EXPLORATION OF PATTERNS FOR USE IN CLASS

1. Fundamental Patterns

2. Definitions

- (1) Singleton: A set with one value.
- (2) Set: A mathematical set. Ex. An undirected graph is a set of edge descriptions.
- (3) Sequence: A mathematical sequence. Ex. A digraph is a sequence of edge descriptions.

3. Functor Pattern

A pattern that allows a generic function to apply a specific function without changing or modifying the generic function.

4. Fold Pattern: set or sequence to singleton

For function f, set or sequence S, and singleton a,

$$fold(f, S, a) = \begin{cases} a & \text{if } S = \emptyset\\ fold(f, S, f(x : x \in S, a)) & \text{otherwise} \end{cases}$$

5. Unfold Pattern: singleton to set or sequence

For function f, and singleton d

$$unfold(f,d) = \begin{cases} \varnothing & \text{if } f(d) = \varnothing \\ f(d) \cup unfold(f,f(d)) & \text{otherwise} \end{cases}$$

6. Derived Patterns

6.1. **Hylomorphism Pattern.** For functions f and g, singleton d, and singleton a,

$$hylo(f,g,d,a) = fold(f,unfold(g,d),a)$$

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6.2. **Map Pattern.** For set or sequence $A = \emptyset$, set or sequence S, and function f, where $f(s: s \in S, A)$ performs some transformation t as well as $\{t(s)\} \cup A$,

$$map(f, S) = fold(f, S, A)$$

6.3. **Filter Pattern.** For set or sequence $A = \emptyset$, set or sequence S, and function f, where $f(s: s \in S, A)$ performs some comparison c and $\{t(s)\} \cup A$ when c(s) = true,

$$filter(f, S) = fold(f, S, A)$$

- 6.4. Monad Pattern.
- 6.5. **Sream Pattern.** unfold pattern derivative (Stream is the same as Lazy Evaluation)