

RadLib: a radiative heat transfer model library for CFD

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Abstract

Ca. 100 words

Keywords: radiative heat transfer, reacting flows, CFD

Required Metadata

Current code version

Ancillary data table required for subversion of the codebase. Kindly replace examples in right column with the correct information about your current code, and leave the left column as it is.

Nr.	Code metadata description	Please fill in this column
C1	Current code version	TODO 2.1
C2	Permanent link to code/repository used for this code version	<i>github.com/BYUignite/RadLib</i>
C3	Code Ocean compute capsule	N/A
C4	Legal Code License	MIT license (MIT)
C5	Code versioning system used	Git
C6	Software code languages, tools, and services used	C++, Python 3
C7	Compilation requirements, operating environments & dependencies	Python 3, Cython
C8	If available Link to developer documentation/manual	TODO
C9	Support email for questions	davidlignell@byu.edu

Table 1: Code metadata (mandatory)

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1. Motivation and significance

Modeling radiative heat transfer, and particular radiation absorption coefficients, for CFD is complex and challenging. More specifically, combustion simulations are often complicated by the need for accurate radiation modeling, which can be difficult to implement and computationally expensive relative to simulation cost. As a result, researchers typically manufacture configurations in which radiation can be safely ignored, which can lead to results inapplicable to practical systems, or use oversimplified models and assumptions, which can produce inaccurate results. Unfortunately, these approaches are neither rigorous nor applicable to real engineering systems.

In some cases, other modes of heat transfer dominate the system, and radiation can be safely neglected, but many practical engineering systems do not allow this. Simple jet flames, for example, demonstrate both possibilities: early in a flame’s development, convection typically dominates heat transfer and dictates flame behavior; late-stage flame phenomena like soot behavior and flame sheet breakthrough, however, increasingly depend on the magnitude of radiative heat losses and cannot be simulated accurately without a radiation model.

Like combustion, the core mechanisms of radiation are physically and mathematically complex. Unlike other modes of heat transfer, it is governed by a set of integro-differential equations that depend on both direction and wavelength. Only the simplest systems have analytic solutions, and most practical systems require a numerical solution. Ray tracing (Monte Carlo) solutions are very accurate but extremely computationally expensive, and often require high-performance computing resources to execute. Modeling assumptions are common and can reduce simulation cost at the expense of accuracy, depending on their validity for the system in question.

Currently, there is no convenient or easy-to-use access point for CFD radiation models. As such, we present RadLib, a modular library of radiation models that can be applied alongside various simulation tools. RadLib focuses on calculation of radiation absorption coefficients, often the most difficult and time-consuming portion of radiation calculations, which permits its use with various solvers. The models are fully implemented and validated and all use a common interface, allowing researchers easy and convenient access to radiation modeling tools regardless of the field of application.

2. Model descriptions

RadLib includes three models of varying complexity and accuracy to calculate the radiation absorption coefficients and their weighting factors for

each gas considered by the model. Radiation absorption coefficients are typically calculated using correlations relating them local properties such as temperature, total pressure, or species partial pressure, depending on the model. Correlations come from curve fits to high-resolution radiation property databases. At present, RadLib considers up to four gas species (H_2O , CO , CO_2 , and CH_4) and, optionally, soot volume fraction in its calculation of absorption coefficients and weighting factors.

Once the radiative absorption coefficients are calculated, they are then used to solve the radiative transfer equation (RTE), which depends on the simulation configuration and assumptions. Solving the RTE is not the focus of this software, but RadLib’s example cases do employ a simple implicit trapezoid method solver to calculate the radiative heat flux and volumetric heat source profiles between two parallel planes. [MORE DESCRIPTION OF SOLVER GOES HERE?]

[OTHER THINGS THAT APPLY TO ALL MODELS GO HERE]
[MAYBE INCLUDE SOME BASIC INFO ON LBL?]

2.1. Planck Mean absorption coefficients

RadLib’s simplest model uses Planck Mean absorption coefficients calculated from the correlations given on the TNF Workshop site [1]. The temperature-dependent correlations are based on the RADCAL model in [2]. The TNF radiation model is also documented in [3].

Planck Mean absorption coefficients are commonly used to model radiation, especially in combustion systems, because the model is relatively easy to implement, computationally inexpensive, and reasonably accurate in many cases. The TNF Workshop correlations were developed for use with an optically thin radiation model, which assumes that radiation passes through a medium mostly undisturbed. In cases where the optically thin assumption applies, such as simple hydrogen jet flames, this model and the associated Planck Mean absorption coefficients can produce accurate results [4]. In cases where the optically thin assumption is not reasonable, including many other combustion scenarios, this model does not produce accurate results. For example, it significantly overpredicts radiative losses from the TNF library’s CH_4 flames [5, 6, 7].

Because RadLib does not specify case geometry or medium, there is no optically thin assumption inherent in its use of the Planck Mean absorption coefficients. However, the correlations were developed with the intention of use with an optically thin assumption, and, as a result, depend only on local temperature values. RadLib users must take care to consider these limitations before using this model.

78 2.2. Weighted sum of gray gases (WSGG)

79 The basic assumption of weighted sum of gray gases (WSGG) models
80 in general is that the non-gray behavior of gas mixtures, in this case H₂O
81 and CO₂, can be modeled by a weighted sum of several gray gases and one
82 transparent gas (which represents the spectral windows between absorption
83 bands). RadLib uses the WSGG model presented by Bordbar et al. [8, 9],
84 which uses correlations based on the HITEMP 2010 database [10]. RadLib,
85 in accordance with the Bordbar et al. WSGG method cited above, uses a
86 mixture of four gray gases and one transparent gas. Absorption coefficients
87 are calculated by

$$K_i = \sum_{k=0}^4 d_{i,k} M_r^k, \quad (1)$$

88 where K_i is the absorption coefficient for species i , $d_{i,k}$ is a species-specific
89 correlated model coefficient, and M_r is the molar ratio $Y_{\text{H}_2\text{O}}/Y_{\text{CO}_2}$. The
90 weight factors are calculated by

$$a_i = \sum_{j=0}^4 b_{i,j} T_r^j, \quad (2)$$

91 where a_i is the weighting factor for species i and T_r is a normalized tem-
92 perature equal to T/T_{ref} with $T_{ref} = 1200\text{K}$. The value of $b_{i,j}$ is calculated
93 by

$$b_{i,j} = \sum_{k=0}^4 C_{i,j} M_r^k, \quad (3)$$

94 where $C_{i,j}$ is another correlated model coefficient and M_r is the molar ratio
95 $Y_{\text{H}_2\text{O}}/Y_{\text{CO}_2}$ as above. The model coefficients $d_{i,k}$ and $C_{i,j}$ can be found in
96 the literature [8, 9]. RadLib uses the updated model coefficients from [9],
97 which extends the model presented in [8] to include all possible values of the
98 H₂O-CO₂ molar ratio.

99 2.3. Rank Correlated SLW (RCSLW)

100 The Spectral Line Weighted-sum-of-gray gases (SLW) model represents
101 a family of global approaches to radiative heat transfer in high-temperature
102 gases that also includes Absorption Distribution Function (ADF) and Full
103 Spectrum k -distribution (FSK) models, all of which are based on the same
104 fundamental principle in modeling the gas absorption spectrum [11]. In order
105 to extend their spectral models from uniform conditions (isothermal, homo-
106 geneous gases) to nonuniform conditions (non-isothermal, non-homogeneous
107 gases), these models take a reference approach in which local gas states are

corrected relative to a reference state. Reference approaches, however, generally lack consistent reference states and can yield significant errors in cases with large spatial temperature gradients [12]. The Rank Correlated SLW (RCSLW) model is a unique extension of the generalized SLW model that does not require a specified gas reference state and preserves the emission term of the spectrally integrated RTE. Recent comparison of advanced SLW modeling approaches revealed that "the Rank Correlated SLW model is the most robust of all models, and demonstrates that it can achieve accurate solutions with as few as 3–5 gray gases" [13]. A brief overview of the general SLW and RCSLW models will be given here; detailed discussion can be found in the literature [14, 15, 16, 17, 18, 11, 12, 19].

The radiative transfer equation (RTE) for an absorbing, emitting, and non-scattering medium along a given path length s in a direction $\hat{\Omega}$ is given by

$$\frac{dI_\eta}{ds} = -\kappa_\eta I_\eta + \kappa_\eta I_{b\eta}, \quad (4)$$

where I_η is the radiative spectral intensity, $I_{b\eta}$ is the Planck spectral distribution of blackbody intensity, and κ_η is the spectral absorption coefficient of the medium. Integrating with respect to wavenumber and subdividing the absorption cross-section into gray gases gives the SLW form of the RTE:

$$\frac{dI_j}{ds} = -\kappa_j I_j + a_j \kappa_j I_b, \quad j = 0, 1, \dots, n. \quad (5)$$

Here, n is the number of gray gases in the model and I_j is the intensity of gray gas j . κ_j is the gray gas absorption coefficient, which can be calculated as $\kappa_j = N\sqrt{C_{j-1}C_j}$, where C_{j-1} and C_j are supplemental absorption cross-sections used to discretize the absorption spectrum [15]. The gray gas weights corresponding to each absorption coefficient are given by $a_j = F(C_j) - F(C_{j-1})$, where $F(C_j)$ is the absorption line blackbody distribution function (ALBDF) for species j , calculated from the detailed absorption spectrum of that species. The absorption cross-sections are chosen with respect to a thermodynamic reference state, which makes generalized SLW methods reference approaches. Once Equation 5 is solved for each gray gas species, to total radiative intensity I can be calculated by summing the gray gas intensities:

$$I = \int_{\eta=0}^{\infty} I_\eta d\eta = \sum_{j=1}^n I_j. \quad (6)$$

The Rank-Correlated SLW (RCSLW) model avoids specifying a reference state by relating thermodynamic states to one another instead. If two arbitrary absorption cross-sections define identical wavenumber intervals, the

141 two cross-sections (neither of which is designated a reference cross-section)
 142 can be said to be rank-correlated. The inverse ALBDF, defined such that
 143 $C[F(C, \phi_g, T_b), \phi_g, T_b] = C$ and $F[C(F, \phi_g, T_b), \phi_g, T_b] = F$ for a given gas
 144 thermodynamic state ϕ_g and blackbody temperature T_b , is proven to have
 145 this property and can also be called the rank-correlated reordered absorption
 146 cross-sections [12]. As a result, the inverse ALBDF can be used to construct
 147 cross-section intervals for the RCSLW model that do not rely on a defined
 148 reference state or spectrum. RadLib's RCSLW model uses Method 1.2.2 as
 149 defined and recommended in [12]

150 3. Software Description

151 RadLib is an object-oriented C++ class library that includes both C++
 152 and Python interfaces. The RadLib package contains five subdirectories
 153 (upon initial download): **source** contains the RadLib source code; **build**
 154 contains installation files; **examples** contains instructive example cases, in-
 155 cluding a simple interface and solver for a parallel planes geometry; **data**
 156 contains ALBDF data tables required for the RCSLW model; and **docs** con-
 157 tains files used to generate code documentation with Doxygen (optional).

158 The **source** and **examples** directories are further divided into C++ and
 159 Python subdirectories to differentiate between interfaces. There are three
 160 interface options for using this code: C++, Python, and Cython-wrapped
 161 Python. C++ interfaces are located within the **examples/c++** folder, while
 162 Python interfaces are located within the **examples/python** folder. When
 163 running examples with Python, the Cython-wrapped version is the default;
 164 to run the regular Python version without the Cython wrapper, edit the com-
 165 ments near the top of the example files (i.e **ex.S1.py**). The C++ interface
 166 produces the fastest-running code, followed by the Cython-wrapped Python
 167 interface and then the regular Python interface. [INSERT RUNTIME COM-
 168 PARISONS HERE]

169 RadLib installation is automated with CMake. First, navigate to the
 170 **radlib/build** directory. If the user requires an installation location other
 171 than the default **radlib/installed** directory, edit the **user_config** file be-
 172 fore running CMake. To compile the package, run the command **cmake -C**
 173 **user_config ../source**. Upon successful completion, run **make** and then
 174 **make install** to complete the process. The generated C++ library file is
 175 located at **radlib/installed/lib/libradlib.a**.

176 Figure 1 illustrates the basic structure use of the RadLib package within
 177 a generic example using the provided interfaces. The RadLib library gen-
 178 erates absorption coefficients and their weighting factors for use within the
 179 appropriate RTE, but does not specify any particular geometry, making it

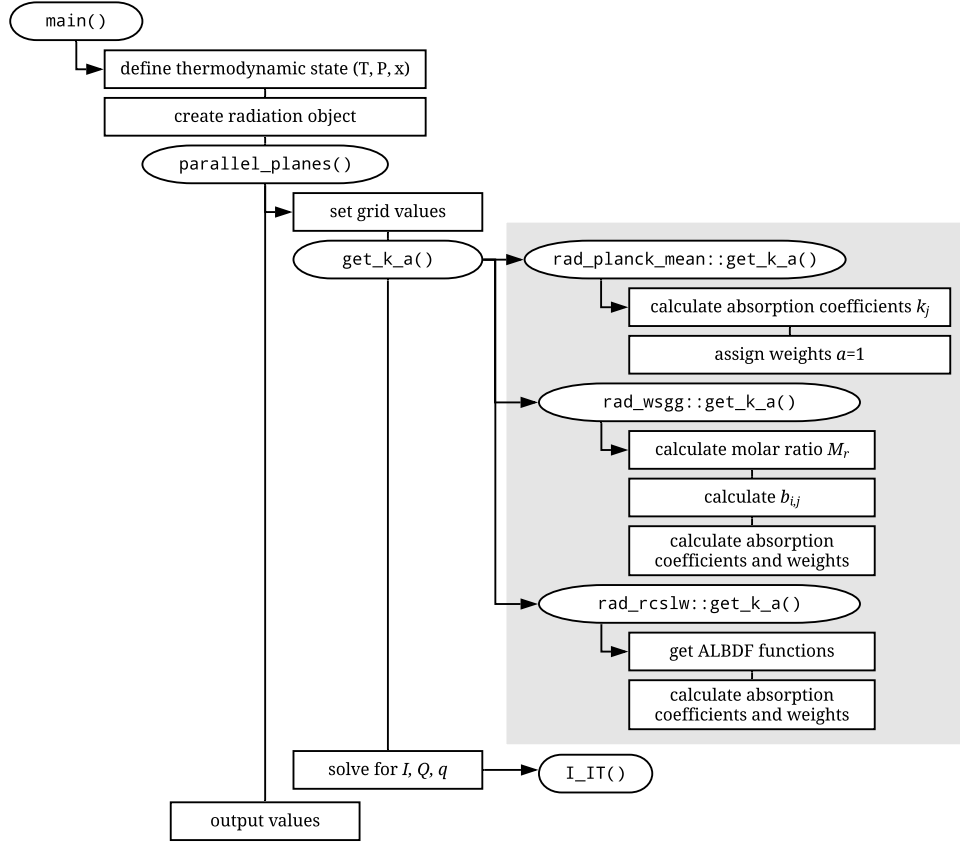


Figure 1: Example workflow diagram. Highlighted areas are part of the RadLib library; other areas represent example infrastructure for using the package.

180 a versatile tool for any simulation that requires radiative heat transfer, re-
 181 gardless of configuration. The interfaces, solver, and examples included with
 182 the library serve to illustrate its use and validate the implementation and
 183 results.

184 4. Illustrative Examples

185 Several examples are presented to illustrate the behavior of the models.
 186 The examples show heat flux q or volumetric heat source Q in one one-
 187 dimensional configurations with varying gas compositions and temperatures.
 188 We compare the PM, WSGG, and RCSSLW models for each example. The
 189 examples correspond to those presented by Solvojev et al. (S) [12] and Bor-
 190 dbar et al. (B) [9], and the number of each example corresponds to the

Example	T(K)	y_{H_2O} y_{CO_2} (mole frac.)	L (m)	T_{walls} (K)
S1	$T(x < 0.5) = 2000; T(x > 0.5) = 300$	$y_{CO_2} = 0.1, y_{H_2O} = 0.2$	0.5-2.5	cold, cold
S2	$T=1000$	$y_{CO_2}(x < 0.5) = 0.4, y_{CO_2}(x > 0.5) = 0.1$ $y_{H_2O} = 0.0$	0.5-2.5	cold, cold
S3	$T(x) = 4000x(L-x)/L^2 + 800$	$y_{H_2O}(x) = 0.8x(L-x)/L^2 + 0.12$ $y_{CO_2} = 0$	1	800, 800
S4	middle third triangular to 2500	$y_{H_2O} = 0.1, y_{CO_2} = 0$	0.3	500, 500
S5	$T(x) = 1000 + 500 \cos(\pi x/L)$	$y_{H_2O} = 0.1, y_{CO_2} = 0$	2	1500, 500
B3	$T(x) = 400 + 1400 \sin(\pi x/L)^2$	$y_{H_2O}(x) = 0.0001 + 0.9999 \sin(\pi x/L)^2$ $y_{CO_2} = 1 - y_{H_2O}$	1	400, 400

Table 2: Summary of example cases presented. S1-S5 are from [12]; B3 is from [9]. All cases use $P = 1$ atm and black walls.

example number in the respective reference. A ray-tracing code is used to solve the radiative transport equation between two parallel plates. Table 2 summarizes the cases. Example S1 is a hot slab next to a cold slab where the cold slab’s thickness varies; Example S2 is isothermal with a thick slab of high CO_2 next to a thin slab of low CO_2 with variable thickness; Example S3 uses parabolic temperature and H_2O mole fraction profiles; Example S4 has a triangular temperature profile between equally-spaced isothermal regions; Example S5 uses a half-sinusoid temperature profile that decreases from 1500 to 500 K; and Example B3 has symmetric temperature and H_2O mole fraction profiles with central peaks of 1800 K and 1, respectively (with $y_{CO_2} = 1 - y_{H_2O}$). Each case is presented alongside the line-by-line (LBL) data presented in the references.

The examples are provided with the RadLib code and implemented in both C++ and Python. A Jupyter notebook is provided with the Python examples that runs the examples, displays the plots, and saves the plots to PDF files. Python and Cython versions of the one-dimensional solver `parallel_planes.py` are provided for convenience.

These cases are intended to illustrate the use of the RadLib library and are not exhaustive. Details about these examples and their motivations can be found in their respective references. While omitted here for brevity, the implemented WSGG and RCLW models give essentially identical results to those presented in [12, 9] such that these examples also serve as a validation of the implementation of the models.

Figure 2 shows comparative results for the different radiation models for these cases. In general, the PM model performs poorly compared to the WSSGG and RCLW models. A notable exception is Example S4. In Example S2, the PM $q(L)/\sigma T^4$ is off scale at an essentially constant at a value of unity. The PM absorption coefficient is $27.4 \text{ atm}^{-1}\text{m}^{-1}$, giving optical thicknesses of 0.09 and 0.36 m in the thick and thin layers, respectively, which are relatively small compared to the isothermal domain size greater than 0.5

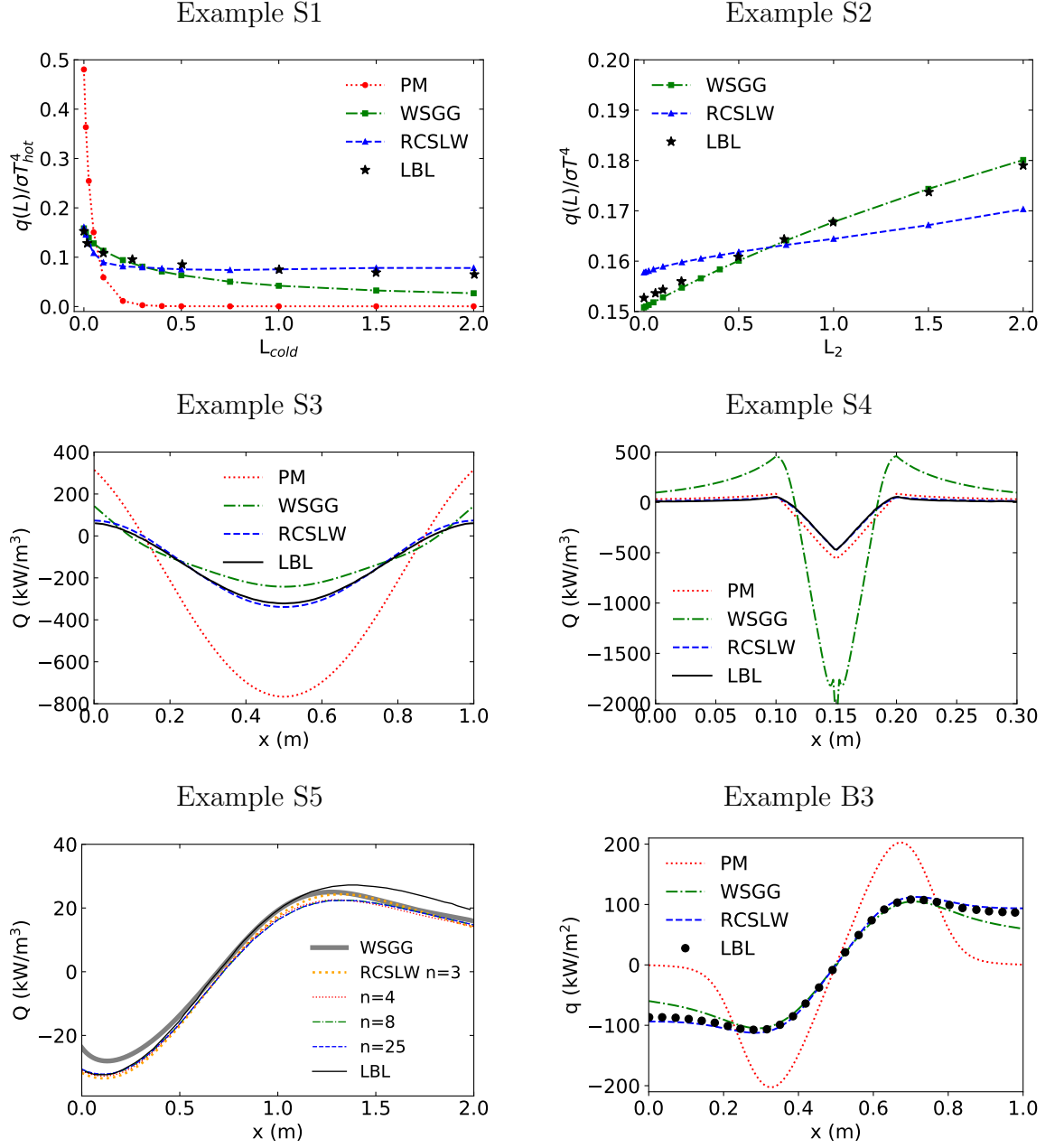


Figure 2: Results for examples summarized in Table 2.

221 m. Example S5 omits the PM model to more clearly show the behavior of
 222 the WSGG and RCSLW models. For that example, the PM values follow the
 223 shape of the other curves but Q varies from around -80 at $x = 0$ to a peak of
 224 200 at $x=1.5$ m, and dropping to 100 kW/m³ at $x = 2$ m. In all examples,
 225 four gray ($n = 4$) and one clear gas are computed for the RCSLW models
 226 to give a consistent comparison to the WSGG model. Example S5 shows
 227 the sensitivity of the RCSLW model to the number of gases used. When
 228 n is increased to eight the RCSLW model improves to show nearly perfect
 229 agreement with the LBL data in Example S2. In all Examples, the RCSLW
 230 model is initialized using the mean temperature and composition on the
 231 domain. In Example S5, the RCSLW model converges to the LBL solution
 232 when the model is initialized using the maximum temperature instead of the
 233 average temperature.

234 5. Impact

235 As far as I'm aware, there isn't an easy way to incorporate radiative heat
 236 transfer into a CFD simulation. Most cases use optically thin assumption
 237 (which works in some cases, but not in others) or neglect radiation entirely
 238 (also applicable sometimes, but not always). [Refer to TNF website radia-
 239 tion page here.] Unfortunately, this means that when you simulation some
 240 configuration in which radiation might be important to the overall heat trans-
 241 fer, you won't get accurate simulation results. Furthermore, if your study is
 242 about something else entirely, your radiation model (or lack thereof) becomes
 243 a source of error that may be very difficult to separate from other sources of
 244 error in your simulation study (i.e. soot modeling studies). As of right now,
 245 if you want any detailed radiation treatment, you have to code it yourself,
 246 which is difficult and requires external validation.

247 RadLib can make researchers' lives easier by providing a library of preval-
 248 idated radiation models that can be switched out with no difficulty. Addi-
 249 tional models can be added easily using the provided modular framework.
 250 Researchers can even use Radlib as a tool for comparing models. No need
 251 to code multiple different complex radiation models yourself just to decide
 252 which one works best for your simulation. And no need to puzzle through
 253 the literature to figure out which model(s) might be best for your simula-
 254 tion, either; instead, you can test them yourself. It saves tons of time and
 255 effort that researchers can now put toward results rather than code or model
 256 development.

257 By putting all these models side by side in a modular framework, RadLib
 258 also provides a structure on which new or altered radiation models can be
 259 tested against existing ones. Maybe more comparative studies can be done,

260 especially for more complex simulation cases. We plan to add radiation
261 models as appropriate to RadLib, too.

262 RadLib opens up new horizons for CFD simulations, especially in combus-
263 tion cases. It is designed such that it can be easily incorporated into existing
264 research codes. Our group plans to use it with ODT [CITE OTHER SOFT-
265 WAREX PAPER HERE?] alongside soot model library (in development) to
266 study late-flame phenomena such as soot oxidation, flame extinction, and
267 soot-flame breakthrough. These topics in particular are difficult because
268 they require accurate simulation data over a relatively long computational
269 time in addition to good models for both soot chemistry (which is an active
270 research area) and radiation heat transfer (which is the difficult part that
271 RadLib can solve). Using RadLib for such studies allows us to separate and
272 quantify sources of error that may occur due to various models, which is
273 super difficult if you only have one model to work with or it hasn't been
274 validated well.

275 RadLib can also be used outside of combustion CFD research for anything
276 involving radiative heat transfer. Potential research areas that could benefit
277 include atmospheric and climate sciences, interstellar phenomena, improving
278 efficiency of energy-producing processes, safety in chemical plant design, etc.
279 We aren't experts in these areas, but radiative heat transfer is a universal
280 phenomena that applies to any system or process that involves heat transfer.

281 This software has not been used outside of the current research group,
282 and it is not used in any commercial settings at this time.

283 6. Conclusions

284 Set out the conclusion of this original software publication.

285 7. Conflict of Interest

286 We wish to confirm that there are no known conflicts of interest associated
287 with this publication and there has been no significant financial support for
288 this work that could have influenced its outcome.

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References

- [1] N. Smith, J. Gore, J. Kim, Q. Tang, Tnf workshop radiation models (2003).
URL <https://tnfworkshop.org/radiation/>
- [2] W. L. Grosshandler, Radcal: A narrow-band model for radiation calculations in a combustion environment: Nist technical note 1402.
- [3] R. S. Barlow, A. N. Karpetis, J. H. Frank, J.-Y. Chen, Scalar profiles and no formation in laminar opposed-flow partially premixed methane/air flames, *Combustion and Flame* 127 (3) (2001) 2102–2118. doi:10.1016/S0010-2180(01)00313-3.
- [4] R. Barlow, N. Smith, J. Chen, R. Bilger, Nitric oxide formation in dilute hydrogen jet flames: isolation of the effects of radiation and turbulence-chemistry submodels, *Combustion and Flame* 117 (1-2) (1999) 4–31. doi:10.1016/S0010-2180(98)00071-6.
URL <http://www.sciencedirect.com/science/article/pii/S0010218098000716>
- [5] J. H. Frank, R. S. Barlow, C. Lundquist, Radiation and nitric oxide formation in turbulent non-premixed jet flames, *Proceedings of the Combustion Institute* 28 (1) (2000) 447–454. doi:10.1016/S0082-0784(00)80242-8.
- [6] X. Zhu, J. Gore, A. N. Karpetis, R. S. Barlow, The effects of self-absorption of radiation on an opposed flow partially premixed flame, *Combustion and Flame* 129 (3) (2002) 342–345. doi:10.1016/S0010-2180(02)00341-3.
URL <http://www.sciencedirect.com/science/article/pii/S0010218002003413>
- [7] P. J. Coelho, O. J. Teerling, D. Roekaerts, Spectral radiative effects and turbulence-radiation-interaction in sandia flame d, in: Barlow, Robert S., Pope, Stephan B., Masri, Assaad R., Oefelein, Joseph C. (Ed.), *The Proceedings of the Sixth International Workshop on Measurement and Computation of Turbulent Nonpremixed Flames*, 2002.
- [8] M. H. Bordbar, G. Wecl, T. Hyppanen, A line by line based weighted sum of gray gases model for inhomogeneous co₂–h₂o mixture in oxy-fired combustion, *Combustion and Flame* 161 (9) (2014) 2435–2445. doi:10.1016/j.combustflame.2014.03.013.

- [9] H. Bordbar, G. C. Fraga, S. Hostikka, An extended weighted-sum-of-gray-gases model to account for all $\text{CO}_2 - \text{H}_2\text{O}$ molar fraction ratios in thermal radiation, *International Communications in Heat and Mass Transfer* 110 (2020) 104400. doi:10.1016/j.icheatmasstransfer.2019.104400. URL <http://www.sciencedirect.com/science/article/pii/S0735193319302660>
- [10] L. S. Rothman, I. E. Gordon, R. J. Barber, H. Dothe, R. R. Gamache, A. Goldman, V. I. Perevalov, S. A. Tashkun, J. Tennyson, Hitemp, the high-temperature molecular spectroscopic database, *Journal of Quantitative Spectroscopy & Radiative Transfer* 111 (15) (2010) 2139–2150. doi:10.1016/j.jqsrt.2010.05.001. URL <http://www.sciencedirect.com/science/article/pii/S002240731000169X>
- [11] V. P. Solovjov, F. André, D. Lemonnier, B. W. Webb, The generalized slw model, *Journal of Physics: Conference Series* 676 (2016) 1–36.
- [12] V. P. Solovjov, F. André, D. Lemonnier, B. W. Webb, The rank correlated slw model of gas radiation in non-uniform media, *Journal of Quantitative Spectroscopy & Radiative Transfer* 197 (2017) 26–44. doi:10.1016/j.jqsrt.2017.01.034.
- [13] J. Badger, B. W. Webb, V. P. Solovjov, An exploration of advanced slw modeling approaches in comprehensive combustion predictions, *Combustion Science and Technology* 012022 (676) (2019) 1–17. doi:10.1080/00102202.2019.1678907.
- [14] V. P. Solovjov, B. W. Webb, Slw modeling of radiative transfer in multicomponent gas mixtures, *Journal of Quantitative Spectroscopy and Radiative Transfer* 65 (2000) 655–672.
- [15] V. P. Solovjov, B. W. Webb, An efficient method for modeling radiative transfer in multicomponent gas mixtures with soot, *Transactions of the ASME* 123 (2001) 450–457.
- [16] V. P. Solovjov, B. W. Webb, Multilayer modeling of radiative transfer by slw and cw methods in non-isothermal gaseous medium, *Journal of Quantitative Spectroscopy and Radiative Transfer* 109 (2) (2008) 245–257. doi:10.1016/j.jqsrt.2007.08.015.
- [17] V. P. Solovjov, D. Lemonnier, B. W. Webb, The slw-1 model for efficient prediction of radiative transfer in high temperature gases, *Journal of Quantitative Spectroscopy and Radiative Transfer* 112 (7) (2011) 1205–1212. doi:10.1016/j.jqsrt.2010.08.009.

- [18] V. P. Solovjov, D. Lemonnier, B. W. Webb, Extension of the exact slw model to non-isothermal gaseous media, *Journal of Quantitative Spectroscopy and Radiative Transfer* 143 (2014) 83–91. doi:10.1016/j.jqsrt.2013.10.008.
- [19] B. W. Webb, V. P. Solovjov, F. André, An exploration of the influence of spectral model parameters on the accuracy of the rank correlated slw model, *Journal of Quantitative Spectroscopy and Radiative Transfer* 218 (2018) 161–170. doi:10.1016/j.jqsrt.2018.06.023.

Current executable software version

Ancillary data table required for sub version of the executable software: (x.1, x.2 etc.) kindly replace examples in right column with the correct information about your executables, and leave the left column as it is.

Nr.	(Executable) software meta-data description	Please fill in this column
S1	Current software version	TODO 2.1
S2	Permanent link to executables of this version	TODO For example: https://github.com/combogenomics/DuctApe/releases/tag/DuctApe-0.16.4
S3	Legal Software License	MIT license (MIT)
S4	Computing platforms/Operating Systems	Linux, OS X, Microsoft Windows
S5	Installation requirements & dependencies	Python 3, Cython
S6	If available, link to user manual - if formally published include a reference to the publication in the reference list	TODO For example: http://mozart.github.io/documentation/
S7	Support email for questions	davidlignell@byu.edu

Table 3: Software metadata (optional)