

EEP 596: Adv Intro ML || Lecture 13

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Univ. of Washington, Seattle

February 16, 2023

Logistics

Atrial Fibrillation Detection

- ① Please pick a team-mate for your project
- ② Checkpoint submission for mini-project - Early submission to stay on track!
- ③ Anything else?

Kaggle Contest

Spreadsheet → Teams of 2

Last Time

- a) Anomaly Detection Baselines: SMA and EMA

Last Time

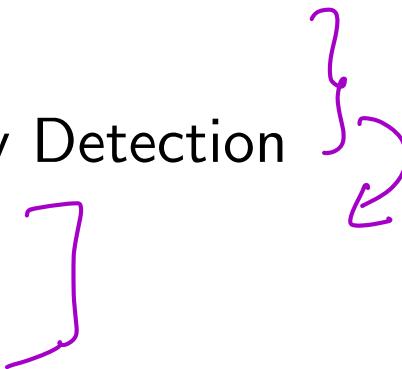
- (a) Anomaly Detection Baselines: SMA and EMA
- (b) Anomaly Detection: STL

Last Time

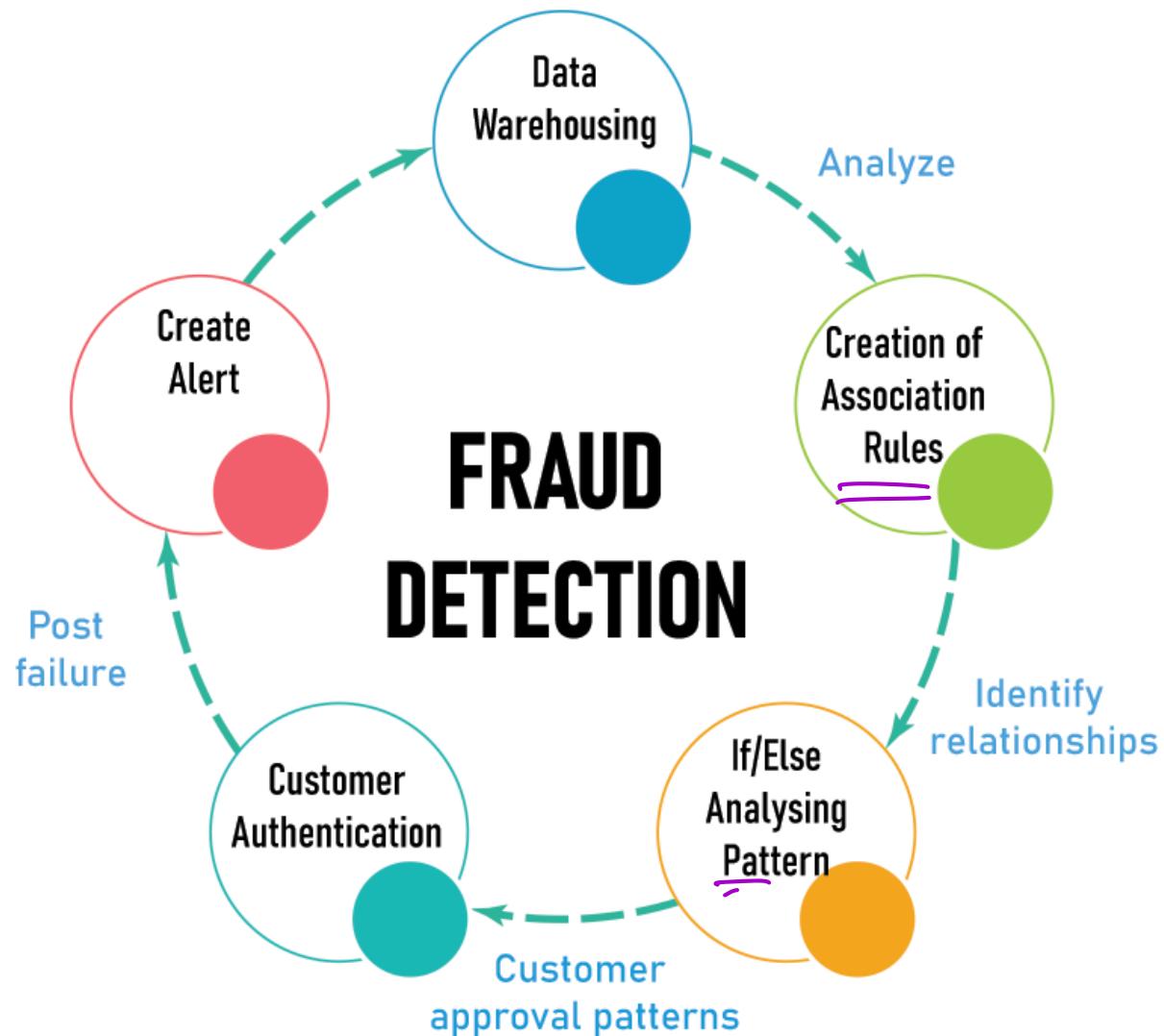
- (a) Anomaly Detection Baselines: SMA and EMA
- (b) Anomaly Detection: STL
- (c) Anomaly Detection on Alpaca

Today

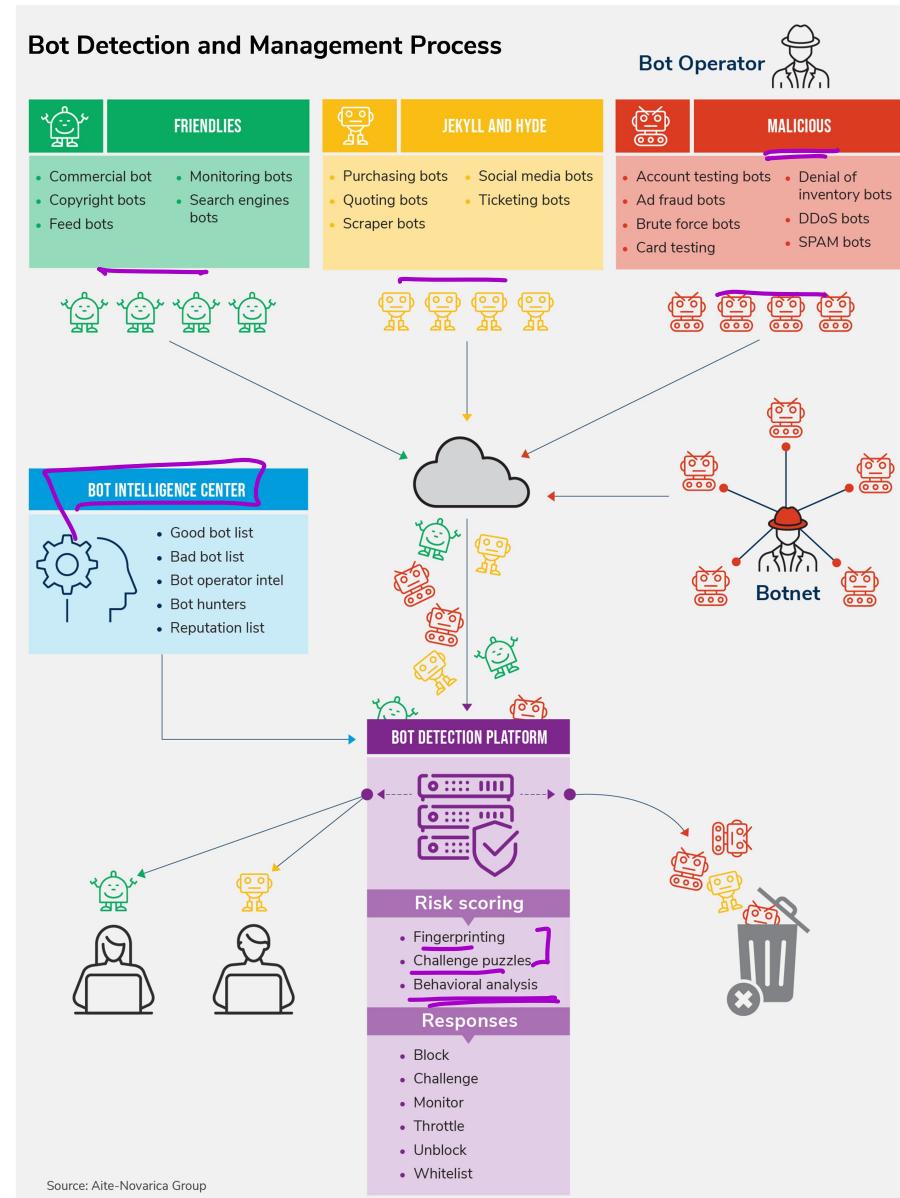
- Anomaly Detection Recap
- Time-series methods for Anomaly Detection
- Introduction to Deep Learning
- Deep Learning Applications
- Deep Learning Theory
- Deep Learning Modeling



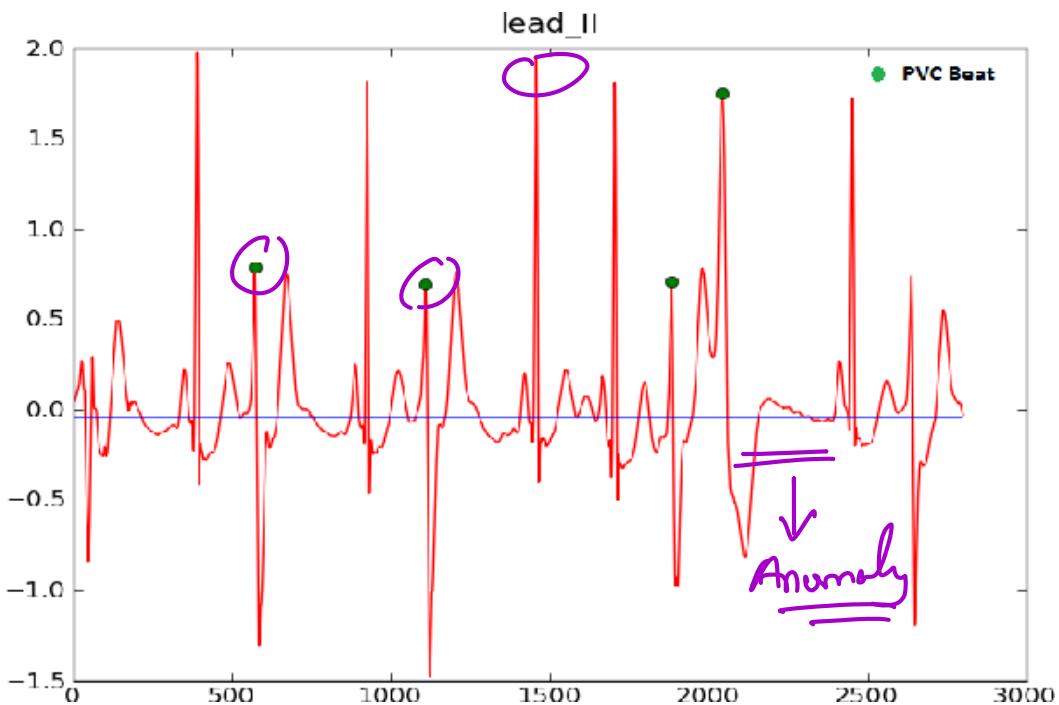
Fraud Detection



Got Bot?

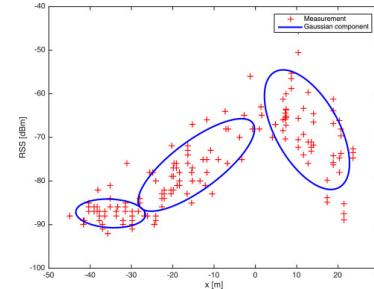
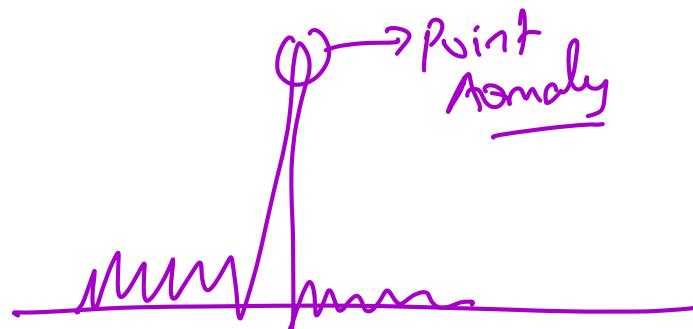


Arrhythmia Detection



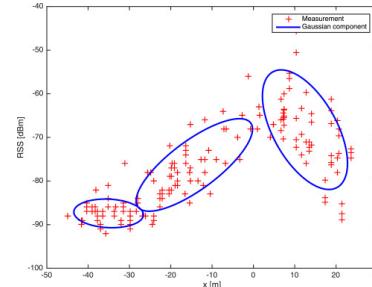
Types of Anomalies

① **Point Anomaly:** Deviation from a set of data points.

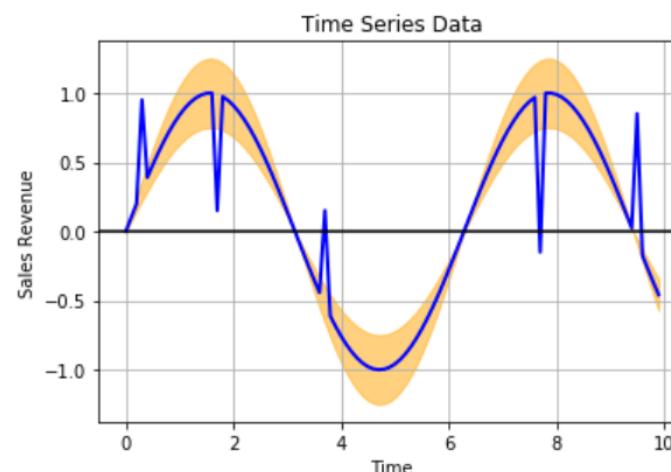


Types of Anomalies

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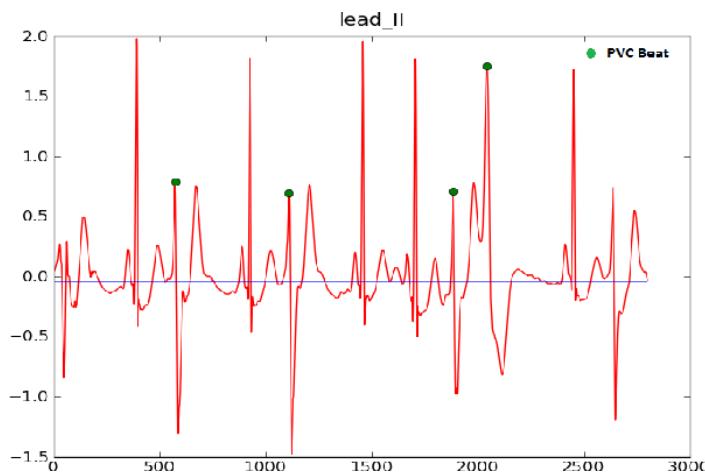


- ② **Contextual Anomaly:** Depending on the context, a data point could be an anomaly or not. For instance 35 degrees is not an anomalous temperature for Seattle winter but it is for Seattle summer. Same is true for anomalies in a time-series data e.g. Sales Revenue data.

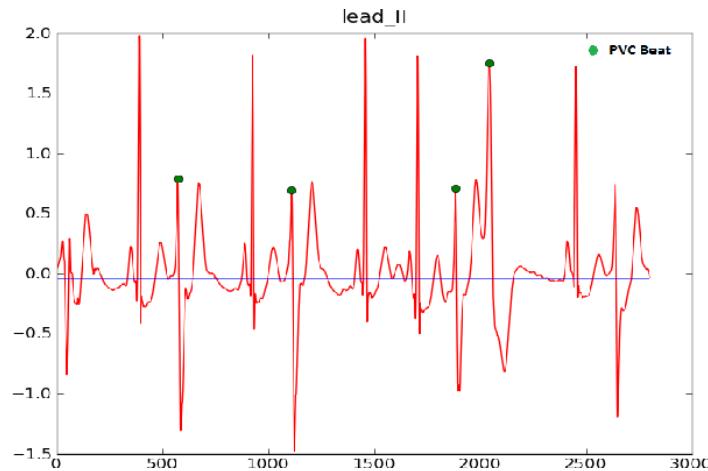


Types of Anomalies

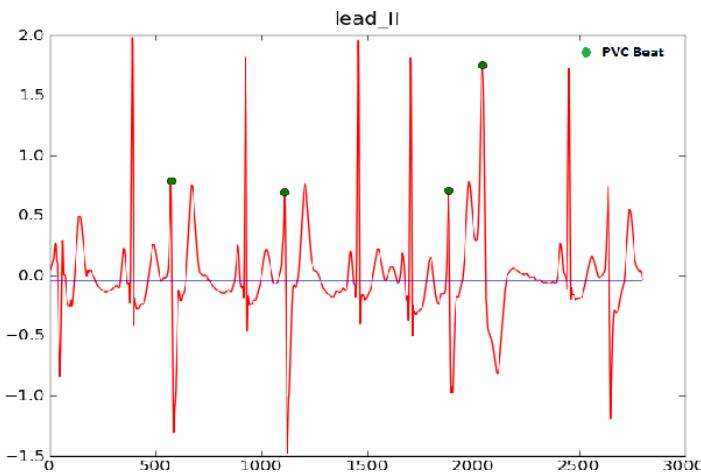
- ③ **Collective Anomalies:** No one data point is anomalous but a collection of them become anomalous. E.g. the Arrhythmia time series.



Arrhythmia detection



Arrhythmia detection



Next Assignment: Automated Arrhythmia Detection

You want to build an automated algorithm for Arrhythmia detection from time-series data on heart beats. What would be a baseline un-supervised learning algorithm you can think of Arrhythmia detection? If you wanted to do supervised learning for arrhythmia detection, what features would you use? How would you cast it as a machine learning problem? How would you evaluate the performance of your automated algorithm? What would be the metrics you would use? Discuss in groups - We will implement this as part of the next programming assignment.

Deep Learning for Anomaly Detection

Deep Learning

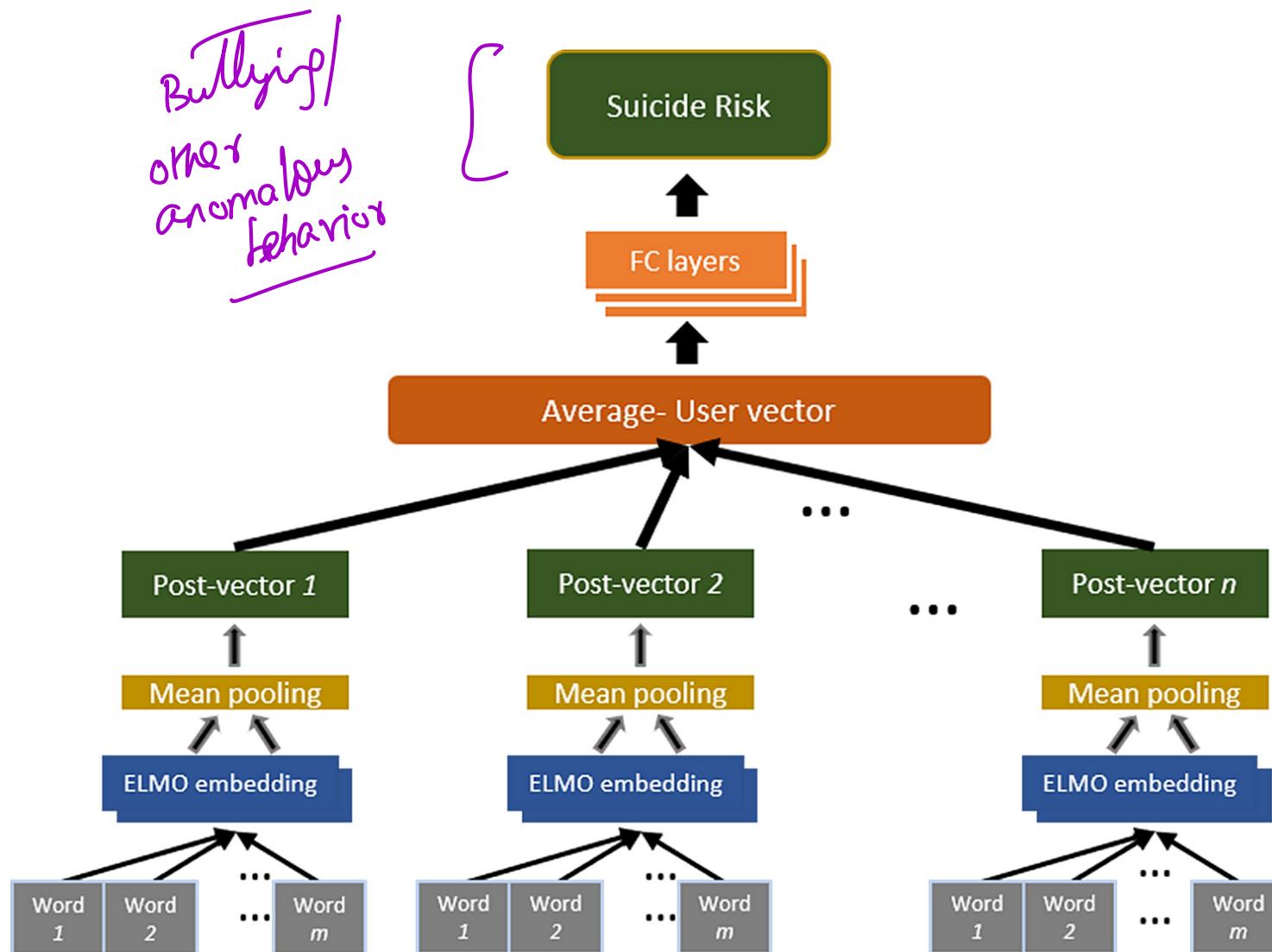
Deep Learning can provide powerful non-linear supervised models for anomaly detection provided there is enough data (both positive and negative examples) and we account for over-fitting. On the upcoming assignment, can also try out deep learning!

Detecting bots/in-appropriate posts

Biasing the metrics

Do you bias more towards high precision or high recall? Is there a middle ground? Can we have higher recall (i.e. detect the bots/inappropriate posts) without pissing people off with incorrect flags?

Suicide detection from Social Media posts



Suicide Detection Reference

Anomaly Detection Methods so far

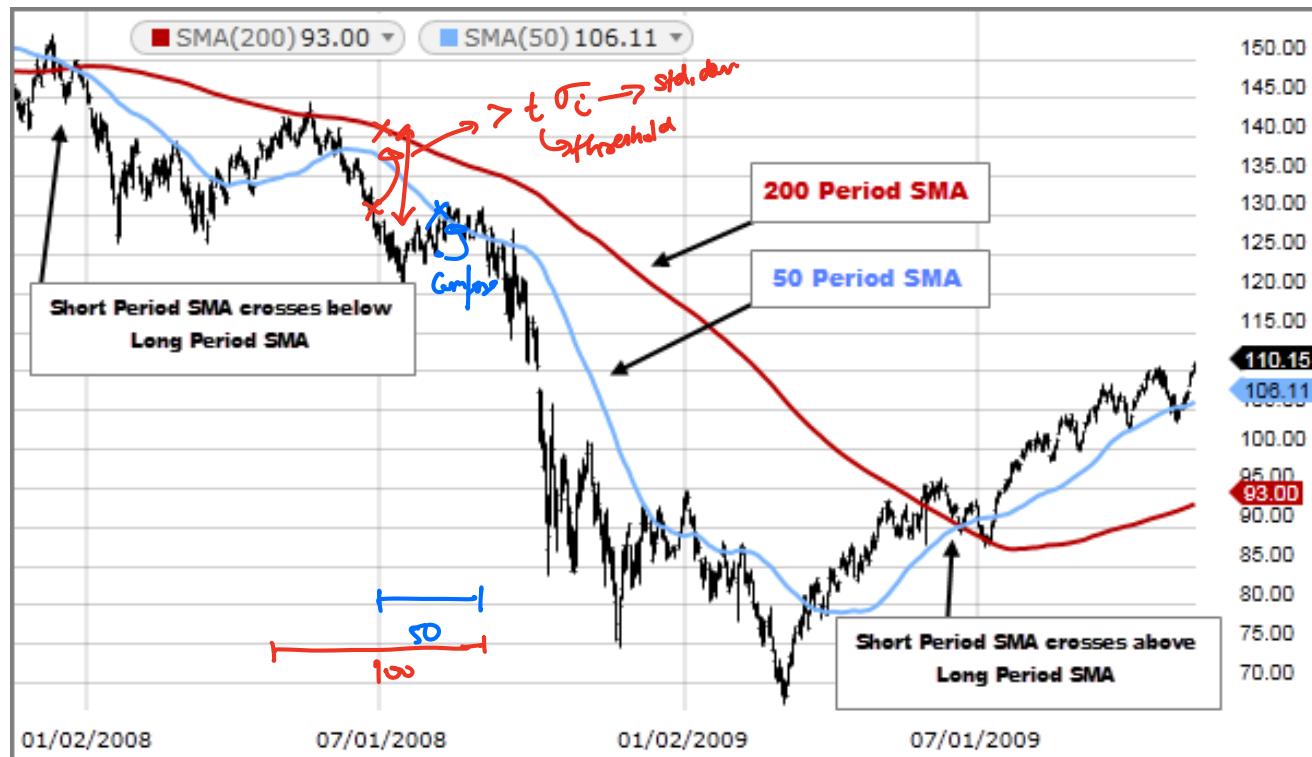
	Method	Pros	Cons
1	<u>Mean/Std Deviation</u>	Identifies some anomalies	False positives
2	<u>Supervised Learning</u>	Precise detection	As good as features

Anomaly Detection Methods - Coming up

	Method	Pros
1	Mean/Std Deviation	Identifies some anomalies
2	Supervised Learning	Precise detection
3	Simple Moving Average (SMA)	Improves on mean/std deviation
4	Exponential Moving Average (EMA)	More sensitive than SMA
5	STL	Accounts for seasonality

Moving Averages - Simple Moving Average

↑
Quantity
Stock price



$x_t = []^d$ dates
At time t , have a d -dimensional data point

Simple Moving Average and Anomalies

SMA

- ① There is a window size 50? that helps you track the **moving** average.
- ② 50-SMA is a 50 day moving average
- ③ $50\text{-SMA}(i) = \frac{1}{50} \sum_{j=i-50}^{i-1} x_j$

Simple Moving Average and Anomalies

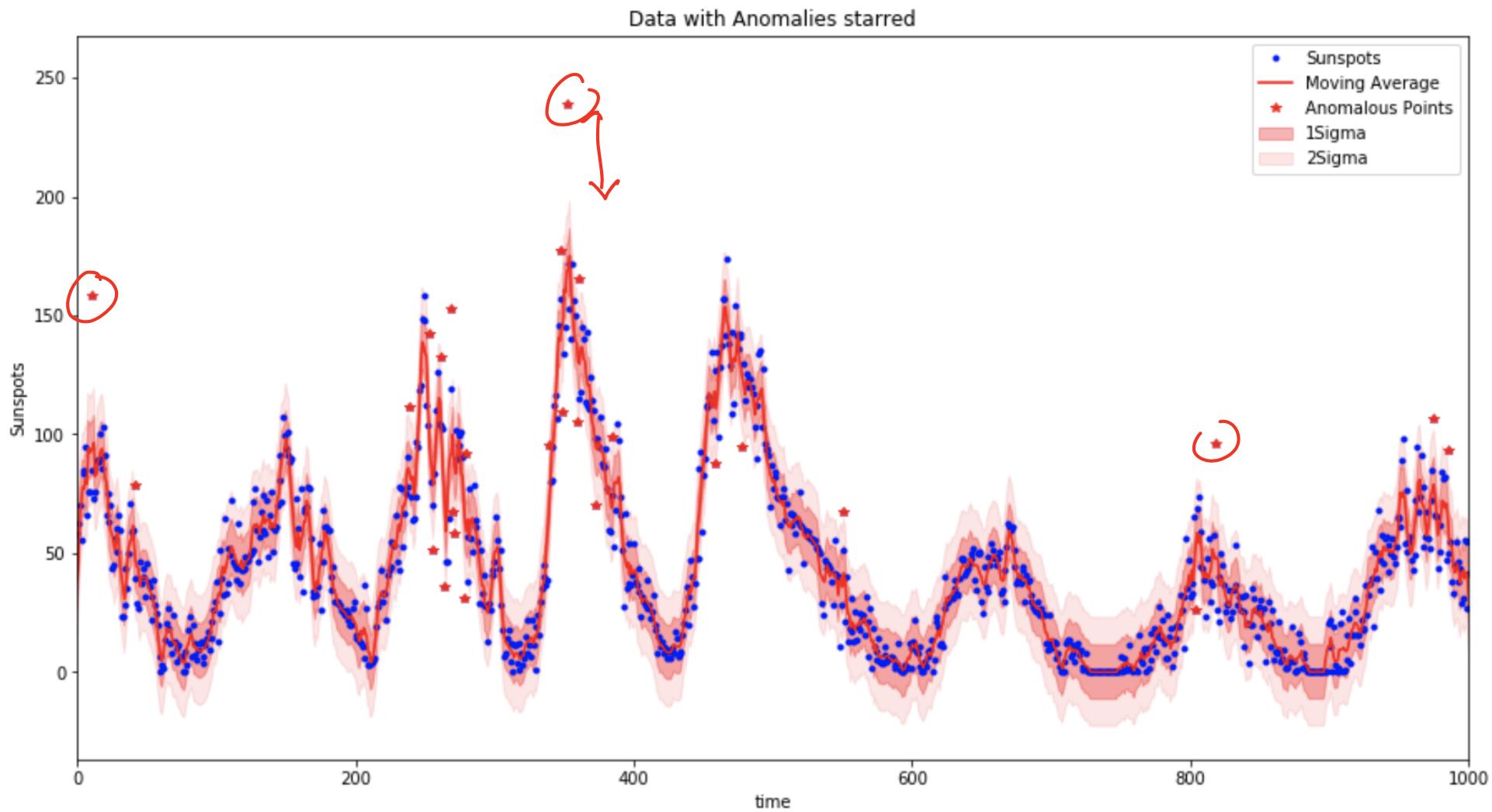
SMA

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- ② 50-SMA is a 50 day moving average
- ③ $50\text{-SMA}(i) = \frac{1}{50} \sum_{j=i-50}^{i-1} x_j$

Anomaly detection

- ① \underline{x}_i is an anomaly if $\|\underline{SMA}(i) - \underline{x}_i\|$ deviates above a $t \times \underline{SD}(i)$ where $\underline{SD}(i)$ is the standard deviation and N is the size of the window, t is the threshold.

SMA example



Github Library to try!]

ICE #1

Moving mean computation

Let's say you wanted to implement SMA yourself. Let the window size be 100. You have $SMA(i - 1)$. How do you compute it from $SMA(i - 1)$?

- a $SMA(i) = SMA(i - 1) + (x_i - x_{i-N})/N$
- b $SMA(i) = SMA(i - 1) + x_i/N$
- c $SMA(i) = SMA(i - 1)$
- d $SMA(i) = SMA(i - 1) - x_{i-N}/N$

$$\begin{aligned}SMA(i) &= \frac{x_i + x_{i-1} + \dots + x_{i-N+1}}{N} \\SMA(i-1) &= \frac{x_{i-1} + \dots + x_{i-N+1} + x_{i-N}}{N}\end{aligned}$$

ICE #2

Moving mean computation

Based on the previous question, what's the computational complexity and memory/storage complexity of SMA at point i , i.e. $SMA(i)$?

- a $O(N), O(N)$
- b $O(1), O(N)$
- c $O(N), O(1)$
- d $O(1), O(1)$

$$SMA(i) = \frac{\overline{SMA(i-1)} + (\underline{x_i} - \underline{x_{i-N}})}{N}$$

$O(1)$ storage

$O(1)$ time

$O(N)$ storage

Moving Variance computation for SMA

Moving Variance

Same principle as computing the moving mean for SMA.

Exponential Moving Average and Anomalies

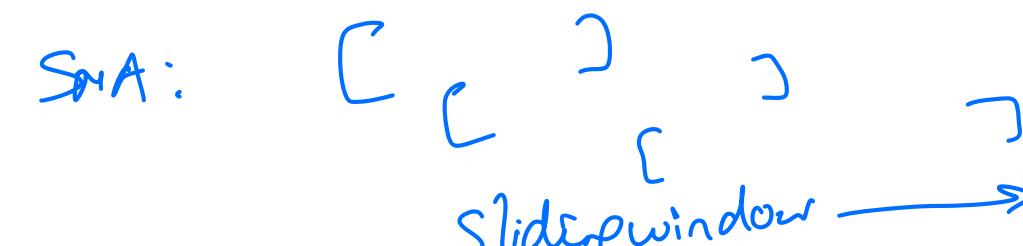
EMA

- ① Similar to SMA - Except the moving window is **soft**
- ② Weight more of the recent terms than before and weight it exponentially.

③ $\boxed{EMA(i) = (1 - \beta) * EMA(i - 1) + \beta * x_i}$ where $0 \leq \beta \leq 1$

④ $EMA(i) = \underbrace{\beta x_i}_{\text{More weight}} + \beta(1 - \beta)x_{i-1} + \beta(1 - \beta)^2x_{i-2} + \dots$

- ⑤ EMA has a hyper-parameter β instead of window size N as in SMA.



Exponential Moving Average and Anomalies

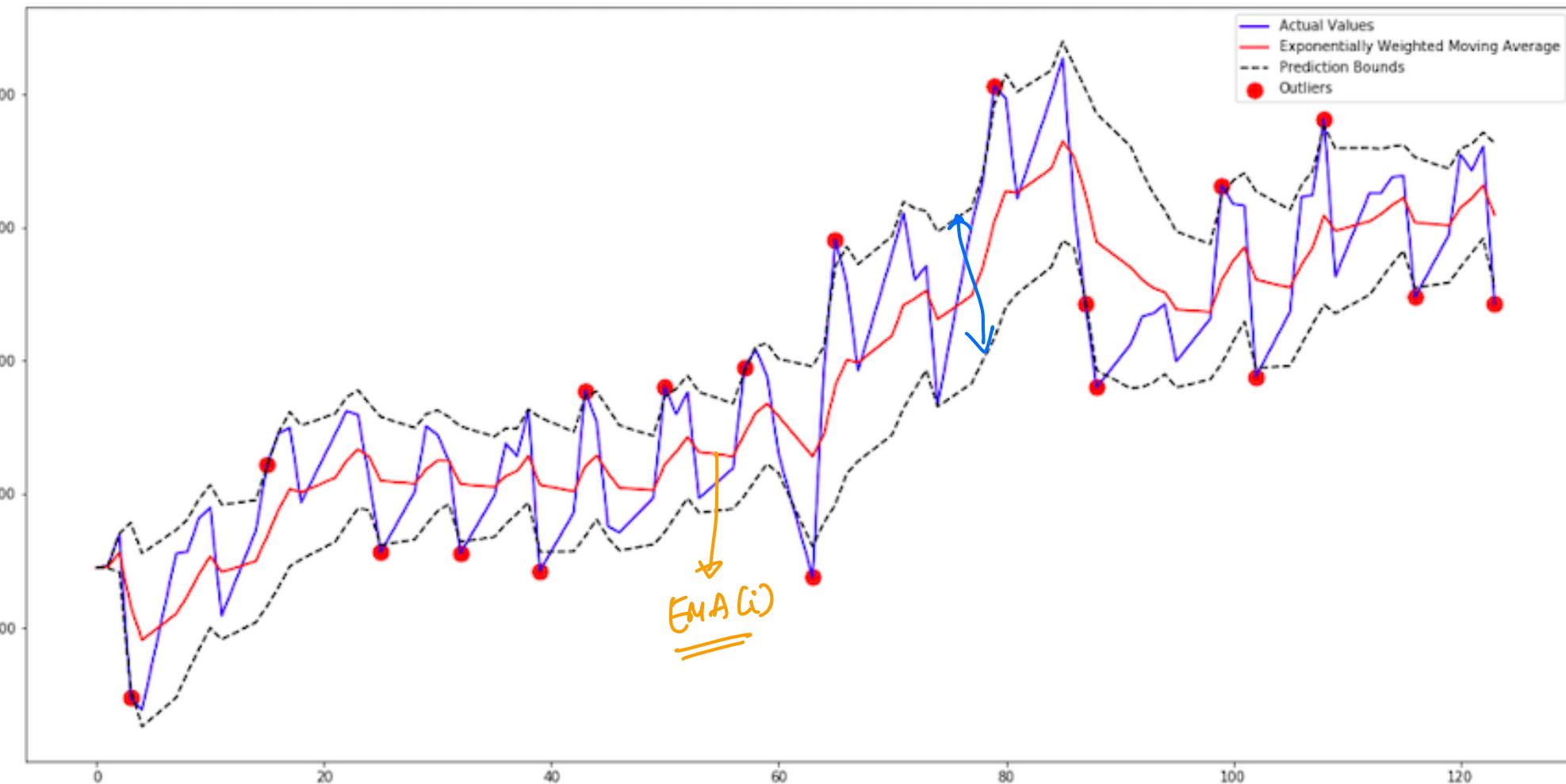
EMA

- ① Similar to SMA - Except the moving window is **soft**
- ② Weight more of the recent terms than before and weight it exponentially.
- ③ $EMA(i) = (1 - \beta) * EMA(i - 1) + \beta * x_i$; where $0 \leq \beta \leq 1$
- ④ $EMA(i) = \beta x_i + \beta(1 - \beta)x_{i-1} + \beta(1 - \beta)^2x_{i-2} + \dots$
- ⑤ EMA has a hyper-parameter β instead of window size N as in SMA.

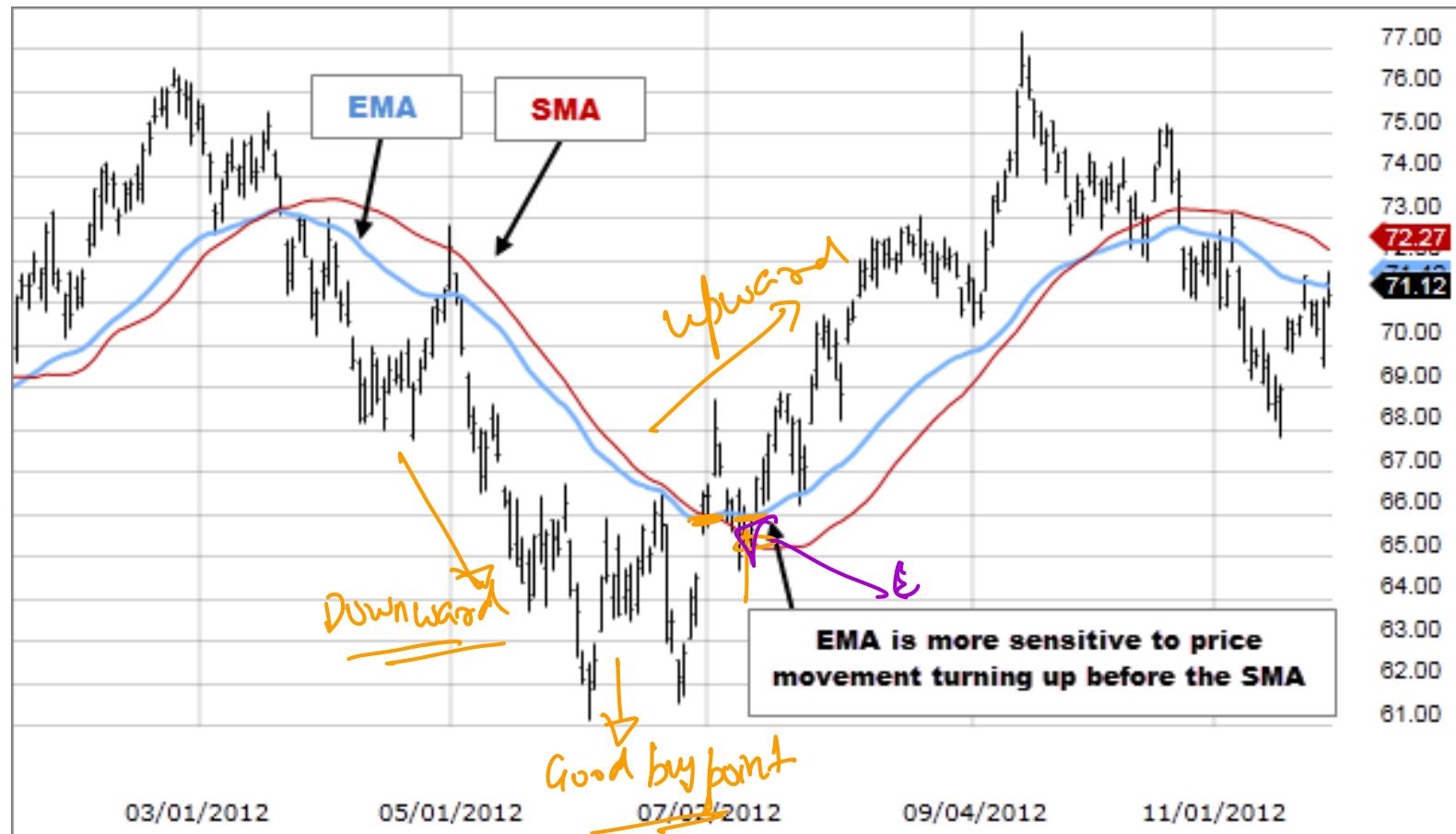
Anomaly detection

- ① x_i is an anomaly if $\|EMA(i) - x_i\|$ deviates above a $t \times SD(i)$ where $SD(i)$ is the standard deviation of the deviation.

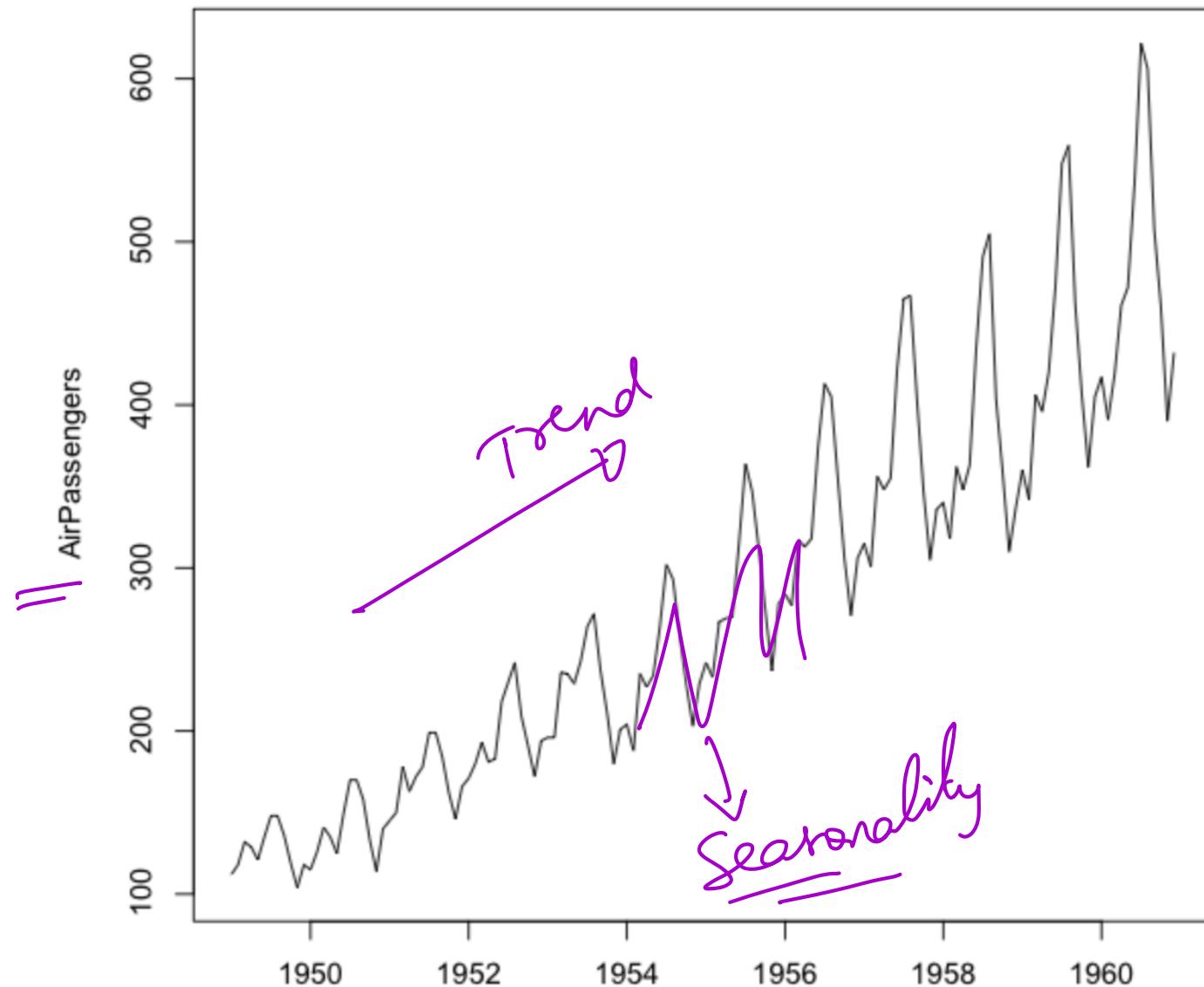
Exponential Moving Average



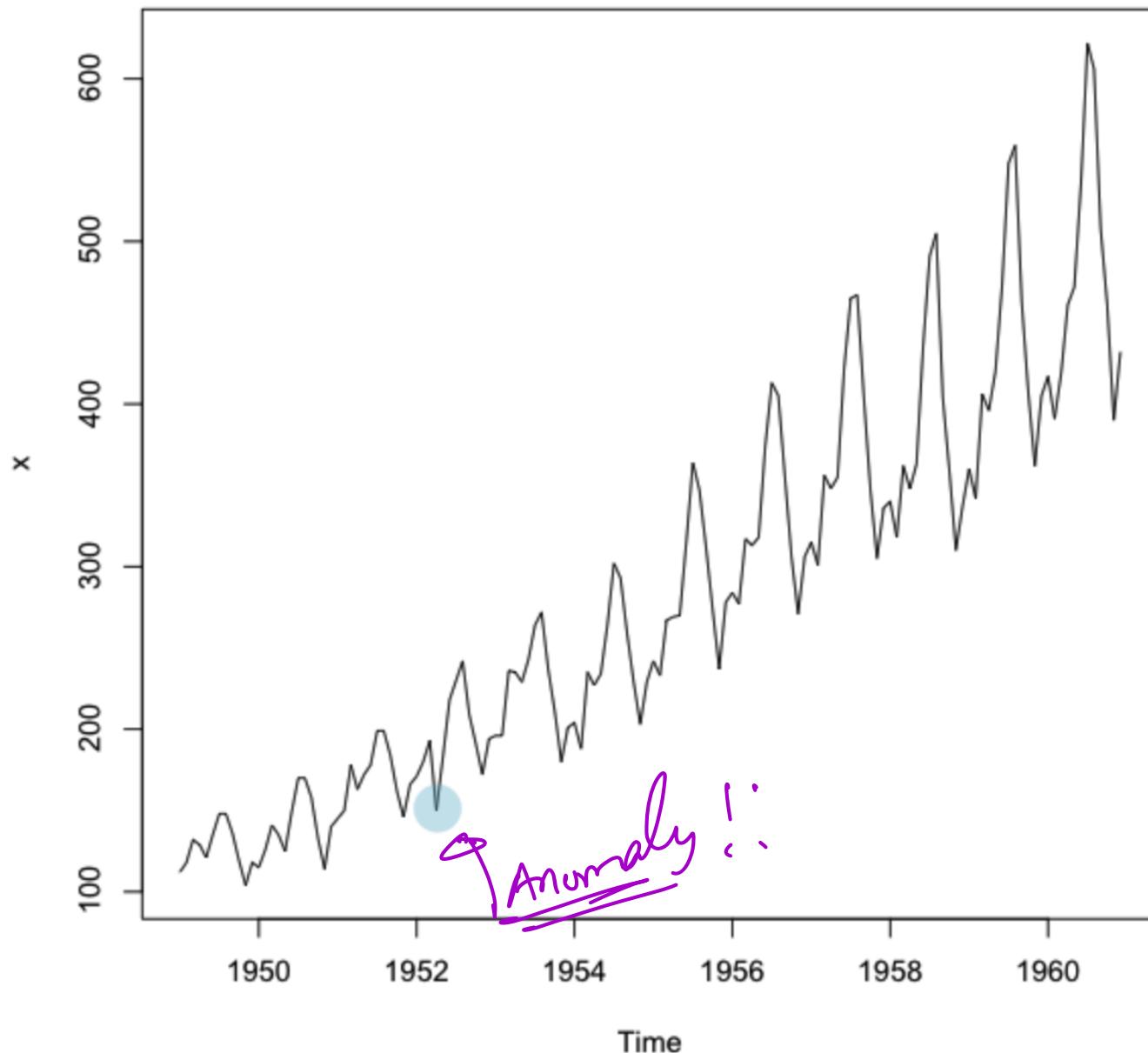
SMA vs EMA



Accounting for Seasonality



Accounting for Seasonality



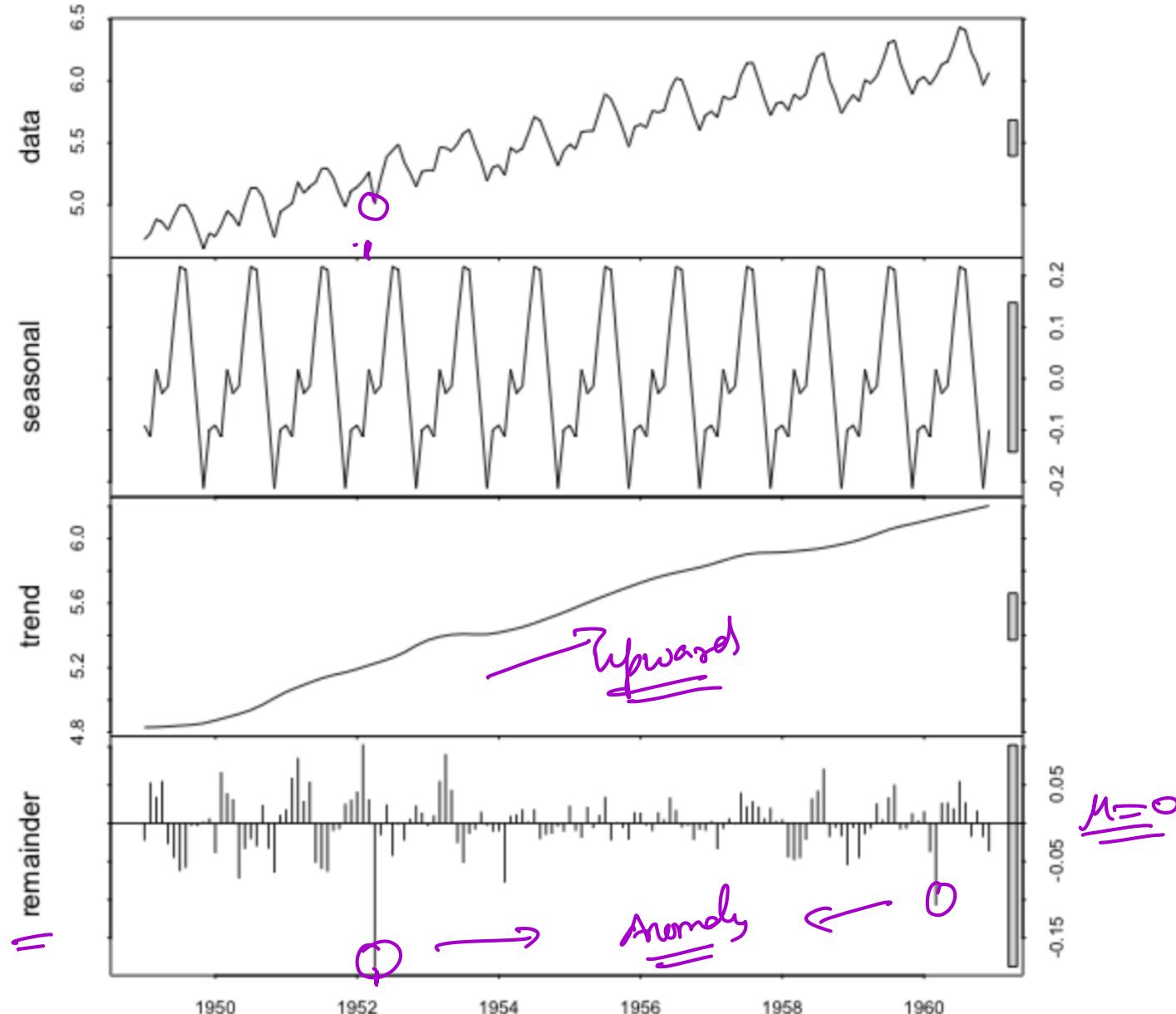
STL: Accounting for Seasonality

Data

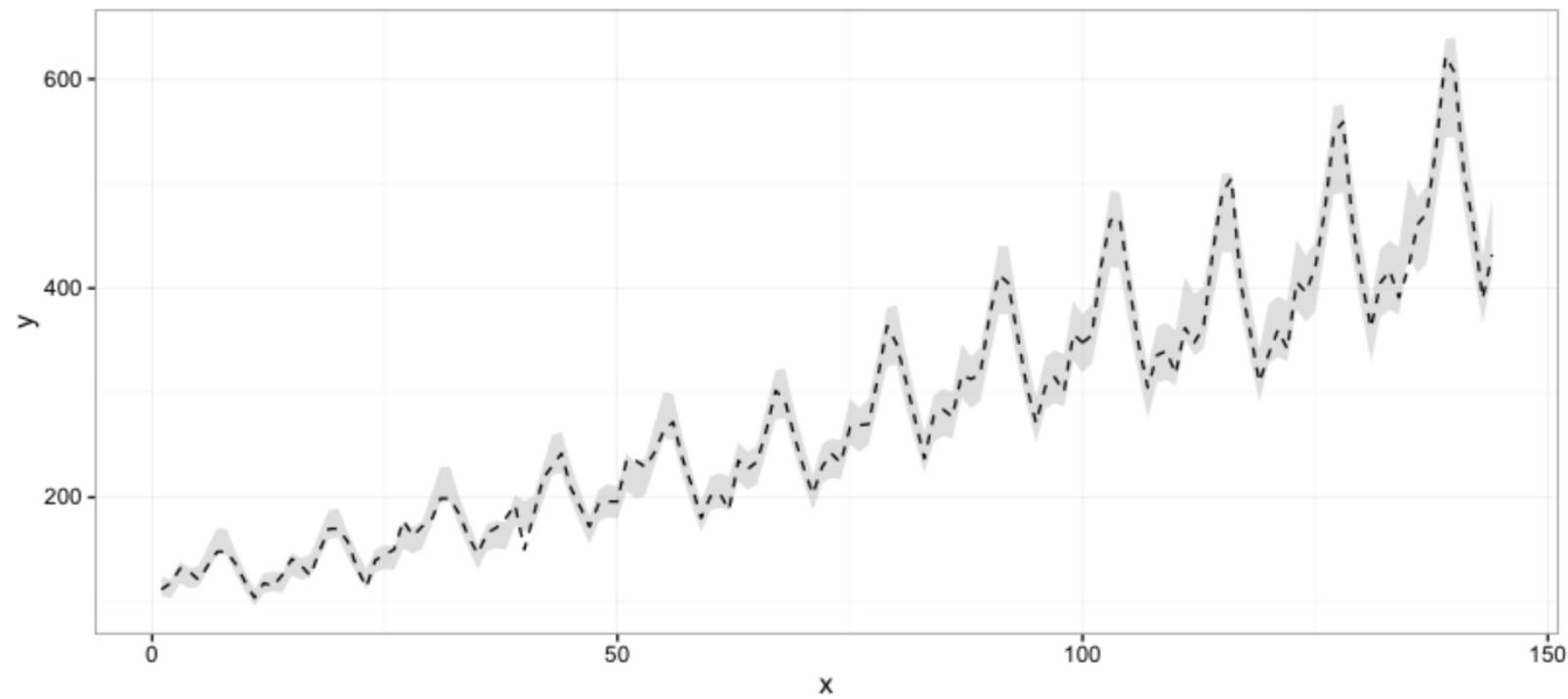
=
Seasonality

+
Trend

+
Residual



STL: Accounting for Seasonality

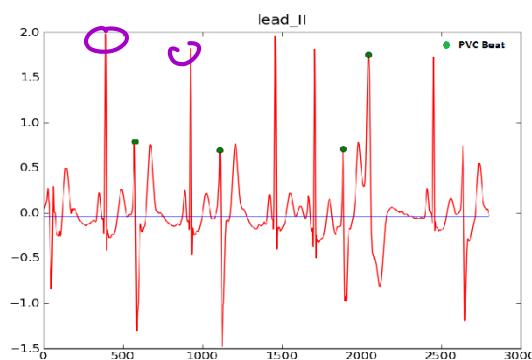


STL Library

Prophet Anomaly Detection

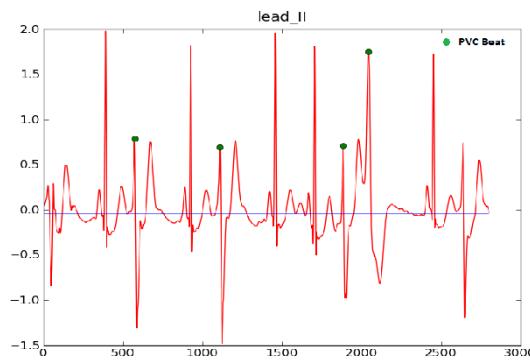


For the upcoming assignment on Arrhythmia Detection



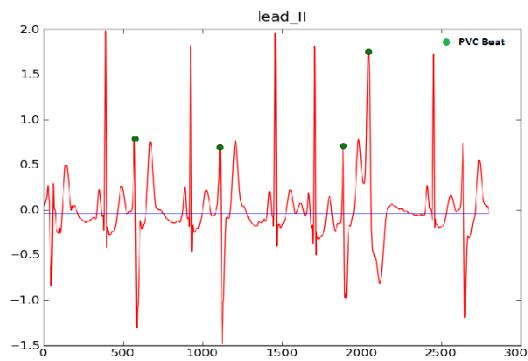
- ① Try SMA/EMA (unsupervised baseline)

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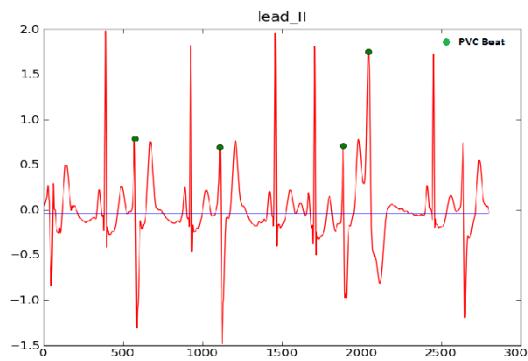
- ① Try SMA/EMA (unsupervised baseline)
- ② Try a supervised linear-model baseline like Logistic Regression / SVM

For the upcoming assignment on Arrhythmia Detection



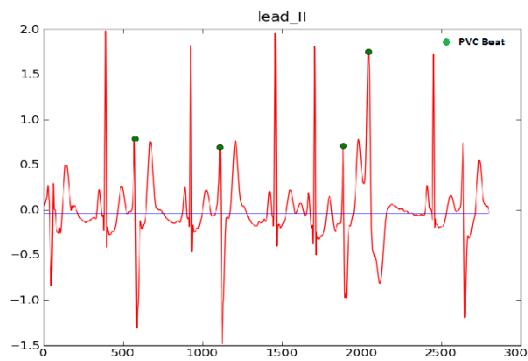
- ① Try SMA/EMA (unsupervised baseline)
- ② Try a supervised linear-model baseline like Logistic Regression
- ③ Try a supervised non-linear model like Random Forest *(Non-deep Learning)*

For the upcoming assignment on Arrhythmia Detection



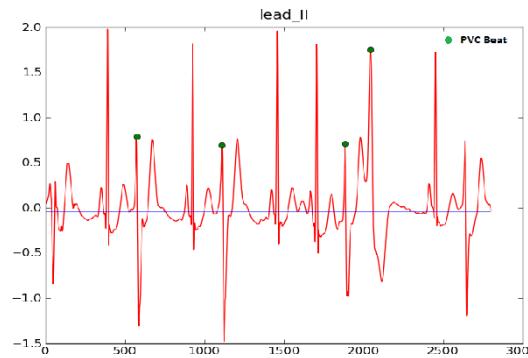
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- ② Try a supervised linear-model baseline like Logistic Regression
- ③ Try a supervised non-linear model like Random Forest
- ④ Try a deep learning model

For the upcoming assignment on Arrhythmia Detection



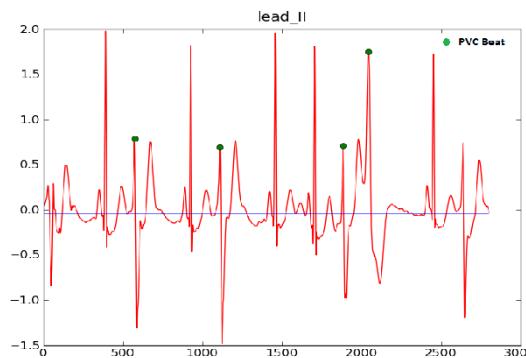
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- ④ Try a deep learning model
- ⑤ Benchmark offline results in a tabular format with algorithms and metrics.

For the upcoming assignment on Arrhythmia Detection



- ① Try SMA/EMA (unsupervised baseline)
- ② Try a supervised linear-model baseline like Logistic Regression
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- ⑥ Kaggle competition benchmarks performance on held-out and unseen test set

For the upcoming assignment on Arrhythmia Detection



- ① Try SMA/EMA (unsupervised baseline) *J [SQL]*
- ② Try a supervised linear-model baseline like Logistic Regression
- ③ Try a supervised non-linear model like Random Forest
- ④ Try a deep learning model
- ⑤ Benchmark offline results in a tabular format with algorithms and metrics.
- ⑥ Kaggle competition benchmarks performance on held-out and unseen test set *why??*
- ⑦ Share your insights in the process - Pros/cons of different approaches and what changes give you a boost in performance and why?

Next Topic: Deep Learning

Introduction to Deep Learning

Deep Learning

- ➊ Lot of buzz around Deep Learning in the past decade!

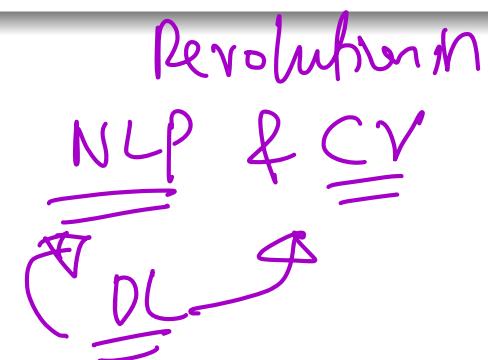
Introduction to Deep Learning

Deep Learning

- ① Lot of buzz around Deep Learning in the past decade!
- ② Deep Learning refers to Neural Networks that is a loose approximation of how the brain works

Why was NN not popular in 2000's?

- Not enough data
- Not enough Compute power
- No cloud infra
- overfitting issues



Applications of Deep Learning

Applications

- ① Self-driving cars |CV

Applications of Deep Learning

Applications

- ① Self-driving cars
- ② Sentiment analysis *InLP*

Applications of Deep Learning

Applications

- ① Self-driving cars
- ② Sentiment analysis
- ③ Text Summarization

NLP?

Applications of Deep Learning

Applications

- ① Self-driving cars
- ② Sentiment analysis
- ③ Text Summarization
- ④ Arrythmia detection - Possible assignment for this course! (TS)

Applications of Deep Learning

Applications

- ① Self-driving cars
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- ⑤ Image to text generation. Caption images automatically. *Or/NLP*

Applications of Deep Learning

Applications

- ① Self-driving cars
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- ⑤ Image to text generation. Caption images automatically.
- ⑥ Machine Translation. Translate a French sentence to English sentence. Sequence to sequence architecture *NLP*

Applications of Deep Learning

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- ⑦ Auto-complete sentence in Emails. How many of us use this?

Applications of Deep Learning

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- ⑧ Auto-complete search results.

Applications of Deep Learning

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- ⑦ Auto-complete sentence in Emails. How many of us use this?
- ⑧ Auto-complete search results. *bard* *Google*
- ⑨ Chat bots - Like ChatGPT / Sparrow / Anthropic, etc *NLP*
OpenAI

Email auto-complete

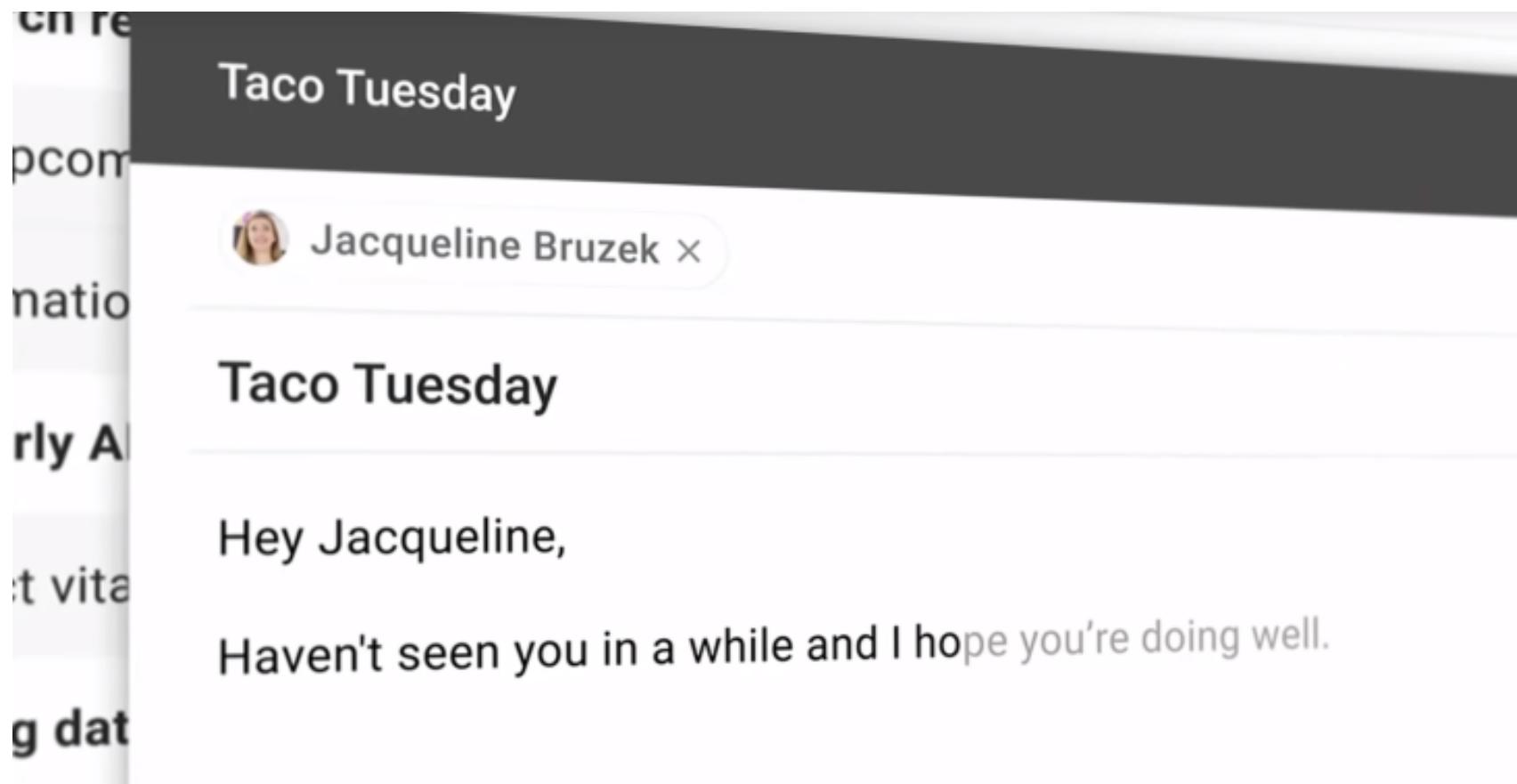
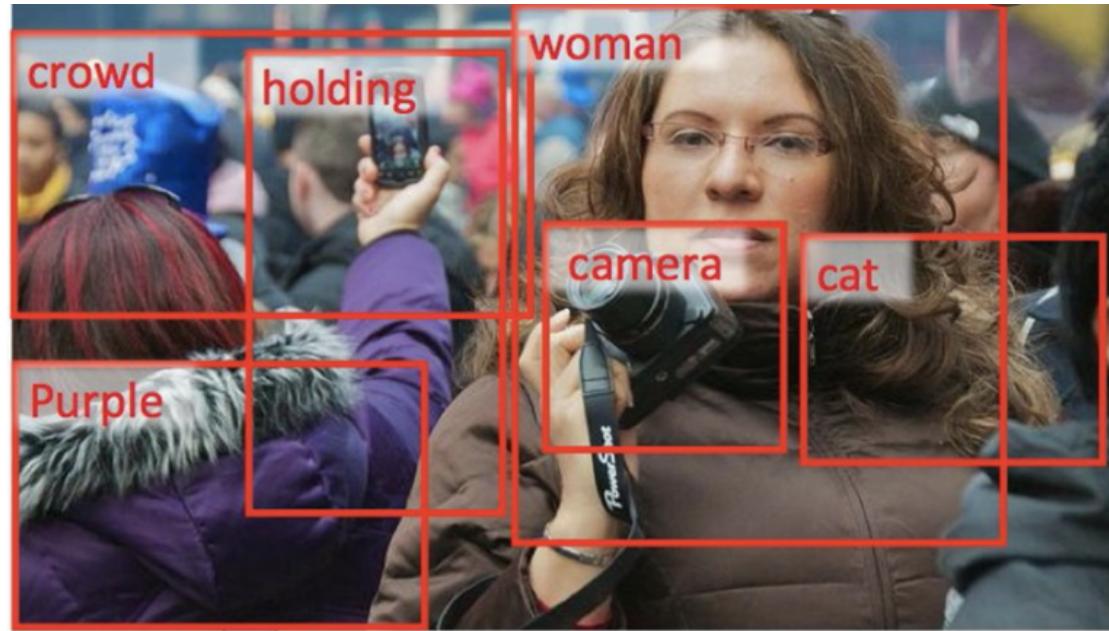
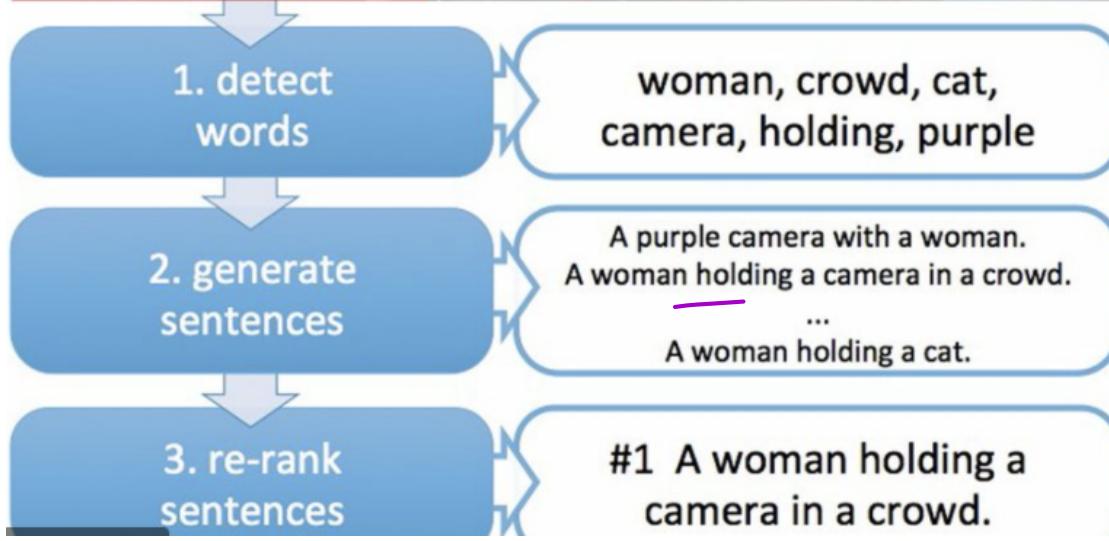


Image to Text!

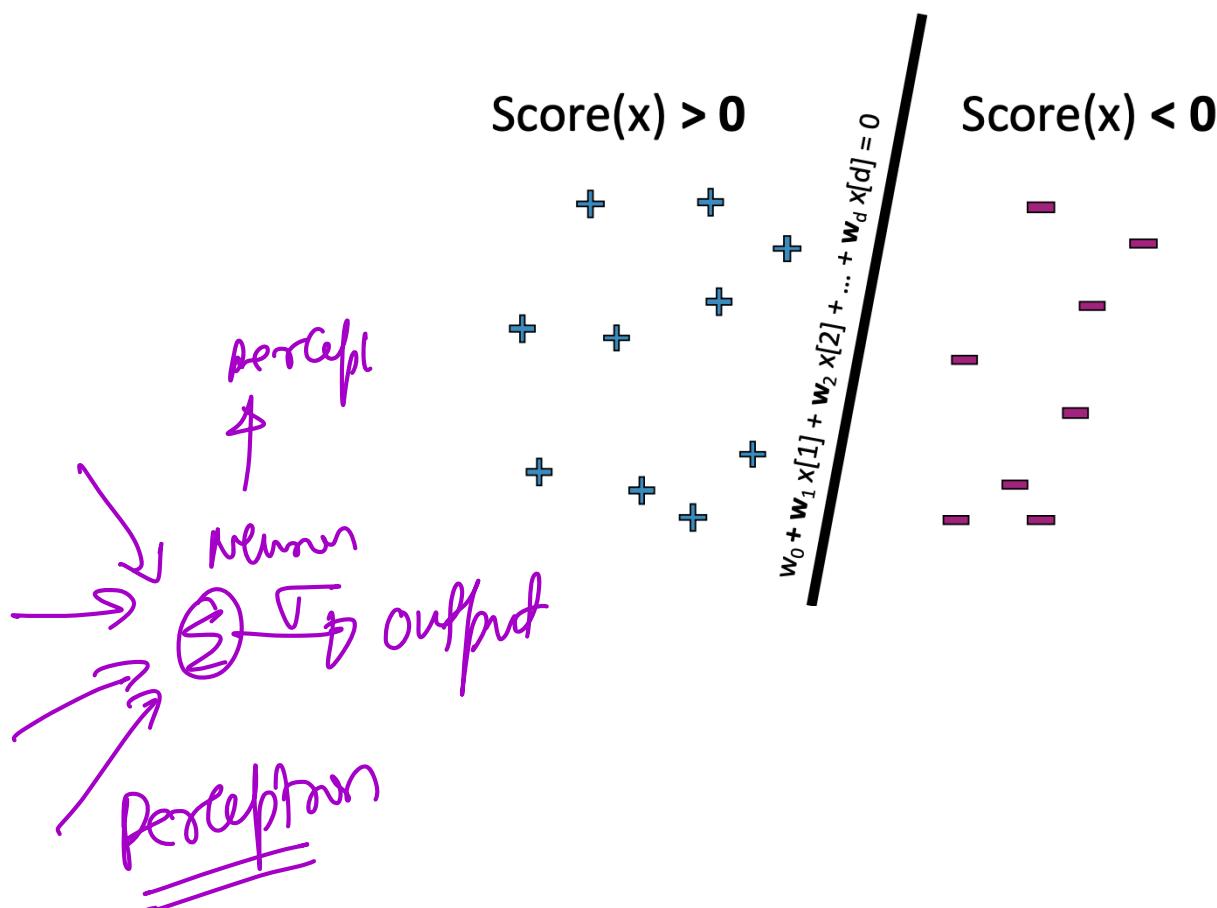


← CNN model →
+
Transformer
LSTM model

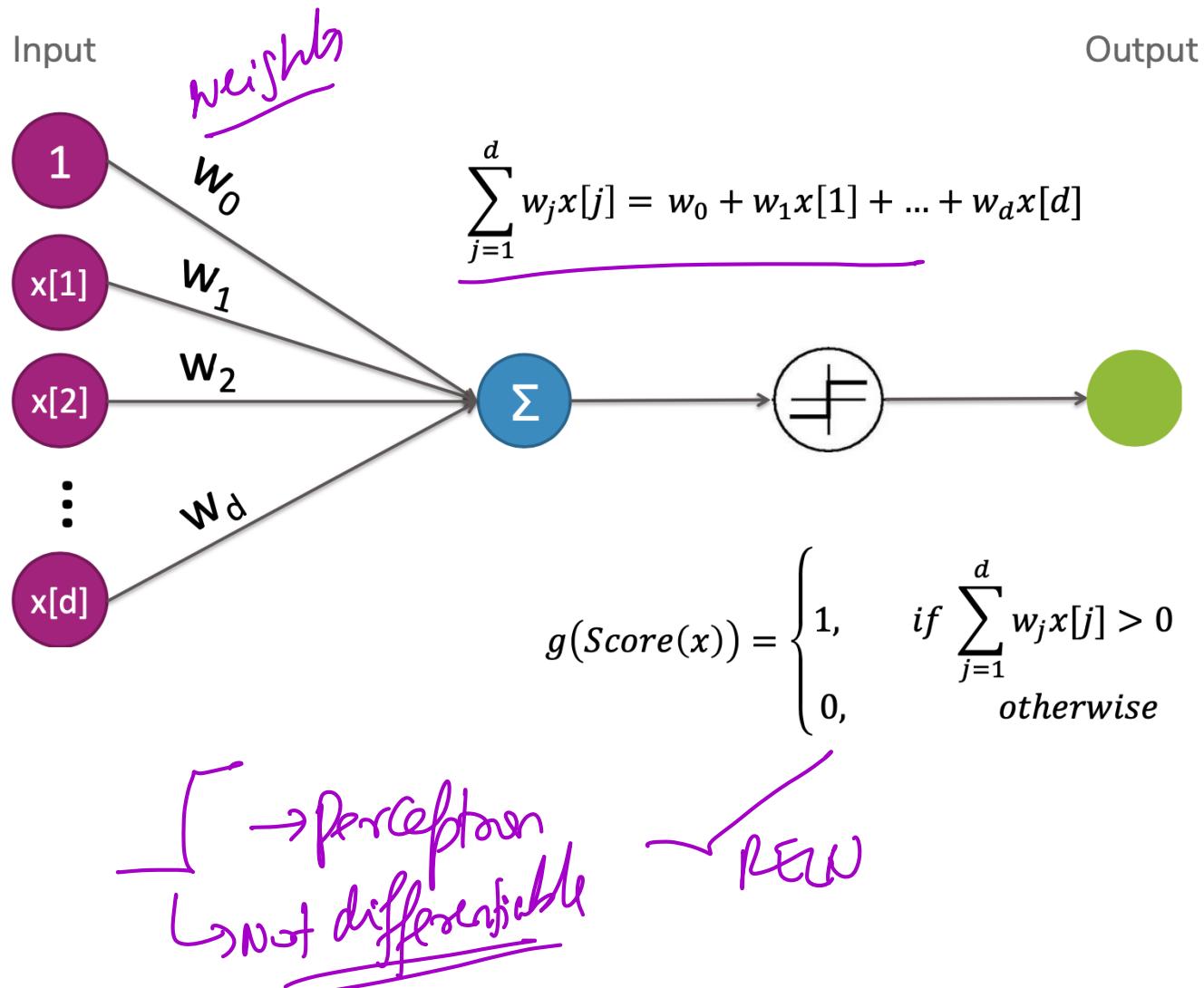


Perceptron

$$\text{Score}(x) = w_0 + w_1 x[1] + w_2 x[2] + \dots + w_d x[d]$$

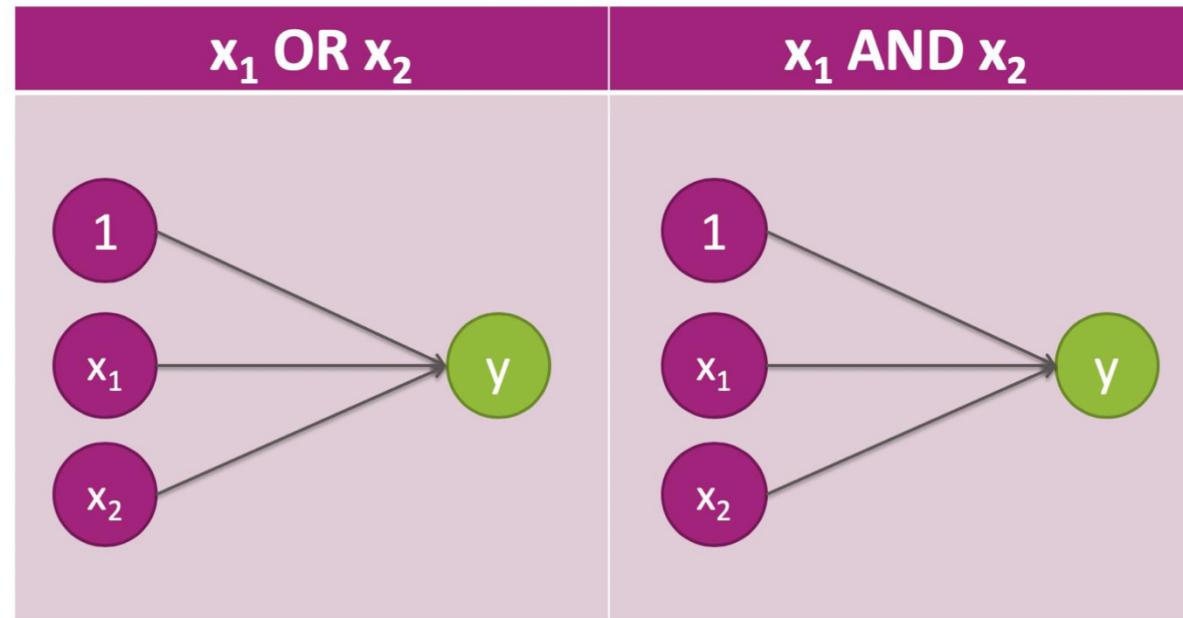


Perceptron



OR and AND Functions

What can a perceptrons represent?



x_1	x_2	y
0	0	0
0	1	1
1	0	1
1	1	1

x_1	x_2	y
0	0	0
0	1	0
1	0	0
1	1	1

Learning XOR

XOR through Multi-layer perceptron

This is a 2-layer neural network

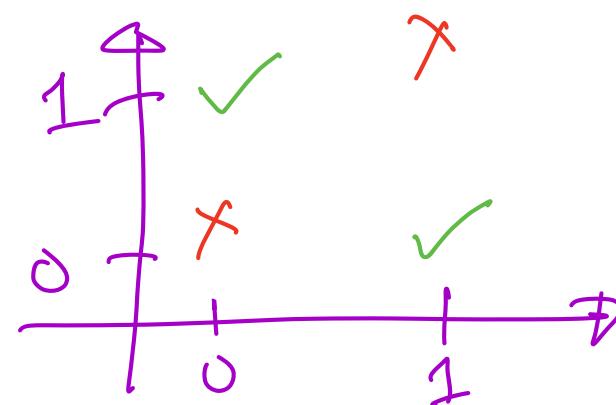
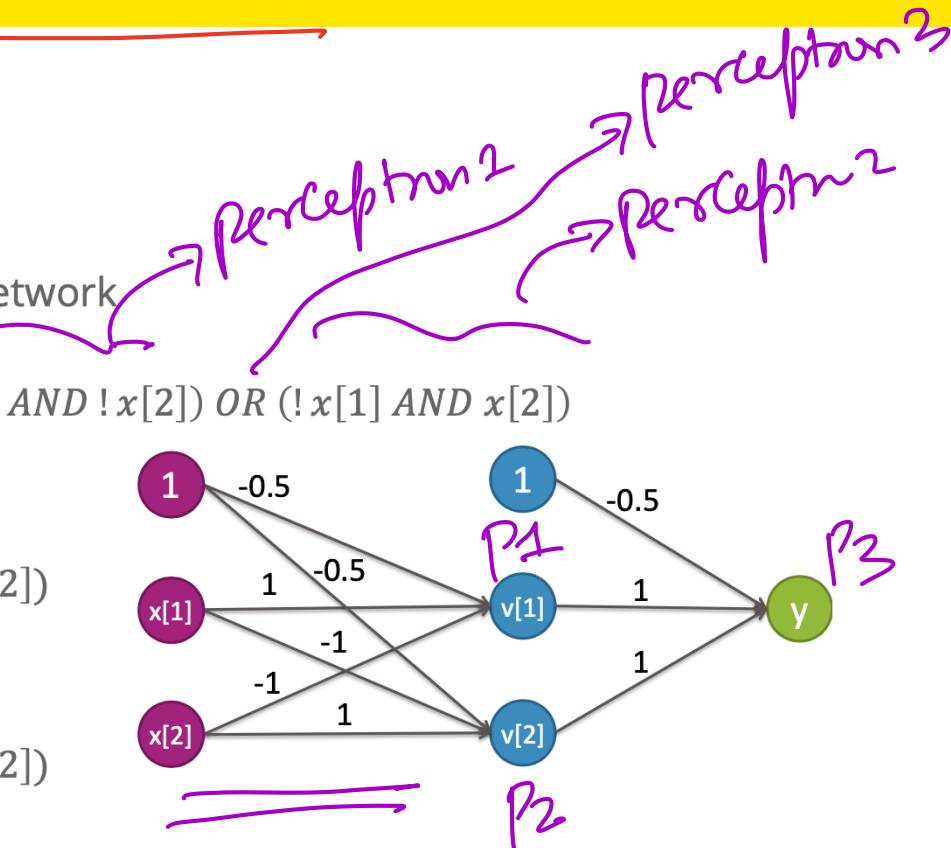
$$y = x[1] \text{ XOR } x[2] = (x[1] \text{ AND } !x[2]) \text{ OR } (!x[1] \text{ AND } x[2])$$

$$v[1] = (x[1] \text{ AND } !x[2]) \\ = g(-0.5 + x[1] - x[2])$$

$$v[2] = (!x[1] \text{ AND } x[2]) \\ = g(-0.5 - x[1] + x[2])$$

$$y = v[1] \text{ OR } v[2] \\ = g(-0.5 + v[1] + v[2])$$

MLP
= Extension of
Single Perceptron
↳ Logistic Regression

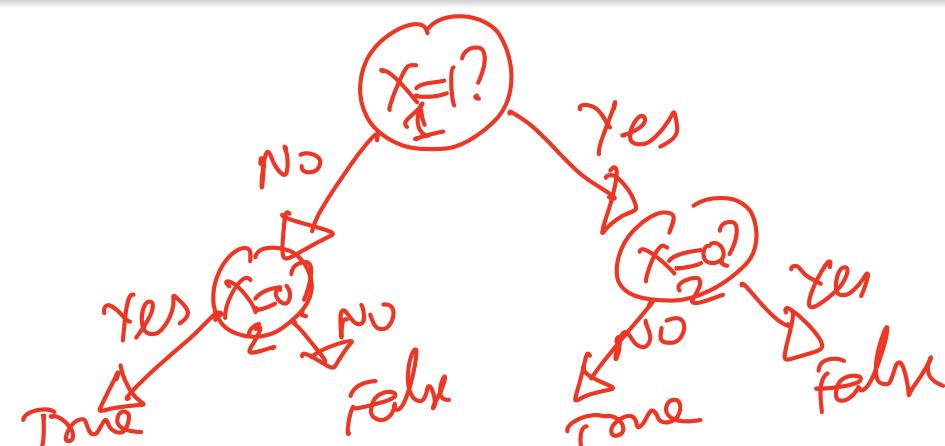


ICE #3

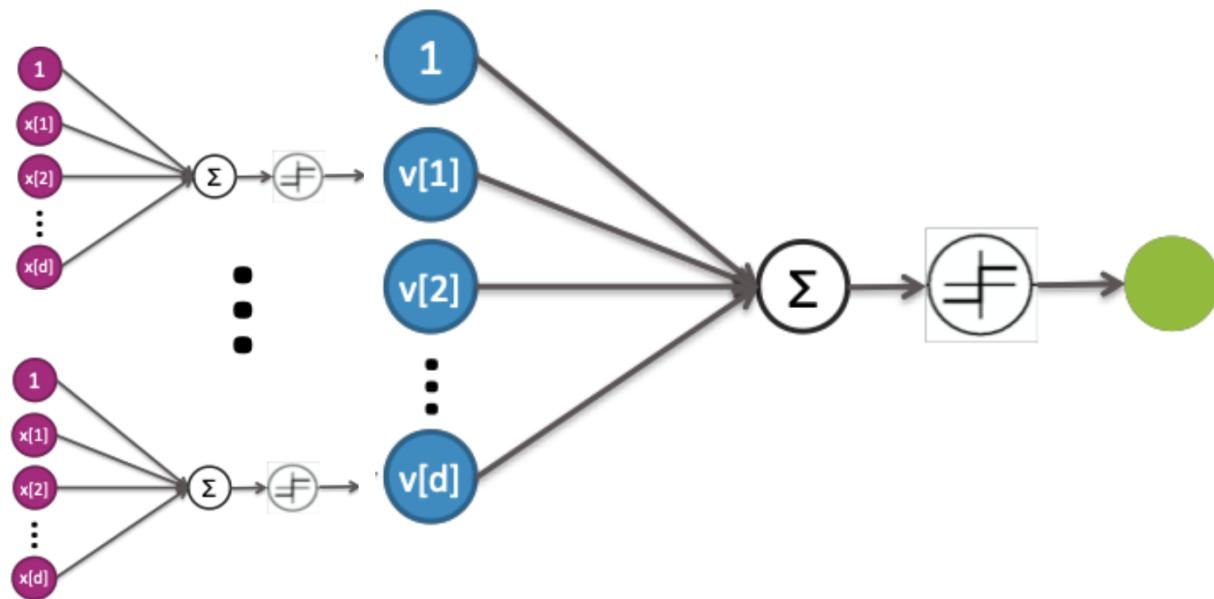
Which methods can learn the XOR function?

- ① Logistics Regression
- ② Naive Bayes Classifier
- ③ Decision Trees
- ④ Support Vector Machines

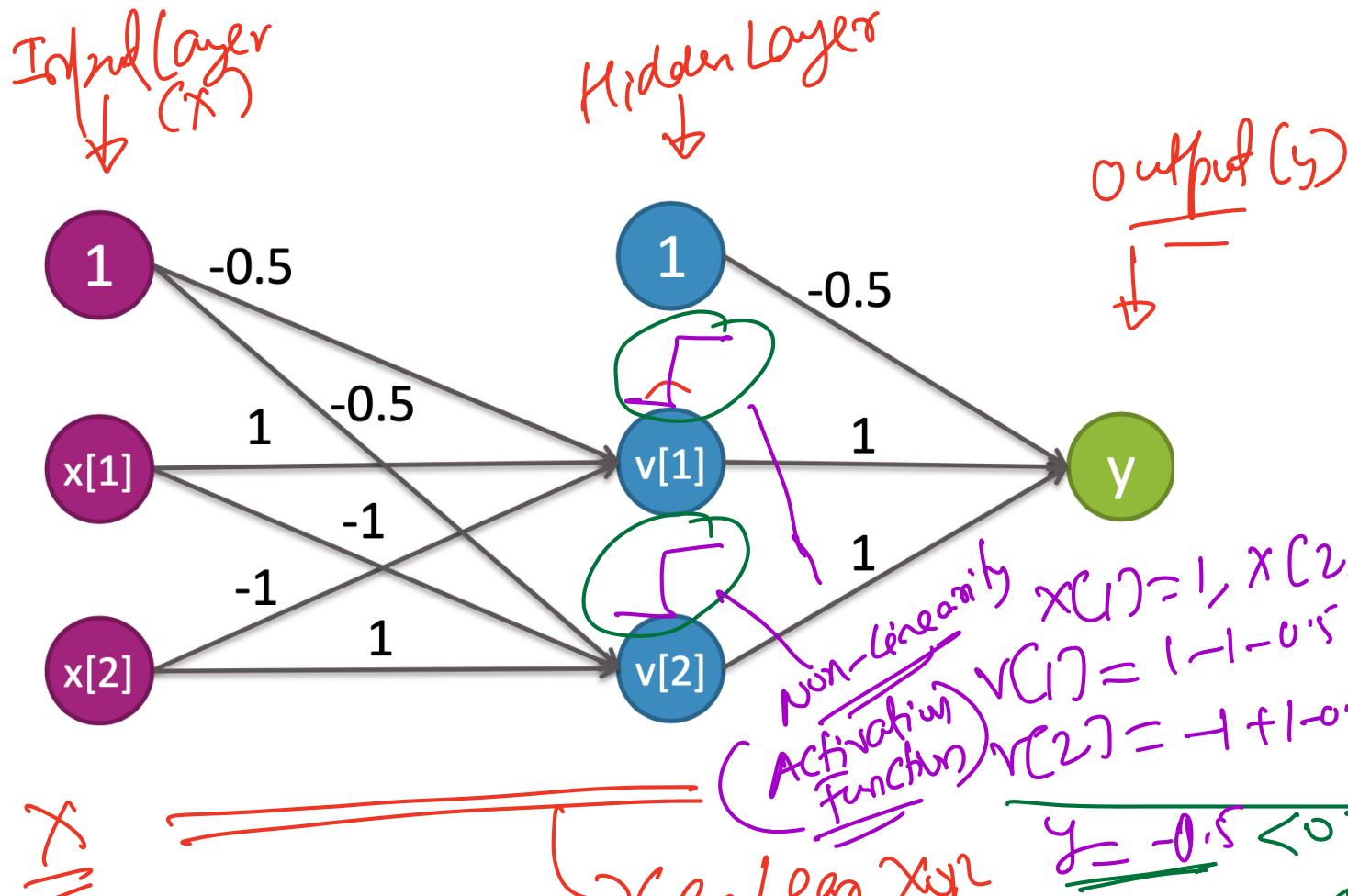
$\xrightarrow{\text{Baye rule}}$ $P(Y|X) \stackrel{\text{local}}{=} \frac{\tilde{P}(X|Y) P(Y)}{P(X)}$



Multi-Layer Perceptron (MLP)



Multi-Layer Perceptron (MLP)



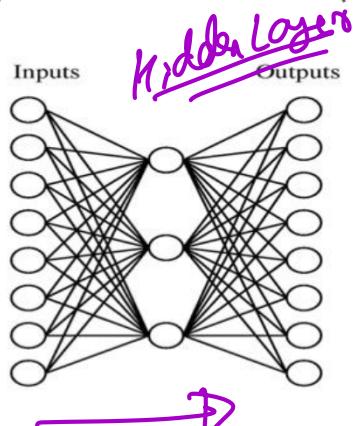
$$x[1] = 1, x[2] = 0$$

$$v(1) = \boxed{1 - 0.5} \quad v(2) = -1 + 0.5 = \boxed{0}$$

$$\begin{aligned} & \text{Non-linearity } x[1] = 1, x[2] = 1 \\ & v(1) = 1 - 0.5 = 0.5 \\ & v(2) = -1 + 0.5 = -0.5 \\ & y = v(1) + v(2) - 0.5 \\ & \quad \cancel{-0.5} \\ & \quad \cancel{+1} + 1 + 0.5 = 0.5 \\ & \boxed{y = 0.5 > 0} \end{aligned}$$

2 Layer Neural Network

Two layer neural network (alt. one hidden-layer neural network)



Feedforward NN

2 layers NN
Non-linear model

Single
(Linear model)

$$y_{out}(x) = g\left(w_0 + \sum_i w_j x[j]\right)$$

Sigmoid / Softmax

Logistic regression
(one-layer NN)

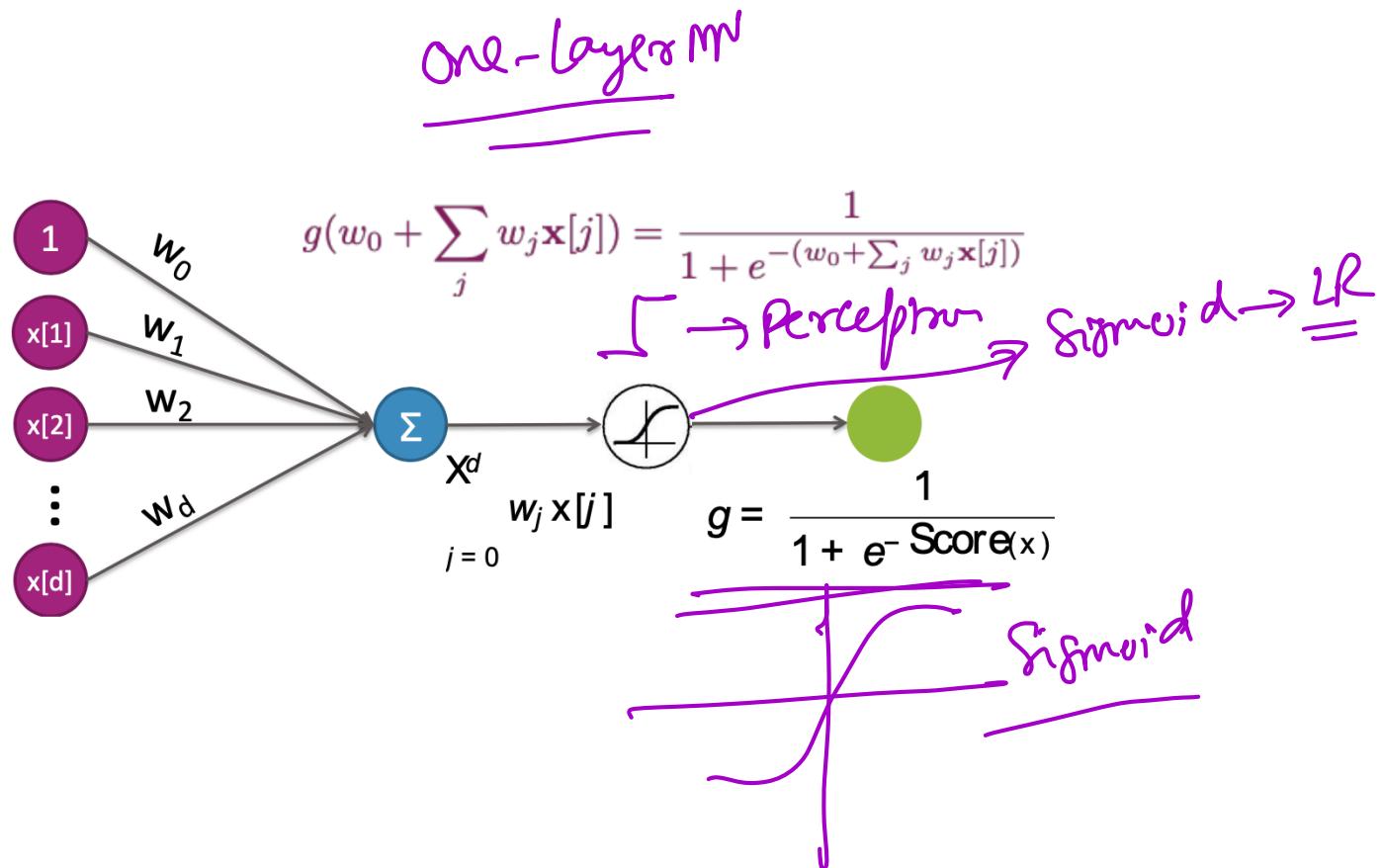
$$y = g\left(w_0 + \sum_k w_k g\left(w_0^{(k)} + \sum_j w_j^{(k)} x[j]\right)\right)$$

Activation
function

First Layer

Second Layer

Perceptron to Logistic Regression



Choices for Non-Linear Activation Function

Sigmoid

- Historically popular, but (mostly) fallen out of favor
- Neuron's activation saturates
(weights get very large -> gradients get small)
- Not zero-centered -> other issues in the gradient steps
- When put on the output layer, called "softmax" because interpreted as class probability (soft assignment)

Hyperbolic tangent $g(x) = \tanh(x)$

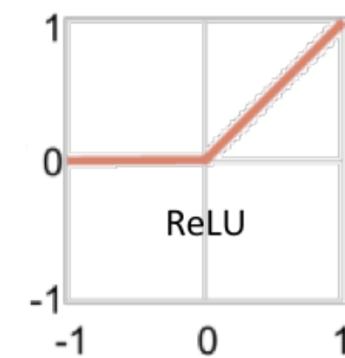
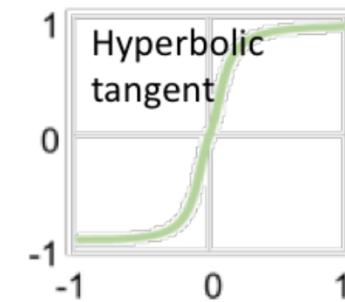
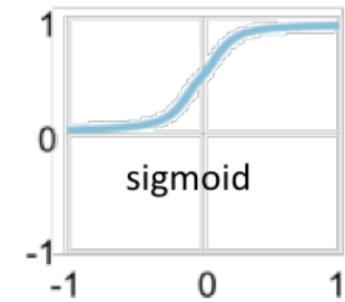
- Saturates like sigmoid unit, but zero-centered

Rectified linear unit (ReLU) $g(x) = x^+ = \max(0, x)$

- Most popular choice these days
- Fragile during training and neurons can "die off" ...
be careful about learning rates
- "Noisy" or "leaky" variants

Softplus $g(x) = \log(1+\exp(x))$

- Smooth approximation to rectifier activation

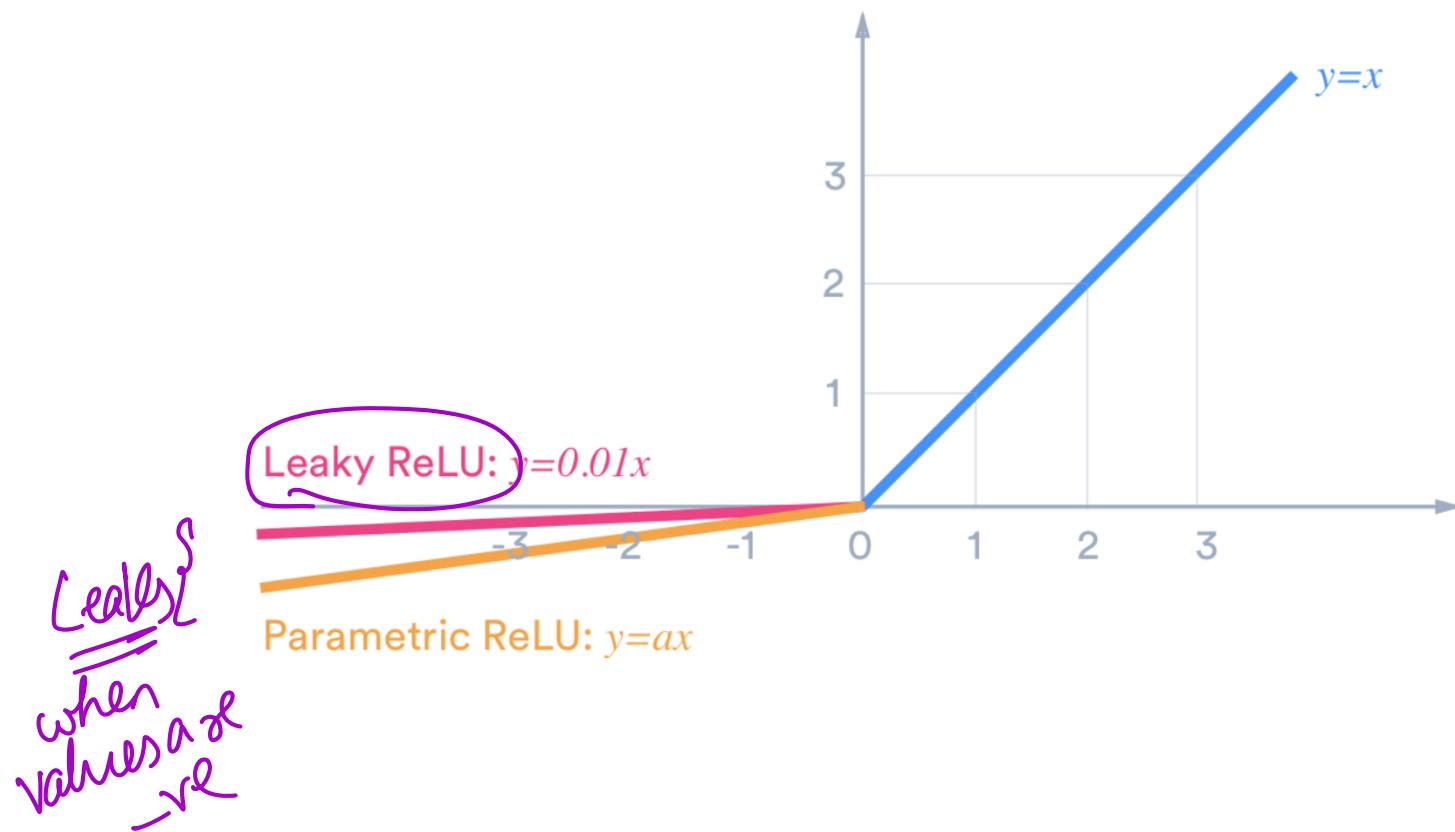


worthful for getting a good fit

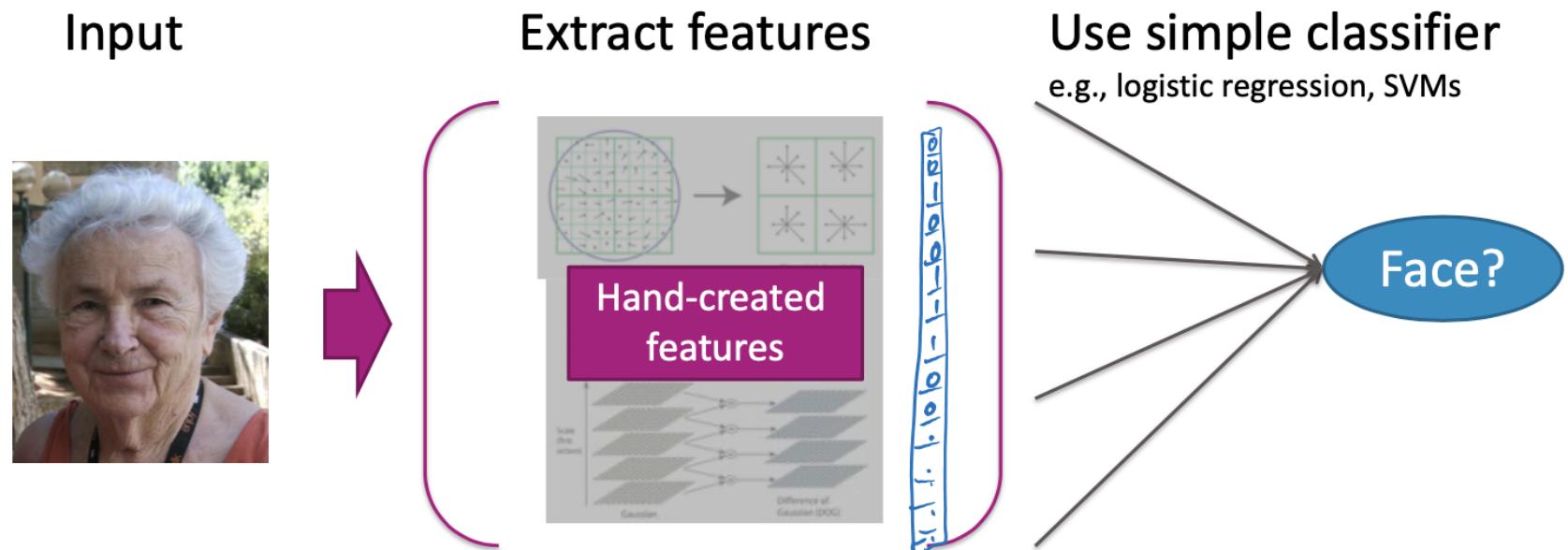
Linear
flexible

ReLU

ReLU vs Leaky ReLU



Computer vision before deep learning



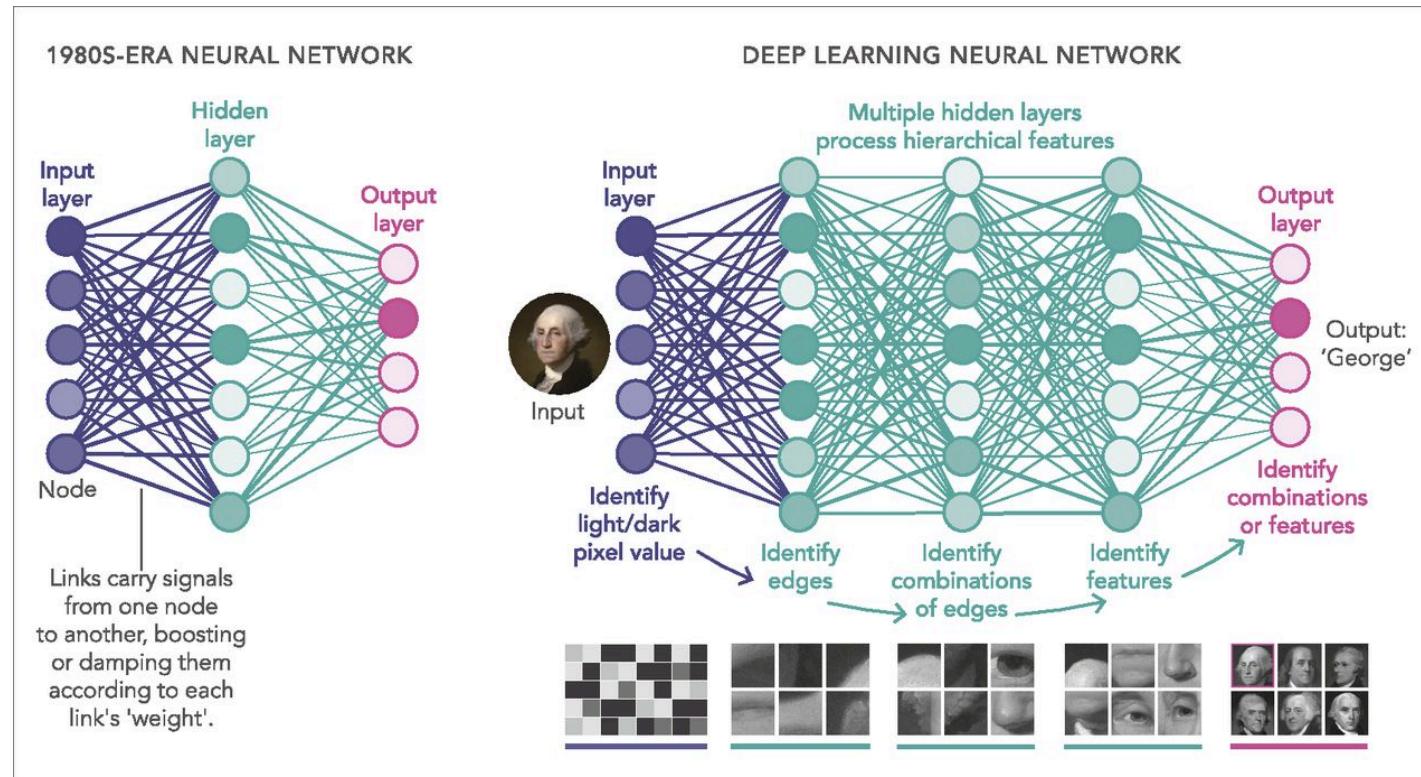
Computer vision after deep learning



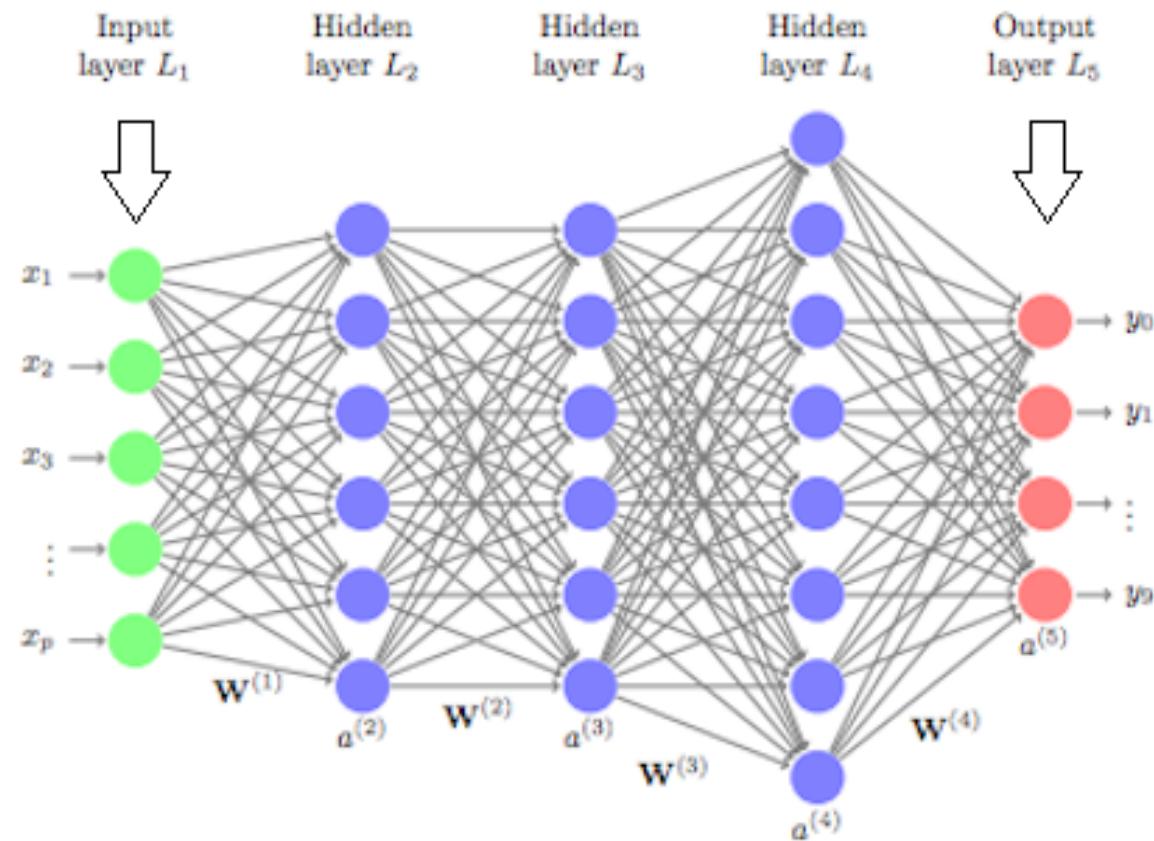
Example detectors learned		A 4x5 grid of small square images showing various learned facial detectors.	A 4x5 grid of small square images showing various learned object detectors, such as people and animals.
Example interest points detected	A 4x5 grid of small square images showing detected interest points on a textured surface.	A 4x5 grid of small square images showing detected interest points on a textured surface.	A 4x5 grid of small square images showing detected interest points on a textured surface.

[Zeiler & Fergus '13]

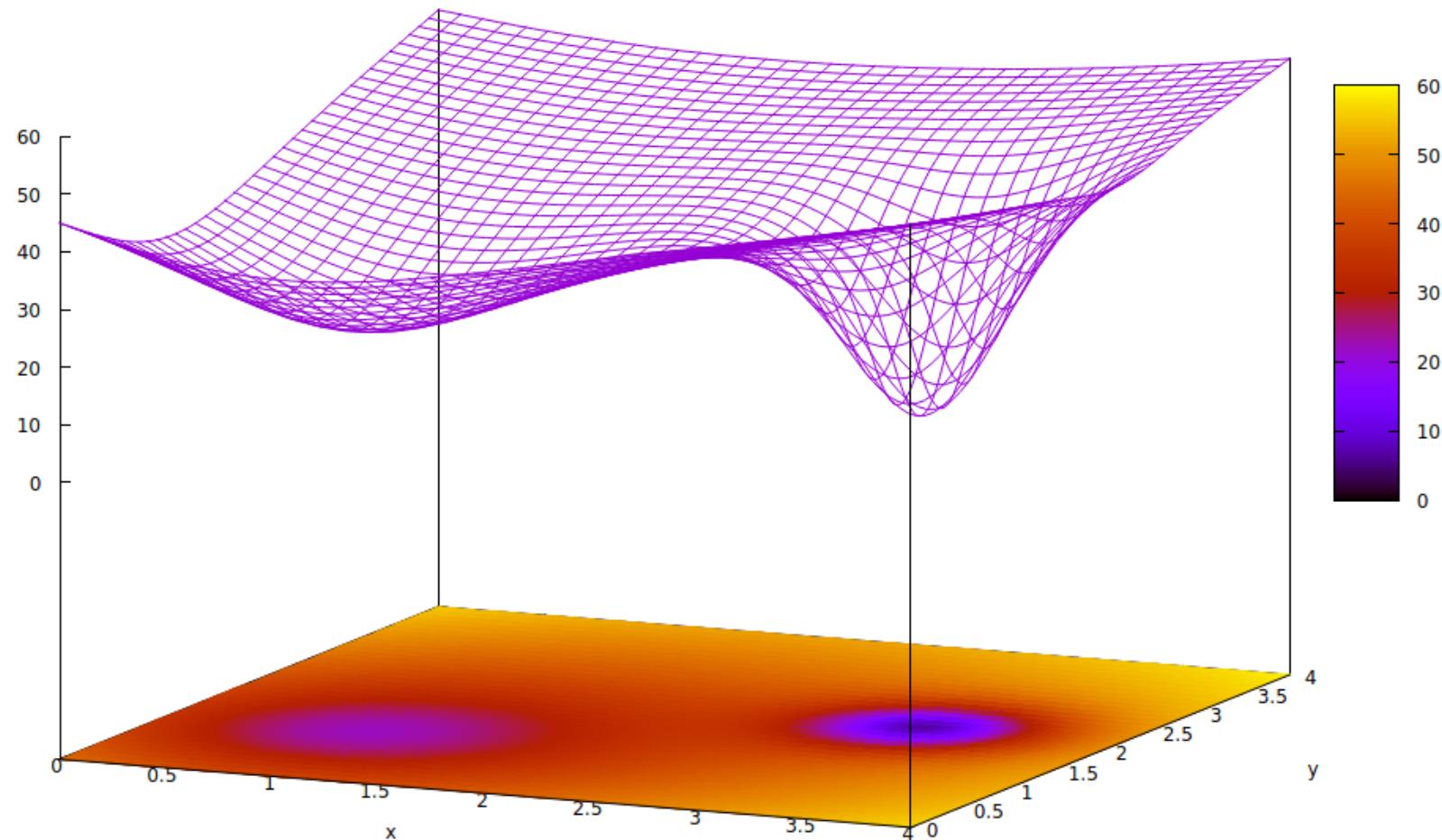
Feed-forward Deep Learning Architecture Example



Feed-forward Deep Learning Architecture Example



Good vs Bad Local minima



Hyper-parameters in Deep Learning

ICE #4: Which of the following is not a hyper-parameter in deep learning?

- ① Learning rate
- ② Number of Hidden Layers
- ③ Number of neurons per hidden layer
- ④ None of the above
- ⑤ All of the above

Hyper-parameters in Deep Learning

Hyper-parameters

- ① Learning rate
- ② Number of Hidden Layers
- ③ Number of neurons per hidden layer

Hyper-parameters in Deep Learning

Hyper-parameters

- ① Learning rate
- ② Number of Hidden Layers
- ③ Number of neurons per hidden layer
- ④ Type of non-linear activation function used

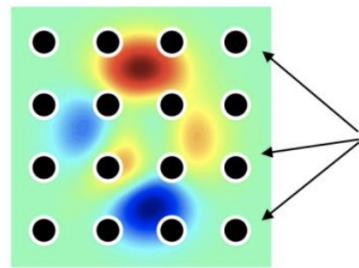
Hyper-parameters in Deep Learning

Hyper-parameters

- ① Learning rate
- ② Number of Hidden Layers
- ③ Number of neurons per hidden layer
- ④ Type of non-linear activation function used
- ⑤ Anything else?

Hyper-parameter tuning methods

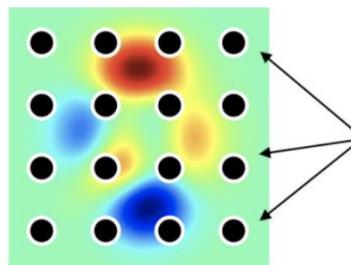
Grid search:



Hyperparameters
on 2d uniform grid

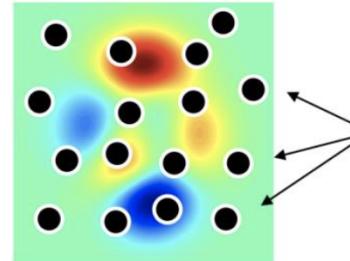
Hyper-parameter tuning methods

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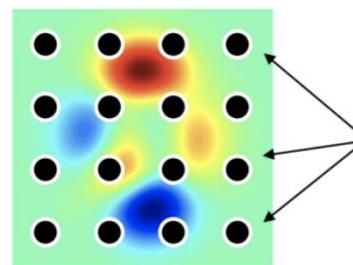
Random search:



Hyperparameters
randomly chosen

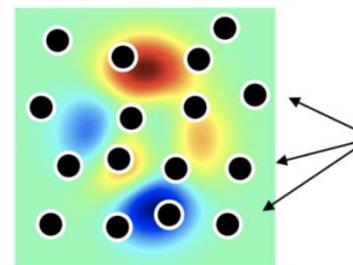
Hyper-parameter tuning methods

Grid search:



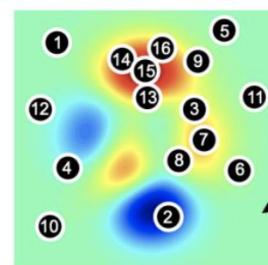
Hyperparameters
on 2d uniform grid

Random search:



Hyperparameters
randomly chosen

Bayesian Optimization:



Hyperparameters
adaptively chosen

ICE #5

Compute the number of parameters in DNN model

Consider a DNN model with 3 hidden layers where each hidden layer has 1000 neurons. Let the input layer be raw pixels from a 100×100 image and the output layer has 10 dimensions, let's say for a 10 class image classification example. How many total parameters exist in the DNN model?

- ① 10 million parameters
- ② 11 million parameters
- ③ 12 million parameters
- ④ 13 million parameters

Over-fitting in DNNs

How to handle over-fitting in DNNs

- ① A DNN model with 100 million parameters and only 100k data points or even a million data points will overfit unless we take care of over-fitting.

Over-fitting in DNNs

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Over-fitting in DNNs

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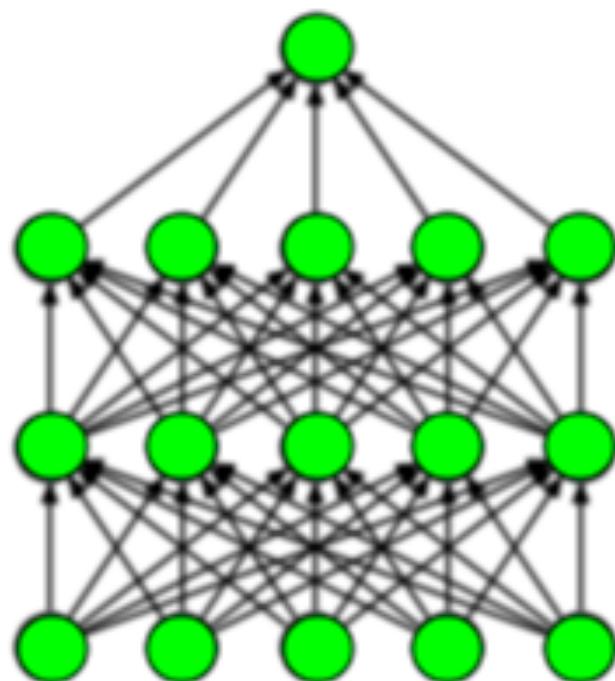
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Over-fitting in DNNs

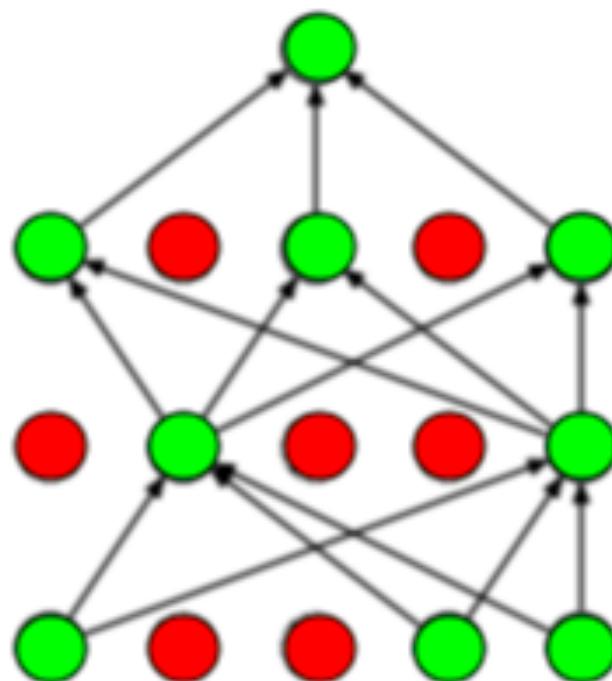
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- ④ Dropouts!
- ⑤ Early stopping is also a great strategy! Stop training the DL model when the validation error starts increasing. How's this different from regular validation we were doing earlier??
- ⑥ Book by Yoshua Bengio has tons of details and great reference for Deep Learning!

Taking care of Over-fitting: Dropouts

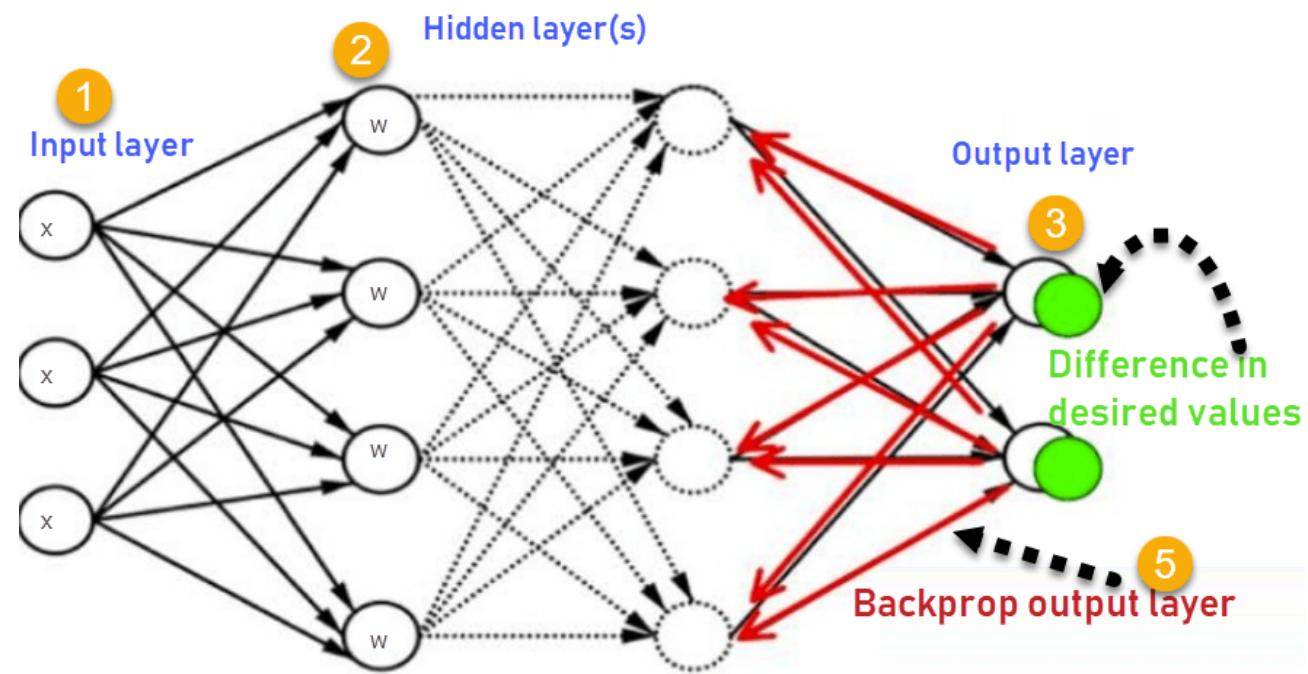


(a) Standard Neural Net

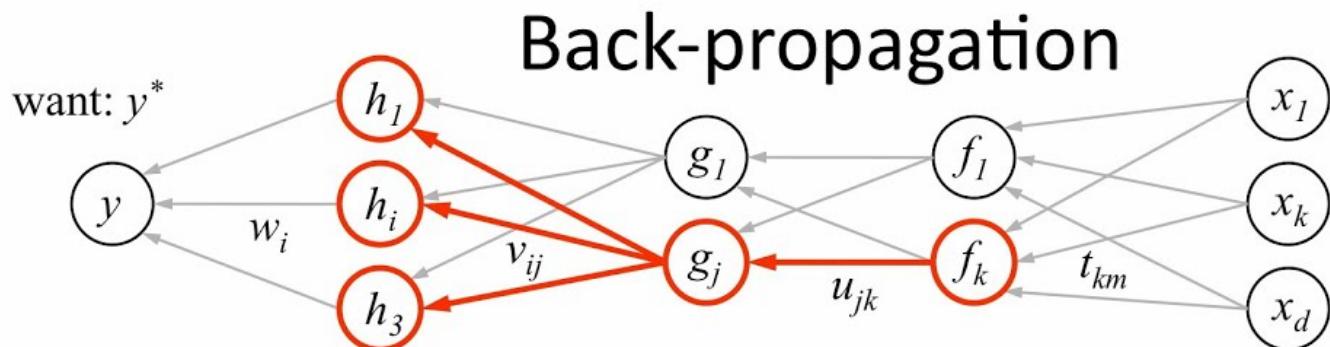


(b) After applying dropout.

Forward Propagation vs Back-propagation



Back Propagation explained



1. receive new observation $x = [x_1 \dots x_d]$ and target y^*
2. **feed forward:** for each unit g_j in each layer $1 \dots L$
compute g_j based on units f_k from previous layer: $g_j = \sigma\left(u_{j0} + \sum_k u_{jk} f_k\right)$
3. get prediction y and error $(y - y^*)$
4. **back-propagate error:** for each unit g_j in each layer $L \dots 1$

(a) compute error on g_j

$$\frac{\partial E}{\partial g_j} = \sum_i \underbrace{\sigma'(h_i)}_{\substack{\text{should } g_j \\ \text{be higher or lower?}}} \underbrace{v_{ij}}_{\substack{\text{how } h_i \text{ will} \\ \text{change as } g_j \text{ changes}}} \underbrace{\frac{\partial E}{\partial h_i}}_{\substack{\text{was } h_i \text{ too} \\ \text{high or} \\ \text{too low?}}}$$

(b) for each u_{jk} that affects g_j

(i) compute error on u_{jk}

$$\frac{\partial E}{\partial u_{jk}} = \underbrace{\frac{\partial E}{\partial g_j}}_{\substack{\text{do we want } g_j \text{ to} \\ \text{be higher/lower}}} \underbrace{\sigma'(g_j) f_k}_{\substack{\text{how } g_j \text{ will change} \\ \text{if } u_{jk} \text{ is higher/lower}}}$$

(ii) update the weight

$$u_{jk} \leftarrow u_{jk} - \eta \frac{\partial E}{\partial u_{jk}}$$

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