# RadLib: a radiative heat transfer model library for CFD

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# Abstract

Ca. 100 words

Keywords: radiative heat transfer, reacting flows, CFD

# Required Metadata

### Current code version

Ancillary data table required for subversion of the codebase. Kindly replace examples in right column with the correct information about your current code, and leave the left column as it is.

Nr.	Code metadata description	Please fill in this column
C1	Current code version	TODO 2.1
C2	Permanent link to code/repository	github.com/BYUignite/RadLib
	used for this code version	
С3	Code Ocean compute capsule	N/A
C4	Legal Code License	MIT license (MIT)
C5	Code versioning system used	Git
C6	Software code languages, tools, and	C++, Python 3
	services used	
C7	Compilation requirements, operat-	TODO
	ing environments & dependencies	
C8	If available Link to developer docu-	TODO
	mentation/manual	
С9	Support email for questions	davidlignell@byu.edu

Table 1: Code metadata (mandatory)

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#### 1. Motivation and significance

Modeling radiative heat transfer, and particular radiation absorption coefficients, for CFD is complex and challenging. More specifically, combustion simulations are often complicated by the need for accurate radiation modeling, which can be difficult to implement and computationally expensive relative to simulation cost. As a result, researchers typically manufacture configurations in which radiation can be safely ignored, which can lead to results inapplicable to practical systems, or use oversimplified models and assumptions, which can produce inaccurate results. Unfortunately, these approaches are neither rigorous nor applicable to real engineering systems.

In some cases, other modes of heat transfer dominate the system, and radiation can be safely neglected, but many practical engineering systems do not allow this. Simple jet flames, for example, demonstrate both possibilities: early in a flame's development, convection typically dominates heat transfer and dictates flame behavior; late-stage flame phenomena like soot behavior and flame sheet breakthrough, however, increasingly depend on the magnitude of radiative heat losses and cannot be simulated accurately without a radiation model.

Like combustion, the core mechanisms of radiation are physically and mathematically complex. Unlike other modes of heat transfer, it is governed by a set of integro-differential equations that depend on both direction and wavelength. Only the simplest systems have analytic solutions, and most practical systems require a numerical solution. Ray tracing (Monte Carlo) solutions are very accurate but extremely computationally expensive, and often require high-performance computing resources to execute. Modeling assumptions are common and can reduce simulation cost at the expense of accuracy, depending on their validity for the system in question.

Currently, there is no convenient or easy-to-use access point for CFD radiation models. As such, we present RadLib, a modular library of radiation models that can be applied alongside various simulation tools. RadLib focuses on calculation of radiation absorption coefficients, often the most difficult and time-consuming portion of radiation calculations, which permits its use with various solvers. The models are fully implemented and validated and all use a common interface, allowing researchers easy and convenient access to radiation modeling tools regardless of the field of application.

### 36 2. Model descriptions

RadLib includes three models of varying complexity and accuracy to calculate the radiation absorption coefficients and their weighting factors for each gas considered by the model. Radiation absorption coefficients are typically calculated using correlations relating them local properties such as
temperature, total pressure, or species partial pressure, depending on the
model. Correlations come from curve fits to high-resolution radiation property databases. At present, RadLib considers up to four gas species (H<sub>2</sub>O,
CO, CO<sub>2</sub>, and CH<sub>4</sub>) and, optionally, soot volume fraction in its calculation
of absorption coefficients and weighting factors.

Once the radiative absorption coefficients are calculated, they are then used to solve the radiative transfer equation (RTE), which depends on the simulation configuration and assumptions. Solving the RTE is not the focus of this software, but RadLib's example cases do employ a simple implicit trapezoid method solver to calculate the radiative heat flux and volumetric heat source profiles between two parallel planes. [MORE DESCRIPTION OF SOLVER GOES HERE?]

[OTHER THINGS THAT APPLY TO ALL MODELS GO HERE] [MAYBE INCLUDE SOME BASIC INFO ON LBL?]

### 2.1. Planck Mean absorption coefficients

RadLib's simplest model uses Planck Mean absorption coefficients calculated from the correlations given on the TNF Workshop site [1]. The temperature-dependent correlations are based on the RADCAL model in [2]. The TNF radiation model is also documented in [3].

Planck Mean absorption coefficients are commonly used to model radiation, especially in combustion systems, because the model is relatively easy to implement, computationally inexpensive, and reasonably accurate in many cases. The TNF Workshop correlations were developed for use with an optically thin radiation model, which assumes that radiation passes through a medium mostly undisturbed. In cases where the optically thin assumption applies, such as simple hydrogen jet flames, this model and the associated Planck Mean absorption coefficients can produce accurate results [4]. In cases where the optically thin assumption is not reasonable, including many other combustion scenarios, this model does not produce accurate results. For example, it significantly overpredicts radiative losses from the TNF library's CH<sub>4</sub> flames [5, 6, 7].

Because RadLib does not specify case geometry or medium, there is no optically thin assumption inherent in its use of the Planck Mean absorption coefficients. However, the correlations were developed with the intention of use with an optically thin assumption, and, as a result, depend only on local temperature values. RadLib users must take care to consider these limitations before using this model.

## 2.2. Weighted sum of gray gases (WSGG)

The basic assumption of weighted sum of gray gases (WSGG) models in general is that the non-gray behavior of gas mixtures, in this case H<sub>2</sub>O and CO<sub>2</sub>, can be modeled by a weighted sum of several gray gases and one transparent gas (which represents the spectral windows between absorption bands). RadLib uses the WSGG model presented by Bordbar et al. [8, 9], which uses correlations based on the HITEMP 2010 database [10]. RadLib, in accordance with the Bordbar et al. WSGG method cited above, uses a mixture of four gray gases and one transparent gas. Absorption coefficients are calculated by

$$K_i = \sum_{k=0}^{4} d_{i,k} M_r^k,$$
 (1)

where  $K_i$  is the absorption coefficient for species i,  $d_{i,k}$  is a species-specific correlated model coefficient, and  $M_r$  is the molar ratio  $Y_{\rm H_2O}/Y_{\rm CO_2}$ . The weight factors are calculated by

$$a_i = \sum_{j=0}^{4} b_{i,j} T_r^j, \tag{2}$$

where  $a_i$  is the weighting factor for species i and  $T_r$  is a normalized temperature equal to  $T/T_{ref}$  with  $T_{ref}=1200{\rm K}$ . The value of  $b_{i,j}$  is calculated by

$$b_{i,j} = \sum_{k=0}^{4} C_{i,j} M_r^k, \tag{3}$$

where  $C_{i,j}$  is another correlated model coefficient and  $M_r$  is the molar ratio  $Y_{\rm H_2O}/Y_{\rm CO_2}$  as above. The model coefficients  $d_{i,k}$  and  $C_{i,j}$  can be found in the literature [8, 9]. RadLib uses the updated model coefficients from [9], which extends the model presented in [8] to include all possible values of the  $H_2O\text{-}CO_2$  molar ratio.

### 2.3. Rank Correlated SLW (RCSLW)

The Spectral Line Weighted-sum-of-gray gases (SLW) model represents a family of global approaches to radiative heat transfer in high-temperature gases that also includes Absorption Distribution Function (ADF) and Full Spectrum k-distribution (FSK) models, all of which are based on the same fundamental principle in modeling the gas absorption spectrum [11]. In order to extend their spectral models from uniform conditions (isothermal, homogeneous gases) to nonuniform conditions (non-isothermal, non-homogeneous gases), these models take a reference approach in which local gas states are

corrected relative to a reference state. Reference approaches, however, generally lack consistent reference states and can yield significant errors in cases with large spatial temperature gradients [12]. The Rank Correlated SLW (RCSLW) model is a unique extension of the generalized SLW model that does not require a specified gas reference state and preserves the emission term of the spectrally integrated RTE. Recent comparison of advanced SLW modeling approaches revealed that "the Rank Correlated SLW model is the most robust of all models, and demonstrates that it can achieve accurate solutions with as few as 3–5 gray gases" [13]. A brief overview of the general SLW and RCSLW models will be given here; detailed discussion can be found in the literature [14, 15, 16, 17, 18, 11, 12, 19].

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The radiative transfer equation (RTE) for an absorbing, emitting, and non-scattering medium along a given path length s in a direction  $\hat{\Omega}$  is given by

$$\frac{dI_{\eta}}{ds} = -\kappa_{\eta} I_{\eta} + \kappa_{\eta} I_{b\eta},\tag{4}$$

where  $I_{\eta}$  is the radiative spectral intensity,  $I_{b\eta}$  is the Planck spectral distribution of blackbody intensity, and  $\kappa_{\eta}$  is the spectral absorption coefficient of the medium. Integrating with respect to wavenumber and subdividing the absorption cross-section into gray gases gives the SLW form of the RTE:

$$\frac{dI_j}{ds} = -\kappa_j I_j + a_j \kappa_j I_b, \qquad j = 0, 1, ..., n.$$
(5)

Here, n is the number of gray gases in the model and  $I_j$  is the intensity of 126 gray gas j.  $\kappa_j$  is the gray gas absorption coefficient, which can be calcu-127 lated as  $\kappa_j = N\sqrt{C_{j-1}C_j}$ , where  $C_{j-1}$  and  $C_j$  are supplemental absorption cross-sections used to discretize the absorption spectrum [15]. gray gas weights corresponding to each absorption coefficient are given by 130  $a_i = F(C_i) - F(C_{i-1})$ , where  $F(C_i)$  is the absorption line blackbody distri-131 bution function (ALBDF) for species j, calculated from the detailed absorp-132 tion spectrum of that species. The absorption cross-sections are chosen with 133 respect to a thermodynamic reference state, which makes generalized SLW 134 methods reference approaches. Once Equation 5 is solved for each gray gas 135 species, to total radiative intensity I can be calculated by summing the gray 136 gas intensities: 137

$$I = \int_{\eta=0}^{\infty} I_{\eta} d\eta = \sum_{j=1}^{n} I_{j}.$$
 (6)

The Rank-Correlated SLW (RCSLW) model avoids specifying a reference state by relating thermodynamic states to one another instead. If two arbitrary absorption cross-sections define identical wavenumber intervals, the

two cross-sections (neither of which is designated a reference cross-section) can be said to be rank-correlated. The inverse ALBDF, defined such that  $C[F(C,\phi_g,T_b),\phi_g,T_b]=C$  and  $F[C(F,\phi_g,T_b),\phi_g,T_b]=F$  for a given gas thermodynamic state  $\phi_q$  and blackbody temperature  $T_b$ , is proven to have this property and can also be called the rank-correlated reordered absorption cross-sections [12]. As a result, the inverse ALBDF can be used to construct cross-section intervals for the RCSLW model that do not rely on a defined reference state or spectrum. RadLib's RCSLW model uses Method 1.2.2 as defined and recommended in [12] 

#### 3. Software Description

RadLib is an object-oriented C++ class library that includes both C++ and Python interfaces. The RadLib package contains five subdirectories (upon initial download): source contains the RadLib source code; build contains installation files; examples contains instructive example cases, including a simple interface and solver for a parallel planes geometry; data contains ALBDF data tables required for the RCSLW model; and docs contains files used to generate code documentation with Doxygen (optional).

The source and examples directories are further divided into C++ and Python subdirectories to differentiate between interfaces. There are three interface options for using this code: C++, Python, and Cython-wrapped Python. C++ interfaces are located within the examples/c++ folder, while Python interfaces are located within the examples/python folder. When running examples with Python, the Cython-wrapped version is the default; to run the regular Python version without the Cython wrapper, edit the comments near the top of the example files (i.e ex\_S1.py). The C++ interface produces the fastest-running code, followed by the Cython-wrapped Python interface and then the regular Python interface. [INSERT RUNTIME COMPARISONS HERE]

RadLib installation is automated with CMake. First, navigate to the radlib/build directory. If the user requires an installation location other than the default radlib/installed directory, edit the user\_config file before running CMake. To compile the package, run the command cmake -C user\_config ../source. Upon successful completion, run make and then make install to complete the process. The generated C++ library file is located at radlib/installled/lib/libradlib.a.

Figure 1 illustrates the basic structure use of the RadLib package within a generic example using the provided interfaces. The RadLib library generates absorption coefficients and their weighting factors for use within the appropriate RTE, but does not specify any particular geometry, making it

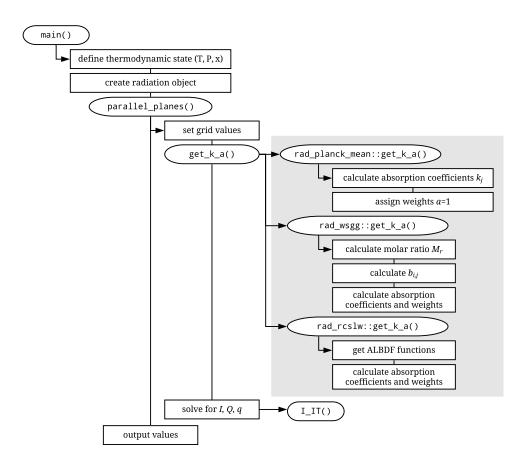


Figure 1: Example workflow diagram. Highlighted areas are part of the RadLib library; other areas represent example infrastructure for using the package.

a versatile tool for any simulation that requires radiative heat transfer, regardless of configuration. The interfaces, solver, and examples included with the library serve to illustrate its use and validate the implementation and results.

# 4. Illustrative Examples

Several examples are presented to illustrate the behavior of the models. The examples show heat flux q or volumetric heat source Q one one-dimensional configurations with varying gas compositions and temperatures. We compare the PM, WSGG, and RCSLW models for each example. The examples are taken from those presented by Solvojov et al., (2017) [12], and

Example	T(K)	$y_{H2O} y_{CO2}$ (mole frac.)	L (m)	$T_{walls}$ (K)
S1	T(x < 0.5) = 2000; T(x > 0.5) = 300	$y_{CO2} = 0.1, y_{H2O} = 0.2$	0.5 - 2.5	cold, cold
S2	T=1000	$y_{CO2}(x < 0.5) = 0.4, y_{CO2}(x > 0.5) = 0.1$	0.5 - 2.5	cold, cold
S3	$T(x) = 4000x(L - x)/L^2 + 800$	$y_{H2O} = 0.0$ $y_{H2O}(x) = 0.8x(L-x)/L^2 + 0.12$	1	800, 800
S4	middle third triangular to 2500	$y_{CO2} = 0$ $y_{H2O} = 0.1, y_{CO2} = 0$	0.3	500, 500
S5	$T(x) = 1000 + 500\cos(\pi x/L)$	$y_{H2O} = 0.1, y_{CO2} = 0$	2	1500, 500
В3	$T(x) = 400 + 1400\sin(\pi x/L)^2$	$y_{H2O}(x) = 0.0001 + 0.9999 \sin(\pi x/L)^2$	1	400, 400
		$y_{CO2} = 1 - y_{H2O}$		

Table 2: Summary of example cases presented. S1-S5 are from [12]; B3 is from [9]. All cases have P = 1 atm, black walls.

Bordbar et al., 2020 [9]; the number corresponds to the example in the respective referece. A ray-tracing code is used to solve the radiative transport equation between two parallel plates. Table 2 summarizes the cases. Example S1 is a hot slab next to a cold slab where the cold thickness varies; Example S2 is similar but isothermal with a *thick* slab of high CO<sub>2</sub> next to a *thin* slab of low CO<sub>2</sub> of varying thickness; Example S3 has parabolic temperature and H<sub>2</sub>O profiles; Example S4 has a triangular temperature profile between equally-spaced isothermal regions; Example S5 is a half-sinusoid decreasing in temperature from 1500 to 500 K; and Example B3 has symmetric temperature and H<sub>2</sub>O profiles with central peaks of 1800 K and 1, respectively (with  $y_{CO2} = 1 - y_{H2O}$ ). In each case, comparison is made to the line-by-line (LBL) data presented in the references.

The examples are provided with the radlib code and implemented in both C++ and Python. A Juptyer notebook is provided with the Python examples that runs the examples, displays the plots, and saves the plots to PDF files. Python and Cython versions of the one-dimensional solver parallel\_planes are provided for convenience.

These examples are not meant to be exhaustive, and details about the motivation of these examples and the behavior of the specific models is to be found in the respective references. The cases presented are intended to illustrate the use of the radiative library. While not shown for brevity, the implemented WSGG and RCSLW models give essentially identical results to those presented in [12, 9], so that these examples also serve as a validation of the implementation of the models.

Figure 2 shows comparative results for the different radiation models for these cases. In general, the PM model performs poorly compared to the WSSGG and RCSLW models. A notable exception is Example S4. In Example S2, the PM  $q(L)/\sigma T^4$  is off scale at an essentially constant at a value of unity. The PM absorption coefficient is 27.4 atm<sup>-1</sup>m<sup>-1</sup>, giving optical thicknesses of 0.09 and 0.36 m in the thick and thin layers, respectively, which

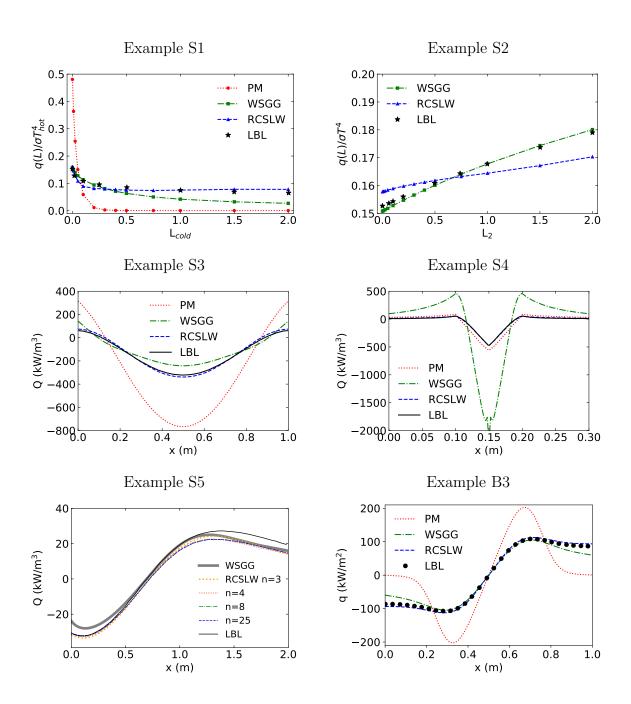


Figure 2: Results for examples summarized in Table 2.

are relatively small compared to the isothermal domain size greater than 0.5 m. Example S5 omits the PM model to more clealy show the behavior of the WSGG and RCSLW models. For that example, the PM values follow the shape of the other curves but Q varies from around -80 at x=0 to a peak of 200 at x=1.5 m, and dropping to 100 kW/m<sup>3</sup> at x=2 m. In all examples, four gray (n = 4) and one clear gas are computed for the RCSLW models to give a consistent comparison to the WSGG model. Example S5 shows the sensitivity of the RCSLW model to the number of gases used. When n is increased to eight the RCSLW model improves to show nearly perfect agreement with the LBL data in Example S2. In all Examples, the RCSLW model is initialized using the mean temperature and composition on the domain. In Example S5, the RCSLW model converges to the LBL solution when the model is initialized using the maximum temperature instead of the average temperature. 

# 5. Impact

As far as I'm aware, there isn't an easy way to incorporate radiative heat transfer into a CFD simulation. Most cases use optically thin assumption (which works in some cases, but not in others) or neglect radiation entirely (also applicable sometimes, but not always). [Refer to TNF website radiation page here.] Unfortunately, this means that when you simulation some configuration in which radiation might be important to the overall heat transfer, you won't get accurate simulation results. Furthermore, if your study is about something else entirely, your radiation model (or lack thereof) becomes a source of error that may be very difficult to separate from other sources of error in your simulation study (i.e. soot modeling studies). As of right now, if you want any detailed radiation treatment, you have to code it yourself, which is difficult and requires external validation.

RadLib can make researchers' lives easier by providing a library of prevalidated radiation models that can be switched out with no difficulty. Additional models can be added easily using the provided modular framework. Researchers can even use Radlib as a tool for comparing models. No need to code multiple different complex radiation models yourself just to decide which one works best for your simulation. And no need to puzzle through the literature to figure our which model(s) might be best for your simulation, either; instead, you can test them yourself. It saves tons of time and effort that researchers can now put toward results rather than code or model development.

By putting all these models side by side in a modular framework, RadLib also provides a structure on which new or altered radiation models can be tested against existing ones. Maybe more comparative studies can be done, especially for more complex simulation cases. We plan to add radiation models as appropriate to RadLib, too.

RadLib opens up new horizons for CFD simulations, especially in combustion cases. It is designed such that it can be easily incorporated into existing research codes. Our group plans to use it with ODT [CITE OTHER SOFT-WAREX PAPER HERE?] alongside soot model library (in development) to study late-flame phenomena such as soot oxidation, flame extinction, and soot-flame breakthrough. These topics in particular are difficult because they require accurate simulation data over a relatively long computational time in addition to good models for both soot chemistry (which is an active research area) and radiation heat transfer (which is the difficult part that RadLib can solve). Using RadLib for such studies allows us to separate and quantify sources of error that may occur due to various models, which is super difficult if you only have one model to work with or it hasn't been validated well.

RadLib can also be used outside of combustion CFD research for anything involving radiative heat transfer. Potential research areas that could benefit include atmospheric and climate sciences, interstellar phenomena, improving efficiency of energy-producing processes, safety in chemical plant design, etc. We aren't experts in these areas, but radiative heat transfer is a universal phenomena that applies to any system or process that involves heat transfer.

This software has not been used outside of the current research group, and it is not used in any commercial settings at this time.

#### 283 6. Conclusions

Set out the conclusion of this original software publication.

#### <sup>285</sup> 7. Conflict of Interest

We wish to confirm that there are no known conflicts of interest associated with this publication and there has been no significant financial support for this work that could have influenced its outcome.

#### 289 Acknowledgements

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### 370 Current executable software version

Ancillary data table required for sub version of the executable software: (x.1, x.2 etc.) kindly replace examples in right column with the correct information about your executables, and leave the left column as it is.

Nr.	(Executable) software meta-	Please fill in this column
	data description	
S1	Current software version	TODO 2.1
S2	Permanent link to executables of	TODO For example: https:
	this version	//github.com/combogenomics/
		DuctApe/releases/tag/DuctApe -
		0.16.4
S3	Legal Software License	MIT license (MIT)
S4	Computing platforms/Operating	Linux, OS X, Microsoft Windows
	Systems	
S5	Installation requirements & depen-	TODO
	dencies	
S6	If available, link to user manual - if	TODO For example: $http$ :
	formally published include a refer-	//mozart.github.io/documentation/
	ence to the publication in the refer-	
	ence list	
S7	Support email for questions	davidlignell@byu.edu

Table 3: Software metadata (optional)