]+[1]*x+[2]*x**2",0,20);
format_line(&parabola,kBlue,2);

TF1 gaussian("gaussian","[0]*TMath::Gaus(x,[1],[2])",0,20);
format_line(&gaussian,kRed,2);
```

- Next we define and initialise an instance of TF1.

```
TF1 gausppar("gausppar",the_gausppar,-0,20,6);
double a=15; double b=-1.2; double c=.03;
double normal=4; double mean=7; double sigma=1;
gausppar.SetParameters(normal,mean,sigma,a,b,c);
gausppar.SetParNames("Normal","Mean","Sigma","a","b","c");
format_line(&gausppar,kBlue,1);
```

- Followed by the definition and the filling of a histogram.

```
TH1F histo("histo","Signal plus background;X vals;Y Vals",50,0,20);
histo.SetMarkerStyle(8);

// Fake the data
for (int i=1;i<=5000;++i) histo.Fill(gausppar.GetRandom());
```

- For convenience, the same function as for the generation of the pseudo-data is used in the fit; hence, we need to reset the function parameters. This part of the code is very important for each fit procedure, as it sets the initial values of the fit.

```
// Reset the parameters before the fit and set
// by eye a peak at 6 with an area of more or less 50
gausppar.SetParameter(0,50);
gausppar.SetParameter(1,6);
int npar=gausppar.GetNpar();
for (int ipar=2;ipar<npar;++ipar) gausppar.SetParameter(ipar,1);
```

- Next a very simple command, well known by now: fit the function to the histogram.

```
// perform fit ...
auto fitResPtr = histo.Fit(&gausppar, "S");
 FCN=42.0305 FROM MIGRAD    STATUS=CONVERGED   1207 CALLS        1208 TOTAL
                    EDM=5.17306e-07    STRATEGY= 1  ERROR MATRIX UNCERTAINTY   2.2 per cent
  EXT PARAMETER                                STEP        FIRST
  NO.   NAME      VALUE            ERROR       SIZE      DERIVATIVE
   1  Normal      5.78269e+01   7.94068e+00   5.77561e-02   4.28977e-05
   2  Mean        7.01009e+00   1.35383e-01  -3.22514e-04   7.29243e-05
   3  Sigma       9.23834e-01   1.57793e-01  -2.59746e-04   2.77085e-03
   4  a           2.00626e+02   5.50591e+00   2.33533e-03  -2.57315e-04
```

```
    5   b                  -1.67332e+01    1.03021e+00  -1.03565e-04    1.76478e-04
    6   c                   4.43814e-01    4.63690e-02  -4.30880e-05    2.61849e-02
```

- We then retrieve the output from the fit. Here, we simply print the fit result and access and print the covariance matrix of the parameters.

```
// ... and retrieve fit results
fitResPtr->Print(); // print fit results
// get covariance Matrix an print it
TMatrixDSym covMatrix (fitResPtr->GetCovarianceMatrix());
covMatrix.Print();

// Set the values of the gaussian and parabola
for (int ipar=0;ipar<3;ipar++){
    gaussian.SetParameter(ipar,gausppar.GetParameter(ipar));
    parabola.SetParameter(ipar,gausppar.GetParameter(ipar+3));
}

****************************************
Minimizer is Minuit / Migrad
Chi2                      =         42.0305
NDf                       =              44
Edm                       =     5.17306e-07
NCalls                    =            1208
Normal                    =         57.8269   +/-   7.94068
Mean                      =         7.01009   +/-   0.135383
Sigma                     =        0.923834   +/-   0.157793
a                         =         200.626   +/-   5.50591
b                         =        -16.7332   +/-   1.03021
c                         =        0.443814   +/-   0.046369


6x6 matrix is as follows

        |       0    |       1    |       2    |       3    |       4    |
        --------------------------------------------------------------------
    0 |      63.05       0.08809      -0.5976       -2.663      -0.3044
    1 |     0.08809      0.01833    -0.005144       0.1111     -0.01496
    2 |     -0.5976    -0.005144       0.0249      -0.1629    -0.009859
    3 |      -2.663       0.1111      -0.1629        30.32       -4.738
    4 |     -0.3044     -0.01496    -0.009859       -4.738        1.061
    5 |     0.02711    0.0004654     0.001147       0.1721     -0.04605


        |       5    |
        --------------------------------------------------------------------
    0 |     0.02711
    1 |   0.0004654
    2 |    0.001147
    3 |      0.1721
    4 |    -0.04605
    5 |     0.00215
```

- Finally we plot the pseudo-data, the fitted function and the signal and background components at the best-fit values.

```
histo.GetYaxis()->SetRangeUser(0,250);
histo.DrawClone("PE");
parabola.DrawClone("Same"); gaussian.DrawClone("Same");
TLatex latex(2,220,"#splitline{Signal Peak over}{background}");
latex.DrawClone("Same");
canvas_6_1->Draw();
```
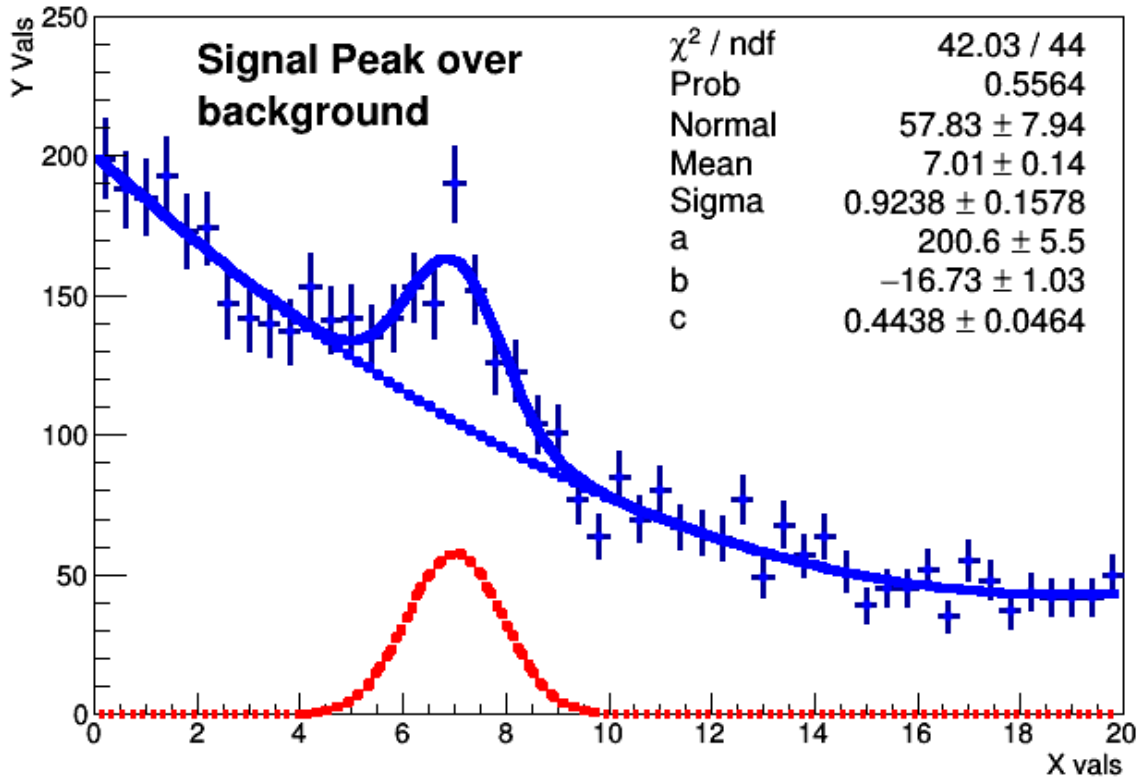
Figure 20: Fit of pseudo data: a signal shape over a background trend

Fit of pseudo data: a signal shape over a background trend. This plot is another example of how making a plot "self-explanatory" can help you better displaying your results.

6.2 Toy Monte Carlo Experiments

Let us look at a simple example of a toy experiment comparing two methods to fit a function to a histogram, the \(\chi^{2}\)

method and a method called "binned log-likelihood fit", both available in ROOT.

As a very simple yet powerful quantity to check the quality of the fit results, we construct for each pseudo-data set the so-called "pull", the difference of the estimated and the true value of a parameter, normalised to the estimated error on the parameter, \(\frac{(p_{estim} - p_{true})}{\sigma_{p}}\). If everything is OK, the distribution of the pull values is a standard normal distribution, i.e. a Gaussian distribution centred around zero with a standard deviation of one.

The macro performs a rather big number of toy experiments, where a histogram is repeatedly filled with Gaussian distributed numbers, representing the pseudo-data in this example. Each time, a fit is performed according to the selected method, and the pull is calculated and filled into a histogram. Here is the code:

```
// %jsroot off
```

```
%%cpp -d
// Toy Monte Carlo example.
// Check pull distribution to compare chi2 and binned
// log-likelihood methods.
```

```
void pull( int n_toys = 10000,
    int n_tot_entries = 100,
    int nbins = 40,
    bool do_chi2=true ){

    TString method_prefix("LogLikelihood");
    if (do_chi2)
        method_prefix="chi2";

    // Create histo
    TH1F h4(method_prefix+"h4",
            method_prefix+" Random Gauss",
            nbins,-4,4);
    h4.SetMarkerStyle(21);
    h4.SetMarkerSize(0.8);
    h4.SetMarkerColor(kRed);

    // Histogram for sigma and pull
    TH1F sigma(method_prefix+" sigma",
                method_prefix+" sigma from gaus fit",
                50,0.5,1.5);
    TH1F pull(method_prefix+" pull",
                method_prefix+" pull from gaus fit",
                50,-4.,4.);
    // Make a nice devided canvas
    auto *canvas_6_2 = new TCanvas(method_prefix+"canvas_6_2",method_prefix+"canvas_6_2",800,400);
    canvas_6_2->Divide(2,1);
    canvas_6_2->cd(1);canvas_6_2->SetGrid();


    float sig, mean;
    for (int i=0; i<n_toys; i++){
        // Reset histo contents
        h4.Reset();
        // Fill histo
        for ( int j = 0; j<n_tot_entries; j++ )
        h4.Fill(gRandom->Gaus());
        // perform fit
        if (do_chi2) h4.Fit("gaus","q"); // Chi2 fit
        else h4.Fit("gaus","lq"); // Likelihood fit
        // some control output on the way
        if (!(i%100)){
            h4.DrawClone("ep");
            canvas_6_2->Update();
        }

        // Get sigma from fit
        TF1 *fit = h4.GetFunction("gaus");
        sig = fit->GetParameter(2);
        mean= fit->GetParameter(1);
        sigma.Fill(sig);
        pull.Fill(mean/sig * sqrt(n_tot_entries));
    }
    // end of toy MC loop
    h4.DrawClone("ep");
    canvas_6_2->Draw();
    canvas_6_2->cd(2);
```

```
      // print result
      pull.DrawClone();
      canvas_6_2->Draw();


}

int n_toys=10000;
int n_tot_entries=100;
int n_bins=40;
pull(n_toys,n_tot_entries,n_bins,true);
pull(n_toys,n_tot_entries,n_bins,false);
```
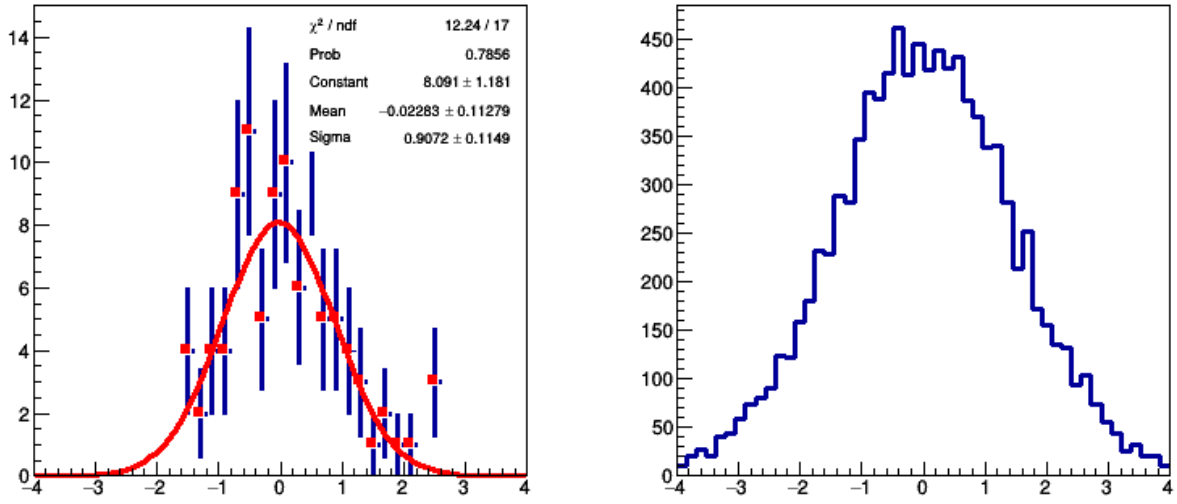

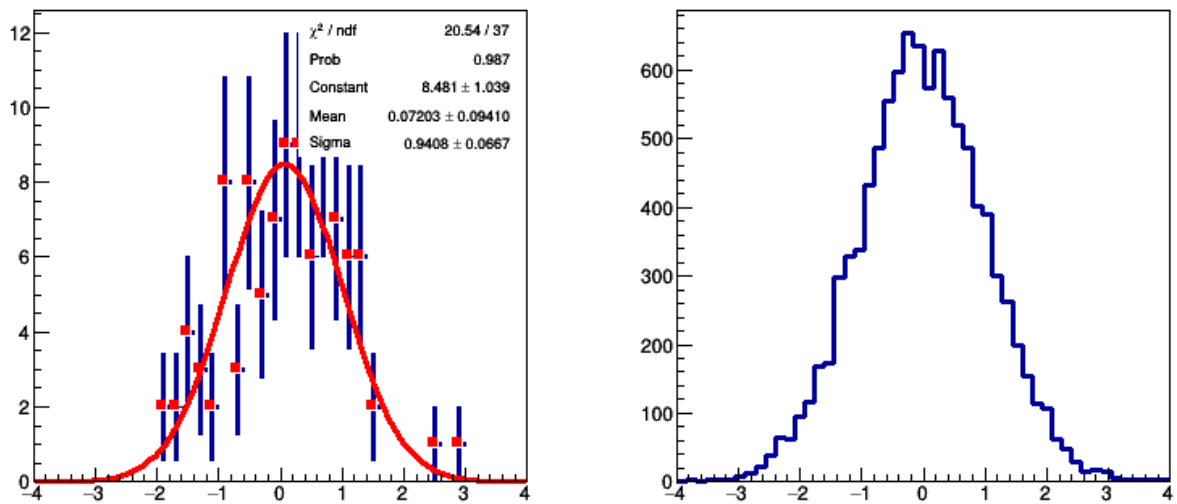Figure 21: A simple example of a toy experiment comparing two methods to fit a function to a histogram

Figure 22: A simple example of a toy experiment comparing two methods to fit a function to a histogram

Your present knowledge of ROOT should be enough to understand all the technicalities behind the macro. Note that the variable pull in line 61 is different from the definition above: instead of the parameter error on mean, the fitted standard deviation of the distribution divided by the square root of the number of entries, `sig/sqrt(n_tot_entries)`, is used.

- What method exhibits the better performance with the default parameters?

- What happens if you increase the number of entries per histogram by a factor of ten? Why?

The answers to these questions are well beyond the scope of this guide. Basically all books about statistical methods provide a complete treatment of the aforementioned topics.

7 File IO and Parallel Analysis

7.1 Storing ROOT Objects

ROOT offers the possibility to write instances of classes on disk, into a ROOT-file (see the `TFile` class for more details). One says that the object is made "persistent" by storing it on disk. When reading the file back, the object is reconstructed in memory. The requirement to be satisfied to perform I/O of instances of a certain class is that the ROOT type system is aware of the layout in memory of that class. This topic is beyond the scope of this document: it is worth to mention that I/O can be performed out of the box for the almost complete set of ROOT classes.

We can explore this functionality with histograms and two simple macros.

```
// Instance of our histogram
TH1F histogram_7_1("stored_histogram","histogram_7_1;X;# of entries",100,-5,5);

// Let's fill it randomly
histogram_7_1.FillRandom("gaus");

// Let's open a TFile
TFile out_file("../data/my_rootfile.root","RECREATE");

// Write the histogram in the file
histogram_7_1.Write();
// Close the file
out_file.Close();
```

Not bad, eh ? Especially for a language that does not foresees persistency natively like C++. The RECREATE option forces ROOT to create a new file even if a file with the same name exists on disk.

Now, you may use the Cling command line to access information in the file and draw the previously written histogram:

```
>  root my_rootfile.root
root [0]
Attaching file my_rootfile.root as _file0...
root [1] _file0->ls()
TFile**     my_rootfile.root
 TFile*     my_rootfile.root
  KEY: TH1F my_histogram;1 My Title
root [2] my_histogram->Draw()
```

Alternatively, you can use a simple macro to carry out the job:

```
// %jsroot debug
auto canvas_7_1=new TCanvas("canvas_7_1","canvas_7_1");
// Let's open the TFile
TFile in_file("../data/my_rootfile.root");
```

```
// Get the Histogram out
TH1F* histogram_7_1_2;
in_file.GetObject("stored_histogram",histogram_7_1_2);

// Draw it
histogram_7_1_2->Draw();
canvas_7_1->Draw();
```
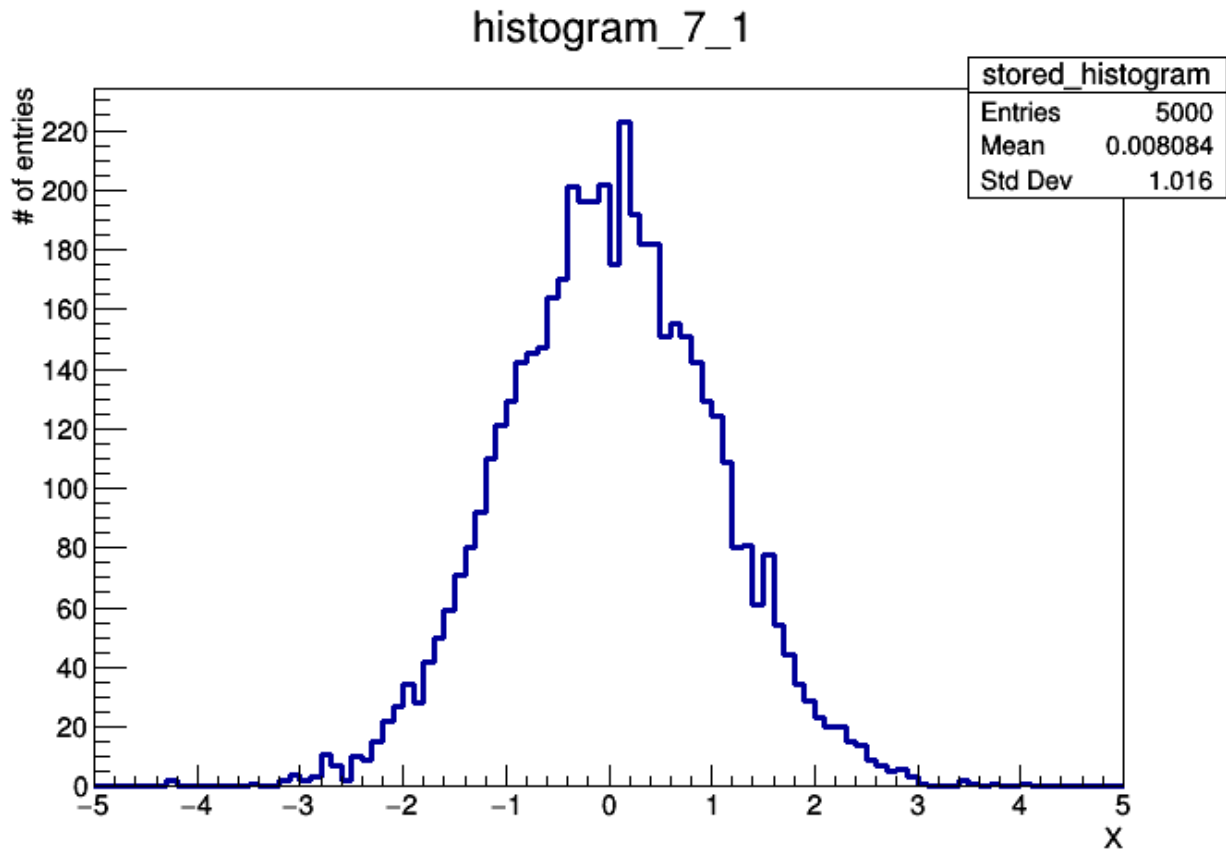

Figure 23: Creating persistent objects

7.2 N-tuples in ROOT

7.2.1 Storing simple N-tuples

Up to now we have seen how to manipulate input read from ASCII files. ROOT offers the possibility to do much better than that, with its own n-tuple classes. Among the many advantages provided by these classes one could cite

- Optimised disk I/O.

- Possibility to store many n-tuple rows.

- Write the n-tuples in ROOT files.

- Interactive inspection with `TBrowser`.

- Store not only numbers, but also objects in the columns.

In this section we will discuss briefly the `TNtuple` class, which is a simplified version of the `TTree` class. A ROOT `TNtuple` object can store rows of float entries. Let's tackle the problem according to the usual strategy commenting a minimal example

```cpp
// Fill an n-tuple and write it to a file simulating measurement of
// conductivity of a material in different conditions of pressure
// and temperature.

    TFile ofile("../data/conductivity_experiment.root","RECREATE");

    // Initialise the TNtuple
    TNtuple cond_data("cond_data",
                      "Example N Tuple",
                      "Potential:Current:Temperature:Pressure");

    // Fill it randomly to fake the acquired data
    TRandom3 rndm;
    float pot,cur,temp,pres;
    for (int i=0;i<10000;++i){
        pot=rndm.Uniform(0.,10.);      // get voltage
        temp=rndm.Uniform(250.,350.);  // get temperature
        pres=rndm.Uniform(0.5,1.5);    // get pressure
        cur=pot/(10.+0.05*(temp-300.)-0.2*(pres-1.)); // current
// add some random smearing (measurement errors)
        pot*=rndm.Gaus(1.,0.01); // 1% error on voltage
        temp+=rndm.Gaus(0.,0.3); // 0.3 abs. error on temp.
        pres*=rndm.Gaus(1.,0.02);// 1% error on pressure
        cur*=rndm.Gaus(1.,0.01); // 1% error on current
// write to ntuple
        cond_data.Fill(pot,cur,temp,pres);
        }

    // Save the ntuple and close the file
    cond_data.Write();
//      ofile.Close();
```

This data written to this example n-tuple represents, in the statistical sense, three independent variables (Potential or Voltage, Pressure and Temperature), and one variable (Current) which depends on the others according to very simple laws, and an additional Gaussian smearing. This set of variables mimics a measurement of an electrical resistance while varying pressure and temperature.

Imagine your task now consists in finding the relations among the variables – of course without knowing the code used to generate them. You will see that the possibilities of the `NTuple` class enable you to perform this analysis task. Open the ROOT file (`cond_data.root`) written by the macro above in an interactive session and use a `TBrowser` to interactively inspect it:

```
root[0] TBrowser b
```

You find the columns of your n-tuple written as leafs. Simply clicking on them you can obtain histograms of the variables!

Next, try the following commands at the shell prompt and in the interactive ROOT shell, respectively:

```
> root conductivity_experiment.root
Attaching file conductivity_experiment.root as _file0...
root [0] cond_data->Draw("Current:Potential")
```

```cpp
auto canvas_7_2=new TCanvas("canvas_7_2","canvas_7_2");
cond_data.Draw("Current:Potential");
canvas_7_2->Draw();
```
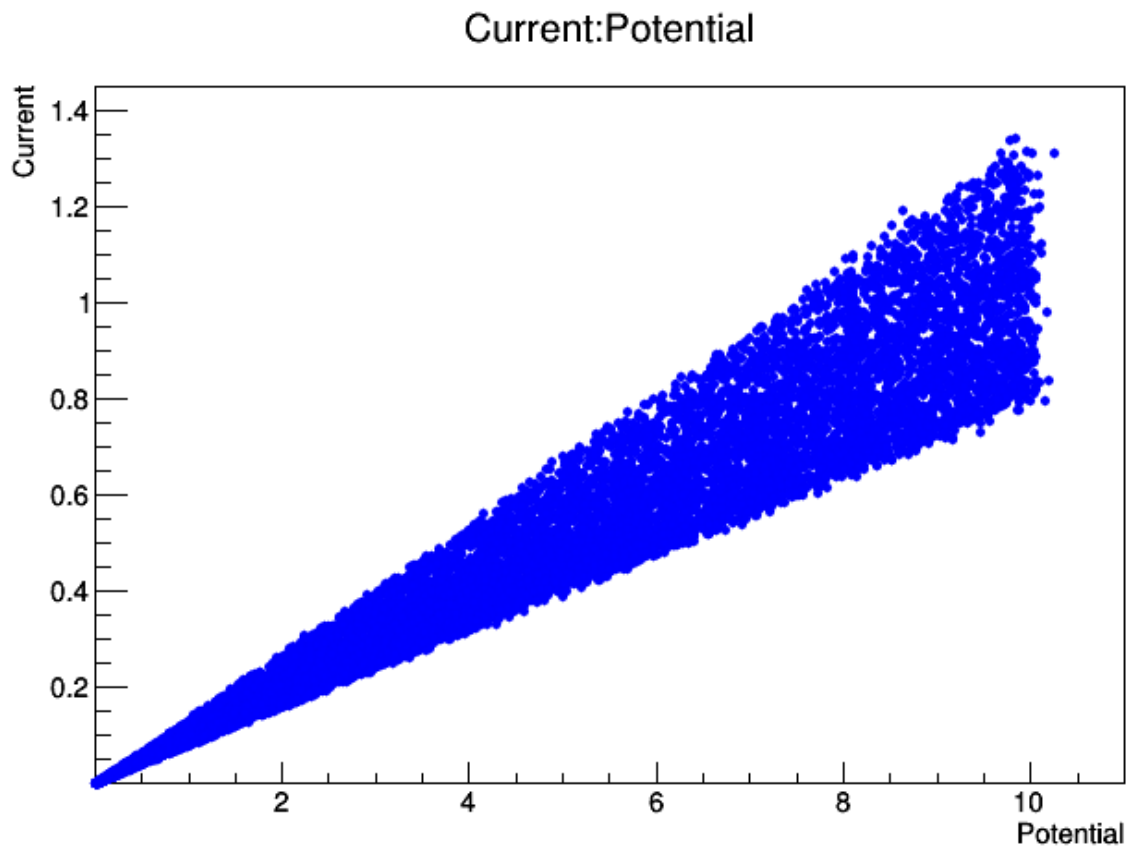
Figure 24: Drawing stored Ntuple objects

You just produced a correlation plot with one single line of code!

Try to extend the syntax typing for example

```
root [1] cond_data->Draw("Current:Potential","Temperature<270")
```

```cpp
auto canvas_7_3=new TCanvas("canvas_7_3","canvas_7_3");
cond_data.Draw("Current:Potential","Temperature<270");
canvas_7_3->Draw();
```
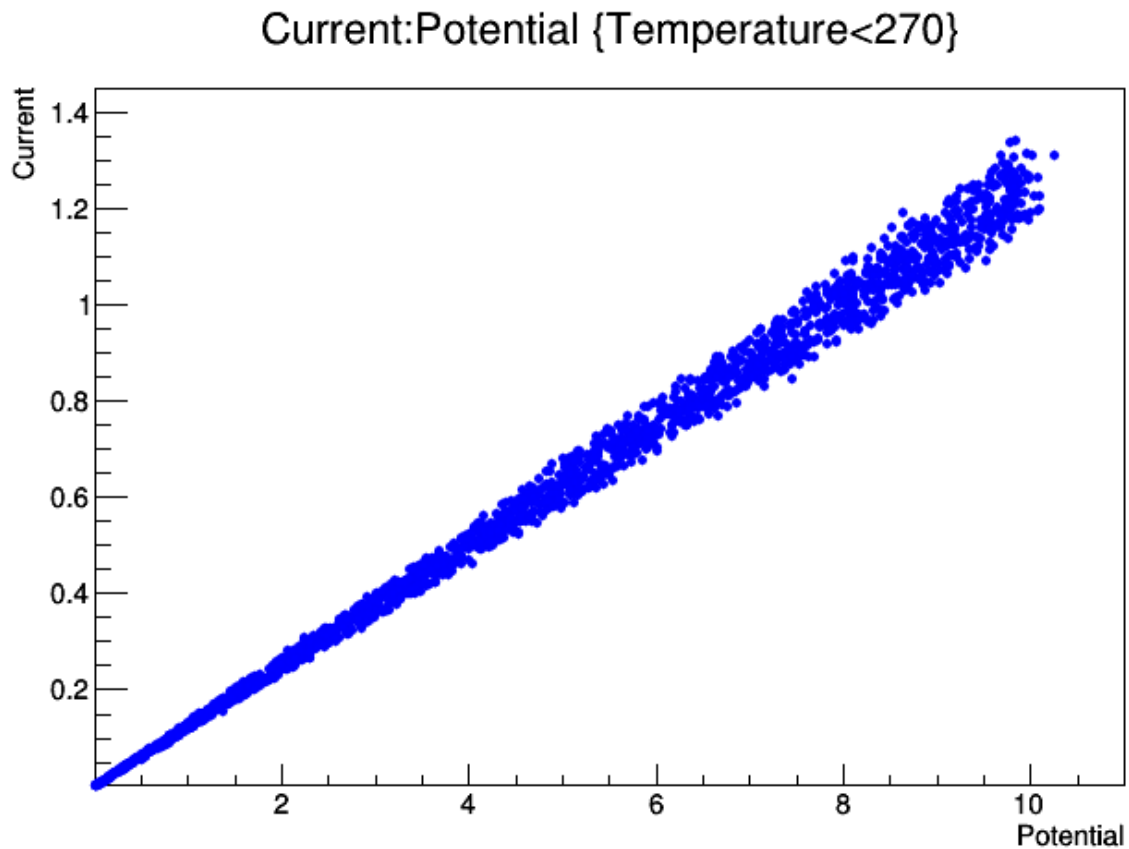
Figure 25: Stored Ntuple objects with data selection example1

What do you obtain ?

Now try

```
root [2] cond_data->Draw("Current/Potential:Temperature")
```

You will see this result:

```
auto canvas_7_4=new TCanvas("canvas_7_4","canvas_7_4");
cond_data.Draw("Current/Potential:Temperature");
canvas_7_4->Draw();
```
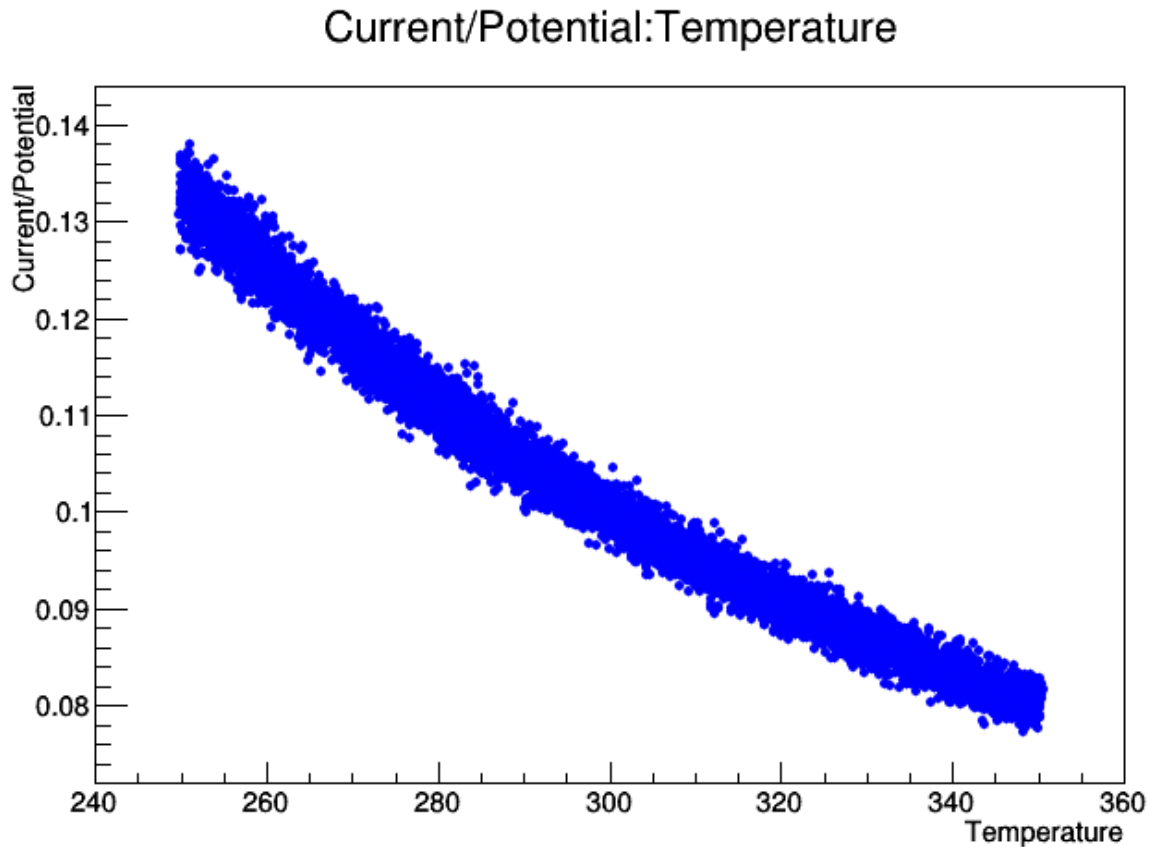
Figure 26: Stored Ntuple objects with data selection example2

It should have become clear from these examples how to navigate in such a multi-dimensional space of variables and unveil relations between variables using n-tuples.

7.2.2 Reading N-tuples

For completeness, you find here a small macro to read the data back from a ROOT n-tuple

```cpp
%%cpp -d
// Read the previously produced N-Tuple and print on screen
// its content

void read_ntuple_from_file(){

    // Open a file, save the ntuple and close the file
    TFile in_file("../data/conductivity_experiment.root");
    TNtuple* my_tuple;in_file.GetObject("cond_data",my_tuple);
    float pot,cur,temp,pres; float* row_content;

    cout << "Potential\tCurrent\tTemperature\tPressure\n";
    for (int irow=0;irow<my_tuple->GetEntries();++irow){
        my_tuple->GetEntry(irow);
        row_content = my_tuple->GetArgs();
        pot = row_content[0];
        cur = row_content[1];
        temp = row_content[2];
        pres = row_content[3];
```

```
        cout << pot << "\t" << cur << "\t" << temp
             << "\t" << pres << endl;
    }


}
```

The macro shows the easiest way of accessing the content of a n-tuple: after loading the n-tuple, its branches are assigned to variables and `GetEntry(long)` automatically fills them with the content for a specific row. By doing so, the logic for reading the n-tuple and the code to process it can be split and the source code remains clear.

7.2.3 Storing Arbitrary N-tuples

It is also possible to write n-tuples of arbitrary type by using ROOT's `TBranch` class. This is especially important as `TNtuple::Fill()` accepts only floats. The following macro creates the same n-tuple as before but the branches are booked directly. The `Fill()` function then fills the current values of the connected variables to the tree.

`%%cpp -d`

```cpp
// Fill an n-tuple and write it to a file simulating measurement of
// conductivity of a material in different conditions of pressure
// and temperature using branches.

void write_ntuple_to_file_advanced(
    const std::string& outputFileName="../data/conductivity_experiment.root"
    ,unsigned int numDataPoints=1000000){

    TFile ofile(outputFileName.c_str(),"RECREATE");

    // Initialise the TNtuple
    TTree cond_data("cond_data", "Example N-Tuple");

    // define the variables and book them for the ntuple
    float pot,cur,temp,pres;
    cond_data.Branch("Potential", &pot, "Potential/F");
    cond_data.Branch("Current", &cur, "Current/F");
    cond_data.Branch("Temperature", &temp, "Temperature/F");
    cond_data.Branch("Pressure", &pres, "Pressure/F");

    for (int i=0;i<numDataPoints;++i){
        // Fill it randomly to fake the acquired data
        pot=gRandom->Uniform(0.,10.)*gRandom->Gaus(1.,0.01);
        temp=gRandom->Uniform(250.,350.)+gRandom->Gaus(0.,0.3);
        pres=gRandom->Uniform(0.5,1.5)*gRandom->Gaus(1.,0.02);
        cur=pot/(10.+0.05*(temp-300.)-0.2*(pres-1.))*
                    gRandom->Gaus(1.,0.01);
        // write to ntuple
        cond_data.Fill();}

    // Save the ntuple and close the file
    cond_data.Write();
    ofile.Close();
}
```

The `Branch()` function requires a pointer to a variable and a definition of the variable type. The following table lists some of the possible values. Please note that ROOT is not checking the input and mistakes are likely to result in serious problems. This holds especially if values are read as another type than they have been written, e.g. when storing a variable as float and reading it as double.

List of variable types that can be used to define the type of a branch in ROOT:

type	size	C++	identifier
signed integer	32 bit	int	I
	64 bit	long	L
unsigned integer	32 bit	unsigned int	i
	64 bit	unsigned long	l
floating point	32 bit	float	F
	64 bit	double	D
boolean	-	bool	O

7.2.4 Processing N-tuples Spanning over Several Files

Usually n-tuples or trees span over many files and it would be difficult to add them manually. ROOT thus kindly provides a helper class in the form of `TChain`. Its usage is shown in the following macro which is very similar to the previous example. The constructor of a `TChain` takes the name of the `TTree` (or `TNuple`) as an argument. The files are added with the function `Add(fileName)`, where one can also use wild-cards as shown in the example.

```cpp
%%cpp -d
// Read several previously produced N-Tuples and print on screen its
// content.
//
// you can easily create some files with the following statement:
//
// for i in 0 1 2 3 4 5; \\
// do root -l -x -b -q \\
// "write_ntuple_to_file.cxx \\
// (\"conductivity_experiment_${i}.root\", 100)"; \\
//  done


void read_ntuple_with_chain(){
   // initiate a TChain with the name of the TTree to be processed
   TChain in_chain("cond_data");
   in_chain.Add("../data/conductivity_experiment*.root"); // add files,
                                          // wildcards work

   // define variables and assign them to the corresponding branches
   float pot, cur, temp, pres;
   in_chain.SetBranchAddress("Potential", &pot);
   in_chain.SetBranchAddress("Current", &cur);
   in_chain.SetBranchAddress("Temperature", &temp);
   in_chain.SetBranchAddress("Pressure", &pres);

   cout << "Potential\tCurrent\tTemperature\tPressure\n";
   for (size_t irow=0; irow<in_chain.GetEntries(); ++irow){
      in_chain.GetEntry(irow); // loads all variables that have
                               // been connected to branches
      cout << pot << "\t" << cur << "\t" << temp <<
                     "\t" << pres << endl;
   }
}
```

7.2.5 For the advanced user: Processing trees with a selector script

Another very general and powerful way of processing a `TChain` is provided via the method `TChain::Process()`. This method takes as arguments an instance of a – user-implemented– class of type `TSelector`, and – optionally

– the number of entries and the first entry to be processed. A template for the class `TSelector` is provided by the method `TTree::MakeSelector`, as is shown in the little macro makeSelector.C below.

It opens the n-tuple `conductivity_experiment.root` from the example above and creates from it the header file `MySelector.h` and a template to insert your own analysis code, `MySelector.C`.

```
{
// create template class for Selector to run on a tree
//////////////////////////////////////////////////////
//
// open root file containing the Tree
    TFile f("conductivity_experiment.root");
// create TTree object from it
    TTree *t; f.GetObject("cond_data",t);
// this generates the files MySelector.h and MySelector.C
    t->MakeSelector("MySelector");
}
```

The template contains the entry points `Begin()` and `SlaveBegin()` called before processing of the TChain starts, Process() called for every entry of the chain, and `SlaveTerminate()` and `Terminate()` called after the last entry has been processed. Typically, initialization like booking of histograms is performed in `SlaveBegin()`, the analysis, i.e. the selection of entries, calculations and filling of histograms, is done in `Process()`, and final operations like plotting and storing of results happen in `SlaveTerminate()` or `Terminate()`.

The entry points `SlaveBegin()` and `SlaveTerminate()` are called on so-called slave nodes only if parallel processing via PROOF or PROOF lite is enabled, as will be explained below.

A simple example of a selector class is shown in the macro MySelector.C. The example is executed with the following sequence of commands:

```
> TChain *ch=new TChain("cond_data", "Chain for Example N-Tuple");
> ch->Add("conductivity_experiment*.root");
> ch->Process("MySelector.C+");
```

As usual, the "+" appended to the name of the macro to be executed initiates the compilation of the `MySelector.C` with the system compiler in order to improve performance.

The code in `MySelector.C`, shown in the listing below, books some histograms in `SlaveBegin()` and adds them to the instance fOutput, which is of the class TList.4 The final processing in `Terminate()` allows to access histograms and store, display or save them as pictures. This is shown in the example via the TList fOutput. See the commented listing below for more details; most of the text is actually comments generated automatically by `TTree::MakeSelector`.

```
#define MySelector_cxx
// The class definition in MySelector.h has been generated automatically
// by the ROOT utility TTree::MakeSelector(). This class is derived
// from the ROOT class TSelector. For more information on the TSelector
// framework see $ROOTSYS/README/README.SELECTOR or the ROOT User Manual.


// The following methods are defined in this file:
//    Begin():        called every time a loop on the tree starts,
//                    a convenient place to create your histograms.
//    SlaveBegin():   called after Begin(), when on PROOF called only on the
//                    slave servers.
//    Process():      called for each event, in this function you decide what
//                    to read and fill your histograms.
//    SlaveTerminate: called at the end of the loop on the tree, when on PROOF
//                    called only on the slave servers.
//    Terminate():    called at the end of the loop on the tree,
//                    a convenient place to draw/fit your histograms.
//
// To use this file, try the following session on your Tree T:
//
```

```
// root> T->Process("MySelector.C")
// root> T->Process("MySelector.C","some options")
// root> T->Process("MySelector.C+")
//

#include "MySelector.h"
#include <TH2.h>
#include <TStyle.h>


void MySelector::Begin(TTree * /*tree*/)
{
   // The Begin() function is called at the start of the query.
   // When running with PROOF Begin() is only called on the client.
   // The tree argument is deprecated (on PROOF 0 is passed).

   TString option = GetOption();

}

void MySelector::SlaveBegin(TTree * /*tree*/)
{
   // The SlaveBegin() function is called after the Begin() function.
   // When running with PROOF SlaveBegin() is called on each slave server.
   // The tree argument is deprecated (on PROOF 0 is passed).

   TString option = GetOption();

}

Bool_t MySelector::Process(Long64_t entry)
{
   // The Process() function is called for each entry in the tree (or possibly
   // keyed object in the case of PROOF) to be processed. The entry argument
   // specifies which entry in the currently loaded tree is to be processed.
   // It can be passed to either MySelector::GetEntry() or TBranch::GetEntry()
   // to read either all or the required parts of the data. When processing
   // keyed objects with PROOF, the object is already loaded and is available
   // via the fObject pointer.
   //
   // This function should contain the "body" of the analysis. It can contain
   // simple or elaborate selection criteria, run algorithms on the data
   // of the event and typically fill histograms.
   //
   // The processing can be stopped by calling Abort().
   //
   // Use fStatus to set the return value of TTree::Process().
   //
   // The return value is currently not used.

   return kTRUE;
}

void MySelector::SlaveTerminate()
{
   // The SlaveTerminate() function is called after all entries or objects
   // have been processed. When running with PROOF SlaveTerminate() is called
   // on each slave server.
```

```
}

void MySelector::Terminate()
{
   // The Terminate() function is the last function to be called during
   // a query. It always runs on the client, it can be used to present
   // the results graphically or save the results to file.

}
```

7.2.6 For power-users: Multi-core processing with PROOF lite

The processing of n-tuples via a selector function of type `TSelector` through `TChain::Process()`, as described at the end of the previous section, offers an additional advantage in particular for very large data sets: on distributed systems or multi-core architectures, portions of data can be processed in parallel, thus significantly reducing the execution time. On modern computers with multi-core CPUs or hardware-threading enabled, this allows a much faster turnaround of analyses, since all the available CPU power is used.

On distributed systems, a PROOF server and worker nodes have to be set up, as described in detail in the ROOT documentation. On a single computer with multiple cores, `PROOF` lite can be used instead. Try the following little macro, RunMySelector.C, which contains two extra lines compared to the example above (adjust the number of workers according to the number of CPU cores):

```
{// set up a TChain
TChain *ch=new TChain("cond_data", "My Chain for Example N-Tuple");
 ch->Add("conductivity_experiment*.root");
// eventually, start Proof Lite on cores
TProof::Open("workers=4");
ch->SetProof();
ch->Process("MySelector.C+");}
```

The first command, `TProof::Open(const char*)` starts a local PROOF server (if no arguments are specified, all cores will be used), and the command `ch->SetProof();` enables processing of the chain using PROOF. Now, when issuing the command `ch->Process("MySelector.C+);`, the code in `MySelector.C` is compiled and executed on each slave node. The methods `Begin()` and `Terminate()` are executed on the master only. The list of n-tuple files is analysed, and portions of the data are assigned to the available slave processes. Histograms booked in SlaveBegin() exist in the processes on the slave nodes, and are filled accordingly. Upon termination, the PROOF master collects the histograms from the slaves and merges them. In `Terminate()` all merged histograms are available and can be inspected, analysed or stored. The histograms are handled via the instances fOutput of class TList in each slave process, and can be retrieved from this list after merging in Terminate.

To explore the power of this mechanism, generate some very large n-tuples using the script from the section Storing Arbitrary N-tuples - you could try 10 000 000 events (this results in a large n-tuple of about 160 MByte in size). You could also generate a large number of files and use wildcards to add the to the TChain. Now execute: `> root -l RunMySelector.C` and watch what happens:

```
Processing RunMySelector.C...
 +++ Starting PROOF-Lite with 4 workers +++
Opening connections to workers: OK (4 workers)
Setting up worker servers: OK (4 workers)
PROOF set to parallel mode (4 workers)

Info in <TProofLite::SetQueryRunning>: starting query: 1
Info in <TProofQueryResult::SetRunning>: nwrks: 4
Info in <TUnixSystem::ACLiC>: creating shared library
                            ~/DivingROOT/macros/MySelector_C.so
*==* ----- Begin of Job ----- Date/Time = Wed Feb 15 23:00:04 2012
Looking up for exact location of files: OK (4 files)
Looking up for exact location of files: OK (4 files)
```

```
Info in <TPacketizerAdaptive::TPacketizerAdaptive>:
                        Setting max number of workers per node to 4
Validating files: OK (4 files)
Info in <TPacketizerAdaptive::InitStats>:
                        fraction of remote files 1.000000
Info in <TCanvas::Print>:
        file ResistanceDistribution.png has been created
*==* ----- End of Job ----- Date/Time = Wed Feb 15 23:00:08 2012
Lite-0: all output objects have been merged
```

Log files of the whole processing chain are kept in the directory `~.proof` for each worker node. This is very helpful for debugging or if something goes wrong. As the method described here also works without using PROOF, the development work on an analysis script can be done in the standard way on a small subset of the data, and only for the full processing one would use parallelism via PROOF.

It is worth to remind the reader that the speed of typical data analysis programs limited by the I/O speed (for example the latencies implied by reading data from a hard drive). It is therefore expected that this limitation cannot be eliminated with the usage of any parallel analysis toolkit.

7.2.7 Optimisation Regarding N-tuples

ROOT automatically applies compression algorithms on n-tuples to reduce the memory consumption. A value that is in most cases the same will consume only small space on your disk (but it has to be decompressed on reading). Nevertheless, you should think about the design of your n-tuples and your analyses as soon as the processing time exceeds some minutes.

- Try to keep your n-tuples simple and use appropriate variable types. If your measurement has only a limited precision, it is needless to store it with double precision.

- Experimental conditions that do not change with every single measurement should be stored in a separate tree. Although the compression can handle redundant values, the processing time increase with every variable that has to be filled.

- The function SetCacheSize(long) specifies the size of the cache for reading a TTree object from a file. The default value is 30MB. A manual increase may help in certain situations. Please note that the caching mechanism can cover only one TTree object per TFile object.

- You can select the branches to be covered by the caching algorithm with AddBranchToCache and deactivate unneeded branches with SetBranchStatus. This mechanism can result in a significant speed-up for simple operations on trees with many branches.

- You can measure the performance easily with TTreePerfStats. The ROOT documentation on this class also includes an introductory example. For example, TTreePerfStats can show you that it is beneficial to store meta data and payload data separately, i.e. write the meta data tree in a bulk to a file at the end of your job instead of writing both trees interleaved.

8 ROOT in Python

ROOT offers the possibility to interface to Python via a set of bindings called PyROOT. Python is used in a wide variety of application areas and one of the most used scripting languages today. With the help of PyROOT it becomes possible to combine the power of a scripting language with ROOT tools. Introductory material to Python is available from many sources on the web, see e. g. http://docs.python.org.

8.1 PyROOT

The access to ROOT classes and their methods in PyROOT is almost identical to C++ macros, except for the special language features of Python, most importantly dynamic type declaration at the time of assignment. Coming back to our first example, simply plotting a function in ROOT, the following C++ code:

```
TF1 *f1 = new TF1("f2","[0]*sin([1]*x)/x",0.,10.);
f1->SetParameter(0,1);
f1->SetParameter(1,1);
f1->Draw();
```

in Python becomes:

```
import ROOT
```

```
Welcome to JupyROOT 6.07/07
```

Notice: The above commands are not necessary in your environment!

```
#from ROOT import gStyle, TCanvas, TGraphErrors
canvas_8_1=ROOT.TCanvas("canvas_8_1" ,"Data" ,200 ,10 ,700 ,500)
f1 = ROOT.TF1("f2","[0]*sin([1]*x)/x",0.,10.)
f1.SetParameter(0,1);
f1.SetParameter(1,1);
f1.Draw();
canvas_8_1.Draw();
```
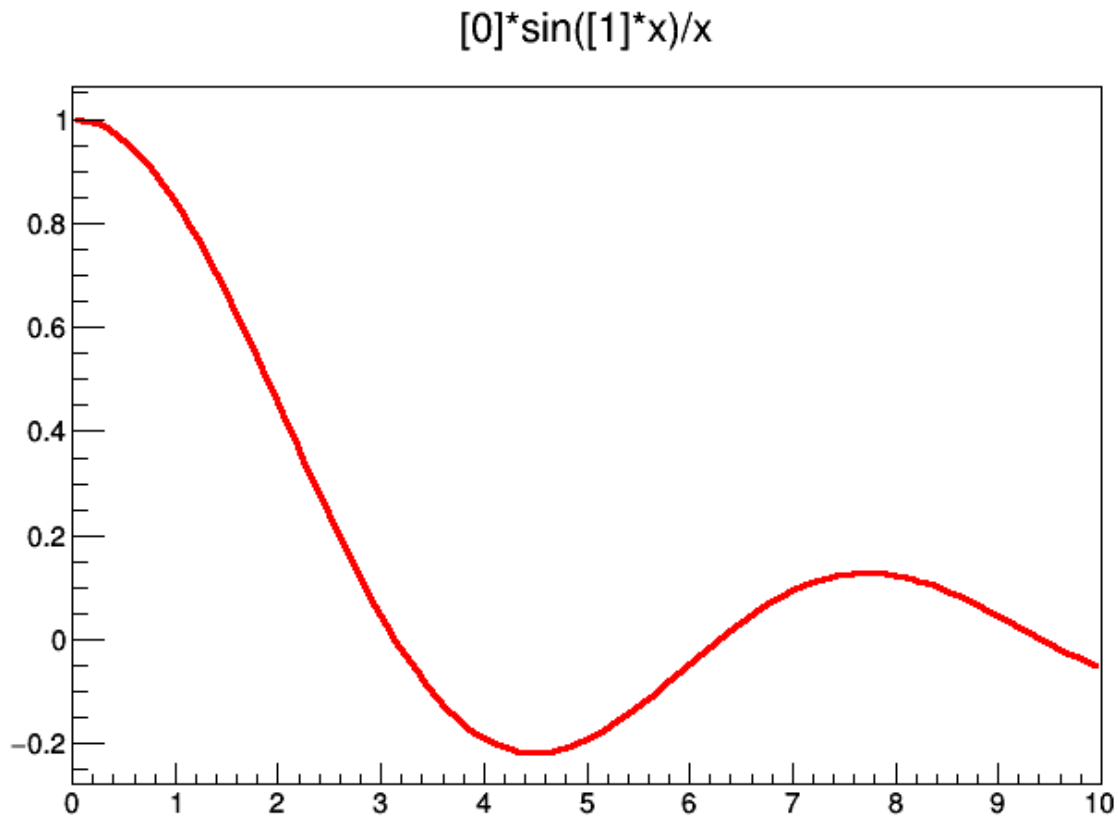

Figure 27: PyROOT:Using ROOT via Python

A slightly more advanced example hands over data defined in the macro to the ROOT class TGraphErrors. Note that a Python array can be used to pass data between Python and ROOT. The first line in the Python script allows it to be executed directly from the operating system, without the need to start the script from python or the highly recommended powerful interactive shell ipython. The last line in the python script is there to allow you to have a look at the graphical output in the ROOT canvas before it disappears upon termination of the script.

Here is the C++ version:

```cpp
%%cpp
//
// Draw a graph with error bars and fit a function to it
//
gStyle->SetOptFit(111) ; //superimpose fit results
// make nice Canvas
auto *c1 = new TCanvas("c1" ,"Daten" ,200 ,10 ,700 ,500) ;
c1->SetGrid( ) ;
//define some data points ...
const Int_t n = 10;
Float_t x[n] = {-0.22, 0.1, 0.25, 0.35, 0.5, 0.61, 0.7, 0.85, 0.89, 1.1};
Float_t y[n] = {0.7, 2.9, 5.6, 7.4, 9., 9.6, 8.7, 6.3, 4.5, 1.1};
Float_t ey[n] = {.8 ,.7 ,.6 ,.5 ,.4 ,.4 ,.5 ,.6 ,.7 ,.8};
Float_t ex[n] = {.05 ,.1 ,.07 ,.07 ,.04 ,.05 ,.06 ,.07 ,.08 ,.05};
// and hand over to TGraphErros object
TGraphErrors *gr = new TGraphErrors(n,x,y,ex,ey);
gr->SetTitle("TGraphErrors with Fit") ;
// now perform a fit (with errors in x and y!)
gr->Fit("gaus");
gr->DrawClone("AP");
c1->Draw();
```

```
 FCN=1.53213 FROM MIGRAD    STATUS=CONVERGED      90 CALLS          91 TOTAL
                    EDM=2.58725e-08    STRATEGY= 1      ERROR MATRIX ACCURATE
  EXT PARAMETER                                STEP         FIRST
  NO.   NAME      VALUE            ERROR        SIZE       DERIVATIVE
   1  Constant    9.54303e+00    3.54707e-01   2.49013e-04   5.51076e-04
   2  Mean        5.66472e-01    2.69815e-02   2.04103e-05   4.18957e-03
   3  Sigma       2.85465e-01    3.04454e-02   2.72043e-05   1.85906e-03
```
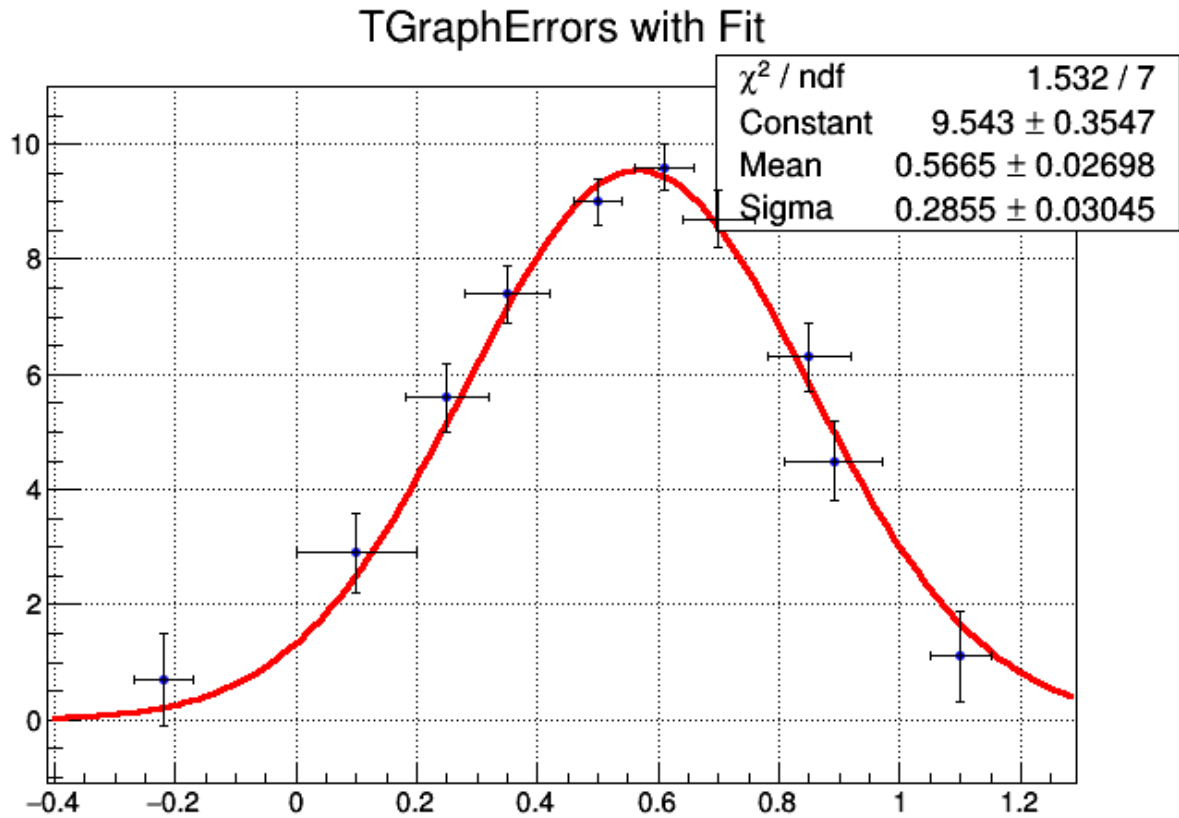
Figure 28: Using TGraphErrors with C++

In Python it looks like this:

```python
#
# Draw a graph with error bars and fit a function to it
#
from ROOT import gStyle, TCanvas, TGraphErrors
from array import array
canvas_8_2=ROOT.TCanvas("canvas_8_2" ,"TGraphErrors" ,200 ,10 ,700 ,500)
gStyle.SetOptFit (111) # superimpose fit results
canvas_8_1.SetGrid ()
#define some data points . . .
x = array('f', (-0.22, 0.1, 0.25, 0.35, 0.5, 0.61, 0.7, 0.85, 0.89, 1.1) )
y = array('f', (0.7, 2.9, 5.6, 7.4, 9., 9.6, 8.7, 6.3, 4.5, 1.1) )
ey = array('f', (.8 ,.7 ,.6 ,.5 ,.4 ,.4 ,.5 ,.6 ,.7 ,.8) )
ex = array('f', (.05 ,.1 ,.07 ,.07 ,.04 ,.05 ,.06 ,.07 ,.08 ,.05) )
nPoints=len ( x )
# . . . and hand over to TGraphErros object
gr=TGraphErrors ( nPoints , x , y , ex , ey )
gr.SetTitle("TGraphErrors with Fit")
gr.Draw ( "AP" )
gr.Fit("gaus")
# canvas_8_1.Update ()
canvas_8_2.Update ()
canvas_8_2.Draw ()
```

```
 FCN=1.53213 FROM MIGRAD    STATUS=CONVERGED      88 CALLS          89 TOTAL
                 EDM=2.57894e-08     STRATEGY= 1      ERROR MATRIX ACCURATE
```

```
 EXT PARAMETER                                STEP         FIRST
 NO.   NAME      VALUE          ERROR          SIZE      DERIVATIVE
  1  Constant    9.54303e+00   3.54707e-01   2.49013e-04   5.50385e-04
  2  Mean        5.66472e-01   2.69815e-02   2.04103e-05   4.18001e-03
  3  Sigma       2.85465e-01   3.04454e-02   2.72043e-05   1.85849e-03
```
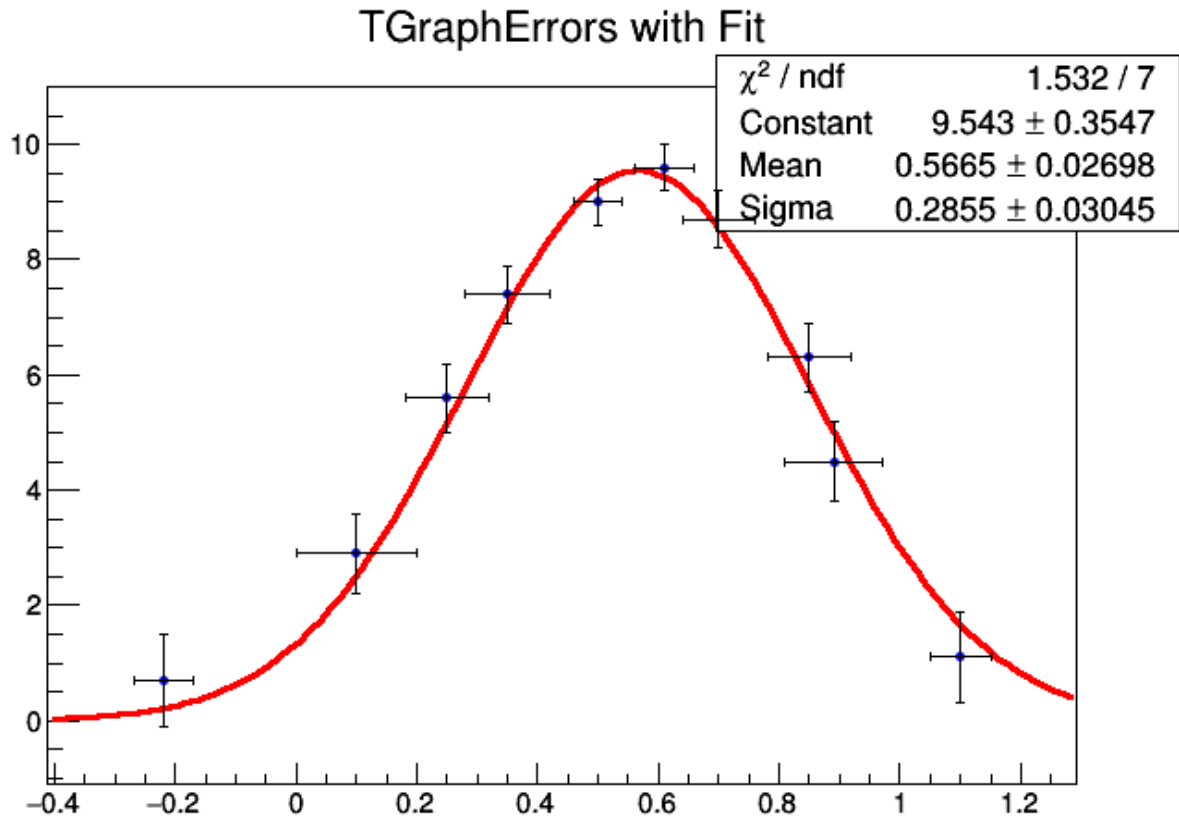

Figure 29: Using TGraphErrors with PyROOT

Comparing the C++ and Python versions in these two examples, it now should be clear how easy it is to convert any ROOT Macro in C++ to a Python version.

As another example, let us revisit macro3 from Chapter 4. A straight-forward Python version relying on the ROOT class `TMath`:

```python
# Builds a polar graph in a square Canvas.

from ROOT import TGraphPolar, TCanvas, TMath
from array import array

canvas_8_1_sq = TCanvas("canvas_8_1_sq","myCanvas",600,600)
rmin = 0.
rmax = TMath.Pi()*6.
npoints = 300
r = array('d',[0]*npoints)
theta  = array('d',[0]*npoints)
for ipt in xrange(0,npoints):
    r[ipt] = ipt*(rmax-rmin)/npoints+rmin
    theta[ipt] = TMath.Sin(r[ipt])
```

```
grP1 = TGraphPolar(npoints,r,theta)
grP1.SetTitle("A Fan")
grP1.SetLineWidth(3)
grP1.SetLineColor(2)
grP1.DrawClone("L")
grP1.Draw()
canvas_8_1_sq.Draw()
```
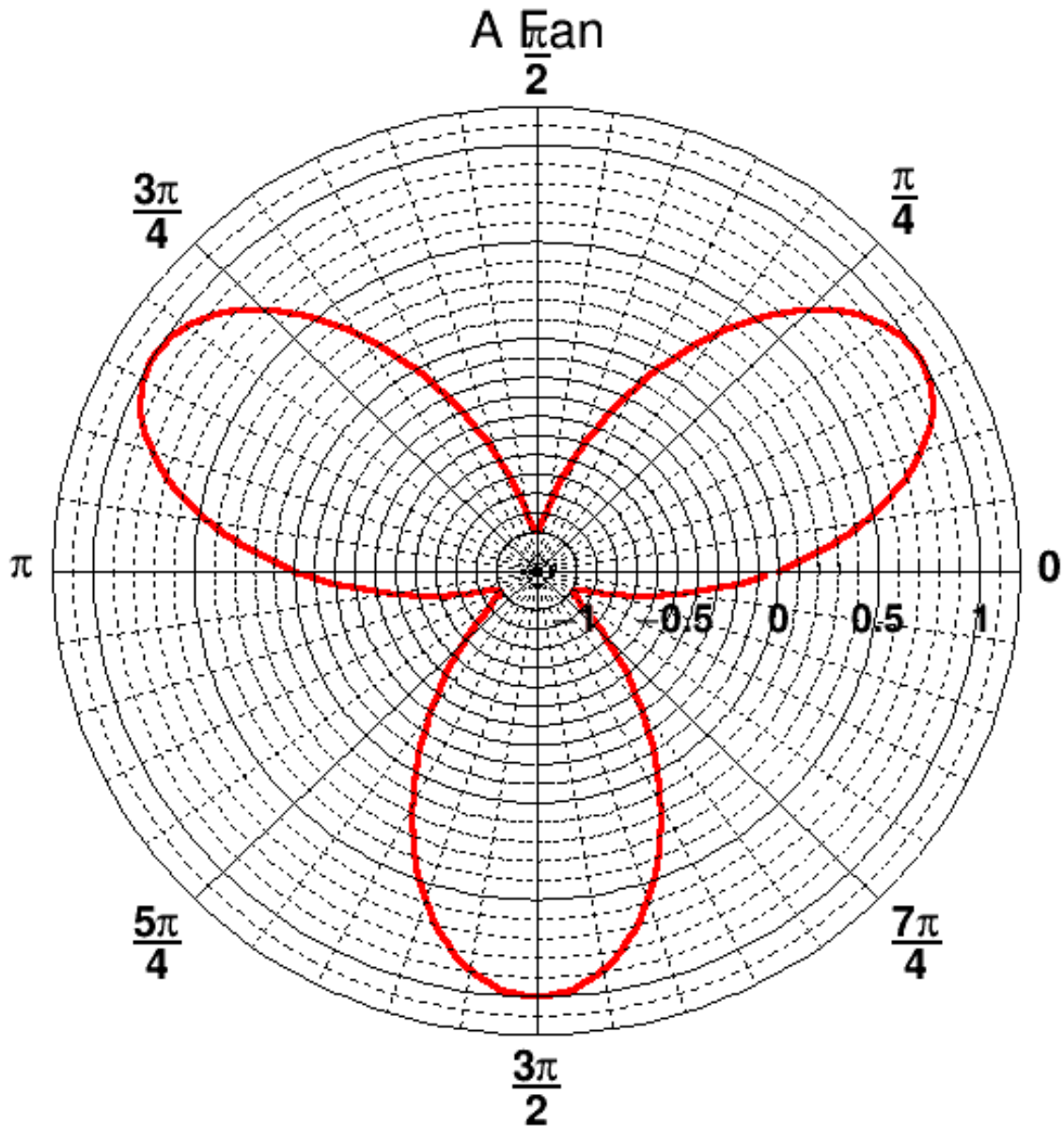
Figure 30: Using TMath with PyROOT

8.1.1 More Python- less C++

You may have noticed already that there are some Python modules providing functionality similar to ROOT classes, which fit more seamlessly into your Python code.

A more "pythonic" version of the above macro3 would use a replacement of the ROOT class TMath for the provisoining of data to TGraphPolar. With the math package, the part of the code becomes

```
import math
from array import array
from ROOT import TCanvas , TGraphPolar
...
ipt=range(0,npoints)
r=array('d',map(lambda x: x*(rmax-rmin)/(npoints-1.)+rmin,ipt))
theta=array('d',map(math.sin,r))
e=array('d',npoints*[0.])
...
```

8.1.1.1 Customised Binning

This example combines comfortable handling of arrays in Python to define variable bin sizes of a ROOT histogram. All we need to know is the interface of the relevant ROOT class and its methods (from the ROOT documentation):

```
TH1F(const char* name , const char* title , Int_t nbinsx , const Double_t* xbins)
```

Here is the Python code:

```python
import ROOT
from array import array
canvas_8_1_1 = TCanvas("canvas_8_1_1","myCanvas")
arrBins = array('d' ,(1 ,4 ,9 ,16) ) # array of bin edges
histogram_8_1 = ROOT.TH1F("histogram_8_1", "histogram_8_1", len(arrBins)-1, arrBins)
# fill it with equally spaced numbers
for i in range (1 ,16) :
   histogram_8_1.Fill(i)
histogram_8_1.Draw ()
canvas_8_1_1.Draw ()
```
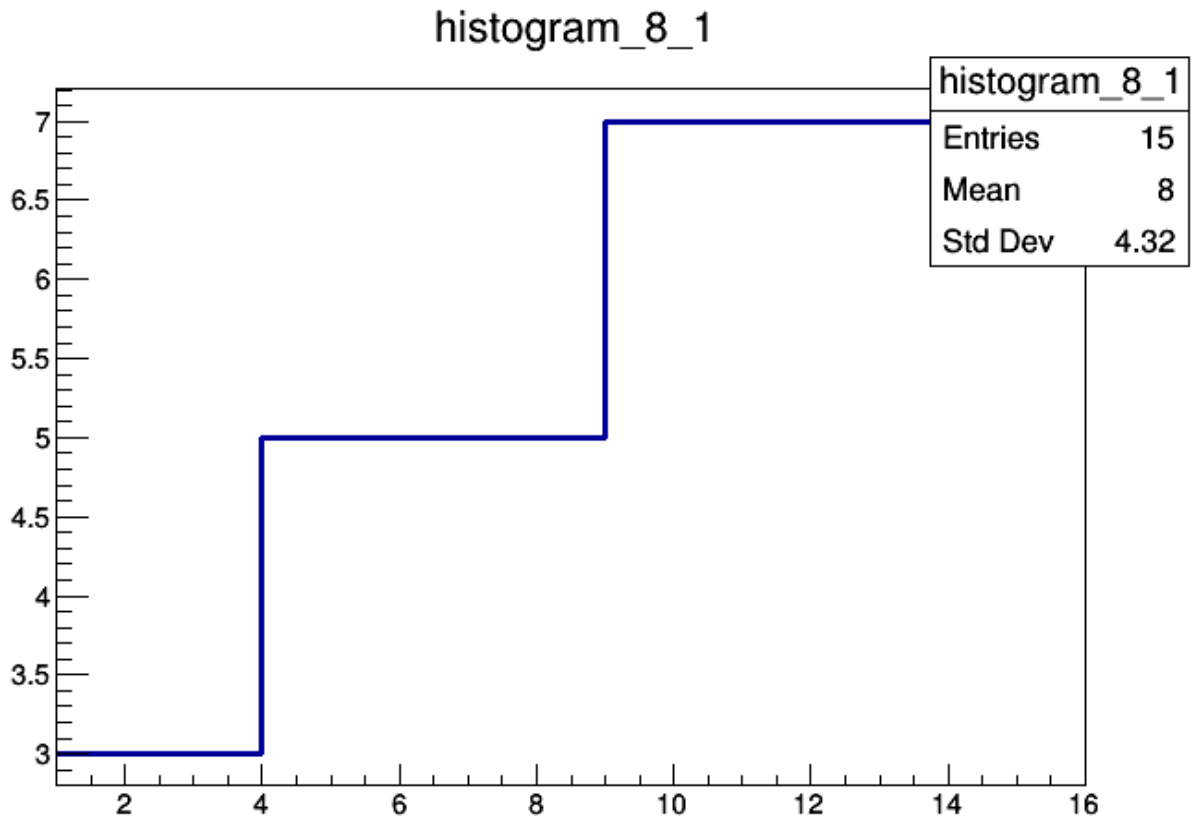
Figure 31: Define variable bin sizes of a ROOT histogram in Python

8.2 Custom code: from C++ to Python

The ROOT interpreter and type sytem offer interesting possibilities when it comes to JITting of C++ code. Take for example this header file, containing a class and a function.

```
##file cpp2pythonExample.h
#include "stdio.h"

class A{
public:
 A(int i):m_i(i){}
 int getI() const {return m_i;}
private:
 int m_i=0;
};

void printA(const A& a ){
  printf ("The value of A instance is %i.\n",a.getI());
}
```

This example might seem trivial, but it shows a powerful ROOT feature. C++ code can be JITted within PyROOT and the entities defined in C++ can be transparently used in Python!

```
>>> import ROOT
>>> ROOT.gInterpreter.ProcessLine('#include "cpp2pythonExample.h"')
>>> a = ROOT.A(123)
>>> ROOT.printA(a)
```

```
The value of A instance is 123.
```

9 Concluding Remarks

This is the end of our guided tour for beginners through ROOT. There is still a lot coming to mind to be said, but by now you are experienced enough to use the ROOT documentation, most importantly the ROOT home page and the ROOT reference guide with the documentation of all ROOT classes, or the ROOT users guide.

A very useful way for you to continue exploring ROOT is to study the examples in the sub-directory `tutorials/` of any ROOT installation.

There are some powerful features of ROOT which were not treated in this document, e.g. packages named RooFit and RooStats providing an advanced framework for model building, fitting and statistical analysis. The ROOT namespace `TMVA` offers multi-variate analysis tools including an artificial neural network and many other advanced tools for classification problems. The remarkable ability of ROOT to handle large data volumes was already mentioned in this guide, implemented through the class `TTree`. But there is still much more for you to explore!

End of this guide . . . but hopefully not of your interaction with ROOT !

9.1 References

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