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Evaluating the Impacts of Parameter Uncertainty in a Practical **Transportation Demand Model**

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Abstract: The inherent uncertainty in travel forecasting models — arising from potential and unkown errors in input data, parameter estimation, or model formulation — is receiving increasing attention from the scholarly and practicing community. In this research, we investigate the variance in forecasted traffic volumes resulting from varying the mode and destination choice parameters in an advanced trip-based travel demand model. Using Latin hypercube sampling to construct several hundred combinations of parameters across the plausible parameter space, we introduce substantial changes to implied travel impedances and modal utilities. However, the aggregate effects of of these changes on forecasted traffic volumes is small, with a variance of approximately 1 percent on high-volume facilities. It is likely that in this example — and perhaps in others — the static network assignment places constraints on the possible volume solutions and limits the practical impacts of parameter uncertainty. Further research should examine the robustness of this finding to other less constrained networks and to activity-based travel model frameworks.

Keywords: Travel modeling; Uncertainty

1. Introduction

The inherent accuracy and uncertainty in travel forecasting models is receiving increasing attention from the scholarly and practicing community. Given that such models are used in the allocation of billions of dollars of infrastructure financing each year, the financial risks for inaccurate or imprecise forecasts are high (Flyvbjerg et al., 2005; Voulgaris, 2019).

Transportation demand forecasting models, like other mathematical-statistical models, might be abstracted to the following basic form,

$$y = f(X, \beta)$$

where y is the variable being predicted based on input data X, moderated through a specific functional form f() and parameters β . Three general sources of error may lead a forecast value \hat{y} to differ from the "true" or "actual" value of y (Rasouli and Timmermans, 2012):

- The input data *X* might contain errors, due to inaccuracies in the base year, or an inaccurate projection of land use, petroleum price, or other key input variable. This was among the primary issues identified by Hoque et al. (2021) in a historical analysis of the accuracy of travel forecasts.
- The model form f() may be improperly specified. Variables that play a major role in travel behavior may not be included due to lack of information, or the unobserved error components may have a different correlation than was assumed during model development. A detailed description of specifying mode choice model variables and nesting of error structures is given by Koppelman and Bhat (2006).

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3. The parameter estimates $\hat{\beta}$ of the "true" parameters β may have incorrect values. This may be because the parameters were estimated on an improperly specified model f(), or because the estimation dataset was improperly weighted.

Of these potential sources of error, only the third is substantively addressed in classical statistics. The standard errors of the model parameter estimates in a theoretical perspective address the parameter uncertainty question to a great degree. Yet even this source of uncertainty has been largely ignored in transportation forecasts, and model development documentation often elides the variance in these values completely (National Academies of Sciences, Engineering, and Medicine., 2012). Zhao and Kockelman (2002) examined the effects of this parameter uncertainty in a trip-based model of a contrived 25 zone region, but a systemic analysis of this uncertainty in a practical model is not common.

In this research, we investigate the uncertainty in traffic forecasts resulting from plausible parameter uncertainty in an advanced trip-based transportation demand model. Using a Latin hypercube sampling (LHS) methodology, we simulate one hundred potential parameter sets for a combined mode and destination choice model in Roanoke, Virginia, USA. We then assign the resulting trip matrices to the highway network for the region and evaluate the PM and daily assigned traffic volumes alongside the variation in implied impedance and accessibility.

This paper proceeds first with a description of the model design and simulation sampling methodology in Chapter 3, followed by a discussion of the variation in mode, destination, and traffic performance measures in Chapter 4. The paper concludes in Chapter 5 with a summary of the key findings alongside a presentation of limitations and related indications for future research.

2. Literature Review

Uncertainty has been examined in various ways over the last two decades, and is becoming increasingly important for researchers. This review looks at why uncertainty is important to evaluate in transportation demand models, and research that has been done to evaluate uncertainty. Rasouli and Timmermans (2012) has an extensive literature review on this topic. An overview of the literature and which source of uncertainty they evaluate can be found in Table 1.

Table 1. Studies of Forecasting Uncertainty

Reference	Uncertainty Source(s) Evaluated		
Rodier & Johnson (2002) Zhao & Kockelman (2002) Clay & Johnson (2005) Flyvbjerg (2005) Armoogum et al. (2009)	Input Data Input Data & Parameter Estimates Input Data & Parameter Estimates Model Form Model Form		
Duthie et al. (2010) Welde & Odeck (2011) Yang et al. (2013) Manzo et al. (2015) Petrik et al. (2016)	Input Data & Parameter Estimates Model Form Input Data & Parameter Estimates Input Data & Parameter Estimates Input Data & Parameter Estimates		
Petrik et al. (2020) Hoque et al. (2021)	Model Form & Parameter Estimates Input Data		

Model accuracy is the basis for why uncertainty of input data and/or parameter estimates are important to study. Travel forecasters have always been cognizant of the uncertainty in their forecasts, especially as project decisions are made using these models, often with high financial impacts.

Flyvbjerg et al. (2005) collected data from various forecasting traffic models with an emphasis on rail projects. They used the forecast data for a given year and the actual

value that was collected for the same year. Their study found that there is a statistical significance in the difference of the estimated and actual values. Rail projects are generally overestimating passenger forecasts by 106%, and half of road projects have a traffic forecast difference of plus or minus 20%. They did not identify where this inaccuracy came from, but they identified that it was important for future research.

Armoogum et al. (2009) looked at uncertainty within a forecasting model for the Paris and Montreal metropolitan regions. The sources of uncertainty analysed were calibration of the model, behavior of future generations, and demographic projections. A jackknife technique, rather than sampling methods, was used to estimated confidence intervals for each source of error using multiple years of analysis. This technique is a way to reduce the bias of an estimator and permits the estimation of confidence intervals to produce variance estimates. They found that the longer the forecasting period was, the larger the uncertainty. Generally the model forecast within 10-15%, reaching higher percentage ranges for variables with small values or small sample sizes.

Welde and Odeck (2011) compared actual and forecast traffic values for 25 toll and 25 toll free roads in Norway. They evaluated the accuracy of Norwegian transportation planning models over the years. Generally traffic models overestimate traffic. This study found that toll projects, on average, overestimated traffic, but only by an average of 2.5%. Toll free projects, however, underestimated traffic by an average of 19%. They concluded that Norwegian toll projects have been fairly accurate, with a probable cause coming from the scrutiny that planners get when developing a toll project. A similar scrutiny should then also be placed on toll free projects as they are significantly less accurate.

These articles show that models have errors which effects traffic projections by a significant amount. These articles identified that error existed but did not quantitatively identify the source of the error. The most researched error source has been on model form but that research has mostly been excluded in this review as it is not the main focus of this research. The second most researched form has been on input data. Chronologically, Rodier and Johnston (2002), Zhao and Kockelman (2002), Clay and Johnston (2005), Duthie et al. (2010), Yang et al. (2013), Manzo et al. (2015), and Petrik et al. (2016) have all researched input error, with all but the first also looking at parameter estimate error as well. Parameter estimation error has been the least researched source of uncertainty, where there have been no studies focused only on that source of error. Petrik et al. (2020) looked at parameter estimates, but with a focus also on model form error. The details of each study are described below in chronological order.

Rodier and Johnston (2002) looked at uncertainty in socioeconomic projections (population and employment, household income, and petroleum prices) at the county-level for the Sacramento, California region. They wanted to know if the uncertainty in the range of plausible socioeconomic values was a significant source of error in the projection of future travel patterns and vehicle emissions. They identified ranges for population and employment, household income, and petroleum price for two scenario years (2005 and 2015). The ranges varied based on the scenario year and the socioeconomic variable. They changed one variable at a time for a total of 19 iterations of the model run for 2005 and 21 iterations for 2015. Their results indicated that the error in projections for household income and petroleum prices is not a significant source of uncertainty, but error ranges for population and employment projections are a significant source for changes in travel and emissions. The input data of population and employment were a significant factor to the model result uncertainty.

Zhao and Kockelman (2002) looked at the propagation of uncertainty through each step of a trip-based travel model from variation among inputs and parameters. This analysis used a traditional four-step urban transportation planning process (trip generation, trip attraction, mode split, and trip assignment) on a 25-zone sub-model of the Dallas-Fort Worth metropolitan region. Monte Carlo simulation was used to vary the input and parameter values. These values were all ranged using a coefficient of variation (c_v) of 0.30. The four-step model was run 100 times with 100 different sets of input and parameter

values. The results of these runs showed that uncertainty increased in the first three steps of the model and the final assignment step reduced the compounded uncertainty, although not below the levels of input uncertainty. The authors determined that uncertainty propagation was significant from changes in inputs and parameters, but the final step nearly stabilizes the uncertainty to the same amount as assumed (0.30 c_v assumption with a 0.31 c_v in the results of trip assignment).

Another study that looked at input data uncertainty was Clay and Johnston (2005). These researchers varied three inputs and one parameter to analyze uncertainty of outputs on a fully integrated land use and travel demand model of six counties in the Sacramento, California region. The variables used for analysis were productions, commercial trip generation rates, perceived out-of-pocket costs of travel for single occupant vehicles, and concentration parameter. Exogenous production, commercial trip generation rates, and the concentration parameter were varied by plus or minus 10, 25 and 50%, while the cash cost of driving was varied by plus or minus 50 and 100%. This resulted in 23 model runs, one for each changed variable and one for the base scenario. Their research found that any uncertainty in the inputs resulted in large difference in the vehicle miles traveled output, although this difference was a lower percentage than the uncertainty in the input.

Duthie et al. (2010) evaluated uncertainty at a different level. They use a small generic gravity-based land use model with the traditional four steps, using a coefficient of variation of 0.3 from Zhao and Kockelman (2002) for input and parameters, although using antithetic sampling. In this sampling method, pairs of negatively correlated realizations of the uncertain parameters are used to obtain an estimate of the expected value of the function. The uncertainty was evaluated on the rankings of various transportation improvement projects. They found that there are a few significant differences that arise when changing the input and parameter values that result in different project rankings, and thus neglecting uncertainty can lead to suboptimal network improvement decisions.

Yang et al. (2013) evaluated a quantitative uncertainty analysis of a combined travel demand model. They looked at input and parameter uncertainty *also* using a coefficient of variation of 0.30. Rather than using a random sampling method for choices they used a systematic framework with a variance-covariance matrix. Their research found that the coefficient of variation of the outputs are similar to the coefficient of variation of the inputs, and that the effect of parameter uncertainty on output uncertainty is generally higher than that of input uncertainty. This finding contradicts the finding of Zhao and Kockelman (2002). The authors concluded that improving the accuracy of parameter estimation is more effective that that of improving input estimation as they found that in most steps of the model, the impact of parameter uncertainty was more important that that of input uncertainty.

Manzo et al. (2015) looked at uncertainty on model input and parameters for a trip-based transportation demand model in a small Danish town. They used a triangular distribution with LHS to create the range in parameters, and using the information from Zhao and Kockelman (2002) they also used a coefficient of variation of 0.30 and 100 draws, choosing these values at they had been previously used. Their addition to the research of uncertainty, was by examining uncertainty under different levels of congestion. Their research found that there is an impact on the model output from the change in input and parameter uncertainty and requires attention when planning. Also, model output uncertainty was not sensitive to the level of congestion.

Petrik et al. (2016) evaluated uncertainty in mode shift predictions due to uncertainty from input parameters, socioeconomic data, and alternative specific constants. This study was based on a high-speed rail project in Portugal as a component of the Trans-European Transport Network. They collected survey data and developed discrete choice models. The authors created their own parameter values from the collected data, obtaining the mean or "best" value from the surveys and the corresponding t-statistic. With these they generated 10,000 samples each of parameter values, socioeconomic inputs, and mode-specific constants, using bootstrap re-sampling, Monte Carlo sampling, and triangular

distribution methods respectively. The authors found that variance in alternative specific attributes is the major contributor to output uncertainty in comparison to parameter variance or socioeconomic variance. Socioeconomic data had the least contribution to overall output variance, and there was a relatively insignificant mode shift due to variability in parameters.

Petrik et al. (2020) used an activity based microsimulation travel demand model for Singapore to evaluate model form and parameter uncertainty. This model has 22 submodels and 817 parameters. The authors determined which of the 817 parameters the sub-models were most sensitive to and applied a full sensitivity analysis of the top 100 of the parameters, preserving correlations. Using the mean parameter value and the standard deviations they had for all of them they used Latin hypercube sampling with 100 draws to look at the outcomes of the change in each parameter value. Different sized samples of the model population were also considered in their research. They found that of the 100 most sensitive parameter values, the outcome coefficient of variation varied from 3% to 49%. The variance of the parameter variables did not exceed 19%, and thus the results from the parameter uncertainty were higher than the variance in the parameters. They also found that the results of the parameter uncertainty was higher than simulation uncertainty.

In transportation demand models, when uncertainty is analysed, most research to this point has focused on input uncertainty or model forms, rather than parameter estimate uncertainty (Rasouli and Timmermans, 2012). Of the 12 articles in this review, two look at input data as the only focus of their uncertainty research, three focus on model form uncertainty, one looks at both model form and parameter estimate uncertainty, and six focus on both input data and parameter estimate uncertainty. No researchers have looked at parameter estimate uncertainty as the only source of error in their models. When parameter uncertainty has been examined in existing literature, it is often in conjunction with input errors, or on small and non-practicing models. No studies that we could identify have used real models for their analyses. Uncertainty research is needed as transportation demand models provide estimates and forecasts for decision and policy makers. An inaccurate model or large output variance could change what decisions are made and when (AEP50 Committee on Transportation Demand Forecasting, 2023). Thus there is a critical research need for a detailed exploration of parameter estimation uncertainty in a practical travel model.

3. Model Design and Methodology

3.1. Model Design

To examine the effects of parameter input sensitivity, we adapted a trip-based travel demand model from the Roanoke Valley Transportation Planning Organization (RVTPO). The RVTPO model provides an ideal testing environment for this research because it uses an integrated mode and destination choice framework common in more advanced trip-based models. At the same time, its small size (approximately 215 zones) means the entire model runs in a few minutes and thus allows for efficient testing of multiple model runs.

The total passenger trips T traveling from zone i to zone j on the highway in a period t is

$$T_{ijt} = P_i * \mathcal{P}_{\text{auto}}(\beta, C_{ijt}) * \mathcal{P}_i(\gamma, A_i, MCLS_{ijt}) * \Delta_t$$
 (1)

where P is the productions at zone i; \mathcal{P}_{car} is the car mode choice probability determined by utility parameters β and the travel costs C between i and j at time period t; \mathcal{P}_j is the destination choice probability of choosing destination j given the utility parameters γ , attractions A, and the impedance as the mode choice model logsum $MCLS_{ijt}$. A time-of-day and direction factor Δ finalizes the total assigned trips.

The productions P_i , and attractions A_j were extracted from the RVTPO Model and held constant. The attractions are determined from the socioeconomic (SE) data. The SE data included information by TAZ for the total population, number of households, total workers, and workers by employment type. The trip productions are organized by TAZ and trip purpose. The trip purposes used in this model are Home Based Work (HBW), Home

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HBW NHB Variable **HBO Mode Choice Coefficients** In-vehicle travel time -0.0250-0.0150-0.0200 β_{ivtt} Travel cost -0.0016-0.0024-0.0025 β_{tc} β_{wd} Walk distance -0.0625-0.0375-0.0500 Auto operating cost (cents/mile) β_{ac} 13.6000 13.6000 13.6000 **Mode Choice Constants** -2.2714Transit constant k_{trn} -0.3903 -1.9811NonMotorized constant -1.2258-0.3834-0.8655 k_{nmot} **Destination Choice Parameters** 0.0000 0.5664 Households 1.1657 γ_{hh} Other + Office $\gamma_{oth+off}$ 0.0000 0.8064 0.5626 Office 0.4586 0.0000 0.0000 γ_{off} Other 0.0000 0.0000 1.6827 γ_{oth} Retail 0.6087 2.2551 5.1190

Table 2. Choice model parameters

Based Other (HBO), Non-Home Based (NHB), Commercial Vehicles (CV), Internal-External (IXXI), and External-External (XX). Only the first three are analysed, but all of the purposes are assigned to the network. CV, IXXI, and XX trips were kept fixed for this analysis.

 γ_{ret}

The two parameter vectors β and γ describe the mode choice model and destination choice model coefficients, respectively. Mode choice estimates how many trips from i to j will happen on each available mode k.This model analyses three modes of transportation: auto, non-motorized, and transit. The mode by which a trip is made is determined by calculated utilities for the three modes. These utilities take inputs from parameter values and time and distance skims X. Skims are either the time or distance to travel between zone pairs. Travel time for auto used the single occupancy vehicle peak time, non-motorized travel time used the distance skim multiplied by a factor of average walking speed (3 mph), and transit time used the walk to bus peak time. The mode choice parameters (constants and coefficients) were also obtained from the RVTPO model. These values are shown in Table 2.

The utility equations for the mode choice model are as follows:

$$U_{auto} = \beta_{ivtt} * X_{auto} + \beta_{tc} * \beta_{ac} * X_{dist}$$

$$U_{nmot} = k_{nmot} + 20 * \beta_{wd} * X_{nmot}$$

$$U_{trn} = k_{trn} + \beta_{ivtt} * X_{trn}$$

These utilities are used to calculate the MCLS by:

$$MCLS_{ij} = \ln\left(\sum_{k \in K} e^{U_{ijk}}\right).$$
 (2)

If the distance was greater than 2 miles, non-motorized travel was excluded.

This logsum value is then used as the primary impedance for a destination choice model (Ben-Akiva and Lerman, 1985). Destination choice estimates travel patterns based on mode choice, trip generators (workers and households), and destination choice parameters. These parameter values are also shown in Table 2. The destination choice utility is the primary impedance (mode choice logsum value) plus the natural log of the size term, where the sized term is calculated as:

$$A_{j} = \gamma_{hh} * HH + \gamma_{off} * OFF + \gamma_{ret} * RET + \gamma_{oth} * OTH + \gamma_{oth+off} * OFFOTH$$
 (3)

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HH is the total households in zone j. OFF, RET, and OTH are the jobs in zone j by employment type office, retail, and other respectively. The destination choice utility is then transformed into a destination choice logsum value with:

$$DCLS = \ln\left(\sum_{i \in I} e^{\ln(A_i) + 1 * MCLS_{ij}}\right)$$
(4)

The probability of both the mode choice and destination choice are calculated using the exponentiated utility divided by the corresponding logsum. These probabilities in conjunction with the trip productions can calculate the number of production-attraction (PA) trips between each zone by each mode and purpose. The auto trips are calculated by multiplying the probability of the destination by PA pair, the productions for each origin, and the probability of an auto mode choice by PA pair. This results in PA auto trips. The same process is followed for the other two modes. These PA trips are converted into origin destination (OD) trips by multiplying the trips by corresponding time of day factors (see #eq-trips). These trips are calculated using Bentley's CUBE and the RVTPO model. The trips, by time period, are assigned to the highway network by the shortest path by time using free flow speed and with link capacity as a restriction.

3.2. Uncertainty Design

Within the mode and destination models there exists uncertainty within the parameters in Table 2. Sampling methods can take the defined uncertainty and choose potential parameter values within the possible range. Two common methods for parameter sampling include, Monte Carlo (MC) simulation and Latin hypercube sampling (LHS). MC simulation draws independently from multiple distributions, while LHS makes draws that cover the parameter space more efficiently and can capture the joint distribution between two or more parameter values (Helton and Davis, 2003). As a result, LHS can reduce the number of draws needed to fully re-create the statistical variance in a model, but the amount of reduction is unknown and may not be universal to all problems (Yang et al., 2013).

With the trip-based model described above, MC and LHS methods were used to develop alternative parameter sets to evaluate uncertainty. To identify a standard deviation for each parameter, a coefficient of variation was used. A set coefficient of variation of 0.10 was used for the four mode choice coefficients and the destination choice parameters. The mode choice constants were kept the same across all iterations. Literature had identified a coefficient of variation of 0.30, but for this analysis that caused an unrealistic value of time, and thus it was changed to be 0.10 (Zhao and Kockelman, 2002). Value of time is a ratio in units of money per time that should be compared to the regional wage rate. Using a c_v of 0.30 the value of time range was from \$2 to \$32 /hr, whereas using a c_v of 0.10 the range was \$6 to \$14 /hr. The latter seemed more rational because it is related to wage rates and thus a c_v of 0.10 was used for our analysis. The standard deviation was equal to 0.10 multiplied by the mean, where the mean values in this situation are the base scenario parameters (as identified in Table 2).

The MC random sampling uses the R function of rnorm. LHS uses the 1hs package in R. Since this package only chooses variables on a zero to one scale, the values given use a function to put the random sampling on the right scale needed for the given parameter. The full code for both methods can be found in a public GitHub repository. One hundred and 600 draws of random samples for both methods are generated. With these generated parameters, the mode choice model step was run for every set of input parameters for each purpose. The average MCLS value for each run was determined to compare each continuous draw. This allowed us to see how many iterations of which sampling type would be sufficient to show a full range of possible outcomes.

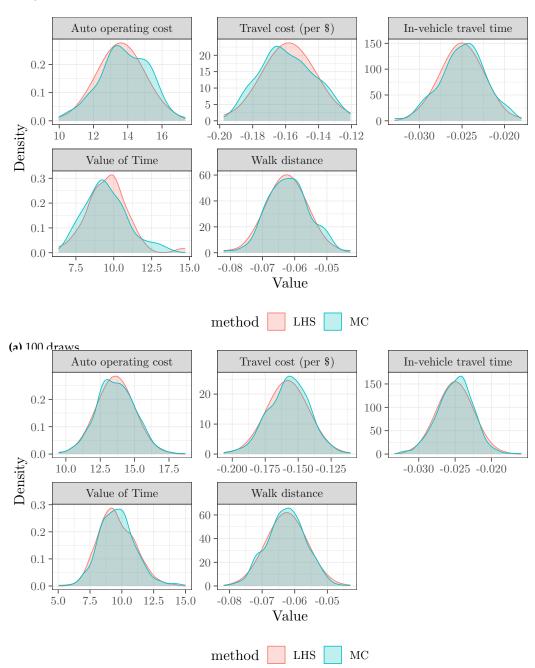
The parameters generated were compared for both sampling methods. Figure 1 shows the distributions for the HBW parameters when using 100 and 600 draws. These distributions show that LHS gives normally distributed parameters with fewer draws than

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MC sampling: at 100 draws LHS shows a nearly perfect normal distribution, where there are some discrepancies for the MC generated parameters. These Figures show that LHS is likely to estimate the full variance of the results with fewer draws.



(b) 600 draws

Figure 1. Sampled mode and destination choice parameters for HBW trip purpose.

To determine if LHS is effective at a reasonable amount of iterations, the cumulative mean and the cumulative standard deviation of the average MCLS value for every zone (see Equation 2) was calculated for each additional draw for both sampling methods. MCLS is an impedance term which is an important value for destination choice and region routing. The average MCLS, x, was used as a measure of outcome possibilities to simplify a complex term as a single value to compare by across all iterations. The cumulative mean is calculated as:

$$\mu_i = \frac{x_1 + \dots + x_i}{n} \tag{5}$$

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and the cumulative standard deviation is calculated as:

$$SD_i = \sqrt{\frac{\sum (x_i - \mu_i)^2}{n - 1}}.$$
(6)

The cumulative mean shows how the average MCLS stabilizes across each iteration, and the cumulative standard deviation is used to show the 95% confidence interval of that mean. When the cumulative mean for the draws stabilizes, that shows that the amount of generated parameters has captured the possible variance of the results. This is shown for two of the three trip purposes in Figure 2.

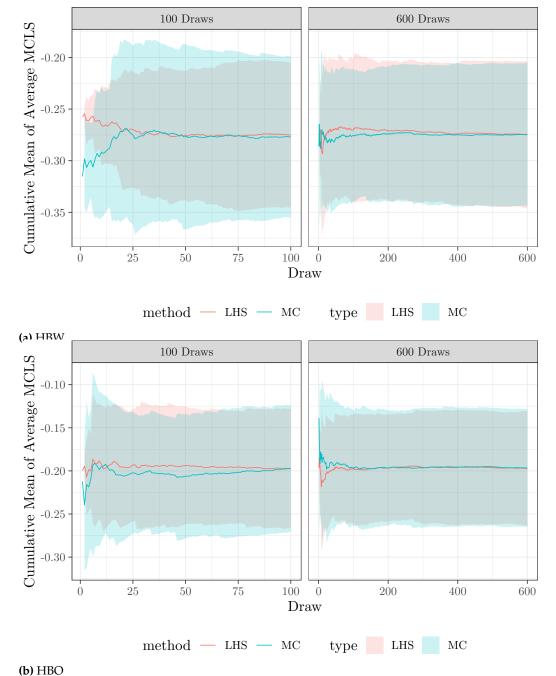


Figure 2. Average mode choice logsum (impedance) cumulative mean and 95% confidence interval with 100 and 600 draws.

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For all three trip purposes, both sampling methods had a stabilized mean by 100 draws. The LHS methods standard deviation ribbon was generally thinner than the MC method. From the narrowed cumulative standard deviation, and that the parameter values are better normally distributed when using LHS, that method of sampling was used for the assignment analysis of the model. Since LHS captures the possible variance at a small enough number of iterations, it can be used for large transportation demand models. From these results it was decided to use 100 LHS samples parameters to evaluate uncertainty within each step of the model. The next chapter includes the results of applying these sampled parameters to the travel demand model.

4. Sensitivity Analysis Results

Each of the 100 LHS parameter draws was applied to the RVTPO model, generating mode choice utilities, destination choice utilities, and trip matrices for each draw. The resulting uncertainty can then be quantified using the outputs from the trip-based model. This section will first look at the uncertainty of trips by mode, and how the mode split changes when the parameters vary. Then uncertainty will be quantified using the highway assigned trips, and how link volume changes across each draw. The results will then be summarized.

4.1. Mode Choice Trips

Uncertainty can be evaluated by looking at how mode choices change. The total number of trips by purpose are fixed, but the number of trips by each mode changes as a result of mode choice, combined with the availability of modes in the travel time skims. Table 3 lists the base trip amount by mode and purpose. It also lists the the average number of trips across all 100 iterations, with the corresponding standard deviation and coefficient of variation. For HBW trips there are 103,320 auto trips. Across all 100 iterations there is a mean value of 103,298 trips with a standard deviation of 527.07. This results in a coefficient of variation of 0.0052 or 0.52% variation in the number of auto trips. The other modes of transportation are included and similar patterns can be seen in HBO and NHB. The results listed in the table show that the variation of the output trips - by mode and purpose - are less than the input variation (as all c_v 's are smaller than 0.10). This confirms previous research that the outcome variance is less than or near the parameters variance (Clay and Johnston, 2005; Zhao and Kockelman, 2002). In all three purposes that were evaluated, the coefficient of variation in auto trips are lower than transit or non-motorized trips, meaning that there is greater confidence in the models accuracy to generate auto trips. The input parameter variability has a smaller effect on auto trips than on trips on the other modes.

Table 3. Coefficient of Variation of Trips by Mode

	Base	Mean	SD	c_v
HBW				
Auto	103320	103298	537.07	0.0052
Non-Motorized	1103	1105	50.38	0.0456
Transit	13254	13274	566.01	0.0426
НВО				
Auto	250489	250475	453.11	0.0018
Non-Motorized	4310	4316	235.24	0.0545
Transit	9276	9283	363.09	0.0391
NHB				
Auto	60212	60209	78.28	0.0013
Non-Motorized	736	737	35.77	0.0485
Transit	1576	1579	74.89	0.0474

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The variation among mode choices can be visualized graphically using a density of a scaled change in trips by mode. Figure 3 shows density plots for HBW trips by mode for 12 zones - the zones are divided into three volume categories: low is less than 200 trips per zone, mid is 200 to 700 trips per zone, and top is greater than 700 trips per zone – and four zones are randomly selected from each volume category. Zones that do not have any transit accessibility have been excluded. Those zones have very high density in auto trips as with the ability to choose transit was removed, the choice to choose auto was more certain. The zones included in Figure 3 all have greater certainty in auto trips, as the change in trips across all 100 iterations is relatively small. This reinforces the previous claim that the model has more confidence in auto trips than the other modes. It is also important to note that the modes are correlated to each other. In zones with a greater confidence in one mode, the other modes are more confident as well. Since the number of trips by origin zone are held constant, when there are an increase in trips on one mode there must be a decrease in trips on one or both of the other modes. Also, the distribution of non-motorized trips is similar for every zone suggesting that generally, the most variable mode is non-motorized trips which you can see in the spread of the graphic. This is also verified using Table 3 as the c_v is largest for the non-motorized mode across all three purposes.

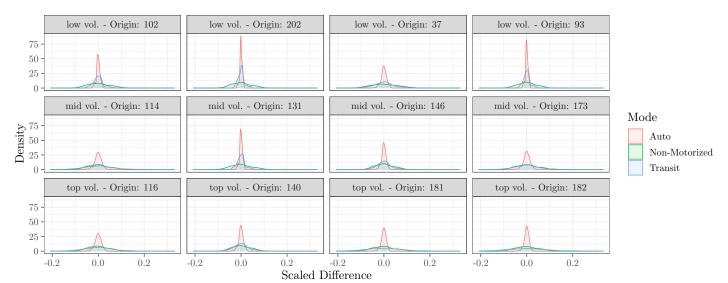


Figure 3. Trip density for coefficient of variation by mode for HBW trips.

4.2. Link Volume

Highway volumes are the most commonly used output of a travel model. Uncertainty can additionally be evaluated by looking at how assigned link volume varies across iterations. Figure 4 displays variation in forecast link volume spatially. This shows that the links with the highest standard deviation in forecast volume are high-volume roads including freeways and principal arterials where the majority of traffic is internal to the study region. Although these links have the largest standard deviation, when compared to the total volume of the road, the variation is in reality very small. A standard deviation of 400 vehicles on a road with 40,000 total vehicles corresponds to a small variation (1%).

The highway assignment results can be grouped by facility type to show how the coefficient of variation compares to link volume. Figure 5 shows the coefficient of variation for the daily volume assigned to each network link, across the 100 draws, plotted against the mean forecast link volume for each link. The values are the volume for 100 randomly sampled links for each facility type. The plots shows that for the high-volume roads such as major arterials and freeways, the coefficient of variation converges to approximately 0.01, or about 1% of the road's total forecast volume. For lower-volume links, the coefficient of variation is more widely distributed, with some local roads and small collectors having considerably higher values. Some links in the model show no variation at all; these are

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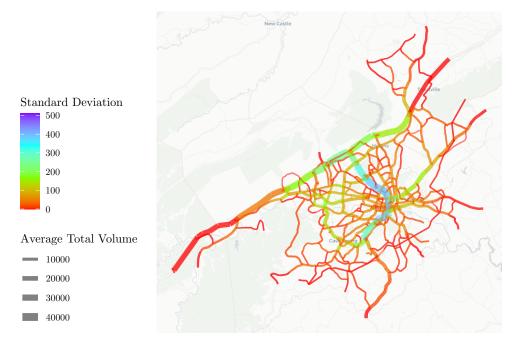


Figure 4. Standard deviation in daily forecast volume.

presumably links near the edges of the model region where the only traffic is to and from external zones, trips which were held constant in this framework.

Variation among a link can also be visualized with a density plot of the total volume across all iterations, as shown in Figure 6. In this plot, the density of forecast volumes in three randomly selected links in each of the freeway, collector, and arterial functional types are plotted alongside the baseline forecast and the Average Annual Weekday Daily Traffic (AAWDT) measured by the Virginia Department of Transportation, and to which the model estimates were calibrated. In all cases, the error or uncertainty in the forecast is considerably narrower than the error inherent in the model construction, as evidenced by the fact that the AAWDT target value is well outside the bell curve created by the statistically varied simulation forecasts.

As expected from using the base parameter values as the mean of the LHS parameter sampling, the base results are at or near the median of the statistical density for each link's volume. But it is notable that the estimated volumes are not perfectly, normally distributed as might be naively expected. In this case, the combined effects of the mode and destination choice parameter sampling appear to be constrained by the geographic specificity of the RVTPO model network: even when the demand for trips changes between zone pairs, the realities of the highway capacity, volume-delay, and static user equilibrium procedures may be limiting the possibilities for forecast highway volumes.

5. Conclusions

In general, this research has shown that statistical parameter uncertainty does not appear to be a significant factor in forecasting traffic volumes using trip-based travel demand models. The result uncertainty is generally equal to or smaller than the input parameter variance. The uncertainty in parameter inputs appears to lead to variation in highway volumes that is lower than the error between the model forecast and the highway counts. Any variation in mode and destination choice probabilities appears to be constrained by the limitations of the highway network assignment.

There are several limitations that must be mentioned in this research, however. First, we did not attempt to address the statistical uncertainty in trip production estimates; these may play a substantially larger role than destination and mode choice parameters, given that lower trip rates may lead to lower traffic volumes globally, which could not be

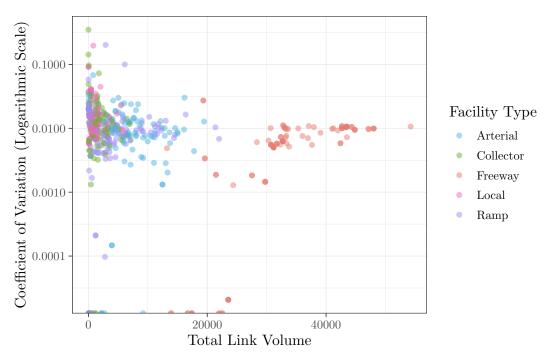


Figure 5. Coefficient of variation in daily link volume by facility type for a random sample of highway links.

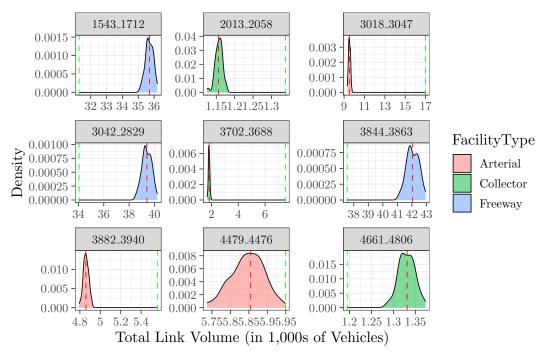


Figure 6. Density plot of forecast volume on selected links, with default parameter results marked in red, and AAWDT values in green.

"corrected" by the static user equilibrium assignment. Additionally, the relatively sparse network of the RVTPO model region — lacking parallel high-capacity highway facilities — may have meant that the static network assignment would converge to a similar solution point regardless of modest changes to the trip matrix. It may be that in a larger network with more path redundancies, the assignment may not have been as helpful in constraining the forecast volumes.

In this research we had only the estimates of the statistical coefficients, and therefore had to assume a coefficient of variation to derive variation in the sampling procedure. It would be better if model user and development documentation more regularly provided estimates of the standard errors of model parameters. Even better would be variance-covariance matrices for the estimated models, enabling researchers to ensure that covariance relationships between sampled parameters are maintained.

Notwithstanding these limitations, statistical parameter variance does not appear to be the largest source of uncertainty in travel forecasting. There are likely more important factors at play that planners and government agencies should address. Research on all sources of uncertainty is somewhat limited, but in many ways has been hampered by the burdensome computational requirements of many modern travel models (Voulgaris, 2019). This research methodology benefited from a lightweight travel model that could be repeatedly re-run with dozens of sampled choice parameters. One strategy for applying this methodology to larger models may be relatively recent TMIP-EMAT exploratory modeling toolkit (Milkovits et al., 2019). But a better understanding the other sources of uncertainty – model specification and input accuracy – might also benefit from lightweight models constructed for transparency and flexibility rather than heavily constrained models emphasizing precise spatial detail and strict behavioral constraints. This might allow forecasts to be made with an ensemble approach (Wu and Levinson, 2021), identifying preferred policies as the consensus of multiple plausible model specifications.

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