

RadLib: a radiative heat transfer model library for CFD

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Abstract

Ca. 100 words

Keywords: radiative heat transfer, reacting flows, CFD

Required Metadata

Current code version

Ancillary data table required for subversion of the codebase. Kindly replace examples in right column with the correct information about your current code, and leave the left column as it is.

Nr.	Code metadata description	Please fill in this column
C1	Current code version	TODO 2.1
C2	Permanent link to code/repository used for this code version	<i>github.com/BYUignite/RadLib</i>
C3	Code Ocean compute capsule	N/A
C4	Legal Code License	MIT license (MIT)
C5	Code versioning system used	Git
C6	Software code languages, tools, and services used	C++, Python 3
C7	Compilation requirements, operating environments & dependencies	Python 3, Cython
C8	If available Link to developer documentation/manual	TODO
C9	Support email for questions	davidlignell@byu.edu

Table 1: Code metadata (mandatory)

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1. Motivation and significance

Modeling radiative heat transfer, and particular radiation absorption coefficients, for CFD is complex and challenging. More specifically, combustion simulations, which can require many complex property models already, are often complicated by the need for accurate radiation modeling, which can be difficult to implement and computationally expensive relative to simulation cost. This can lead to simulations that use oversimplified radiation models, but in cases where radiation is significant relative to the other physical phenomena, oversimplified models can negatively impact the accuracy of simulation results. In some cases, radiative gains or losses are small compared to other sources, sinks, or modes of heat transfer, and radiation can be safely neglected, but many practical engineering systems do not allow this. For example, simple jet flames demonstrate both possibilities: early in a flame’s development, turbulent mixing typically dominates heat transfer and dictates flame behavior; late-stage flame phenomena like soot behavior and flame sheet breakthrough, however, increasingly depend on the magnitude of radiative heat losses and are difficult to simulate accurately without a robust radiation model. These problems motivated development of the RadLib library, which provides a framework and uniform interface for radiation property models and implements three powerful models in C++ and Python, giving researchers easier and more convenient access to advanced radiation property models and a consistent framework for further model development.

The core mechanisms of radiative phenomena are physically and mathematically complex. Unlike other modes of heat transfer, radiation is governed by a set of integro-differential equations that depend on both direction and wavelength, known as the radiative transfer equations (RTE). Solving the RTE for a given system also requires information about the radiative properties of the materials and media involved, typically radiation absorption coefficients. Depending on the model, absorption coefficients can be dependent on a number of local system properties such as temperature, pressure, and gas composition. As a result, computational radiation solvers require two parts: first, a solution approach for the radiative transfer equations (RTE); and second, a radiation property model. RadLib addresses the second part by providing a set of implemented and validated radiation property models that can be applied to various solution approaches for the RTE.

With RadLib, we provide a convenient, easy-to-use access point for radiative property models that can be interfaced with various RTE solution approaches suitable for CFD applications. RadLib is a modular C++ library with an optional Python interface used to compute the radiation properties

of participating media, often the most difficult and time-consuming portion of radiation calculations. RadLib’s current focus is calculating radiation absorption coefficients and weighting factors for use in global radiation models, but the flexible framework permits expansion to other radiative properties. Three models are fully implemented and validated and all use a common interface, allowing researchers easy and convenient access to radiation modeling tools regardless of the field of application.

2. Model descriptions

RadLib includes three models of varying complexity and accuracy to calculate the radiation absorption coefficients and their weighting factors for each gas considered by the model. Radiation absorption coefficients are typically calculated using correlations relating them local properties such as temperature, total pressure, or species partial pressure, depending on the model. Correlations come from curve fits to high-resolution radiation property databases. At present, RadLib considers up to four gas species (H_2O , CO , CO_2 , and CH_4) and, optionally, soot volume fraction in its calculation of absorption coefficients and weighting factors.

Once the radiative absorption coefficients are calculated, they are then used to solve the radiative transfer equation (RTE), which depends on the simulation configuration and assumptions. Solving the RTE is not the focus of this software, but RadLib’s example cases do employ a simple implicit trapezoid method solver to calculate the radiative heat flux and volumetric heat source profiles between two parallel planes. [MORE DESCRIPTION OF SOLVER GOES HERE?]

[OTHER THINGS THAT APPLY TO ALL MODELS GO HERE]

[MAYBE INCLUDE SOME BASIC INFO ON LBL?]

2.1. Planck Mean absorption coefficients

RadLib’s simplest model uses Planck Mean absorption coefficients calculated from the correlations given on the TNF Workshop site [1]. The temperature-dependent correlations are based on the RADCAL model in [2]. The TNF radiation model is also documented in [3].

Planck Mean absorption coefficients are commonly used to model radiation, especially in combustion systems, because the model is relatively easy to implement, computationally inexpensive, and reasonably accurate in many cases. The TNF Workshop correlations were developed for use with an optically thin radiation model, which assumes that radiation passes through a medium mostly undisturbed. In cases where the optically thin assumption applies, such as simple hydrogen jet flames, this model and the associated

79 Planck Mean absorption coefficients can produce accurate results [4]. In cases
80 where the optically thin assumption is not reasonable, including many other
81 combustion scenarios, this model does not produce accurate results. For ex-
82 ample, it significantly overpredicts radiative losses from the TNF library’s
83 CH₄ flames [5, 6, 7].

84 Because RadLib does not specify case geometry or medium, there is no
85 optically thin assumption inherent in its use of the Planck Mean absorption
86 coefficients. However, the correlations were developed with the intention
87 of use with an optically thin assumption, and, as a result, depend only on
88 local temperature values. RadLib users must take care to consider these
89 limitations before using this model.

90 2.2. Weighted sum of gray gases (WSGG)

91 The basic assumption of weighted sum of gray gases (WSGG) models
92 in general is that the non-gray behavior of gas mixtures, in this case H₂O
93 and CO₂, can be modeled by a weighted sum of several gray gases and one
94 transparent gas (which represents the spectral windows between absorption
95 bands). RadLib uses the WSGG model presented by Bordbar et al. [8, 9],
96 which uses correlations based on the HITEMP 2010 database [10]. RadLib,
97 in accordance with the Bordbar et al. WSGG method cited above, uses a
98 mixture of four gray gases and one transparent gas. Absorption coefficients
99 are calculated by

$$K_i = \sum_{k=0}^4 d_{i,k} M_r^k, \quad (1)$$

100 where K_i is the absorption coefficient for species i , $d_{i,k}$ is a species-specific
101 correlated model coefficient, and M_r is the molar ratio $Y_{\text{H}_2\text{O}}/Y_{\text{CO}_2}$. The
102 weight factors are calculated by

$$a_i = \sum_{j=0}^4 b_{i,j} T_r^j, \quad (2)$$

103 where a_i is the weighting factor for species i and T_r is a normalized tem-
104 perature equal to T/T_{ref} with $T_{ref} = 1200\text{K}$. The value of $b_{i,j}$ is calculated
105 by

$$b_{i,j} = \sum_{k=0}^4 C_{i,j} M_r^k, \quad (3)$$

106 where $C_{i,j}$ is another correlated model coefficient and M_r is the molar ratio
107 $Y_{\text{H}_2\text{O}}/Y_{\text{CO}_2}$ as above. The model coefficients $d_{i,k}$ and $C_{i,j}$ can be found in
108 the literature [8, 9]. RadLib uses the updated model coefficients from [9],

109 which extends the model presented in [8] to include all possible values of the
 110 H₂O-CO₂ molar ratio.

111 2.3. Rank Correlated SLW (RCSLW)

112 The Spectral Line Weighted-sum-of-gray gases (SLW) model represents
 113 a family of global approaches to radiative heat transfer in high-temperature
 114 gases that also includes Absorption Distribution Function (ADF) and Full
 115 Spectrum k -distribution (FSK) models, all of which are based on the same
 116 fundamental principle in modeling the gas absorption spectrum [11]. In order
 117 to extend their spectral models from uniform conditions (isothermal, homo-
 118 geneous gases) to nonuniform conditions (non-isothermal, non-homogeneous
 119 gases), these models take a reference approach in which local gas states are
 120 corrected relative to a reference state. Reference approaches, however, gen-
 121 erally lack consistent reference states and can yield significant errors in cases
 122 with large spatial temperature gradients [12]. The Rank Correlated SLW
 123 (RCSLW) model is a unique extension of the generalized SLW model that
 124 does not require a specified gas reference state and preserves the emission
 125 term of the spectrally integrated RTE. Recent comparison of advanced SLW
 126 modeling approaches revealed that "the Rank Correlated SLW model is the
 127 most robust of all models, and demonstrates that it can achieve accurate
 128 solutions with as few as 3–5 gray gases" [13]. A brief overview of the general
 129 SLW and RCSLW models will be given here; detailed discussion can be found
 130 in the literature [14, 15, 16, 17, 18, 11, 12, 19].

131 The radiative transfer equation (RTE) for an absorbing, emitting, and
 132 non-scattering medium along a given path length s in a direction $\hat{\Omega}$ is given
 133 by

$$\frac{dI_{\eta}}{ds} = -\kappa_{\eta}I_{\eta} + \kappa_{\eta}I_{b\eta}, \quad (4)$$

134 where I_{η} is the radiative spectral intensity, $I_{b\eta}$ is the Planck spectral distri-
 135 bution of blackbody intensity, and κ_{η} is the spectral absorption coefficient of
 136 the medium. Integrating with respect to wavenumber and subdividing the
 137 absorption cross-section into gray gases gives the SLW form of the RTE:

$$\frac{dI_j}{ds} = -\kappa_j I_j + a_j \kappa_j I_b, \quad j = 0, 1, \dots, n. \quad (5)$$

138 Here, n is the number of gray gases in the model and I_j is the intensity of
 139 gray gas j . κ_j is the gray gas absorption coefficient, which can be calcu-
 140 lated as $\kappa_j = N\sqrt{C_{j-1}C_j}$, where C_{j-1} and C_j are supplemental absorp-
 141 tion cross-sections used to discretize the absorption spectrum [15]. The
 142 gray gas weights corresponding to each absorption coefficient are given by

143 $a_j = F(C_j) - F(C_{j-1})$, where $F(C_j)$ is the absorption line blackbody distri-
 144 bution function (ALBDF) for species j , calculated from the detailed absorp-
 145 tion spectrum of that species. The absorption cross-sections are chosen with
 146 respect to a thermodynamic reference state, which makes generalized SLW
 147 methods reference approaches. Once Equation 5 is solved for each gray gas
 148 species, to total radiative intensity I can be calculated by summing the gray
 149 gas intensities:

$$I = \int_{\eta=0}^{\infty} I_{\eta} d\eta = \sum_{j=1}^n I_j. \quad (6)$$

150 The Rank-Correlated SLW (RCSLW) model avoids specifying a reference
 151 state by relating thermodynamic states to one another instead. If two ar-
 152 bitrary absorption cross-sections define identical wavenumber intervals, the
 153 two cross-sections (neither of which is designated a reference cross-section)
 154 can be said to be rank-correlated. The inverse ALBDF, defined such that
 155 $C[F(C, \phi_g, T_b), \phi_g, T_b] = C$ and $F[C(F, \phi_g, T_b), \phi_g, T_b] = F$ for a given gas
 156 thermodynamic state ϕ_g and blackbody temperature T_b , is proven to have
 157 this property and can also be called the rank-correlated reordered absorption
 158 cross-sections [12]. As a result, the inverse ALBDF can be used to construct
 159 cross-section intervals for the RCSLW model that do not rely on a defined
 160 reference state or spectrum. RadLib’s RCSLW model uses Method 1.2.2 as
 161 defined and recommended in [12]

162 3. Software Description

163 RadLib is an object-oriented C++ class library that includes both C++
 164 and Python interfaces. The RadLib package contains five subdirectories
 165 (upon initial download): **source** contains the RadLib source code; **build**
 166 contains installation files; **examples** contains instructive example cases, in-
 167 cluding a simple interface and solver for a parallel planes geometry; **data**
 168 contains ALBDF data tables required for the RCSLW model; and **docs** con-
 169 tains files used to generate code documentation with Doxygen (optional).

170 The **source** and **examples** directories are further divided into C++ and
 171 Python subdirectories to differentiate between interfaces. There are three
 172 interface options for using this code: C++, Python, and Cython-wrapped
 173 Python. C++ interfaces are located within the **examples/c++** folder, while
 174 Python interfaces are located within the **examples/python** folder. When
 175 running examples with Python, the Cython-wrapped version is the default;
 176 to run the regular Python version without the Cython wrapper, edit the com-
 177 ments near the top of the example files (i.e **ex.S1.py**). The C++ interface
 178 produces the fastest-running code, followed by the Cython-wrapped Python

179 interface and then the regular Python interface. [INSERT RUNTIME COM-
180 PARISONS HERE]

181 RadLib installation is automated with CMake. First, navigate to the
182 `radlib/build` directory. If the user requires an installation location other
183 than the default `radlib/installed` directory, edit the `user_config` file be-
184 fore running CMake. To compile the package, run the command `cmake -C`
185 `user_config ../source`. Upon successful completion, run `make` and then
186 `make install` to complete the process. The generated C++ library file is
187 located at `radlib/installed/lib/libradlib.a`.

188 Figure 1 illustrates the basic structure use of the RadLib package within
189 a generic example using the provided interfaces. The RadLib library gen-
190 erates absorption coefficients and their weighting factors for use within the
191 appropriate RTE, but does not specify any particular geometry, making it
192 a versatile tool for any simulation that requires radiative heat transfer, re-
193 gardless of configuration. The interfaces, solver, and examples included with
194 the library serve to illustrate its use and validate the implementation and
195 results.

196 4. Illustrative Examples

197 Several examples are presented to illustrate the behavior of the models.
198 The examples show heat flux q or volumetric heat source Q in one one-
199 dimensional configurations with varying gas compositions and temperatures.
200 We compare the PM, WSGG, and RCSLW models for each example. The
201 examples correspond to those presented by Solvojev et al. (S) [12] and Bor-
202 dbar et al. (B) [9], and the number of each example corresponds to the
203 example number in the respective reference. A ray-tracing code is used to
204 solve the radiative transport equation between two parallel plates. Table 2
205 summarizes the cases. Example S1 is a hot slab next to a cold slab where
206 the cold slab's thickness varies; Example S2 is isothermal with a thick slab
207 of high CO_2 next to a thin slab of low CO_2 with variable thickness; Exam-
208 ple S3 uses parabolic temperature and H_2O mole fraction profiles; Example
209 S4 has a triangular temperature profile between equally-spaced isothermal
210 regions; Example S5 uses a half-sinusoid temperature profile that decreases
211 from 1500 to 500 K; and Example B3 has symmetric temperature and H_2O
212 mole fraction profiles with central peaks of 1800 K and 1, respectively (with
213 $y_{\text{CO}_2} = 1 - y_{\text{H}_2\text{O}}$). Each case is presented alongside the line-by-line (LBL)
214 data presented in the references.

215 The examples are provided with the RadLib code and implemented in
216 both C++ and Python. A Jupyter notebook is provided with the Python
217 examples that runs the examples, displays the plots, and saves the plots

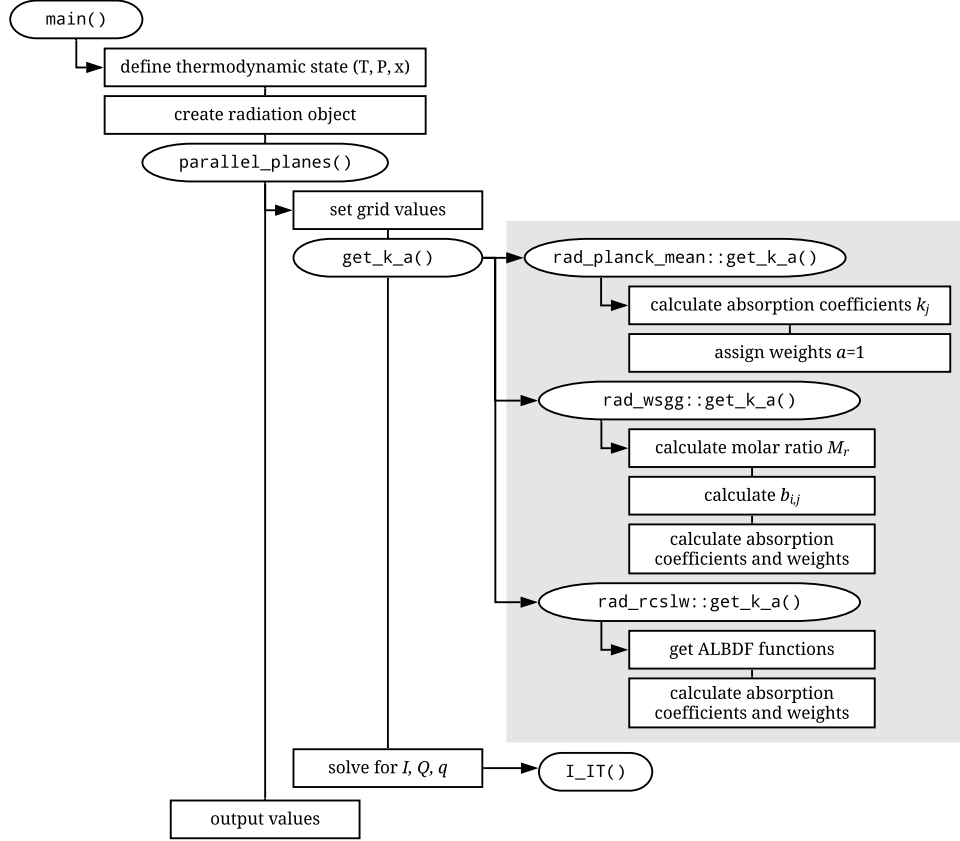


Figure 1: Example workflow diagram. Highlighted areas are part of the RadLib library; other areas represent example infrastructure for using the package.

Example	T(K)	y_{H_2O} y_{CO_2} (mole frac.)	L (m)	T_{walls} (K)
S1	$T(x < 0.5) = 2000; T(x > 0.5) = 300$	$y_{CO_2} = 0.1, y_{H_2O} = 0.2$	0.5-2.5	cold, cold
S2	T=1000	$y_{CO_2}(x < 0.5) = 0.4, y_{CO_2}(x > 0.5) = 0.1$	0.5-2.5	cold, cold
S3	$T(x) = 4000x(L - x)/L^2 + 800$	$y_{H_2O} = 0$ $y_{H_2O}(x) = 0.8x(L - x)/L^2 + 0.12$ $y_{CO_2} = 0$	1	800, 800
S4	middle third triangular to 2500	$y_{H_2O} = 0.1, y_{CO_2} = 0$	0.3	500, 500
S5	$T(x) = 1000 + 500 \cos(\pi x/L)$	$y_{H_2O} = 0.1, y_{CO_2} = 0$	2	1500, 500
B3	$T(x) = 400 + 1400 \sin(\pi x/L)^2$	$y_{H_2O}(x) = 0.0001 + 0.9999 \sin(\pi x/L)^2$ $y_{CO_2} = 1 - y_{H_2O}$	1	400, 400

Table 2: Summary of example cases presented. S1-S5 are from [12]; B3 is from [9]. All cases use $P = 1$ atm and black walls.

218 to PDF files. Python and Cython versions of the one-dimensional solver
219 `parallel_planes.py` are provided for convenience.

220 These cases are intended to illustrate the use of the RadLib library and
221 are not exhaustive. Details about these examples and their motivations can
222 be found in their respective references. While omitted here for brevity, the
223 implemented WSGG and RCSLW models give essentially identical results to
224 those presented in [12, 9] such that these examples also serve as a validation
225 of the implementation of the models.

226 Figure 2 shows comparative results for the different radiation models
227 for these cases. In general, the PM model performs poorly compared to
228 the WSSGG and RCSLW models. A notable exception is Example S4. In
229 Example S2, the PM $q(L)/\sigma T^4$ is off scale at an essentially constant at a value
230 of unity. The PM absorption coefficient is $27.4 \text{ atm}^{-1}\text{m}^{-1}$, giving optical
231 thicknesses of 0.09 and 0.36 m in the thick and thin layers, respectively, which
232 are relatively small compared to the isothermal domain size greater than 0.5
233 m. Example S5 omits the PM model to more clearly show the behavior of
234 the WSGG and RCSLW models. For that example, the PM values follow the
235 shape of the other curves but Q varies from around -80 at $x = 0$ to a peak of
236 200 at $x=1.5$ m, and dropping to 100 kW/m^3 at $x = 2$ m. In all examples,
237 four gray ($n = 4$) and one clear gas are computed for the RCSLW models
238 to give a consistent comparison to the WSGG model. Example S5 shows
239 the sensitivity of the RCSLW model to the number of gases used. When
240 n is increased to eight the RCSLW model improves to show nearly perfect
241 agreement with the LBL data in Example S2. In all Examples, the RCSLW
242 model is initialized using the mean temperature and composition on the
243 domain. In Example S5, the RCSLW model converges to the LBL solution
244 when the model is initialized using the maximum temperature instead of the
245 average temperature.

246 5. Impact

247 Radiative heat transfer models are historically difficult to implement in
248 CFD codes due to their complexity and high computational costs. Neglecting
249 radiation or using simple models like the optically thin assumption is ade-
250 quate for some cases with simple geometry or limited chemical reactions, but
251 most simulations of interest to engineers and researchers require more ad-
252 vanced radiation modeling to yield accurate results. In such cases, radiation
253 models that are incorrectly implemented or inappropriate for the simulation
254 parameters can become additional sources of error that may be extremely dif-
255 ficult to separate from existing sources or error. Currently, researchers that

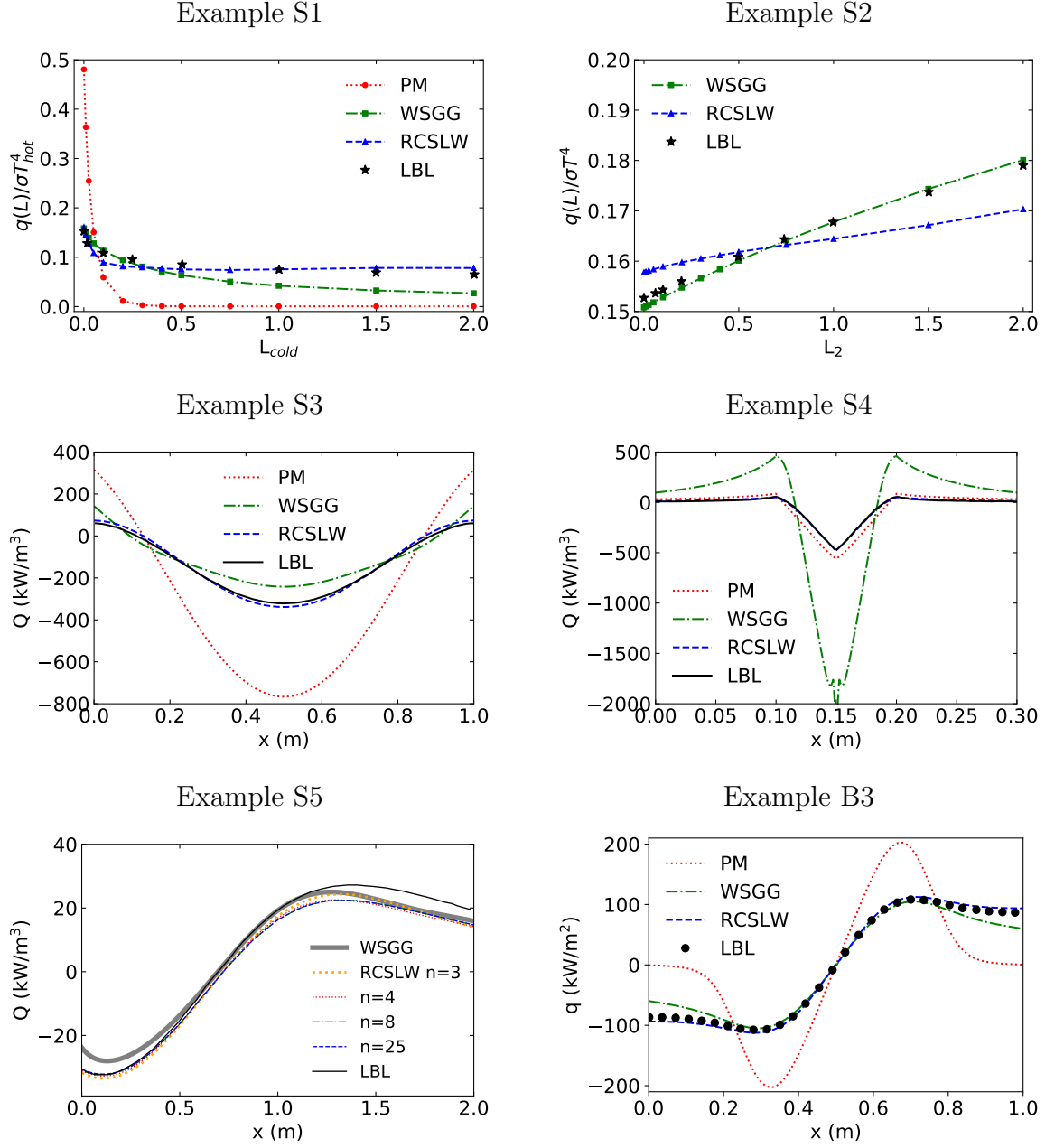


Figure 2: Results for examples summarized in Table 2.

256 require detailed radiation modeling must code and validate it themselves at
257 the expense of valuable research time and funding.

258 RadLib makes researchers' work easier by consolidating various approaches
259 into a modular library of interchangeable, prevalidated radiation models. Ad-
260 ditionally, RadLib's modular framework is designed to easily accommodate
261 new models as well, allowing researchers to compare new or existing mod-
262 els with very little overhead. Sometimes, it is not clear which radiation
263 model may be the best fit for a particular simulation. When simulations
264 are especially complex or computationally expensive, researchers may have
265 to extrapolate from theory and literature to choose an appropriate radiation
266 model rather than testing for their specific case. RadLib is designed to ease
267 both of these obstacles by facilitating comparison between radiation mod-
268 els through a common interface and providing a practical means of testing
269 various models without the restriction of prespecified geometry or case pa-
270 rameters. With RadLib, researchers can put more of their time and effort
271 into useful results rather than code or model development.

272 Currently, RadLib is only used within the authors' research group, where
273 it is applied to combustion CFD simulations using the One-Dimensional Tur-
274 bulence (ODT) model [20], but its design and structure as a C++ library
275 allows it to be incorporated easily into existing codes. It can be applied
276 to research questions in various other fields involving radiative heat transfer
277 as well, including energy engineering or atmospheric and climate sciences.
278 Radiation is a universal phenomenon, and RadLib can assist researchers in
279 many areas with systems and processes that involve heat transfer.

280 **6. Conclusions**

281 Set out the conclusion of this original software publication.

282 **7. Conflict of Interest**

283 We wish to confirm that there are no known conflicts of interest associated
284 with this publication and there has been no significant financial support for
285 this work that could have influenced its outcome.

286 **Acknowledgements**

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Current executable software version

Ancillary data table required for sub version of the executable software: (x.1, x.2 etc.) kindly replace examples in right column with the correct information about your executables, and leave the left column as it is.

Nr.	(Executable) software meta-data description	Please fill in this column
S1	Current software version	TODO 2.1
S2	Permanent link to executables of this version	TODO For example: https://github.com/combogenomics/DuctApe/releases/tag/DuctApe-0.16.4
S3	Legal Software License	MIT license (MIT)
S4	Computing platforms/Operating Systems	Linux, OS X, Microsoft Windows
S5	Installation requirements & dependencies	Python 3, Cython
S6	If available, link to user manual - if formally published include a reference to the publication in the reference list	TODO For example: http://mozart.github.io/documentation/
S7	Support email for questions	davidlignell@byu.edu

Table 3: Software metadata (optional)